

Tau detection and new physics

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(through video or phone)

Many apologies for
my physical absence
at this meeting!



- 1. Introduction**
- 2. New Physics in propagation (matter effect)**
- 3. New Physics at source and detector**
- 4. Violation of unitarity**
- 5. Light sterile neutrinos**
- 6. Summary**

References:

- Donini, talk at 3rd IDS Plenary Meeting@CERN, March 2009**
- “ ν_τ detection and the IDS-NF baseline”, Donini-Kopp, IDS-NF note**

1. Introduction

Motivation for research on **New Physics** and τ detection

- Just like at B factories, **high precision** measurements of ν oscillation in future experiments will allow us to probe **physics beyond SM** by looking at deviation from SM+massive ν .
- If θ_{13} turns out to be large, search for **new physics** and test of **unitarity** will be even more important subjects at ν factory. (cf. $\sin^2\theta_{13}=0.02\pm 0.01 @1\sigma$, Fogli et al, arXiv:0905.3549 [hep-ph])

- τ detection is potentially advantage of ν factory:
- Detection of large number of τ 's is possible at ν factory
- No ν_τ contamination at a neutrino factory (cf. super-beam, [Van de Vyver-Zucchelli, NIM A385:91,1997])
- τ channels in 3 family model are not so useful:
- **(golden)** @4000km+7500km is better than **(silver)+(golden)** @4000km to solve intrinsic degeneracy [ISS report]
- **(disappearance)** is better than **(discovery)** to measure atmospheric parameters [Donini, 0th IDS mtg@CERN]

$$\nu_e \rightarrow \nu_\mu$$

golden channel

$$\nu_\mu \rightarrow \nu_\mu$$

disappearance channel

$$\nu_e \rightarrow \nu_\tau$$

silver channel

$$\nu_\mu \rightarrow \nu_\tau$$

discovery channel

- If 3 flavor unitarity is guaranteed, then roughly speaking, we could guess **(discovery)** from **(golden) + (disappearance)** at ν factory from 3 flavor unitarity:

$$P(\nu_{\mu} \rightarrow \nu_e) + P(\nu_{\mu} \rightarrow \nu_{\mu}) + P(\nu_{\mu} \rightarrow \nu_{\tau}) = 1$$

disappearance channel

discovery channel

$$\nu_e \rightarrow \nu_{\mu}$$

golden channel

Probability of the time reversal process could be obtained if we can guess the CP phase.

- Intuitively, therefore, τ detection is supposed to be important to test New Physics which violates unitarity.
→ Quantitative estimate is necessary to draw conclusions.

New physics which can be probed at a neutrino factory includes:

- ◆ Non standard interactions in propagation
- ◆ Non standard interactions at production / detection
- ◆ Violation of unitarity due to heavy particles
- ◆ Schemes with light sterile neutrinos

$$\sum_{\beta=e,\mu,\tau} P(\nu_\alpha \rightarrow \nu_\beta) = 1$$

Scenarios	3 flavor unitarity
NSI in propagation	✓
NSI at production / detection	✗
Violation of unitarity due to heavy particles	✗
Light sterile neutrinos	✗

τ detectors

- **Emulsion Cloud Chamber (ECC)**

Prototype: the OPERA detector at the CNGS

active target: lead

spectrometers to measure the charge

only $\tau \rightarrow \mu$ decay is used: detection efficiency $\sim O(5\%)$

→ **Proposal of Magnetized Emulsion Cloud Chamber (MECC)**

active target: iron

$\tau \rightarrow \mu$ decay + $\tau \rightarrow e$ decay + $\tau \rightarrow$ hadron decay are used:

detection efficiency $\sim O(25\%)$

- **Liquid Argon TPC (LAr-TPC)**

Prototype: the ICARUS T600 at the CNGS

2. New Physics in propagation (matter effect)

● Oscillation probability w/ NP in propagation

$$\mathcal{M} \equiv U \text{diag}(E_j) U^{-1} + \mathcal{A} = \tilde{U} \text{diag}(\tilde{E}_j) \tilde{U}^{-1}$$

$$\mathcal{A} \equiv A \begin{pmatrix} 1 + \epsilon_{ee} & \epsilon_{e\mu} & \epsilon_{e\tau} \\ \epsilon_{e\mu}^* & \epsilon_{\mu\mu} & \epsilon_{\mu\tau} \\ \epsilon_{e\tau}^* & \epsilon_{\mu\tau}^* & \epsilon_{\tau\tau} \end{pmatrix}$$

