



東北大学

重陽子一陽子弾性散乱測定 による三体力の研究

東北大学大学院理学研究科

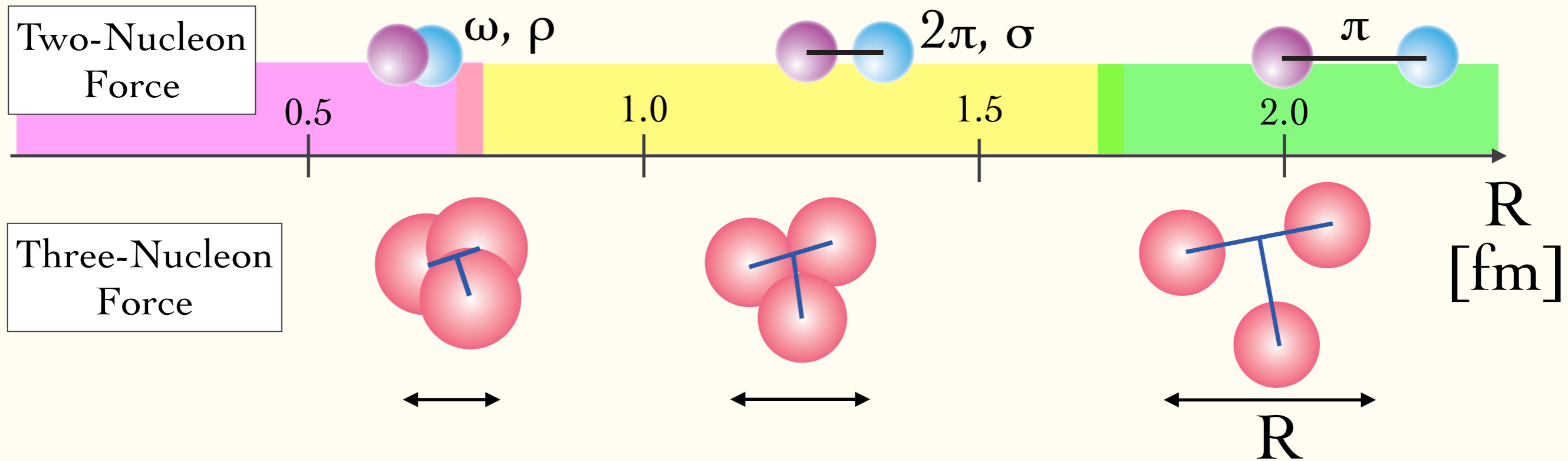
関口仁子

原子核の **力** - 2 & 3 Nucleon Force -

①. Repulsive
-Short Range-

②. Attractive (strong)
-Intermediate Range-

③. Attractive (weak)
- Long Range -



3NF は 2NF と同様に距離, スピン, 荷電スピン依存

Nuclear Matter
Neutron Star

Nuclear Structure

Deuteron-Proton (dp) Scattering

a good probe to study the dynamical aspects of 3NFs.

- ✓ Momentum dependence
- ✓ Spin & Iso-spin dependence

Direct Comparison between Theory and Experiment

• Theory : **Faddeev Calculations**

Rigorous Numerical Calculations of 3, 4N System

2NF Input

- CDBonn
- Argonne V18 (AV18)
- Nijmegen I, II, 93

3NF Input

- Tucson-Melbourne
- Urbana IX
- etc..

2NF & 3NF Input

- Chiral Effective Field Theory

• Experiment : **Precise Data**

- $d\sigma/d\Omega$, Spin Observables (A_p , K_{ij} , C_{ij})

Extract fundamental information of Nuclear Forces

Our interest is **Three-Nucleon Force (3NF)**.

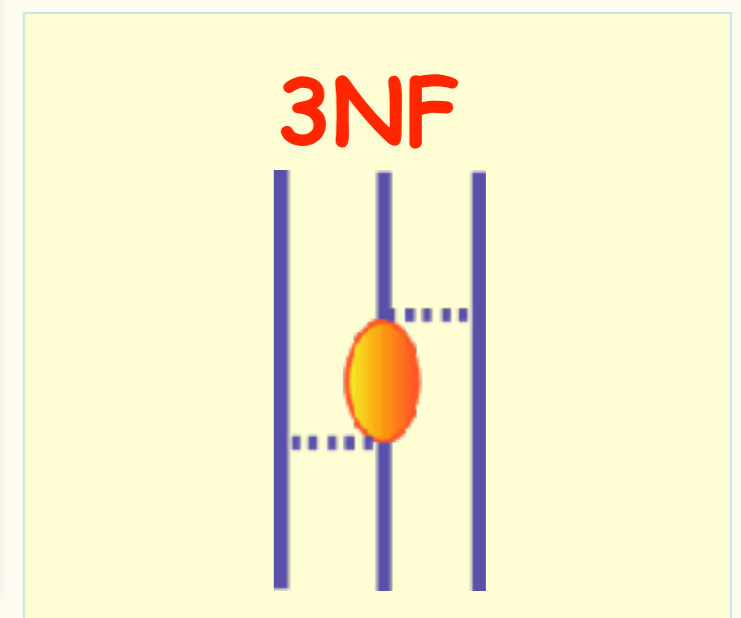
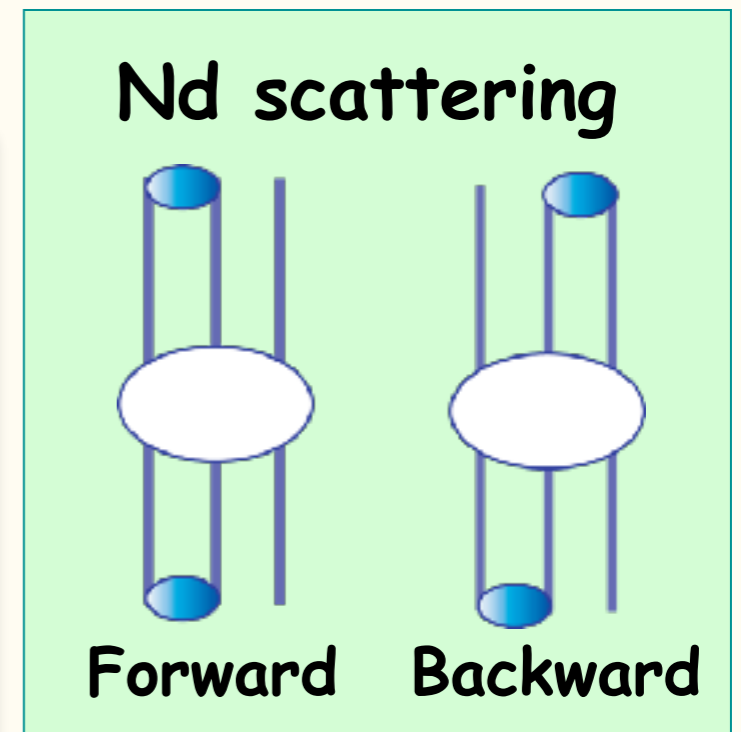
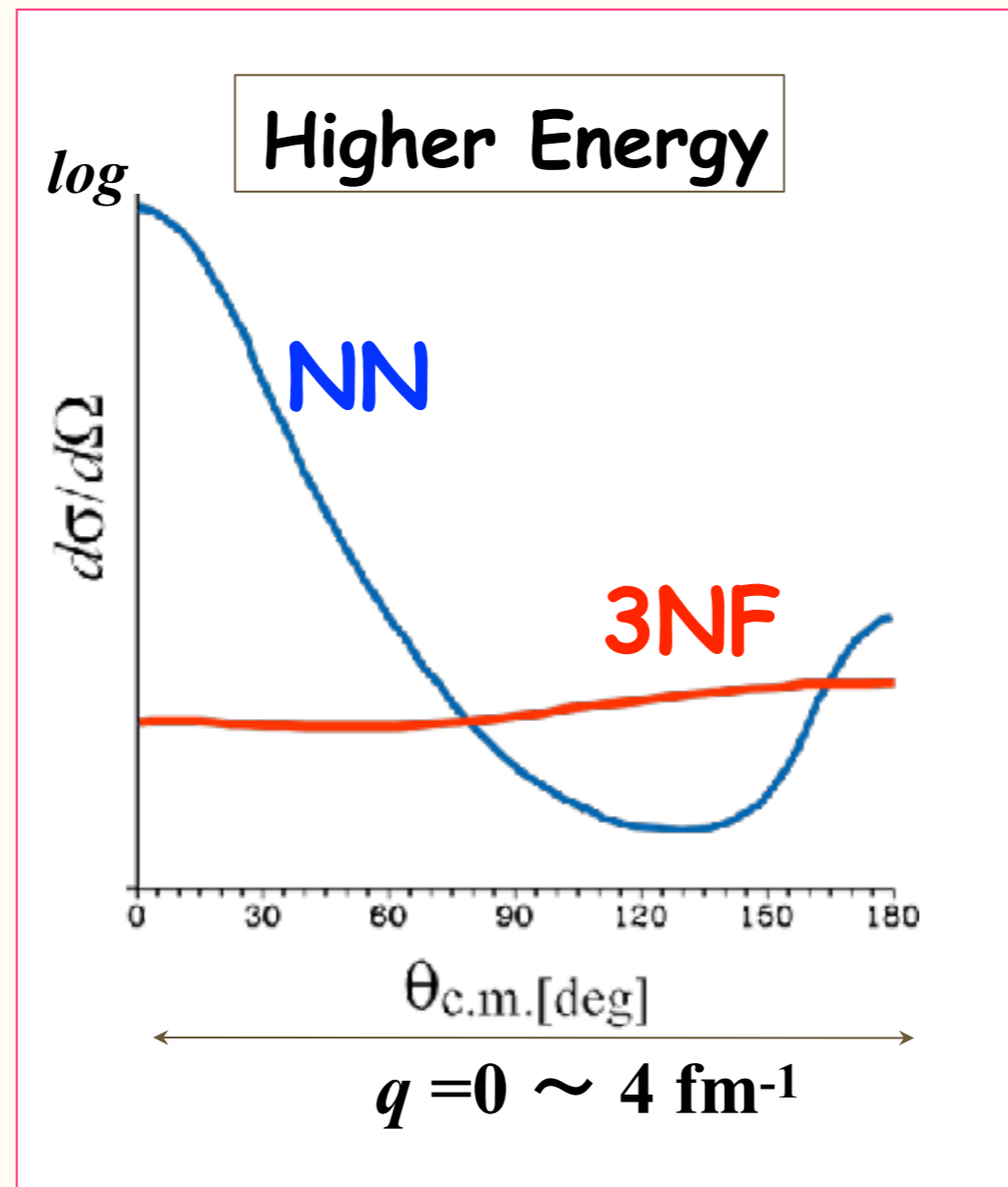
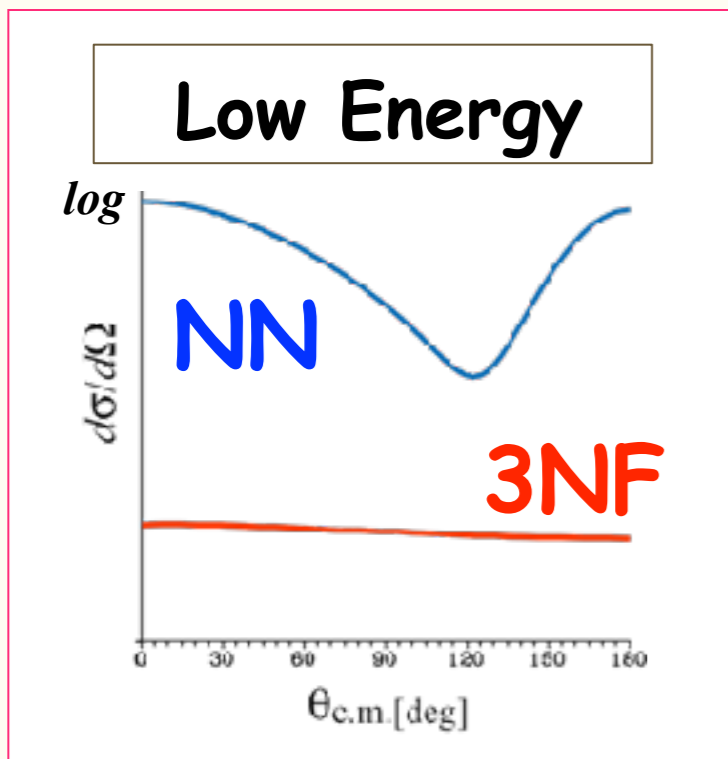
Where is the hot spot for study of 3NFs ?

