Comment: 3, 4 or @ neutrinos?

· 3 active neutrinos

(Lisi, Yasuda)

conservative = attractive
but have to discard some experimental evidence
or introduce sterile neutrino (v)

o 3 active + 1 light sterile V

rich phenomenology (Giunti, Smirnor) but: why only one? naively expect 3, if any

Big Bang Nucleosynthesis limit on No

but: limit can be avoided through lepton number asymmetry in early universe (generated by P-Ps oscillations themselves)
Foot, Volkay, ... (Smirnor)

o 3 pairs of active/sterile 7's

atmospheric: Pn-Pt or In-1's ? experimentally solar: Pe-Pn or Ve-1's open question

example: scenario with 6 neutrinos with simplified phenomenological assumptions Pseudo - Dirac neutrinos as a potential complete solution of the neutrino oscillation puzzle

A.G., CERN-EP/98-56 application of old idea Bilenley, Pontecervo 1974, 1983 to present data

goal:

simultaneously satisfy all experimental indications + all oscillation limits with

- hierarchical standard 32 mixing small mixing angles analogous to quark sector
- universal mass fine splitting

 (pseudo Dirac neutrinos)

 > V V oscillations sin220 = 1

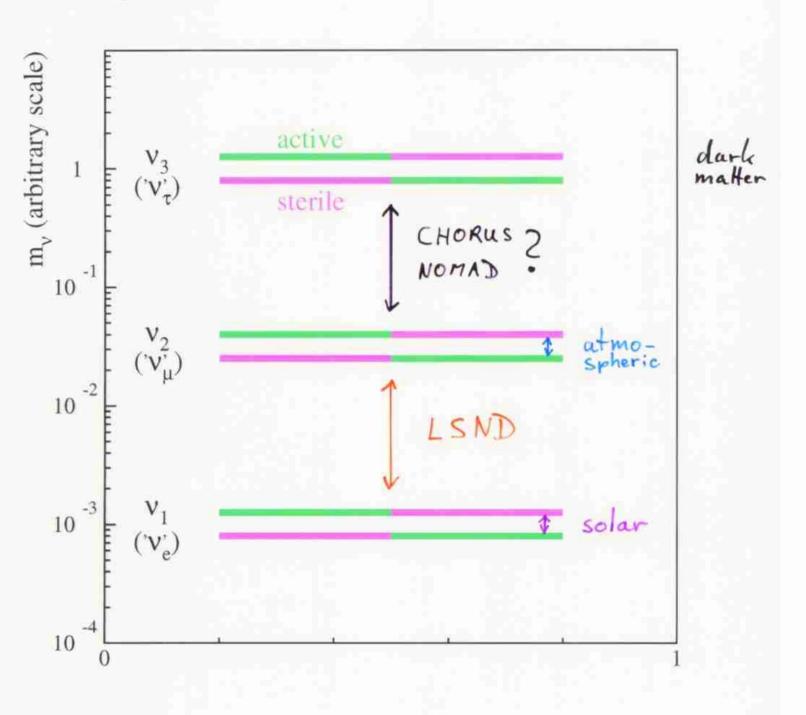
 (l'autive l'sterile oscillations)

 analogous to K° K° mixing

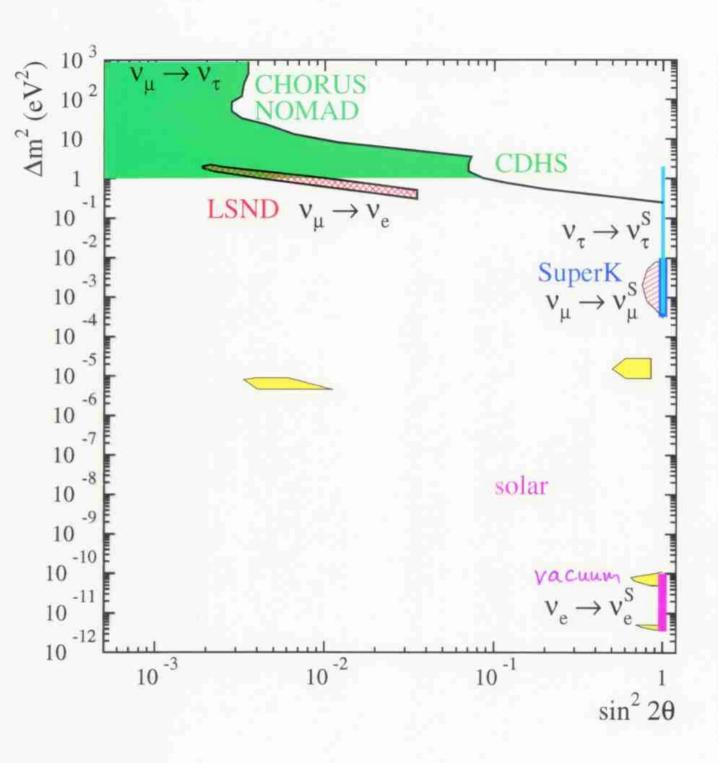
other models with similar phenomenology: Kobayashi, Lim, Nojiri 1991 Giunti, Kim, Lee 1992 Foot, Volkas 1995 Fusuoka, Koide 1998

