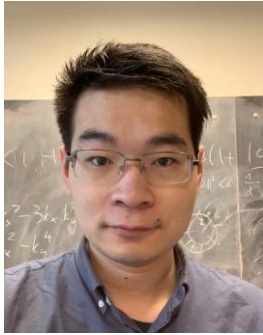


# Topological Mott Insulator in Semiconductor Moire Heterostructure

Liang Fu

SIMONS  
FOUNDATION





Yang Zhang



Trithep Devakul

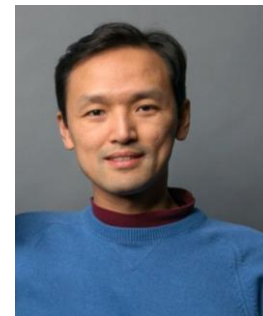


Margarita Davydova

Cornell:



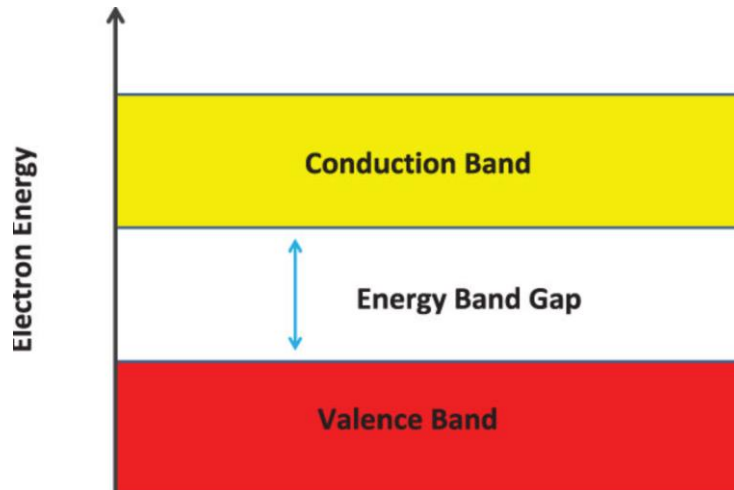
Jie Shan



Kin Fai Mak

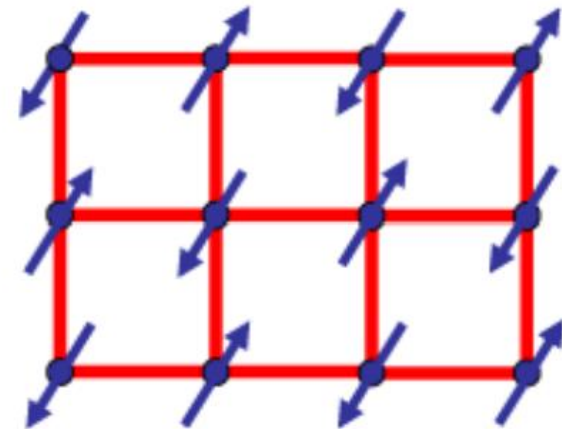
# Two Types of Insulators

## Band insulators



- even integer fillings
- energy gap due to Pauli exclusion

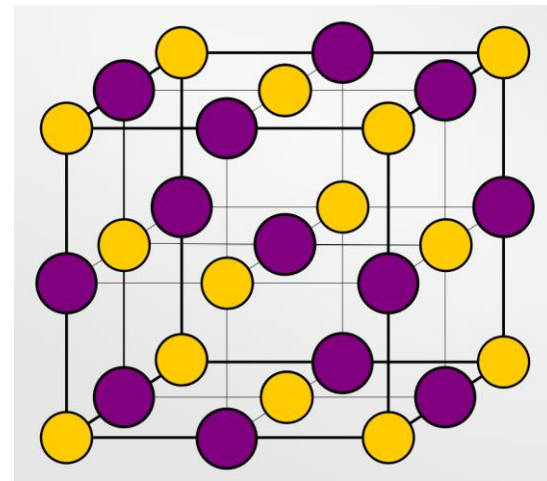
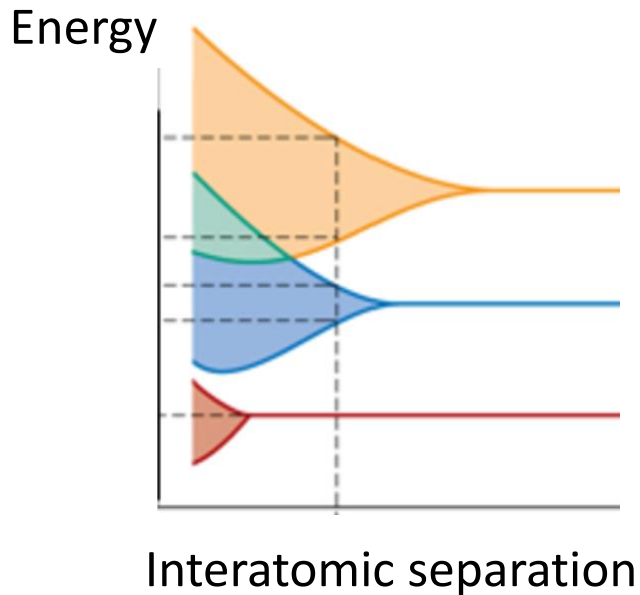
## Mott insulators



- odd integer fillings
- interaction induced gap

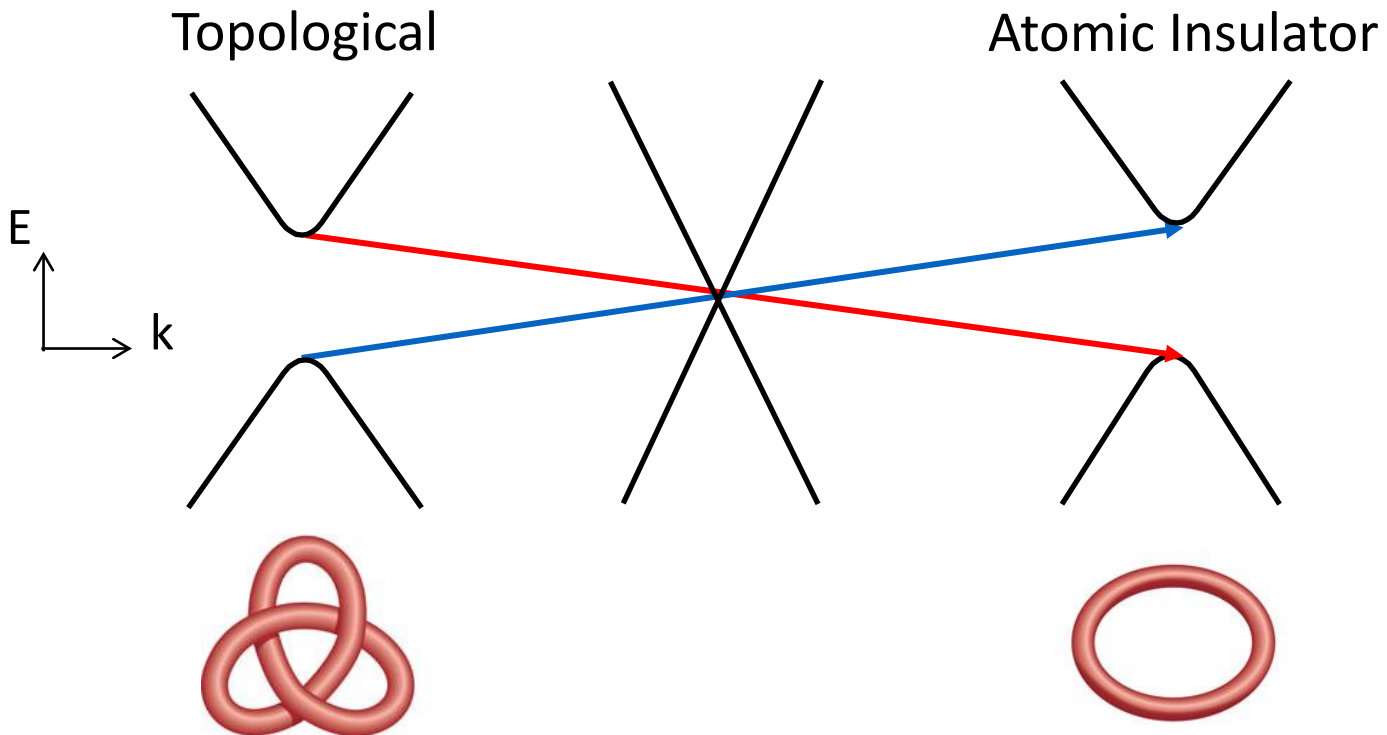
# Normal Band Insulators

- energy gap remains finite as the crystal is taken apart
- topologically equivalent to atomic limit

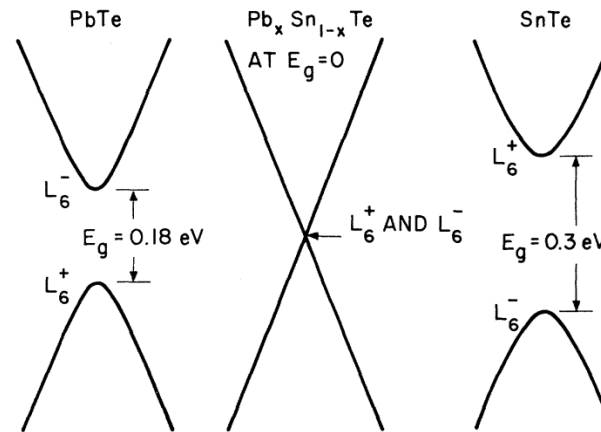
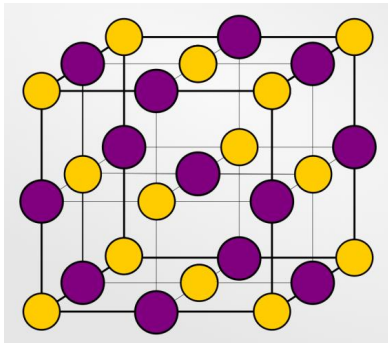


