

**Signatures of sterile  $\nu$  mixing  
in high energy cosmic  $\nu$  flux**

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# 1. Introduction

## Standard framework of 3 flavor $\nu$ oscillation

### Mixing matrix

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

Functions of mixing angles  $\theta_{12}$ ,  $\theta_{23}$ ,  $\theta_{13}$ , and CP phase  $\delta$

### Information we have obtained so far:

$\nu_{\text{solar}}$  + KamLAND (reactor)

$$\theta_{12} \cong \frac{\pi}{6}, \Delta m_{21}^2 \cong 8 \times 10^{-5} \text{ eV}^2$$

$\nu_{\text{atm}}$  + K2K, MINOS (accelerators)

$$\theta_{23} \cong \frac{\pi}{4}, |\Delta m_{32}^2| \cong 2.5 \times 10^{-3} \text{ eV}^2$$

CHOOZ (reactor)

$$|\theta_{13}| \leq \sqrt{0.15/2}$$

# Original motivation for sterile $\nu$

● accelerator  $\nu$  anomaly: **LSND**

$$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$$

→  $\Delta m^2 \cong O(1) \text{eV}^2$  ??  
 $\sin^2 2\theta \cong O(10^{-2})$

$$\Delta m_{\text{sol}}^2 \sim 10^{-4} \text{eV}^2$$

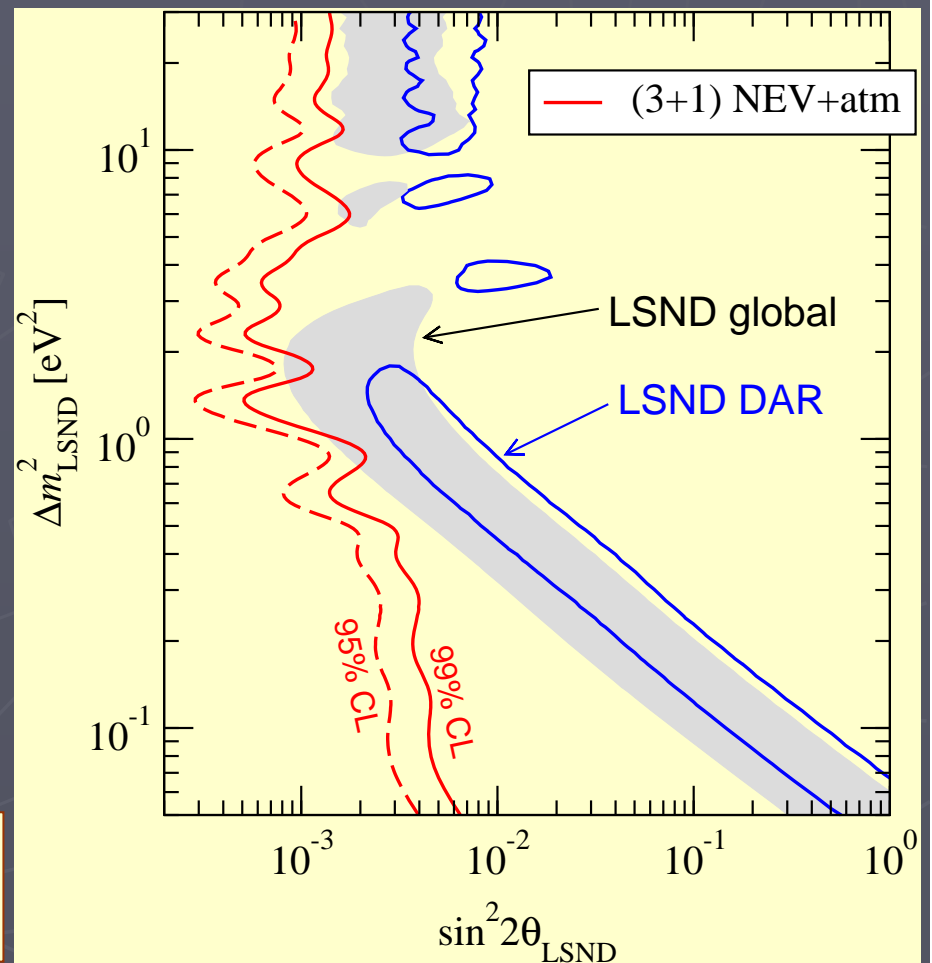
$$\Delta m_{\text{atm}}^2 \sim 10^{-3} \text{eV}^2$$

$$\Delta m_{\text{LSND}}^2 \sim O(1) \text{eV}^2$$

→ at least one more massive  $\nu$  eigenstate is required

→ From LEP any extra  $\nu$  flavor eigenstate has to be sterile  $\nu$  ( $\nu_s$ )

Maltoni et al., hep-ph/0405172



## 2. $N_\nu=4$ schemes

Because of the hierarchy:  $\Delta m_{\text{sol}}^2 \ll \Delta m_{\text{atm}}^2 \ll \Delta m_{\text{LSND}}^2$

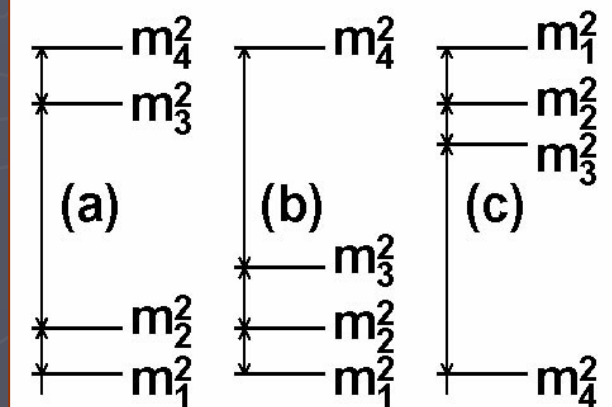
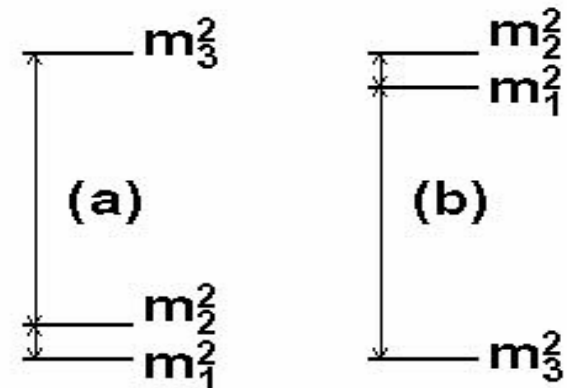
$N_\nu=3$  schemes can't explain LSND.

$$\Delta m_{21}^2 = \Delta m_{\text{sol}}^2, \Delta m_{32}^2 = \Delta m_{\text{atm}}^2$$

$N_\nu=4$  schemes may be able to explain all.

