

# Search for sterile neutrinos at reactors

Osamu Yasuda  
Tokyo Metropolitan University

16 December, 2011



- 1. Introduction**
- 2. Sterile neutrino oscillations at reactors**
- 3. Summary**

**Based on OY,**

**arXiv:1107.4766 [hep-ph], 1110.2579 [hep-ph]**

# 1. Introduction

## 1.1 $\nu$ oscillation

### Mass eigenstates

$$i \frac{d}{dt} \begin{pmatrix} \mathbf{v}_1 \\ \mathbf{v}_2 \end{pmatrix} = \begin{pmatrix} E_1 & 0 \\ 0 & E_2 \end{pmatrix} \begin{pmatrix} \mathbf{v}_1 \\ \mathbf{v}_2 \end{pmatrix}$$

$$E_j \equiv \sqrt{\vec{p}^2 + m_j^2}$$

### Flavor eigenstates

$$\begin{pmatrix} \mathbf{v}_\mu \\ \mathbf{v}_\tau \end{pmatrix} = U \begin{pmatrix} \mathbf{v}_1 \\ \mathbf{v}_2 \end{pmatrix}$$

$$U \equiv \begin{pmatrix} U_{\mu 1} & U_{\mu 2} \\ U_{\tau 1} & U_{\tau 2} \end{pmatrix}$$

### Probability of flavor conversion

$$P(\mathbf{v}_\mu \rightarrow \mathbf{v}_\tau) = \sin^2 2\theta \sin^2 \left( \frac{\Delta E L}{2} \right)$$

$$\Delta E = E_2 - E_1 \cong \frac{m_2^2 - m_1^2}{2E} = \frac{\Delta m^2}{2E}$$

# 1.2 Framework of 3 flavor $\nu$ oscillation

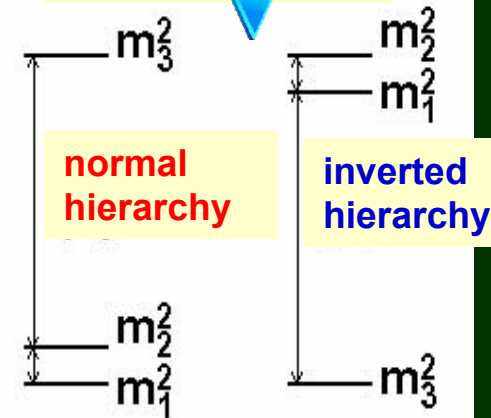
## Mixing matrix

Functions of mixing angles

$\theta_{12}$ ,  $\theta_{23}$ ,  $\theta_{13}$ ,  
and CP phase  $\delta$

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

Both hierarchy patterns are allowed



# 1.3 Information we have obtained so far

$\nu_{\text{solar}}$  + KamLAND (reactor)

$$\theta_{12} \cong \frac{\pi}{6}, \Delta m_{21}^2 \cong 8 \times 10^{-5} \text{ eV}^2$$

$\nu_{\text{atm}}$  + K2K, MINOS (accelerators)

$$\theta_{23} \cong \frac{\pi}{4}, |\Delta m_{32}^2| \cong 2.5 \times 10^{-3} \text{ eV}^2$$

DCHOOZ (reactor)  
+ T2K + MINOS + others

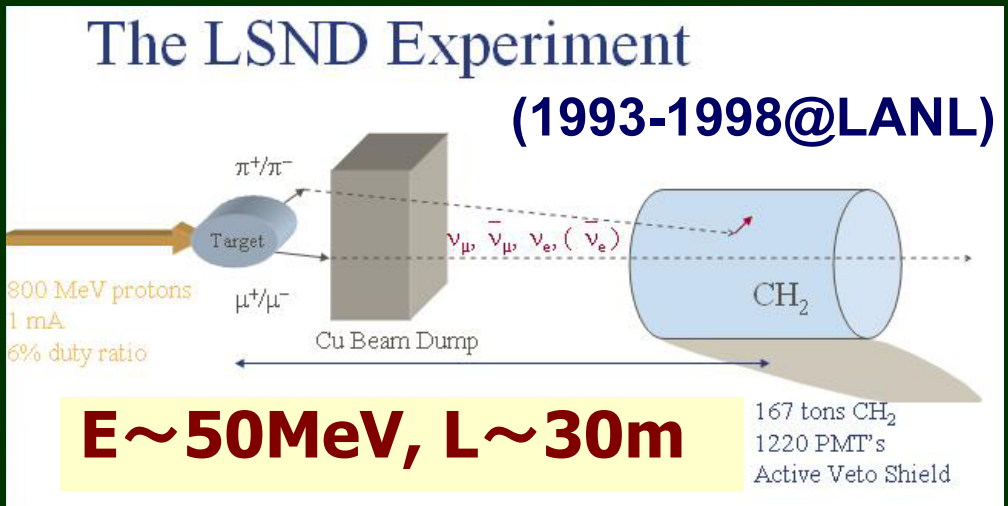
$$\theta_{13} \cong 0.14^{+0.02}_{-0.03}$$

**New!!**

# 1.4 Hints for beyond $N_\nu=3$ oscillation

● **LNSD experiment**

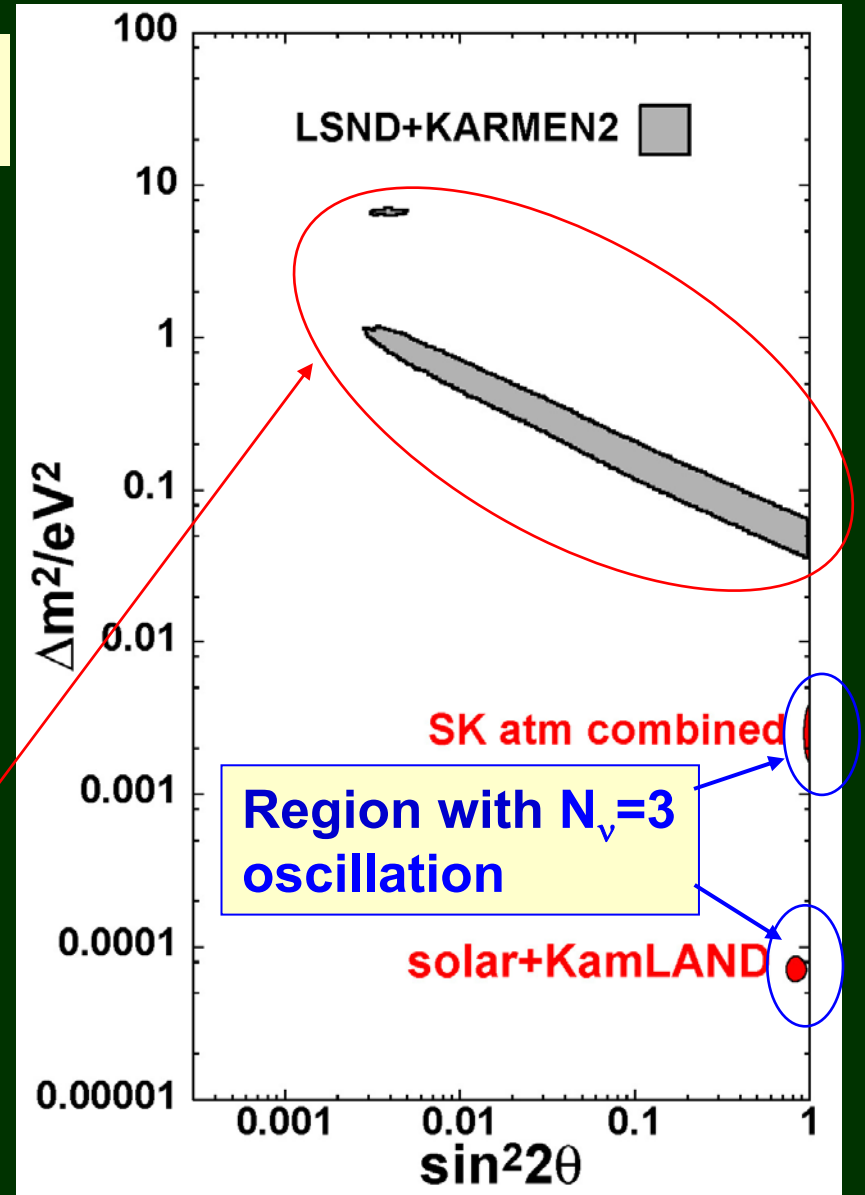
$$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$$



➔  $\Delta m^2 \cong \mathcal{O}(1)\text{eV}^2$  ??

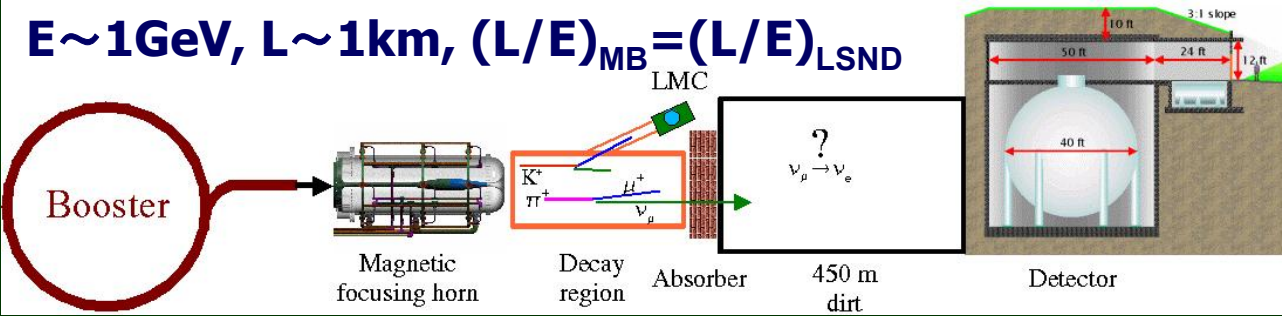
$\sin^2 2\theta \cong \mathcal{O}(10^{-2})$