The pseudo-Dirac mass spectrum

generic:



The pseudo-Dirac neutrino solution



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Pseudo-Dirac neutrinos as a potential complete solution to the neutrino oscillation puzzle

A. Geiser¹

Abstract

A solution for the neutrino mass and mixing pattern is proposed which is compatible with all available experimental data on neutrino oscillations. This solution involves Majorana neutrinos of the pseudo-Dirac type, i.e. $m_{\rm Majorana} \ll m_{\rm Dirac}$. The solar and atmospheric neutrino observations are mainly explained as $\nu_e - \nu_e^S$ and $\nu_\mu - \nu_\mu^S$ oscillations, where S indicates the sterile ("righthanded") partner of each neutrino generation, while the LSND result is interpreted in terms of standard $\nu_\mu - \nu_e$ oscillations. The resulting constraints on $\nu_\mu - \nu_\tau$ and $\nu_\tau - \nu_\tau^S$ oscillations are also discussed. This solution leaves room for a hierarchical mass and mixing scheme with a ν_τ mass in the few eV range, as favoured by some dark matter scenarios. The apparent conflict with standard Big Bang nucleosynthesis is addressed and the implications for current and future experiments are discussed. It is argued that both short and long baseline accelerator neutrino experiments are needed in order to decide between this solution and other oscillation scenarios.

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keywords: pseudo-Dirac, neutrino, oscillation, oscillations, sterile, mass

¹ CERN

1 Introduction

Currently there is a wealth of unexplained phenomena in neutrino physics which can be interpreted as indications for the existence of neutrino oscillations. The solar neutrino problem [1], lacking a satisfactory astrophysical solution, is commonly attributed to the disappearance of electron (anti)neutrinos into some other neutrino type. Similarly, the atmospheric neutrino anomaly [2] is often interpreted as an indication of neutrino oscillations involving ν_{μ} disappearance, with or without partial reappearance as ν_{e} . The LSND experiment [3] claims direct evidence for $\nu_{\mu} - \nu_{e}$ oscillations in a region which is partially unconstrained by other experiments. Furthermore, neutrinos are a prime candidate for a partial solution to the missing dark matter problem [4] if at least one mass eigenstate lies in the eV range. These current indications are summarized in Fig. 1.

Within the framework of 3 generation neutrino mixing, all recent solutions [5][6][7] to this neutrino puzzle either discard some of the experimental evidence or have to accept a bad fit to part of the data. Other solutions [8] involve the existence of one additional light sterile neutrino, yielding at least two extra degrees of freedom (mass and mixing angle(s)). Solutions involving more than one such neutrino [9][10] are often discarded due to bounds on the number of neutrino types suggested by Big Bang nucleosynthesis [11][12].

In this paper a solution is presented based on the assumption that neutrinos are of the pseudo-Dirac type, i.e. $m_{\rm Majorana} \ll m_{\rm Dirac}$ [13]. This involves the splitting of each neutrino generation into two almost degenerate mass eigenstates, leading to neutrino-antineutrino oscillations with maximal mixing, similar to oscillations in the $K^0 - \bar{K}^0$ system. Since oscillations do not change the handedness, left-handed neutrinos (right handed antineutrinos) will transform into left-handed antineutrinos (right handed neutrinos) which do not participate in weak interactions, and therefore appear sterile.