# Topological Insulators

- cannot be taken apart smoothly
- rely on the wave nature of electron

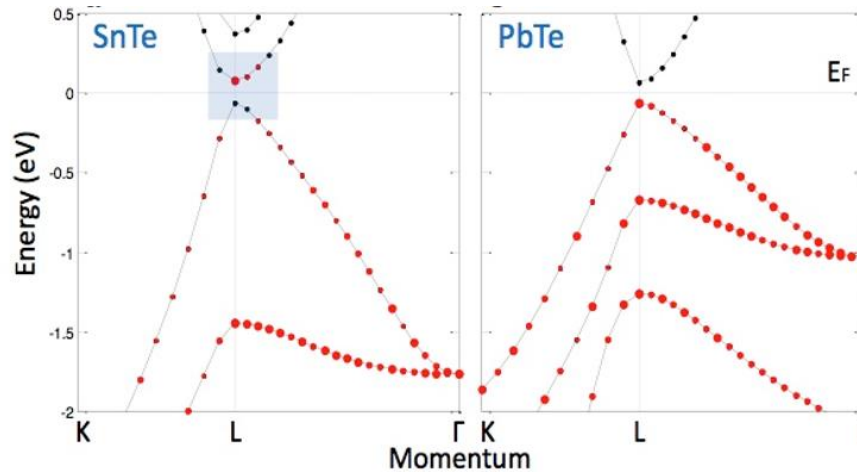


# Atomic versus Topological Insulators



Dimmock et al  
(1966)

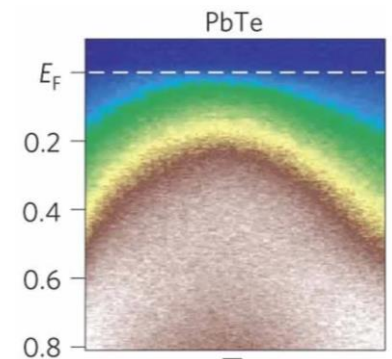
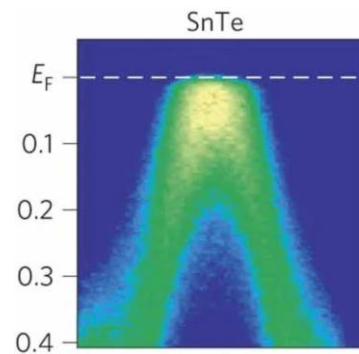
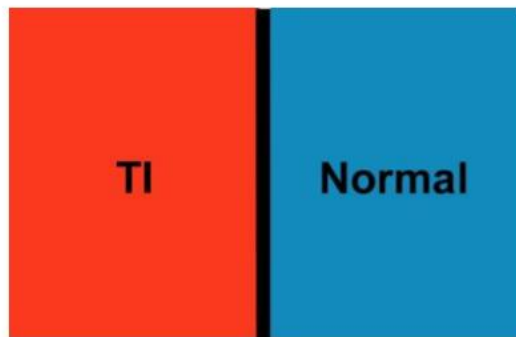
- $\text{PbTe} = \text{Pb}^{2+} \& \text{Te}^{2-}$
- $\text{SnTe} \neq \text{Sn}^{2+} \& \text{Te}^{2-}$



Hsieh et al  
(2012)

# Continuous Phase Transition between normal and topological band insulators

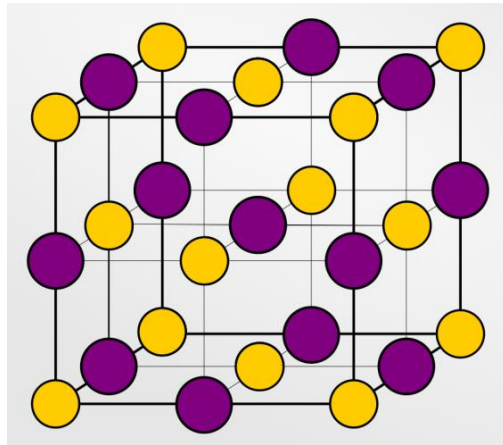
Dirac field theory:  $H = -i \nabla \cdot \Gamma + m\Gamma_0$



Ando et al (2012)

- change of topology = sign change of Dirac mass
- boundary (= domain wall) hosts massless Weyl fermion
- interaction is irrelevant at critical point

# Mott Insulators



- electrons bound to individual atoms
- electron motion prohibited by local repulsion  $Un_{i\uparrow}n_{i\downarrow}$

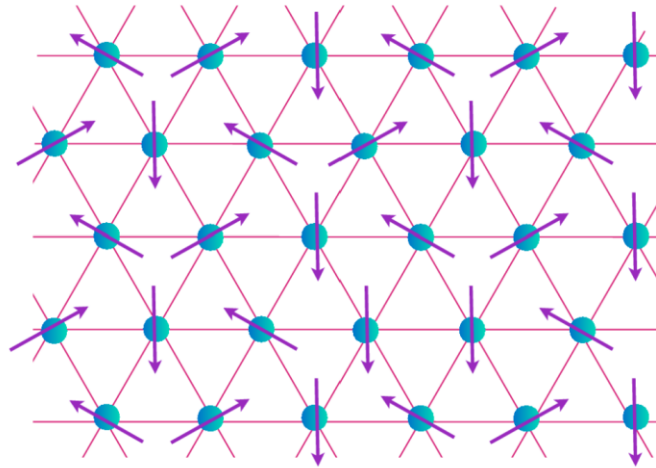


Mott

Topology



# Part 1: Inverting Mott Insulators



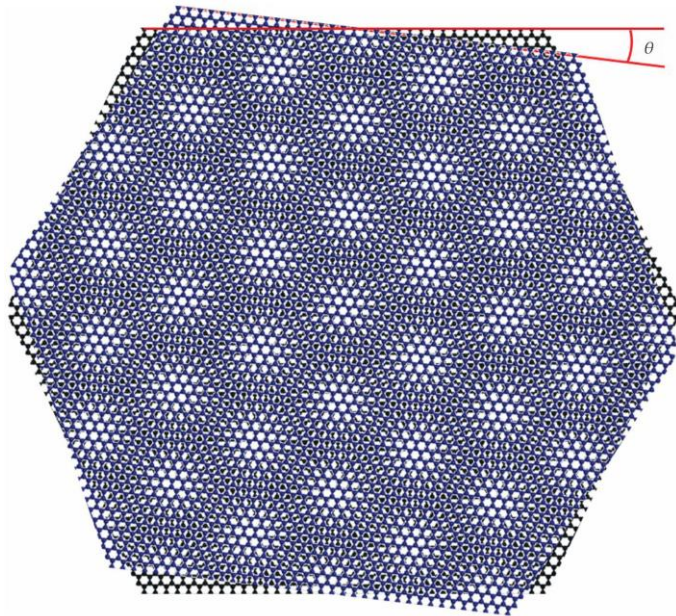
Continuous phase transition from  $120^\circ$  AFM Mott insulator to Chern insulator with spin chirality

Zhang, Devakul & LF, PNAS (2021)

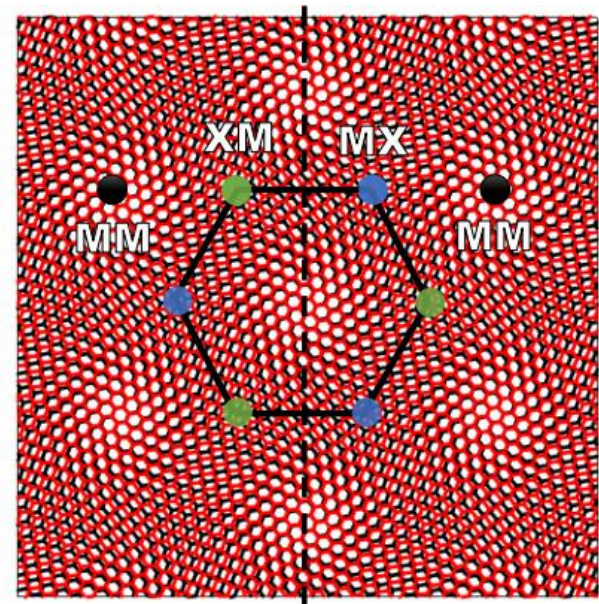
Devakul & LF, PRX (2022)

# Moire Superlattices

Twisted bilayer graphene

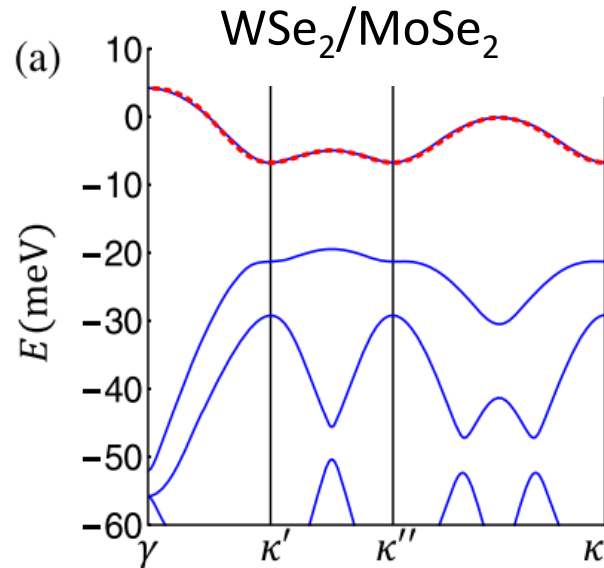
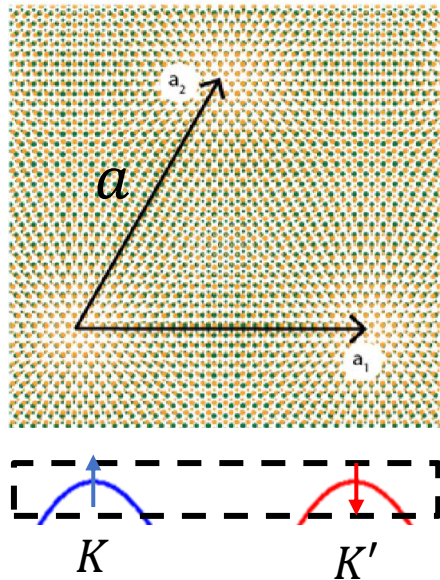