**This region cannot be explained by  $N_\nu=3$  oscillation**



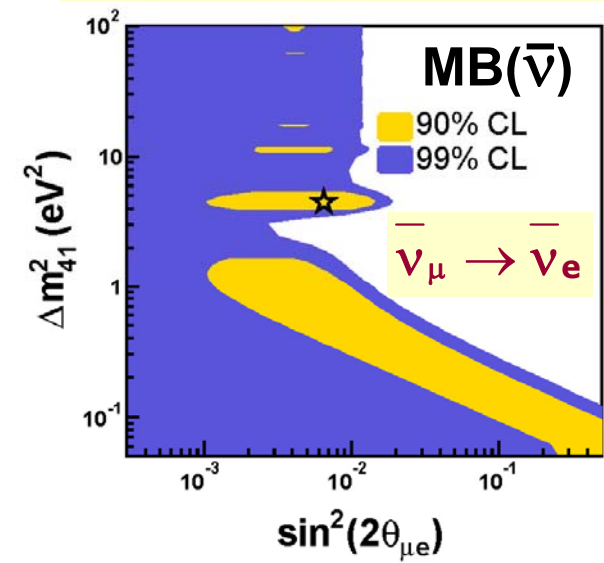
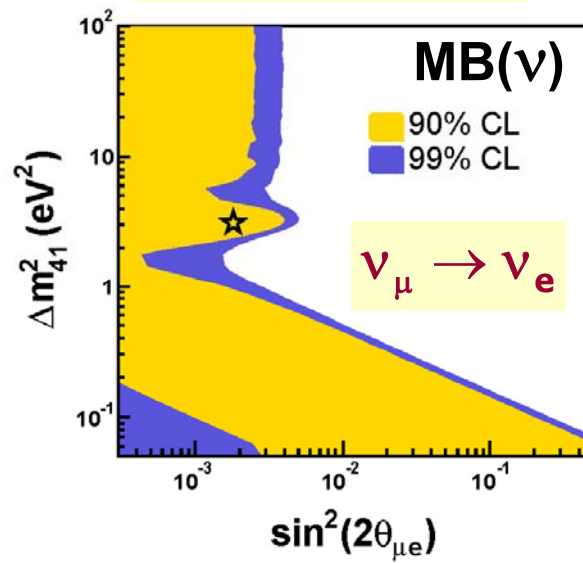
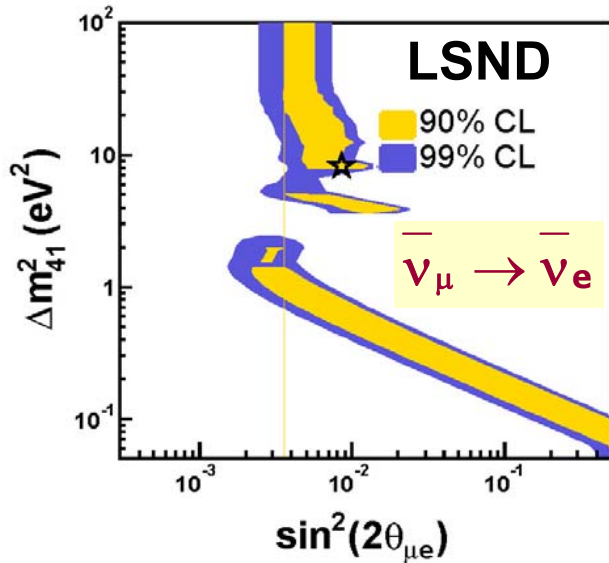
● MiniBooNE (2002-, FNAL)

Check of the LSND data



$\nu$  mode(2007)  
(negative)

anti- $\nu$  mode(2010)  
(affirmative)



1995  
Is LSND correct?

2007  
LSND was wrong!

2010  
LSND was correct?

Note the time dependence of reputation of  $\nu_s$  scenarios!

# ● Reactor $\nu$ anomaly

Mention et al, 2011

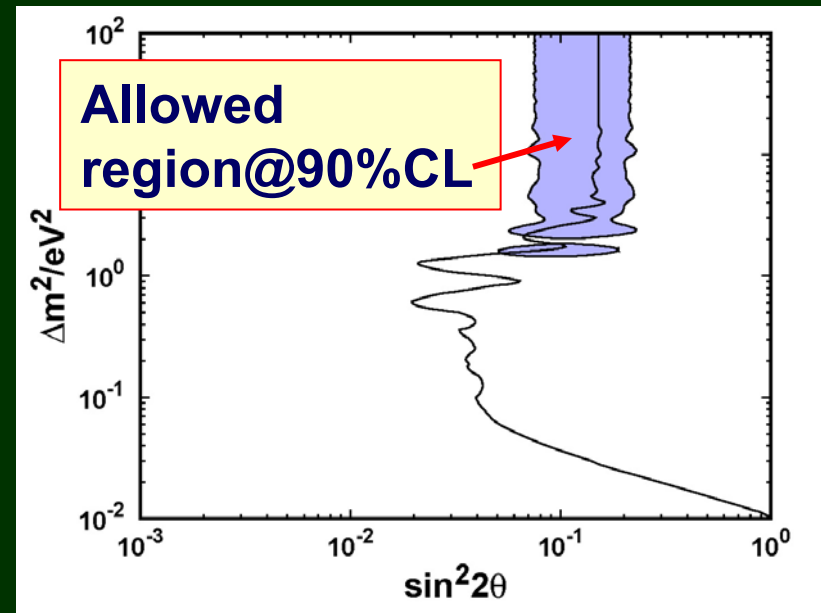
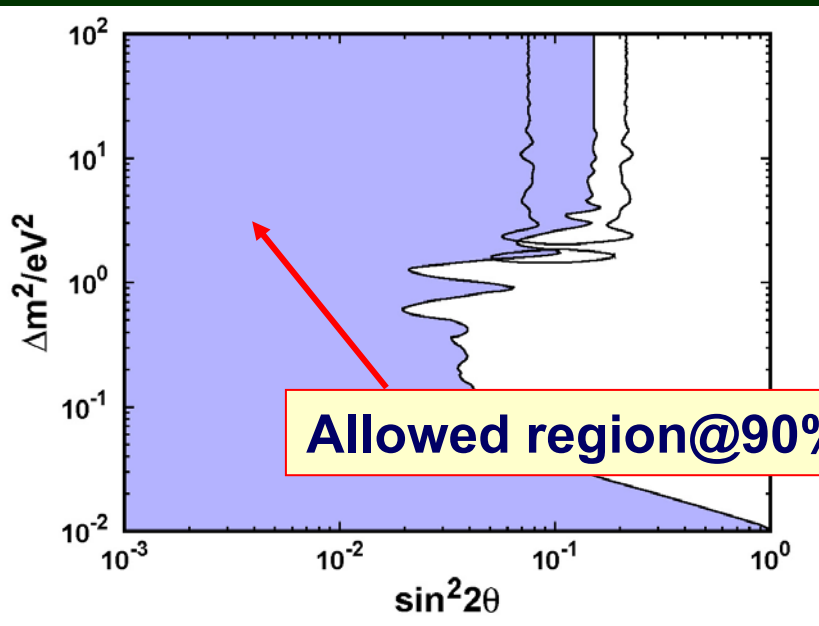
Recent reevaluation of reactor  $\nu$  flux suggests affirmative interpretation of  $\bar{\nu}_e \rightarrow \bar{\nu}_e$  oscillation

**(new flux) = (old flux) x 1.03**

Bugey(reactor  $\bar{\nu}_e \rightarrow \bar{\nu}_e$ ):  
**Negative w/ old flux**



Bugey(reactor)+etc:  
**Affirmative w/ new flux?**



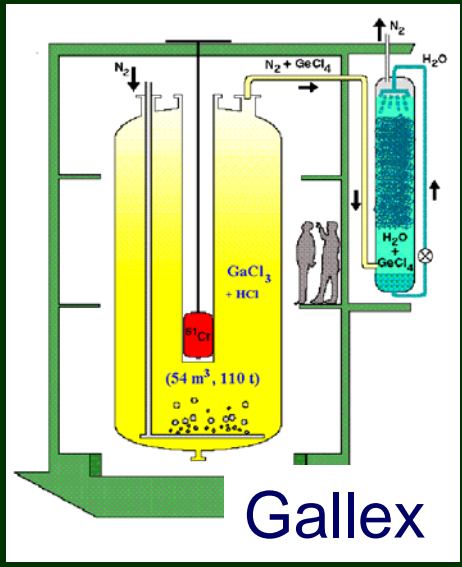
No  $\nu$  oscillation for  
 $\Delta m_{41}^2 = 0(1) \text{ eV}^2$



$\nu$  oscillation may exist for  
 $\Delta m_{41}^2 = 0(1) \text{ eV}^2$

● Gallium anomaly

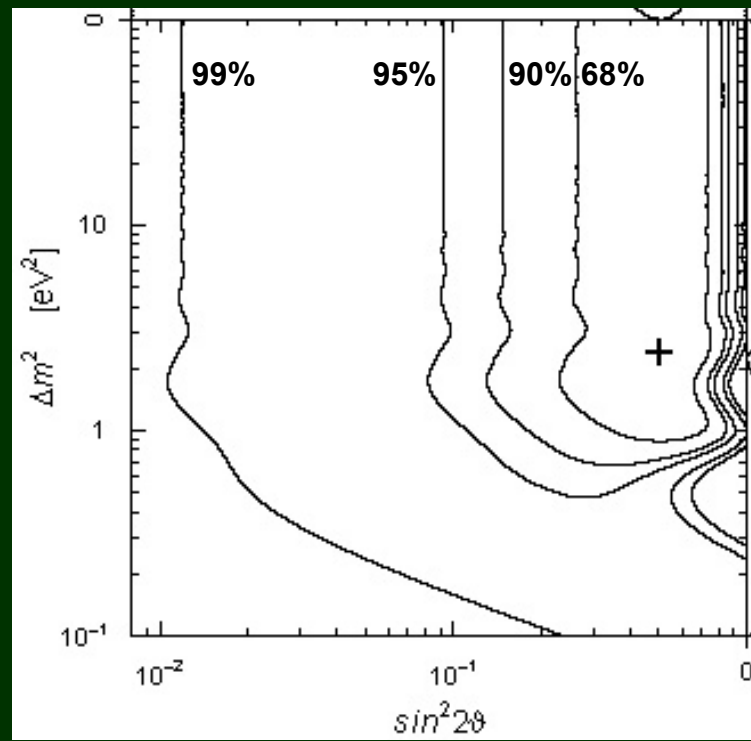
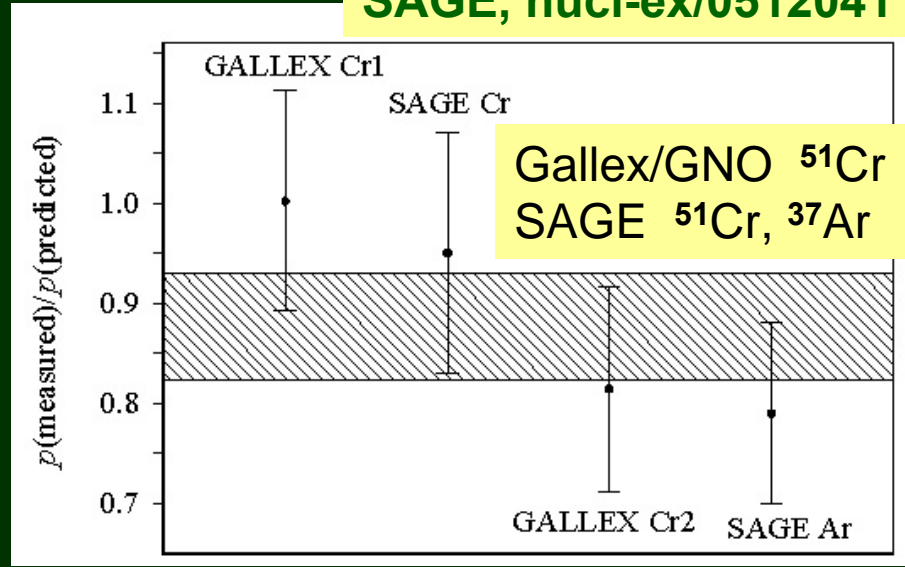
Gallium radioactive source experiments



$$R \equiv \frac{p(\text{measured})}{p(\text{predicted})} = 0.88 \pm 0.05(1\sigma)$$

Giunti-Laveder, 1006.3244v3 [hep-ph]

Results of the Ga radioactive source calibration experiments may be interpreted as an indication of the disappearance of  $\nu_e$  due to active-sterile oscillations.





