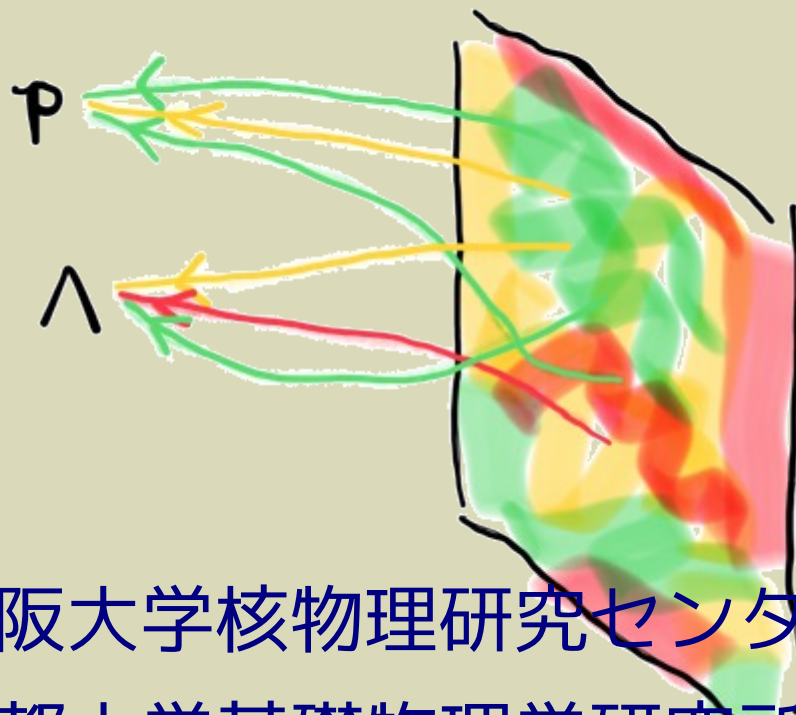


# 格子 QCD によるハイペロン核力の研究

根村英克<sup>1</sup>,

$$\langle P(x) \Lambda(x+r) \overline{P \Lambda} \rangle$$



<sup>1</sup>大阪大学核物理研究センター  
京都大学基礎物理学研究所

arXiv:1510.00903 [hep-lat]

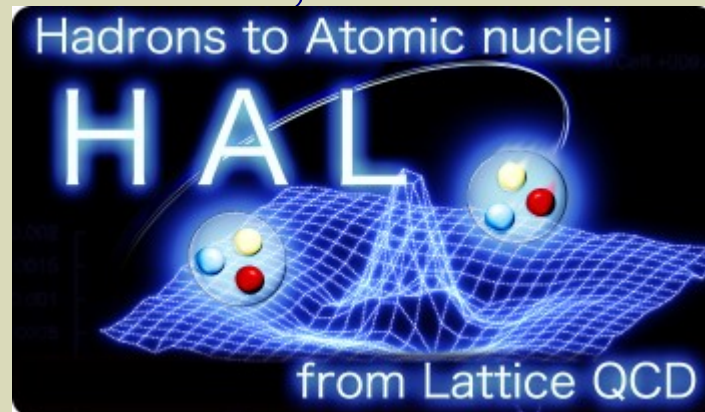
arXiv:1810.04046 [hep-lat]

# Study of hyperonic nuclear forces from lattice QCD

H. Nemura<sup>1,2</sup>,

for HAL QCD Collaboration

Y. Akahoshi<sup>2</sup>, S. Aoki<sup>2</sup>, T. Aoyama<sup>2</sup>, T. Doi<sup>3</sup>, T. M. Doi<sup>3</sup>,  
F. Etminan<sup>4</sup>, S. Gongyo<sup>3</sup>, T. Hatsuda<sup>3</sup>, Y. Ikeda<sup>1</sup>,  
T. Inoue<sup>5</sup>, T. Iritani<sup>3</sup>, N. Ishii<sup>1</sup>, T. Miyamoto<sup>2</sup>,  
K. Murano<sup>1</sup>, and K. Sasaki<sup>2</sup>,



<sup>1</sup>*Osaka University,*

<sup>2</sup>*Kyoto University,* <sup>3</sup>*RIKEN,* <sup>4</sup>*University of Birjand,*

<sup>5</sup>*Nihon University*

arXiv:1510.00903 [hep-lat]

arXiv:1810.04046 [hep-lat]

# Outline

- ⊗ Introduction
  - ⊗ HAL QCD method for baryon-baryon interaction
- ⊗ Preliminary results of LN-SN potentials at  $(m_{\pi}, m_K) \approx (145, 525) \text{ MeV}$
- ⊗ Single channel analysis for LN  $\implies$  central and tensor potentials
  - ⊗ Phase shifts at low energy region below the SN threshold
- ⊗ LN-SN(I=1/2), central and tensor potentials
  
- ⊗ Effective block algorithm for various baryon-baryon channels, CPC**207**,91(2016)[1510.00903]
  - ⊗ New application of the algorithm
  
- ⊗ Summary

# Plan of research



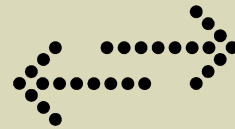
QCD



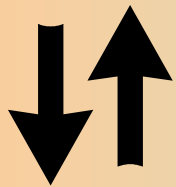
KEI Computer @ AICS (RIKEN)  
(10PFlops)



Baryon interaction



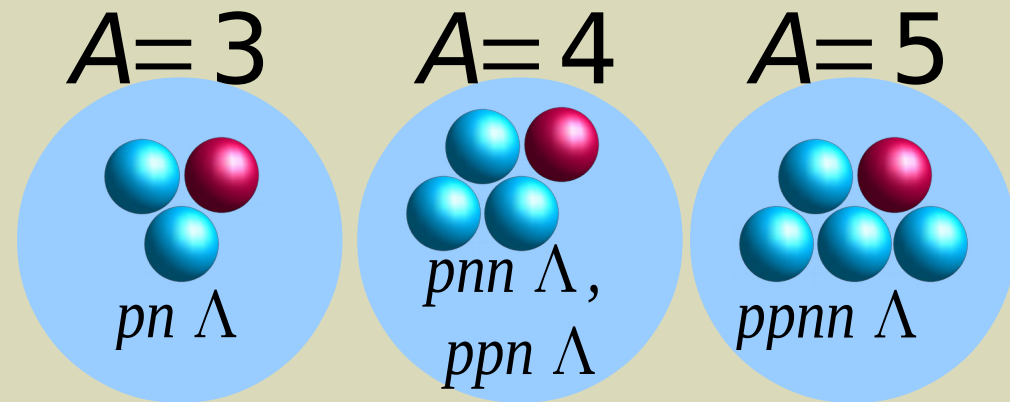
J-PARC,  
JLab, GSI, MAMI, ...  
YN scattering,  
hypernuclei



Structure and reaction of  
(hyper)nuclei

Equation of State (EoS)  
of nuclear matter

Neutron star and  
supernova



# Multi-hadron on lattice

i) basic procedure:

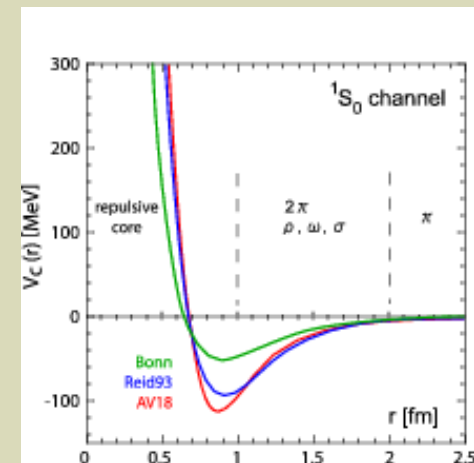
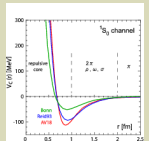
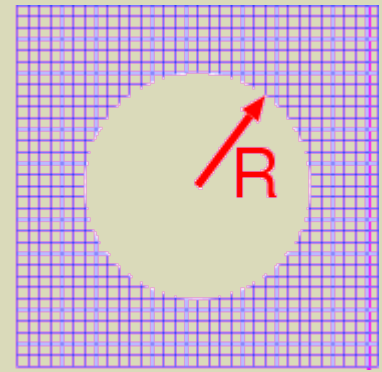
asymptotic region

--> phase shift

ii) HAL's procedure:

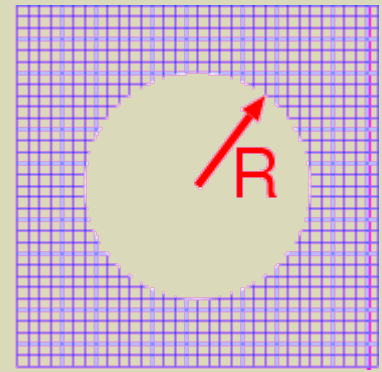
interacting region

--> potential



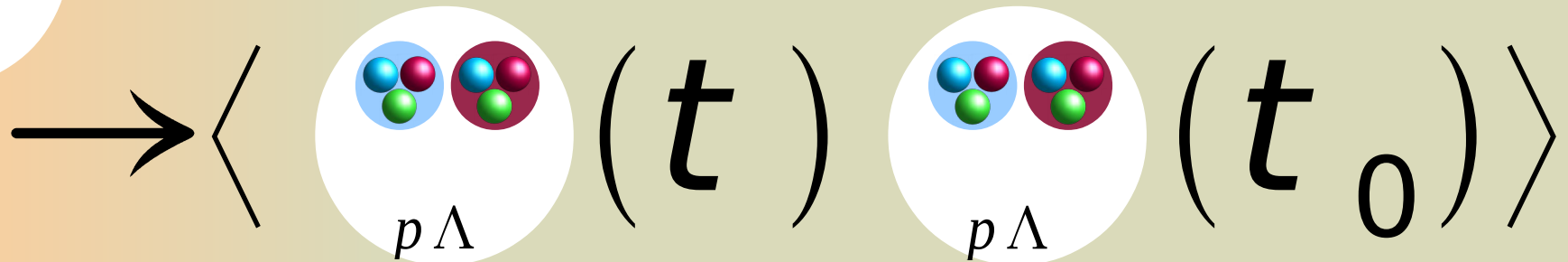
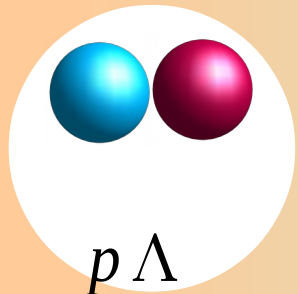
# Multi-hadron on lattice

Lattice QCD simulation

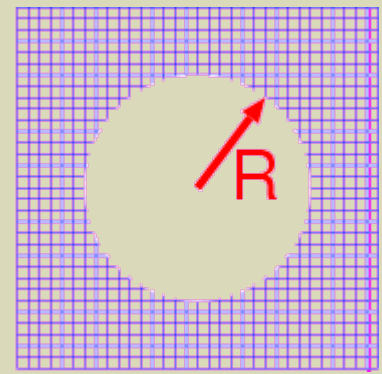
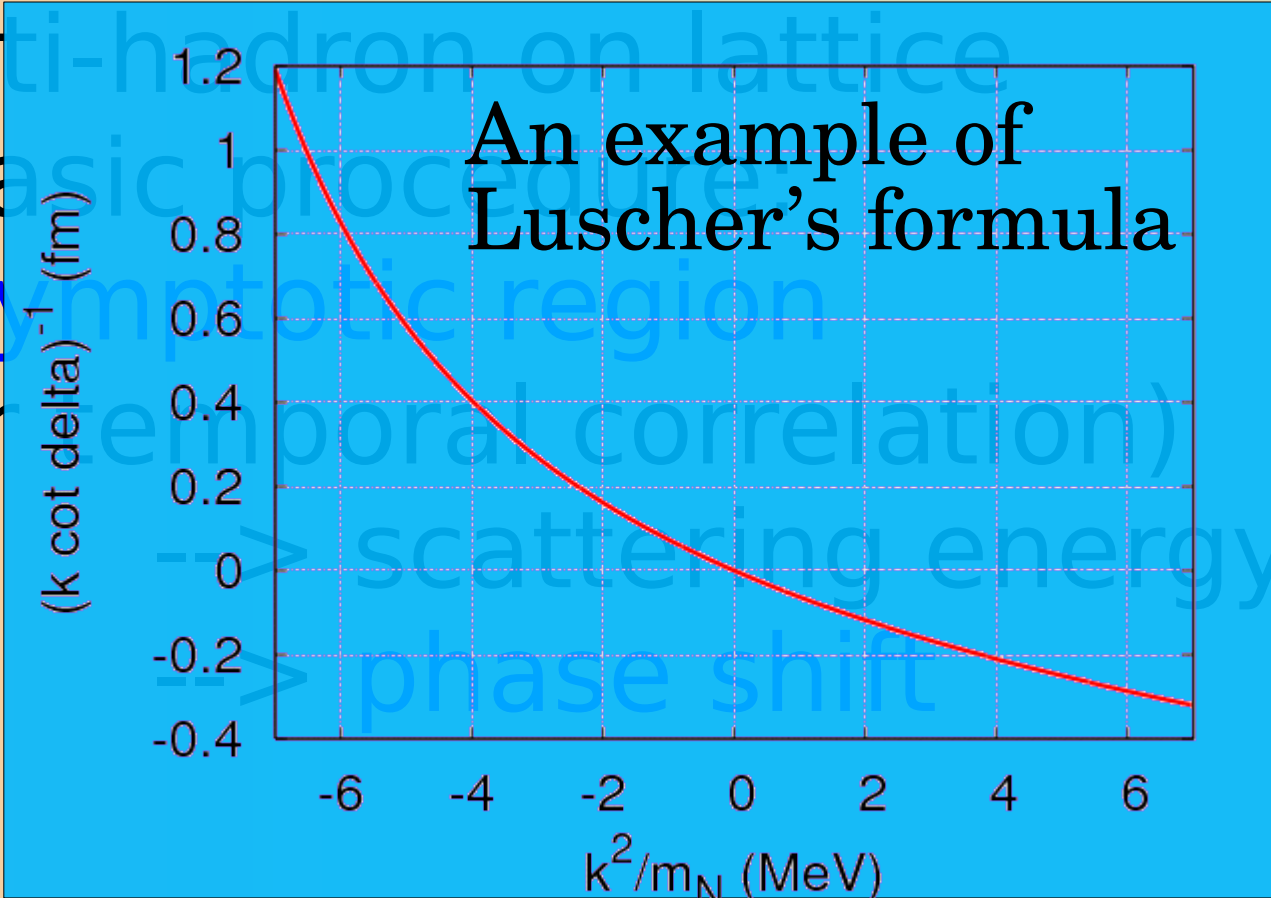


$$L = -\frac{1}{4} G_{\mu\nu}^a G^{a\mu\nu} + \bar{q} \gamma^\mu (i \partial_\mu - g t^a A_\mu^a) q - m \bar{q} q$$

$$\begin{aligned} \langle O(\bar{q}, q, U) \rangle &= \int dU d\bar{q} dq e^{-S(\bar{q}, q, U)} O(\bar{q}, q, U) \\ &= \int dU \det D(U) e^{-S_U(U)} O(D^{-1}(U)) \\ &= \lim_{N \rightarrow \infty} \frac{1}{N} \sum_{i=1}^N O(D^{-1}(U_i)) \end{aligned}$$



Multi-hadron on lattice  
 i) basic  
 asymptotic region  
 (or temporal correlation)



$$E = \frac{k^2}{2\mu}$$

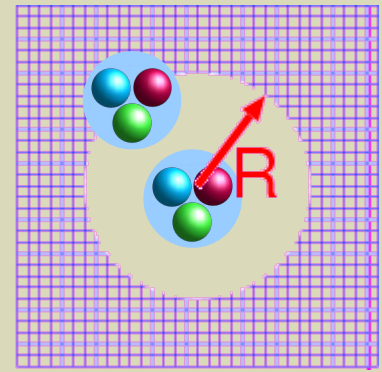
$$k \cot \delta_0(k) = \frac{2}{\sqrt{\pi} L} Z_{00}(1; (kL/(2\pi))^2) = \frac{1}{a_0} + O(k^2)$$

$$Z_{00}(1; q^2) = \frac{1}{\sqrt{4\pi}} \sum_{\vec{n} \in \mathbb{Z}^3} \frac{1}{(n^2 - q^2)^s} \quad \Re s > \frac{3}{2}$$

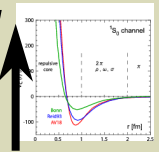
Luscher, NPB354, 531 (1991).  
 Aoki, et al., PRD71, 094504 (2005).

# Multi-hadron on lattice

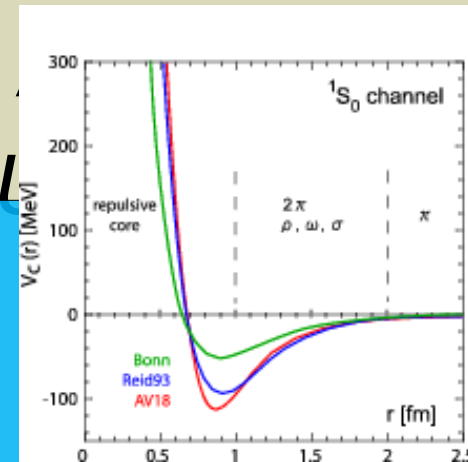
Lattice QCD simulation



$$L = -\frac{1}{4} G_{\mu\nu}^a G^{a\mu\nu} + \bar{q} \gamma^\mu (i \partial_\mu - g t^a A_\mu^a) q - m \bar{q} q$$



$$\begin{aligned} \langle O(\bar{q}, q, U) \rangle &= \int dU d\bar{q} dq e^{-S(\bar{q}, q, U)} O(\bar{q}, q) \\ &= \int dU \det D(U) e^{-S_U(U)} O(D^{-1}(U)) \end{aligned}$$



$$F_{\alpha\beta}^{(JM)}(\vec{r}, t - t_0)$$

$$\rightarrow \left\langle \left( \text{p} \Lambda \right) (\vec{r}, t) \left( \text{p} \Lambda \right) (t_0) \right\rangle$$

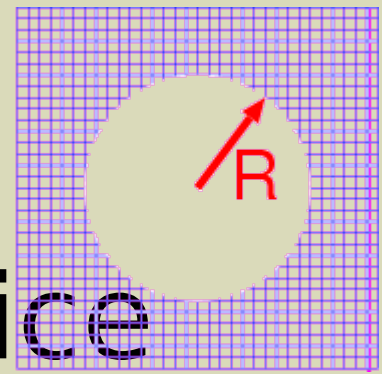
Calculate the scattering state



# Multi-hadron on lattice

ii) HAL's procedure:

make better use of the lattice  
output ! (wave function)



interacting region

--> potential

Ishii, Aoki, Hatsuda,  
PRL99, 022001 (2007);  
ibid., PTP123, 89 (2010).