Nucleon-Deuteron Scattering

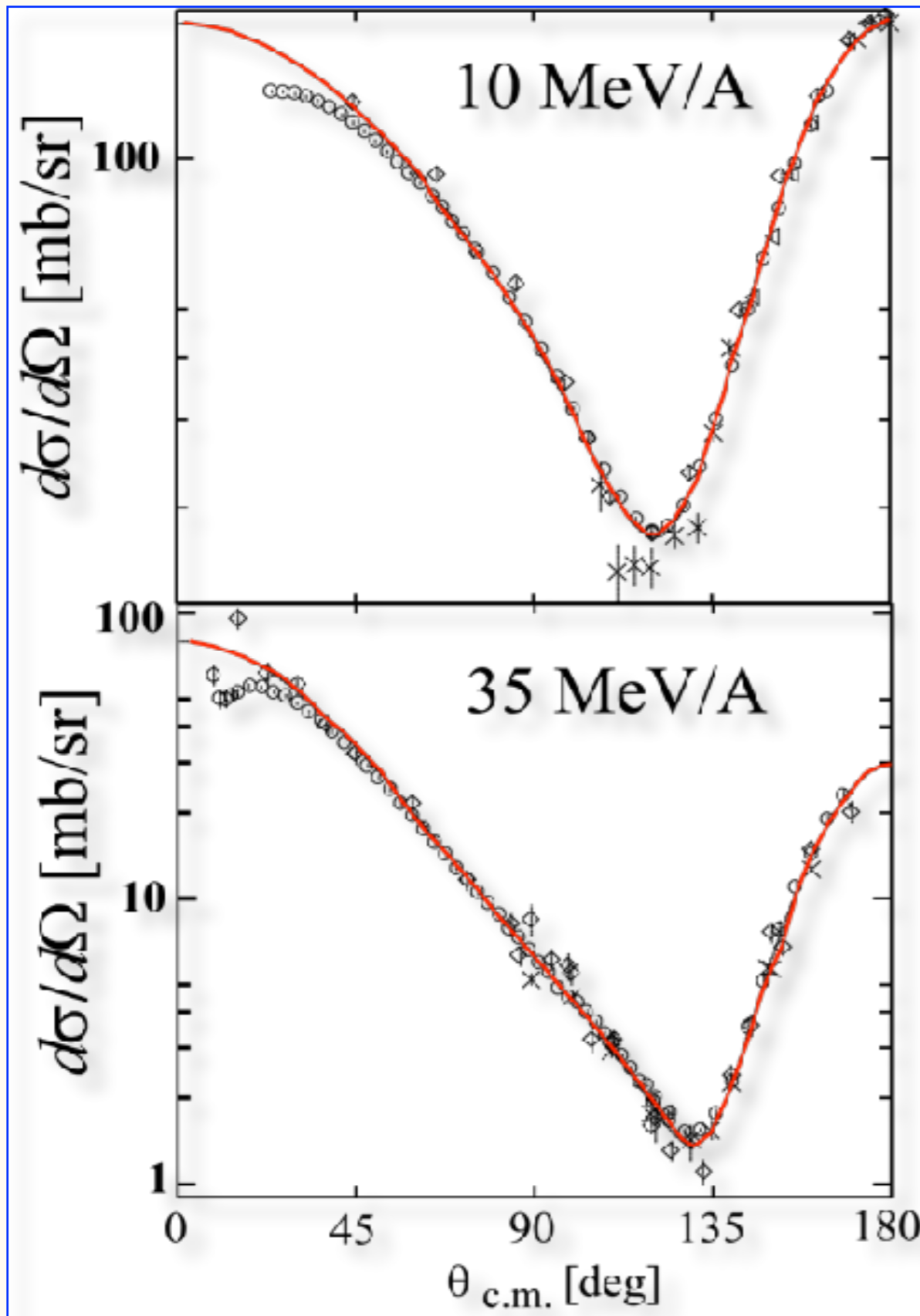
To study momentum & spin dependences
Iso-spin dependence : T=1/2 only

Predictions by H. Witala et al. (1998)

Cross Section minimum for Nd Scattering at ~ 100 MeV/nucleon



Nd Scattering at Low Energies ($E \leq 30$ MeV/A)



- ⊙ High precision data are explained by Faddeev calculations based on 2NF. (Exception : A_y, iT_{11})

No signatures of 3NF

Exp. Data from
Kyushu, TUNL, Cologne etc..

W. Glöckle et al., Phys. Rep. 274, 107 (1996).

Observables for Nd Scattering

• Differential Cross Section

- **Overall Strength**

- **Absolute Quantity** : normalization to pp or np data

$$\frac{d\sigma}{d\Omega} = \frac{\text{yields}}{(\text{target thickness}) \times (\text{beam charge}) \times (\text{solid angle}) \times (\text{efficiency})}$$

• Spin Observables :