## 1.5 $N_\nu = 4$ schemes

Because of the hierarchy:  $\Delta m_{\text{sol}}^2 \ll \Delta m_{\text{atm}}^2 \ll \Delta m_{\text{LSND}}^2$

$N_\nu = 3$  schemes can't explain LSND.

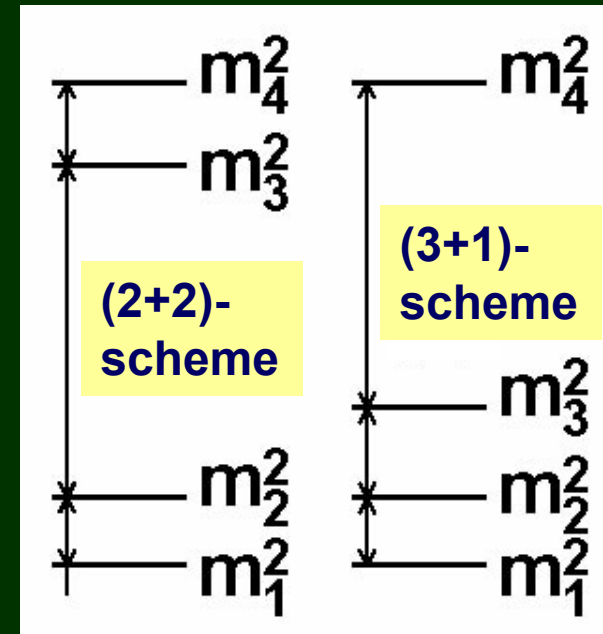
$N_\nu = 4$  schemes may be able to explain all.

$$\Delta m_{21}^2 = \Delta m_{\text{sol}}^2, \Delta m_{32}^2 = \Delta m_{\text{atm}}^2, \Delta m_{43}^2 = \Delta m_{\text{LSND}}^2$$

LEP  $\Rightarrow$  4<sup>th</sup>  $\nu$  has to be sterile

(2+2)-scheme is excluded by solar + atmospheric  $\nu$

$\Rightarrow$  (3+1)-scheme will be discussed



# (3+1)-scheme

$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) = 1 - 4|U_{e4}|^2(1 - |U_{e4}|^2) \sin^2(\Delta m_{41}^2 L/4E)$$

$$P(\nu_\mu \rightarrow \nu_\mu) = 1 - 4|U_{\mu4}|^2(1 - |U_{\mu4}|^2) \sin^2(\Delta m_{41}^2 L/4E)$$

$$P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) = 4|U_{e4}|^2|U_{\mu4}|^2 \sin^2(\Delta m_{41}^2 L/4E)$$

$$\sin^2 2\theta_{\text{Bugey}} > 4|U_{e4}|^2(1 - |U_{e4}|^2) \cong 4|U_{e4}|^2$$

$$\sin^2 2\theta_{\text{CDHSW}} > 4|U_{\mu4}|^2(1 - |U_{\mu4}|^2) \cong 4|U_{\mu4}|^2$$

$$\sin^2 2\theta_{\text{LSND}} = 4|U_{e4}|^2|U_{\mu4}|^2$$

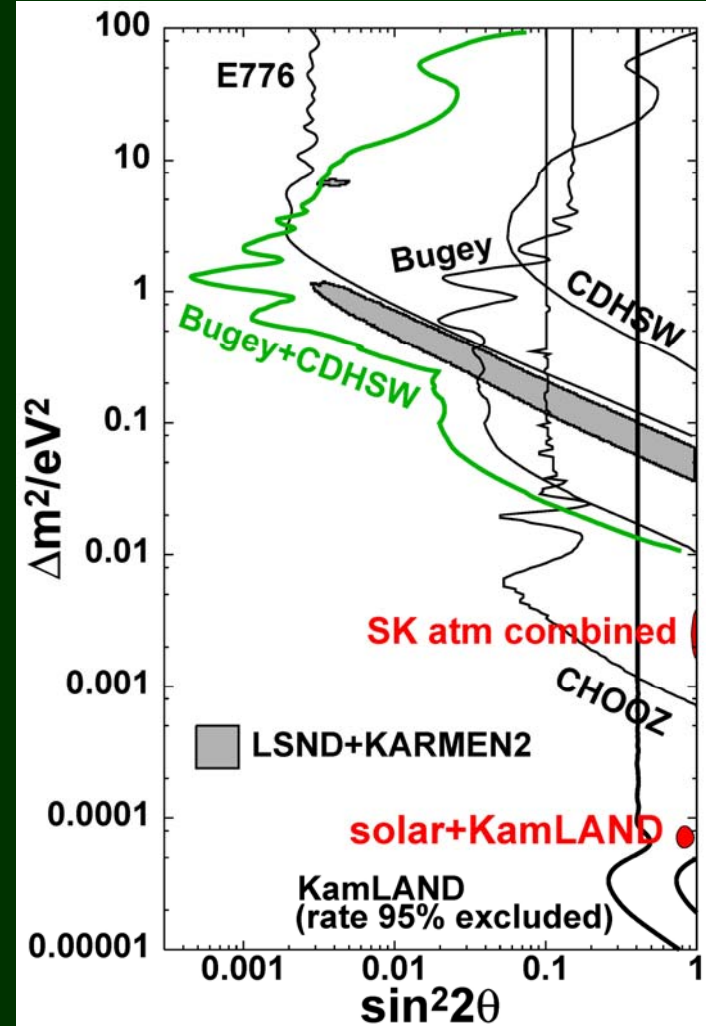
$U_{\alpha 4}$  : an element of 4x4 mixing matrix



$$\sin^2 2\theta_{\text{LSND}}(\Delta m^2) < \frac{1}{4} \sin^2 2\theta_{\text{Bugey}}(\Delta m^2) \sin^2 2\theta_{\text{CDHSW}}(\Delta m^2)$$

**must be satisfied** (Okada-OY,'97; Bilenky-Giunti-Grimus, '98)

But there is no overlap between LSND and left side of **Bugey+CDHSW**



## reactor $\nu$ anomaly + gallium anomaly

→ (3+1)-scheme may fit to the data  
(LSND+MB+other short baseline expts.) better  
with new flux than before (with old flux).

→ It is important to confirm sterile  $\nu$  oscillations

- A ten kilocurie scale anti- $\nu$  source ( $^{144}\text{Ce}$ ,  $^{106}\text{Ru}$ )  $\bar{\nu}_e \rightarrow \bar{\nu}_e$   
M. Cribier et al., arXiv:1107.2335
- A proposal for a  $\beta$ -beam  $\nu_e \rightarrow \nu_e$   
Agarwalla-Huber-Link, JHEP 1001:071,2010
- $\nu$  oscillation experiments at a reactor with a  
small core → Present work arXiv:1107.4766  
[hep-ph]  $\bar{\nu}_e \rightarrow \bar{\nu}_e$

## 2. Analysis of a reactor neutrino oscillation experiment with one reactor & two detectors

$$\chi^2 = \min_{\alpha's} \left\{ \sum_{A=N,F} \sum_{i=1}^n \frac{1}{(t_i^A \sigma_i^A)^2} [m_i^A - t_i^A(1 + \alpha + \alpha^A + \alpha_i) - \alpha_{\text{cal}}^A t_i^A v_i^A]^2 + \sum_{A=N,F} \left[ \left( \frac{\alpha^A}{\sigma_{\text{dB}}} \right)^2 + \left( \frac{\alpha_{\text{cal}}^A}{\sigma_{\text{cal}}} \right)^2 \right] + \sum_{i=1}^n \left( \frac{\alpha_i}{\sigma_{\text{Db}}} \right)^2 + \left( \frac{\alpha}{\sigma_{\text{DB}}} \right)^2 \right\}.$$

$n = \#(\text{bin}) = 32$

OY, arXiv:  
1107.4766  
[hep-ph]

$m_i^A$ : Measured numbers of events

$t_i^A$ : Theoretical prediction

$v_i^A$ : Variation due to energy calibration error

$$(t_i^A \sigma_i^A)^2 = t_i^A + (t_i^A \sigma_{\text{db}}^A)^2$$

statistical errors

systematic errors

In the present case  $\sigma_{\text{stat}} > \sigma_{\text{sys}}$ :  
statistical errors are more important



A=N:  
“near”  
detector



$\nu_e$

A=F: “far”  
detector



## Assumed systematic errors: those of Bugey experiment

$\sigma_{\text{DB}}$ : correlated wrt detectors, correlated wrt bins = **3%**

$\sigma_{\text{Db}}$ : correlated wrt detectors, uncorrelated wrt bins = **2%**

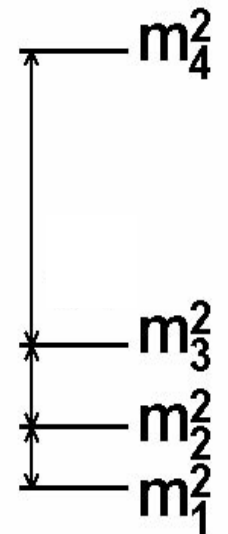
$\sigma_{\text{dB}}$ : uncorrelated wrt detectors, correlated wrt bins = **0.5%**

$\sigma_{\text{db}}$ : uncorrelated wrt detectors, uncorrelated wrt bins = **0.5%**

$\sigma_{\text{cal}}$ : energy calibration error for each bin = **0.6%**

## Formula for oscillation probability

$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) = 1 - \sin^2 2\theta_{14} \sin^2 \left( \frac{\Delta m_{41}^2 L}{4E} \right)$$