➡ It turns out that it doesn't work.

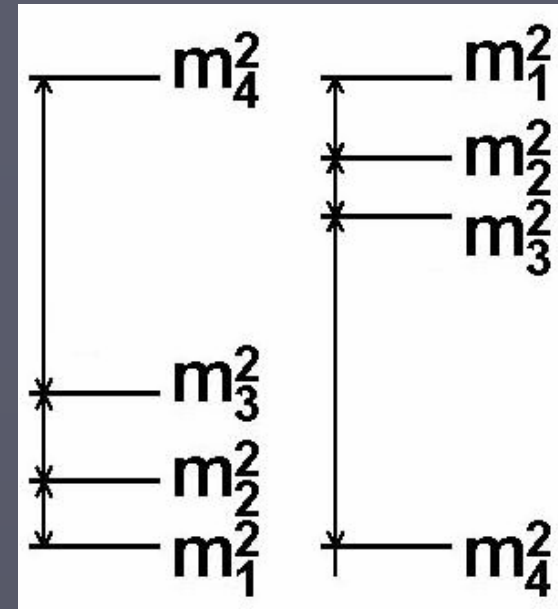
$$\Delta m_{21}^2 = \Delta m_{\text{sol}}^2, \Delta m_{32}^2 = \Delta m_{\text{atm}}^2, \Delta m_{43}^2 = \Delta m_{\text{LSND}}^2$$



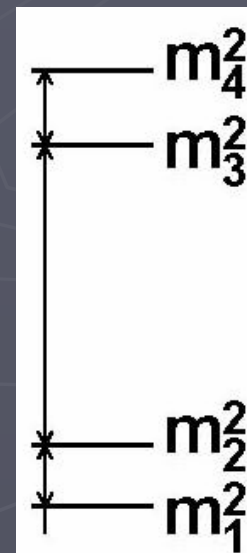
# $N_\nu = 4$ schemes to explain LSND

scheme	accelerator + reactor	solar + atmospheric
(3+1)	tension	✓
(2+2)	✓	excluded

Any of 4  $\nu$  scenarios doesn't work.



(3+1)-scheme



(2+2)-scheme

(2+2)-scheme

$$\eta_s \equiv |\mathbf{U}_{s1}|^2 + |\mathbf{U}_{s2}|^2 \rightarrow \mathbf{0}$$

$$\mathbf{v}_{\text{atm}} : \mathbf{v}_{\mu} \rightarrow \mathbf{v}_s \text{ (100\%)}$$

Strongly disfavored by  
SK  $\nu_{\text{atm}}$  data

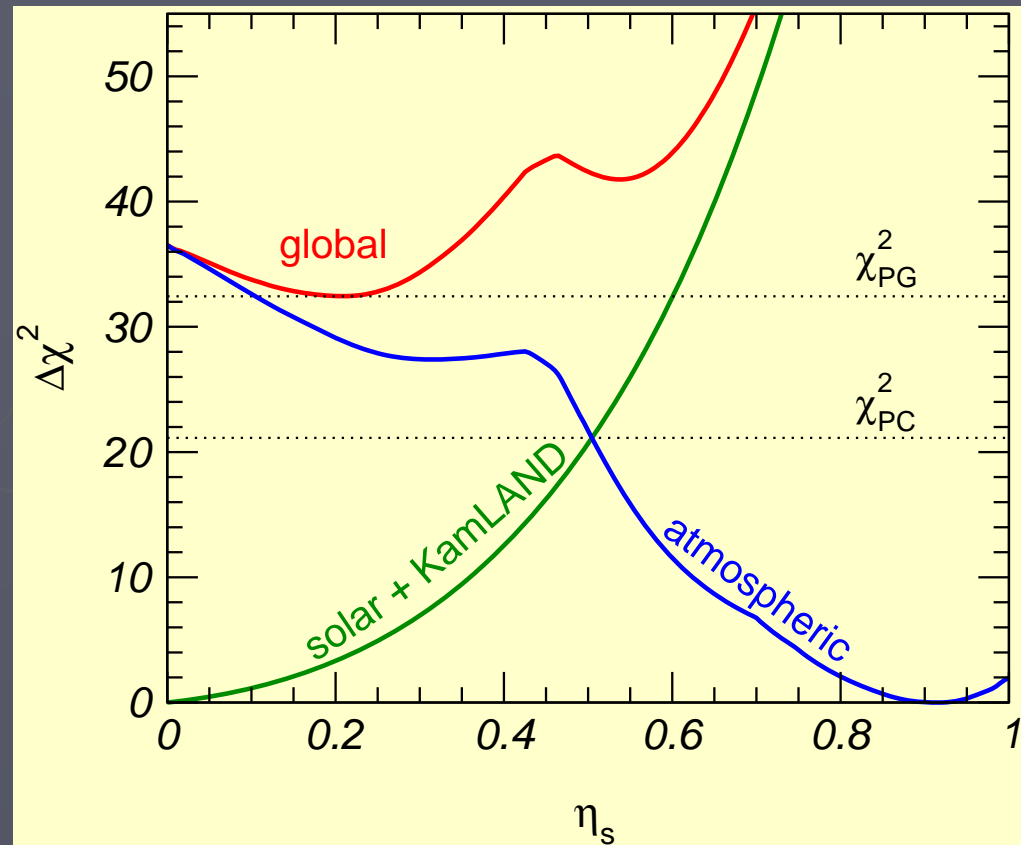
$$\eta_s \equiv |\mathbf{U}_{s1}|^2 + |\mathbf{U}_{s2}|^2 \rightarrow \mathbf{1}$$

$$\mathbf{v}_{\text{sol}} : \mathbf{v}_e \rightarrow \mathbf{v}_s \text{ (100\%)}$$

Strongly disfavored by  
SNO  $\nu_{\text{sol}}$  data

For any value of  $|\mathbf{U}_{s1}|^2 + |\mathbf{U}_{s2}|^2$ ,  
fit to sol+atm data is bad.

