

# ニュートリノ振動研究の現状と展望

2020年4月

首都大理 安田修

2020年3月18日

シンポジウム「宇宙と素粒子の残された謎の解明に向けた、次世代ニュートリノ観測・陽子崩壊実験」  
@日本物理学会年会

**1. Introduction**

**2. 3 flavor  $\nu$  oscillation**

**3. Scenarios beyond the standard 3  $\nu$  oscillation**

**4. Summary**

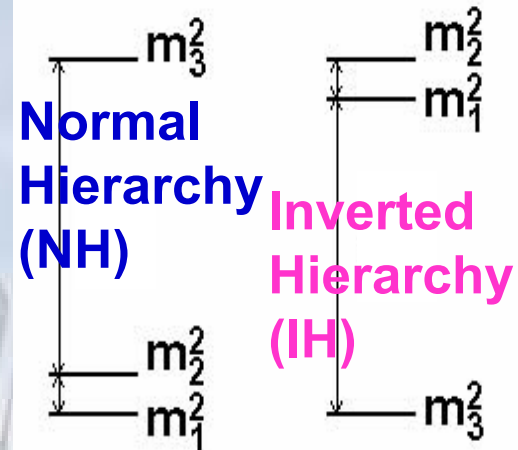
# 1. Introduction

## Framework of 3 flavor $\nu$ oscillation

### Mixing matrix

Functions of mixing angles  $\theta_{12}$ ,  $\theta_{23}$ ,  $\theta_{13}$ , and CP phase  $\delta$

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$



All 3 mixing angles have been measured (2012):

$\nu_{\text{solar}}$ +KamLAND (reactor)



$$\theta_{12} \cong \frac{\pi}{6}, \Delta m_{21}^2 \cong 8 \times 10^{-5} \text{ eV}^2$$

$\nu_{\text{atm}}$ +K2K, MINOS (accelerators)



$$\theta_{23} \cong \frac{\pi}{4}, |\Delta m_{32}^2| \cong 2.5 \times 10^{-3} \text{ eV}^2$$

DCHOOZ+Daya Bay+Reno (reactors), T2K+MINOS, others



$$\theta_{13} \cong \pi / 20$$

# Motivation for precise measurement of oscillation parameters

From symmetry arguments, all kind of predictions have been made for oscillation parameters:

◆ **Quark-lepton complementarity**  
Minakata-Smirnov, PR D70 (2004) 073009

$$\theta_{12} + \theta_c = \pi/4$$

◆ **T' symmetry**  
Eby-Frampton, PR D86 (2012) 117304

$$\pi/4 - \theta_{23} = 2^{-1/2} \theta_{13}$$

◆ **Asymmetric TriBiMaximal Texture**  
Rahat-Ramond-Xu, PR D98 (2018) 055030

$$\delta_{CP} = \pm 1.32\pi$$

**Quark mixing has been measured to the precision of  $O(0.01^\circ)$ :**

**CKM angles @ $1\sigma$  (PDG)**

$$\theta_{12} = 12.975 \pm 0.026 \text{ deg}$$

$$\theta_{23} = 2.415 \pm 0.044 \text{ deg}$$

$$\theta_{13} = 0.204 \pm 0.010 \text{ deg}$$

# Lepton mixing which is measured to date

## Lepton mixings @ $1\sigma$

Capozzi, Lisi,  
Marrone, Palazzo,  
arXiv:1804.09678

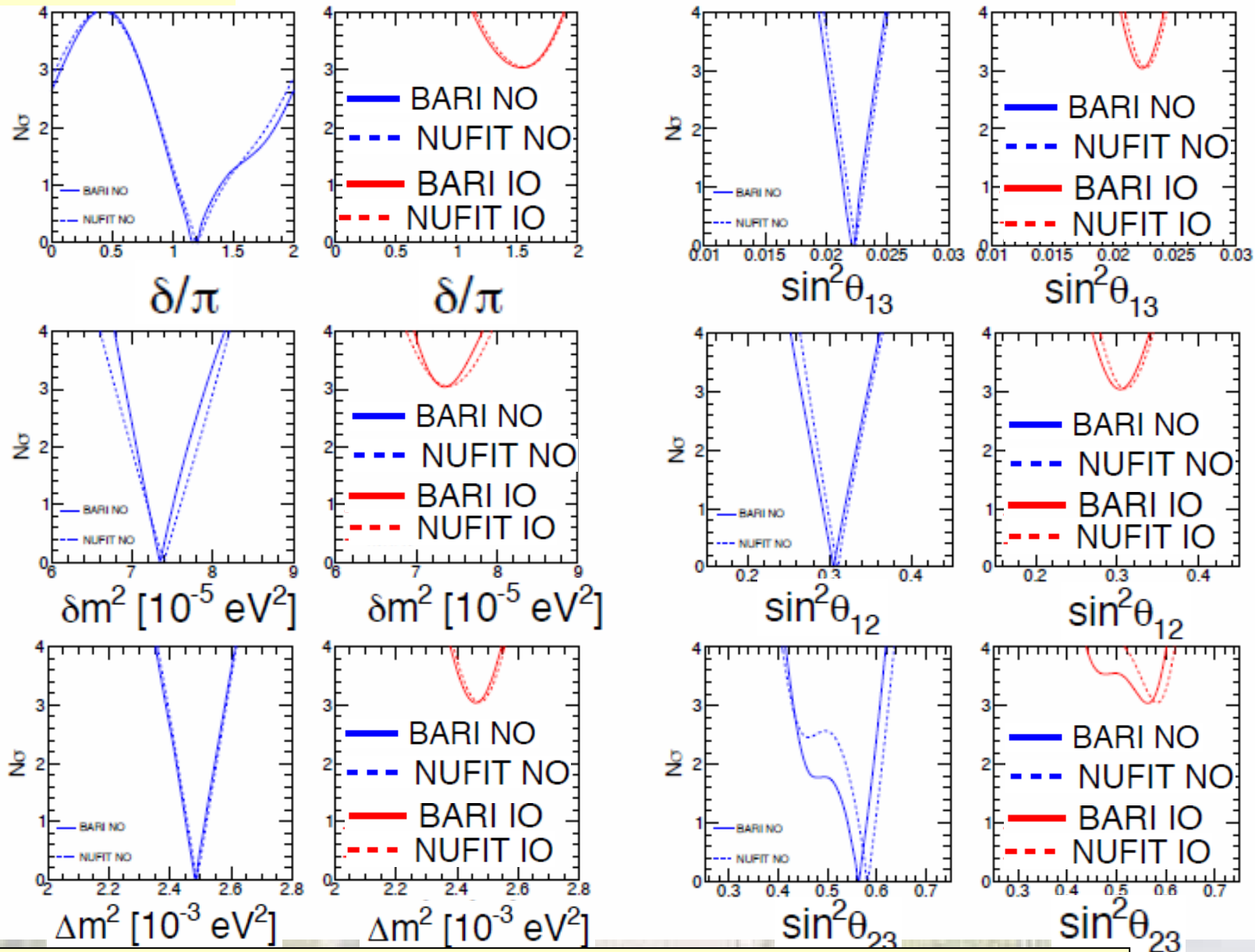
$$\theta_{12} = 33.46 + 0.87 - 0.88 \text{ deg}$$

$$\theta_{23} = 47.9 + 1.1 - 4.0 \text{ deg}$$

$$\theta_{13} = 8.41 + 0.18 - 0.14 \text{ deg}$$

→ To test a hypothesis such as  $\pi/4 - \theta_{23} = 2^{-1/2} \theta_{13}$ ,  
lepton mixing should be measured at least to  
order  $O(0.1^\circ)$

In particular, the precision of  $\theta_{23}$  is a problem



**NH(NO),  $\delta \sim 3\pi/2$  is preferred over IH(IO),  $\delta = 0$**

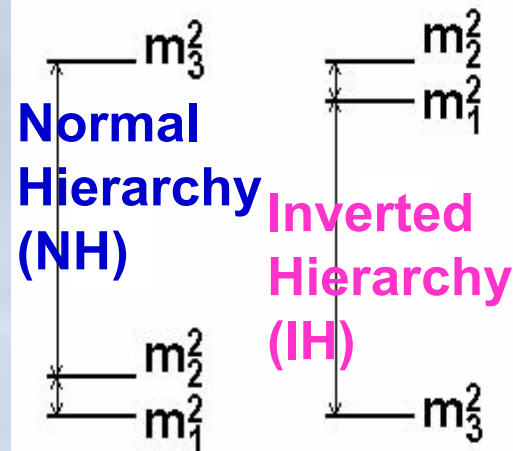
Next task is to measure **Mass Hierarchy** (NH or IH), **Octant** (Higher Octant or Lower Octant) and  $\delta$  (CP)

Experiments under construction / consideration

- **T2HK**(JP, JPARC-->HK) L=295km, E~0.6GeV
- **DUNE** (US, FNAL-->Homestake, SD) , L=1300km, E~2GeV
- **T2HKK**(JP, JPARC-->Korea) L=1100km, E~1GeV

$$\overline{\nu}_\mu \rightarrow \overline{\nu}_\mu + \overline{\nu}_\mu \rightarrow \overline{\nu}_e$$

These experiments are expected to measure  $\text{sign}(\Delta m_{31}^2)$ ,  $\pi/4 - \theta_{23}$  and  $\delta$





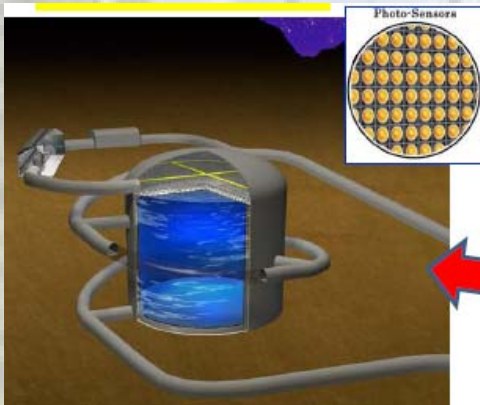
# ● Experiments under construction / consideration

## T2HK

### ● Extension of T2K (large #(events))

1.3MW  $\nu$  beam  $\Rightarrow$  Hyperkamiokande  
(3 times 2K) (10 times SK)

### ● Measurement of CP phase $\delta$



Hyper-kamiokande

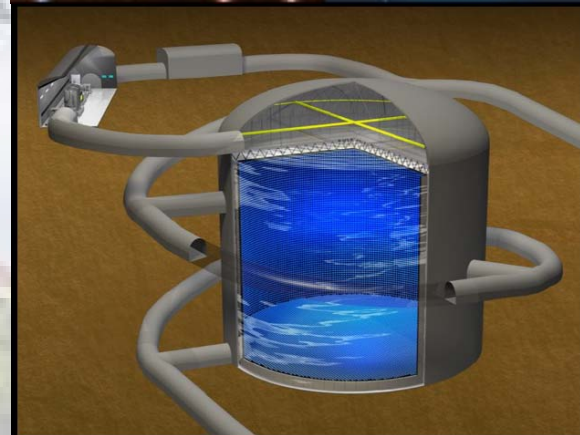
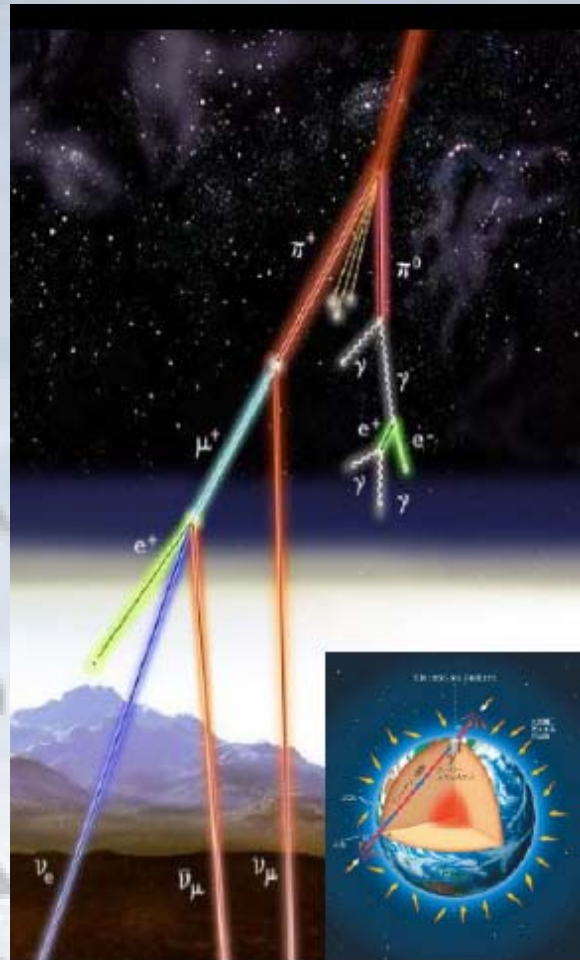
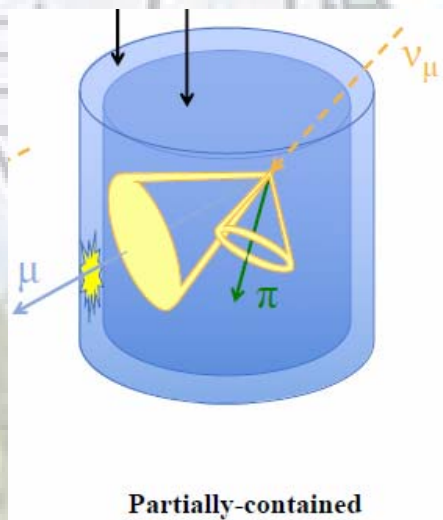
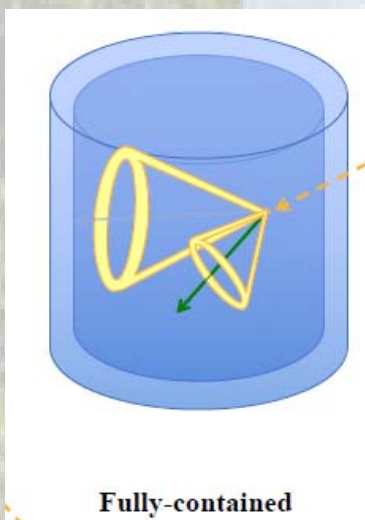


J-PARC Main Ring  
(KEK-JAEA, Tokai)



# $\nu_{\text{atm}}$ @HK

- 186 ( $\times 2$ ) kton fiducial volume ( $2 \times 8.3 \times \text{SK}$ )
- Optically separated into
  - Inner Detector 40,000 ( $\times 2$ ) PMTs ( $2 \times 4 \times \text{SK}$ )
    - 40% Coverage (same as SK)
  - Outer Detector 12,000 ( $\times 2$ ) PMTs ( $2 \times 6 \times \text{SK}$ )
- ID Photosensors will be high QE
  - Single photon detection : 24% ( $2 \times \text{SK}$ )