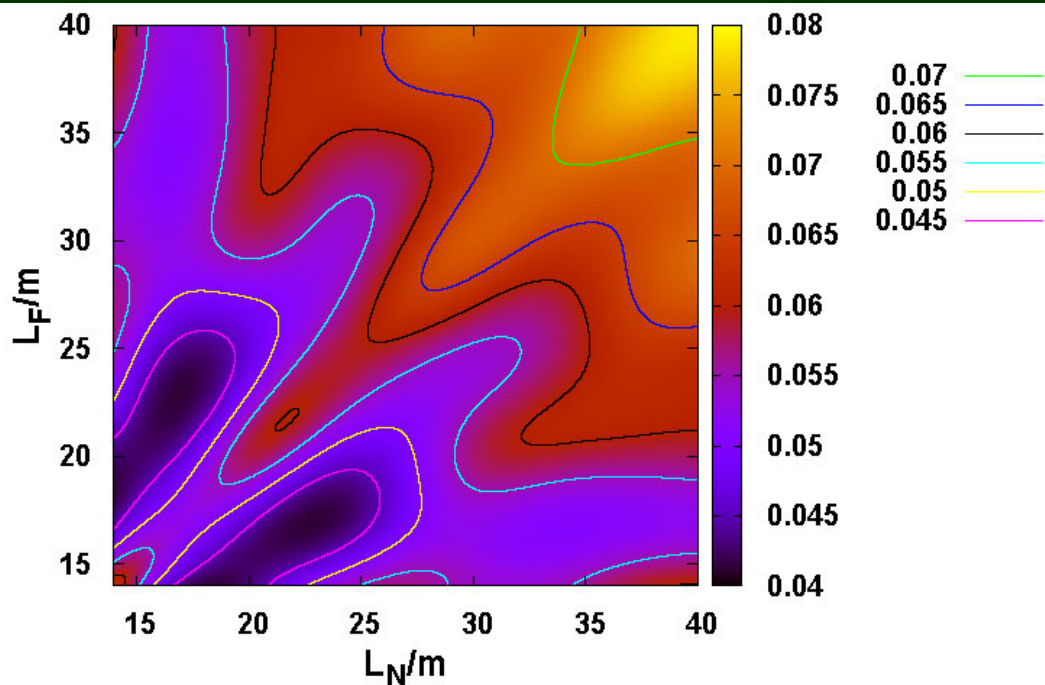
# (1) Commercial reactors

## Assumed parameters (a la Bugey)

- Power: 2.8 GW
- Size of the core: Diameter=4m, Height=4m

Power density  $\sim 50 \text{ MW/m}^3$

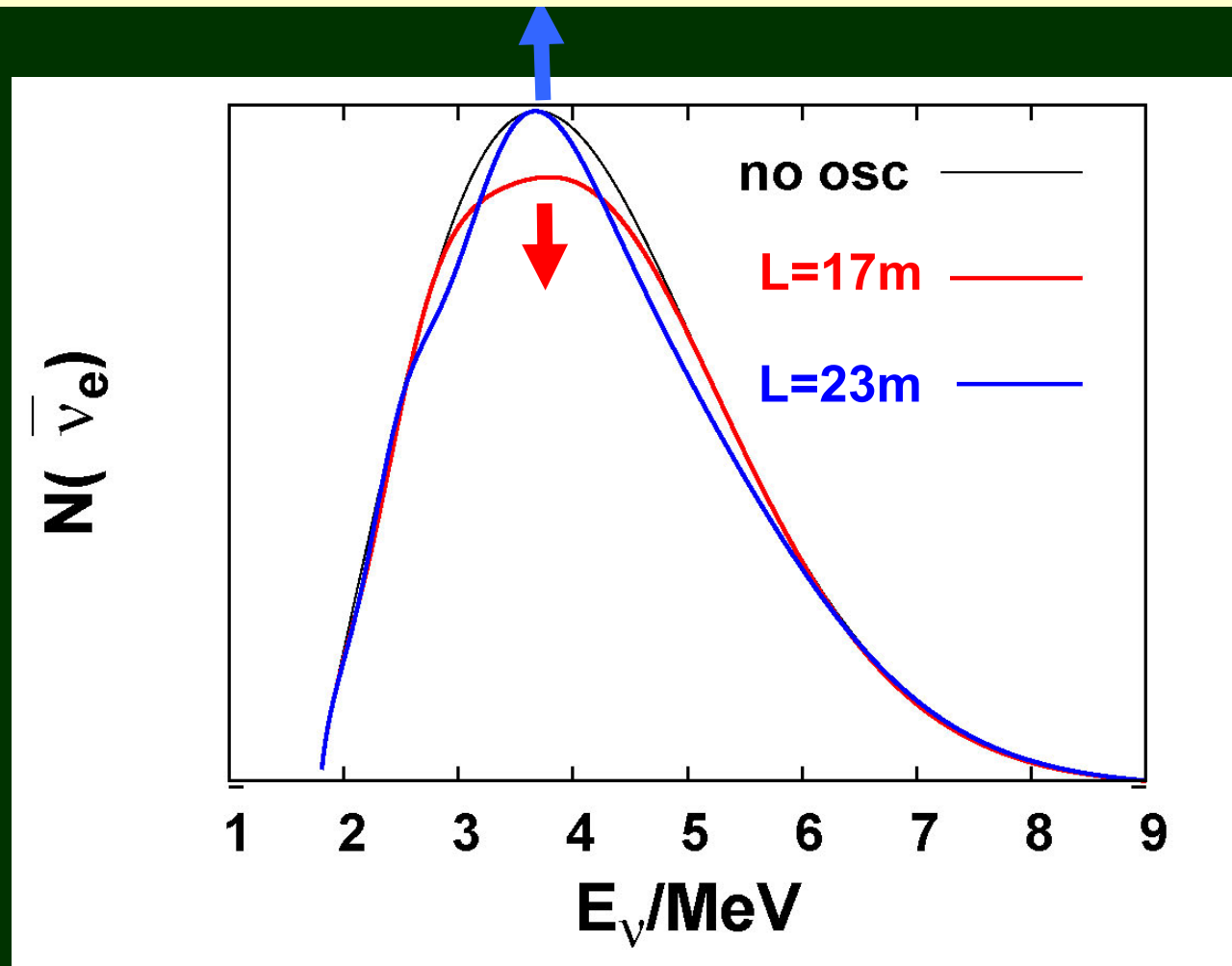
Optimization w.r.t. baseline lengths  $L_N$ ,  $L_F$  for  $\Delta m^2 = 1 \text{ eV}^2$



**Optimized  
baseline  
lengths:  
 $L_N = 17 \text{ m}$ ,  
 $L_F = 23 \text{ m}$**

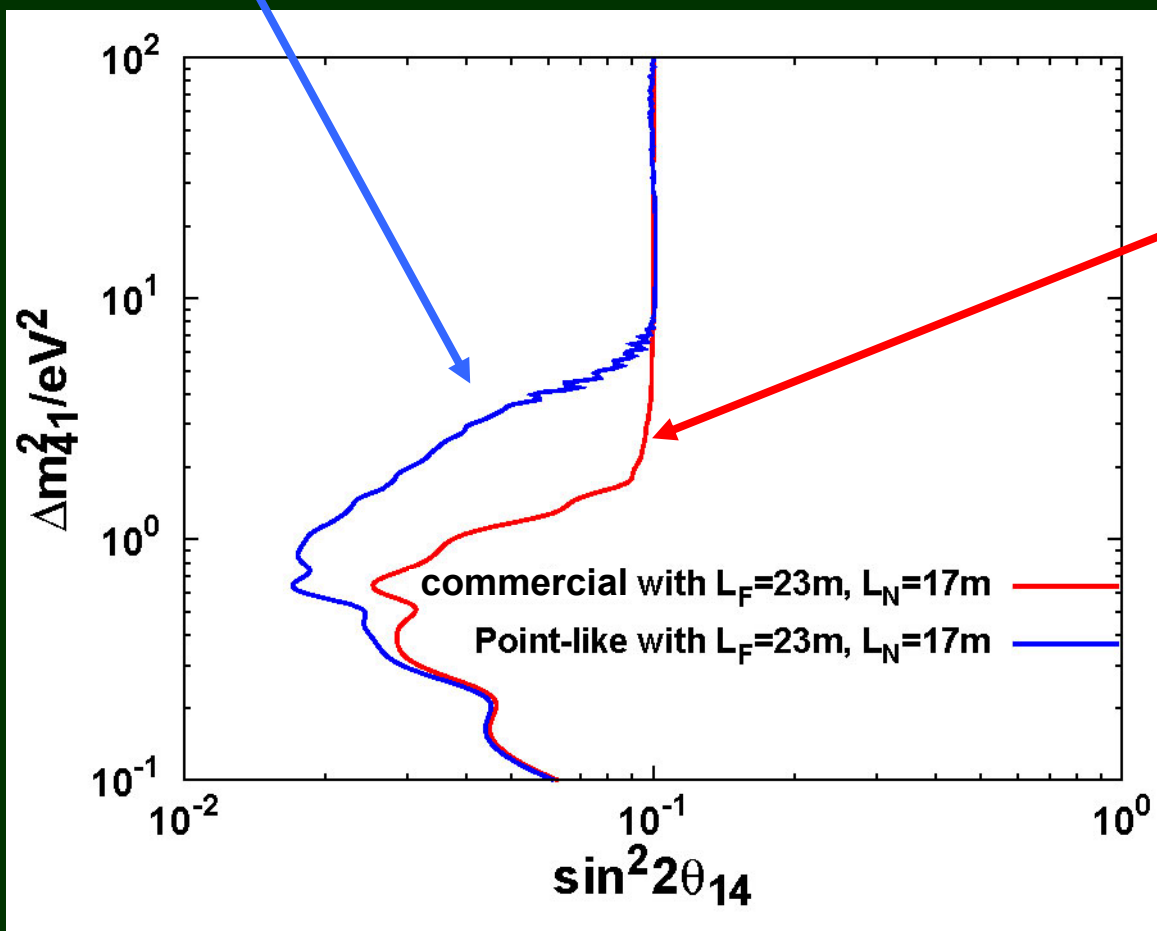
# The role of a “near” detector in the energy spectrum analysis for $\Delta m^2=1\text{eV}^2$

The difference at  $\langle E \rangle \sim 4\text{MeV}$  is most significant for  $L_N=17\text{m}$   $L_F=23\text{m}$



# Sensitivity of Commercial reactors to $\sin^2 2\theta_{14}$ at $L_N=17\text{m}$ $L_F=23\text{m}$

The case of a hypothetical reactor with a **point-like** core  $\rightarrow$  better sensitivity

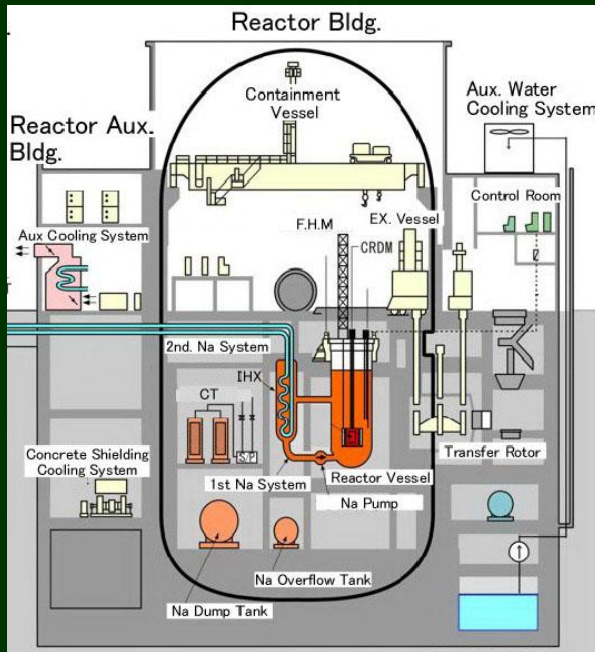


**Finite size** effect  
of a core  $\rightarrow$  poor  
sensitivity for  
 $\Delta m^2 \sim 2\text{eV}^2$



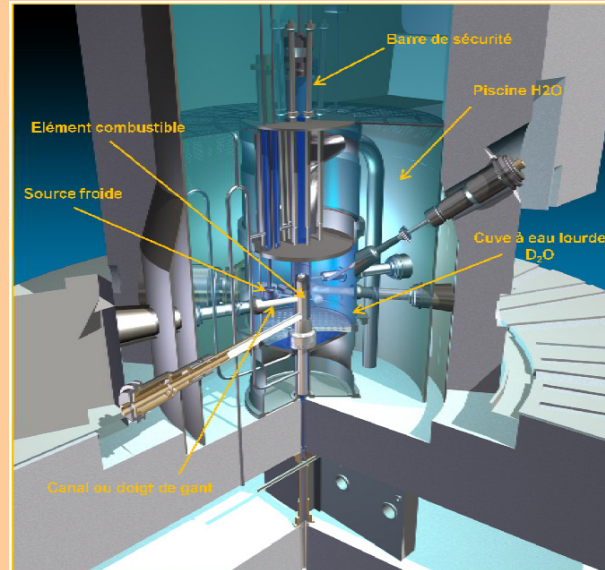
## (2) Research Reactors with a small core