- Analyzing Powers

- **Vector Analyzing Power** : iT_{11}

- **$(L \cdot S)$ interaction**

- **Tensor Analyzing Power** : T_{20}, T_{21}, T_{22}

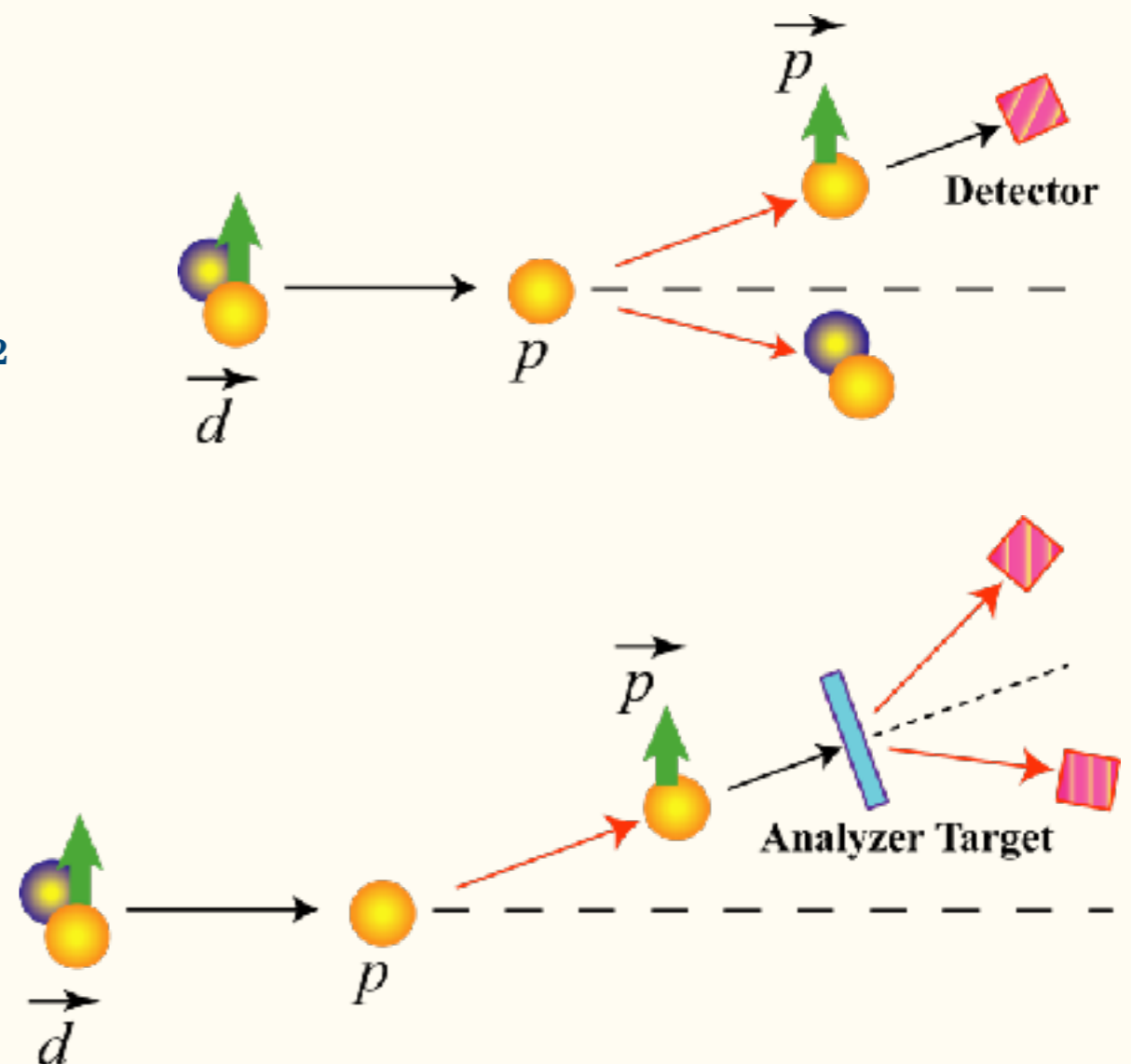
- **Tensor interaction (D-state)**

- **Higher order $(L \cdot S)$ interaction**

- **Polarization Transfer Coefficient** : K_{ij}^l

- **Spin Correlation Coefficients** : $C_{ij,k}$

- **Spin-Spin interaction**



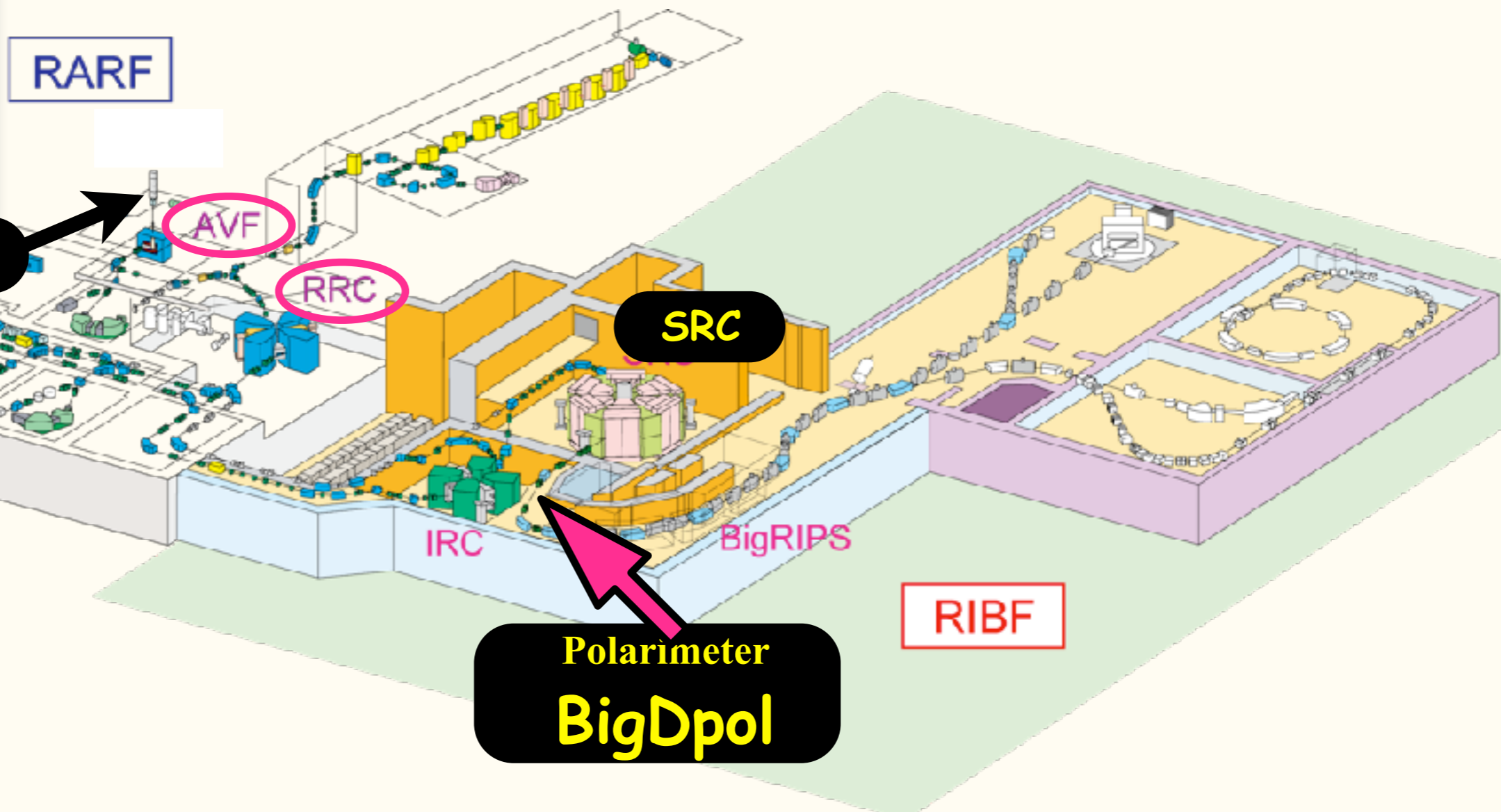
RIKEN RI Beam Factory (RIBF)

- Polarized d beam
 - acceleration by AVF+RRC : 65-135 MeV/nucleon
 - acceleration by AVF+RRC+SRC : 190-300 MeV/nucleon
 - polarization : 60-80% of theoretical maximum values
- Beam Intensity : < 100 nA

Spin axis of polarized d beams is freely controlled !



Polarized Ion Source



RARF

AVF

RRC

SRC

IRC

BigRIPS

RIBF

SMART
(-2005)

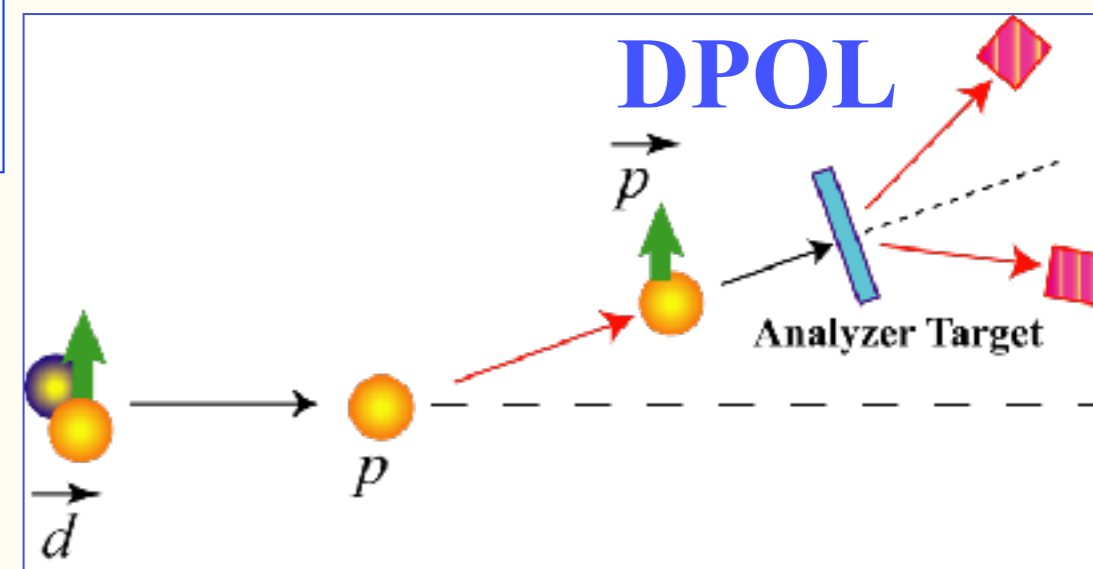
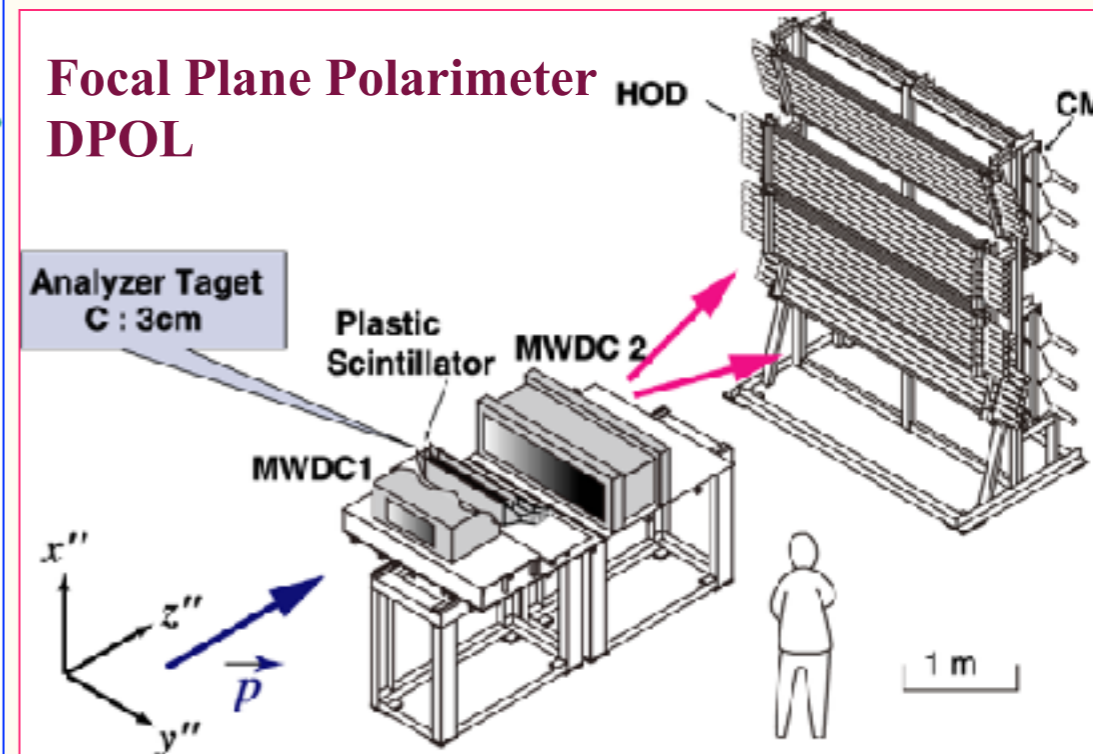
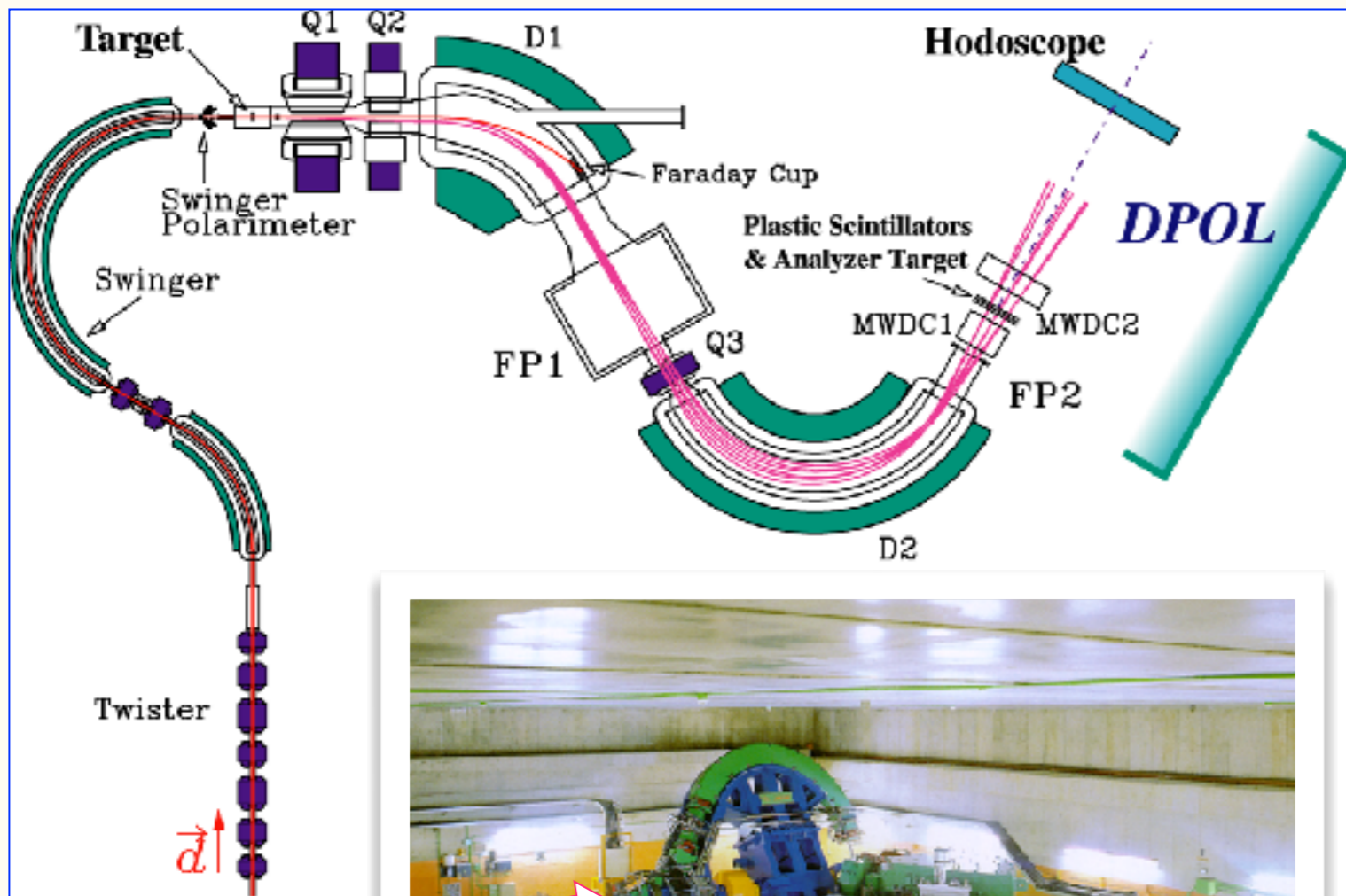
Polarimeter
BigDpol