In contrast to earlier schemes of this kind [10], the neutrino magnetic moments are assumed to be 0, therefore avoiding $\nu_L \leftrightarrow \nu_R$ transitions. Special emphasis is placed on the case of exactly maximal mixing, which minimizes matter effects. Furthermore, the scheme is extended to include 3 generation flavour mixing, and applied to the most recent experimental data.

With only one parameter (a mass splitting parameter chosen to be universal for simplicity) in addition to the standard 3 generation mixing, all experimental indications for neutrino oscillations can be fully explained in the context of a hierarchical mass and mixing pattern, analogous to the quark sector. In addition, this solution suggests a substantial neutrino contribution to the missing dark matter. A problem with the Big Bang nucleosynthesis bounds mentioned earlier is discussed in section 4.

2 The pseudo-Dirac neutrino formalism

The most general neutrino mass term (Dirac-Majorana mass term) that can be added to the standard model Lagrangian leads, for one neutrino generation, to the (Majorana) mass eigenstates [13][14]

$$m_{I,II} = \left| \frac{1}{2} \left[(m_L + m_R) \pm \sqrt{(m_L - m_R)^2 + 4m_D^2} \right] \right|$$

where m_D is the Dirac mass, and m_L, m_R are the left and right handed Majorana masses, and to a mixing angle

$$\tan 2\theta = 2m_D/(m_R - m_L)$$

between these two states.

The standard Dirac case is obtained by setting $m_L = m_R = 0$, while $m_D = 0$ leads to pure Majorana neutrinos. The limit $m_R \gg m_D$, $m_L = 0$ ($\theta = m_D/m_R \ll 1$) yields the mass eigenstates $m_I = m_D^2/m_R$, $m_{II} \simeq m_R$ which corresponds to the well-known see-saw model [15], where m_D is assumed to be of the order of the quark and charged lepton masses, and m_R is a large mass of the order of some unification scale. This forces the mass of the "left-handed" neutrino (m_I) to be small, and makes the "right-handed" neutrino (m_{II}) very heavy, therefore decoupling it from interactions in the accessible energy range.

Finally, the limit $m_D \gg m_L$, m_R ($\theta \simeq 45^o$) yields almost degenerate mass eigenstates $m_{I,II} \simeq m_D$, with close to maximal mixing arising in a "natural" way. This case, which is known as the pseudo-Dirac case, will be pursued further here. Taking $m_L = m_R = \delta m$ for simplicity one obtains

$$m_{I,II} = m_D \pm \delta m$$
, $\theta = 45^{\circ}$.

In this case, the mass eigenstates can be written in terms of the neutrino/antineutrino eigenstates of the weak interactions as

$$|\nu_I> = \frac{1}{\sqrt{2}}(|\nu>+|\bar{\nu}>), \qquad |\nu_{II}> = \frac{1}{\sqrt{2}}(|\nu>-|\bar{\nu}>),$$

a pattern which is similar to the one in the $K^0 - \bar{K}^0$ meson system. As in the K^0 case, this yields maximal oscillations between particle and antiparticle states if pure neutrinos or antineutrinos are produced. Since, up to a small mass effect, neutrinos are emitted lefthanded and oscillations cannot change the handedness (angular momentum conservation) they will oscillate into left-handed antineutrinos which appear sterile. The same is true for right-handed antineutrinos oscillating into right-handed neutrinos. Thus phenomenologically one obtains active-sterile neutrino oscillations with

$$\Delta m^2 = (m_D + \delta m)^2 - (m_D - \delta m)^2 = 4m_D \delta m$$

and maximal mixing ($\sin^2 2\theta = 1$).

