Stability of collapsing protoneutron stars and gravitational waves

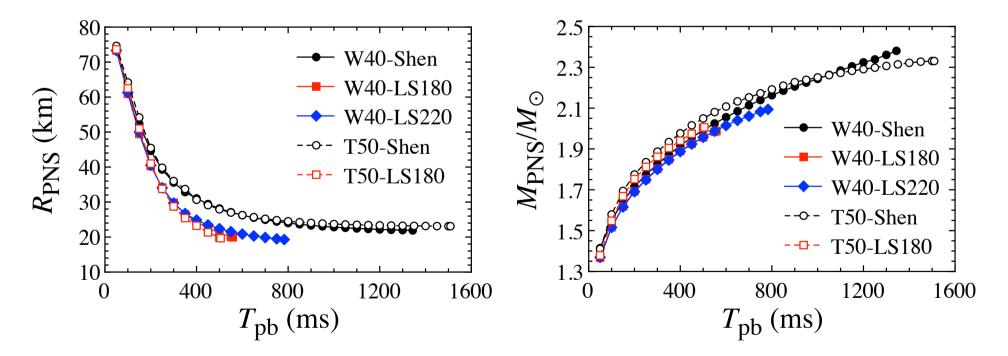
Hajime SOTANI (RIKEN) collaborated with K. Sumiyoshi (NIT, Numazu College)

focusing on failed supernovae

- stability analysis with radial perturbations
- gravitational waves from PNS until apparent horizon appears inside the PNS with linear perturbation analysis

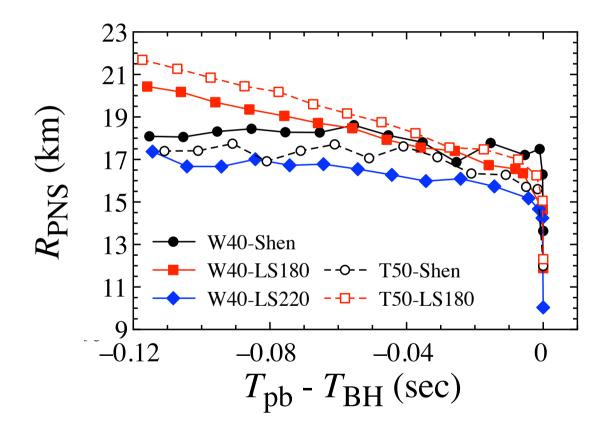
failed supernovae simulations

- 1D-GR core-collapse simulations (by Sumiyoshi)
 - $40M_{\odot}$ progenitor model (W40) based on Woosley & Weaver 95
 - $50M_{\odot}$ progenitor model (T50) based on Tominaga, Umeda & Nomoto 07
 - EOS: Shen (2.2 M_{\odot}), LS180 (1.8 M_{\odot}), LS220 (2.0 M_{\odot})
 - surface density $\approx 10^{11} \text{ g/cm}^3$

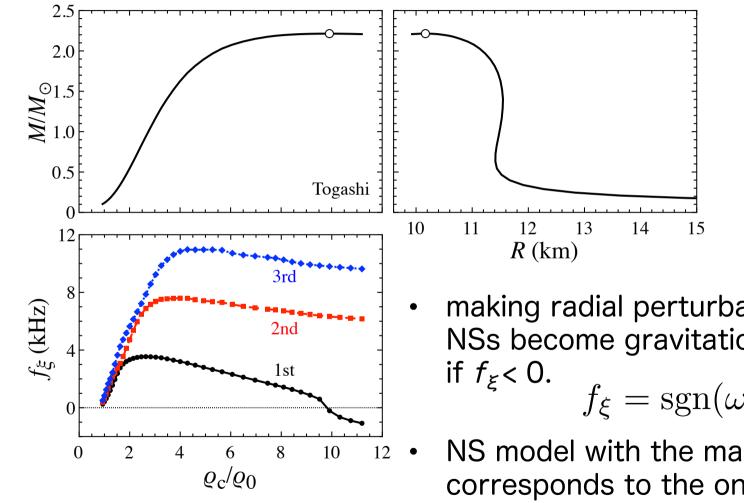


final phase

• at last, the PNS radius is rapidly shrinking.