Semiconductor heterostructure



# Hubbard Model Physics in Transition Metal Dichalcogenide Moiré Bands

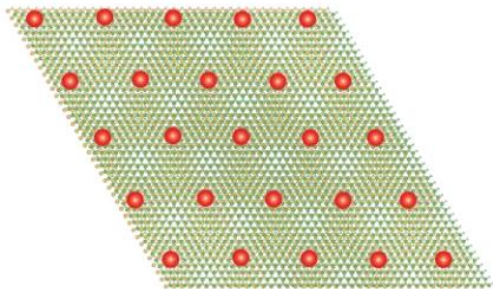
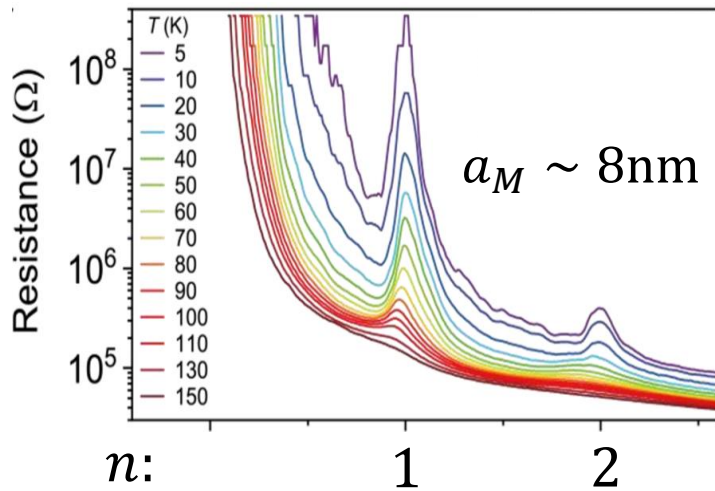
Fengcheng Wu,<sup>1</sup> Timothy Lovorn,<sup>2</sup> Emanuel Tutuc,<sup>3</sup> and A. H. MacDonald<sup>2</sup>



$$H = \frac{\mathbf{p}^2}{2m} + V(\mathbf{r}) \quad V(\mathbf{r}) : \text{superlattice potential}$$

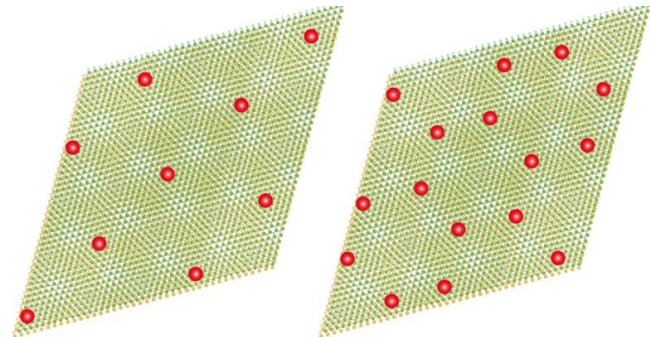
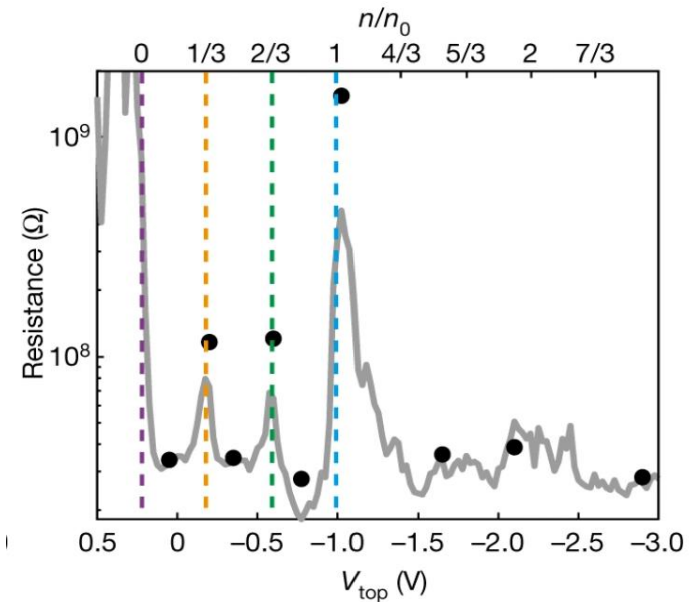
Tight-binding regime at large moire period:  $\hbar^2/ma^2 \ll V$   
 $\Rightarrow$  triangular lattice of “quantum dots” & Hubbard model

## Simulation of Hubbard model physics in WSe<sub>2</sub>/WS<sub>2</sub> moiré superlattices



Mott insulator at  $n = 1$  (half band filling)

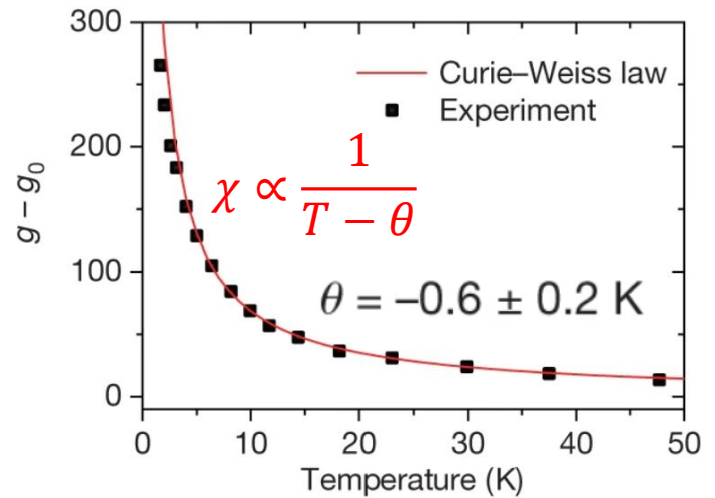
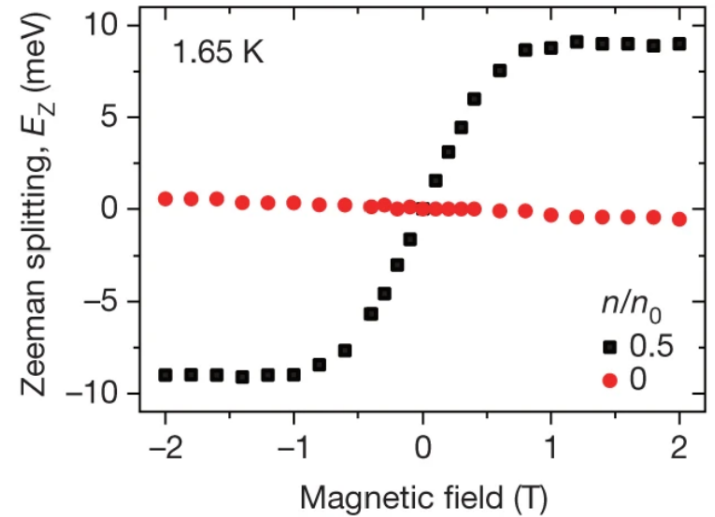
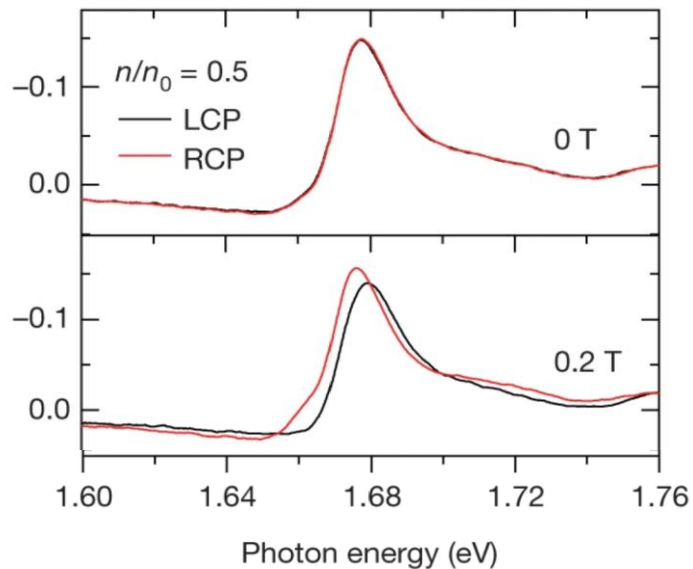
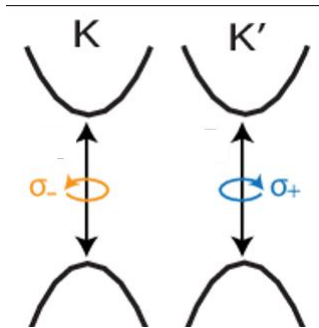
## Mott and generalized Wigner crystal states in WSe<sub>2</sub>/WS<sub>2</sub> moiré superlattices



Wigner crystals at  $n = \frac{1}{3}, \frac{2}{3}, \dots$

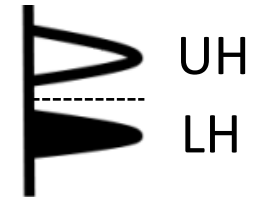
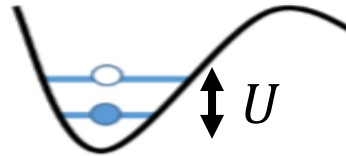
WC & MIT: [Chenhao Jin](#), [Cenke Xu](#), [Senthil](#), [Kim](#), [Das Sarma](#), [Philips](#), [MacDonald](#) ...