Maltoni et al., hep-ph/0405172



**excluded ( $\sim 5\sigma$ CL)**  
**because it contradicts**  
**with  $\mathbf{v}_{\text{atm}}$  or  $\mathbf{v}_{\text{solar}}$  :**  
**independent of LSND**

## (3+1)-scheme (assuming LSND)

$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) = 1 - 4|U_{e4}|^2(1 - |U_{e4}|^2) \sin^2(\Delta m_{41}^2 L/4E)$$

$$P(\nu_\mu \rightarrow \nu_\mu) = 1 - 4|U_{\mu 4}|^2(1 - |U_{\mu 4}|^2) \sin^2(\Delta m_{41}^2 L/4E)$$

$$P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) = 4|U_{e4}|^2|U_{\mu 4}|^2 \sin^2(\Delta m_{41}^2 L/4E)$$

$$\sin^2 2\theta_{\text{Bugey}} > 4|U_{e4}|^2(1 - |U_{e4}|^2) \cong 4|U_{e4}|^2$$

$$\sin^2 2\theta_{\text{CDHSW}} > 4|U_{\mu 4}|^2(1 - |U_{\mu 4}|^2) \cong 4|U_{\mu 4}|^2$$

$$\sin^2 2\theta_{\text{LSND}} = 4|U_{e4}|^2|U_{\mu 4}|^2$$

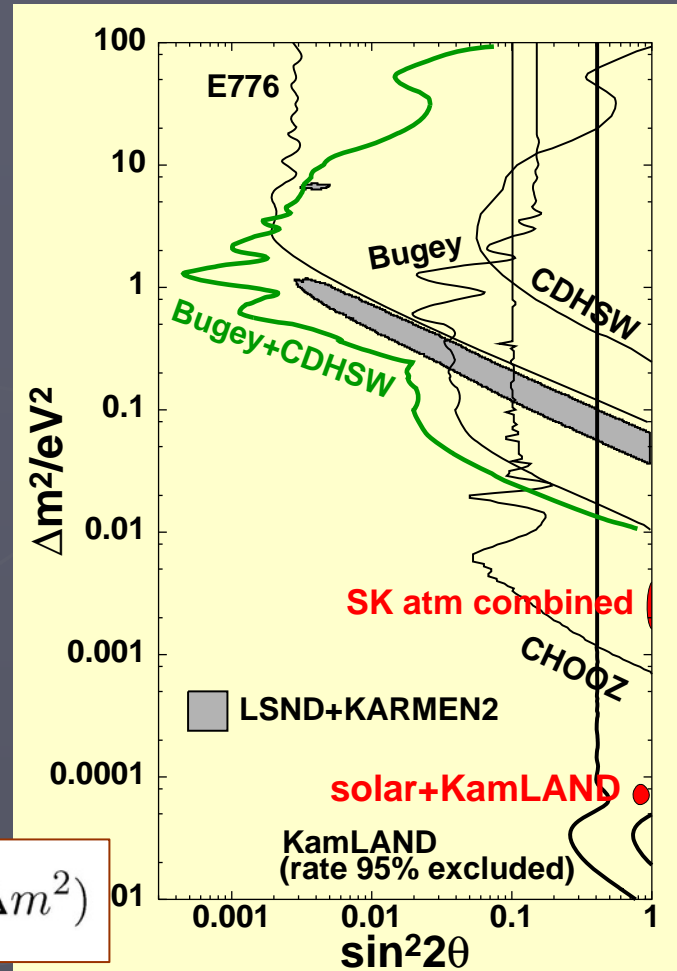


$$\sin^2 2\theta_{\text{LSND}}(\Delta m^2) < \frac{1}{4} \sin^2 2\theta_{\text{Bugey}}(\Delta m^2) \sin^2 2\theta_{\text{CDHSW}}(\Delta m^2)$$

must be satisfied (Okada-OY'97, Bilenky-Giunti-Grimus '98)