$$A \equiv \sqrt{2} G_F N_e$$

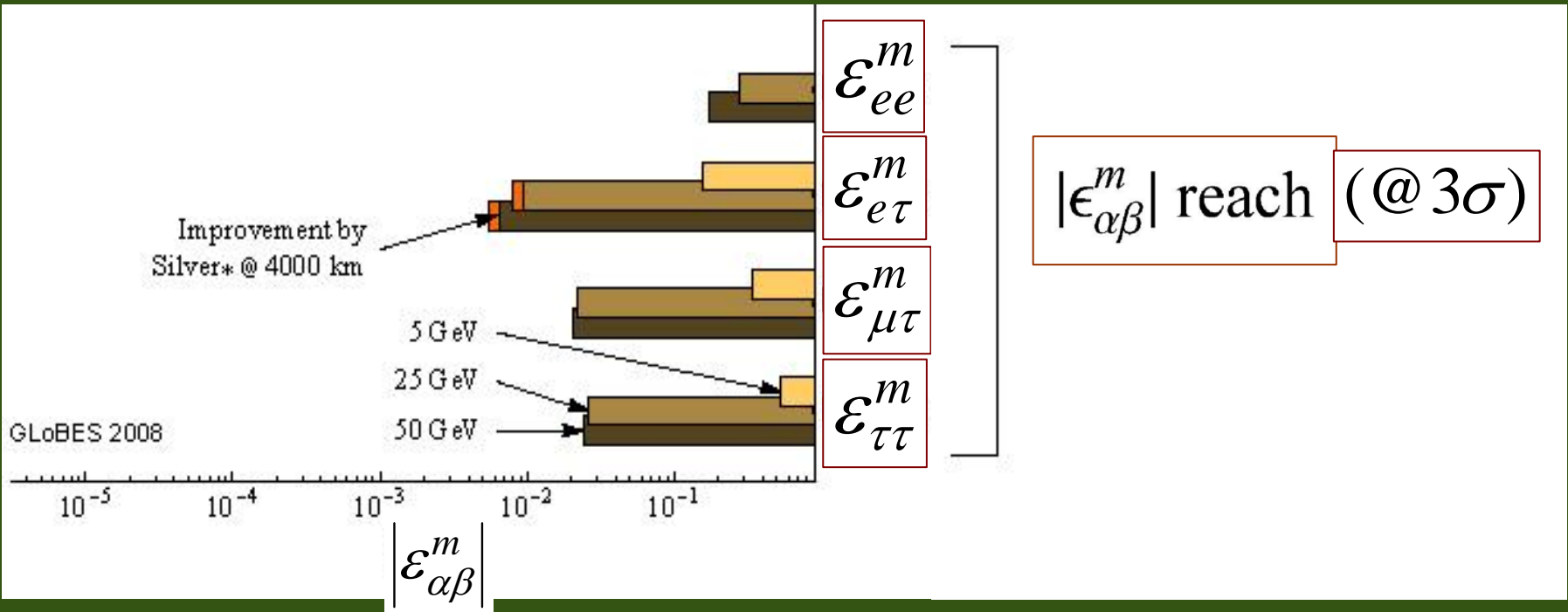
$N_e \equiv$ electron density

$$P(\nu_\alpha \rightarrow \beta) = \left| \left[\tilde{U} \exp \left\{ -i \text{diag}(\tilde{E}_j) L \right\} \tilde{U}^{-1} \right]_{\beta\alpha} \right|^2$$

- Mass matrix \mathcal{M} is hermitian
- There are only 3 flavors



Oscillation probability satisfies **3 flavor unitarity**



- Improvement by silver channel is modest
- Impact of discovery channel has not been investigated but improvement is expected to be modest, too, because of 3 flavor unitarity

Sensitivity at ν factory w/ near τ detector

Tang-Winter,
Phys.Rev.D80:053001,2009

- Near τ detector does not improve, either

	Without ν_τ ND5	With ν_τ ND5
$ \epsilon_{e\tau}^m $	0.004	0.004
$ \epsilon_{\mu\tau}^m $	0.02	0.02

ND5: mass 2 kton, L=1 km

3. New Physics at source and detector

Grossman, Phys. Lett.
B359, 141 (1995)

● NP at source

$$\mu^+ \rightarrow e^+ + \bar{\nu}_\mu + \nu_\mu^s$$

$$\nu_e^s = \nu_e + \epsilon_{e\mu}^s \nu_\mu$$

Effective eigenstate

$$\begin{pmatrix} \nu_e^s \\ \nu_\mu^s \end{pmatrix} = \begin{pmatrix} 1 & \epsilon_{e\mu}^s \\ -\epsilon_{e\mu}^s & 1 \end{pmatrix} \begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix}$$

● NP at detector

$$\nu_\mu^d + n \rightarrow \mu^- + p$$

$$\nu_\mu^d = \nu_\mu - \epsilon_{e\mu}^d \nu_e$$

Effective eigenstate

$$\begin{pmatrix} \nu_e^d \\ \nu_\mu^d \end{pmatrix} = \begin{pmatrix} 1 & \epsilon_{e\mu}^d \\ -\epsilon_{e\mu}^d & 1 \end{pmatrix} \begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix}$$

- Oscillation probability w/ NP @ source/detector

$$\mathcal{M} \equiv U \text{diag}(E_j) U^{-1} + \mathcal{A}_0 = \tilde{U}_0 \text{diag}(\tilde{E}_j^0) \tilde{U}_0^{-1}$$

$$\mathcal{A}_0 \equiv A \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$P(\nu_\alpha \rightarrow \beta) = \left| \left[U^d \tilde{U}_0 \exp \left\{ -i \text{diag}(\tilde{E}_j^0) L \right\} \tilde{U}_0^{-1} (U^s)^{-1} \right]_{\beta\alpha} \right|^2$$

- There are only 3 flavors
- But matrix $U^d \mathcal{M} (U^s)^{-1}$ is **not** hermitian



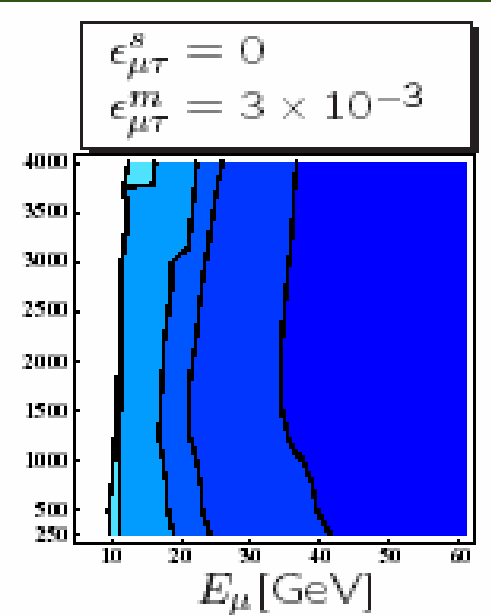
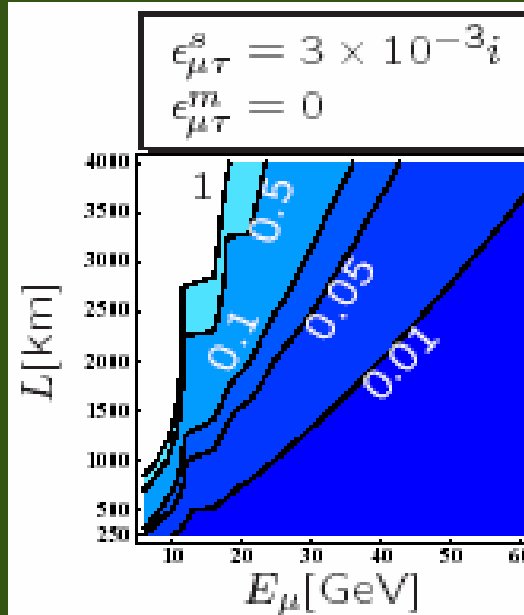
Oscillation probability does **not** satisfy 3 flavor unitarity

Sensitivity to $\epsilon_{\mu\tau}$ at ν factory

$$\nu_{\mu} \rightarrow \nu_{\tau}$$

$$|\epsilon_{\mu\tau}^{s,m}| = 3 \times 10^{-3}$$

Required data size in
unit of $10^{21} \mu \times 100\text{kt}$



■ The expected sensitivity is $\epsilon \gtrsim \mathcal{O}(10^{-4})$.