This can easily be generalized to 3 generations. Neglecting CP violation, the resulting mixing matrix is a real 6×6 matrix in principle. Here, we simplify it with the hypothesis that the oscillations between different generations and the active-sterile oscillations decouple, thus yielding the standard 3 generation mixing matrix $U_{\alpha \bar{i}}$ ($\alpha = e, \mu, \tau, i = 1, 2, 3$), equivalent to the CKM matrix [16], plus maximal active-sterile mixing for each generation

$$|\nu_{\alpha}> = U_{\alpha i} \frac{1}{\sqrt{2}} (|\nu_{i,I}> + |\nu_{i,II}>), \qquad |\bar{\nu}_{\alpha}> = U_{\alpha i} \frac{1}{\sqrt{2}} (|\nu_{i,I}> - |\nu_{i,II}>).$$

Since Majorana mass terms can be introduced ad hoc as bare mass terms without destroying gauge invariance, no attempt is made at this stage to clarify their origin. Phenomenologically, two cases are considered: (1) same $\delta m_i = \varepsilon \times M$ for each generation, where M=1 eV is an arbitrary fixed reference mass, and (2) mass dependent splitting $\delta m_i = \varepsilon \times m_{Di}$. The mass pattern generated by these scenarios is therefore given by $m_{Di} \simeq m_1, m_2, m_3$ for the 3 generations, and by the single additional parameter $\varepsilon \ll 1$ fixing the mass fine splittings.

3 The neutrino oscillation solution

To find a simple general solution to the neutrino oscillation puzzle described in the introduction the following further assumptions are made, in analogy to the quark sector:

- The mass structure is hierarchical, i.e. m₁ ≪ m₂ ≪ m₃.
- Mixing between adjacent generations is small (θ₁₂ and θ₂₃) and mixing between far generations is negligible (θ₁₃ ≈ 0). Flavour eigenstates can therefore be approximately identified with mass eigenstates (1 ≈ e, 2 ≈ μ, 3 ≈ τ).

Including ε this yields a total of six free parameters $(m_i(i=1,2,3), \varepsilon, \theta_{12}, \theta_{23})$.

The Δm^2 values relevant for oscillations are Δm_{12}^2 , Δm_{23}^2 for conventional mixing, and $\Delta m_{I/II,i}^2 = 4m_iM\varepsilon$ for case (1) ($\Delta m_{I/II,i}^2 = 4m_i^2\varepsilon$ for case (2)) for active-sterile oscillations. In the simplified case of only two contributing flavour and mass eigenstates, the probability of a neutrino of type α to oscillate into type β is given by the well known formula

$$P_{\alpha\beta} = \sin^2 2\theta_{\alpha\beta} \sin^2(1.27 \Delta m_{\alpha\beta}^2 L/E)$$

where L is the distance travelled in km, E is the neutrino energy in GeV, and $\Delta m_{\alpha\beta}^2$ is expressed in eV².

In the following, a complete solution for the six free parameters is derived based on all known experimental evidence (table 1). A graphical representation of this solution is shown in Fig. 1.

3.1 LSND

The LSND result [3] is interpreted as direct $\nu_{\mu} - \nu_{e}$ oscillations. The large Δm^{2} region $(\Delta m^{2} > 10 \text{ eV}^{2})$ is excluded by NOMAD [17], CCFR [18], BNL 734 [19], and BNL E766 [20]. The latter constrains also the island around $\Delta m^{2} \sim 6 \text{ eV}^{2}$ advocated by Caldwell [21]. The remaining region $(\Delta m^{2} \leq 2 \text{ eV}^{2})$ is fully consistent with, and even slightly favoured by, the recent KARMEN limits [22] partially based on a small $(\sim 1\sigma)$ positive result. At large $\sin^{2}2\theta$ the result is constrained by reactor experiments, including Gösgen [23], Krasnoyarsk [24], Chooz [25] and Bugey [26]. Note that the Bugey result, which yields the most stringent limit, is also based on a small (up to 1.5 σ) positive effect [26], fully consistent with the limits from the other reactor experiments. Inspired by this effect we choose a reference solution $\Delta m_{12}^{2} \sim 0.5 \text{ eV}^{2}$, $\sin^{2}2\theta_{12} \sim 2 \times 10^{-2}$. However, no significant lower constraint on $\sin^{2}2\theta$ can be derived from the Bugey result, allowing $\sin^{2}2\theta_{12}$ to be as small as 2×10^{-3} for $\Delta m_{12}^{2} \sim 2 \text{ eV}^{2}$.