But there is no overlap between **LSND** and left side of **Bugey+CDHSW**

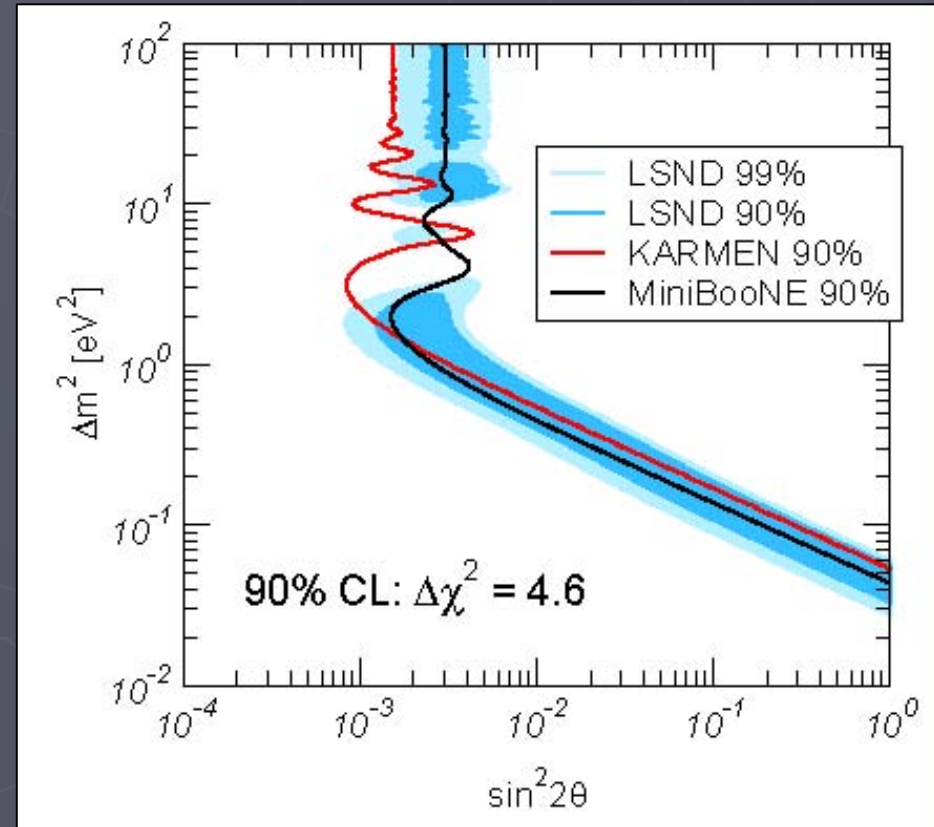
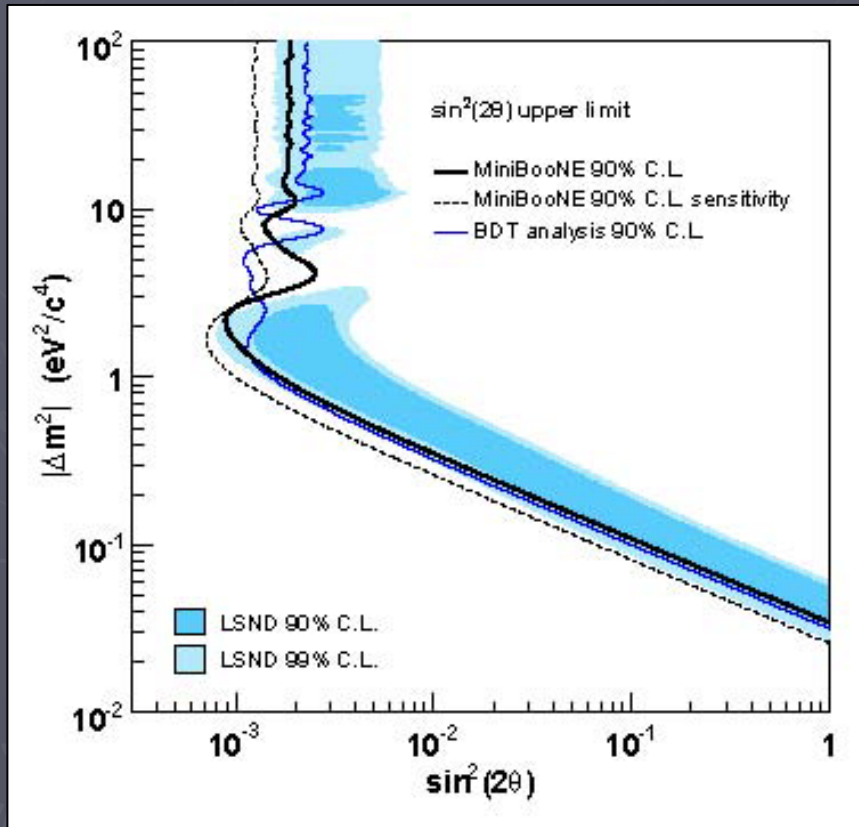
Strongly disfavored ( $\sim 3\sigma\text{CL}$ ) because of the tension between **LSND** and **Bugey+CDHSW** (+other negative results)



Moreover, we have negative result from MiniBooNE

$$\nu_{\mu} \rightarrow \nu_{e}$$

The result may not be conclusive but significance got even larger



Schwetz@nufact07



## Sterile neutrinos w/o assuming LSND

Without assuming LSND and imposing all the negative constraints, one can still consider consistent (3+1)-scheme.

## Why am I still interested in (3+1)-scheme?

The (3+1)-scheme w/o LSND is not motivated by any experimental data, but 4 neutrino schemes offer **phenomenologically natural scenario** for deviation from **3 flavor unitarity**, which may be tested in future neutrino experiments. (cf. B factories)

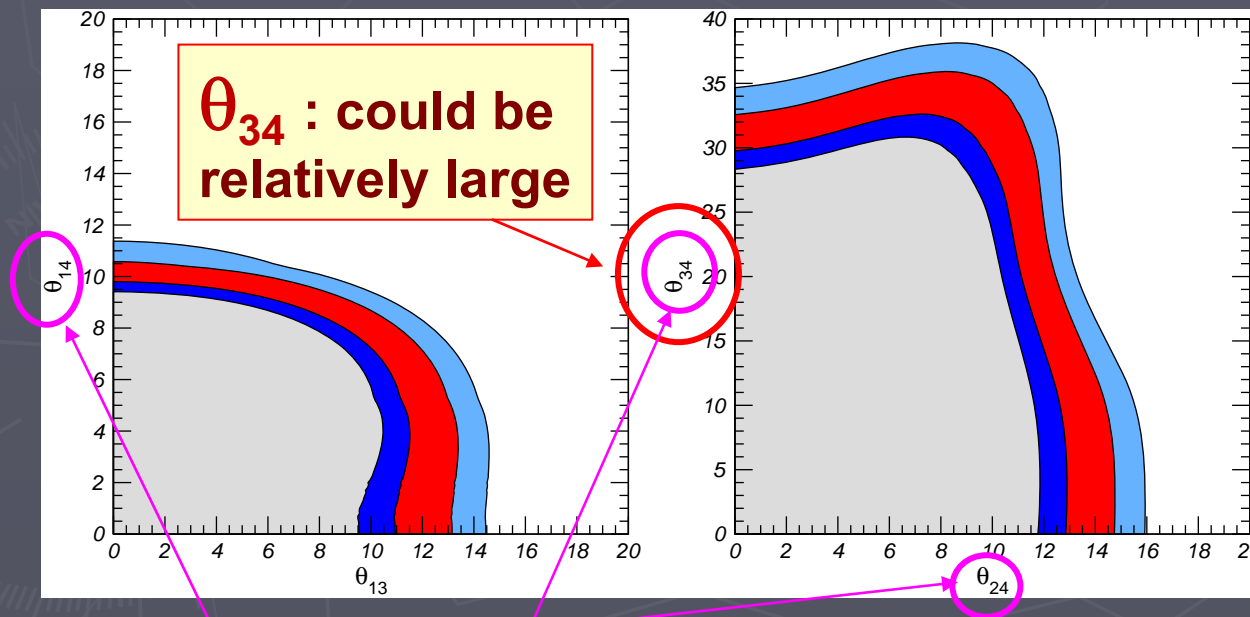
# Sterile neutrinos w/o assuming LSND

Donini-Maltoni-Meloni-Migliozzi-Terranova arXiv:0704.0388v2

Without assuming LSND and imposing all the negative constraints one can still consider (3+1)-scheme

$$U = R_{34}(\theta_{34}) R_{24}(\theta_{24}) R_{23}(\theta_{23}, \delta_3) R_{14}(\theta_{14}) R_{13}(\theta_{13}, \delta_2) R_{12}(\theta_{12}, \delta_1)$$