Sato: ISS 2nd
plenary @ KEK

	$\epsilon_{e\mu}^{s,m} (\epsilon_{\mu e}^s)$	$\epsilon_{e\tau}^{s,m}$	$\epsilon_{\mu\tau}^{s,m}$
$\nu_e \rightarrow \nu_{\mu}$	△	△	×
$\nu_{\mu} \rightarrow \nu_{\mu}$	×	×	○
$\nu_e \rightarrow \nu_{\tau}$	×	○	△
$\nu_{\mu} \rightarrow \nu_{\tau}$	×	△	○
$\nu_{\mu} \rightarrow \nu_e$	△	×	×
$\nu_e \rightarrow \nu_e$	×	×	×

Sensitivity to $\epsilon_{e\tau}$, $\epsilon_{\mu\tau}$ at ν factory

Tang-Winter,
Phys.Rev.D80:053001,2009

- Near τ detector improves sensitivity

	Without ν_τ ND5	With ν_τ ND5
$ \epsilon_{e\tau}^s $	0.004	0.0007
$ \epsilon_{\mu\tau}^s $	0.4	0.0006

ND5: mass 2 kton, L=1 km

4. Violation of unitarity w/o light ν_s (Minimal Unitarity Violation)

Antusch, Biggio, Fernandez-Martinez, Gavela, Lopez-Pavon, JHEP0610,084, '06

In generic see-saw models, after integrating out ν_R , the kinetic term gets modified, and unitarity is expected to be violated.

$$L = \frac{1}{2} \left(i \bar{\nu}_\alpha \not{\partial} K_{\alpha\beta} \nu_\beta - \bar{\nu}^c_\alpha M_{\alpha\beta} \nu_\beta \right) - \frac{g}{\sqrt{2}} \left(W_\mu^+ \bar{l}_\alpha \gamma^\mu P_L \nu_\alpha + h.c. \right) + \dots$$

rescaling ν



$$L = \frac{1}{2} \left(i \bar{\nu}_i \not{\partial} \nu_i - \bar{\nu}^c_i m_{ii} \nu_i \right) - \frac{g}{\sqrt{2}} \left(W_\mu^+ \bar{l}_\alpha \gamma^\mu P_L N_{\alpha i} \nu_i \right) + \dots$$

N: non-unitary

● Oscillation probability w/ Minimal Unitarity Violation

$$P(\nu_\alpha \rightarrow \beta) = \left| \left[H \tilde{U} \exp \left\{ -i \text{diag}(\tilde{E}_j) L \right\} \tilde{U}^{-1} H \right]_{\beta\alpha} \right|^2$$
$$U \text{diag}(E_j) U^{-1} + H \mathcal{A}_0 H = \tilde{U} \text{diag}(\tilde{E}_j) \tilde{U}^{-1}$$

$$\mathbf{N} \equiv \mathbf{HU}$$

$\eta = \mathbf{H}^{-1}$: deviation from unitarity

- There are only 3 flavors
- But matrix $H\tilde{U}$ is **not** unitary



Oscillation probability does **not** satisfy 3 flavor unitarity

Sensitivity to MUV parameters at ν factory (1)

- 4kt OPERA-like near detector @100 m

Antusch et al,
JHEP0610,084, '06

$$\nu_{\mu} \rightarrow \nu_{\tau}$$

$$|\eta_{\mu\tau}| < 1.3 \times 10^{-3} \quad (\text{present: } 6.5 \times 10^{-3})$$

$$H \equiv 1 + \eta$$

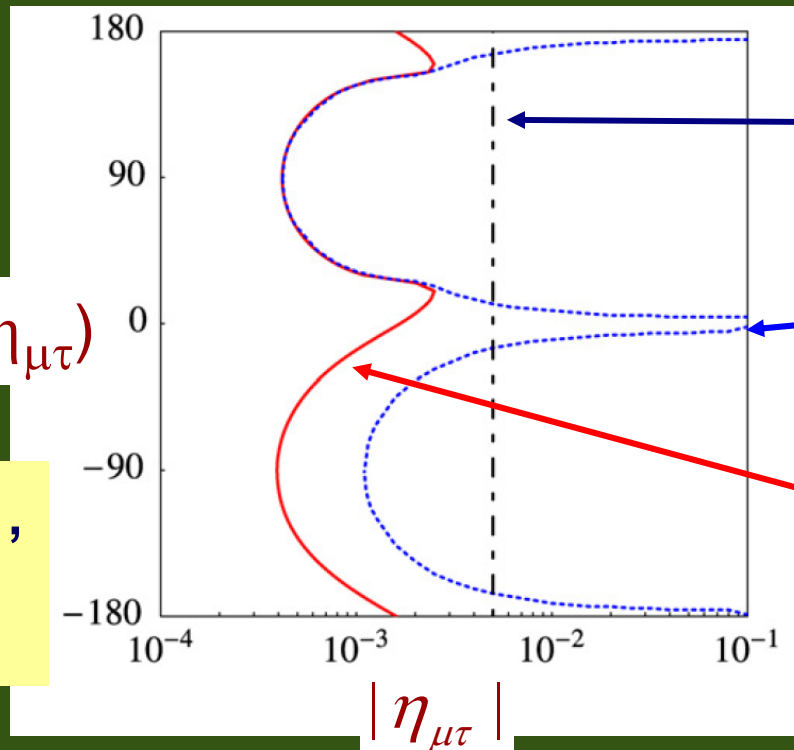
- 5kt OPERA-like far detector @130 km

Fernandez-Martinez et al,
PLB649:427,'07

$$\nu_{\mu} \rightarrow \nu_{\tau}$$

$$\arg(\eta_{\mu\tau})$$

For non-trivial $\arg(\eta_{\mu\tau})$,
one order of magnitude
improvement for $|\eta_{\mu\tau}|$