SMART at RIKEN (- 2005)

Swinger and Magnetic Analyzer with Rotator and Twister

N. Nakamoto et al., *Phys. Lett. B* 367, 60 (1996),
 H. Sakai et al., *Phys. Rev. Lett.* 84, 5288 (2000),
 K. S. et al., *Phys. Rev. C* 65, 034003 (2002),
 K. S. et al., *Phys. Rev. C* 70, 014001 (2004),
 K. S. et al., *Phys. Rev. Lett.* 95, 162301 (2005),
 K. S. et al., *Phys. Rev. C* 79, 054008 (2009)

- ❖ Differential Cross Section at 70, 135 MeV/nucleon
- ❖ All Deuteron Analyzing Powers at 70, 100, 135 MeV/nucleon
- ❖ Deuteron to Proton Polarization Transfer Coefficients at 135 MeV/nucleon

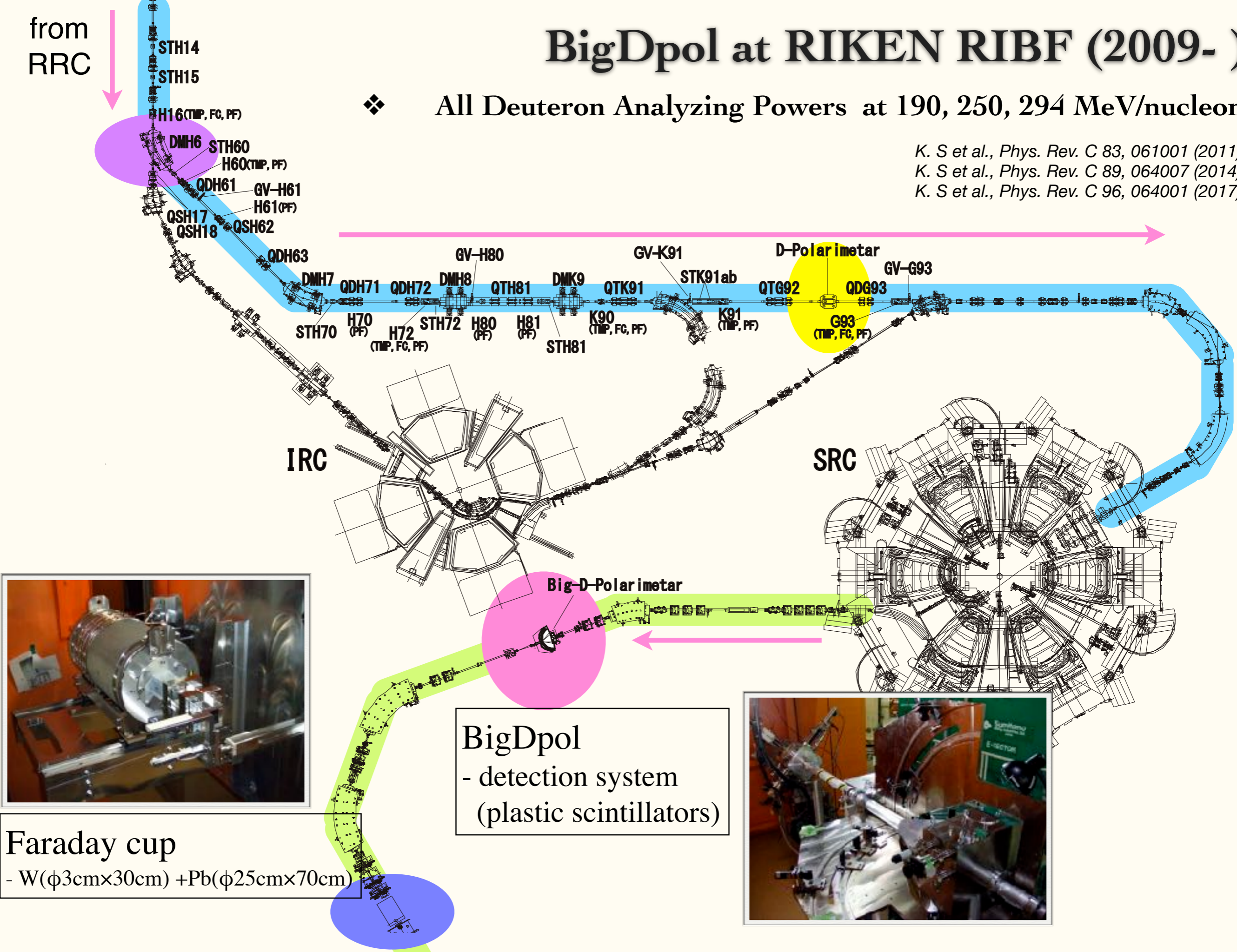


from RRC

BigDpol at RIKEN RIBF (2009-)

❖ All Deuteron Analyzing Powers at 190, 250, 294 MeV/nucleon

K. S et al., Phys. Rev. C 83, 061001 (2011)
K. S et al., Phys. Rev. C 89, 064007 (2014)
K. S et al., Phys. Rev. C 96, 064001 (2017)



IRC

SRC

Big-D-Polarimeter

BigDpol
- detection system
(plastic scintillators)

Faraday cup

- W($\phi 3\text{cm} \times 30\text{cm}$) + Pb($\phi 25\text{cm} \times 70\text{cm}$)



Nd Elastic Scattering Data at Intermediate Energies

pd and *nd* Elastic Scattering at 70–400 MeV/nucleon

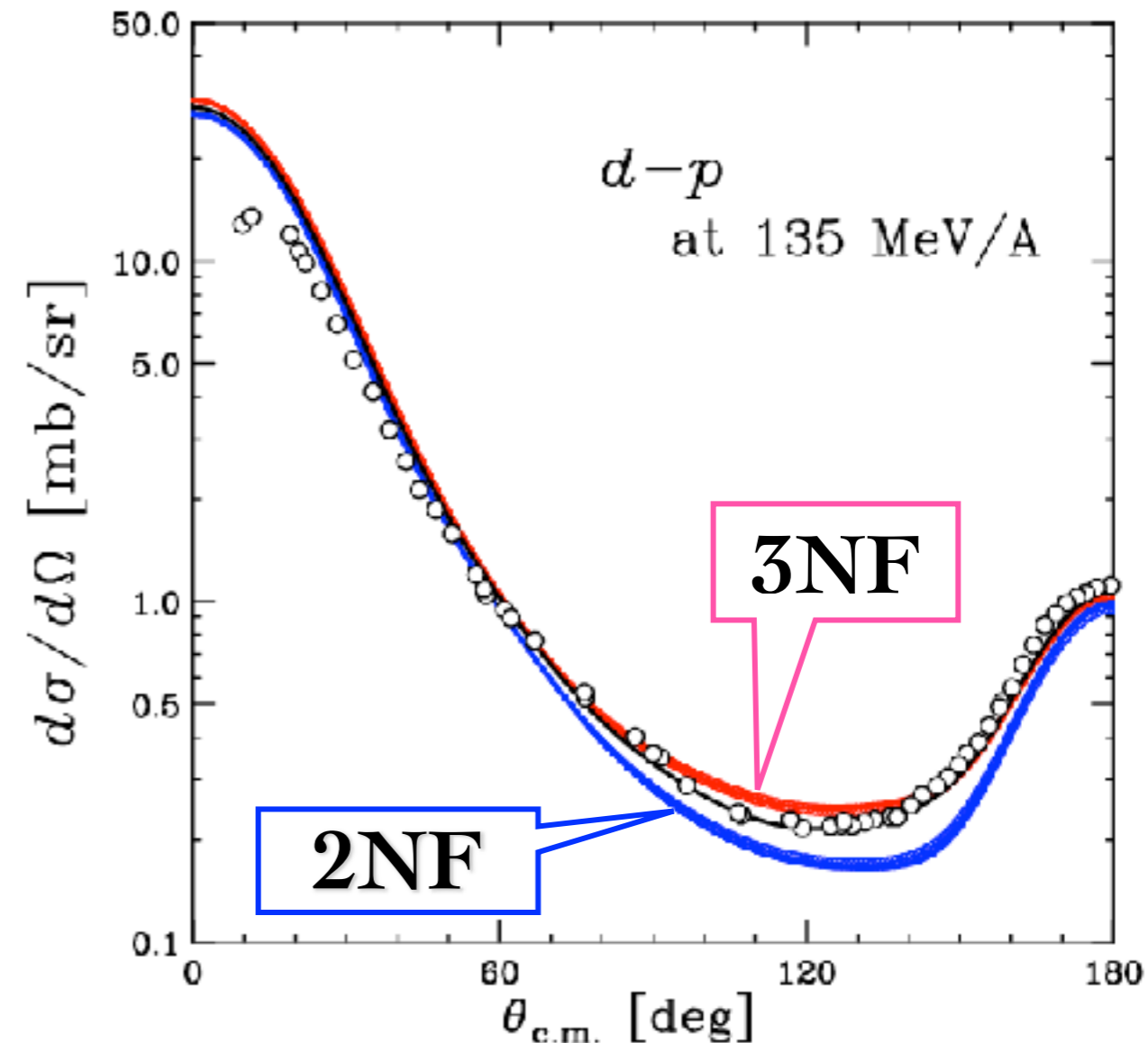
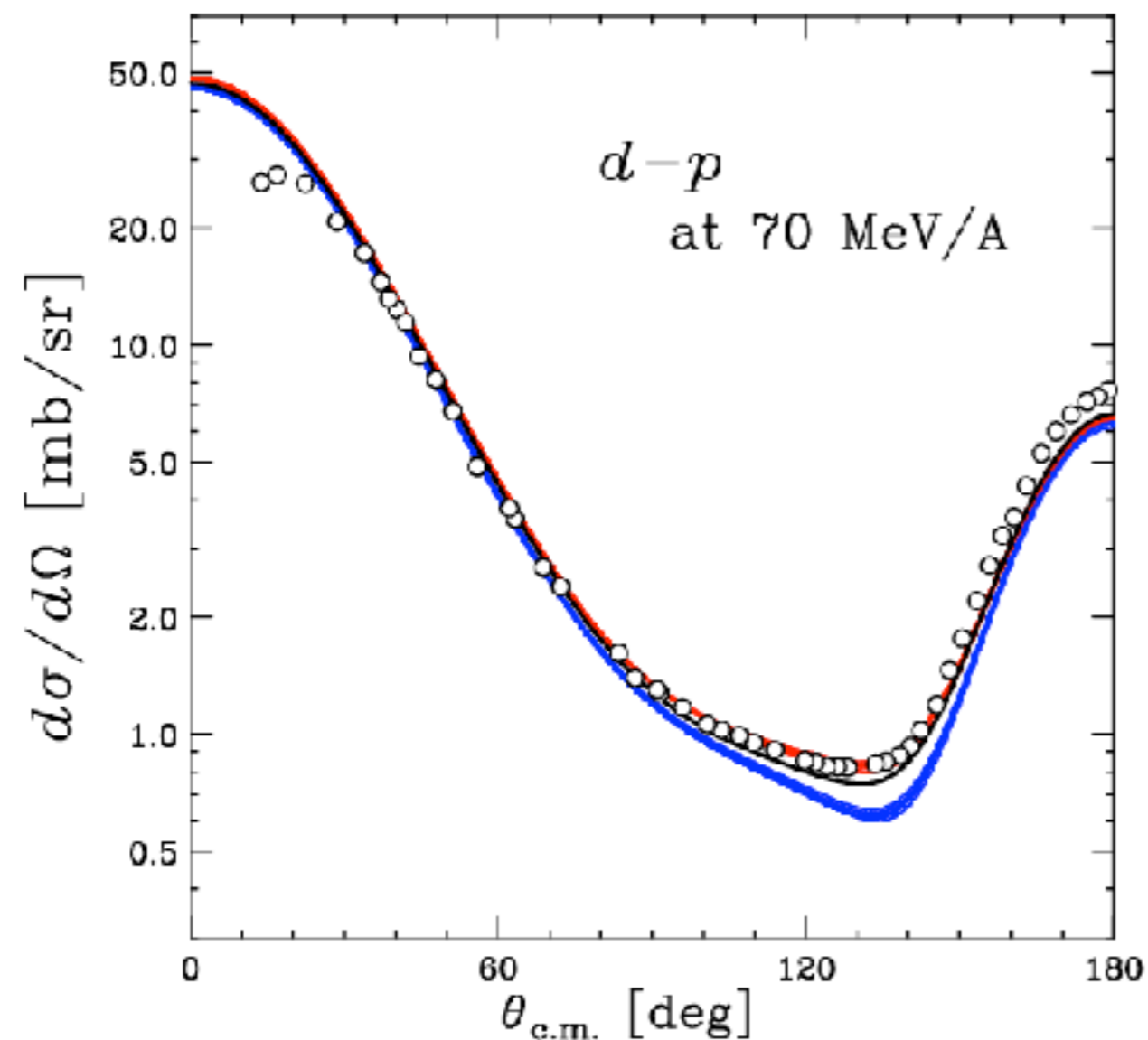
Observable	100	200	300	400
$\frac{d\sigma}{d\Omega}$	•	••••••••••	•	•
\vec{p} A_y^p \vec{n} A_y^n		••••••••••	•	•
\vec{d} iT_{11} T_{29} T_{22} T_{21}	••••••••••	••••••••••	••••••••••	•
$\vec{p} \rightarrow \vec{p}$ $K_y^{y'}$ $K_x^{x'}$ $K_x^{z'}$ $K_z^{x'}$ $K_z^{z'}$			••••••••••	
$\vec{d} \rightarrow \vec{p}$ $K_y^{y'}$ $K_{xx}^{y'}$ $K_{yy}^{y'}$ $K_{xz}^{y'}$	•	••••••••••		
$\vec{p} \rightarrow \vec{d}$ $K_y^{y'}$				•
$\vec{p}\vec{d}$ C_{ij} $C_{ij,k}$		••••••••••	••••••••••	