Constraints by all the negative results give the allowed region



$\theta_{34}$  : ratio of  
 $\nu_{\mu} \rightarrow \nu_{\tau}$  and  
 $\nu_{\mu} \rightarrow \nu_s$

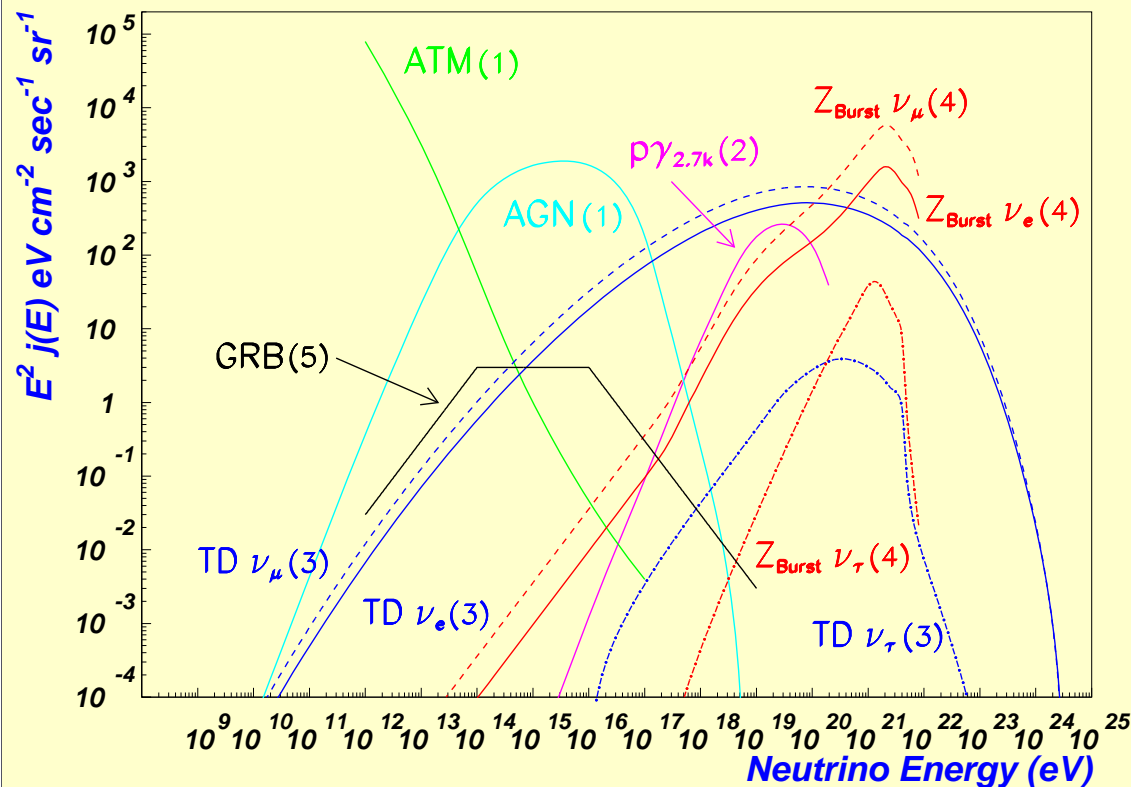
in  $\nu_{\text{atm}}$

$\theta_{24}$  : ratio of  
 $\sin^2(\Delta m_{\text{atm}}^2 L/4E)$   
and  
 $\sin^2(\Delta m_{\text{SBL}}^2 L/4E)$

$\theta_{14}, \theta_{24}, \theta_{34}$  : angles which appear only in 4 $\nu$  scenario

### 3. High energy astrophysical $\nu$

Flux of high energy cosmic  $\nu$  from Active Galactic Nuclei or Gamma Ray Burst etc.



S/N ratio is expected to be large due to little background of atmospheric  $\nu$

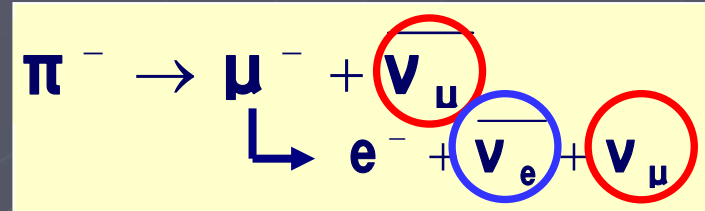
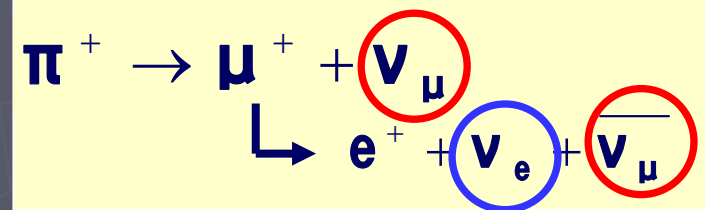
- Precise normalization of flux is not known

→ The ratio of different flavors is important quantity to observe

- Initial flux:

Just like in  $\nu_{\text{atm}}$ , the source of  $\nu$  is  $\pi$  decay

$$\rightarrow F^0(\nu_e) : F^0(\nu_\mu) : F^0(\nu_\tau) \cong 1 : 2 : 0$$



- Observed flux on Earth:

Due to  $\nu$  oscillations

$$|\theta_{13}| \ll 1, |\pi/4 - \theta_{23}| \ll 1 \rightarrow$$

$$F(\nu_e) : F(\nu_\mu) : F(\nu_\tau) \cong 1 : 1 : 1$$

In standard  $N_\nu=3$ , when  $L \rightarrow \infty$   
 oscillation probability in vacuum

$$P_{\alpha\beta} = \sum_j |U_{\alpha j}|^2 |U_{\beta j}|^2$$

$$|U_{\alpha j}|^2 \cong \begin{pmatrix} c_{12}^2 & s_{12}^2 & 0 \\ s_{12}^2/2 & c_{12}^2/2 & 1/2 \\ s_{12}^2/2 & c_{12}^2/2 & 1/2 \end{pmatrix}$$

$$F(\nu_e) = F^0(\nu_e)(P_{ee} + 2P_{\mu e}) = F^0(\nu_e)(1 - P_{\tau e} + P_{\mu e}) = 1$$

$$F(\nu_\mu) = F^0(\nu_e)(P_{e\mu} + 2P_{\mu\mu}) = F^0(\nu_e)(1 - P_{\tau\mu} + P_{\mu\mu}) = 1$$

$$F(\nu_\tau) = F^0(\nu_e)(P_{e\tau} + 2P_{\mu\tau}) = F^0(\nu_e)(1 - P_{\tau\tau} + P_{\mu\tau}) = 1$$

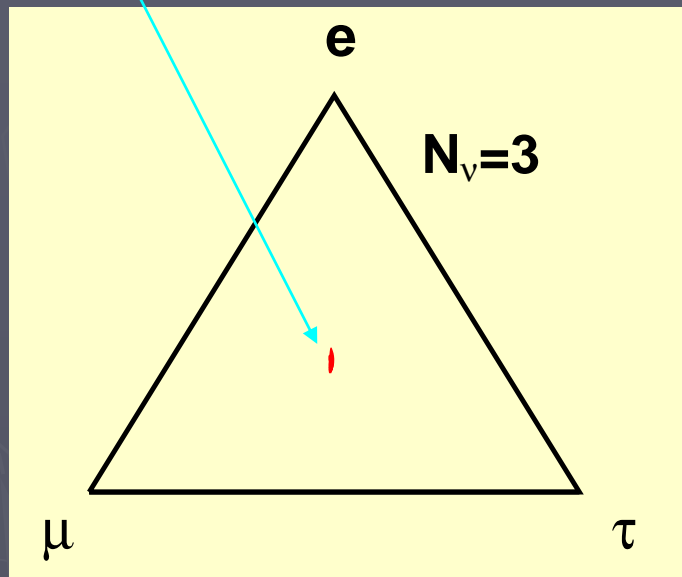
$$F(\nu_\alpha) = F^0(\nu_e)P_{e\alpha} + F^0(\nu_\mu)P_{\mu\alpha} = F^0(\nu_e)(P_{e\alpha} + 2P_{\mu\alpha})$$

$$P_{e\alpha} + 2P_{\mu\alpha} = (P_{e\alpha} + P_{\mu\alpha}) + P_{\mu\alpha} = 1 - P_{\tau\alpha} + P_{\mu\alpha} = 1$$

CHOOZ+ $\nu_{\text{atm}}$ :  $|\theta_{13}| \ll 1$

$\nu_{\text{atm}}$ :  $|\pi/4 - \theta_{23}| \ll 1$

Deviation from 1:1:1 is small for 3 flavor case

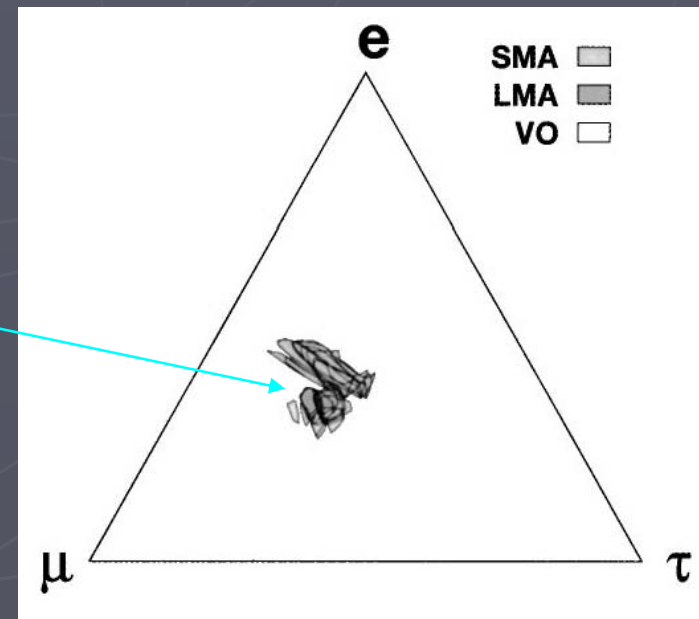
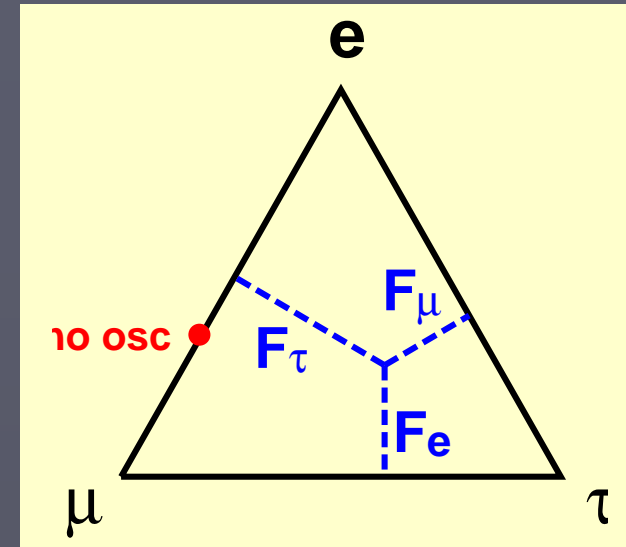


(2+2)-scheme (which was acceptable in '00) gave relatively large deviation

Normalized ratio of active flavors is useful:

$$\tilde{F}(\nu_\alpha) \equiv \frac{F(\nu_\alpha)}{F(\nu_e) + F(\nu_\mu) + F(\nu_\tau)}$$

Athar-Jezabek-OY '00



**A few scenarios to predict deviation from 1:1:1  
have been proposed**

- **Standard flux +  $\nu$  decay**  
 $\alpha:1:1$  ( $\alpha=1.4\sim 6$ )  
Beacom-Bell-Hooper-  
Pakvasa-Weiler '03
- **Standard flux + pseudo-Dirac  $\nu$**   
 $\alpha:1:1$  ( $\alpha=2/3\sim 14/9$ )  
Beacom -Bell-Hooper-  
Learned-Pakvasa-Weiler'04
- **Electromagnetic energy losses of  $\pi$  &  $\mu$**   
 $\alpha:1:1$  ( $\alpha=1/1.8\sim 1$ )  
Kashti-Waxman '05