Present bound
from $\tau \rightarrow \mu \gamma$

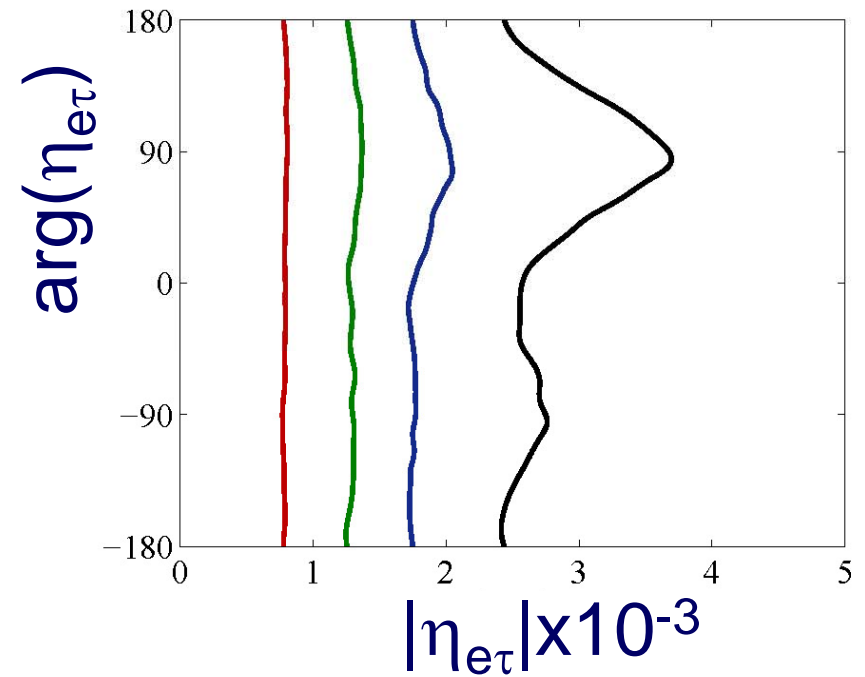
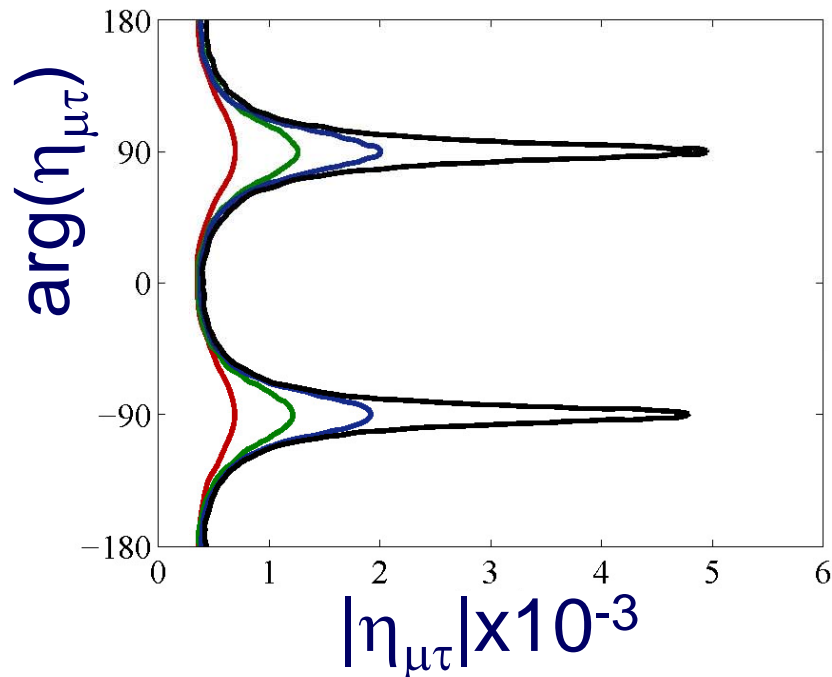
Sensitivity to
 $\arg(\eta_{\mu\tau})$

Sensitivity to
 $|\eta_{\mu\tau}|$

Sensitivity to MUV parameters at ν factory (2)

τ detectors at
 $L=1\text{km}$ & 7500km

Antusch, Blennow, Fernandez-Martinez,
Lopez-Pavon, Phys.Rev.D80:033002,2009



Near detector mass = 10kt, 1kt, 100t, 0

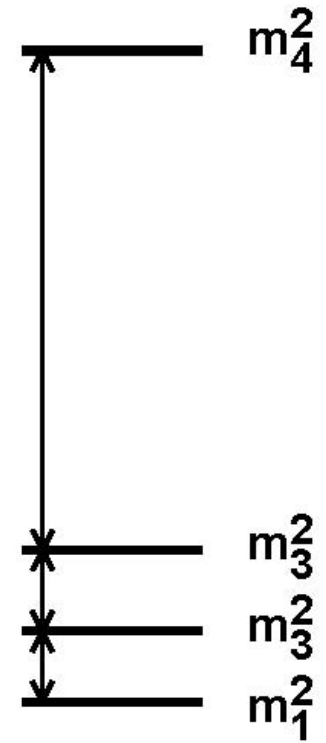
1kt for near detector mass seems to be enough

5. Light sterile neutrinos

(3+1)-scheme w/o LSND: still a possible scenario, provided that the mixing angles satisfy all the constraints of the negative results

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \\ \nu_s \end{pmatrix} = U \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \\ \nu_4 \end{pmatrix}$$

$$U = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} & U_{e4} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} & U_{\mu4} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} & U_{\tau4} \\ U_{s1} & U_{s2} & U_{s3} & U_{s4} \end{pmatrix}$$



Obviously oscillation probability does **not** satisfy **3 flavor unitarity**

Sensitivity to θ_{24} , θ_{34} at ν factory

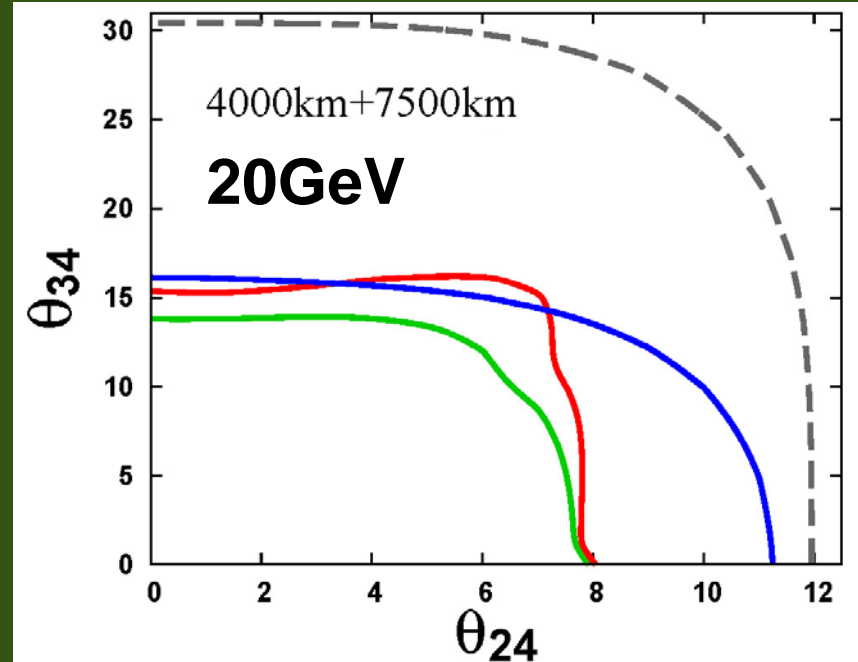
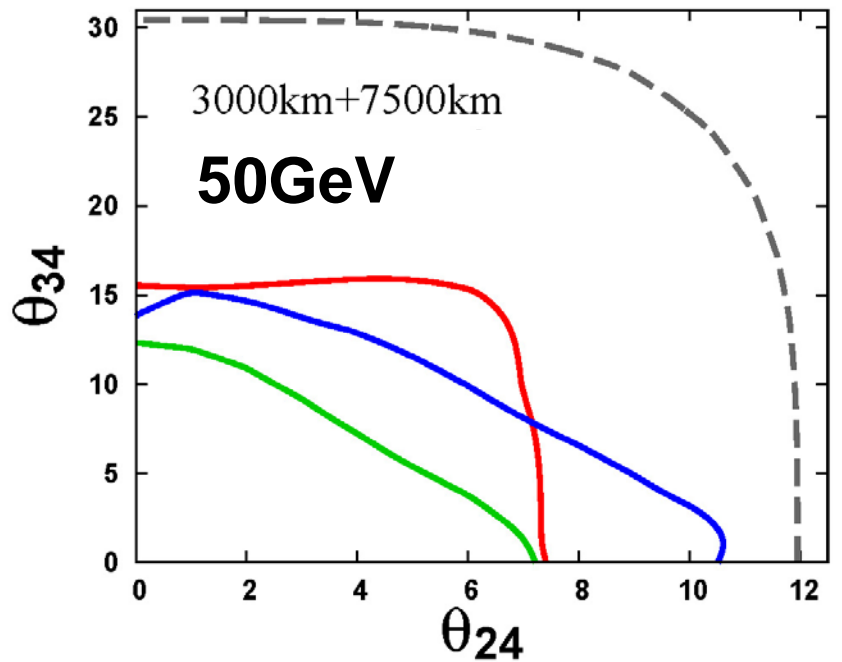
Donini et al, JHEP
0908:041,2009