# Local Moment and AFM Interaction



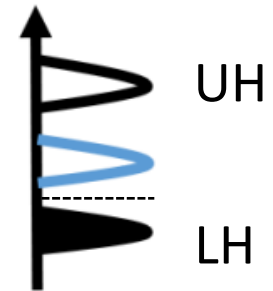
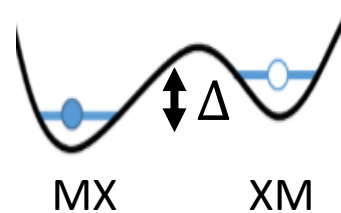
# Charge-Transfer Mott Insulator

Mott-Hubbard insulator




$U > \Delta$ :  
Charge transfer insulator

(similar to  $\text{CuO}_2$ )



- moire potential may have two minima in a unit cell
- doped charges at  $n > 1$  occupy secondary minima to avoid  $U$ .
- insulating gap at  $n = 1$  set by  $\Delta$


## **Moiré quantum chemistry: Charge transfer in transition metal dichalcogenide superlattices**

Yang Zhang <sup>\*</sup>, Noah F. Q. Yuan,<sup>\*</sup> and Liang Fu

## **Charge transfer excitations, pair density waves, and superconductivity in moiré materials**

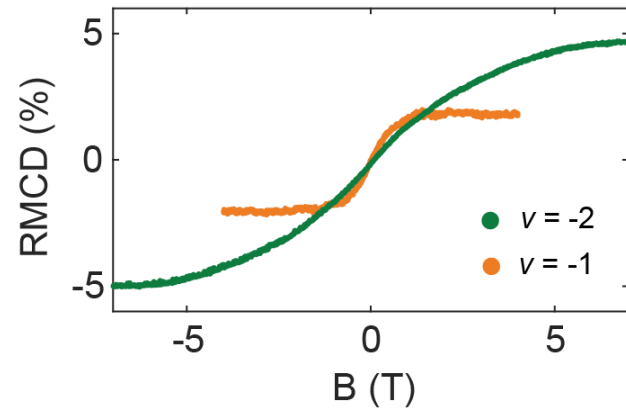
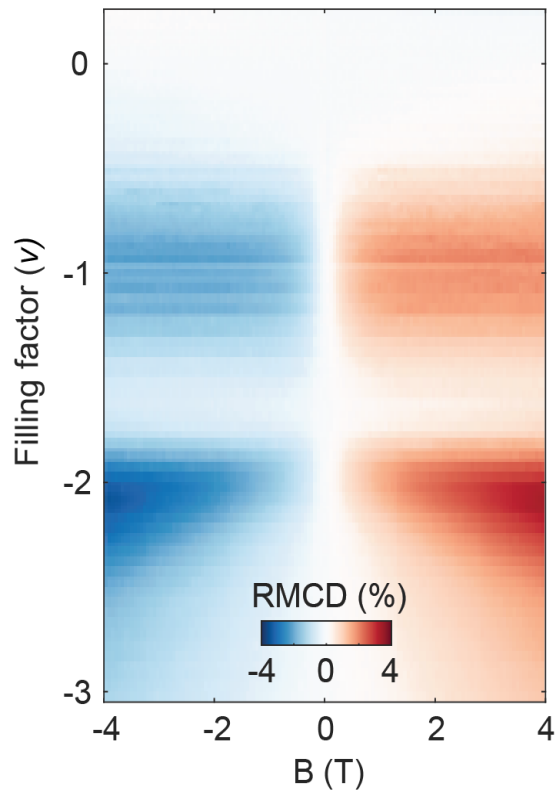
Kevin Slagle <sup>1,2</sup> and Liang Fu<sup>3</sup>

## **Electronic structures, charge transfer, and charge order in twisted transition metal dichalcogenide bilayers**

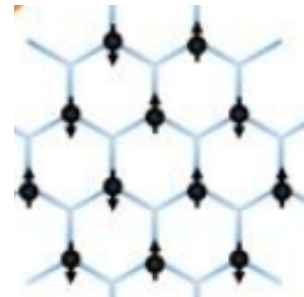
Yang Zhang <sup>\*</sup>, Tongtong Liu, and Liang Fu



# Intralayer Charge Transfer in $\text{WSe}_2/\text{WS}_2$

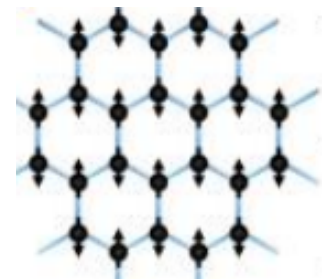


$n = 1$



charge-transfer  
Mott insulator

$n = 2$



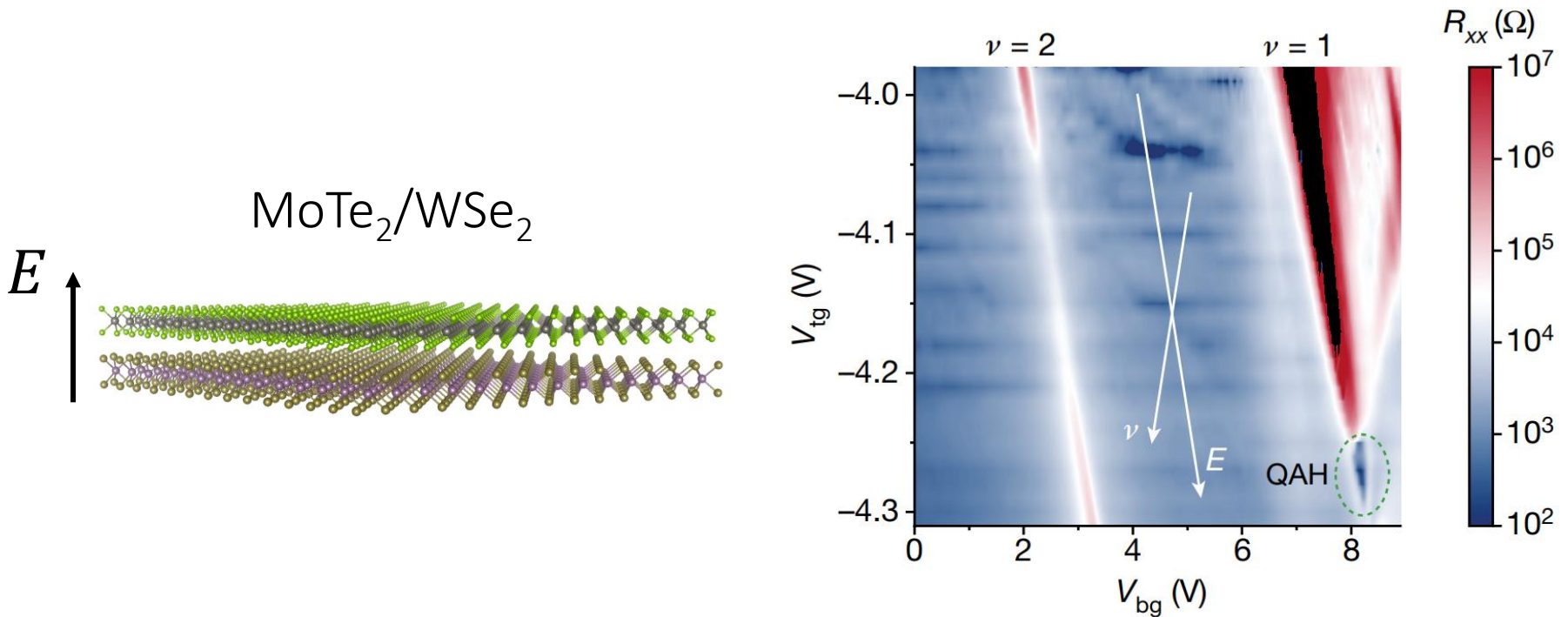
honeycomb lattice  
Mott-Hubbard

Xiaodong Xu's group (submitted)

See also Xu et al, arXiv:2202.02055

# Quantum anomalous Hall effect from intertwined moiré bands

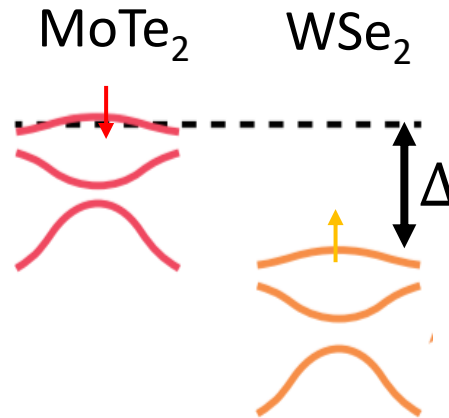
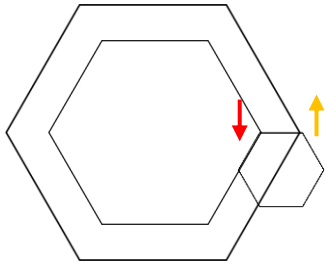
[Tingxin Li](#), [Shengwei Jiang](#), [Bowen Shen](#), [Yang Zhang](#), [Lizhong Li](#), [Zui Tao](#), [Trithep Devakul](#), [Kenji Watanabe](#), [Takashi Taniguchi](#), [Liang Fu](#), [Jie Shan](#)  & [Kin Fai Mak](#) 



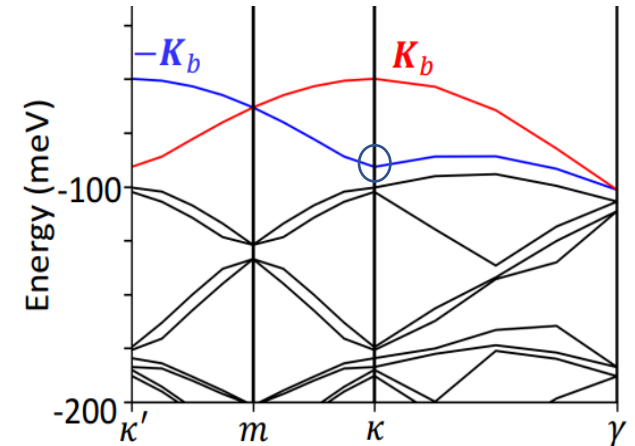
- Electric field tunes interlayer charge transfer