3.2 Solar neutrinos

The solar neutrino problem is interpreted as $\nu_e - \nu_e^S$ oscillations with $\sin^2 2\theta_{eS} = 1$. This yields an average expected suppression factor of 0.5, slightly reduced further by a O(1%) correction from $\nu_e - \nu_\mu$ oscillations. Energy dependent oscillations have to be introduced in order to describe the observed suppression factors [27] with respect to the standard solar model [28] of 0.51 \pm 0.05 for the Gallium experiments [29], 0.27 \pm 0.02 for the Homestake

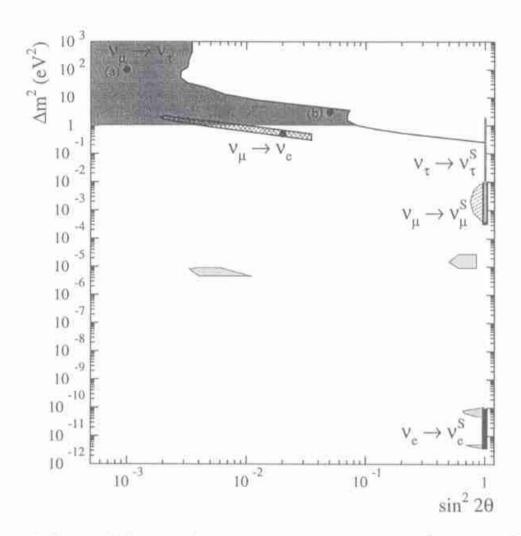


Figure 1: Current indications for neutrino oscillations in the $\sin^2 2\theta$ vs. Δm^2 plane, assuming dominance of two flavour oscillations in each case. The figure shows the 90% c.l. $\nu_{\mu} \rightarrow \nu_{e}$ region favoured by LSND (double hatched), including constraints from BNL 776 and Bugey, the Superkamiokande ν_{μ} disappearance solution to the atmospheric neutrino problem (hatched), the 3 mutually exclusive 95% c.l. solutions to the solar neutrino problem (light shaded), and the 90% c.l. limit on $\nu_{\mu} \rightarrow \nu_{\tau}$ (black line). Also shown is the parameter space of the proposed solutions for $\nu_{X} \rightarrow \nu_{X}^{S}$ (bars at $\sin^{2} 2\theta = 1$), $\nu_{\mu} \rightarrow \nu_{\tau}$ (dark shaded) and $\nu_{\mu} \rightarrow \nu_{e}$ (double hatched, identical to LSND region). The reference solutions described in the text are also indicated (black circles).

experiment [30], and 0.39 \pm 0.03 for the water Čerenkov detectors [31][32]. Since the MSW solution [27][33] is irrelevant for maximal mixing, the vacuum solution [27][34] is the only possible one. This yields $\Delta m_{I/II,1}^2 \sim 5 \times 10^{-12} - 10^{-10} \text{ eV}^2$.

3.3 Atmospheric neutrinos

The atmospheric neutrino anomaly is interpreted as $\nu_{\mu} - \nu_{\mu}^{S}$ oscillations with $\sin^{2}2\theta_{\mu S} = 1$. A small effect from $\nu_{\mu} - \nu_{e}$ and $\nu_{\mu} - \nu_{\tau}$ oscillations should be added. The Δm^{2} for ν_{e} disappearance ($\Delta m_{I/II,1}^{2}$) is too small to have any influence, so electron-like events are expected to be slightly enhanced by $\nu_{\mu} - \nu_{e}$ oscillations without L/E dependence. On the other hand, muon-like events are depleted mainly by $\nu_{\mu} - \nu_{\mu}^{S}$ oscillations, with a small L/E independent suppression from $\nu_{\mu} - \nu_{e}$, and another small but potentially complicated contribution from $\nu_{\mu} - \nu_{\tau}$ followed by $\nu_{\tau} - \nu_{\tau}^{S}$. Using the LSND reference solution quoted above, an L/E independent suppression would imply a value of $R = \frac{\mu/e_{measural}}{\mu/e_{expected}}$ of 0.49 or lower (if $\nu_{\mu} - \nu_{\tau}$ is significant). The observed average suppression of only about 0.63 [32] is therefore an indication for non-maximal ν_{μ} suppression due to dependence on L/E. Indeed such a dependence is observed indirectly through a dependence on the zenith angle by Kamiokande [35] and Superkamiokande [32]. Reinterpretation of the Superkamiokande result in terms of maximal $\nu_{\mu} - \nu_{\mu}^{S}$ oscillations suggests a value of $\Delta m_{I/II,2}^{2}$ in the range $3 \times 10^{-4} - 10^{-2}$ eV² [37]. The detailed consideration of matter effects can potentially induce a slight upward shift of this range [38]. Such low Δm^2 values can also explain why the suppression is stronger for the water Čerenkov detectors [32][35] than for some of the iron detectors [36] which have a higher energy threshold. Experiments looking for upward going muons yield inconclusive results so far [39][40], but are at least unlikely to exclude the low and high ends of the $\Delta m_{I/II,2}^2$ range quoted above.