- Joyo (Ibaraki, Japan):  $D=0.8\text{m}$ ,  $h=0.5\text{m}$ ,  $P_{\text{th}}=140\text{MW}$

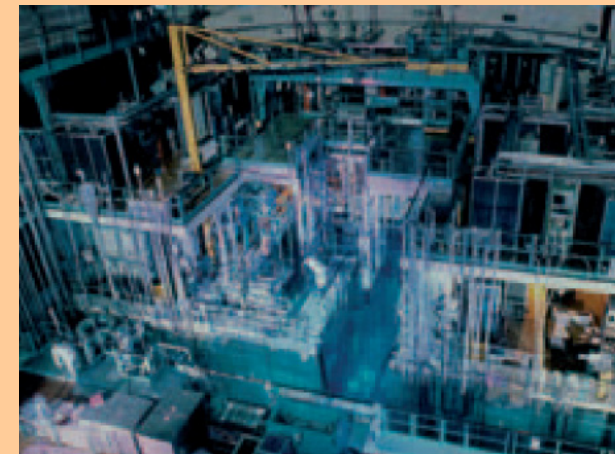


## Nucifer project

- ILL reactor (Grenoble, France):  $D=0.4\text{m}$ ,  $h=0.8\text{m}$ ,  $P_{\text{th}}=58\text{MW}$



- Osiris reactor (Saclay, France):  $0.57\text{m} \times 0.57\text{m} \times 0.6\text{m}$ ,  $P_{\text{th}}=70\text{MW}$



Power density  $\sim 500\text{MW}/\text{m}^3$

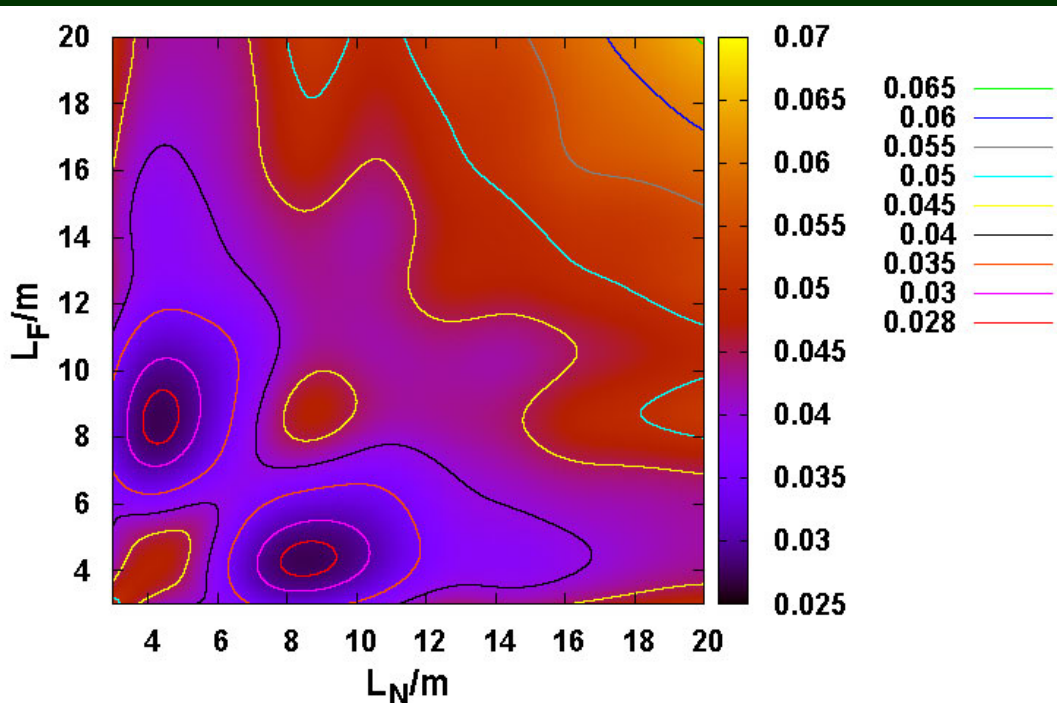
cf.  $\sim 50\text{MW}/\text{m}^3$  for commercial reactors

## ● Joyo (A fast neutron reactor)

### Assumed parameters

- Power: 0.14 GW
- Size of the core: Diameter=0.8m, Height=0.5m

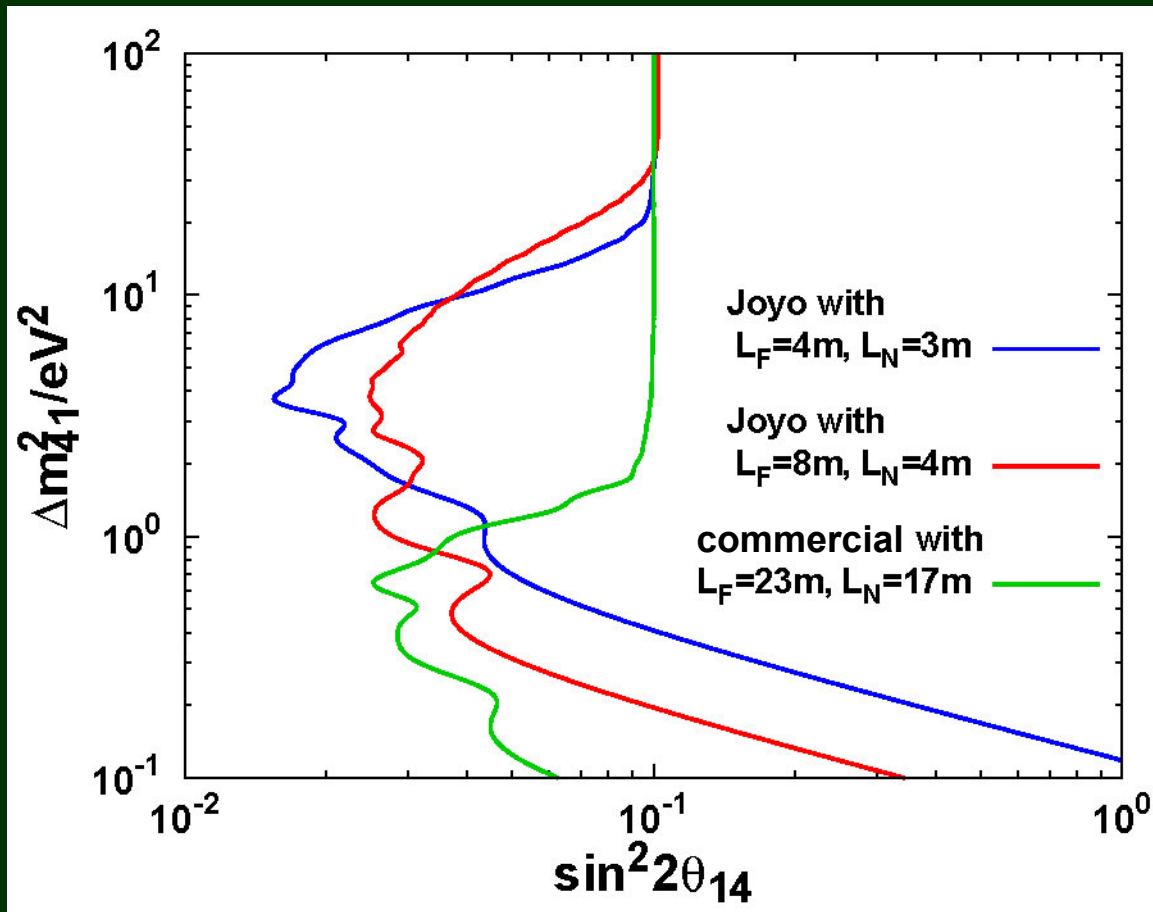
### Optimization w.r.t. baseline lengths $L_N$ , $L_F$ for $\Delta m^2=1\text{eV}^2$



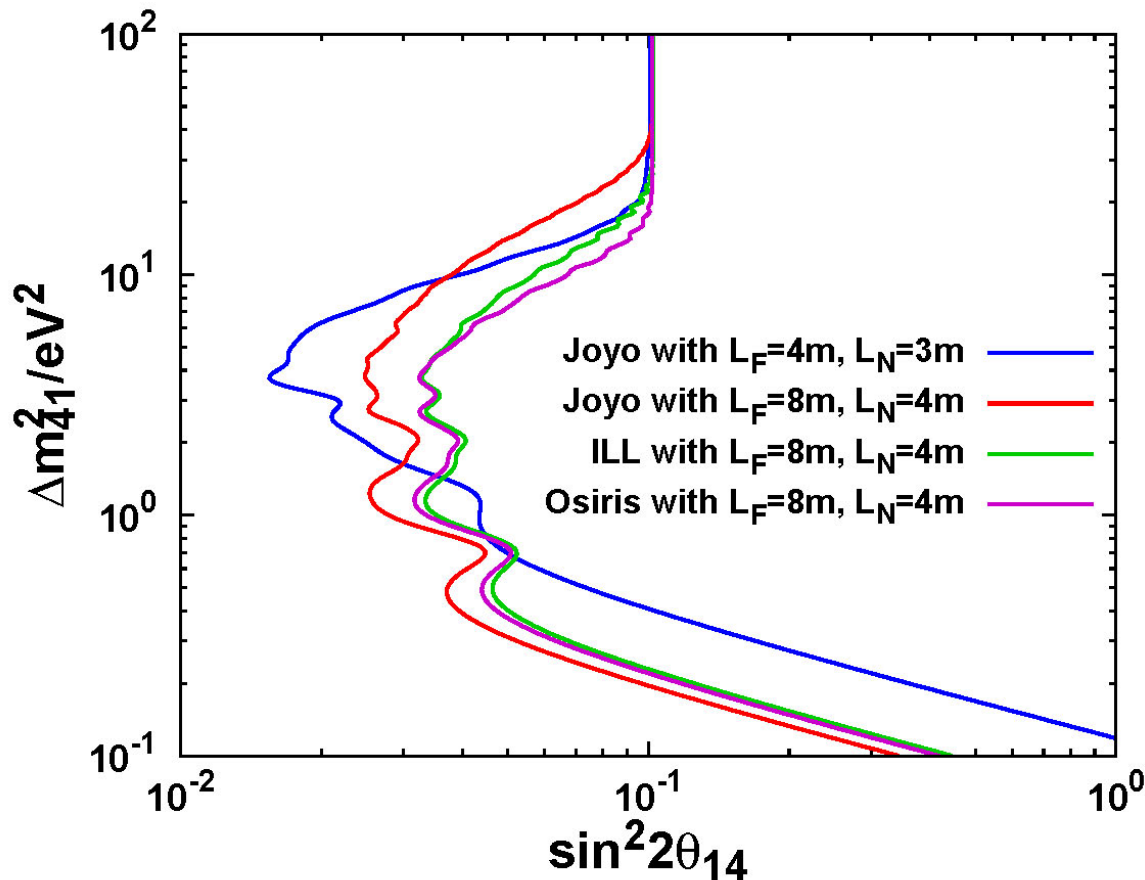
**Optimized  
baseline  
lengths:  
 $L_N=4\text{m}$   
 $L_F=8\text{m}$**