# Moire Bands in MoTe<sub>2</sub>/WSe<sub>2</sub>

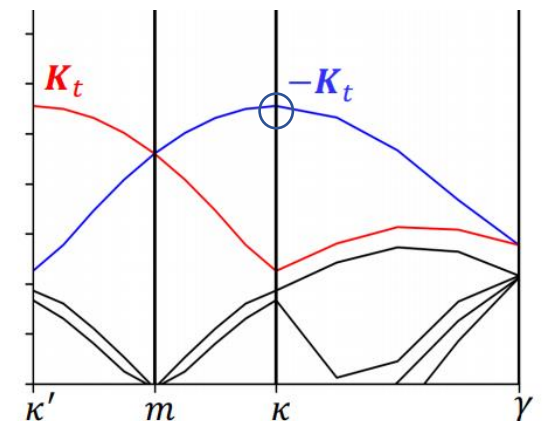
$$a_M = 4.6\text{nm}$$



13 x13 MoTe<sub>2</sub>

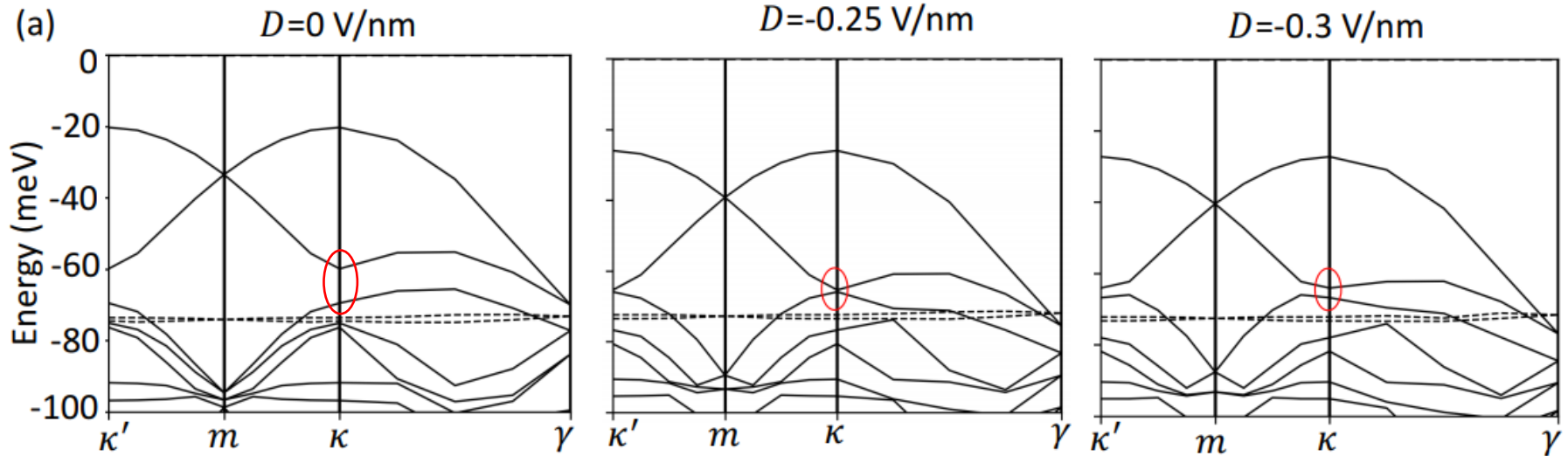


14 x14 WSe<sub>2</sub>



- $\Delta = 0.13\text{eV}$  at zero E field
- majority layer: MoTe<sub>2</sub>  
minority layer: WSe<sub>2</sub>
- moire band due to lattice corrugation with bandwidth  $\sim 50\text{ meV}$

# E Field Tunes Band Inversion

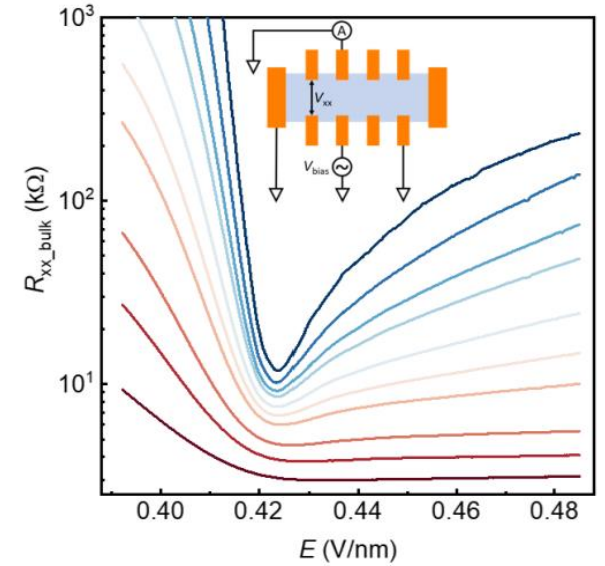
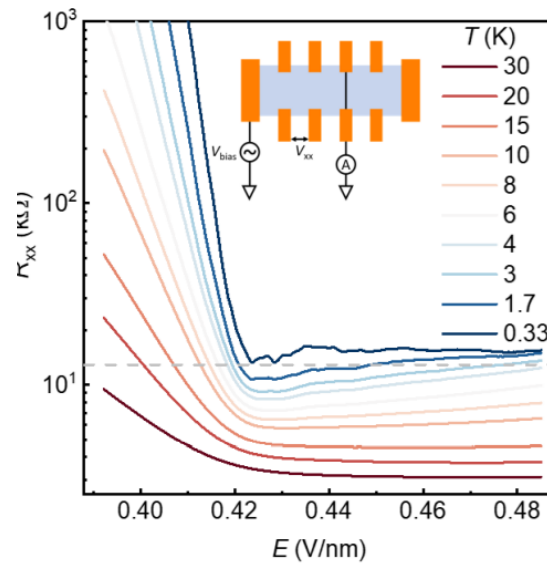
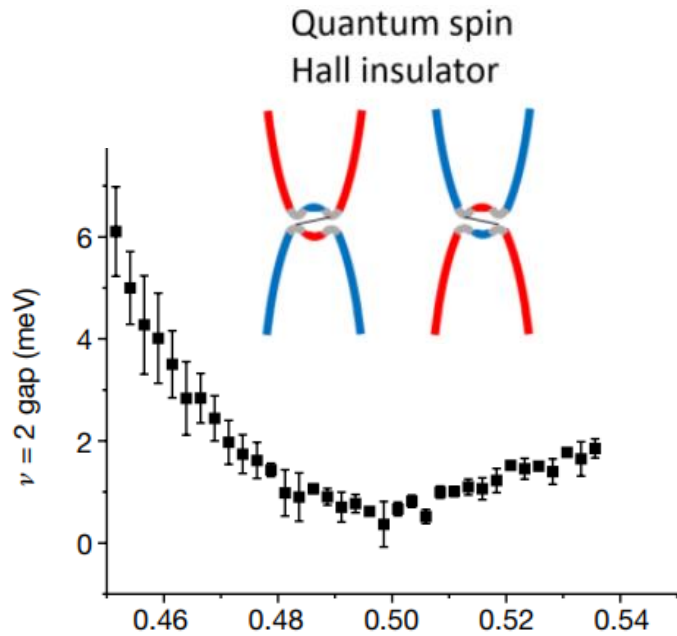


- electric field inverts minibands on two layers
- band inversion + p-wave interlayer tunneling  $\Rightarrow$  valley Chern number

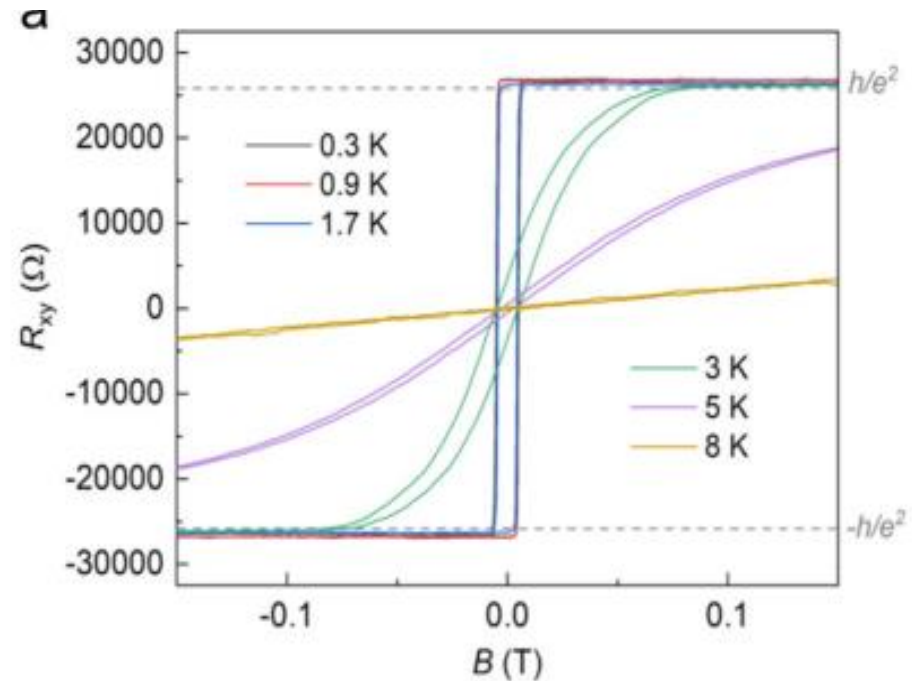
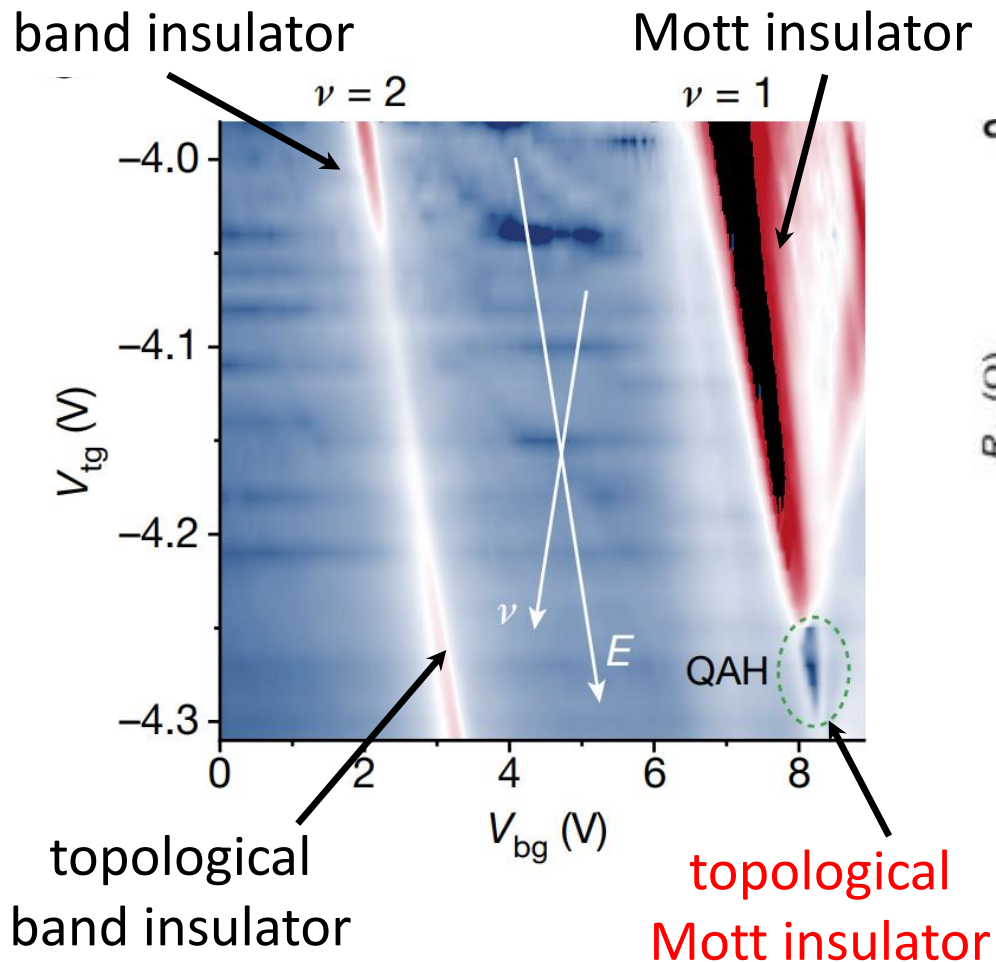
Prediction: E field induced quantum spin Hall insulator at  $n=2$