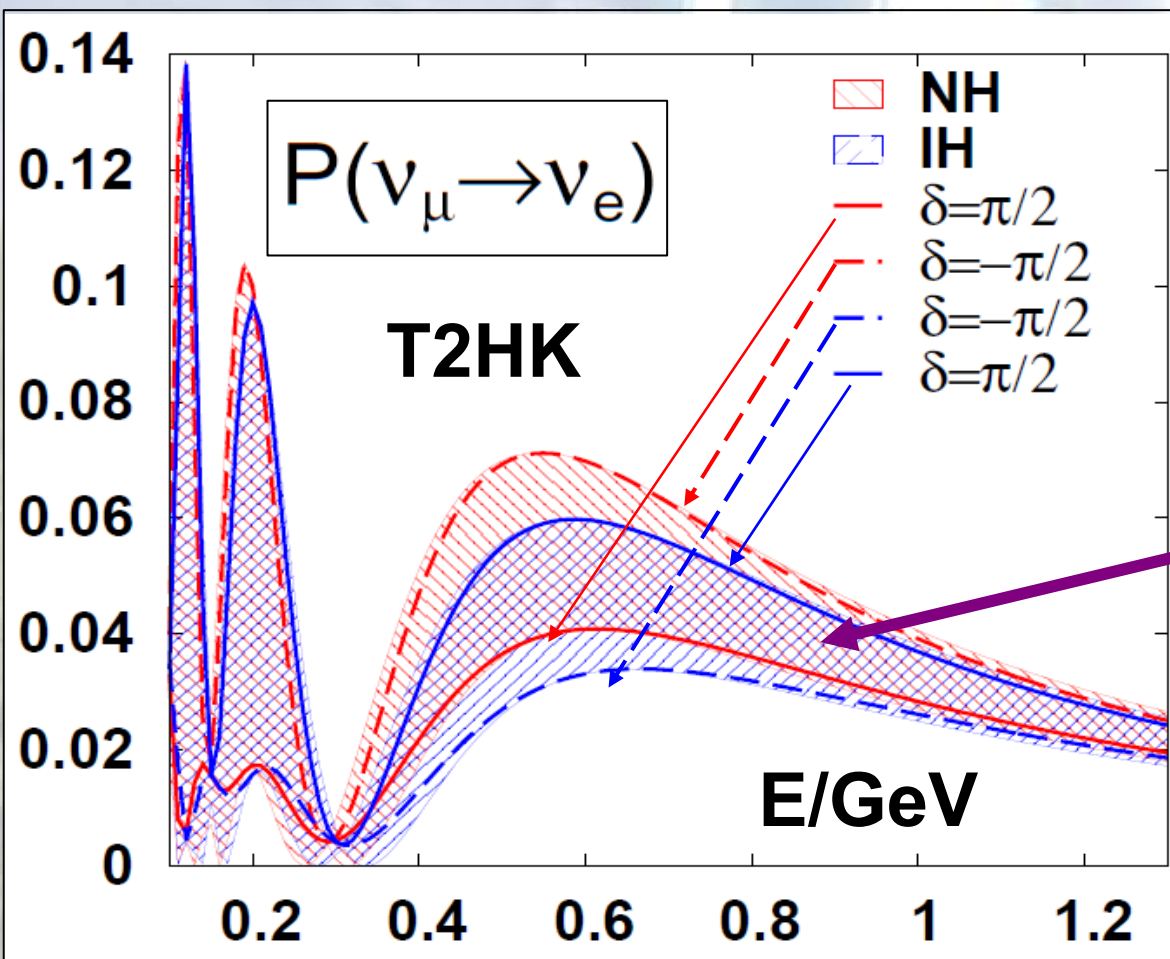
## 2. 3 flavor $\nu$ oscillation

Issue in measurement of  $\delta$  at T2HK:

**Degeneracy** in the appearance probabilities

hierarchy -  $\delta$

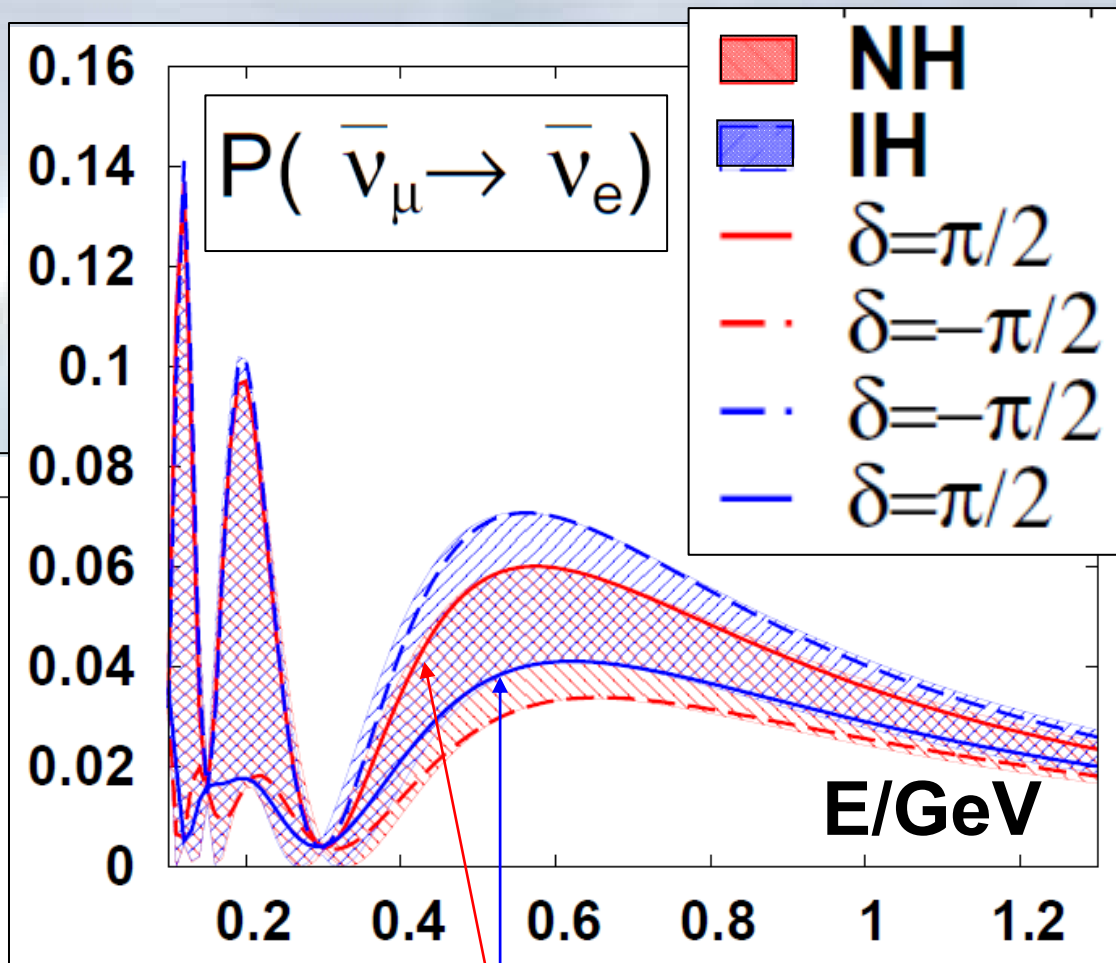
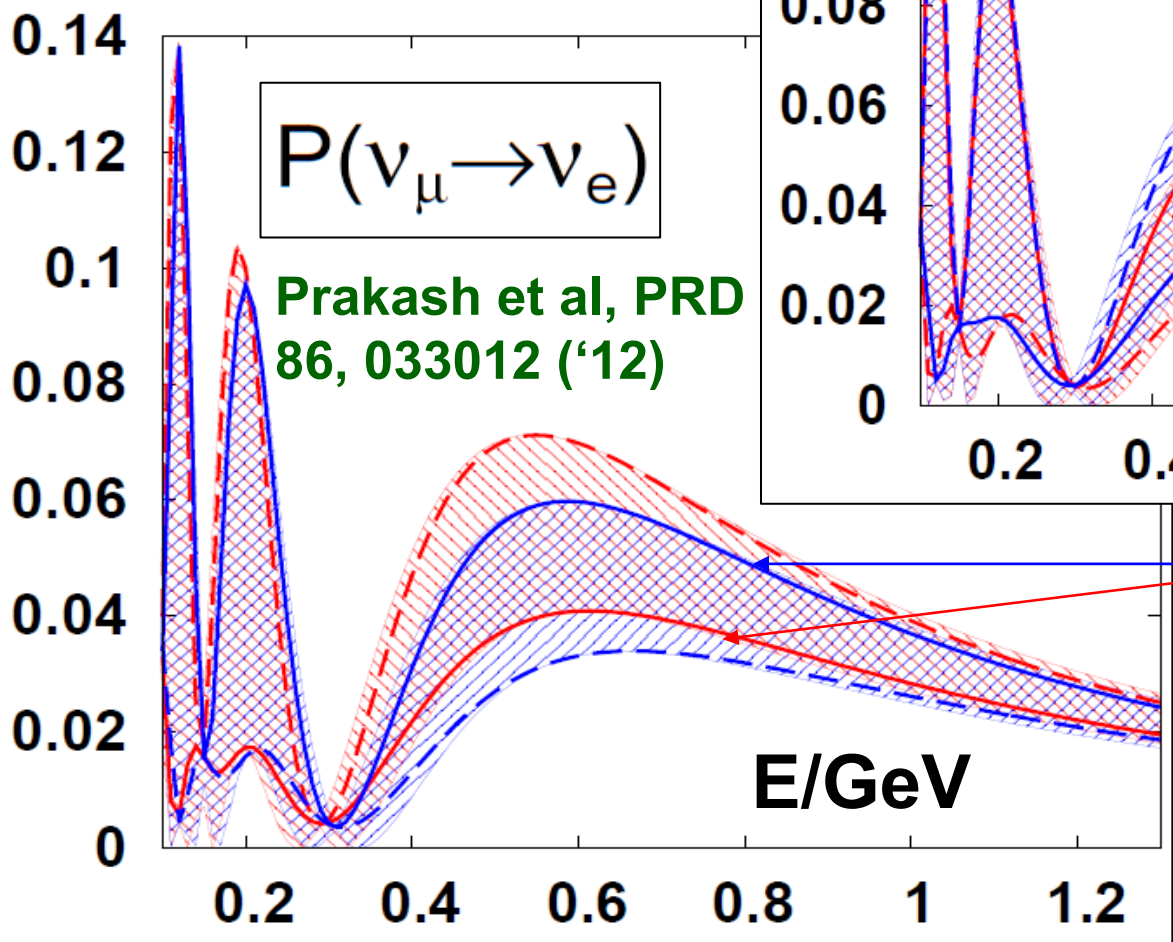
Prakash et al, PRD 86, 033012 ('12)



Due to uncertainty in  $\delta$ , the appearance probabilities has finite width. In the overlap region,  $\delta$  has two possible values.

# Hierarchy degeneracy @T2HK

NH-IH Separation  
is good (bad) for  
 $\delta \sim -\pi/2$  ( $+\pi/2$ )

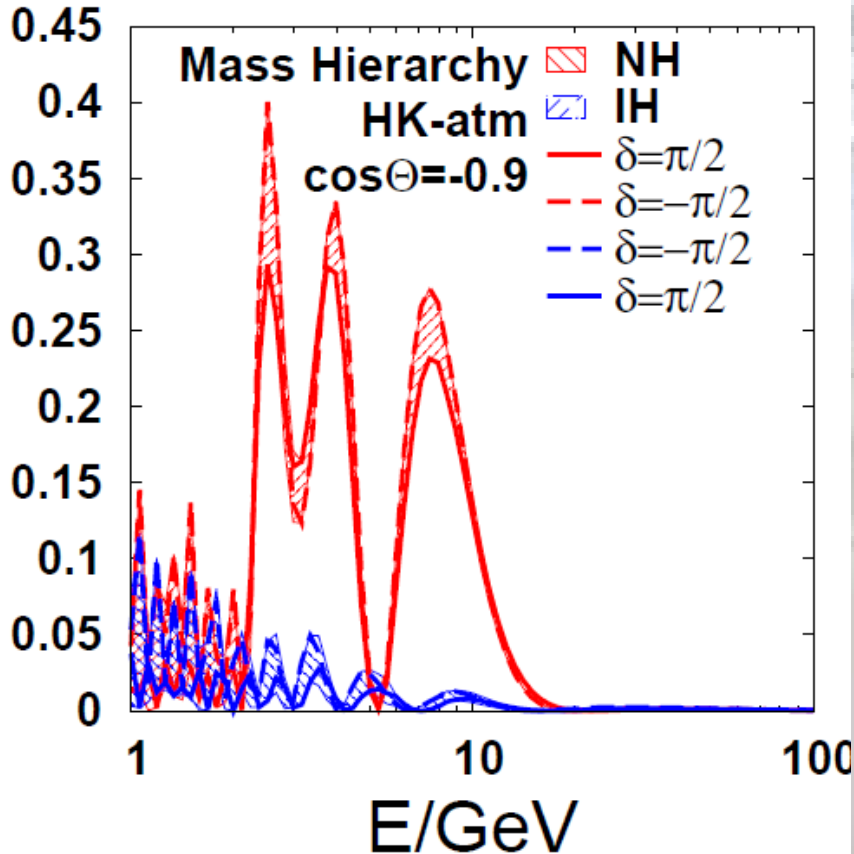


For  $\delta \sim \pi/2$   
degeneracy  
exists both in  
 $\nu$  &  $\bar{\nu}$

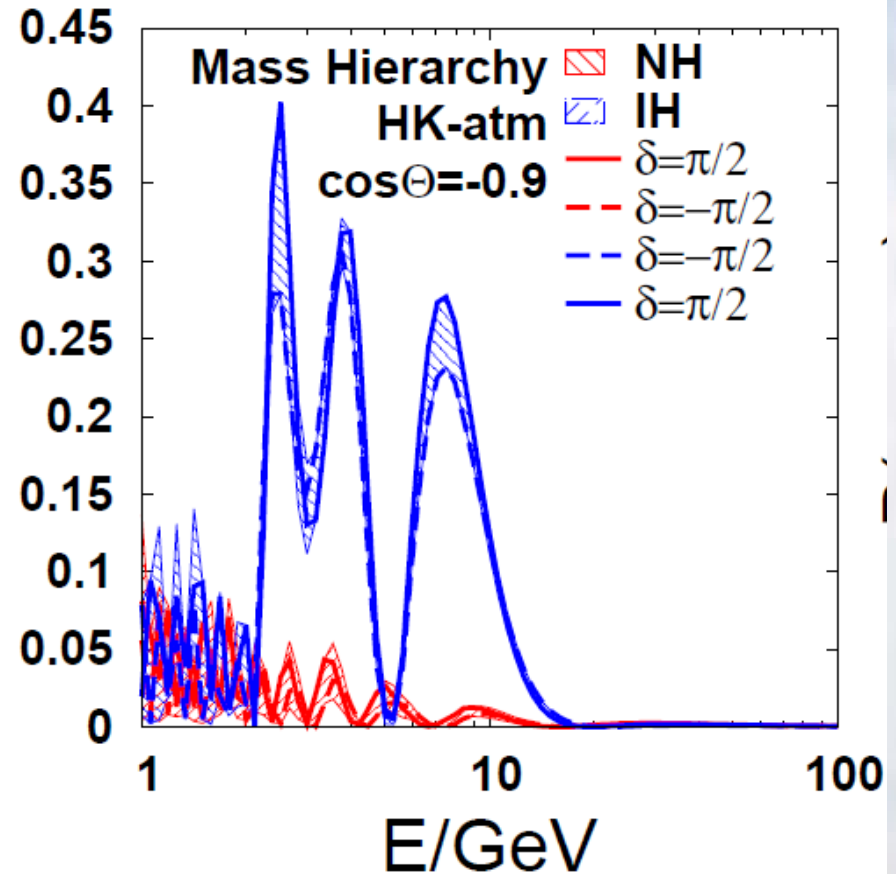
# Hierarchy degeneracy $\nu_{\text{atm}}@HK$