~2021

- High precision data set of $d\sigma/d\Omega$ & Analyzing Powers from RIKEN, RCNP, KVI, IUCF

- NN (CDBonn, AV18, Nijm I,II)
- TM'(99) 3NF +
NN(CD Bonn, AV18, Nijm I,II)
- Urbana IX 3NF+AV18

Calculations by Bochum-Cracow Gr.



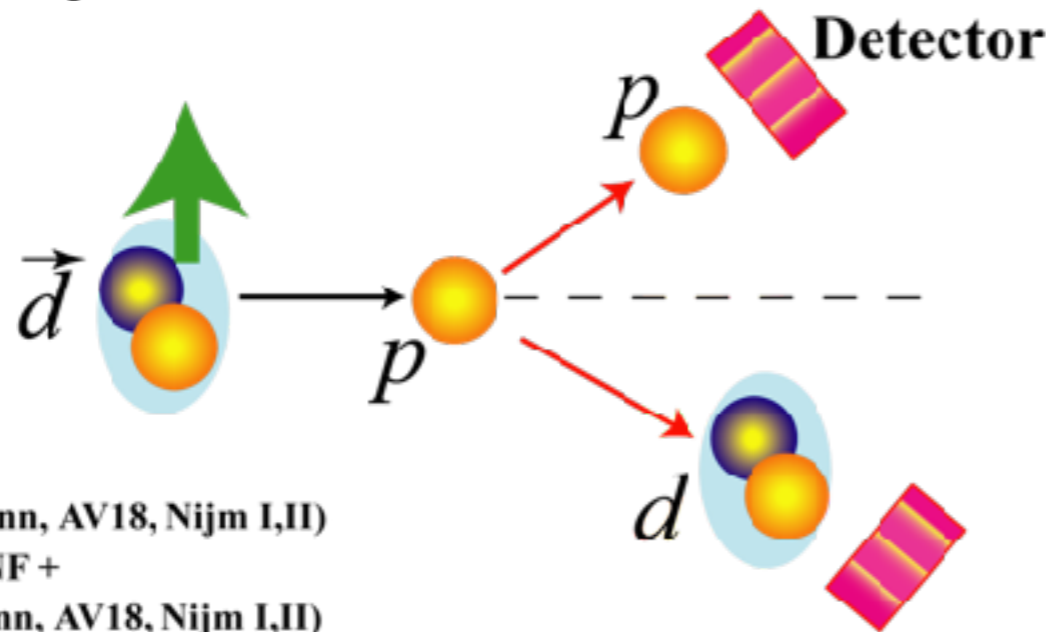
2NF (CDBonn, AV18, Nijmegen I,II)

: Large discrepancy in Cross Section Minimum ($\sim 30\%$)

2π -exchange 3NFs (Tucson-Melbourne, Urbana IX) : Good Agreement

: First Clear Signatures of 3NF effects in 3-Nucleon Scattering

Analyzing Powers



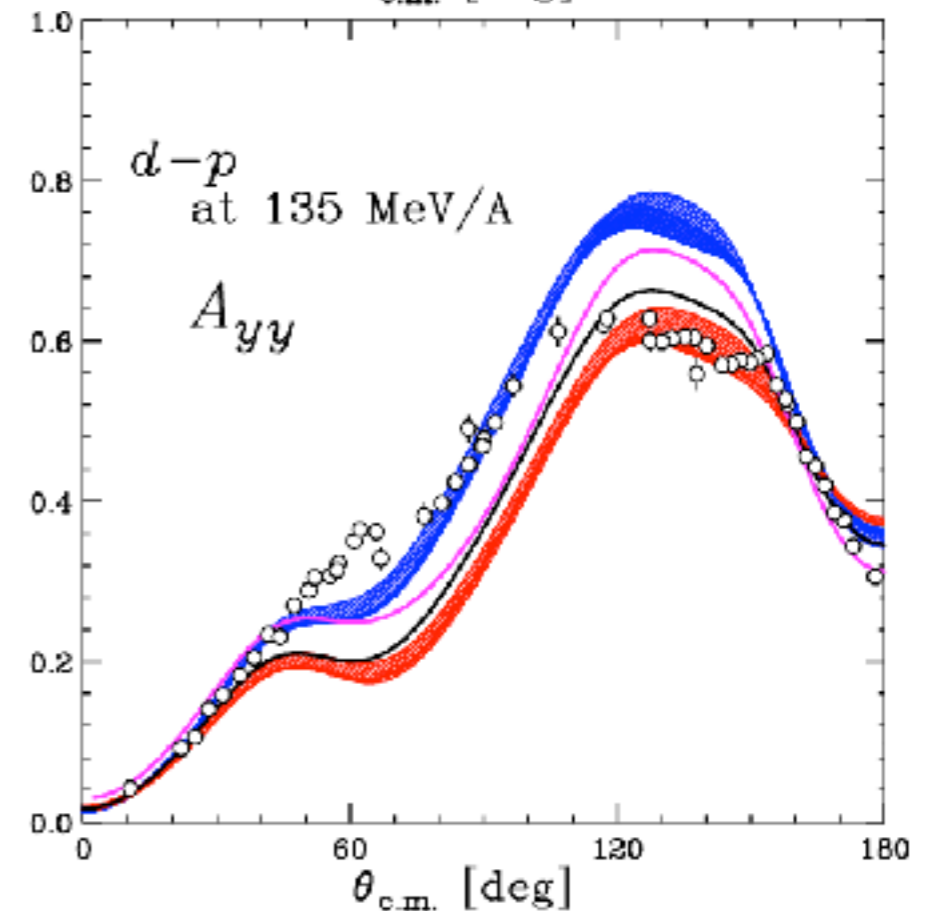
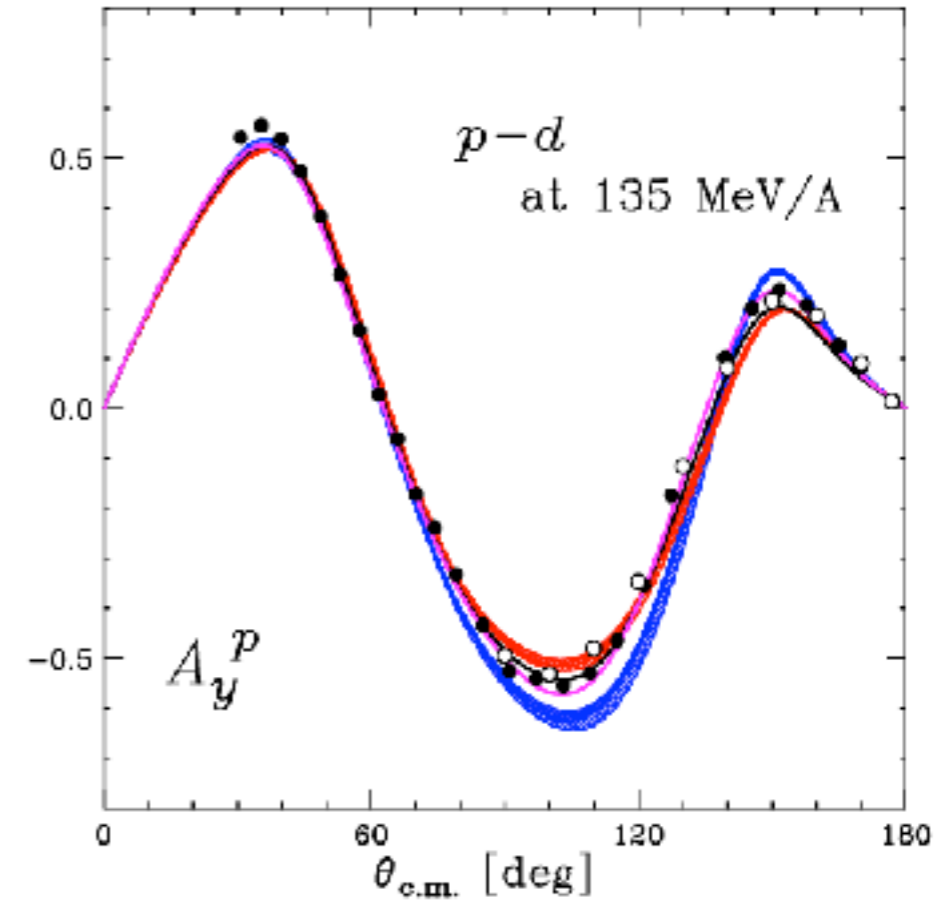
- █ NN (CDBonn, AV18, Nijm I,II)
- █ TM'(99) 3NF + NN(CD Bonn, AV18, Nijm I,II)
- █ with Urbana IX 3NF+AV18
- █ with Δ -isobar + CDBonn