$$U = R_{34}(\theta_{34}, 0) R_{24}(\theta_{24}, 0) R_{23}(\theta_{23}, \delta_3) R_{14}(\theta_{14}, 0) R_{13}(\theta_{13}, \delta_2) R_{12}(\theta_{12}, \delta_1)$$

θ_{34} : ratio of $\nu_\mu \leftrightarrow \nu_\tau$ and $\nu_\mu \leftrightarrow \nu_s$ in ν_{atm}

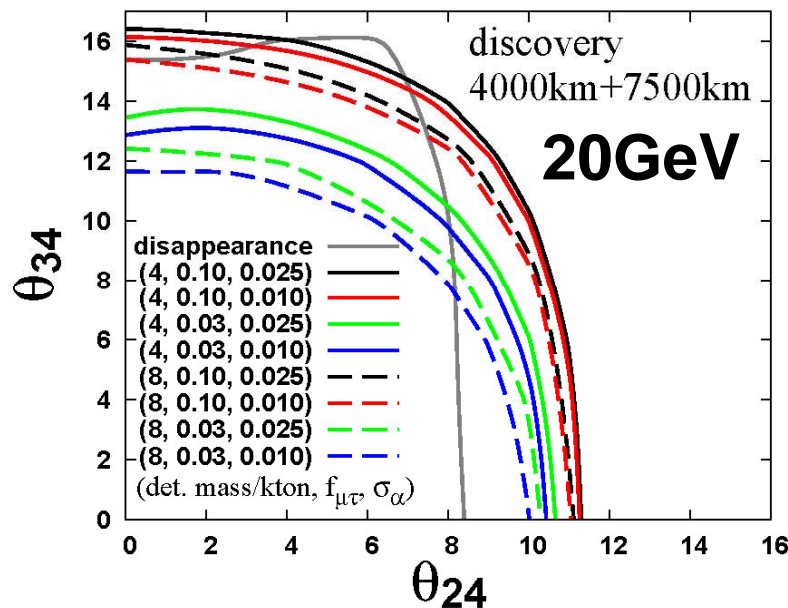
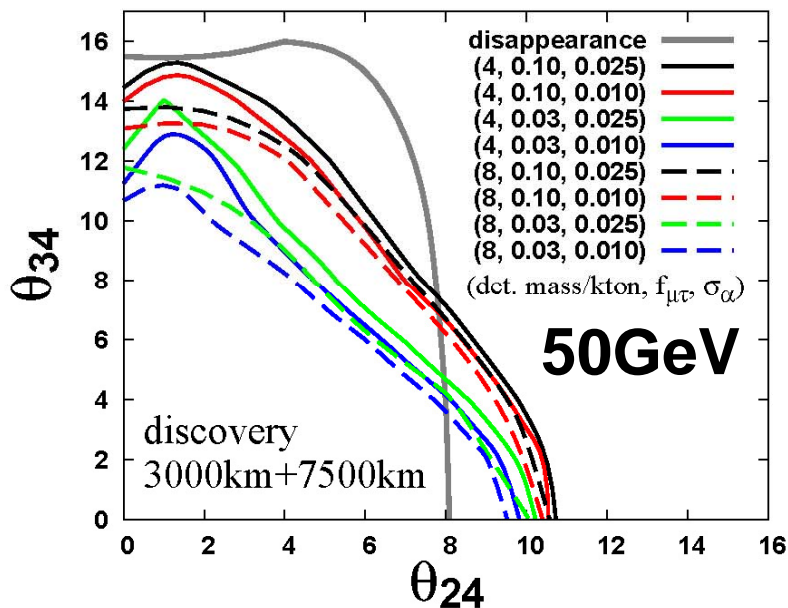
θ_{24} : ratio of $\sin^2\left(\frac{\Delta m_{\text{atm}}^2 L}{4E}\right)$ and $\sin^2\left(\frac{\Delta m_{\text{SBL}}^2 L}{4E}\right)$ in ν_{atm}

--- current - - - disappearance - - - discovery - - - combined



Dependence of sensitivity on systematic errors

Donini et al, JHEP
0908:041,2009



$f_{\mu\tau}$: uncorrelated bin-to-bin systematic error (error in detection efficiency in each bin etc.)

σ_α : correlated systematic error (error in detector volume etc.)

In previous page, $f_{\mu\tau}=10\%$, $\sigma_\alpha=2.5\%$ (black solid lines above) was assumed