Hierarchy separation is excellent for  $\cos\Theta = -0.9$   
( $L=11500\text{km}$ )

$$P(\nu_{\mu} \rightarrow \nu_e)$$



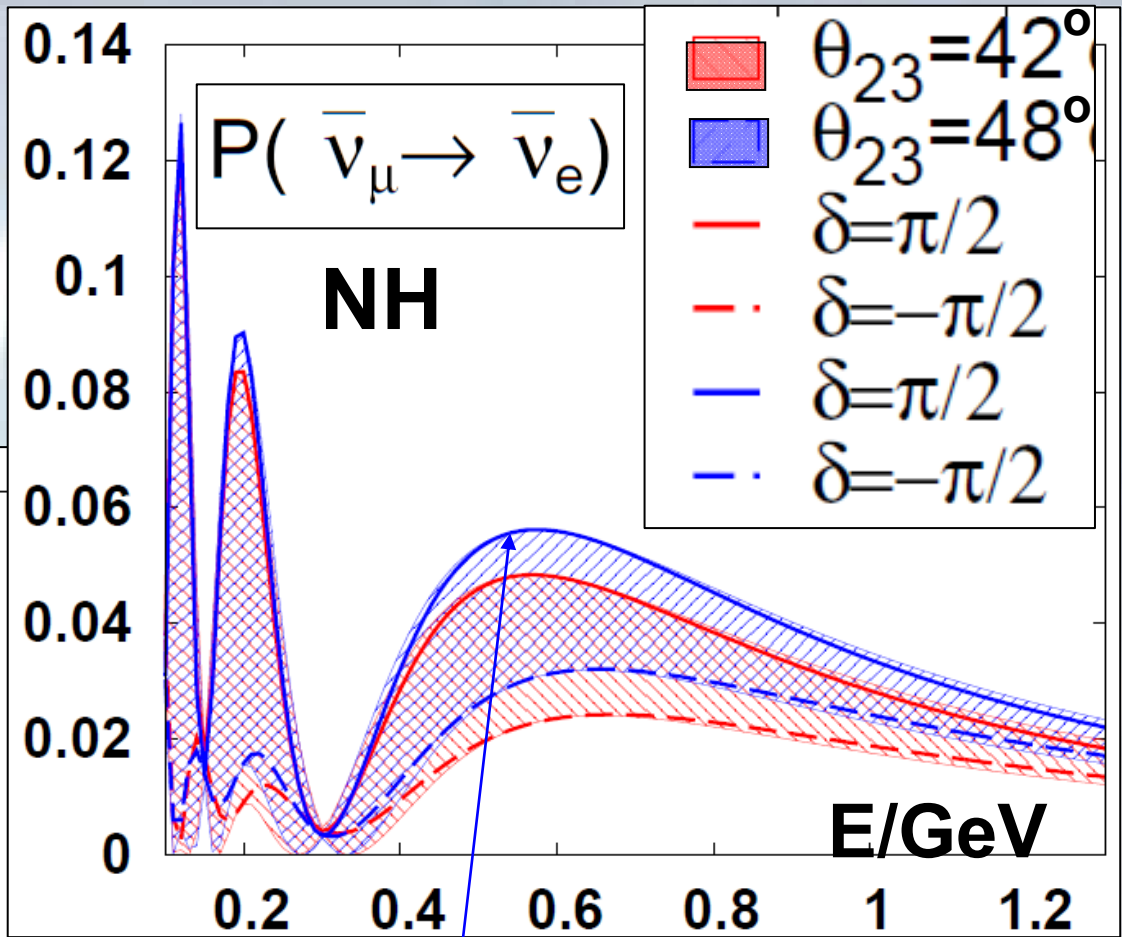
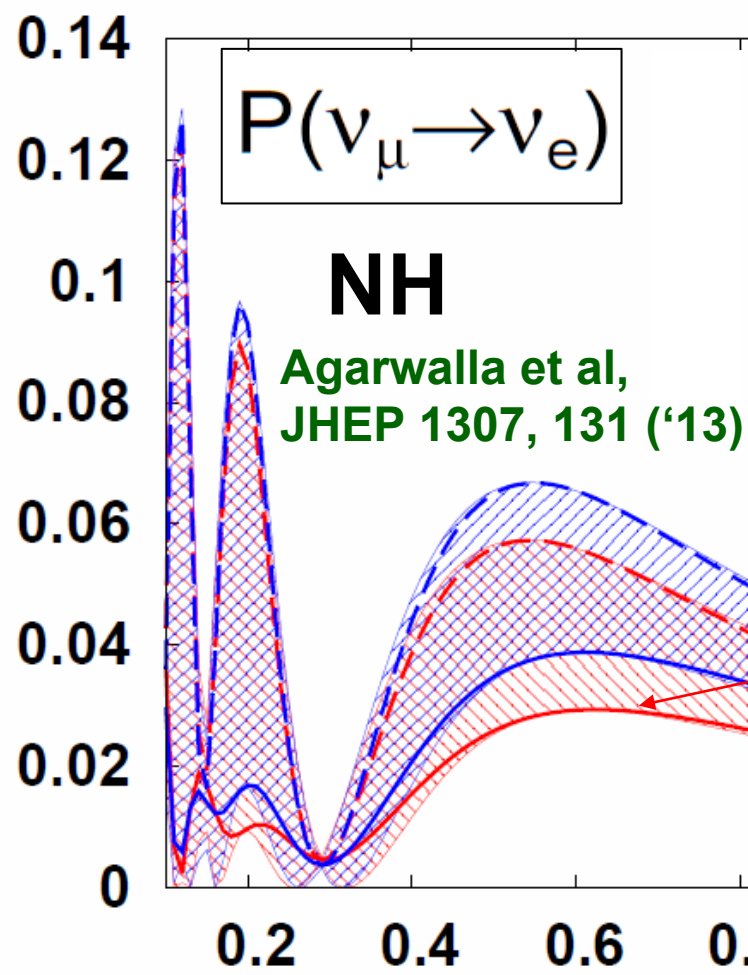
$$P(\bar{\nu}_{\mu} \rightarrow \bar{\nu}_e)$$





# Octant degeneracy @T2HK

HO-LO Separation is possible w/  $\nu$  &  $\bar{\nu}$  for most of  $\delta$



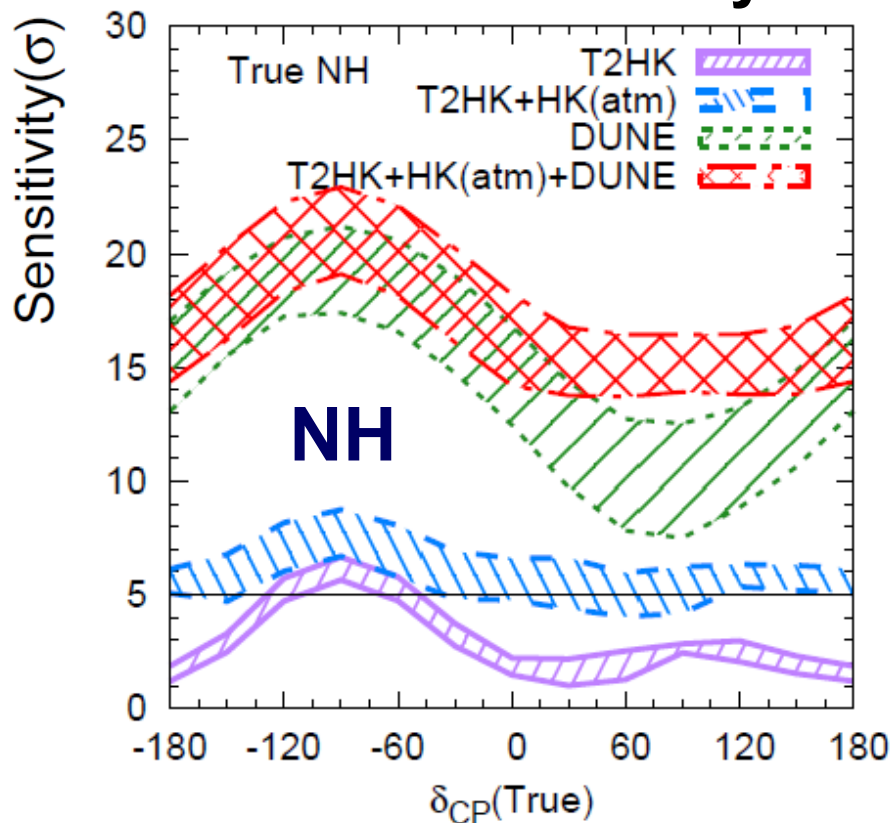
Unlike hierarchy degeneracy,  $\delta=-\pi/2$  lies on the same side for  $\nu$  &  $\bar{\nu}$