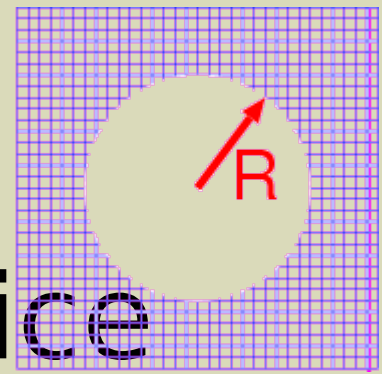
## NOTE:

- > Potential is not a direct experimental observable.
- > Potential is a useful tool to give (and to reproduce) the physical quantities. (e.g., phase shift)

# Multi-hadron on lattice

ii) HAL's procedure:

make better use of the lattice  
output ! (wave function)



interacting region

--> potential

Ishii, Aoki, Hatsuda,  
PRL99, 022001 (2007);  
ibid., PTP123, 89 (2010).

=>

> Phase shift

> Nuclear many-body problems

# An improved recipe for NY potential:

cf. Ishii (HAL QCD), PLB712 (2012) 437.

- Take account of not only the spatial correlation but also the temporal correlation in terms of the R-correlator:

$$-\frac{1}{2\mu} \nabla^2 R(t, \vec{r}) + \int d^3 r' U(\vec{r}, \vec{r}') R(t, \vec{r}') = -\frac{\partial}{\partial t} R(t, \vec{r})$$

$$\rightarrow \frac{k^2}{2\mu} R(t, \vec{r})$$

- A general expression of the potential:  
$$U(\vec{r}, \vec{r}') = V_{NY}(\vec{r}, \vec{V}) \delta(\vec{r} - \vec{r}')$$

$$\begin{aligned} V_{NY} = & V_0(r) + V_\sigma(r) (\vec{\sigma}_N \cdot \vec{\sigma}_Y) \\ & + V_T(r) S_{12} + V_{LS}(r) (\vec{L} \cdot \vec{S}_+) \\ & + V_{ALS}(r) (\vec{L} \cdot \vec{S}_-) + O(\nabla^2) \end{aligned}$$

# 格子QCDによるポテンシャル導出の手順(超簡略版)

(1) 4点相関関数を計算する。

$$F_{\alpha\beta, JM}^{(B_1 B_2 \overline{B_3 B_4})}(\vec{r}, t - t_0) = \sum_{\vec{X}} \left\langle 0 \left| B_{1,\alpha}(\vec{X} + \vec{r}, t) B_{2,\beta}(\vec{X}, t) \overline{\mathcal{J}_{B_3 B_4}^{(J,M)}(t_0)} \right| 0 \right\rangle, \quad (2.3)$$

(2) 時間依存法を使うためにしきい値だけ時間相関をずらす

$$\begin{aligned} R_{\alpha\beta, JM}^{(B_1 B_2 \overline{B_3 B_4})}(\vec{r}, t - t_0) &= e^{(m_{B_1} + m_{B_2})(t - t_0)} F_{\alpha\beta, JM}^{(B_1 B_2 \overline{B_3 B_4})}(\vec{r}, t - t_0) \\ &= \sum_n A_n \sum_{\vec{X}} \left\langle 0 \left| B_{1,\alpha}(\vec{X} + \vec{r}, 0) B_{2,\beta}(\vec{X}, 0) \right| E_n \right\rangle e^{-(E_n - m_{B_1} - m_{B_2})(t - t_0)} + \underline{O(e^{-(E_{th} - m_{B_1} - m_{B_2})(t - t_0)})} \end{aligned} \quad (2.4)$$

(3) チャンネルごとにしきい値が異なるので、それを考慮した時間依存型Schroedinger方程式からポテンシャルを求める

$$\left( \frac{\nabla^2}{2\mu_\lambda} - \frac{\partial}{\partial t} \right) R_{\lambda\varepsilon}(\vec{r}, t) \simeq V_{\lambda\lambda'}^{(LO)}(\vec{r}) \theta_{\lambda\lambda'} R_{\lambda'\varepsilon}(\vec{r}, t), \text{ with } \theta_{\lambda\lambda'} = e^{(m_{B_1} + m_{B_2} - m_{B'_1} - m_{B'_2})(t - t_0)}.$$

(※) “moderately large imaginary time” で計算を行う

(※※) 2種類の励起状態を区別している

<sup>1</sup>The potential is obtained from the NBS wave function at moderately large imaginary time; it would be  $t - t_0 \gg 1/m_\pi \sim 1.4 \text{ fm}$ . In addition, no single state saturation between the ground state and the excited states with respect to the relative motion, e.g.,  $t - t_0 \gg (\Delta E)^{-1} = ((2\pi)^2 / (2\mu(La)^2))^{-1} \simeq 8.0 \text{ fm}$ , is required for the HAL QCD method[13].

# Almost physical point lattice QCD calculation using $N_F=2+1$ clover fermion + Iwasaki gauge action

- ⊗ APE-Stout smearing ( $r=0.1$ ,  $n_{\text{stout}}=6$ )
- ⊗ Non-perturbatively  $O(a)$  improved Wilson Clover action at  $\beta=1.82$  on  $96^3 \times 96$  lattice
- ⊗  $1/a = 2.3 \text{ GeV}$  ( $a = 0.085 \text{ fm}$ )
- ⊗ Volume:  $96^4 \rightarrow (8\text{fm})^4$
- ⊗  $m_D = 145\text{MeV}$ ,  $m_K = 525\text{MeV}$
- ⊗ DDHMC(ud) and UVPHMC(s) with preconditioning
- ⊗ K.-I.Ishikawa, et al., PoS LAT2015, 075;  
arXiv:1511.09222 [hep-lat].



- ⊗ NBS wf is measured using wall quark source with Coulomb gauge fixing, spatial PBD and temporal DBC;  
#stat=207configs x 4rotation x 96src

In lattice QCD calculations, we compute the normalized four-point correlation function

$$R_{\alpha\beta}^{(J,M)}(\vec{r}, t-t_0) = \sum_{\vec{X}} \langle 0 | B_{1,\alpha}(\vec{X} + \vec{r}, t) B_{2,\beta}(\vec{X}, t) \overline{\mathcal{J}_{B_3 B_4}^{(J,M)}}(t_0) | 0 \rangle / \exp\{-(m_{B_1} + m_{B_2})(t-t_0)\},$$

$$p = \varepsilon_{abc} (u_a C \gamma_5 d_b) u_c, \quad n = -\varepsilon_{abc} (u_a C \gamma_5 d_b) d_c, \quad (2)$$

$$\Sigma^+ = -\varepsilon_{abc} (u_a C \gamma_5 s_b) u_c, \quad \Sigma^- = -\varepsilon_{abc} (d_a C \gamma_5 s_b) d_c, \quad (3)$$

$$\Sigma^0 = \frac{1}{\sqrt{2}} (X_u - X_d), \quad \Lambda = \frac{1}{\sqrt{6}} (X_u + X_d - 2X_s), \quad (4)$$