3.4 Dark matter

The potential contribution of neutrinos to hot dark matter is given by $\Omega_{\nu} = \Sigma m_{\nu}/(92h^2 \, {\rm eV})$ [41], where Ω_{ν} is the neutrino energy density parameter expressed as the fraction of the critical density $\Omega=1$ needed to close the universe, h is the dimensionless renormalized Hubble constant (0.5 < h < 0.85 [42]) and Σm_{ν} is the sum over the masses of all neutrino types. For pseudo-Dirac neutrinos each neutrino flavour enters this sum twice. In the hierarchical mass pattern advocated here this contribution arises mainly from τ neutrinos [43]. No direct evidence for $\nu_{\mu} - \nu_{\tau}$ oscillations exists so far in the context of the pseudo-Dirac solution. Constraints are imposed by the exclusion regions obtained by accelerator experiments [17][44][45][46]. Two typical solutions close to the range accessible by current experiments and relevant to the dark matter problem could be (a) $\Delta m_{23}^2 = 100 \, {\rm eV}^2$ ($m_3 = 10 \, {\rm eV}$) with $\sin^2\!2\theta_{23} = 10^{-3}$, and (b) $\Delta m_{23}^2 = 3 \, {\rm eV}^2$ ($m_3 \simeq 2 \, {\rm eV}$) with $\sin^2\!2\theta_{23} = 5 \times 10^{-2}$. Solution (a), with its very small mixing, would have virtually no effect on any of the current measurements with positive indications for oscillations, but yields a large hot dark matter component ($\Omega_{\nu} \sim 0.4$ for $h \sim 0.7$) which is disfavoured by most current dark matter scenarios [4]. The associated Δm_{23}^2 could however be lowered to any value larger than 1 eV² (mass hierarchy limit), corresponding to $\Omega_{\nu} > 0.03$, without significantly changing the conclusions.

Alternatively, it could be raised up to the extreme limit from pure hot dark matter models of about $(30 \text{ eV})^2$ [43]. Solution (b) would yield a small but significant contribution of about 5% to the atmospheric neutrino suppression, with only a moderate hot dark matter contribution ($\Omega_p \sim 0.1$ for $h \sim 0.7$).

3.5 The mass fine splitting

The Δm^2 for $\nu_{\tau} - \nu_{\tau}^S$ oscillations is essentially unconstrained by current data. Since $m_2 \sim 1$ eV (LSND), the atmospheric neutrino solution yields $\varepsilon \sim 10^{-4} - 2 \times 10^{-3}$ for both case (1) and case (2). Folding this with the Δm_{23}^2 parameter space spanned by $\nu_{\mu} - \nu_{\tau}$ solutions (a) and (b), $\Delta m_{I/II,3}^2$ could be anywhere in the range $\sim 10^{-3} - 1$ eV². In combination with $\nu_{\mu} - \nu_{\tau}$ oscillations this could yield a small contribution to the angular effect observed in the atmospheric neutrino anomaly.

Finally, the above ε value applied to the solar neutrino result predicts m_1 in the range $10^{-9} - 10^{-6}$ eV for case (1), and $10^{-5} - 10^{-3}$ eV for case (2). This mass and mixing pattern is in agreement with the nonobservation of neutrinoless double β decay [47].