# ● Sensitivity of T2HK, $\nu_{\text{atm}}@HK$ & their combination

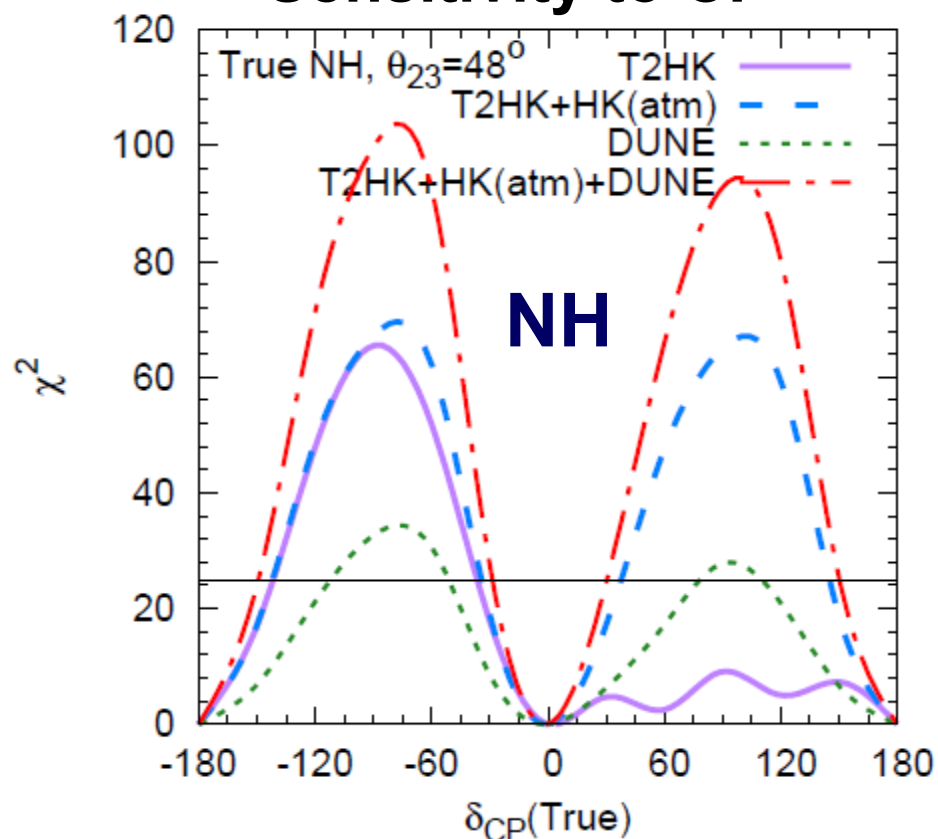
2020年4月

Fukasawa-Ghosh-OY,  
NPB918 ('17) 337

## Mass Hierarchy



## Sensitivity to CP

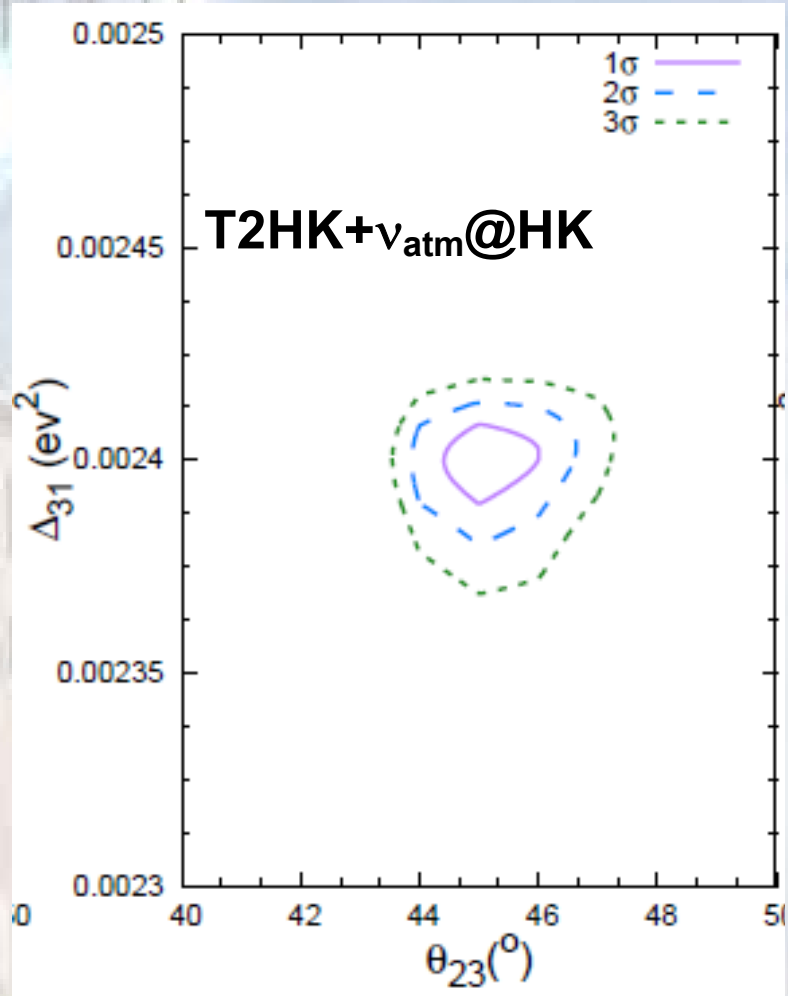
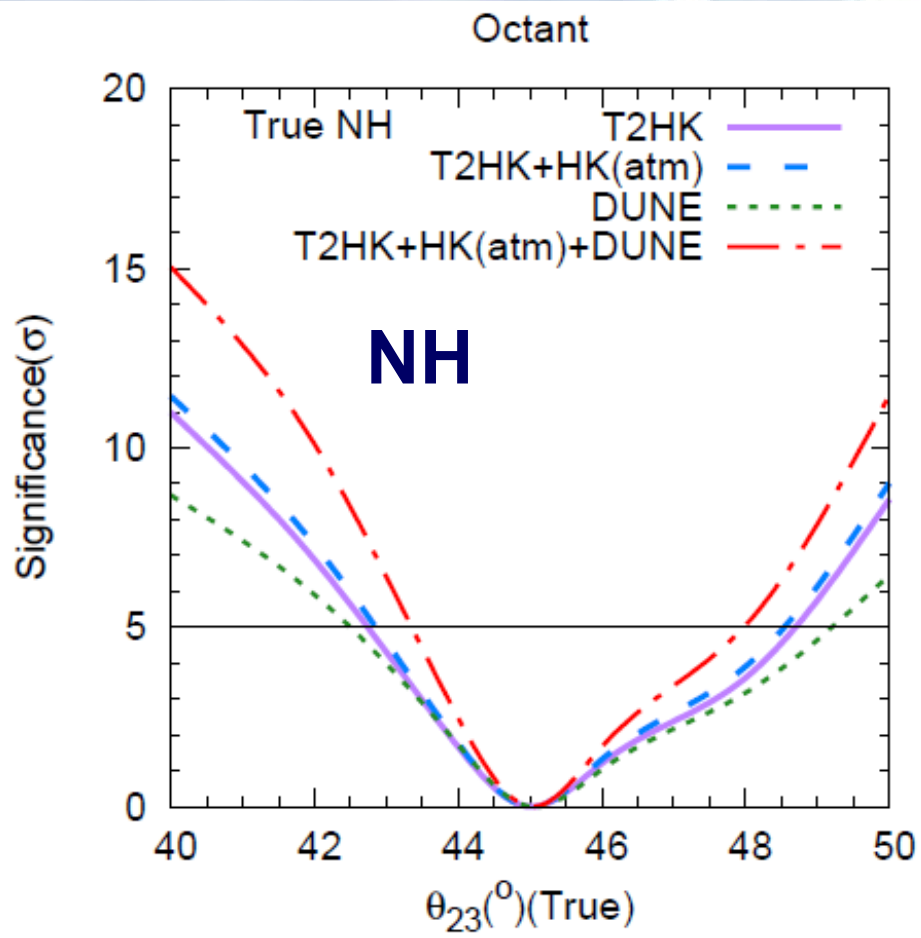




# Sensitivity of T2HK, $\nu_{\text{atm}}@HK$ & their combination

Fukasawa, Ghosh, Yasuda, NPB918 ('17) 337

2020年4月



### 3. Scenarios beyond standard 3 $\nu$ oscillation

#### Motivation for research on **New Physics**

Just like at B factories, **high precision** measurements of  $\nu$  oscillation in future experiments can be used to probe physics **beyond SM** by looking at deviation from **SM+ $m_\nu$**  (beyond the **PMNS** paradigm).  
→ Research on **New Physics** is important.

#### Test of the **PMNS** paradigm

Rather than looking for arbitrary possibilities of **New Physics**, here we discuss possible hints of the scenarios which have been discussed in the past.

# List of popular **NP** in $\nu$ oscillation phenomenology

Scenario beyond SM+m $\nu$	Experimental indication ?	Phenomenological constraints on the magnitude of the effects
<ul style="list-style-type: none"><li>• Light sterile <math>\nu</math> (<math>\nu_s</math>)</li></ul>	Maybe	O(10%)
<ul style="list-style-type: none"><li>• Non Standard Interactions in propagation</li></ul>	Maybe	e- $\tau$ : O(100%) Others: O(1%)
Non Standard Interactions at production / detection	×	O(1%)
Unitarity violation due to heavy particles	×	O(0.1%)

In this talk, we will focus on these two because of potential experimental hints

# In the past we have had some anomalies

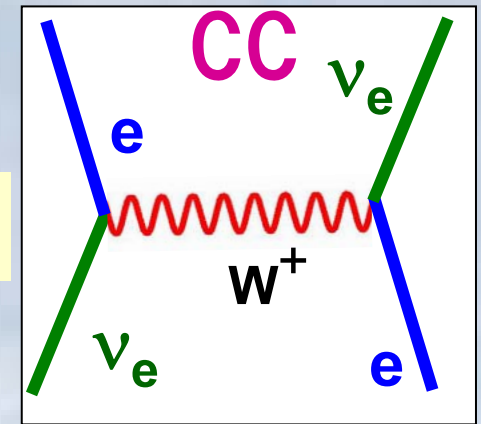
- $\nu_{\text{solar}}$  - KamLAND:  $\Delta m^2_{21}$   $\longrightarrow$  NSI or  $\nu_s$   
 $\Delta m^2 = O(10^{-5}) \text{eV}^2$
- LSND-MiniBooNE anomaly, Reactor anomaly, Gallium anomaly  $\longrightarrow$   $\nu_s$   
 $\Delta m^2 = O(1) \text{eV}^2$

東京都立大学へ。

## 3.1. $\nu_s$

### 3.1.1 Features of light sterile $\nu$ ( $\nu_s$ )

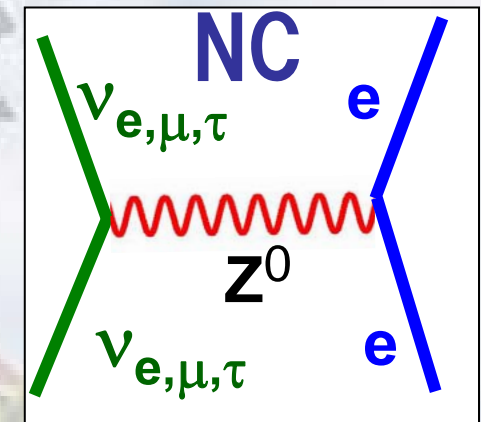
#### Interactions of active & sterile $\nu$



$$A_e = \sqrt{2}G_F N_e$$

$$A_n = -(1/\sqrt{2})G_F N_n$$

	$\nu_e$	$\nu_\mu, \nu_\tau$	$\nu_s$
CC	✓	✗	✗
NC	✓	✓	✗
$\nu$	$A_e + A_n$	$A_n$	0



# Matter effect in the presence of sterile $\nu$

$$i \frac{\partial}{\partial t} \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \\ \nu_s \end{pmatrix} = \left[ U \begin{pmatrix} E_1 & 0 & 0 & 0 \\ 0 & E_2 & 0 & 0 \\ 0 & 0 & E_3 & 0 \\ 0 & 0 & 0 & E_4 \end{pmatrix} U^{-1} + \begin{pmatrix} A_e + A_n & 0 & 0 & 0 \\ 0 & A_n & 0 & 0 \\ 0 & 0 & A_n & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix} \right] \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \\ \nu_s \end{pmatrix}$$

$$U = R_{34}(\theta_{34}, \delta_{34}) R_{24}(\theta_{24}, 0) R_{14}(\theta_{14}, \delta_{14}) R_{23}(\theta_{23}, 0) R_{13}(\theta_{13}, \delta_{13}) R_{12}(\theta_{12}, 0)$$

extra mixing angles

3 $\nu$  mixing angles

The term which is proportional to identity can be ignored

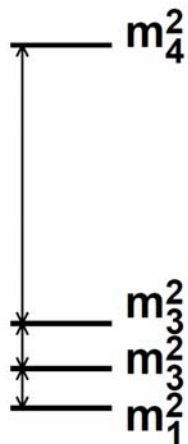
$$U \equiv \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} & U_{e4} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} & U_{\mu4} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} & U_{\tau4} \\ U_{s1} & U_{s2} & U_{s3} & U_{s4} \end{pmatrix}$$

$$A_e \equiv \sqrt{2} G_F N_e$$

$$A_n \equiv -\frac{G_F N_n}{\sqrt{2}}$$

$$= \left[ U \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & \Delta E_{21} & 0 & 0 \\ 0 & 0 & \Delta E_{31} & 0 \\ 0 & 0 & 0 & \Delta E_{41} \end{pmatrix} U^{-1} + \begin{pmatrix} A_e & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & -A_n \end{pmatrix} \right] \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \\ \nu_s \end{pmatrix}$$

$\nu_s$  has matter effect different from others



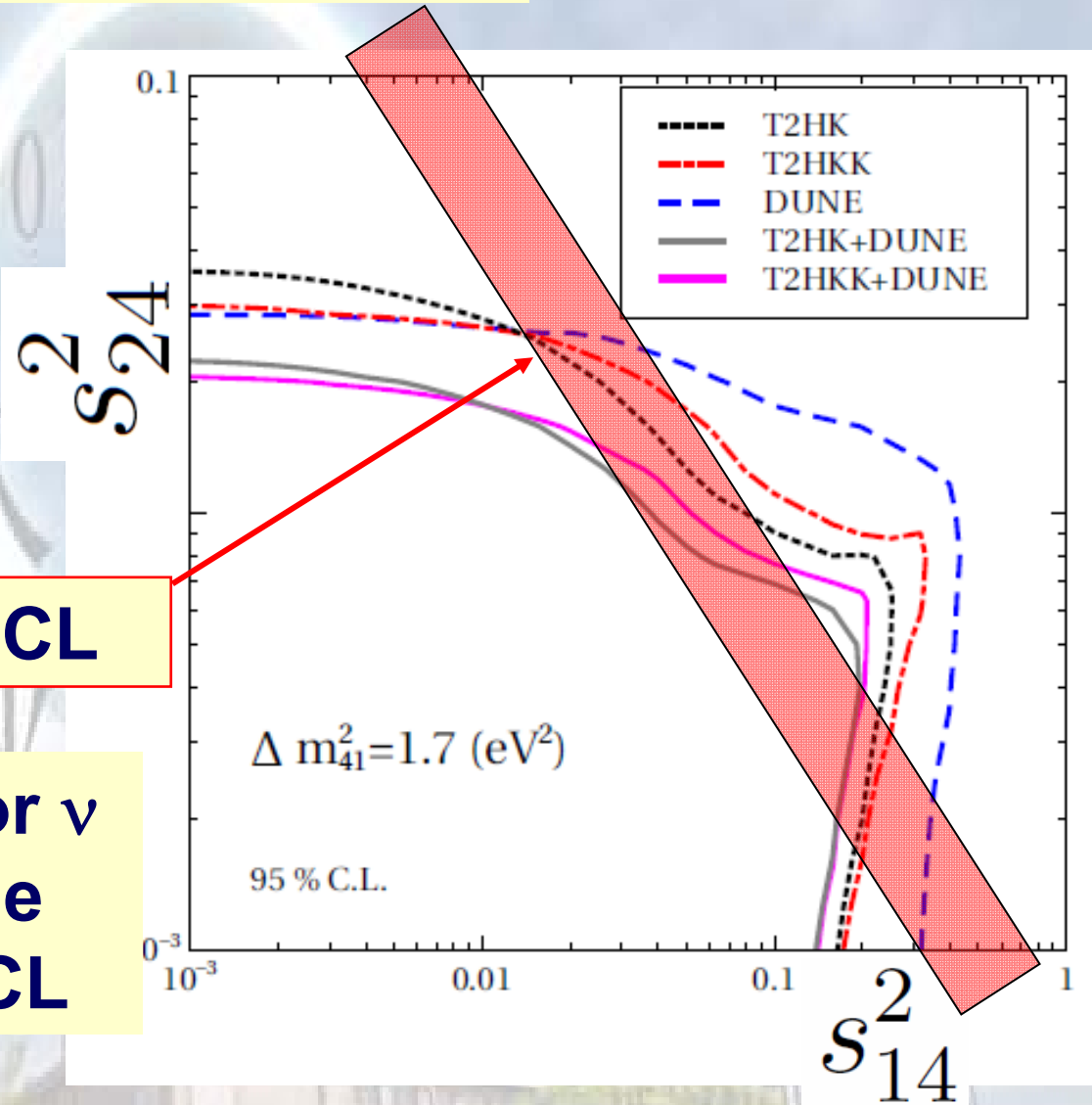
### 3.1.2 Accelerator $\nu$ (T2HK, T2HKK)