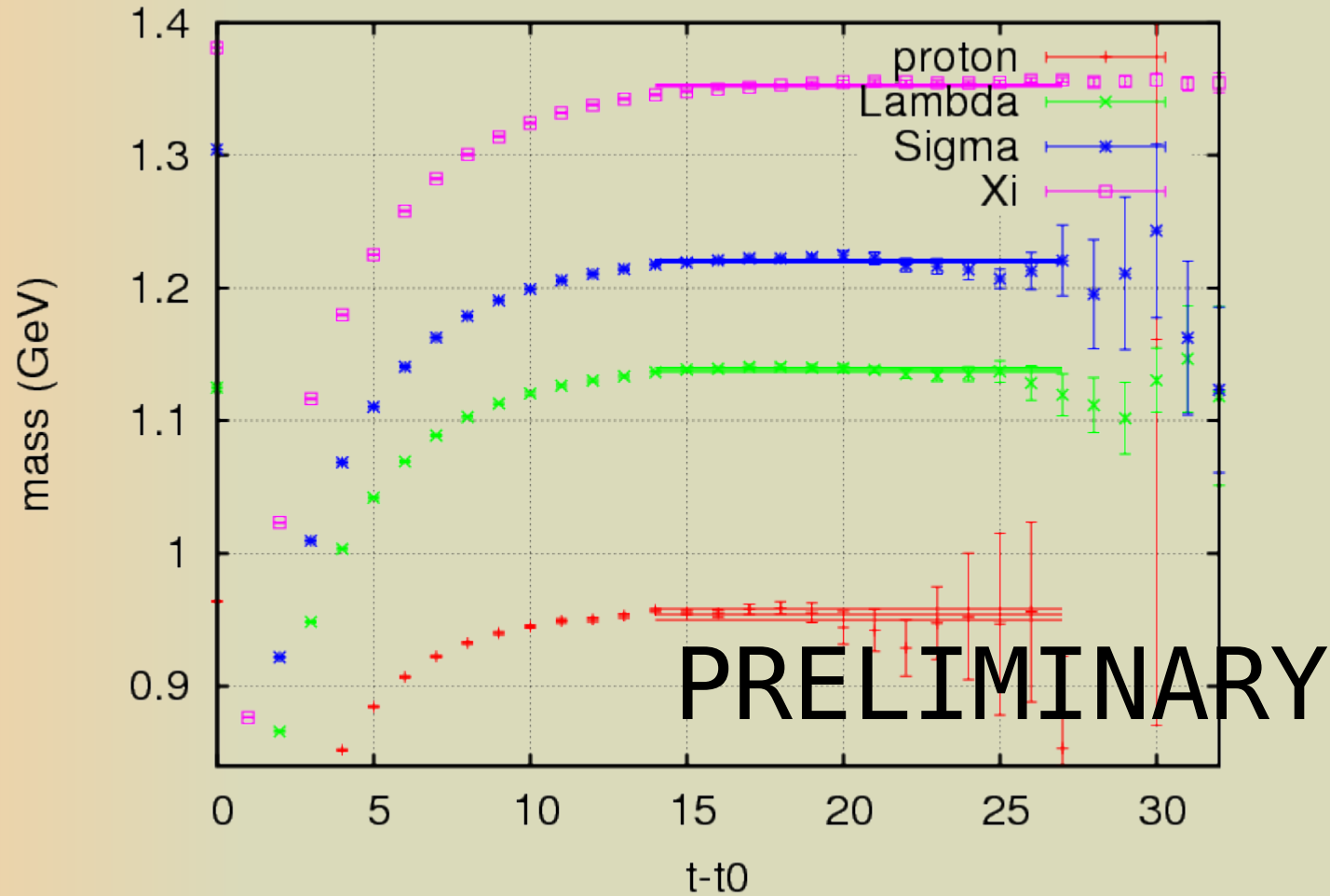
$$\Xi^0 = \varepsilon_{abc} (u_a C \gamma_5 s_b) s_c, \quad \Xi^- = -\varepsilon_{abc} (d_a C \gamma_5 s_b) s_c, \quad (5)$$

where

$$X_u = \varepsilon_{abc} (d_a C \gamma_5 s_b) u_c, \quad X_d = \varepsilon_{abc} (s_a C \gamma_5 u_b) d_c, \quad X_s = \varepsilon_{abc} (u_a C \gamma_5 d_b) s_c, \quad (6)$$

$$\left( \frac{\nabla^2}{2\mu} - \frac{\partial}{\partial t} \right) R(\vec{r}, t) = \int d^3 r' U(\vec{r}, \vec{r}') R(\vec{r}', t) + O(k^4) = V_{\text{LO}}(\vec{r}) R(\vec{r}, t) + \dots (8)$$

# Effective mass plot of the single baryon's correlation function

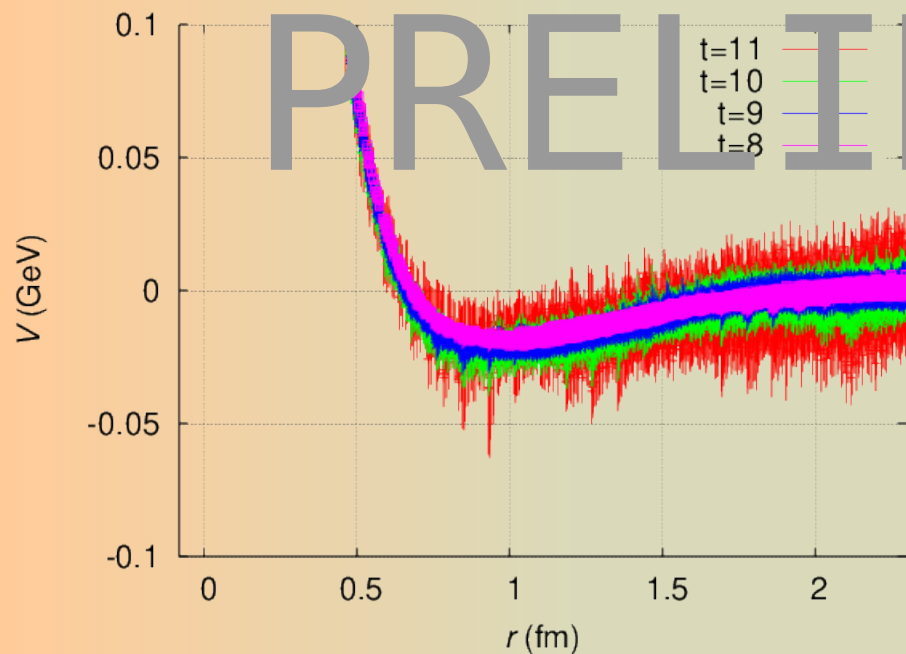


# Preliminary result of LN potential at the $(m_\pi, m_K) \approx (145, 525) \text{ MeV}$

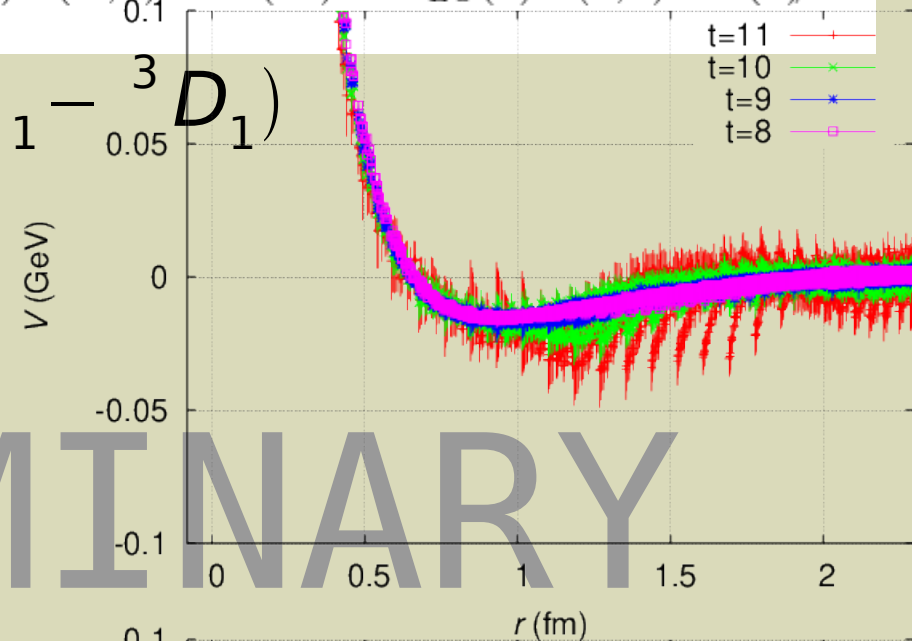
$$\left( \frac{\nabla^2}{2\mu} - \frac{\partial}{\partial t} \right) R(\vec{r}, t) = \int d^3r' U(\vec{r}, \vec{r}') R(\vec{r}', t) + O(k^4) = V_{\text{LO}}(\vec{r}) R(\vec{r}, t) + \dots \quad (8)$$