**All these scenarios predict  $\nu_\mu:\nu_\tau=1:1$  (as long as  $\nu_\mu\leftrightarrow\nu_\tau$   
mixing occurs according to the 3 flavor scenario)**

**Deviation from  $\nu_\mu:\nu_\tau=1:1$  is interesting**

**4 neutrino scenarios offer such a possibility**

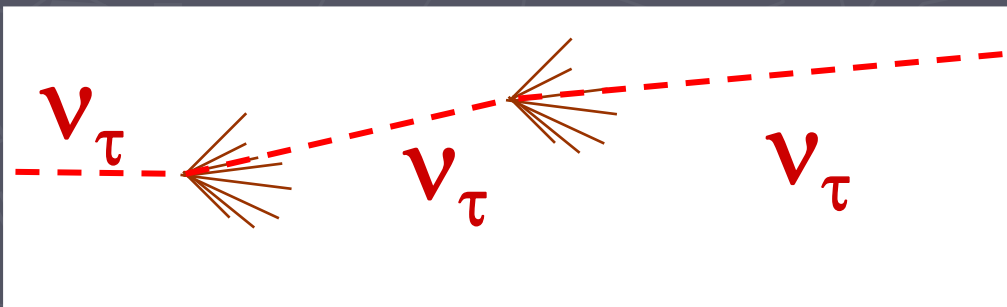
## Identification of $\nu$ flavors

$\nu_e$  : electromagnetic showers

$\nu_\mu$  : muon tracks

$\nu_\tau$  : double bang events ( $E=1-20\text{PeV}$ )

Learned, Pakvasa '95





# Flavor ratio of $\nu$ flux for (3+1)- scheme

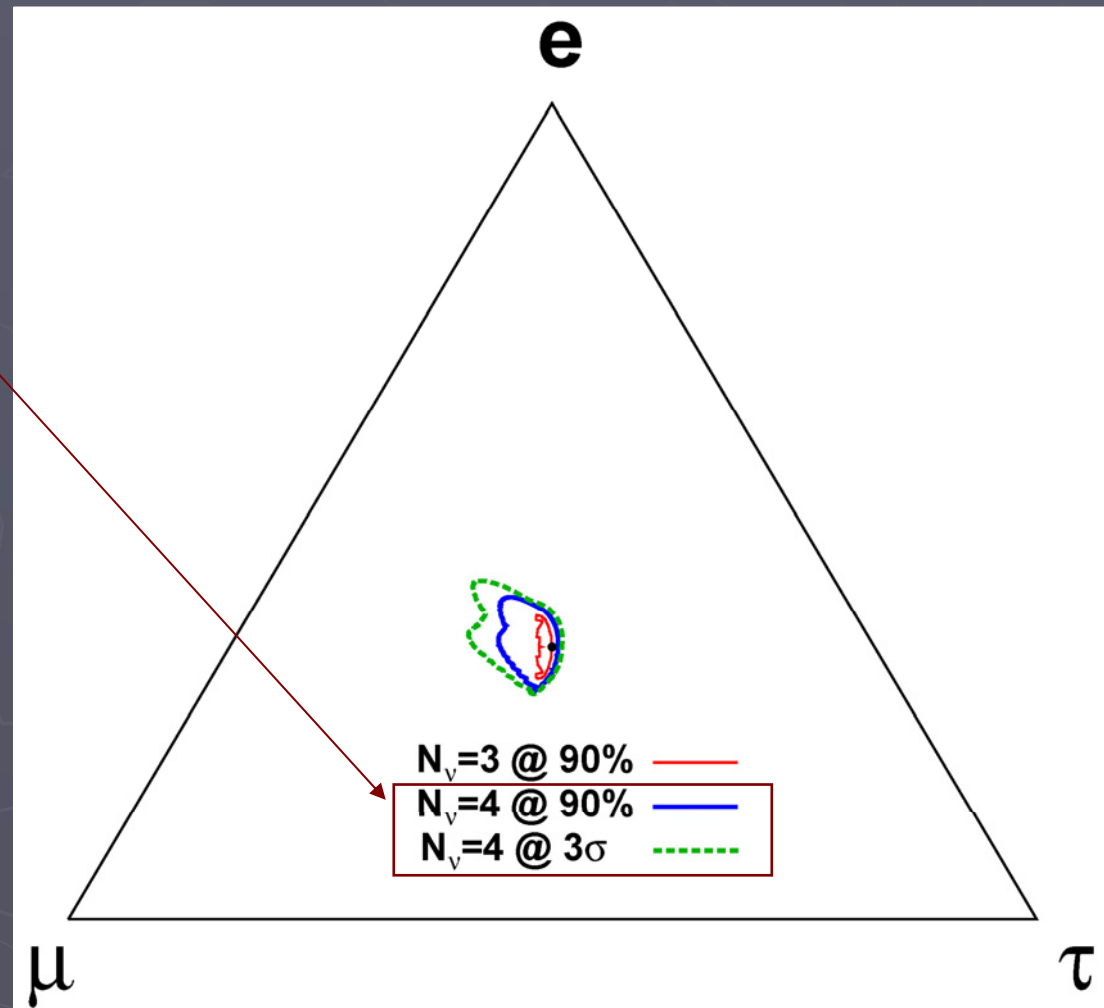
Donini-OY '07

(3+1)-scheme w/o LSND gives the prediction which could be distinguished from  $N_\nu=3$  case



In principle, (3+1)-scheme could be distinguished from the three flavor case

$$\frac{F(\nu_\tau)}{F(\nu_\mu)} = c_{34}^2 \geq 0.67$$



# Theoretical uncertainties of original $\nu$ flux

Lipari-Lusignoli-Meloni Phys.Rev.D75:123005,2007

For illustrations, they discussed  $\nu$  flux from GRB using Waxman-Bahcall

- Proton energy spectrum

$$N_p(E_p) \propto E_p^{-\alpha}$$

- Photon number density

$$n_\gamma(\epsilon) \propto \begin{cases} (\epsilon/\epsilon_b)^{-\beta_1} & \text{for } \epsilon \leq \epsilon_b, \\ (\epsilon/\epsilon_b)^{-\beta_2} & \text{for } \epsilon_b < \epsilon < \epsilon_{\max} \\ 0 & \text{for } \epsilon \geq \epsilon_{\max}, \end{cases}$$