Zhang, Devakul & LF, PNAS (2021)

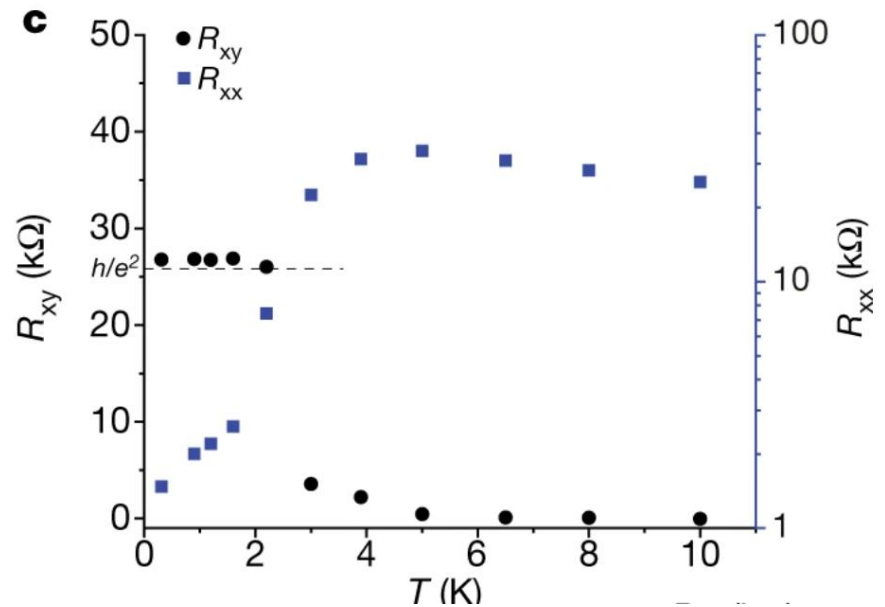
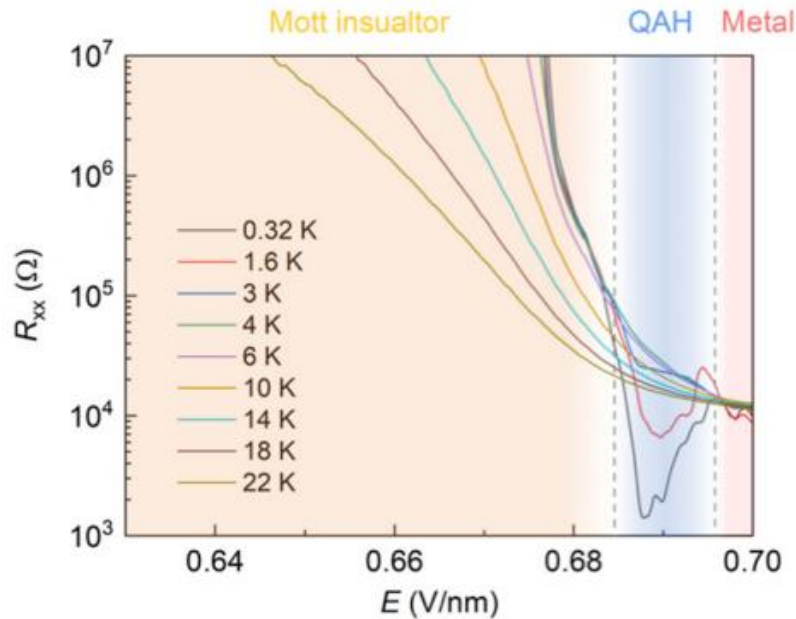
# Edge Transport in MoTe<sub>2</sub>/WSe<sub>2</sub>



# Quantum Anomalous Hall Effect at Half Filling



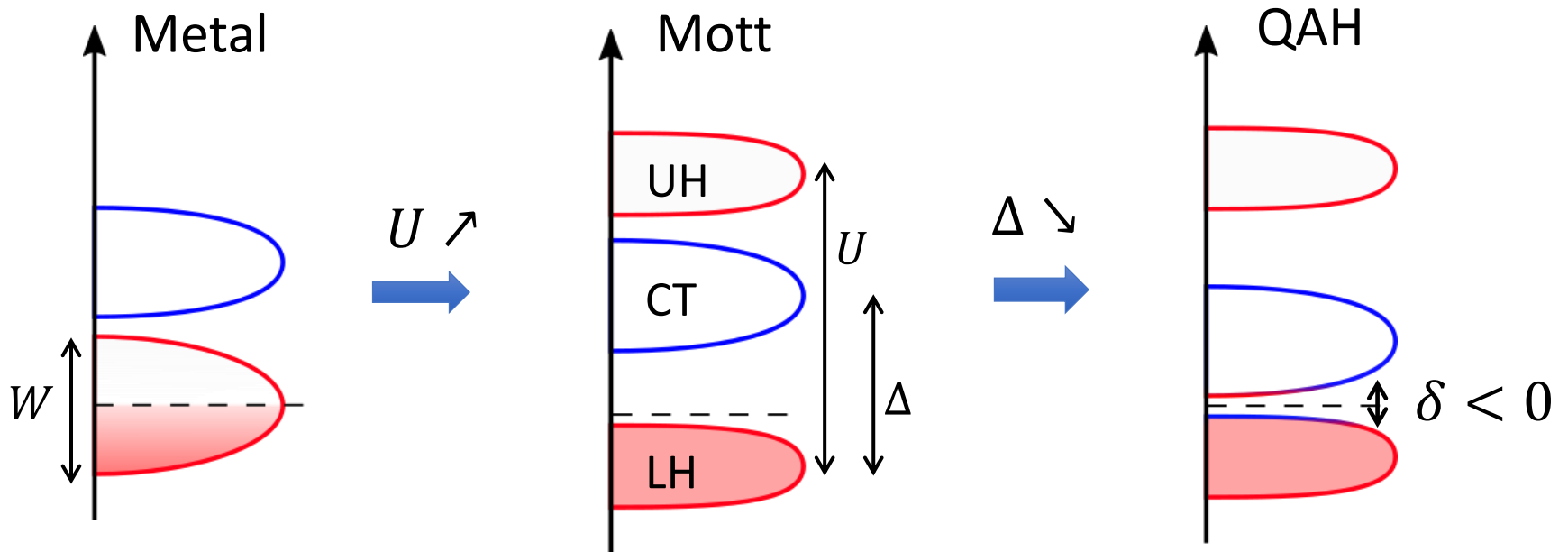
# E Field Induced Mott-QAH Transition



- absence of E field hysteresis
- robust and reproducible

# Mott to QAH Insulators

Mott-QAH transition by inverting charge transfer gap

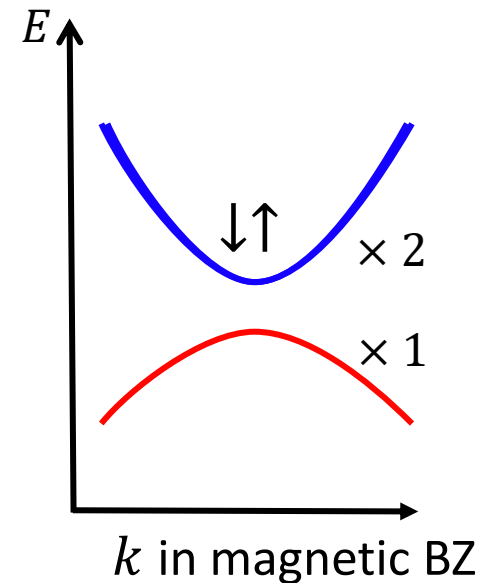
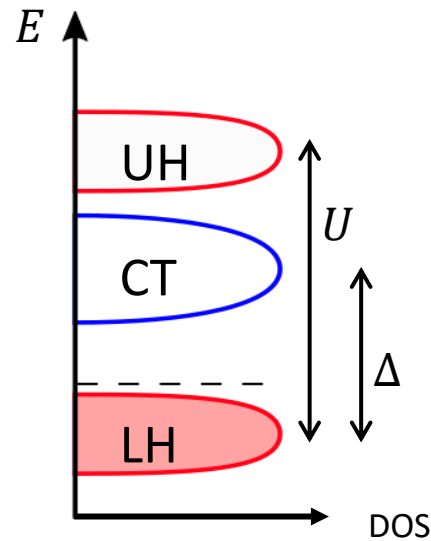
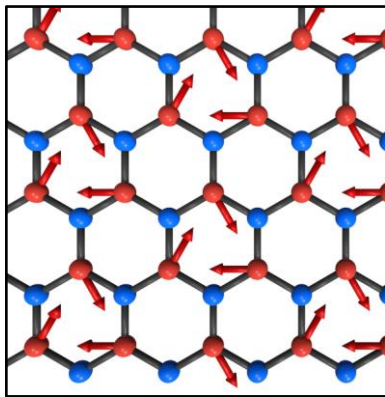