$\Delta N$

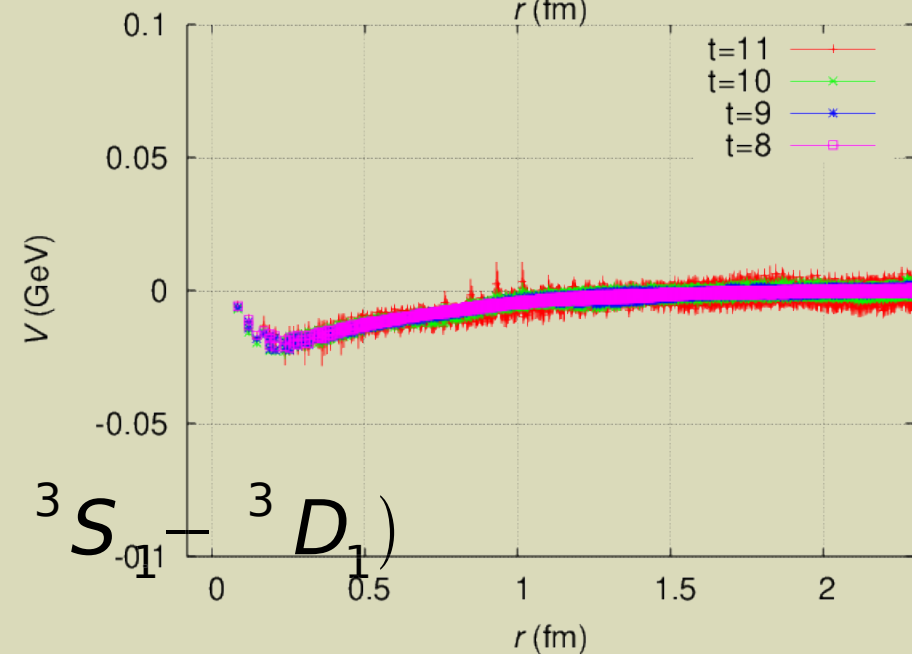
$V_C( {}^3S_1 - {}^3D_1 )$



$V_C( {}^1S_0 )$



$V_T( {}^3S_1 - {}^3D_1 )$



PRELIMINARY

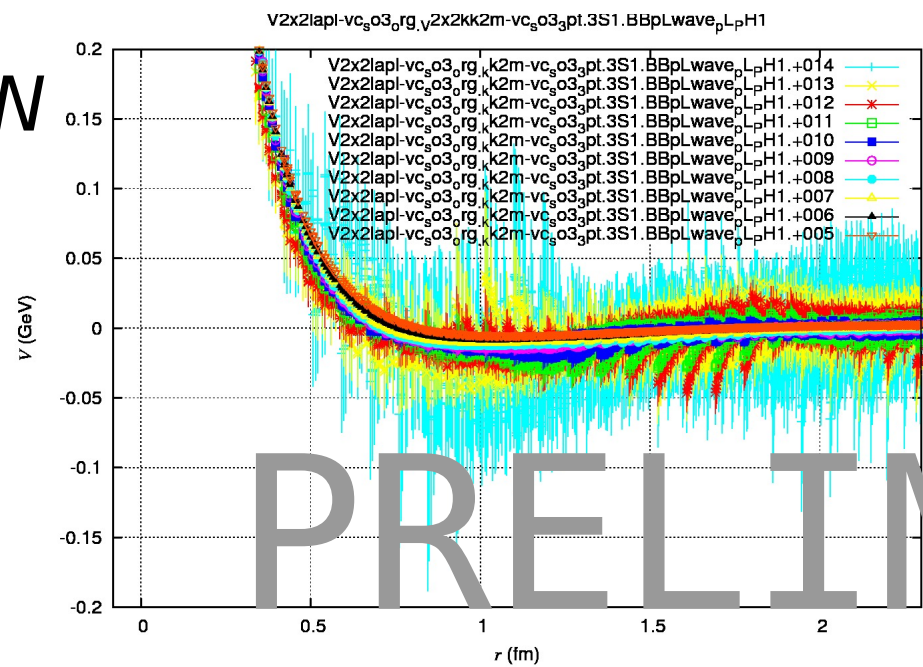


# Very preliminary result of LN potential at the physical point

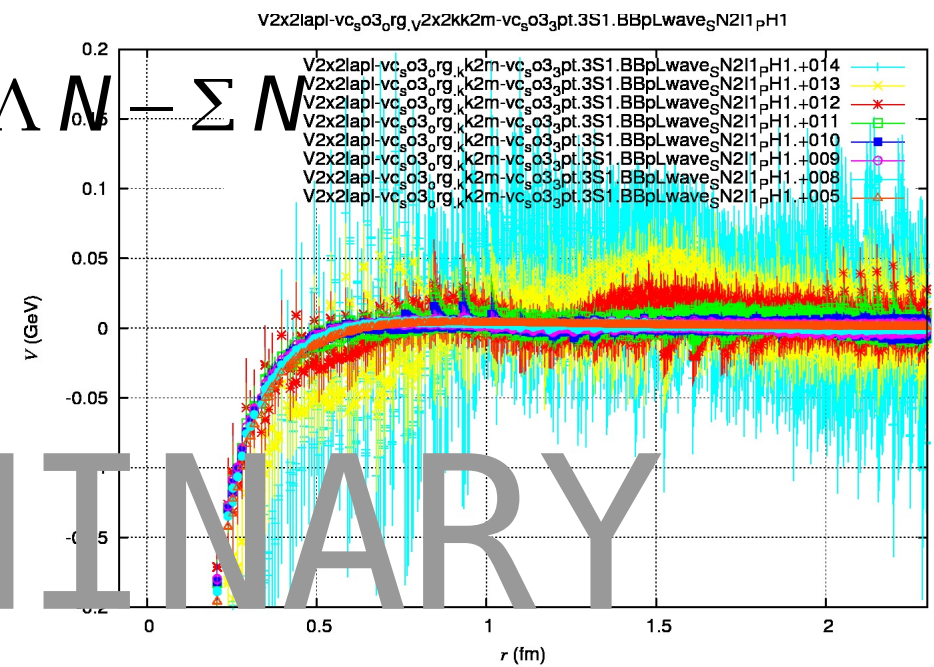
$$V_C({}^3S_1 - {}^3D_1)$$

$$\left(\frac{\nabla^2}{2\mu} - \frac{\partial}{\partial t}\right) R(\vec{r}, t) = \int d^3r' U(\vec{r}, \vec{r}') R(\vec{r}', t) + O(k^4) = V_{LO}(\vec{r}) R(\vec{r}, t) + \dots \quad (8)$$