## Sensitivity of Joyo to $\sin^2 2\theta_{14}$ at $L_N=4\text{m}$ , $L_F=8\text{m}$

- Less power is compensated by closer distance
- A reactor with a small core prevents smearing effect



## (2-2) ILL & Osiris



**ILL** (Institut Laue-Langevin near Grenoble) research reactor

**Power=58 MW,**  
**Diameter=40cm,**  
**Height=80cm**

**Osiris** (in the French Atomic Energy Commission (CEA) centre at Saclay)

**Power=70 MW,**  
**Size=57cmx57cmx60cm**

In the nucifer project, optimization w.r.t baselines is **not** planned. → Great if the detectors are placed very close to a reactor!

### 3. Summary

- Because of the recent re-evaluation of the reactor  $\nu$  flux, scenarios of sterile  $\nu$  oscillations with  $\Delta m^2 \sim O(1\text{eV}^2)$  are reviving.
- To get a useful information from the spectrum analysis of reactor  $\nu$  for  $\Delta m^2 > 1\text{eV}^2$ , a reactor with a small core is necessary to avoid the smearing effect.
- Research reactors have a small core in general, and measurements of  $\nu$  from those may be able to offer a test of LSND/MiniBooNE.

**Backup slides**

(2+2)-scheme

$$\eta_s \equiv |\mathbf{U}_{s1}|^2 + |\mathbf{U}_{s2}|^2 \rightarrow \mathbf{0}$$

$$\mathbf{v}_{\text{atm}} : \mathbf{v}_\mu \rightarrow \mathbf{v}_s \text{ (100\%)}$$

Strongly disfavored by  
SK  $\nu_{\text{atm}}$  data

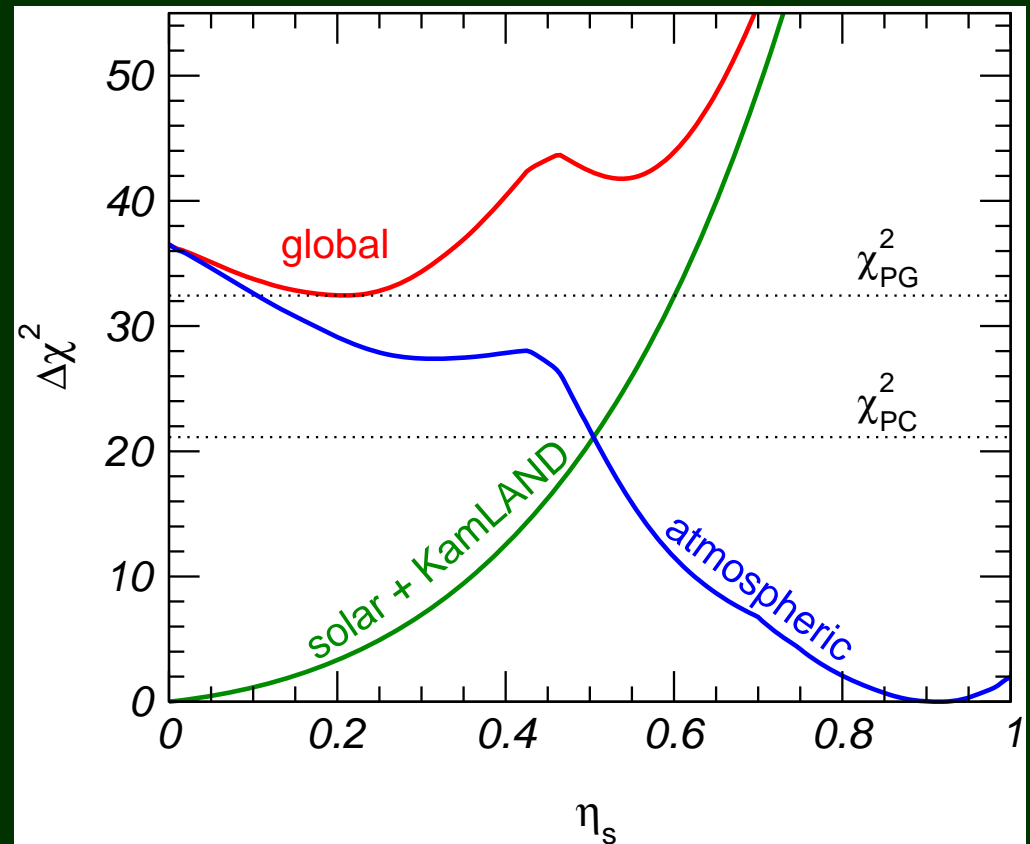
$$\eta_s \equiv |\mathbf{U}_{s1}|^2 + |\mathbf{U}_{s2}|^2 \rightarrow \mathbf{1}$$

$$\mathbf{v}_{\text{sol}} : \mathbf{v}_e \rightarrow \mathbf{v}_s \text{ (100\%)}$$

Strongly disfavored by  
SNO  $\nu_{\text{sol}}$  data

For any value of  $|\mathbf{U}_{s1}|^2 + |\mathbf{U}_{s2}|^2$ , fit to sol+atm data is bad.

Maltoni et al., hep-ph/0405172



PC: parameter consistency test  
PG: parameter goodness-of-fit test

# MiniBooNE's summary



The data is  
still  
confusing

R. Van der Water@Neutrino2010

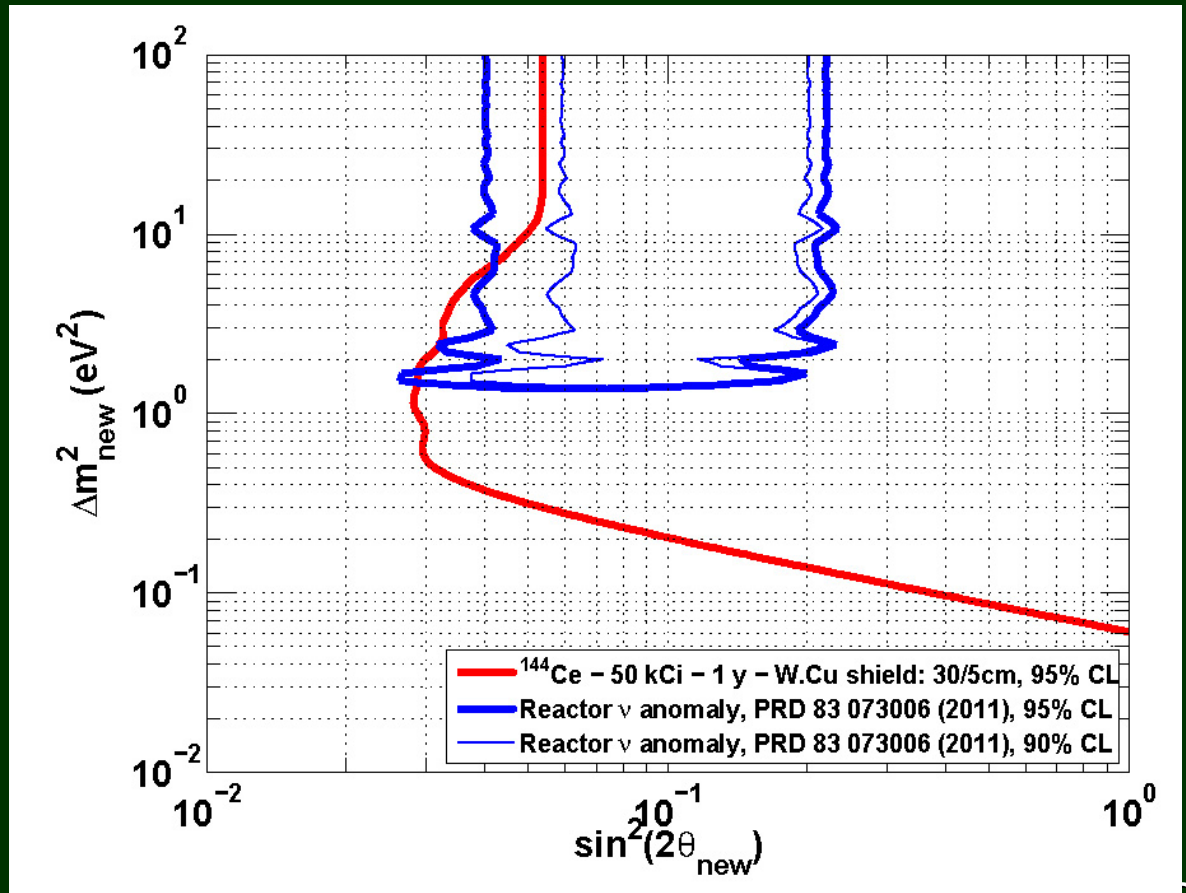
mode	$E < 475 \text{ MeV}$	$E > 475 \text{ MeV}$
$\nu_{\mu} \rightarrow \nu_e$	An unexplained $3\sigma$ electron excess	Inconsistent w/ LSND @ 90%CL
$\bar{\nu}_{\mu} \rightarrow \bar{\nu}_e$	A small $1.3\sigma$ electron excess	Consistent w/ LSND @ 99.4%CL