Choubey-Dutta-Pramanik,  
Eur.Phys.J. C78 ('18) 339

$$\Delta m_{41}^2 = 1.7 \text{ (eV}^2\text{)}$$

LSND region @ 90%CL

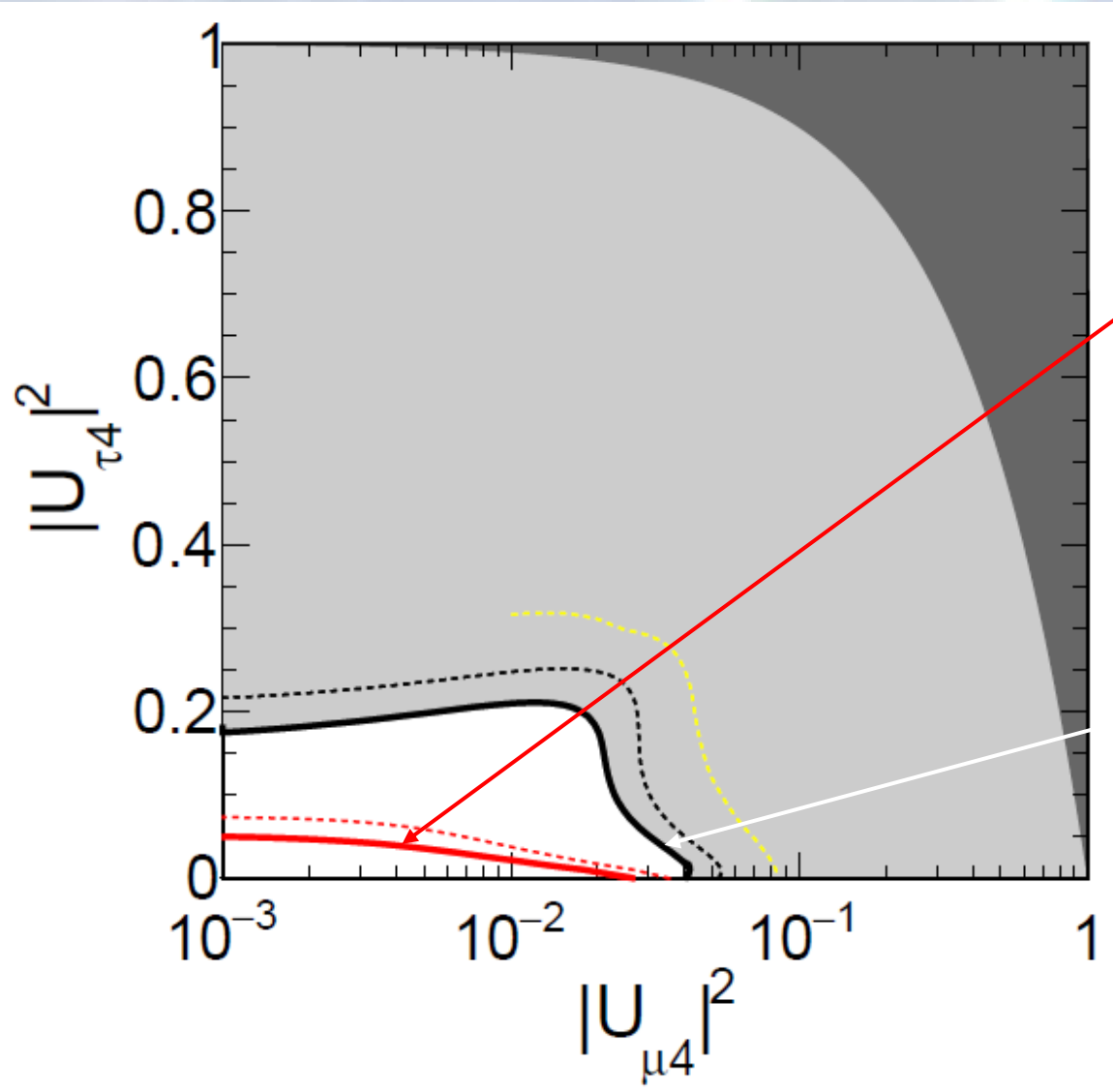
Combined accelerator  $\nu$   
can cover some of the  
LSND region @ 90%CL



$$P(\nu_{\mu} \rightarrow \nu_e) = 4\text{Re} \left[ U_{e3}U_{\mu 3}^* (U_{e3}^*U_{\mu 3} + U_{e4}^*U_{\mu 4}) \right] \sin^2 \left( \frac{\Delta m_{31}^2 L}{4E} \right) + \dots$$

### 3.1.3 HK $\nu_{\text{atm}}$

HK, arXiv:1805.04163v2



**HK Sensitivity to  $\theta_{34}$  ( $\theta_{24}$ ) is (is not much) improved compared to SK:**  
**90% CL (solid)**  
**99% CL (dashed)**

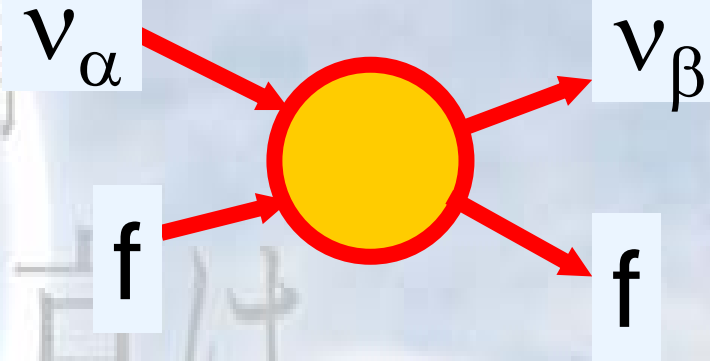


## 3.2 NSI in propagation

### 3.2.1 Features of NSI in propagation

Phenomenological **New Physics** considered in this talk: 4-fermi **Non Standard Interactions**:

$$\mathcal{L}_{eff} = G_{NP}^{\alpha\beta} \bar{\nu}_\alpha \gamma^\mu \nu_\beta \bar{f} \gamma_\mu f'$$



neutral current  
non-standard  
interaction

### Modification of matter effect

$$i \frac{d}{dt} \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \left[ U \text{diag}(E_1, E_2, E_3) U^{-1} + A \begin{pmatrix} 1 & +\epsilon_{ee} & \epsilon_{e\mu} & \epsilon_{e\tau} \\ \epsilon_{\mu e} & \epsilon_{\mu\mu} & \epsilon_{\mu\tau} \\ \epsilon_{\tau e} & \epsilon_{\tau\mu} & \epsilon_{\tau\tau} \end{pmatrix} \right] \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix}$$

$$A \equiv \sqrt{2} G_F N_e \quad N_e \equiv \text{electron density}$$

NP

● NSI for solar  $\nu$ :  $\epsilon_{\alpha\beta}$  vs  $(\epsilon_D, \epsilon_N)$

In solar  $\nu$  analysis,  $\Delta m_{31}^2 \rightarrow$  infinity,  $H \rightarrow H^{\text{eff}}$ , the problem is reduced to the 2 flavor case:

$$H^{\text{eff}} = \frac{\Delta m_{21}^2}{4E} \begin{pmatrix} -\cos 2\theta_{12} & \sin 2\theta_{12} \\ \sin 2\theta_{12} & \cos 2\theta_{12} \end{pmatrix} + \begin{pmatrix} c_{13}^2 A & 0 \\ 0 & 0 \end{pmatrix} + A \sum_{f=e,u,d} \frac{N_f}{N_e} \begin{pmatrix} -\epsilon_D^f & \epsilon_N^f \\ \epsilon_N^{f*} & \epsilon_D^f \end{pmatrix}$$

$(\epsilon_D^f, \epsilon_N^f)$  are related by  $\epsilon_{\alpha\beta}^f$ :

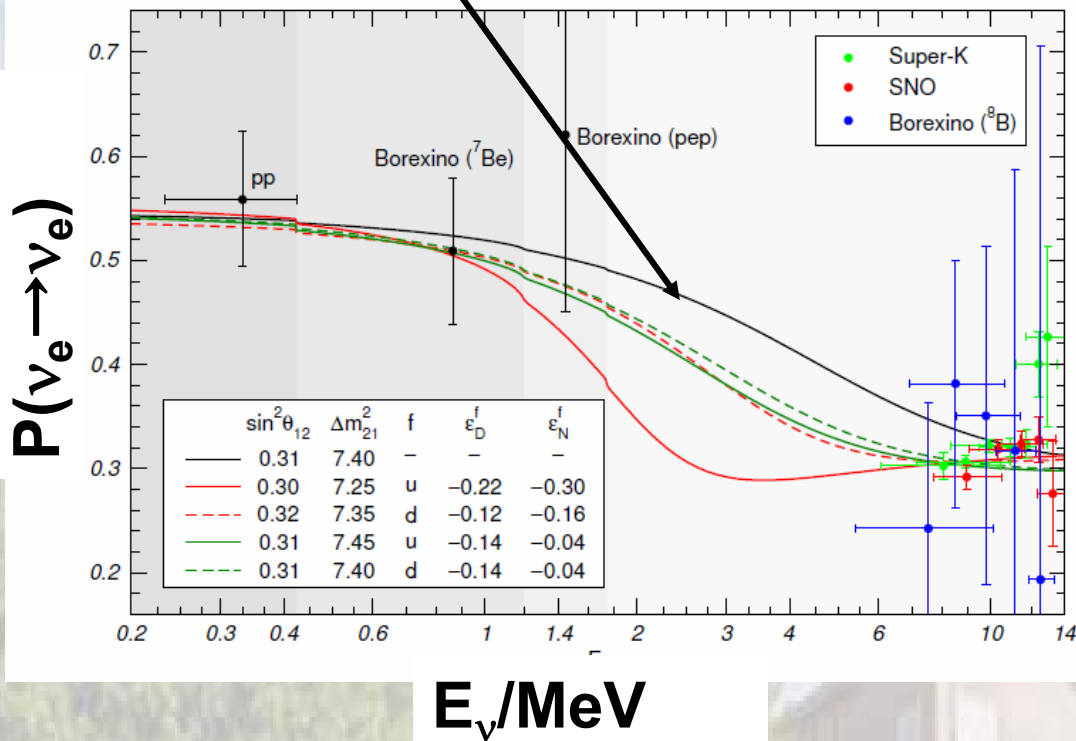
$$\begin{aligned} \epsilon_D^f &= c_{13}s_{13}\text{Re} \left[ e^{i\delta_{\text{CP}}} \left( s_{23}\epsilon_{e\mu}^f + c_{23}\epsilon_{e\tau}^f \right) \right] - \left( 1 + s_{13}^2 \right) c_{23}s_{23}\text{Re} \left[ \epsilon_{\mu\tau}^f \right] \\ &\quad - \frac{c_{13}^2}{2} \left( \epsilon_{ee}^f - \epsilon_{\mu\mu}^f \right) + \frac{s_{23}^2 - s_{13}^2 c_{23}^2}{2} \left( \epsilon_{\tau\tau}^f - \epsilon_{\mu\mu}^f \right) \\ \epsilon_N^f &= c_{13} \left( c_{23}\epsilon_{e\mu}^f - s_{23}\epsilon_{e\tau}^f \right) + s_{13}e^{-i\delta_{\text{CP}}} \left[ s_{23}^2\epsilon_{\mu\tau}^f - c_{23}^2\epsilon_{\mu\tau}^{f*} + c_{23}s_{23} \left( \epsilon_{\tau\tau}^f - \epsilon_{\mu\mu}^f \right) \right] \end{aligned}$$

**f = e, u or d**

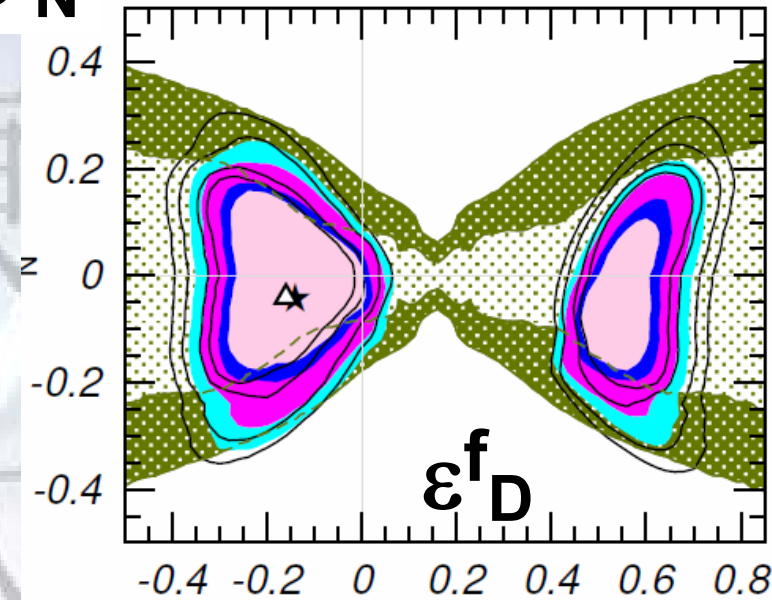
# Tension between solar $\nu$ & KamLAND data comes from little observation of upturn by SK & SNO

Gonzalez-Garcia, Maltoni, JHEP 1309 (2013) 152

Standard scenario w/  $\Delta m_{21}^2$  by KamLAND



$\epsilon_N^f$



Best fit value of global fit

$$(\epsilon_D^u, \epsilon_N^u) = (-0.140, -0.030)$$

$$(\epsilon_D^d, \epsilon_N^d) = (-0.145, -0.036)$$

**In solar  $\nu$  analysis,  $(\epsilon_D, \epsilon_N)$  was used:**

$$U = R_{23}(\theta_{23}, 0) R_{13}(\theta_{13}, \delta_{13}) R_{12}(\theta_{12}, 0)$$

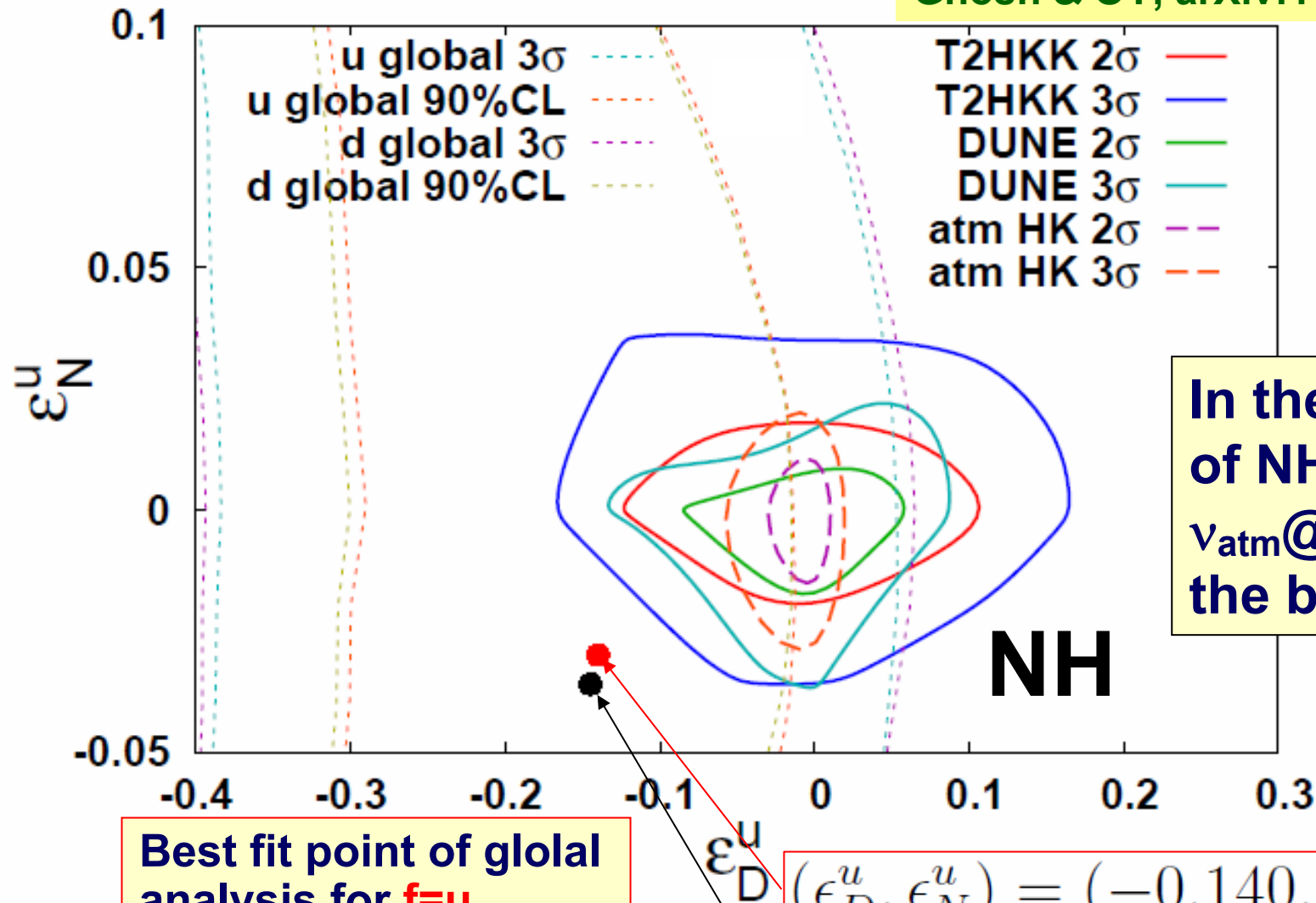
$$(\epsilon'_{\alpha\beta}) \equiv R_{13}^{-1}(\theta_{13}, \delta_{13}) R_{23}^{-1}(\theta_{23}, 0) (\epsilon_{\alpha\beta}) R_{23}(\theta_{23}, 0) R_{13}(\theta_{13}, \delta_{13})$$

$$\equiv \begin{pmatrix} \epsilon'_{11} & \epsilon'_{12} & \epsilon'_{13} \\ \epsilon'_{21} & \epsilon'_{22} & \epsilon'_{23} \\ \epsilon'_{31} & \epsilon'_{32} & \epsilon'_{33} \end{pmatrix} = \begin{pmatrix} \frac{\epsilon'_{11} + \epsilon'_{22}}{2} - \epsilon_D & \epsilon_N & \epsilon'_{13} \\ \epsilon_N^* & \frac{\epsilon'_{11} + \epsilon'_{22}}{2} + \epsilon_D & \epsilon'_{23} \\ \epsilon'_{31} & \epsilon'_{32} & \epsilon'_{33} \end{pmatrix}$$