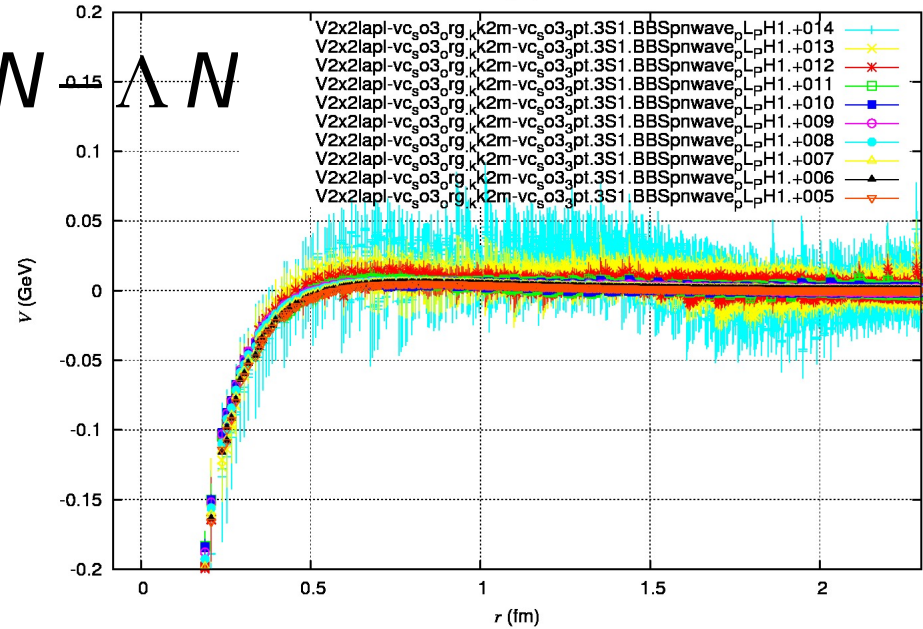
$\Lambda N$



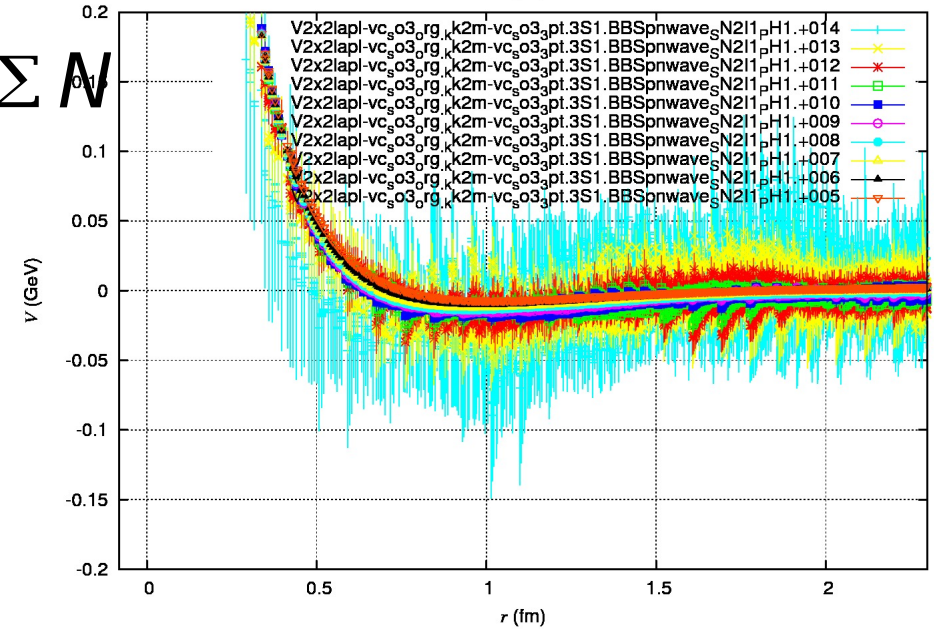
$\Lambda N - \Sigma N$



$\Sigma N$



$\Sigma N$

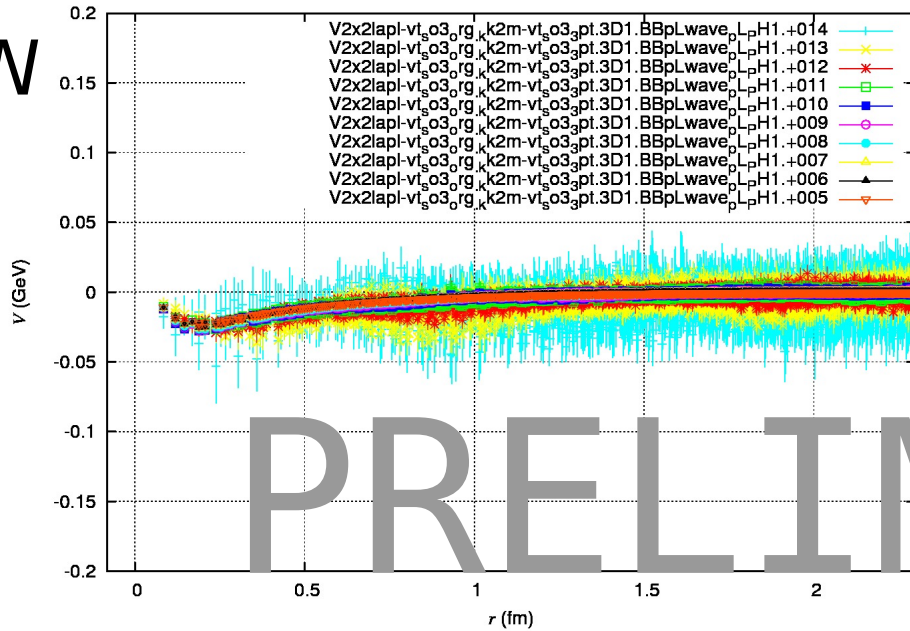


# Very preliminary result of LN potential at the physical point

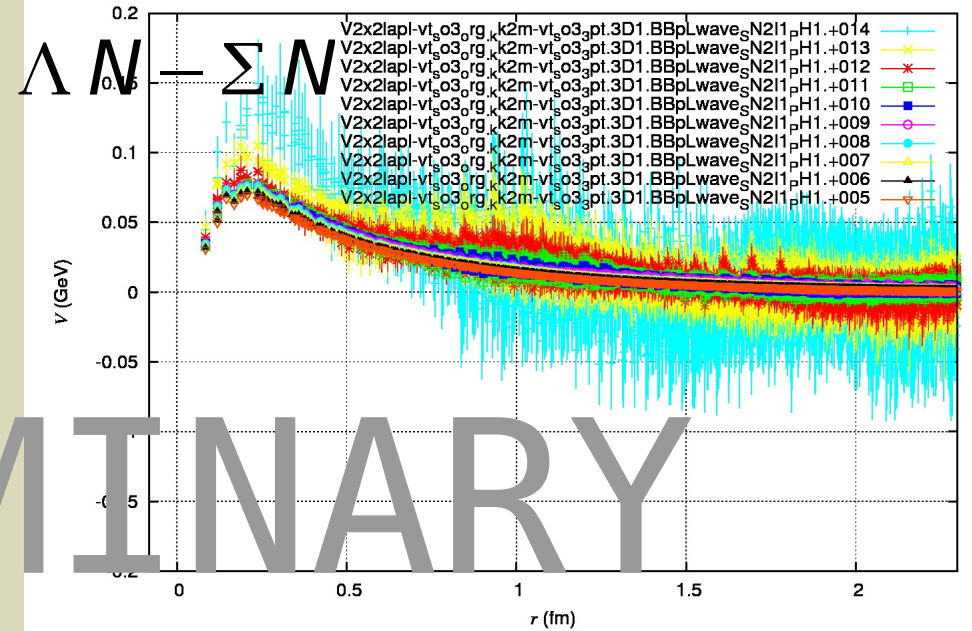
$$\left(\frac{\nabla^2}{2\mu} - \frac{\partial}{\partial t}\right) R(\vec{r}, t) = \int d^3r' U(\vec{r}, \vec{r}') R(\vec{r}', t) + O(k^4) = V_{LO}(\vec{r}) R(\vec{r}, t) + \dots \quad (8)$$

$$V_T({}^3S_1 - {}^3D_1)$$

V2x2lapi-vt<sub>s</sub>o<sub>3</sub>rg\_v2x2kk2m-vt<sub>s</sub>o<sub>3</sub>pt.3D1.BBpLwave<sub>p</sub>LpH1

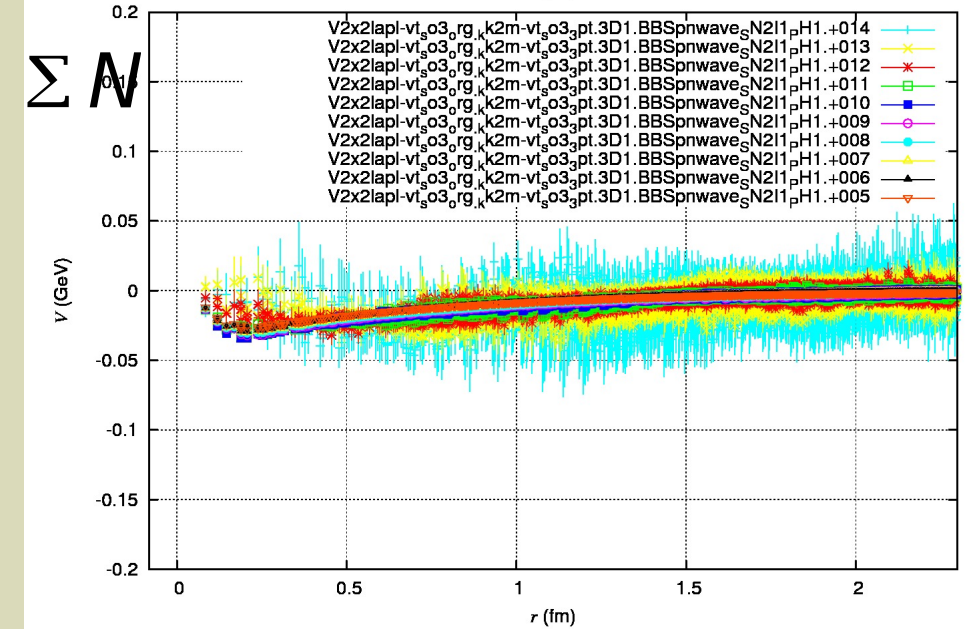
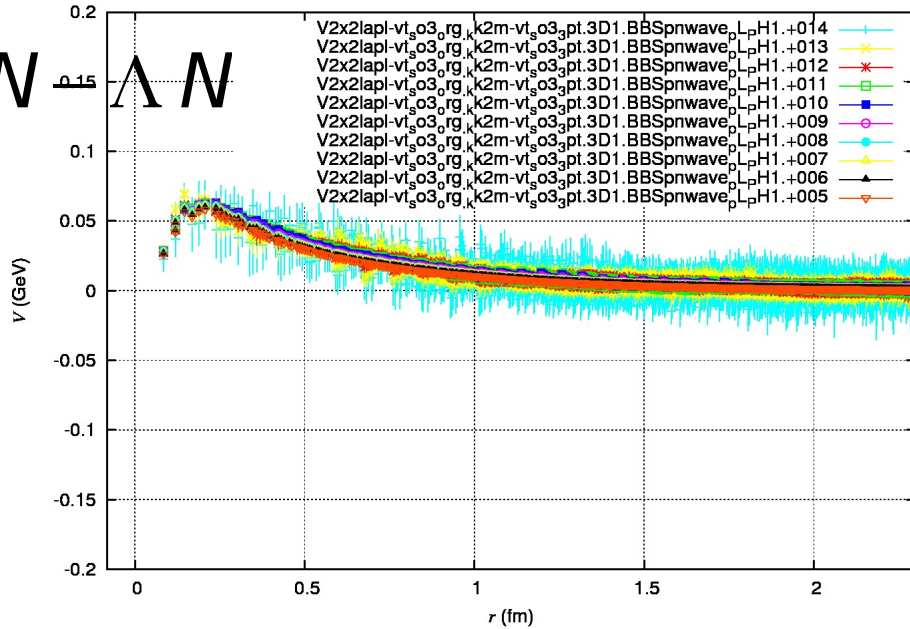


V2x2lapi-vt<sub>s</sub>o<sub>3</sub>rg\_v2x2kk2m-vt<sub>s</sub>o<sub>3</sub>pt.3D1.BBpLwave<sub>s</sub>N211pH1