Stability analysis for cold NSs



HS, Sumiyoshi submitted

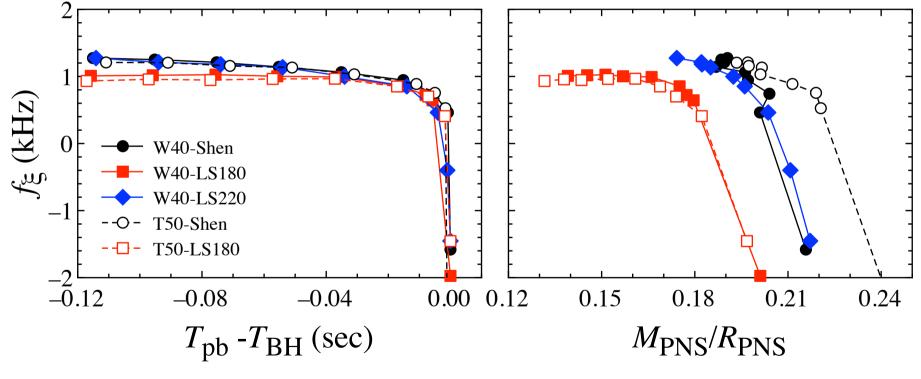
making radial perturbation analysis, NSs become gravitationally unstable,

$$f_{\xi} = \operatorname{sgn}(\omega^2) \sqrt{|\omega^2|/2\pi}$$

NS model with the maximum mass corresponds to the onset of instability.

Stability of PNS @final phase

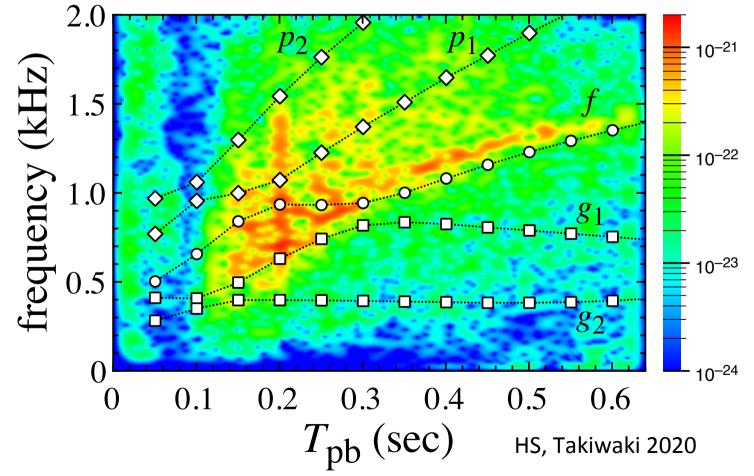
 before the apparent horizon appears inside the PNS, the PNS seems to become gravitationally unstable



HS, Sumiyoshi submitted

GWs from PNS in successful supernova

 GW signals correspond to g₁-mode in early phase and f-mode after avoided crossing.



nuclear burning in massive stars - towards the formation of binary black holes -

Dependence on PNS models HS, Sumiyoshi 2019

3.0

2.5

2.0

1.5

1.0

0.5

0

0

400

800

 $T_{\rm pb}$ (ms)