Table 1: Parameters of the pseudo-Dirac neutrino solution for $\varepsilon = 10^{-4} - 2 \times 10^{-3}$ (cases (1) and (2) of section 3.5 combined). m refers to the Dirac mass of each neutrino generation and Δm^2 to either the mass fine splitting inside each generation, or the mass difference squared between generations where appropriate. $\sin^2 2\theta$ refers to the associated mixing angle. Only the entries in the m and $\sin^2 2\theta$ columns are independent parameters, Δm^2 being fixed by m and ε .

generation	m (eV)	$\Delta m^2 \text{ (eV}^2\text{)}$	$\sin^2 2\theta$
1 ("e")	$10^{-9} - 10^{-3}$	$5 \times 10^{-12} - 10^{-10}$	1
2 ("µ")	0.5 - 1.7	$3 \times 10^{-4} - 10^{-2}$	1
3 ("")	1 - 30	$4 \times 10^{-4} - 2$	1
$1\leftrightarrow 2$	-	0.3 - 3	0.002 - 0.035
$2 \leftrightarrow 3$	-	1 - 30 or $30 - 900$	< 0.07 < 0.0035
$1 \leftrightarrow 3$		1 - 900	negligible

4 Compatibility with Big Bang nucleosynthesis

As is well known [48], the ratio of deuterium to hydrogen (D/H) and the fraction of He⁴ in the universe (Y) is determined in the Big Bang model by the ratio of neutrons to protons at the time of the "weak freeze out", i.e. the time when the reactions $n + e^+ \leftrightarrow p + \bar{\nu}_e$ and $p + e^- \leftrightarrow n + \nu_e$ proceed too slowly compared to the expansion rate of the universe to keep n/p at its thermal equilibrium value. The effective number of light neutrino flavours N_{ν} enters as a contribution to the energy density, which in turn influences the expansion rate. From this effect, a typical upper limit derived from current Big Bang nucleosynthesis (BBN) models is $N_{\nu} < 3.1$ @ 95% c.l. [48] with a central value of about 2.3, only marginally compatible with the standard model $N_{\nu} = 3$.

Active-sterile neutrino mixing can influence this rate in two ways: If active-sterile oscillations occur during thermal equilibrium, i.e. significantly before weak freeze out, the sterile neutrinos will make an additional contribution to the energy density at freeze out, and therefore increase the expansion rate, effectively behaving like additional light neutrino generations. On the other hand, depletion of ν_e due to $\nu_e \rightarrow \nu_e^S$ during freeze-out reduces the reaction rate for n/p interchange. In both cases, the predicted D/H and Y values will be larger than in the standard $N_{\nu} = 3$ case, and therefore even less compatible with the observed values which yield the limit quoted above.

The Δm^2 of 10^{-10} eV² or lower for vacuum $\nu_e - \nu_e^S$ oscillations yields an oscillation time scale which is significantly longer than the freeze with time scale. The oscillation effect is thus negligible for practical purposes [11]. Both $\nu_\mu - \nu_\mu^S$ and $\nu_\tau - \nu_\tau^S$ oscillations approximately fall in the mass range $10^{-3} - 10^{-1}$ eV² for which the BBN implications are discussed in ref. [12]. Each of these contribute 1 unit to N_ν if Δm^2 is at the upper edge of this range, and slightly less than one unit if Δm^2 is of order $10^{-3} - 10^{-4}$ [11], yielding $N_\nu \sim 4.6 - 5$. Such oscillations are therefore ruled out in the context of standard BBN if currently favoured values for Y and D/H are used. However, recent measurements of the primordial D/H abundance yield conflicting results [49], and the higher value of D/H = $(1.9 \pm 0.4) \times 10^{-4}$ is in better agreement with the other observed light element abundances. Using this value and pushing the primordial Helium abundance to its extreme limit of Y=0.25 [48], $N_\nu = 5$ could be allowed [49]. Furthermore, since the origin of the neutrino mass pattern might be associated to physics beyond the standard model, it is not inconceivable that other non standard model effects would modify BBN theory. For example, a significant initial lepton number asymmetry could in some cases generate a reduction of N_ν [50].

Overall, it does not seem impossible that the apparent conflict could be resolved in the future by new measurements and/or further refinement of the BBN theory. Should the current standard results persist, the solution presented here would be ruled out. Alternatively, if the pseudo-Dirac neutrino model would be confirmed experimentally, some reconsideration of the BBN model and its inputs might be required.