PRELIMINARY

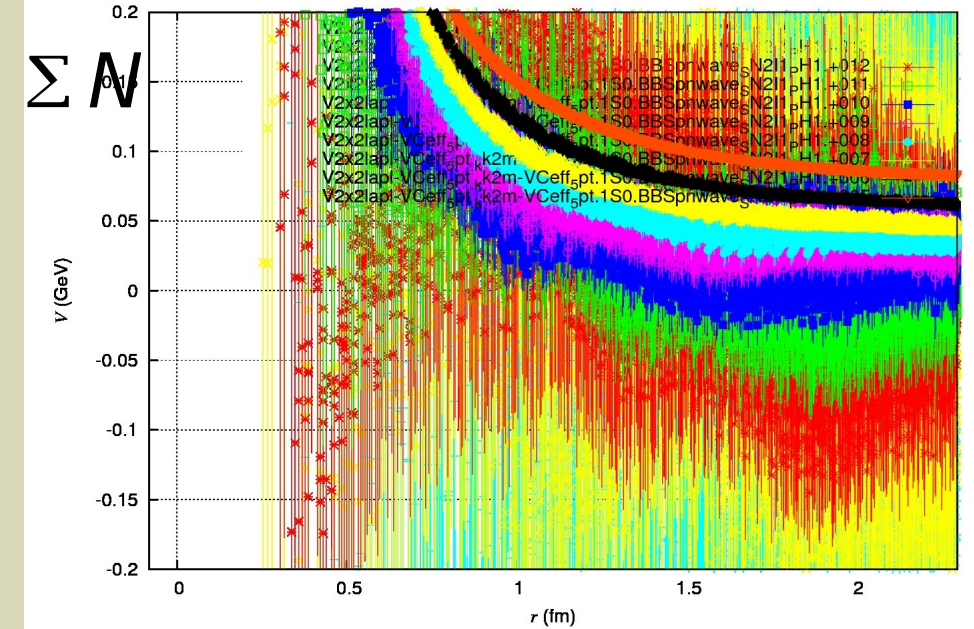
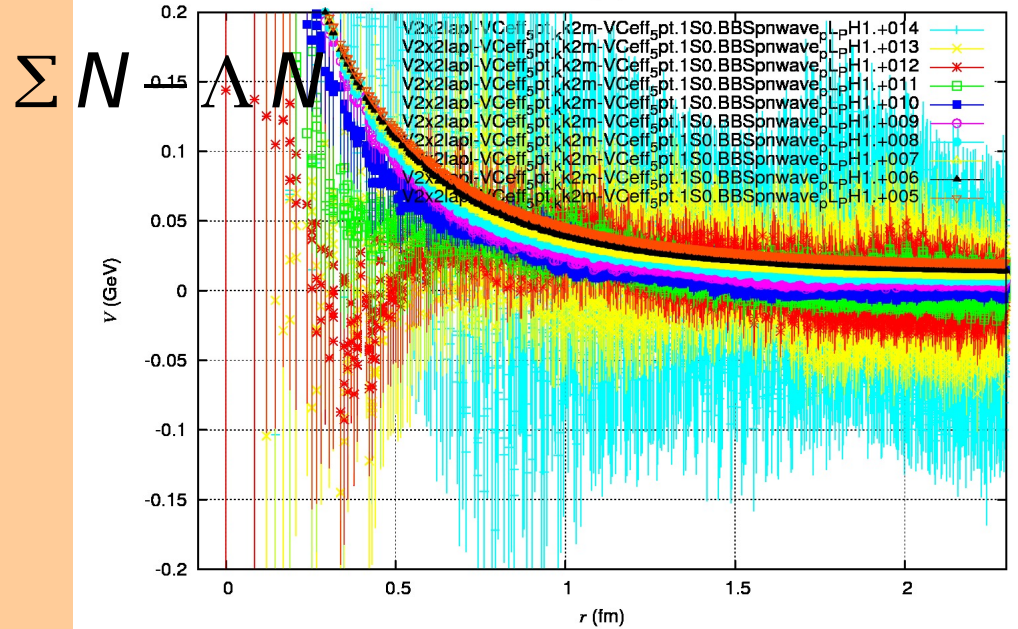
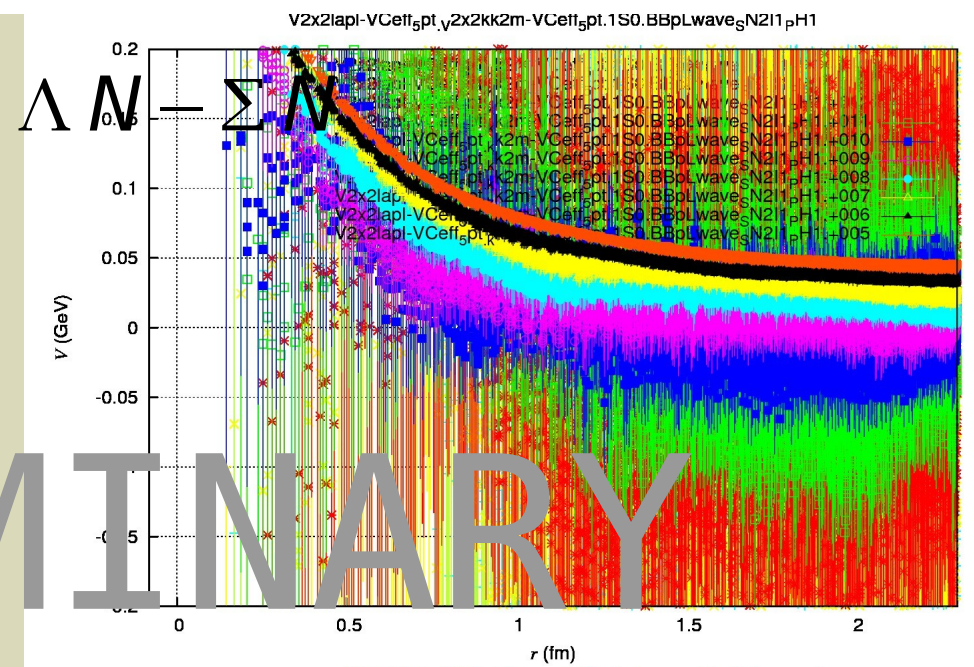
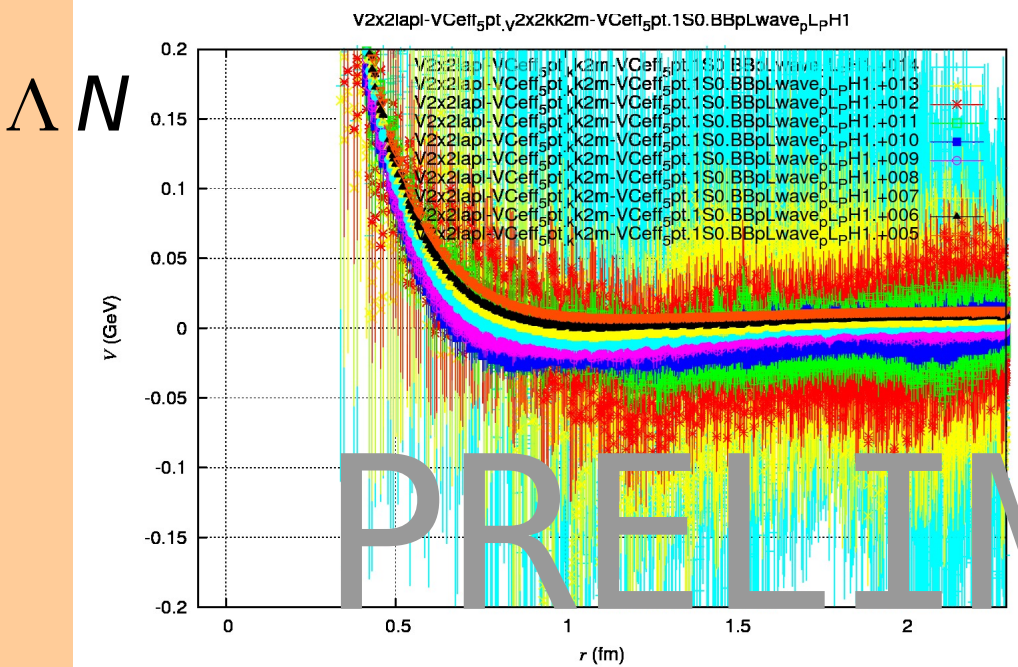
$\Sigma N$   $\Lambda N$



# Very preliminary result of LN potential at the physical point

$$V_C({}^1S_0)$$

$$\left(\frac{\nabla^2}{2\mu} - \frac{\partial}{\partial t}\right) R(\vec{r}, t) = \int d^3r' U(\vec{r}, \vec{r}') R(\vec{r}', t) + O(k^4) = V_{LO}(\vec{r}) R(\vec{r}, t) + \dots \quad (8)$$



PRELIMINARY

# Effective block algorithm for various baryon-baryon correlators

HN, CPC207,91(2016), arXiv:1510.00903(hep-lat)

Numerical cost (# of iterative operations) in this algorithm

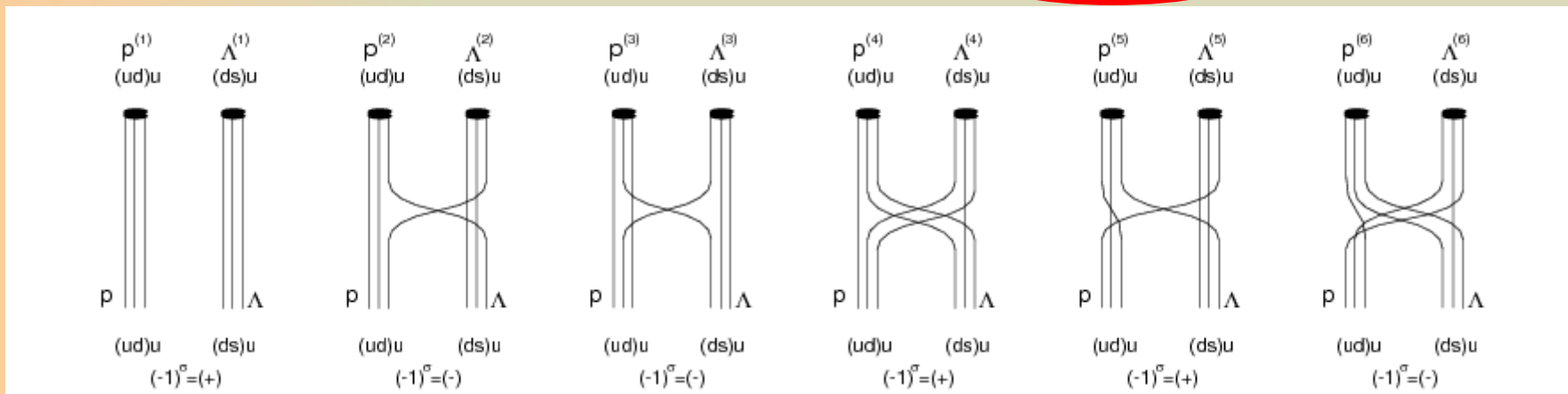
$$1 + N_c^2 + N_c^2 N_\alpha^2 + N_c^2 N_\alpha^2 + N_c^2 N_\alpha + N_c^2 N_\alpha = 370$$