**-> Also for analysis of  $\nu_{\text{atm}}$  & LBL,  $(\epsilon_D, \epsilon_N)$  will be used instead of  $\epsilon_{\alpha\beta}$ .**

### 3.2.2 Comparison of sensitivity T2HKK, DUNE, $\nu_{\text{atm}}@HK$

Ghosh & OY, arXiv:1709.08264



Best fit point of global analysis for  $f=u$

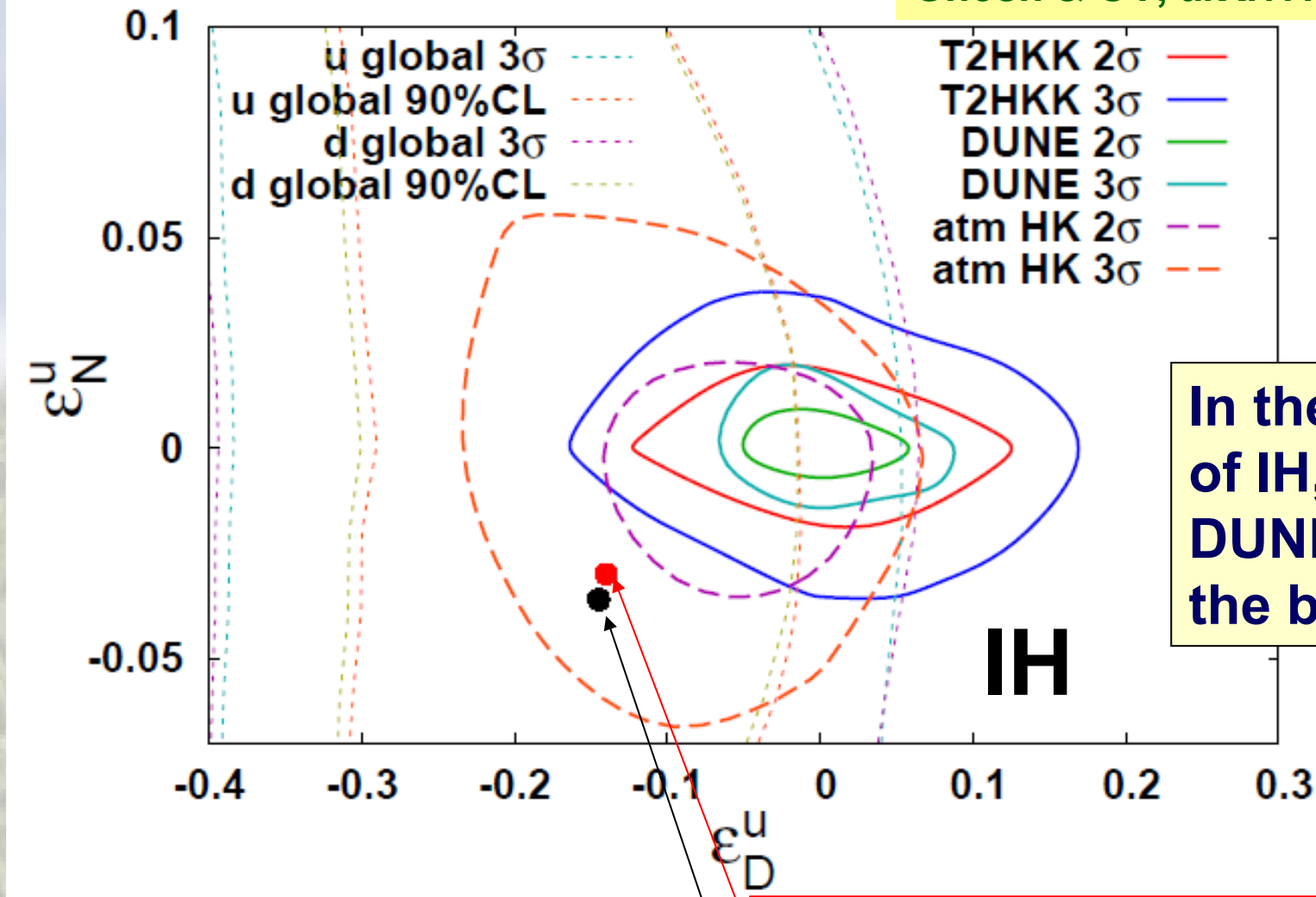
Best fit point of global analysis for  $f=d$

$$(\epsilon_D^u, \epsilon_N^u) = (-0.140, -0.030)$$

$$(\epsilon_D^d, \epsilon_N^d) = (-0.145, -0.036)$$

# Comparison of sensitivity T2HKK, DUNE, $\nu_{\text{atm}}@HK$

Ghosh & OY, arXiv:1709.08264



In the case of IH, DUNE is the best

$$(\epsilon_D^u, \epsilon_N^u) = (-0.140, -0.030)$$

$$(\epsilon_D^d, \epsilon_N^d) = (-0.145, -0.036)$$

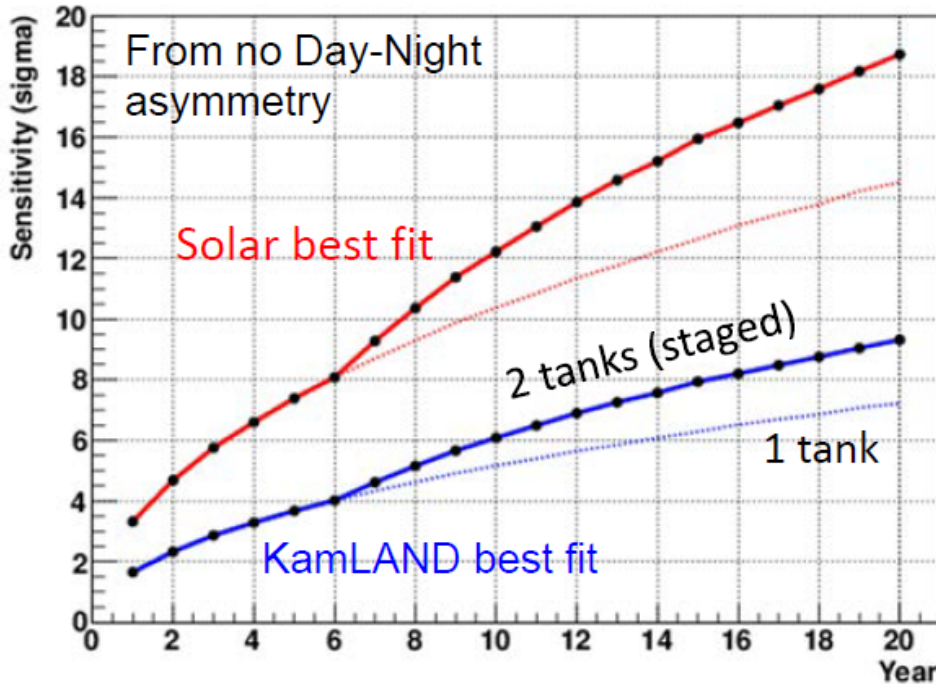


# Sensitivity $\nu_{\text{solar}}@HK$

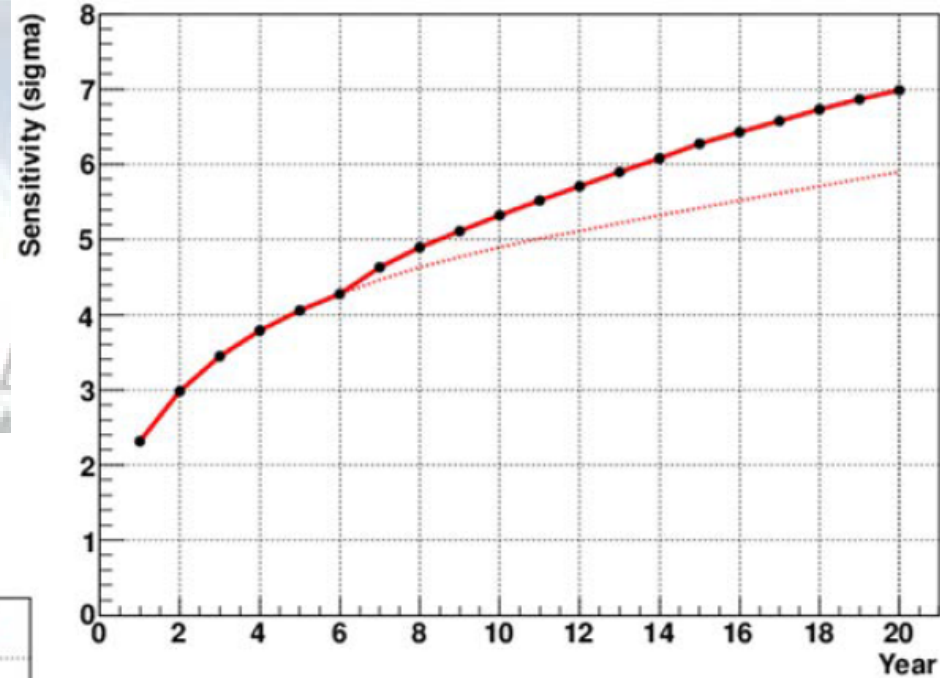
Kajita @ NOW2016

$\nu_{\text{solar}}@HK$  will tell us whether deviation from the PMNS paradigm exists

## Day-night asymmetry sensitivity



## Spectrum upturn discovery sensitivity



## 4. Summary

- In the standard 3 flavor  $\nu$  scenario, the 3 mixing angles have been roughly determined, and we have some indication for  $\Delta m^2_{31} > 0$ ,  $\theta_{23} > \pi/4$ ,  $\delta \neq 0$ .
- T2HK &  $\nu_{\text{atm}}@HK$  will determine Mass Hierarchy and Octant (unless  $|\pi/4 - \theta_{23}|$  is small) and  $\delta$ .
- T2HK,  $\nu_{\text{atm}}@HK$ ,  $\nu_{\text{solar}}@HK$ , T2HKK are expected to constrain the two scenarios, which may be suggested by experiments, beyond the standard 3 flavor  $\nu$  scenario:  
 $\nu_s$  & NSI in propagation.



2020年4月

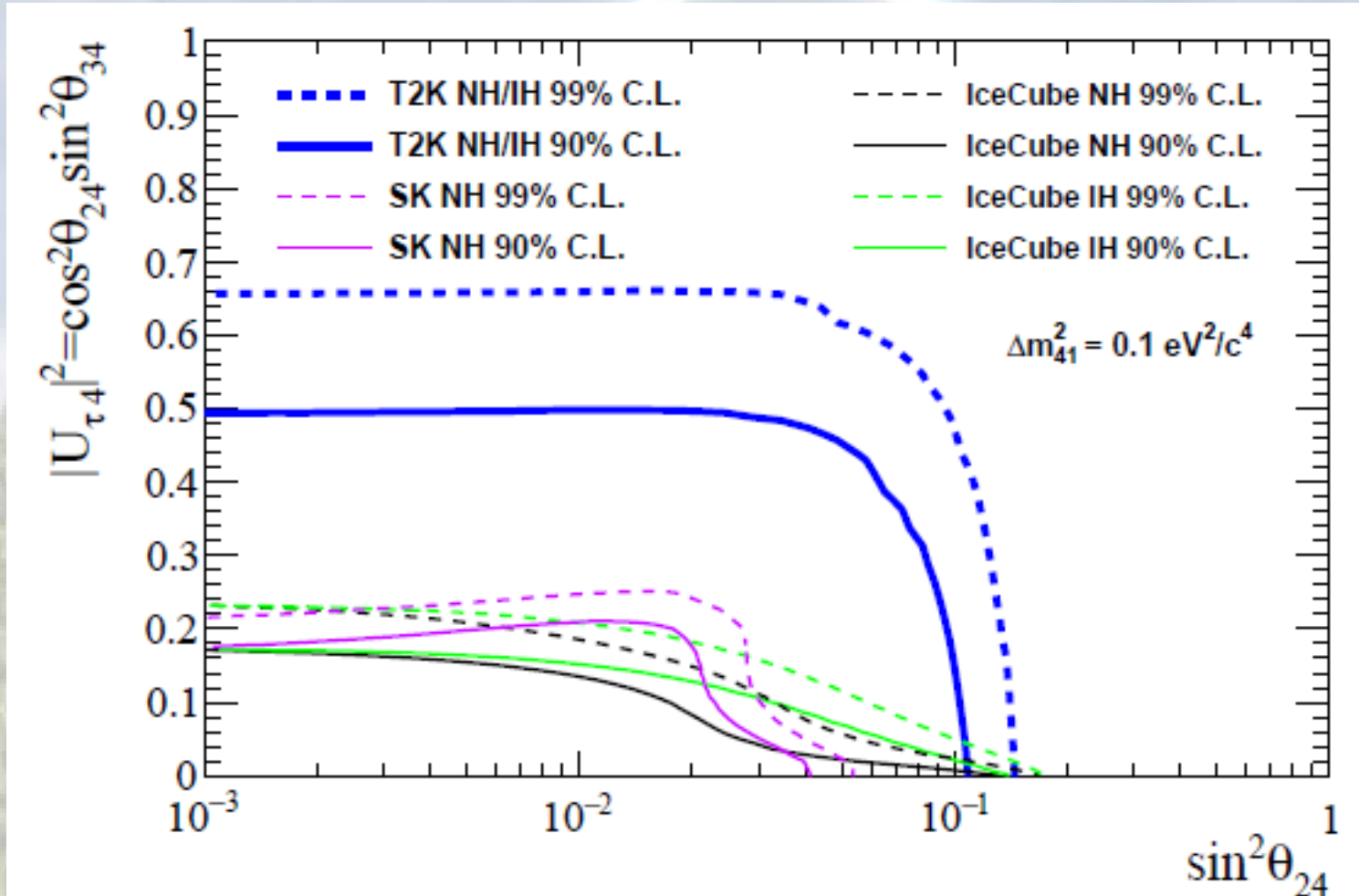
首都大学東京は、  
**Backup slides**  
東京都立大学へ。

# Parametrization of the 4x4 matrix

$$U = R_{34}(\theta_{34}, 0) R_{24}(\theta_{24}, \delta_3) R_{23}(\theta_{23}, 0) R_{14}(\theta_{14}, \delta_1) R_{13}(\theta_{13}, \delta_2) R_{12}(\theta_{12}, 0)$$

$$\left\{ \begin{array}{l} U_{e1} = c_{12}c_{13}c_{14} \\ U_{e2} = c_{13}c_{14}s_{12} \\ U_{e3} = c_{14}s_{13}e^{-i\delta_2} \\ U_{e4} = s_{14}e^{-i\delta_1} \\ U_{\mu 4} = c_{14}s_{24}e^{-i\delta_3} \\ U_{\tau 4} = c_{14}c_{24}s_{34} \\ U_{s4} = c_{14}c_{24}c_{34} \end{array} \right.$$