2NF (CDBonn, AV18, Nijmegen I,II) :
Large discrepancy
in Cross Section Minimum

3NF (Tucson-Melbourne, Urbana IX, Δ -isobar) :

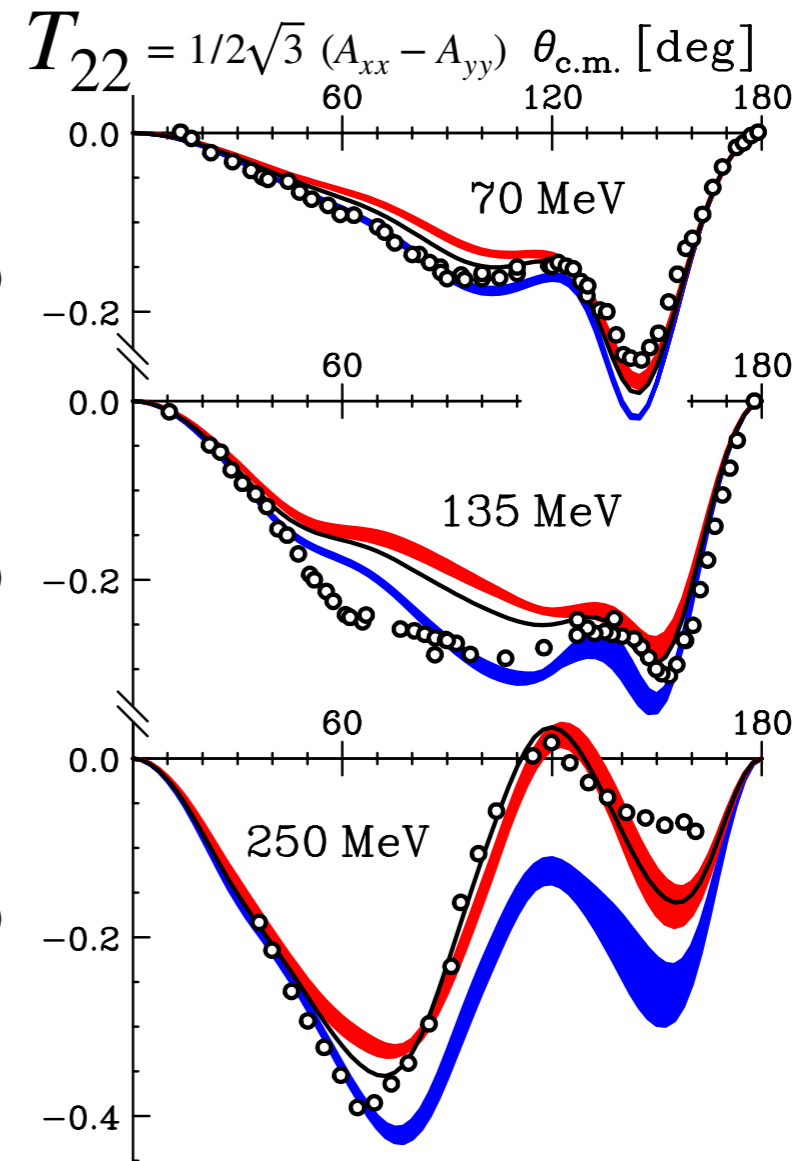
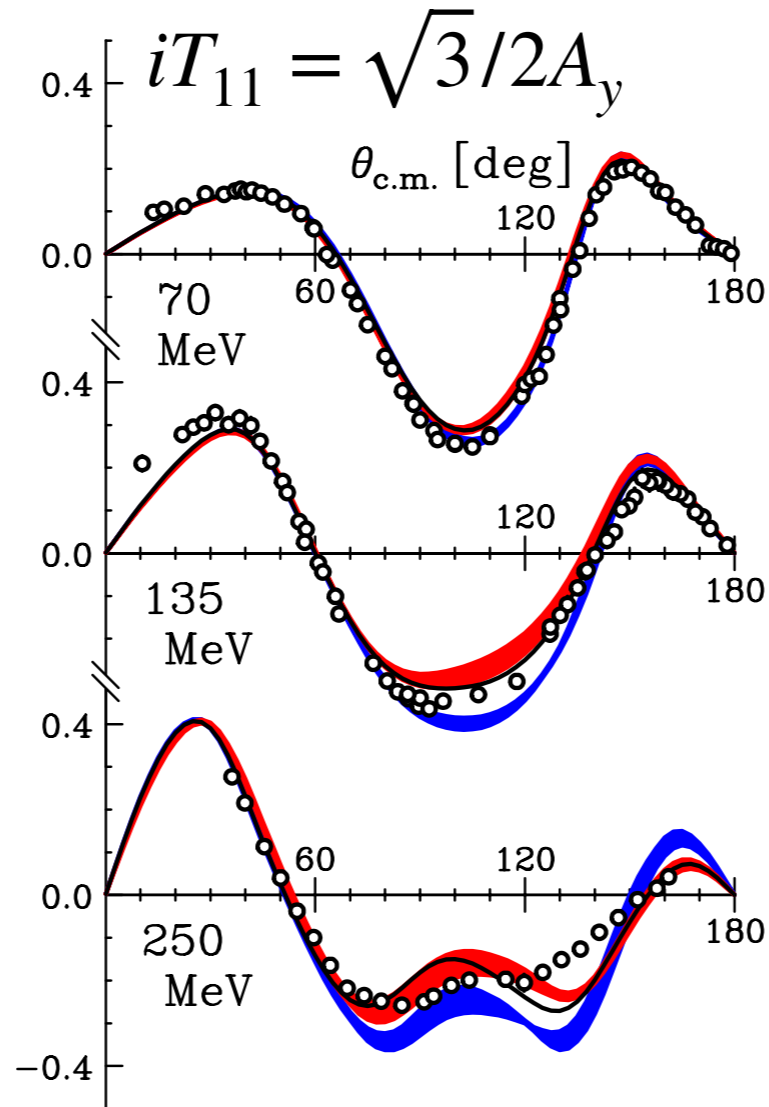
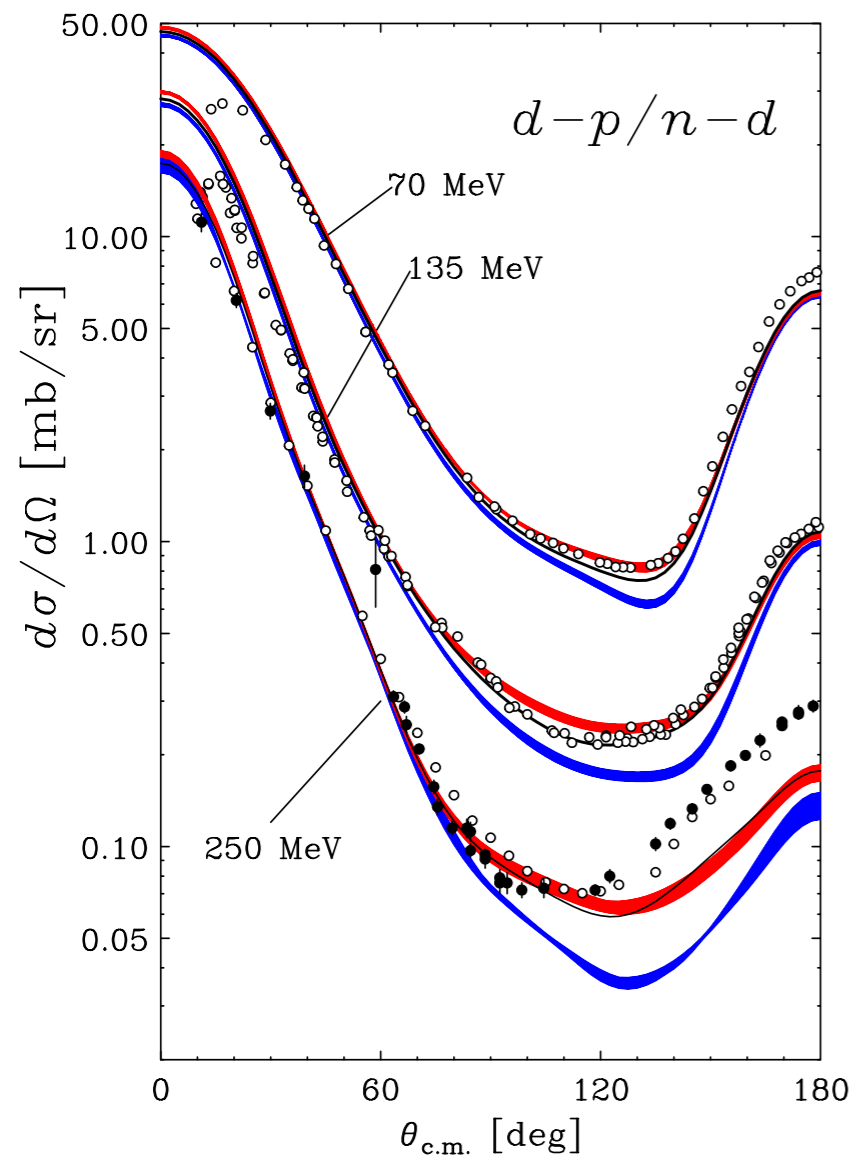
Vector Analyzing Power A_y^p
: Good Agreement

Tensor Analyzing Power A_{yy}
: No superiority



Energy Dependent Study for dp Scattering

- Cross Section & Analyzing Powers -



Serious discrepancies exist at very backward angles.

- NN (CDBonn, AV18, Nijm I,II)
- TM'(99) 3NF+
NN(CD Bonn, AV18, Nijm I,II)
- Urbana IX 3NF+AV18

Summary of Results of Comparison for dp elastic scattering

- Cross section at ~ 100 MeV/nucleon
 - First clear signature of 3NF effects in 3N scattering
 - Magnitudes of 3NFs is O.K. .