In an intermediate step:

$$(N_c! N_\alpha)^B \times N_u! N_d! N_s! \times 2^{N_\Lambda + N_{\Sigma^0} - B} = 3456$$

In a naïve approach:

$$(N_c! N_\alpha)^{2B} \times N_u! N_d! N_s! = 3,981,312$$



# Generalization to the various baryon-baryon channels strangeness S=0 to -4 systems

$$\langle pn\bar{p}\bar{n} \rangle, \quad (4.1)$$

$$\begin{aligned} &\langle p\Lambda\bar{p}\bar{\Lambda} \rangle, \quad \langle p\Lambda\bar{\Sigma}^+n \rangle, \quad \langle p\Lambda\bar{\Sigma}^0p \rangle, \\ &\langle \Sigma^+n\bar{p}\bar{\Lambda} \rangle, \quad \langle \Sigma^+n\bar{\Sigma}^+n \rangle, \quad \langle \Sigma^+n\bar{\Sigma}^0p \rangle, \\ &\langle \Sigma^0p\bar{p}\bar{\Lambda} \rangle, \quad \langle \Sigma^0p\bar{\Sigma}^+n \rangle, \quad \langle \Sigma^0p\bar{\Sigma}^0p \rangle, \end{aligned} \quad (4.2)$$

$$\begin{aligned} &\langle \Lambda\Lambda\bar{\Lambda}\bar{\Lambda} \rangle, \quad \langle \Lambda\Lambda\bar{p}\bar{\Xi}^- \rangle, \quad \langle \Lambda\Lambda\bar{n}\bar{\Xi}^0 \rangle, \quad \langle \Lambda\Lambda\bar{\Sigma}^+\bar{\Sigma}^- \rangle, \quad \langle \Lambda\Lambda\bar{\Sigma}^0\bar{\Sigma}^0 \rangle, \\ &\langle p\bar{\Xi}^- \bar{\Lambda}\bar{\Lambda} \rangle, \quad \langle p\bar{\Xi}^- \bar{p}\bar{\Xi}^- \rangle, \quad \langle p\bar{\Xi}^- \bar{n}\bar{\Xi}^0 \rangle, \quad \langle p\bar{\Xi}^- \bar{\Sigma}^+\bar{\Sigma}^- \rangle, \quad \langle p\bar{\Xi}^- \bar{\Sigma}^0\bar{\Sigma}^0 \rangle, \quad \langle p\bar{\Xi}^- \bar{\Sigma}^0\bar{\Lambda} \rangle, \\ &\langle n\bar{\Xi}^0 \bar{\Lambda}\bar{\Lambda} \rangle, \quad \langle n\bar{\Xi}^0 \bar{p}\bar{\Xi}^- \rangle, \quad \langle n\bar{\Xi}^0 \bar{n}\bar{\Xi}^0 \rangle, \quad \langle n\bar{\Xi}^0 \bar{\Sigma}^+\bar{\Sigma}^- \rangle, \quad \langle n\bar{\Xi}^0 \bar{\Sigma}^0\bar{\Sigma}^0 \rangle, \quad \langle n\bar{\Xi}^0 \bar{\Sigma}^0\bar{\Lambda} \rangle, \\ &\langle \Sigma^+\bar{\Sigma}^- \bar{\Lambda}\bar{\Lambda} \rangle, \quad \langle \Sigma^+\bar{\Sigma}^- \bar{p}\bar{\Xi}^- \rangle, \quad \langle \Sigma^+\bar{\Sigma}^- \bar{n}\bar{\Xi}^0 \rangle, \quad \langle \Sigma^+\bar{\Sigma}^- \bar{\Sigma}^+\bar{\Sigma}^- \rangle, \quad \langle \Sigma^+\bar{\Sigma}^- \bar{\Sigma}^0\bar{\Sigma}^0 \rangle, \quad \langle \Sigma^+\bar{\Sigma}^- \bar{\Sigma}^0\bar{\Lambda} \rangle, \\ &\langle \Sigma^0\bar{\Sigma}^0 \bar{\Lambda}\bar{\Lambda} \rangle, \quad \langle \Sigma^0\bar{\Sigma}^0 \bar{p}\bar{\Xi}^- \rangle, \quad \langle \Sigma^0\bar{\Sigma}^0 \bar{n}\bar{\Xi}^0 \rangle, \quad \langle \Sigma^0\bar{\Sigma}^0 \bar{\Sigma}^+\bar{\Sigma}^- \rangle, \quad \langle \Sigma^0\bar{\Sigma}^0 \bar{\Sigma}^0\bar{\Sigma}^0 \rangle, \\ &\quad \langle \Sigma^0\bar{\Lambda}\bar{p}\bar{\Xi}^- \rangle, \quad \langle \Sigma^0\bar{\Lambda}\bar{n}\bar{\Xi}^0 \rangle, \quad \langle \Sigma^0\bar{\Lambda}\bar{\Sigma}^+\bar{\Sigma}^- \rangle, \quad \langle \Sigma^0\bar{\Lambda}\bar{\Sigma}^0\bar{\Lambda} \rangle, \end{aligned} \quad (4.3)$$

$$\begin{aligned} &\langle \Xi^- \bar{\Lambda}\bar{\Xi}^- \bar{\Lambda} \rangle, \quad \langle \Xi^- \bar{\Lambda}\bar{\Sigma}^- \bar{\Xi}^0 \rangle, \quad \langle \Xi^- \bar{\Lambda}\bar{\Sigma}^0 \bar{\Xi}^- \rangle, \\ &\langle \Sigma^- \bar{\Xi}^0 \bar{\Xi}^- \bar{\Lambda} \rangle, \quad \langle \Sigma^- \bar{\Xi}^0 \bar{\Sigma}^- \bar{\Xi}^0 \rangle, \quad \langle \Sigma^- \bar{\Xi}^0 \bar{\Sigma}^0 \bar{\Xi}^- \rangle, \\ &\langle \Sigma^0 \bar{\Xi}^- \bar{\Xi}^- \bar{\Lambda} \rangle, \quad \langle \Sigma^0 \bar{\Xi}^- \bar{\Sigma}^- \bar{\Xi}^0 \rangle, \quad \langle \Sigma^0 \bar{\Xi}^- \bar{\Sigma}^0 \bar{\Xi}^- \rangle, \end{aligned} \quad (4.4)$$

$$\langle \Xi^- \bar{\Xi}^0 \bar{\Xi}^- \bar{\Xi}^0 \rangle. \quad (4.5)$$

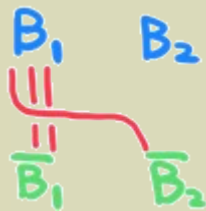
**Make better use of the computing resources!**

HN, CPC **207**, 91(2016) [arXiv:1510.00903[hep-lat]],  
(See also arXiv:1604.08346)

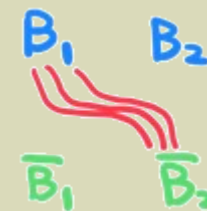
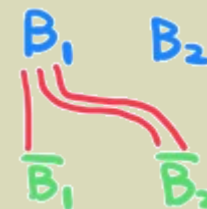
# Classification of baryon blocks in the effective block algorithm

- ⊗ The number of declared blocks in terms of quark propagation form, i.e., from  $[111]$  to  $[222]$ , in the simultaneous calculation of 4pt correlators from NN to  $\Xi\Xi$

⊗ Proton:	18+	0+	31+	0+106+	16+121+	12 = 304
⊗ $\Sigma^+$ :	3+	0+	10+	0+ 52+	3+ 55+	1 = 124
⊗ $\Xi^0$ :	16+	19+	0+	0+118+102+	29+ 14 = 298	
⊗ $\Lambda(\text{dsu})$ :	242+318+436+408+290+266+376+248 = 2584					
⊗ $\Lambda(\text{sud})$ :	94+164+102+132+130+164+102+ 96 = 984					
⊗ $\Lambda(\text{uds})$ :	94+102+130+102+164+132+164+ 96 = 984					



...



# Summary

(I-1) LN potentials (central, tensor) at  $(m_\pi, m_K) \approx (145, 525)\text{MeV}$ .

phase shifts below the SN threshold

Both channels are attractive. (but weaker than empirical values)

Spin dependence is very weak. Relatively large statistical uncertainty.

(I-2) Effective block algorithm for the various baryon-baryon interaction

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Simultaneous calcs (NN to XiXi) is the point we have to take into account for the comprehensive perspective as well as energy-computing-resource efficiency.

The algorithm will be applied to more wide range problems.



Future work:

(II-1) Physical quantities including the binding energies of **few-body problem of light hypernuclei with the lattice YN (and NN) potentials**

(II-2) **New application of effective baryon block algorithm for the various baryon-baryon interaction from NN to  $\Xi\Xi$ .**

> **Classification of baryon blocks from NN to  $\Xi\Xi$ , which comprises 52 4pt-correlators (2639 diagrams)**

> In search of a better approach to conducting lattice nuclear physics.

> Spin-orbit force.