# Present bounds on $\theta_{24}$ & $\theta_{34}$



T2K, PRD99 ('19) 071103

# Constraints on $\epsilon_{\alpha\beta}$ for expts on Earth

Davidson et al., JHEP 0303:011,2003; Berezhiani, Rossi, PLB535 ('02) 207; Barranco et al., PRD73 ('06) 113001; Barranco et al., arXiv:0711.0698

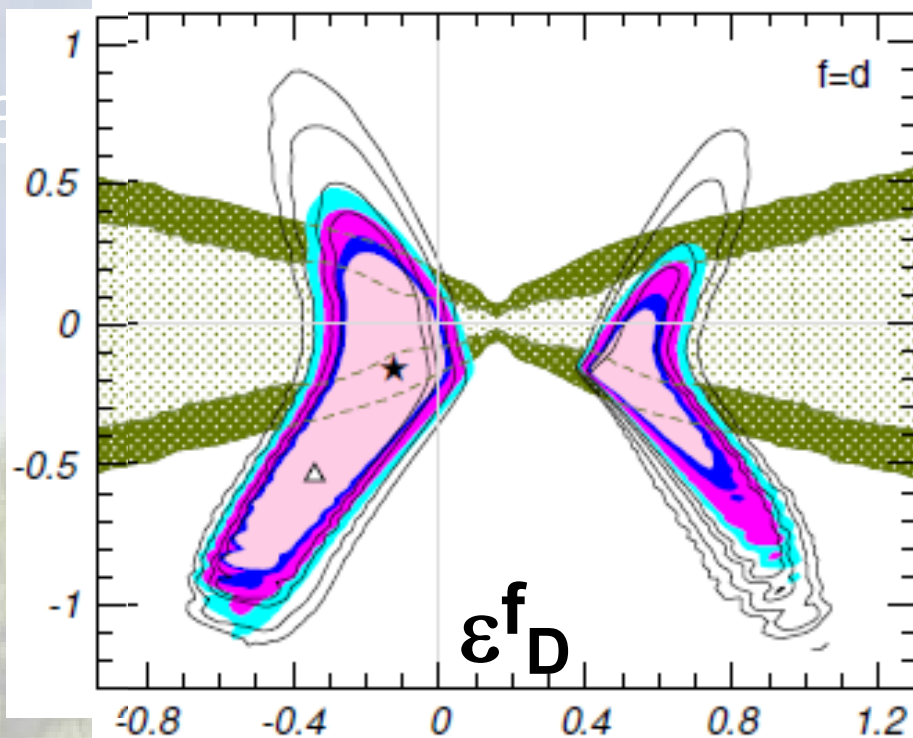
Biggio et al., JHEP 0908, 090 (2009) w/o 1-loop arguments

**Constraints are weak**

$$\left( \begin{array}{ll} |\epsilon_{ee}| \lesssim 4 \times 10^0 & |\epsilon_{e\mu}| \lesssim 3 \times 10^{-1} \\ & |\epsilon_{\mu\mu}| \lesssim 7 \times 10^{-2} \end{array} \right) \quad \left( \begin{array}{l} |\epsilon_{e\tau}| \lesssim 3 \times 10^0 \\ |\epsilon_{\mu\tau}| \lesssim 3 \times 10^{-1} \\ |\epsilon_{\tau\tau}| \lesssim 2 \times 10^1 \end{array} \right)$$

# Tension between solar $\nu$ & KamLAND can be solved by NSI

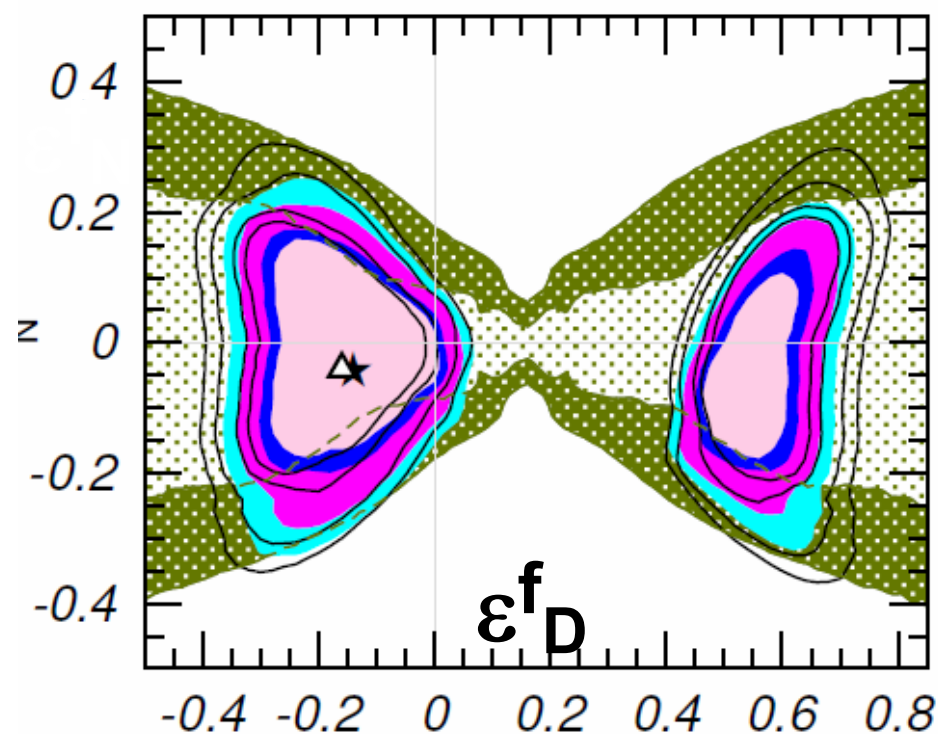
Gonzalez-Garcia, Maltoni, JHEP 1309 (2013) 152



## Best fit value of solar-KL

$$(\epsilon_D^u, \epsilon_N^u) = (-0.22, -0.30)$$

$$(\epsilon_D^d, \epsilon_N^d) = (-0.12, -0.16)$$

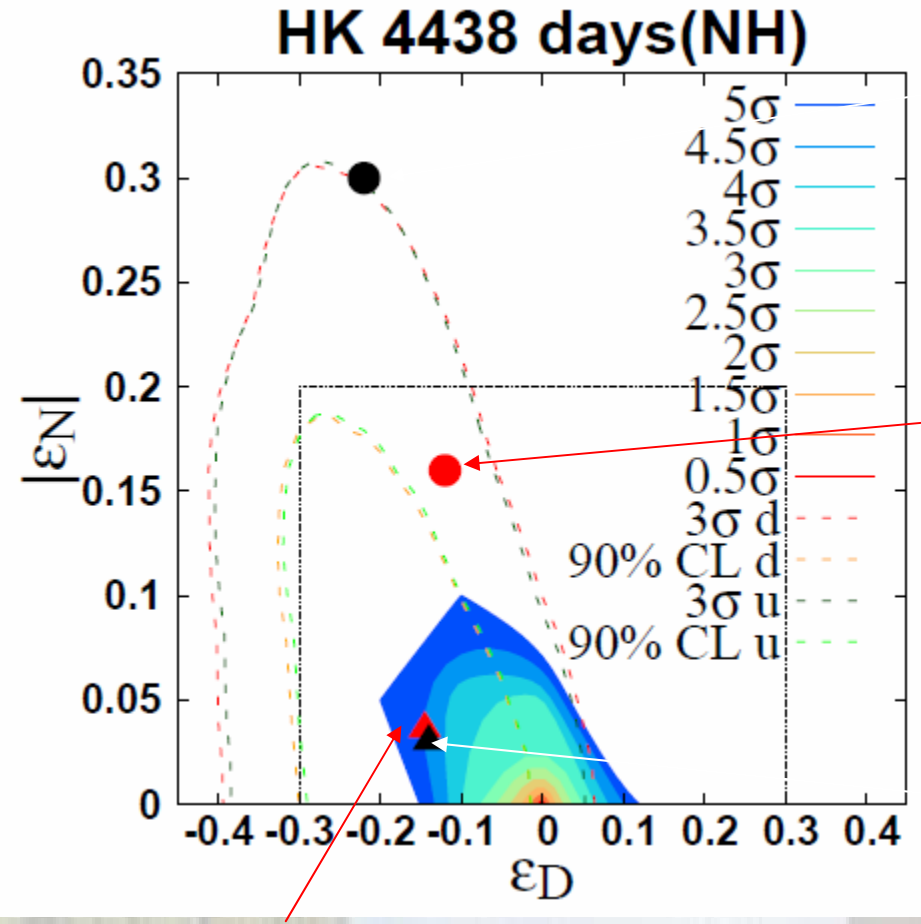


## Best fit value of global fit

$$(\epsilon_D^u, \epsilon_N^u) = (-0.140, -0.030)$$

$$(\epsilon_D^d, \epsilon_N^d) = (-0.145, -0.036)$$

# Sensitivity of HK: (1) Complex $|\epsilon_N|$ for NH



$$(\epsilon_D^u, \epsilon_N^u) = (-0.22, -0.30)$$

**Best fit point of solar & KamLAND for  $f=u$ :  
significance: 38 $\sigma$**

$$(\epsilon_D^d, \epsilon_N^d) = (-0.12, -0.16)$$

**Best fit point of solar & KamLAND for  $f=d$ :  
significance: 11 $\sigma$**

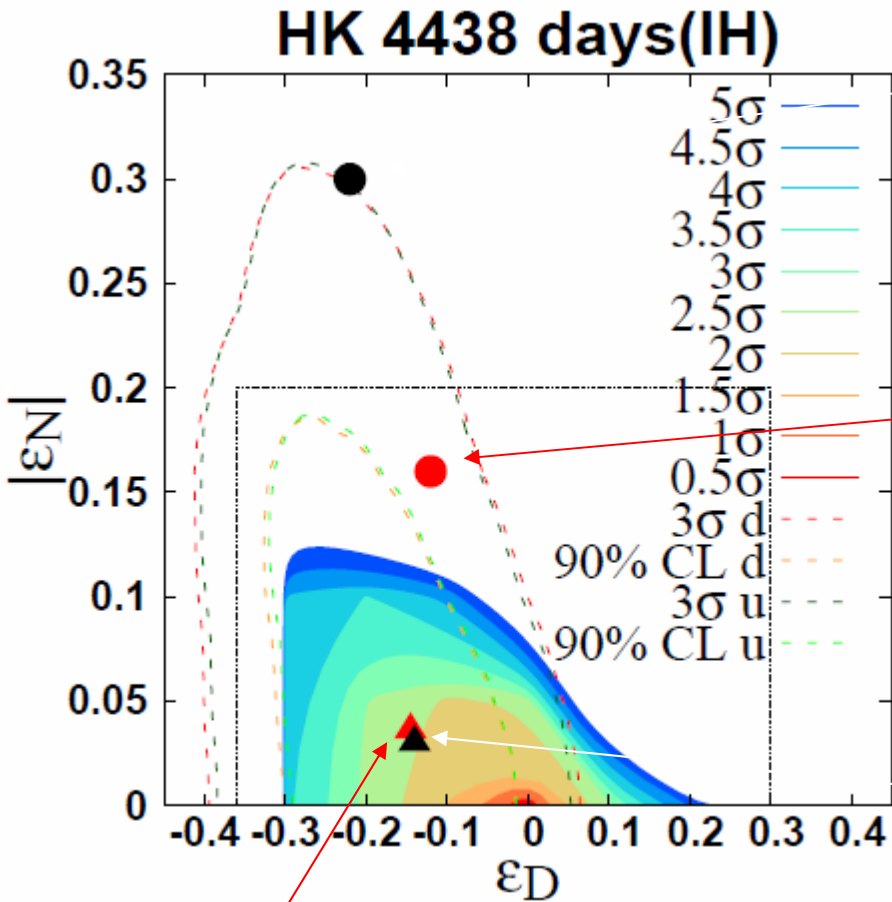
$$(\epsilon_D^u, \epsilon_N^u) = (-0.140, -0.030)$$