Devakul & LF, PRX (2022)

$$\delta \sim \Delta - W$$



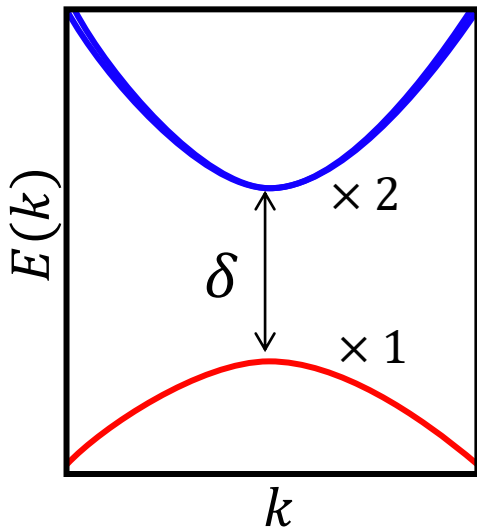
# 120°-AFM Mott Insulator



- Quasiparticle bands in magnetically ordered insulator are different from noninteracting bands.
- Low-energy states: **spin-polarized holes on majority layer** & **spin-degenerate electrons on minority layer**

# Interacting Field Theory

$$\mathcal{H}_{\text{eff}} = \int \psi^\dagger H_{\text{eff}} \psi d\mathbf{k} + g \int n_{B\uparrow}(r)n_{B\downarrow}(r)dr \quad \psi = (\psi_A, \psi_{B\uparrow}, \psi_{B\downarrow})$$

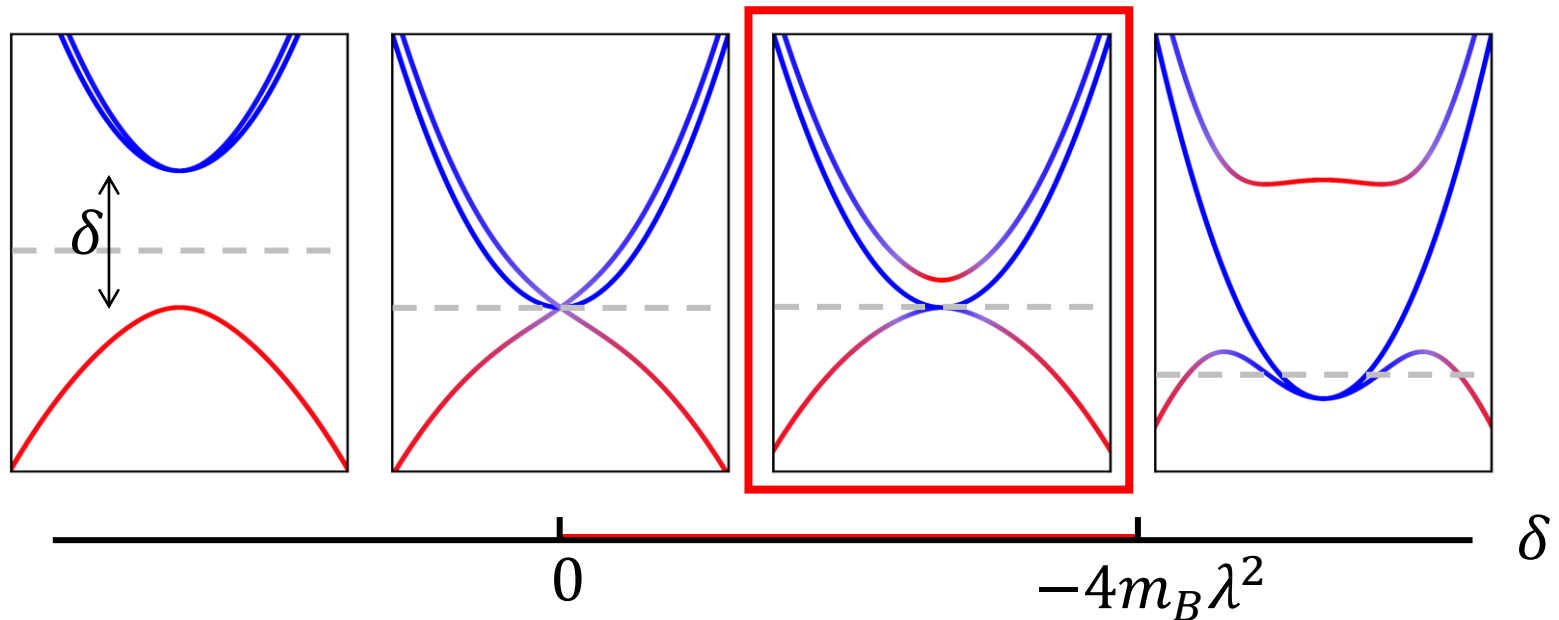


$$H_{\text{eff}} = \begin{pmatrix} -\frac{k^2}{2m_A} & \lambda(k_x + ik_y) & \lambda(k_x - ik_y) \\ " & \frac{k^2}{2m_B} + \delta & 0 \\ " & 0 & \frac{k^2}{2m_B} + \delta \end{pmatrix}$$

- spin degeneracy at  $k=0$  on minority layer protected by  $C_3$  &  $Ts_z$
- p-wave hybridization dictated by band symmetry
- $g$ : electron repulsion on minority layer

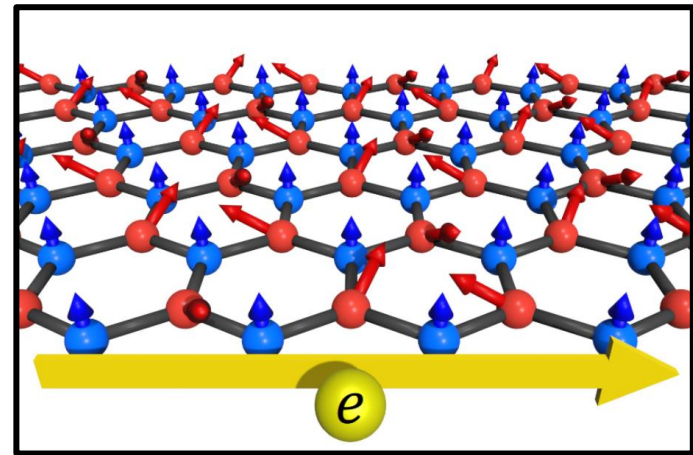
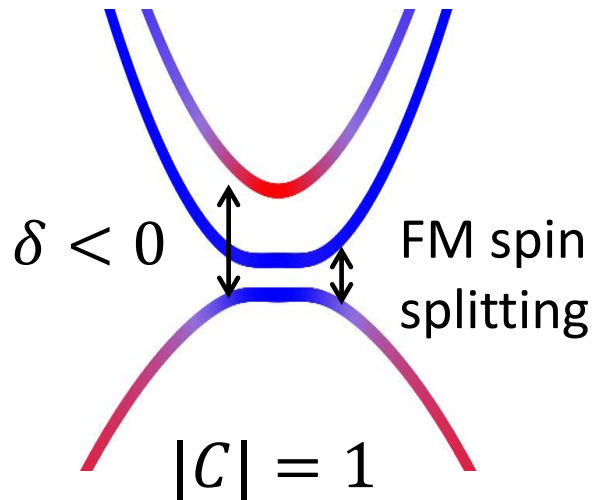
# Interacting Field Theory

Quasiparticle band at  $g = 0$



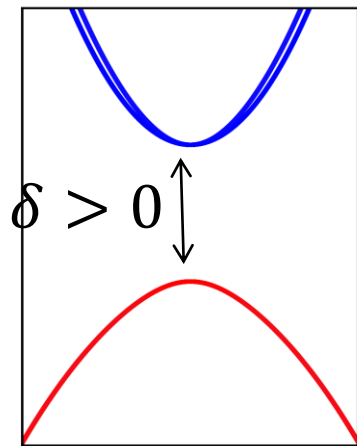
After band inversion  $\delta < 0$ , quadratic band touching appears at Fermi level, which is unstable to repulsion  $g$  [Sun, Yao, Fradkin, Kivelson, PRL 2009](#)  
 $g > 0$  changes from irrelevant to marginally relevant at band inversion!

# QAH with non-coplanar magnetism

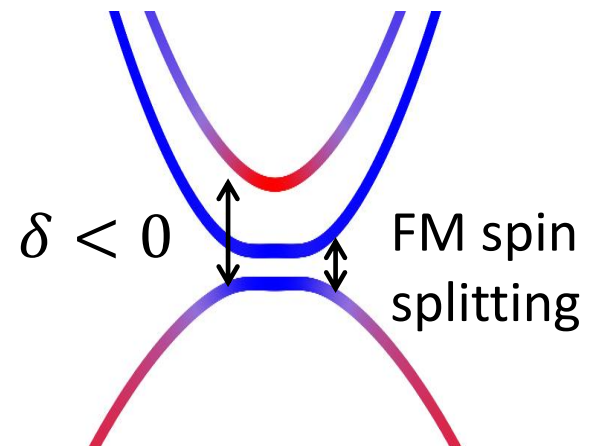
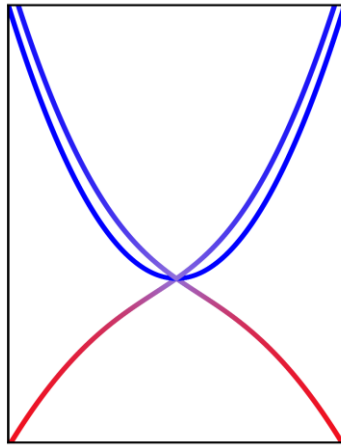


- chiral spin order: (canted) xy-AFM in  $\text{MoTe}_2$  & Ising FM in  $\text{WSe}_2$
- Ising FM opens Chern gap at quadratic band touching

# Continuous Mott-Chern Transition



$$C = 0$$

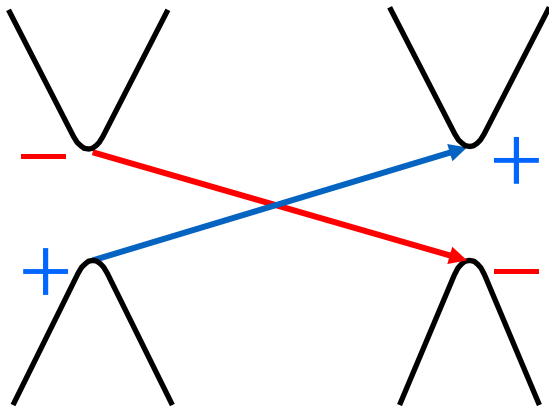


$$|C| = 1$$

Inverting charge transfer gap induces simultaneous change of magnetism & topology.