W40-Shen

T50-Shen T50-LS180

1200

W40-LS180-W40-LS220

1600

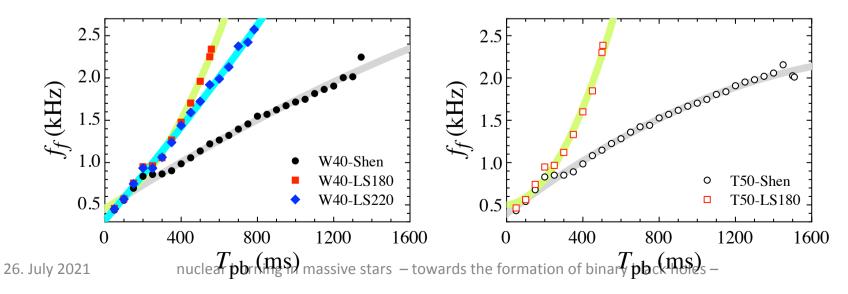
 $f_f(kHz)$

 $\mathbf{2}$

- Time evolution of f-mode GW strongly depends on the progenitor models.
- In any case, it can be well fitted as a function of T_{pb} , such as

$$f_f(\text{kHz}) = c_0 + c_1 \left(\frac{T_{\text{pb}}}{1000 \,\text{ms}}\right) + c_2 \left(\frac{T_{\text{pb}}}{1000 \,\text{ms}}\right)$$

 one can expect high fre. f-mode GW, even though it is not detected directly.

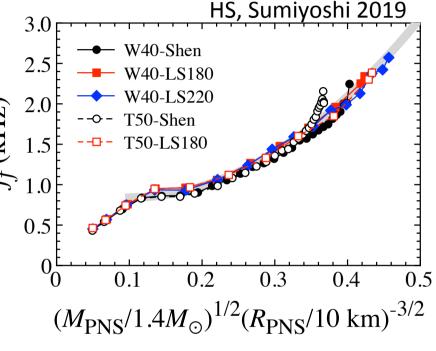


Universality in f-mode GWs

The f-mode frequencies are well-expressed as a function of stellar average density, independently of progenitor models.
W40-She well-expressed as a function of stellar average density, independently of progenitor models.

$$f_f(kH) = 0.9733 - 2.7171X + 13.7809X^2$$

$$X \equiv (M_{\rm PNS}/1.4M_{\odot})^{1/2} (R_{\rm PNS}/10\,{\rm km})^{-3/2}$$



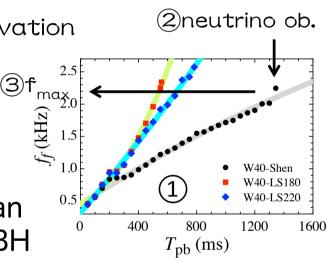
• Through the f-mode GW obs., one can extract the PNS average density, which leads to the time evolution of PNS average density.

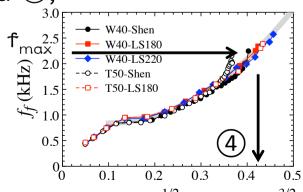
For PNS with maximum mass

 PNS <u>at the moment when it collapses to BH</u>, corresponds to the PNS model with maximum mass.[↑]

one can know via neutrino observation

- How to determine the PNS property
- With the data of the f-mode GW, one can fit the time evolution of the f-mode GW
- ② Owning to the neutrino observation, one can know the moment when PNS collapses to BH
- (3) The f-mode frequency is expected via (1) and (2), even if the f-mode freq. at the final phase would not be detected. $f_{max}^{2.0}$
- ④ Via the universal relation of the f-mode, one can extract the average density of PNS with maximum mass





26. July 2021

nuclear burning in massive stars – towards the formation of binary black ho($M_{PNS}/1.4M_{\odot}$)^{1/2}($R_{PNS}/10$ km)^{-3/2}

summary

- We made a stability analysis on PNS
 - PNS becomes gravitationally unstable before the apparent horizon appears inside the PNS.
- we examine the GW freq. from PNSs for failed supernova
 - f-mode frequency can be expressed well as a function of PNS average density independently of the PNS models
 - Owning to the neutrino observation, one would estimate the average density of PNS with maximum mass, even if the corresponding f-mode GW could NOT be detected.
- We will taken into account the effect of the radial velocity as background properties.