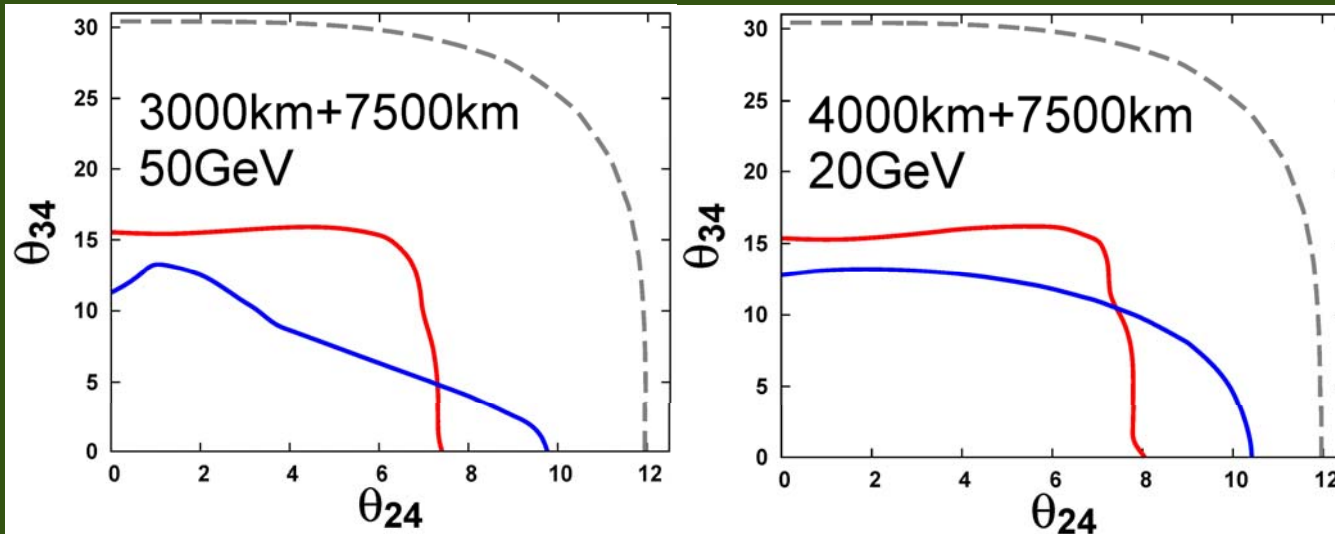
By placing a near τ detector, systematic errors could be reduced

cf. Reduction of systematic errors in the 2 detector complex at reactor experiments

Minakata et al.,
Phys.Rev.D68:033017,2003

CHOOZ-like	absolute normalization	relative normalization (expected)	relative/absolute
flux	2.1%	0.0%	0
number of protons	0.8%	0.3%	0.38
detection efficiency	1.5%	0.7%	0.47
total	2.7%	0.8%	
for bins	8.1%	2.4%	

If we can attain $f_{\mu\tau}=3\%$, $\sigma_{\alpha}=1\%$ w/ ND, then discovery channel could perform better than disappearance:

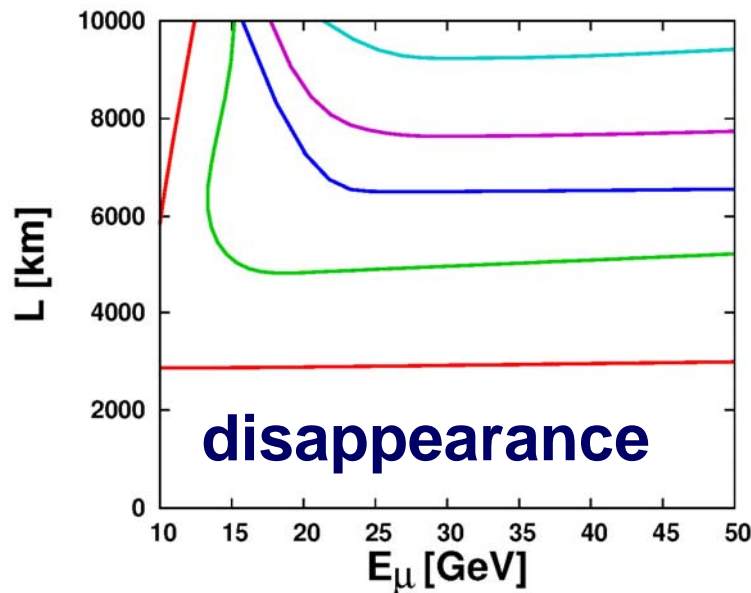


$f_{\mu\tau}=3\%$, $\sigma_{\alpha}=1\%$

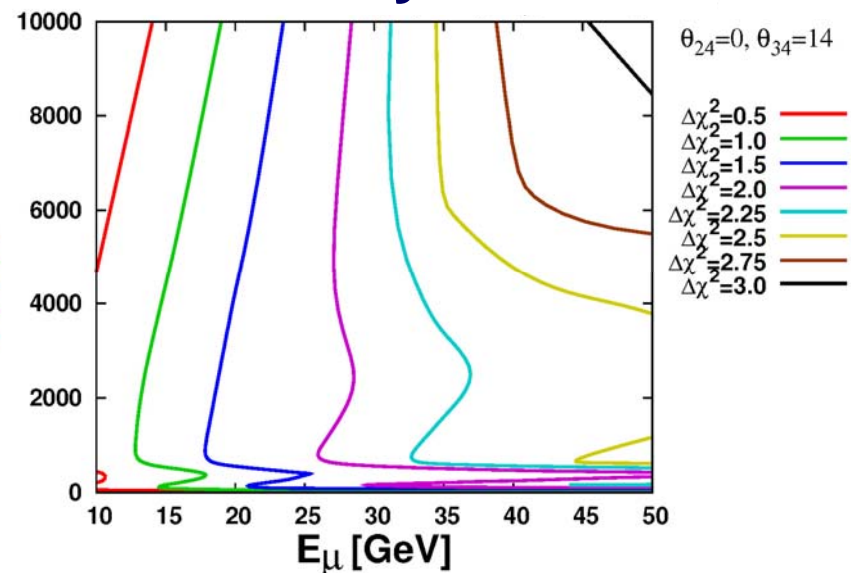
--- current
— disappearance
— discovery

Which τ detector is less important, @3000km or @7500km ?