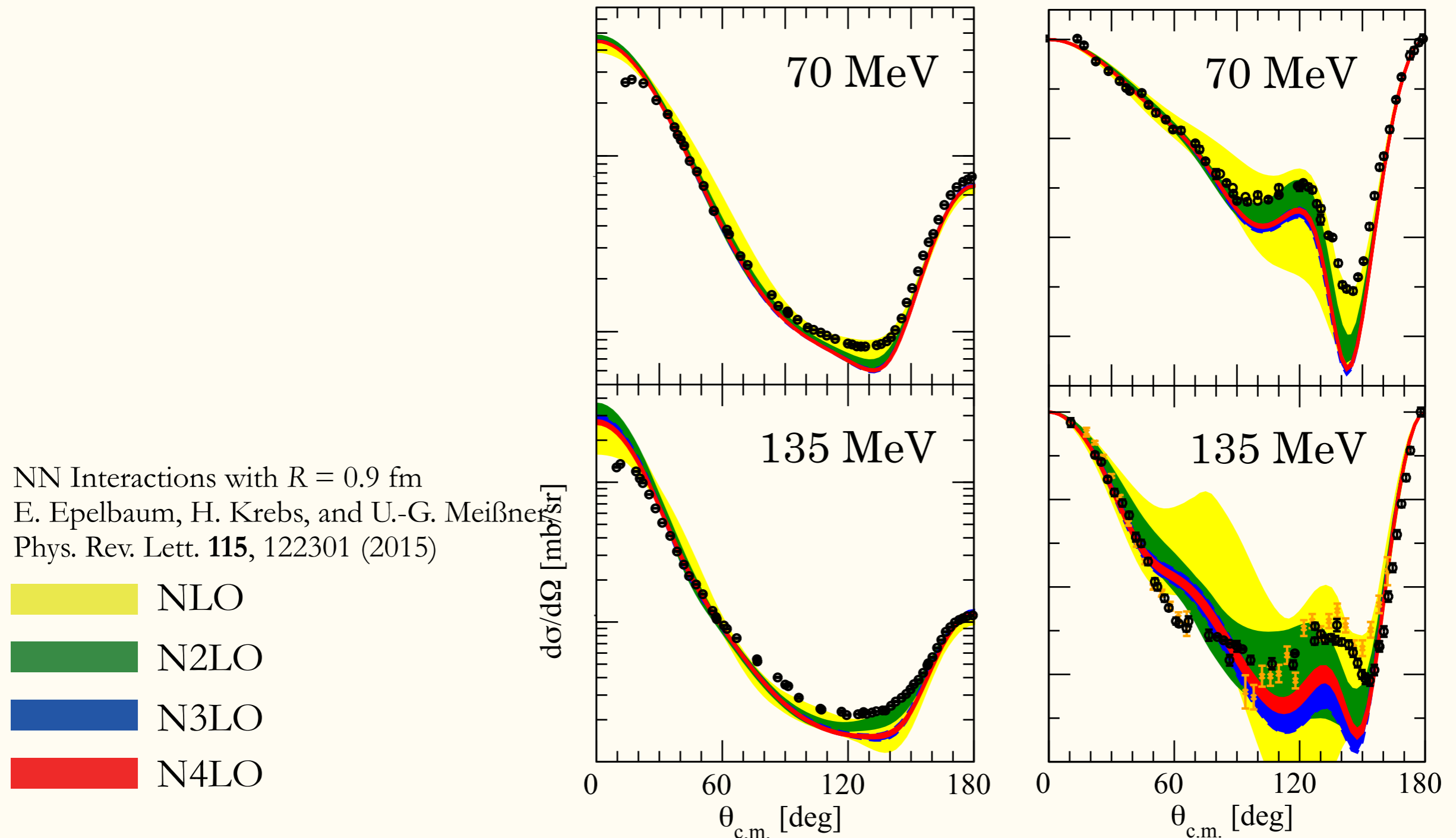
- Spin observables
 - Not always described by 2π -3NFs
 - Defects of spin-dependent parts of 3NFs

- At higher energies ...
 - Serious discrepancy at backward angles
 - Short Range 3NFs are required.

χ EFT & dp elastic scattering

- dp elastic scattering data are not explained by N4LO NN potentials.

PHYSICAL REVIEW C **96**, 064001 (2017)

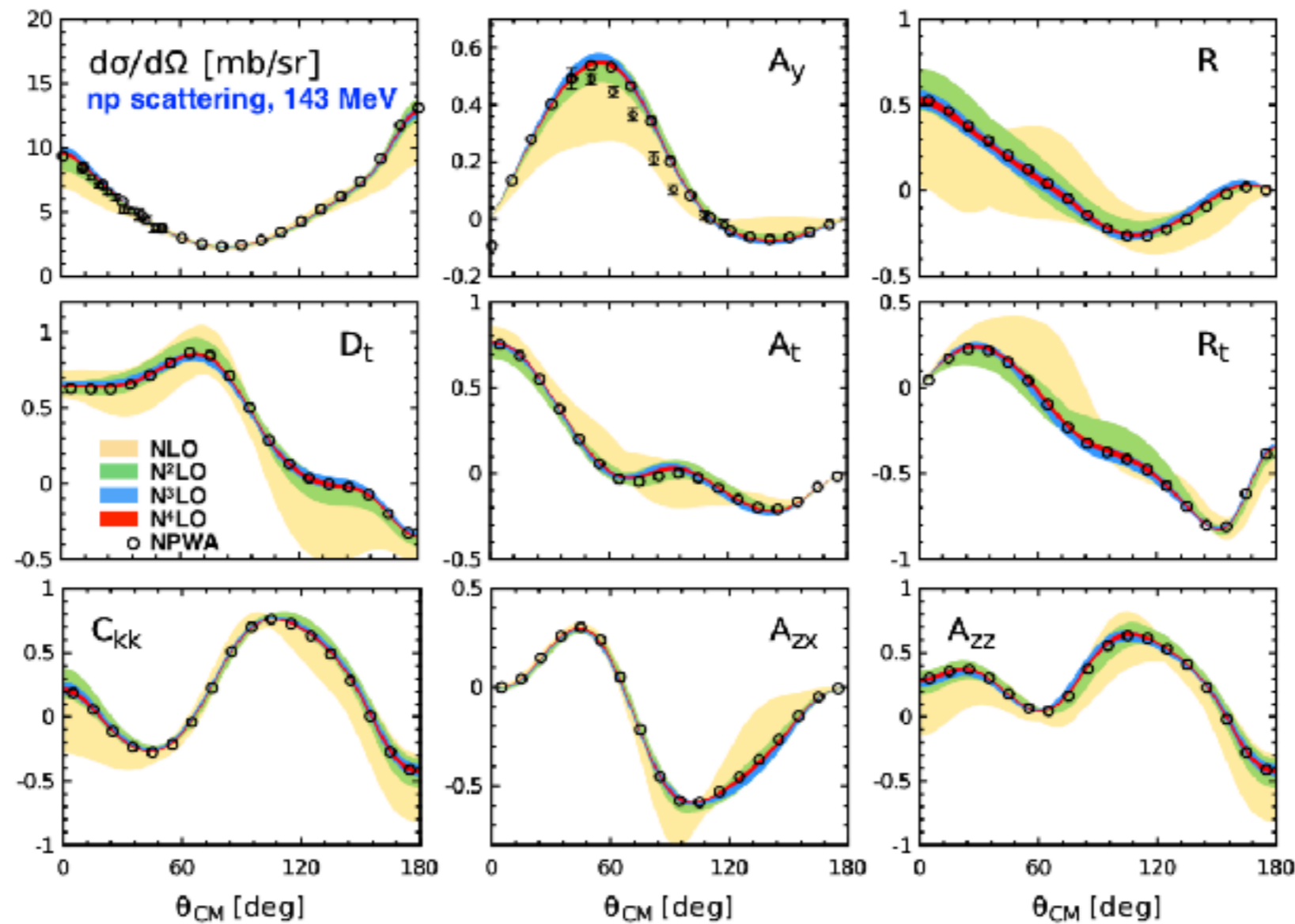


The 2N system

Experience in the 2N sector: **how far should one go to obtain a precise description of data?**

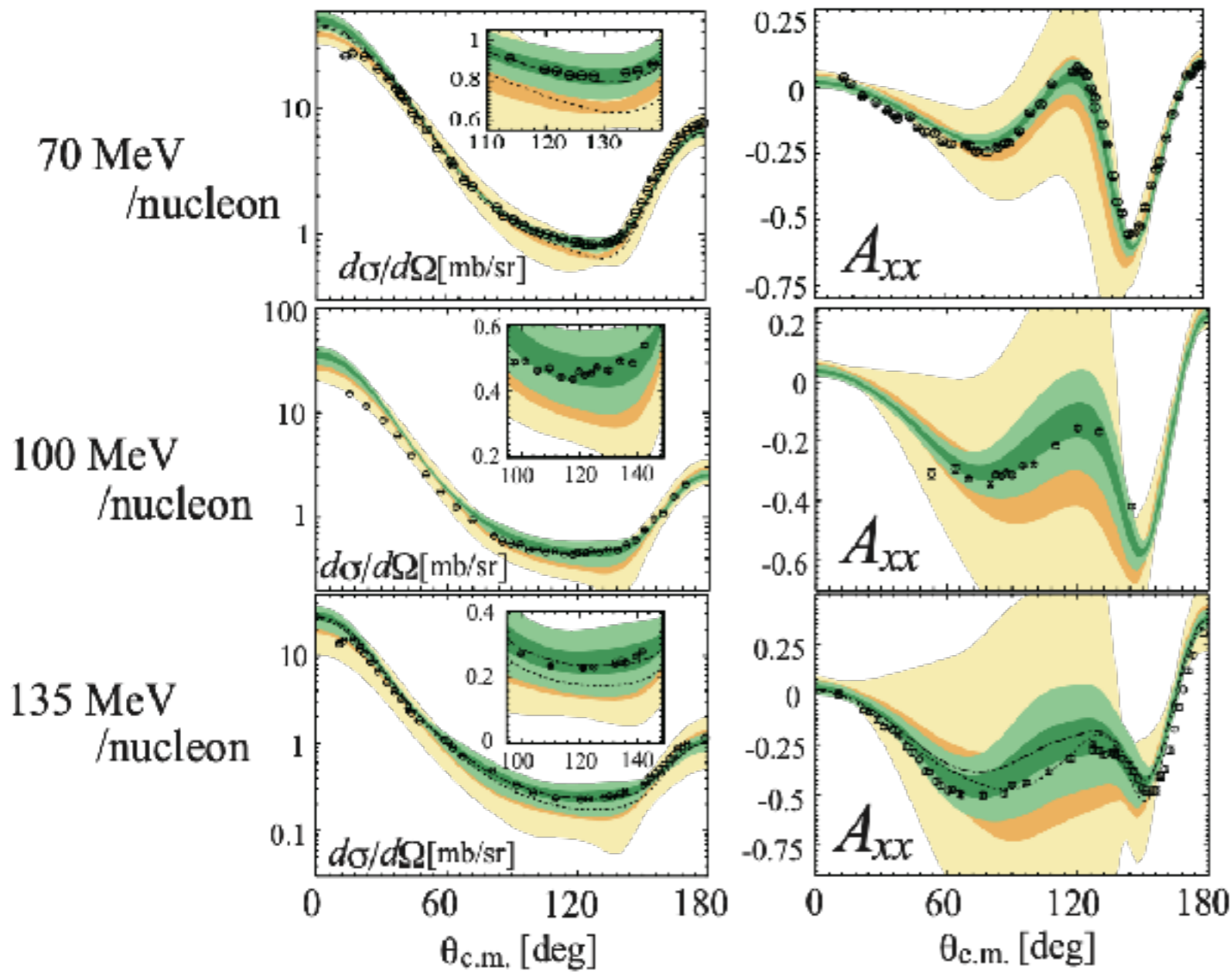
	LO	NLO	N ² LO	N ³ LO	N ⁴ LO ⁺
χ^2/datum (np , 0 – 300 MeV)	75	14	4.1	2.01	1.06
χ^2/datum (pp , 0 – 300 MeV)	1380	91	41	3.43	1.00