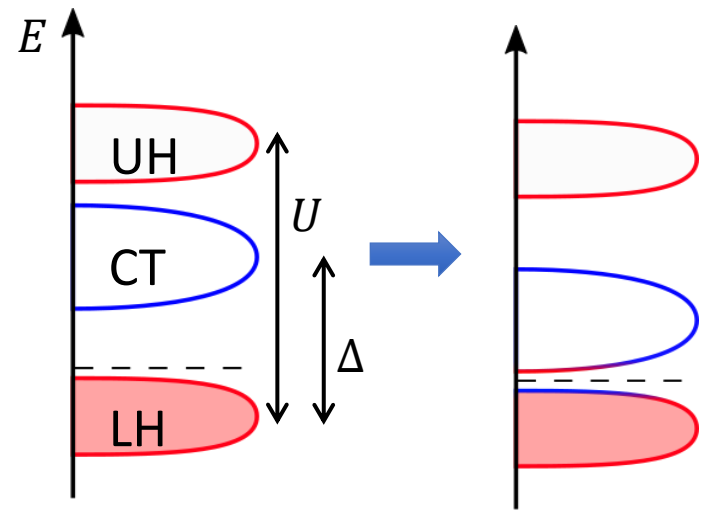
# Topological Band & Mott Insulators

Inverting single-particle gap  
(even-integer filling)



2007

Inverting many-body gap  
(odd-integer filling)



2022

AFM Mott insulators with **negative** charge transfer gap:  
potential route to high-temperature QAH

# Bridging Mott and Chern



# Comparison with Other QAH Systems

Magnetically doped TI film [Chang et al \(2013\)](#)

- FM of dopant opens Chern gap at surface Dirac point
- even integer filling

Magic-angle graphene [Sharpe et al, Serlin et al \(2019\)](#)

- fully valley-polarized flat Chern band

$$C_K = +1$$

---

$$C_{K'} = -1$$

---

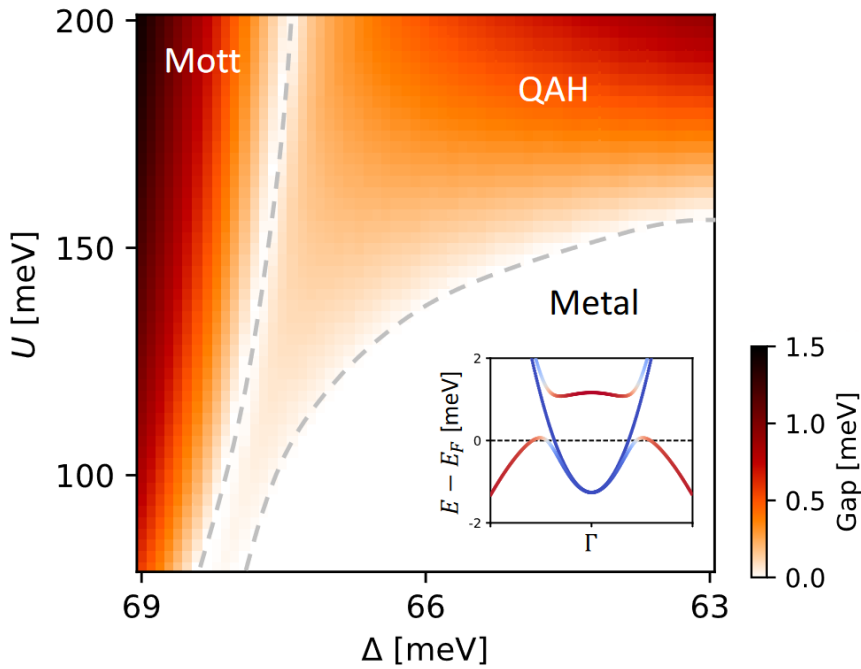
[Zhang & Senthil, MacDonald, Xie et al, Pan et al ...](#)

QAH in  $\text{MoTe}_2/\text{WSe}_2$  differs fundamentally from flat band FM.

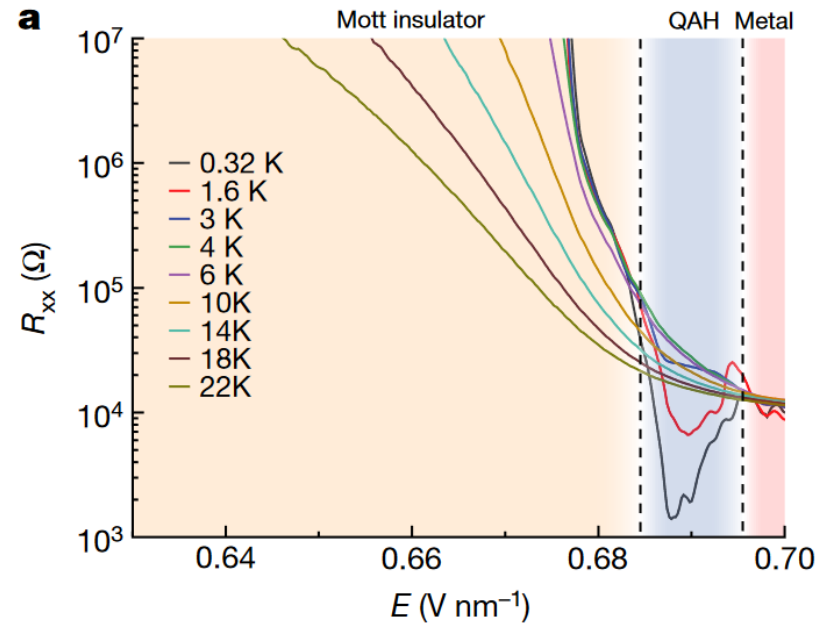


# Comparison with Experiment

## Hartree-Fock Phase Diagram



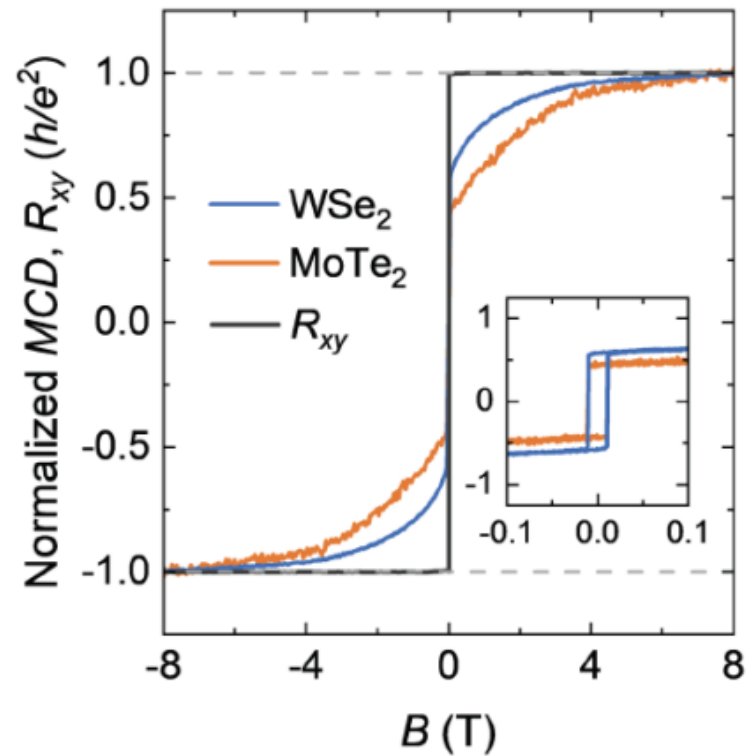
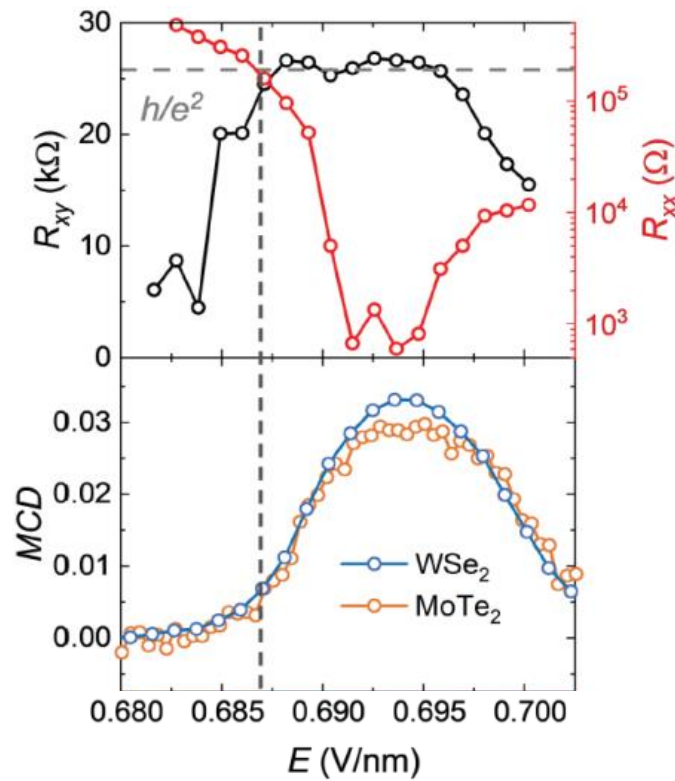
## MoTe<sub>2</sub>/WSe<sub>2</sub>



# Prediction for Magnetism

- Mott: **zero** spin  $S_z$  polarization
- QAH: **finite but incomplete** spin  $S_z$  polarization increasing with B field and E field
- Intervalley  $XY$  magnetic order: **gapless** magnon

# Evidence for Canted Spin Texture in QAH



# Outlook

- charge gap across Mott-Chern transition
- spin superfluidity
- critical exponents
- inverting quantum spin liquid