**Best fit point of global analysis for  $f=u$ :  
significance: 5 $\sigma$**

$$(\epsilon_D^d, \epsilon_N^d) = (-0.145, -0.036)$$

**Best fit point of global analysis for  $f=d$ :  
significance: 5 $\sigma$**

# Sensitivity of HK: (1) Complex $|\epsilon_N|$ for IH



$$(\epsilon_D^u, \epsilon_N^u) = (-0.22, -0.30)$$

**Best fit point of solar & KamLAND for  $f=u$ : significance: 35 $\sigma$**

$$(\epsilon_D^d, \epsilon_N^d) = (-0.12, -0.16)$$

**Best fit point of solar & KamLAND for  $f=d$ : significance: 8 $\sigma$**

$$(\epsilon_D^u, \epsilon_N^u) = (-0.140, -0.030)$$

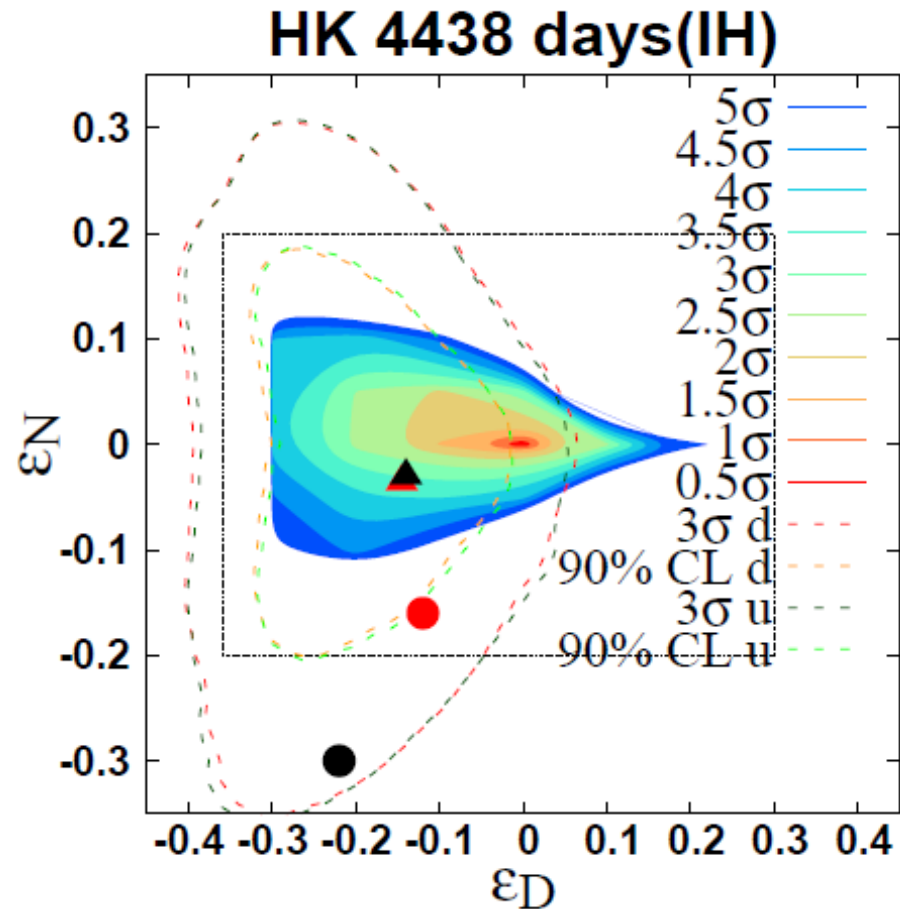
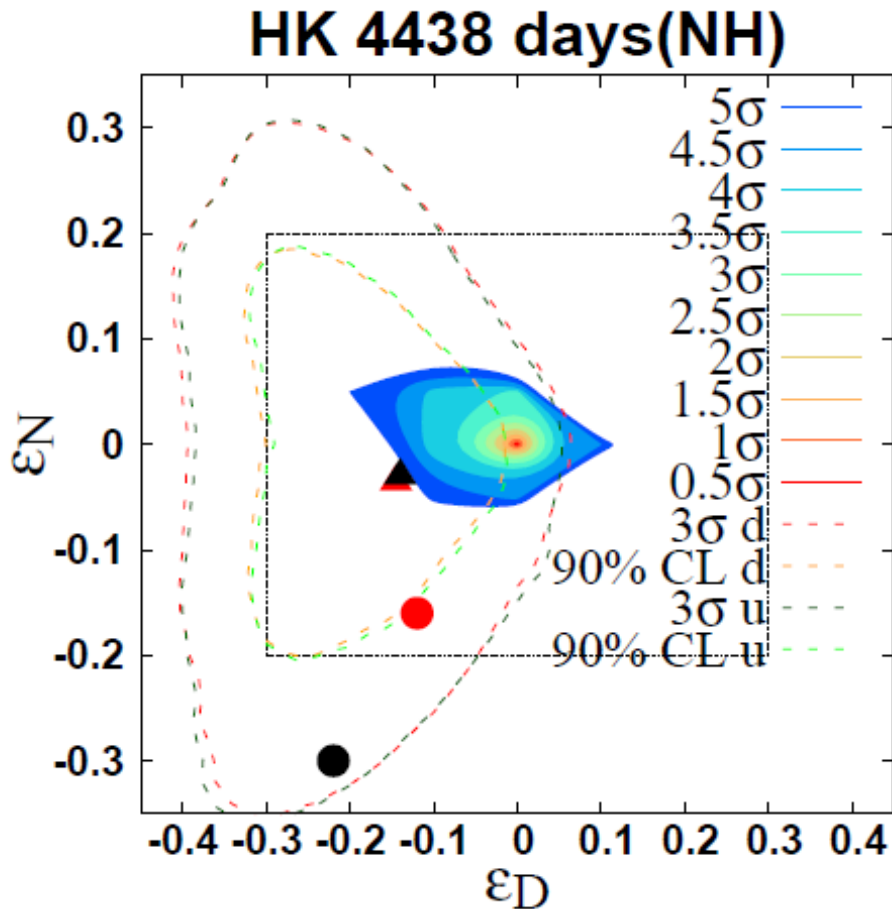
**Best fit point of global analysis for  $f=u$ : significance: 1.4 $\sigma$**

$$(\epsilon_D^d, \epsilon_N^d) = (-0.145, -0.036)$$

**Best fit point of global analysis for  $f=d$ : significance: 1.5 $\sigma$**



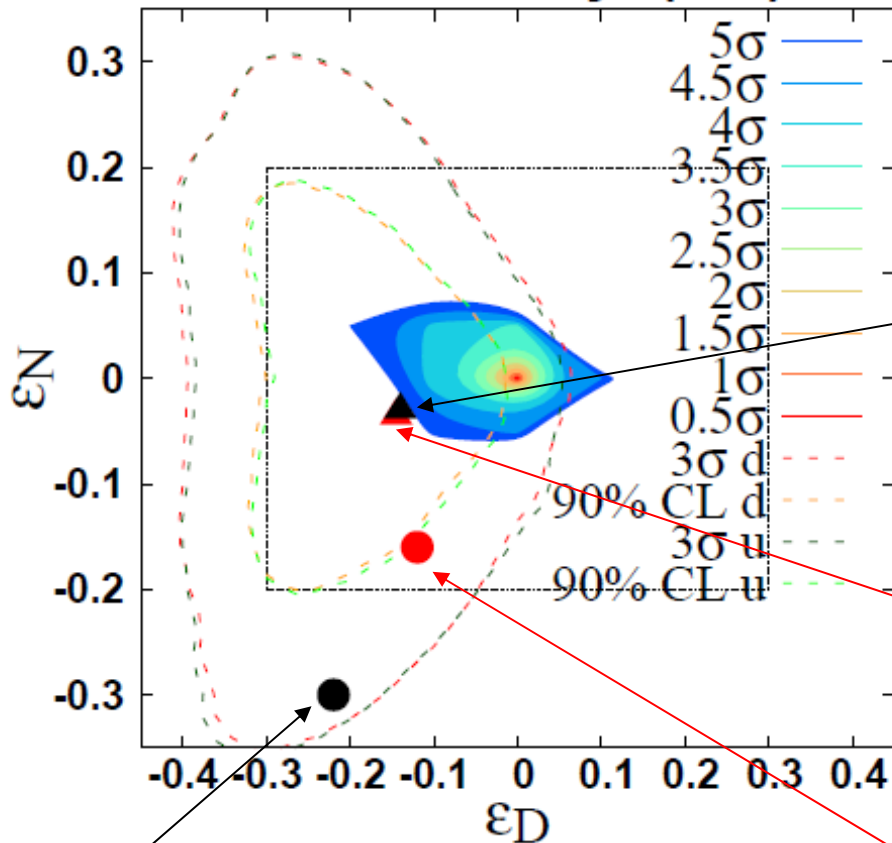
# Sensitivity of HK: (2) Real $|\epsilon_N|$



**Allowed regions and significance are similar to the case for complex  $\epsilon_N$**



HK 4438 days(NH)



HK  $\nu_{\text{atm}}$  has sensitivity to some region of the  $\nu_{\text{solar}}$  anomaly

$$(\epsilon_D^u, \epsilon_N^u) = (-0.140, -0.030)$$

Best fit point of global analysis for  $f=u$ : significance:  $5\sigma$

$$(\epsilon_D^d, \epsilon_N^d) = (-0.145, -0.036)$$

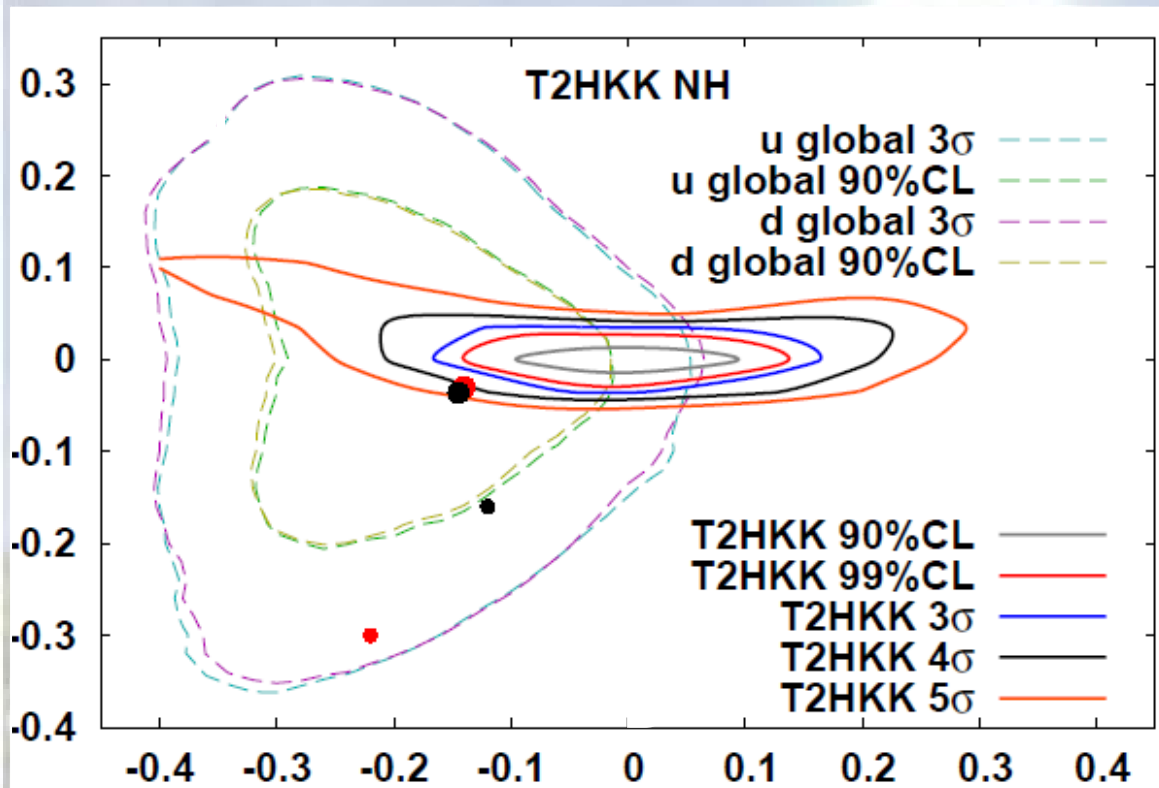
Best fit point of global analysis for  $f=d$ : significance:  $5\sigma$

$$(\epsilon_D^d, \epsilon_N^d) = (-0.12, -0.16)$$

Best fit point of solar & KamLAND for  $f=d$ : significance:  $11\sigma$

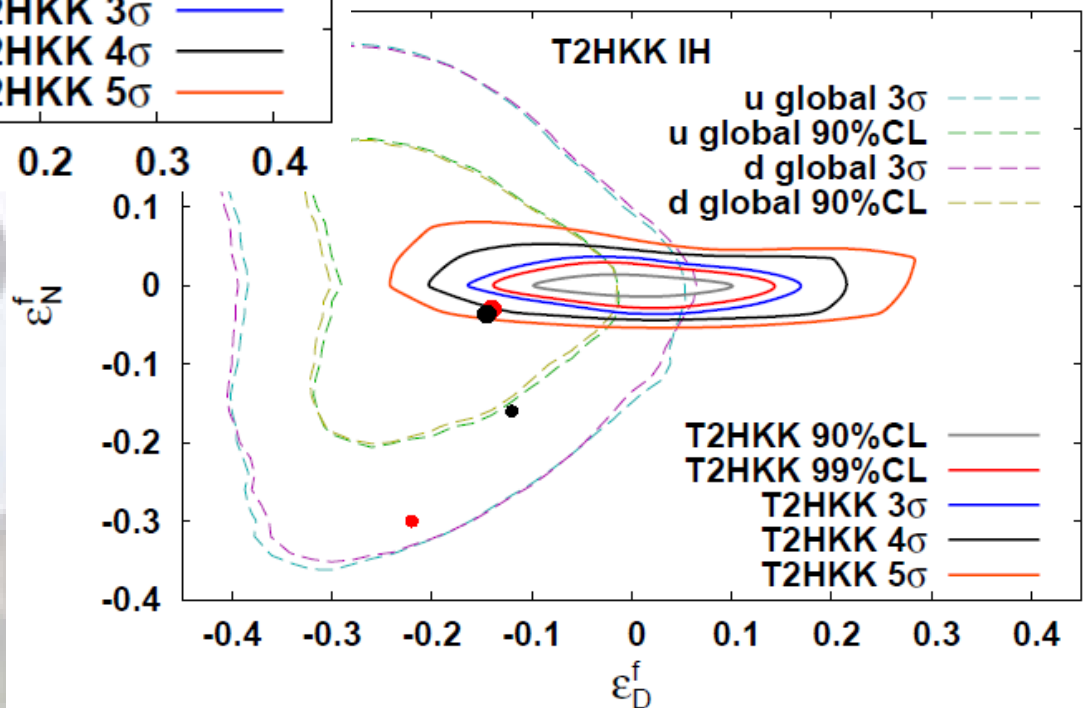
$$(\epsilon_D^u, \epsilon_N^u) = (-0.22, -0.30)$$

Best fit point of solar & KamLAND for  $f=u$ : significance:  $38\sigma$



**Excluded region by LBL is outside of the curve**

$$\delta(\text{true}) = -90^\circ$$



# Dependence of T2HKK on $\theta_{23}$ (true) & $\delta$ (true)