5 Alternative solutions

Only two of the critical experimental inputs are so far not cross-checked independently by at least one other experiment: The LSND result [3], and the Homestake result [30] for solar neutrinos. The former fixes the $\nu_{\mu} - \nu_{e}$ oscillation parameters and, if disproven, would essentially remove any lower constraint on Δm_{12}^{2} . Comparison of the latter to the other solar neutrino experiments yields the main evidence for the energy-dependence of the solar neutrino deficit. A 30% increase of the Homestake neutrino flux measurement (not compatible with the quoted error), and a reduction of the predicted B^{8} solar neutrino flux by about 20% (which is inside the currently discussed error margin [51]) would make all solar neutrino measurements compatible with a flat suppression factor of about 0.5 (see also [5][7]). This would remove the constraint on $\Delta m_{I/II,1}^{2}$ which, ignoring BBN implications, could then be as large as 10^{-4} eV² (bounded by its potential effect on the atmospheric neutrino anomaly). In order to fix the parameters of the pseudo-Dirac model the verification of LSND by KARMEN [22] and later by other experiments [52] is therefore crucial, and a

verification of the energy dependence of the solar neutrino suppression, e.g. by Borexino [53], is highly desirable. Note that the azimuthal dependence of the atmospheric neutrino suppression, which is observed by only one type of experiment, is not an a priori independent experimental input in this context, but rather a prediction of the model based on the observed non-maximal ν_{μ} suppression.

6 Predictions for current and future experiments

The solution of the neutrino oscillation puzzle proposed in this paper can be checked by several current and future experiments.

Since the solar neutrino problem is solved via ν_e disappearance into sterile neutrinos, SNO [54] should not observe an enhancement of the NC/CC ratio as it would in the case of $\nu_e \rightarrow \nu_\mu$. No day/night effect should be present, but a small seasonal effect might be expected (vacuum solution).

The atmospheric neutrino anomaly should be confirmed, including the azimuthal dependence of the μ/e suppression. Since it is mainly due to ν_{μ} disappearance into sterile neutrinos, the muon deficit (rather than electron excess) should be confirmed. Experiments looking at upward going muons [40] should also see an effect, and current reactor experiments testing $\nu_{\mu} - \nu_{e}$ oscillations [25][55] should continue to observe negative or marginal results. Long baseline accelerator experiments [56][57][58] should not observe a strong ν_{τ} appearance effect, but should observe maximal ν_{μ} disappearance if the $\nu_{\mu} - \nu_{\mu}^{S}$ oscillations lie in the experimentally accessible range. Unfortunately, the low Δm^{2} range ($\Delta m^{2} < 10^{-3} \text{ eV}^{2}$) allowed by Superkamiokande [32] can not be fully tested by any of the currently planned long baseline experiments.

However, ICARUS [56] and MINOS [57], if sensitive enough, should observe energy independent $\nu_{\mu} - \nu_{e}$ oscillations, whose (small) rate should finally settle the value of $\sin^{2}2\theta$ for the LSND result.

 $\nu_{\mu} = \nu_{\tau}$ oscillations should be observed in short baseline accelerator experiments within the next decade. If not by the current experiments NOMAD and CHORUS [44], then by future more sensitive experiments [59] with a slightly lower Δm^2 threshold. $\nu_{\mu} = \nu_{\tau}$ solution (b) would also be within the reach of the long baseline τ appearance experiments [56][58], and could possibly be confused with a signal at low Δm^2 in the atmospheric neutrino region. Therefore both short and long baseline experiments are needed to unambigously confirm or rule out this oscillation scenario. Since m_3 is of order eV or more (hierarchy), τ neutrinos should make up a significant part of the missing dark matter.

If $\nu_{\mu} - \nu_{\tau}$ oscillations would be discovered with sizeable mixing, $\nu_{\tau} - \nu_{\tau}^{S}$ disappearance could be verified in the long term by comparing the τ production rates in short, medium, and long baseline experiments. Some corrections to the atmospheric neutrino spectrum might also be observable.

Lastly, if this pseudo-Dirac neutrino solution would be confirmed, higher values of Y and D/H than currently preferred would be required in the context of standard Big Bang nucleosynthesis in order to respect the bounds on the number of neutrino types derived from this mechanism, or the BBN model would have to be modified.

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