P. Reinert, H. Krebs, EE, EPJA 54 (2018) 88



χ EFT N⁴LO 2NF has achieved **high precision**.

dp scattering & χ EFT N2LO 2NF+3NF (green bands)



- LECs of N2LO 3NFs (D and E terms) are determined by
- Cross section of dp scattering at 70 MeV/nucleon
 - ${}^3\text{He}$ binding energy

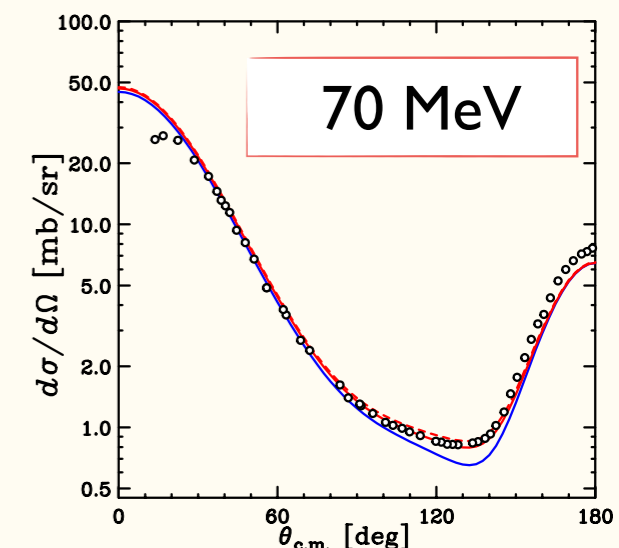
χ EFT & dp elastic scattering

- Calculations of N4LO⁺ NN with N2LO 3NF
(Preliminary)

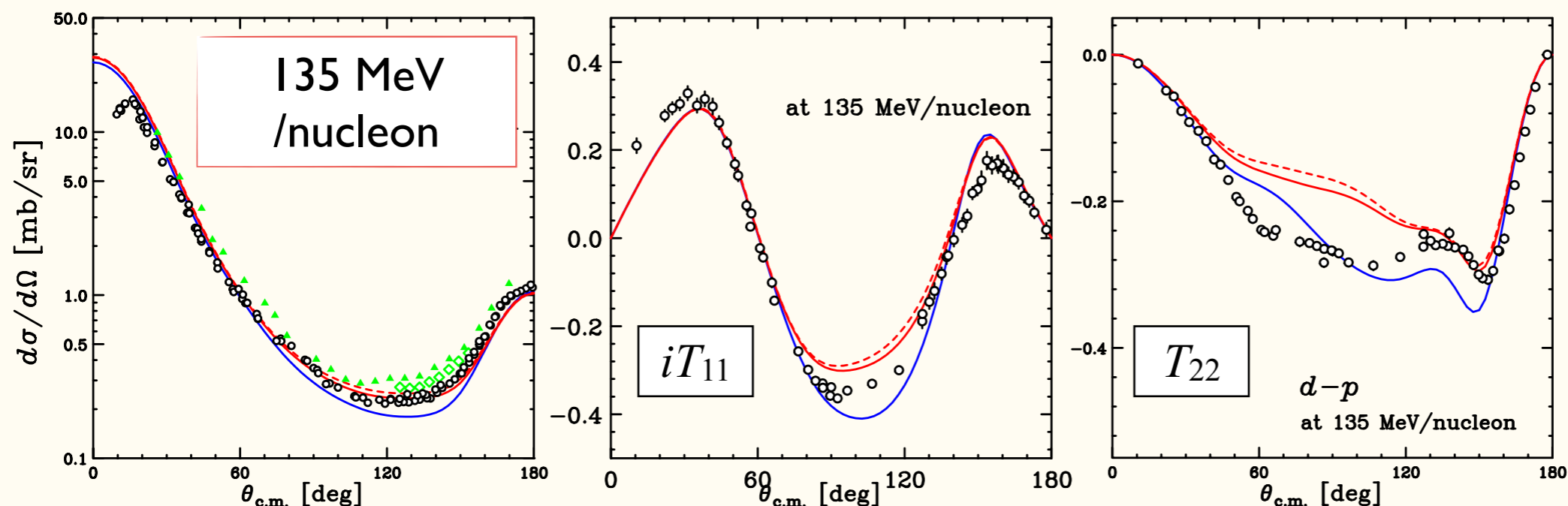
2NF : Semi-local Momentum-Space regularized Chiral NN potentials

P. Reinert, H. Krebs, E. Epelbaum EPJA 54, 86 (2018)

3NF : LECs of N2LO 3NF (D & E terms) are determined
by ^3H B.E. & cross section minimum for Nd @ 70MeV.



— N4LO+, $\Lambda=450\text{MeV}$
— $C_D=2.0, C_E=0.286$
— $C_D=4.0, C_E=0.499$



calculations : H. Witala private communications.

- Spin observables & C.S. at higher energies : N3LO&N4LO 3NFs are needed.
- Cross section minimum region : Golden Window for the higher-order 3NFs.

Project

Determination of $\chi^{\text{EFT N4LO 3NFs}}$ from dp elastic scattering

 "High precision $2N+3N$ forces"

Project of Theory

(ERC Grant Project, PI : Evgeny Epelbaum, Term: 2021-2026)

✓ Partial Wave Analysis

✓ Low Energy Constants for N4LO 3NFs (short-range parts) are determined by 3N scattering data.



High precision data set of dp scattering
at 100 MeV/nucleon and below are highly demanded.

Project of Experiment

(KAKENHI Grant S Project, PI : Kimiko Sekiguchi, Term: FY2020-FY2024)

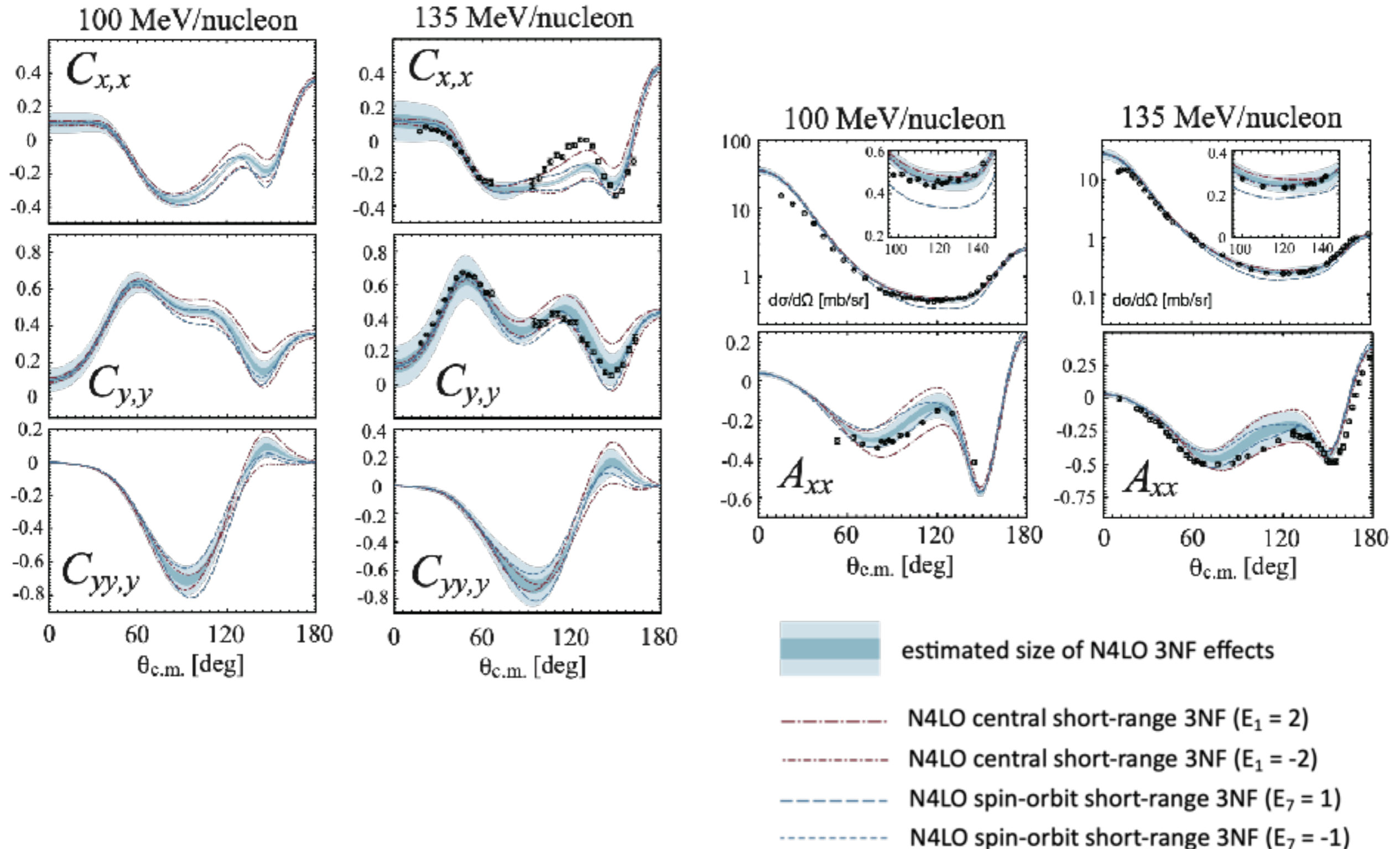
✓ Measurement of spin correlation coefficients for dp scattering
at 100 MeV/nucleon

* Data sets are scarce for spin correlation coefficients.

χ EFT 3NF

		NLO $(Q/\Lambda_\chi)^2$	N2LO $(Q/\Lambda_\chi)^3$	N3LO $(Q/\Lambda_\chi)^4$	N4LO $(Q/\Lambda_\chi)^5$
Long range		—			
Intermediate range		—	—		
Shorter range		—			
		—	—		
		—		—	

➤ **Blue bands in the figure** : Truncation uncertainty at N₃LO → Expected size of N₄LO 3NFs



Summary

Few-Nucleon Scattering

is a good probe to investigate the dynamical aspects of 3NFs .

- Momentum, Spin & Iso-spin dependence - .

Deuteron-Proton Elastic Scattering Experiment at RIKEN

Precise data of $d\sigma/d\Omega$ and spin observables at 70- 300 MeV/nucleon

Comparison with Faddeev calculations based on χEFT NN potential at N^4LO

Cross Section : Large discrepancy at backward angles. 3NFs are clearly needed.

Spin Observables : 3NF effects are spin dependent.

New Project :

- Measurement of spin correlation coefficients at 100 MeV/nucleon for investigation of N^4LO 3NFs .
- Determination of LECs N^4LO 3NFs from dp scattering data is about to start.

RIBF-*d*. Collaboration

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