# A ten kilocurie scale anti- $\nu$ source ( $^{144}\text{Ce}$ , $^{106}\text{Ru}$ )

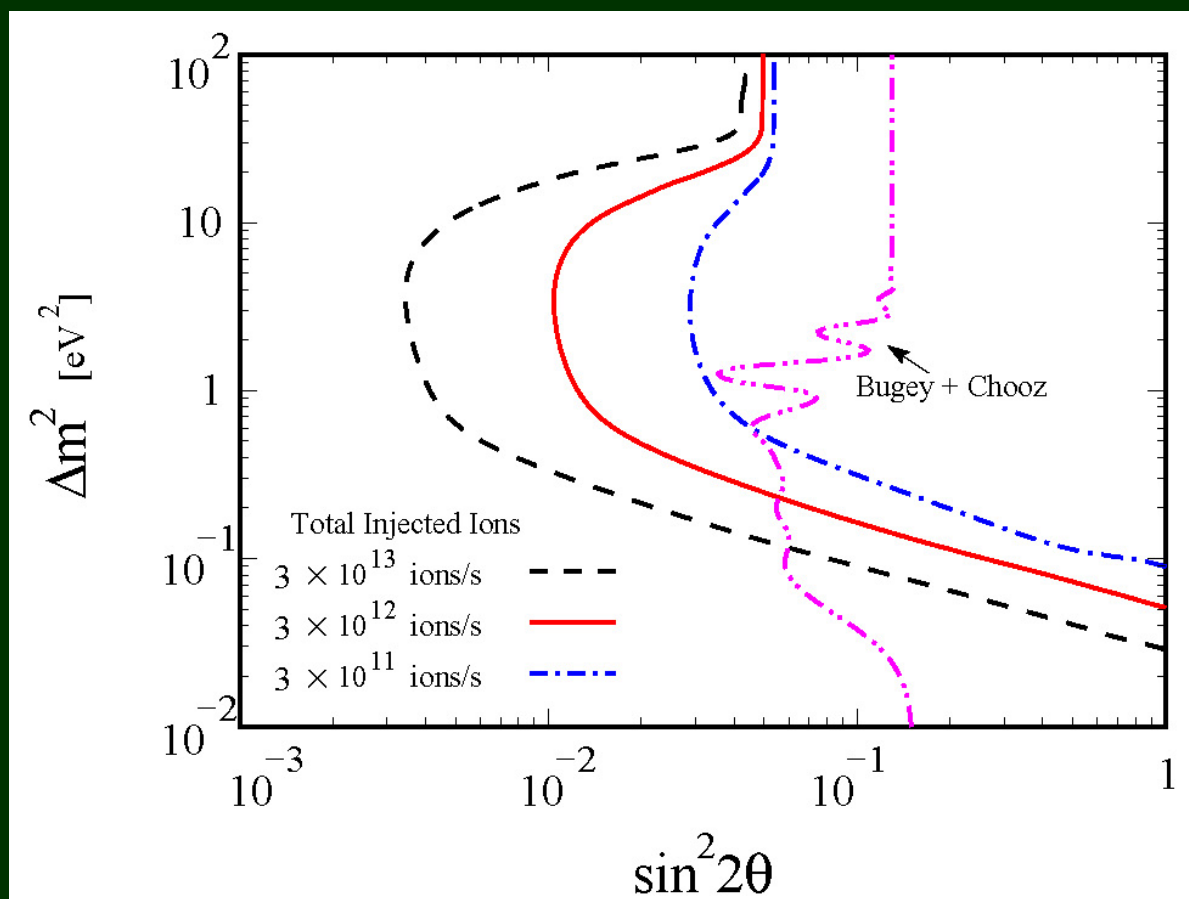
Cribier et al., arXiv:1107.2335v1 [hep-ex]

anti- $\nu$  source placed in a liquid scintillator detector (e.g., KamLAND)



# Proposal of a $\beta$ -beam

Agarwalla-Huber-Link,  
JHEP 1001:071,2010



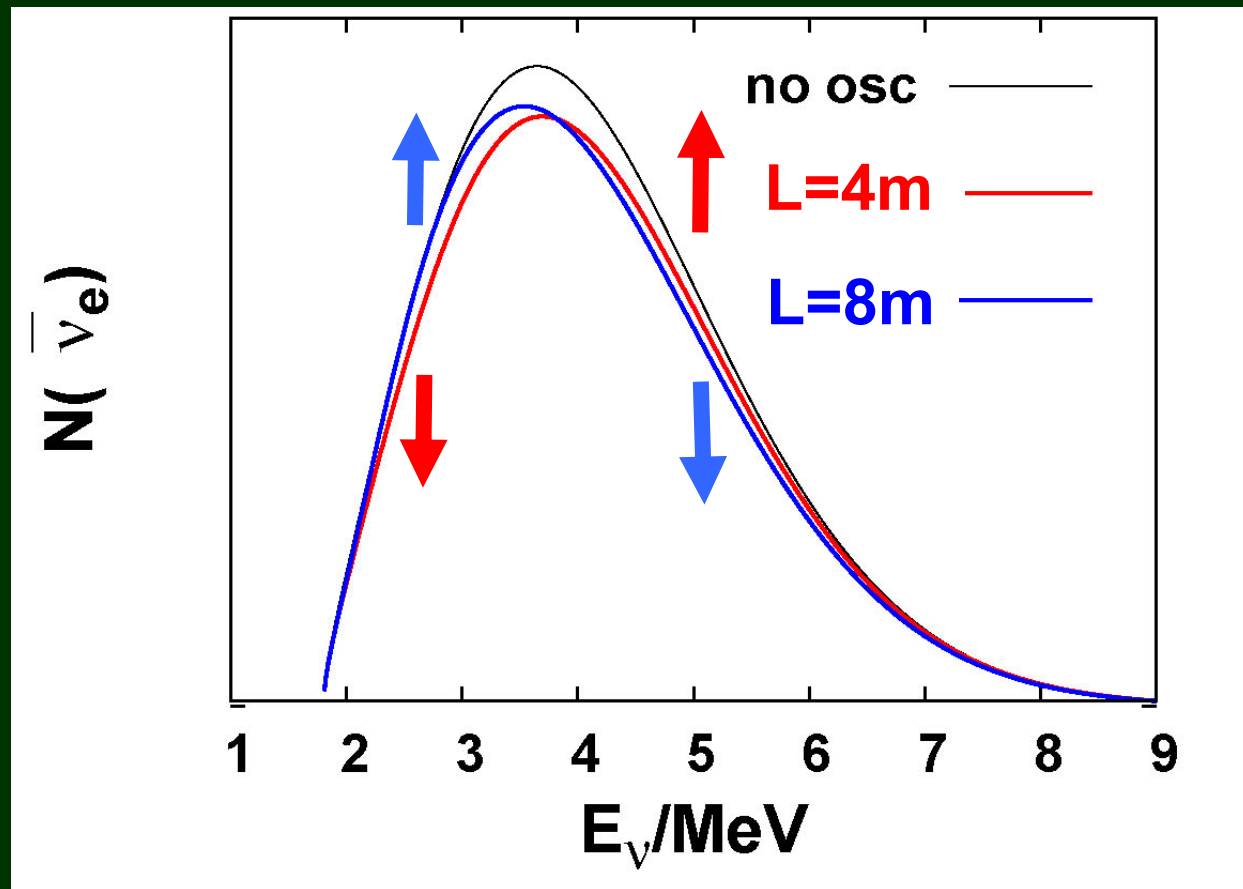
$$v_i^A = \lim_{\alpha_{\text{cal}}^A \rightarrow 0} \frac{1}{\alpha_{\text{cal}}^A t_i^A} \left[ \frac{N_p T}{4\pi L_A^2} \int dE \int_{(1+\alpha_{\text{cal}}^A)E_i}^{(1+\alpha_{\text{cal}}^A)E_{i+1}} dE' R(E_e, E') \epsilon(E) F(E) \sigma(E) - t_i^A \right]$$

$$t_i^A \equiv \frac{N_p T}{4\pi L_A^2} \int dE \int_{E_i}^{E_{i+1}} dE' R(E_e, E') \epsilon(E) F(E) \sigma(E)$$

In Eqs. (4) and (5),  $N_p$  is the number of target protons in the detector,  $T$  denotes the exposure time,  $L_A$  is the baseline for the detector  $A$ ,  $F(E)$  is the flux of  $\bar{\nu}_e$ , and  $\sigma(E)$  is the cross section of the inverse  $\beta$  decay  $\bar{\nu}_e + p \rightarrow n + e^+$ .  $E$  is the energy of the incident  $\bar{\nu}_e$  and it is related to the positron energy  $E_e$  and the masses  $m_n$ ,  $m_p$  of a neutron and a proton by  $E = E_e + m_n - m_p = E_e + 1.3$  MeV.  $E'$  is the measured positron energy and we will assume that the energy resolution is given by  $8\%/\sqrt{E}$ , i.e.,  $R(E_e, E') = R(E - m_n + m_p, E')$  is a Gaussian function which describes the energy resolution and is given by  $R(E_e, E') = (1/\sqrt{2\pi}\sigma) \exp[-(E_e - E')^2/2\sigma^2]$ , where  $\sigma = 0.08\sqrt{(E_e + m_e)/\text{MeV}} = 0.08\sqrt{(E - 0.8/\text{MeV})/\text{MeV}}$ . Our strategy is to *assume no*

# The role of a “near” detector in the energy spectrum analysis for $\Delta m^2=1\text{eV}^2$

Asymmetry at  $\langle E \rangle \sim (4 \mp 1)\text{MeV}$  is most significant for  $L_{N,}=4\text{m}$   $L_F=8\text{m}$



## 1.7 Thermal Neutron Reactors vs Fast Neutron Reactors

Fuels must be distant  $\Rightarrow$  the volume must be larger

	Kinetic energy of neutron	Moderator	Coolant	Power density
Thermal Neutron Reactor (w/ H <sub>2</sub> O)	$\sim 0.02\text{eV}$	H <sub>2</sub> O	H <sub>2</sub> O	$\sim O(10\text{MW}/\text{m}^3)$
Fast Neutron Reactor	$\sim 2\text{MeV}$	None	Na	$\sim O(100\text{MW}/\text{m}^3)$

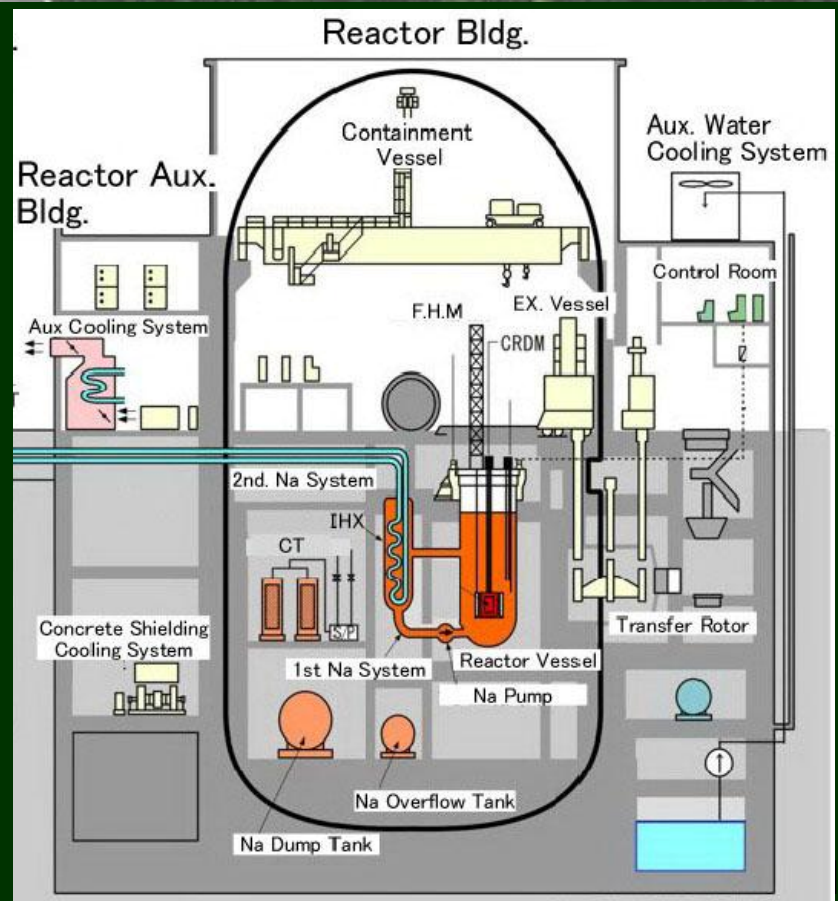
Fuels can be closer  $\Rightarrow$  the volume can be smaller