Contour plot of significance for signal with $\theta_{24}=0, \theta_{34}=14$



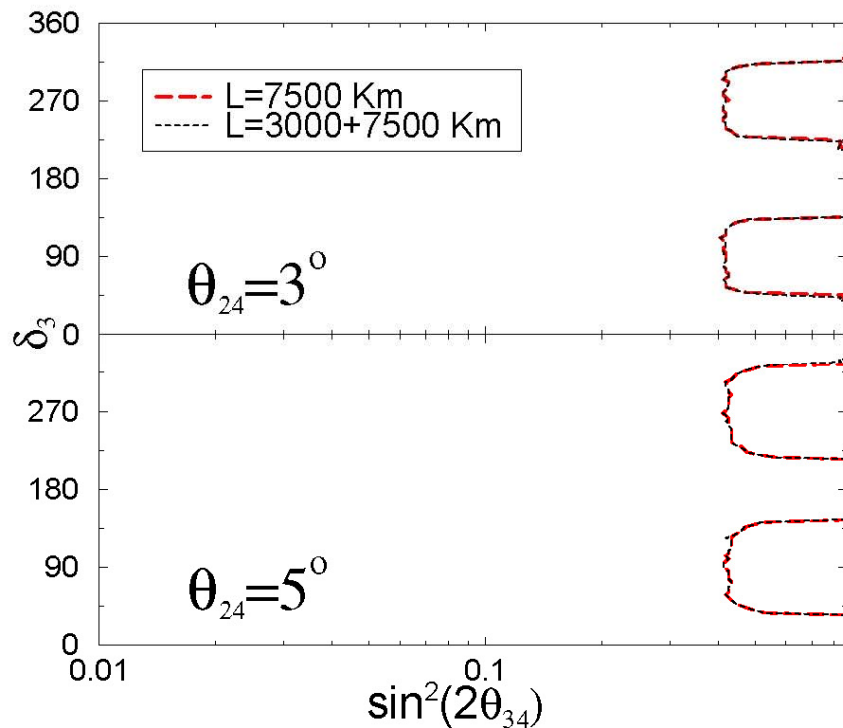
discovery



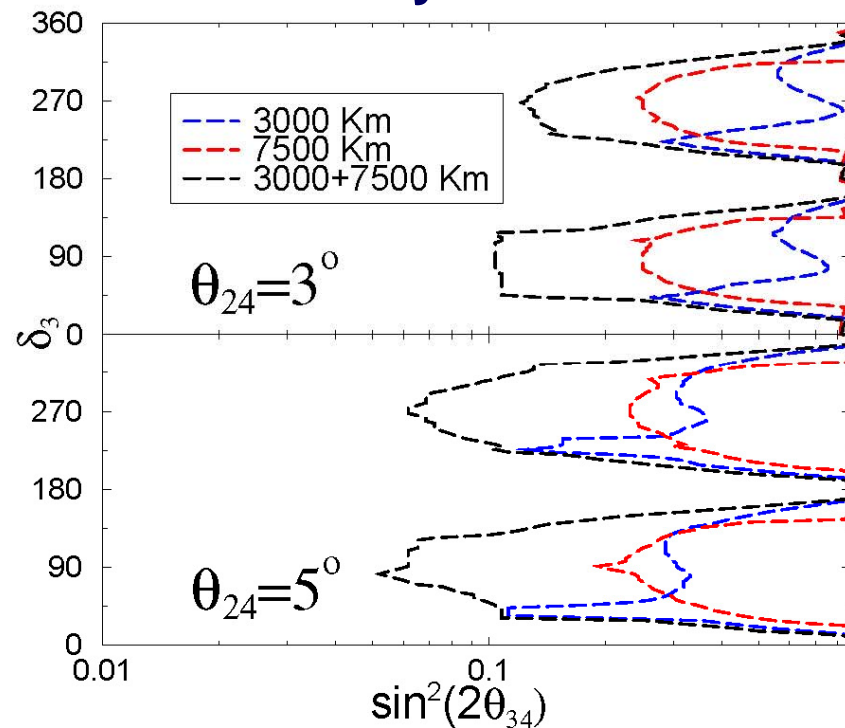
For 50GeV (20GeV), $L=3000$ km ($L=4000$ km) performs (slightly) poor. This is also the case w/ disappearance.

One @7500km seems better in most cases

disappearance only



disappearance
+ discovery



Discovery channel is crucial to measure the new CP phase

6. Summary

- ν factory can search for new physics beyond the standard model with ν mass, such as
 - Non standard interactions in propagation
 - Non standard interactions at production / detection
 - Violation of unitarity due to heavy particles
 - Schemes with light sterile neutrinos
(the last 3 scenarios violate 3 flavor unitarity)
- In absence of 3 flavor unitarity, τ detectors in principle give us important information on New Physics, but in practice it depends on the statistical/systematic errors.
- In some cases disappearance channel performs better than discovery one, but again it depends on the systematic errors.

- To measure the new CP phase due to New Physics, discovery channel is crucial.
- Near τ detectors are useful not only to improve sensitivity to New Physics by themselves, but also to reduce the systematic errors of the far τ detectors.
- Far τ detectors @7500km seem to be more useful than those @3000km or 4000km.
- Study on the systematic errors of τ detectors is very important.
- Study on parameter degeneracy in the presence of New Physics has to be done:
 - Unitarity violation [Goswami-Ota, Phys.Rev.D78:033012,2008]
 - NP in propagation [Gago et al, arXiv:0904.3360 [hep-ph]]

- **We have physics case for τ channels, but the technological requirements to take full advantage of them are not yet met at this moment.**
- **No τ detector is needed in the baseline scenario, but we have to keep going on R&D to take advantage of better understanding of τ detectors after OPERA and to come up with a possible proposal for τ detectors in a few years from now.**

Backup slides

Oscillation probability w/ Minimal Unitarity Violation

Antusch et al,
Phys.Rev.D80,
033002, 2009

$$\hat{P}_{\mu\mu} = P_{\mu\mu}^{\text{SM}} + 4\varepsilon_{\mu\mu} + 4\varepsilon_{\mu\mu}^2 + 4\left[-\varepsilon_{\mu\mu} + 2\text{Re}(\varepsilon_{\mu\tau})\delta\theta_{23} - 2\delta\theta_{23}(\varepsilon_{\mu\mu} - \varepsilon_{\tau\tau})\frac{A}{E_3}\right]\sin^2\left(\frac{E_3L}{2}\right) - [2\text{Re}(\varepsilon_{\mu\tau}) - \delta\theta_{23}(\varepsilon_{\mu\mu} - \varepsilon_{\tau\tau})]AL\sin(E_3L) + \mathcal{O}(\varepsilon_{\alpha\beta}^2),$$

$$\hat{P}_{\mu\tau} = P_{\mu\tau}^{\text{SM}} + 4|\varepsilon_{\mu\tau}|^2 + \left[2\text{Re}(\varepsilon_{\mu\mu} + \varepsilon_{\tau\tau}) + 8\delta\theta_{23}(\varepsilon_{\mu\mu} - \varepsilon_{\tau\tau})\frac{A}{E_3}\right]\sin^2\left(\frac{E_3L}{2}\right) + [-2\text{Im}(\varepsilon_{\mu\tau}) - \delta\theta_{23}(\varepsilon_{\mu\mu} - \varepsilon_{\tau\tau})AL] \times \sin(E_3L) - \sqrt{2}\text{Im}\left\{\varepsilon_{e\tau}\left[\frac{E_2}{A}\sin(2\theta_{12}) + \frac{2E_3s_{13}e^{i\delta}}{A-E_3}\right]\right\}\sin\left(\frac{AL}{2}\right)\sin\left(\frac{E_3L}{2}\right)\sin\left(\frac{E_3-A}{2}L\right) + \sqrt{2}\text{Re}\left\{\varepsilon_{e\tau}\left[\frac{E_2}{A}\sin(2\theta_{12})\sin\left(\frac{AL}{2}\right)\cos\left(\frac{E_3-A}{2}L\right) - \frac{2E_3s_{13}e^{i\delta}}{A-E_3}\cos\left(\frac{AL}{2}\right)\sin\left(\frac{E_3-A}{2}L\right)\right]\right\}\sin\left(\frac{E_3L}{2}\right) + \mathcal{O}(\varepsilon_{\alpha\beta}^2),$$