# Joyo Fast Research Reactor



Oarai,  
Ibaraki

Operated by JAEA  
 $P_{th} = 140\text{MW}$   
Frequent On/Off



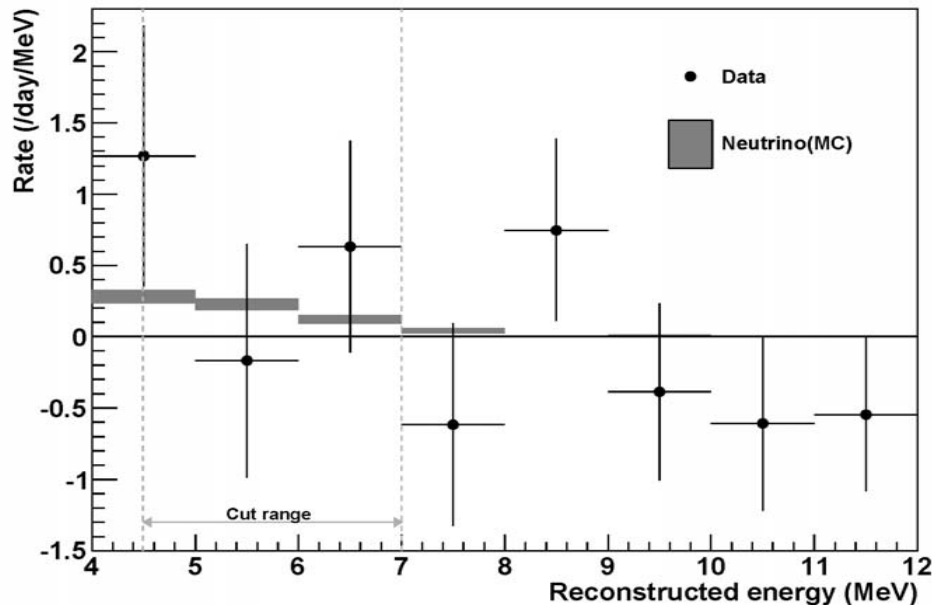
# A Study of Reactor $\nu$ Monitoring at Experimental Fast Reactor JOYO

H.Furuta et al., arXiv:1108.2910v1 [hep-ex]

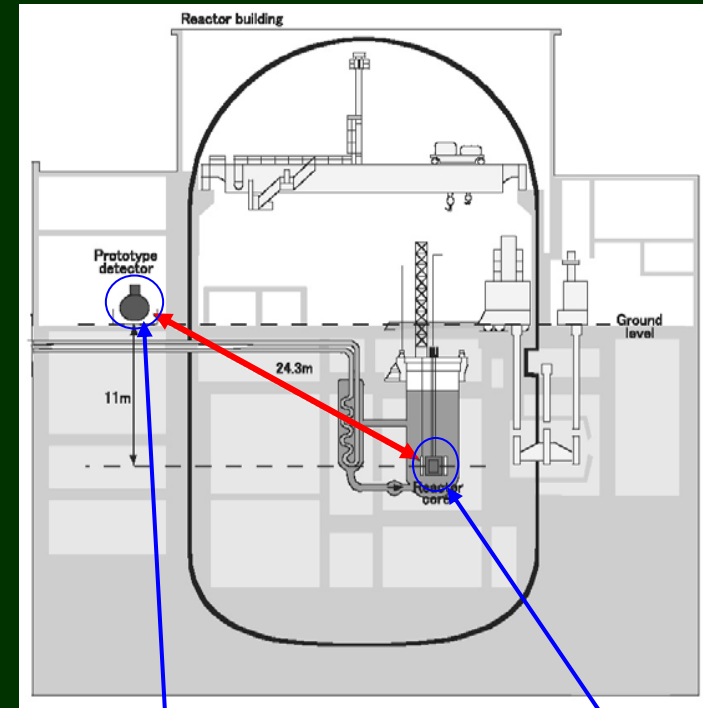
$L=24.3\text{m}$ ; about 150  $\nu p \rightarrow e^+n$  reactions/day

The measured  $\nu$  event rate from reactor on-off comparison was  $1.11 \pm 1.24(\text{stat.}) \pm 0.46(\text{syst.})$  events/day.

The statistical significance of the measurement was not enough.



Their motivation: to detect  $\nu$  from a fast reactor (not motivated by  $\nu_s$ )



Prototype detector

Reactor core





# How to measure Pu/U ratio by $\nu$

(simplified discussion)

$$\begin{cases} P_{th} = q(n_U + n_{Pu}) \\ N_\nu = an_U + bn_{Pu} \end{cases}$$

$$\rightarrow \frac{n_{Pu}}{n_U} = \frac{1 - ar}{br - 1}; \quad r = \frac{P_{th}}{qN_\nu}$$

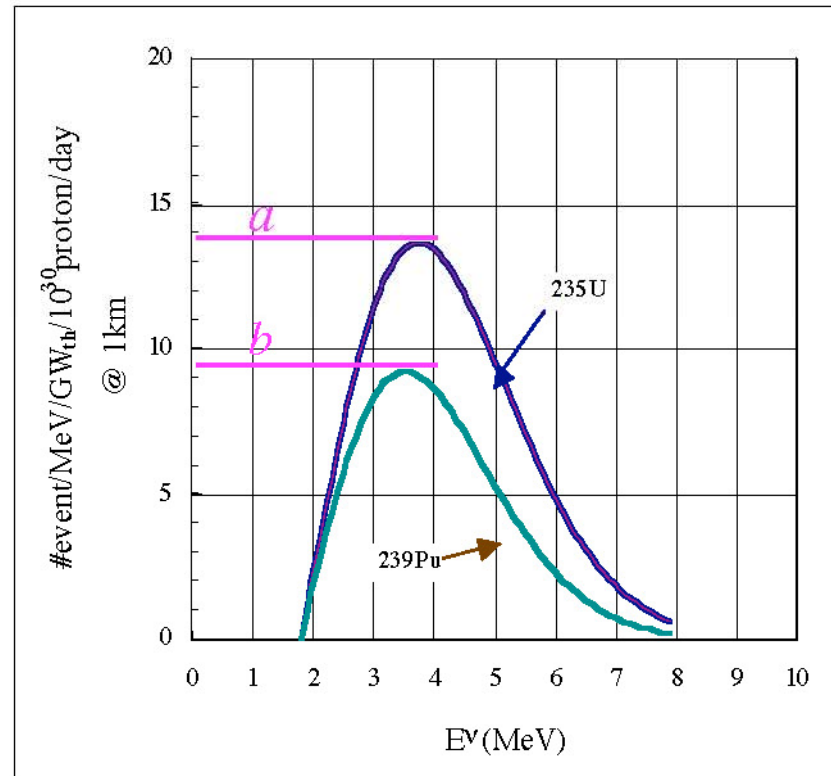
$n_U, n_{Pu}$ : Fission rate of U and Pu

$q$ : Energy release per fission  
(~200MeV)

$P_{th}$ : Thermal power

$N_\nu$ : # of  $\nu$

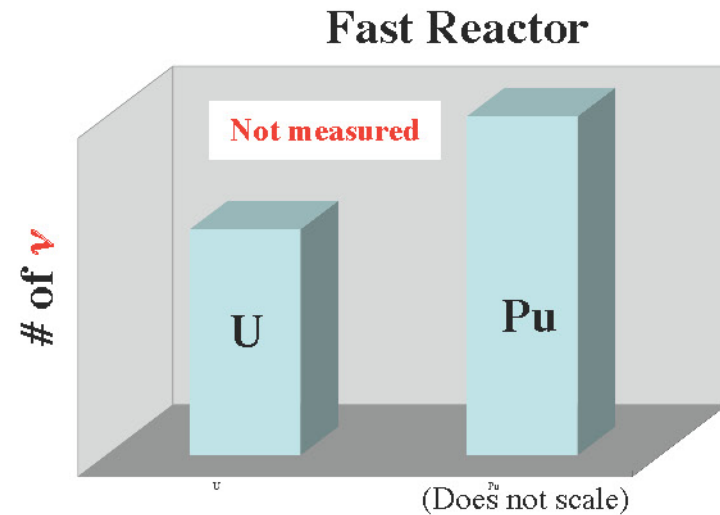
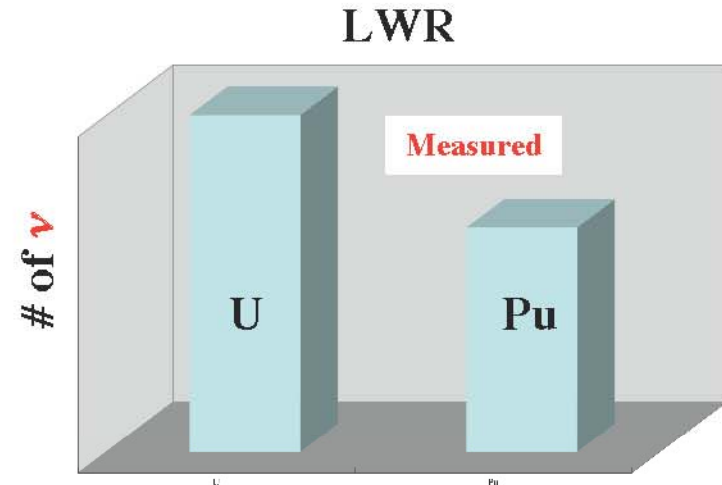
$a, b$ : # of  $\nu$  generation per U, Pu fission  
( $a/b \sim 1.5$ )



# Why Joyo?

- \* Practical Reason:  
Research Reactor is easier to access.
- \* Scientific Interest:  
 $\nu$  from fast reactor has not been measured.
- \* Technological Interest  
 $\nu$  spectrum from U and Pu can be measured separately by combining with the data from Light Water Reactor

However, the thermal power is small (1/20 of San-Onofre) and it is challenging to detect  $\nu$  at Joyo.



# Composition of Thermal Neutron Reactor & Fast Neutron Reactor

	$^{235}\text{U}$	$^{239}\text{Pu}$	$^{238}\text{U}$	$^{241}\text{Pu}$
Thermal Neutron Reactor (w/ $\text{H}_2\text{O}$ )	53.8%	32.8%	7.8%	5.6%
Fast Neutron Reactor	37.1%	51.3%	7.3%	4.3%