$$\hat{P}_{e\mu} = P_{e\mu}^{\text{SM}} + |\varepsilon_{e\tau}|^2\sin^2\left(\frac{E_3L}{2}\right) + \text{Im}\left\{\varepsilon_{e\tau}\left[\frac{1}{2}\frac{E_2}{A}\sin(2\theta_{12}) + \frac{E_3s_{13}e^{i\delta}}{A-E_3}\right]\right\}\sin\left(\frac{AL}{2}\right)\sin\left(\frac{E_3L}{2}\right)\sin\left(\frac{E_3-A}{2}L\right) + \text{Re}\left\{\varepsilon_{e\tau}\left[\frac{1}{\sqrt{2}}\frac{E_2}{A}\sin(2\theta_{12})\sin\left(\frac{AL}{2}\right)\cos\left(\frac{E_3-A}{2}L\right) - \frac{2\sqrt{2}E_3s_{13}e^{i\delta}}{A-E_3}\cos\left(\frac{AL}{2}\right)\sin\left(\frac{E_3-A}{2}L\right)\right]\right\}\sin\left(\frac{E_3L}{2}\right) + \mathcal{O}(\varepsilon^3),$$

$$\hat{P}_{e\tau} = P_{e\tau}^{\text{SM}} + 4|\varepsilon_{e\tau}|^2 - 2\left[|\varepsilon_{e\tau}|^2 - \frac{\sqrt{2}E_3s_{13}}{A-E_3}\text{Re}(\varepsilon_{e\tau}e^{i\delta})\right]\sin^2\left(\frac{E_3-A}{2}L\right) - 2\left[|\varepsilon_{e\tau}|^2 - \frac{1}{\sqrt{2}}\frac{E_2}{A}\sin(2\theta_{12})\text{Re}(\varepsilon_{e\tau})\right] \times \sin^2\left(\frac{AL}{2}\right) - \text{Im}\left\{\varepsilon_{e\tau}^*\left[\frac{1}{\sqrt{2}}\frac{E_2}{A}\sin(2\theta_{12})\sin(AL) - \frac{\sqrt{2}E_3s_{13}e^{-i\delta}}{A-E_3}\sin(\{E_3-A\}L)\right]\right\} - 2\sqrt{2}\text{Re}\left\{\varepsilon_{e\tau}\left[\frac{1}{2}\frac{E_2}{A}\sin(2\theta_{12}) - \frac{E_3s_{13}e^{i\delta}}{A-E_3}\right]\right\}\sin\left(\frac{AL}{2}\right)\cos\left(\frac{E_3L}{2}\right)\sin\left(\frac{E_3-A}{2}L\right) + \text{Im}\left\{\varepsilon_{e\tau}\left[\sqrt{2}\frac{E_2}{A}\sin(2\theta_{12})\sin\left(\frac{AL}{2}\right)\cos\left(\frac{E_3-A}{2}L\right) + \frac{2\sqrt{2}E_3s_{13}e^{i\delta}}{A-E_3}\cos\left(\frac{AL}{2}\right)\sin\left(\frac{E_3-A}{2}L\right)\right]\right\}\cos\left(\frac{E_3L}{2}\right) + \mathcal{O}(\varepsilon^3).$$

$$P_{\mu\mu} = 1 - 2\theta_{24}^2 - \left[1 - 4(\delta\theta_{23})^2 - 2\theta_{24}^2 + \theta_{34}^2 \frac{A_n}{\Delta_{31}} \left(4\delta\theta_{23} - \theta_{34}^2 \frac{A_n}{\Delta_{31}} \right) \right] \sin^2 \frac{\Delta_{31}L}{2} - (A_n L) \left\{ 2\theta_{24} \theta_{34} \cos \delta_3 - \frac{\theta_{34}^2}{2} \left(4\delta\theta_{23} - \theta_{34}^2 \frac{A_n}{2\Delta_{31}} \right) \right\} \sin \Delta_{31}L + O(\epsilon^5), \quad (16)$$

$$P_{\mu\tau} = \left\{ 1 - 4(\delta\theta_{23})^2 - \theta_{24}^2 - \theta_{34}^2 \left[1 - \frac{\theta_{34}^2}{3} - \frac{A_n}{\Delta_{31}} \left(4\delta\theta_{23} - \theta_{34}^2 \frac{A_n}{\Delta_{31}} \right) \right] \right\} \sin^2 \frac{\Delta_{31}L}{2} + \left\{ \theta_{24} \theta_{34} \sin \delta_3 + (A_n L) \left[2\theta_{24} \theta_{34} \cos \delta_3 - \frac{\theta_{34}^2}{2} \left(4\delta\theta_{23} - \theta_{34}^2 \frac{A_n}{2\Delta_{31}} \right) \right] \right\} \sin \Delta_{31}L + O(\epsilon^5), \quad (17)$$

Numbers of events in (3+1)-scheme

Donini, Fuki, Lopez-Pavon, Meloni, Yasuda,
JHEP 0908:041,2009

$$\nu_\mu \rightarrow \nu_\tau \quad \bar{\nu}_e \rightarrow \bar{\nu}_\tau \quad \nu_\mu \rightarrow \nu_\tau \quad \bar{\nu}_e \rightarrow \bar{\nu}_\tau$$

$(\theta_{13}; \theta_{14}; \theta_{24}; \theta_{34})$	$N_{\tau^-}^{3000}$	$N_{\tau^+}^{3000}$	$N_{\tau^-}^{7500}$	$N_{\tau^+}^{7500}$
$(5^\circ; 5^\circ; 5^\circ; 20^\circ)$	559	10	544	2
$(5^\circ; 5^\circ; 10^\circ; 20^\circ)$	474	11	529	2
$(5^\circ; 5^\circ; 10^\circ; 30^\circ)$	384	18	454	3
$(5^\circ; 5^\circ; 10^\circ; 30^\circ)$	384	18	454	3
$(10^\circ; 5^\circ; 5^\circ; 20^\circ)$	522	22	512	2
$(10^\circ; 5^\circ; 10^\circ; 20^\circ)$	443	22	498	2
$(10^\circ; 5^\circ; 5^\circ; 30^\circ)$	397	30	413	4
$(10^\circ; 5^\circ; 10^\circ; 30^\circ)$	361	30	428	4
3 families, $\theta_{13} = 5^\circ$	797	3	666	0
3 families, $\theta_{13} = 10^\circ$	755	12	632	1

Number of events
 2×10^{20} flux
1 year
1 Kton MECC
perfect efficiency

Dependence of sensitivity on systematic errors in (3+1)-scheme

Donini, Fuki, Lopez-Pavon, Meloni, Yasuda, JHEP 0908:041,2009