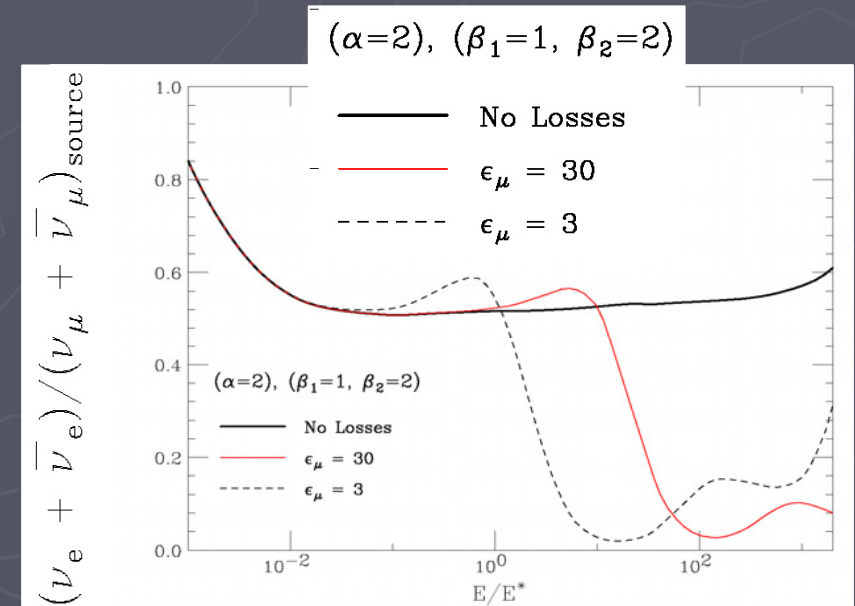
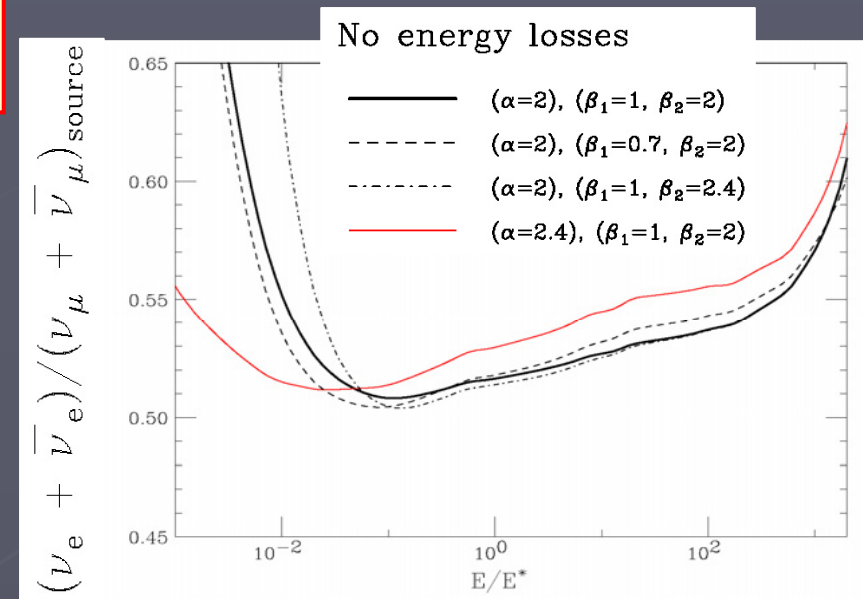
- Muon energy loss due to synchrotron radiation

$$\epsilon_\mu = \frac{E_{\text{syn}}^\mu}{E^*} = 8.4 \times 10^4 \left( \frac{\text{Gauss}}{B} \right) \left( \frac{\epsilon_b}{\text{KeV}} \right)$$

$$E^* \simeq 6.9 \times 10^{13} (\epsilon_b/\text{KeV})^{-1} \text{eV}$$

: Proton threshold energy for inelastic interactions with  $\gamma$

- e: $\mu$ =1:2 not necessarily correct
- Energy dependence expected



# e/ $\mu$ ratio vs $\mu/\tau$ ratio & energy spectrum for (3+1)- scheme

Donini-OY '07

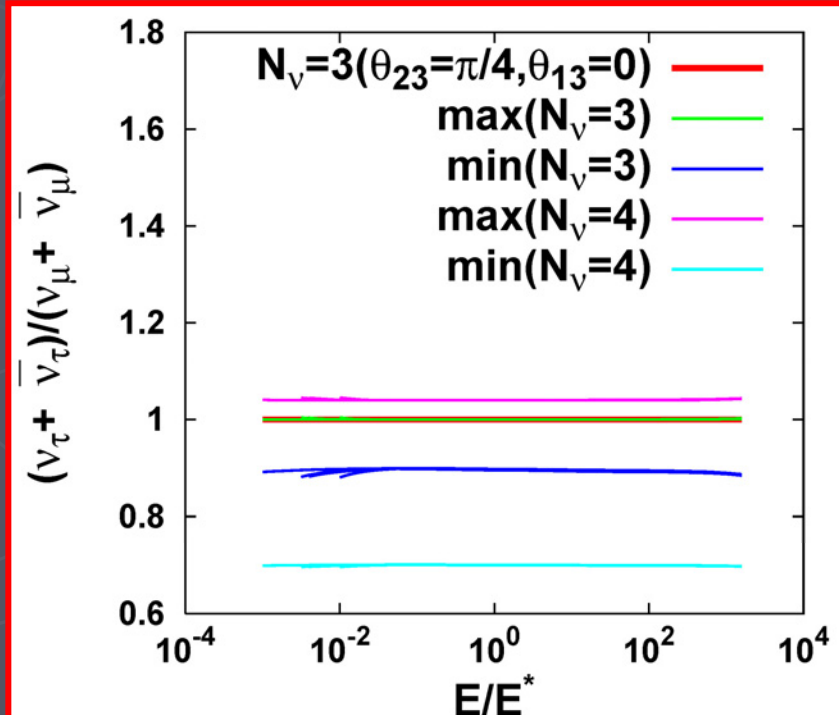
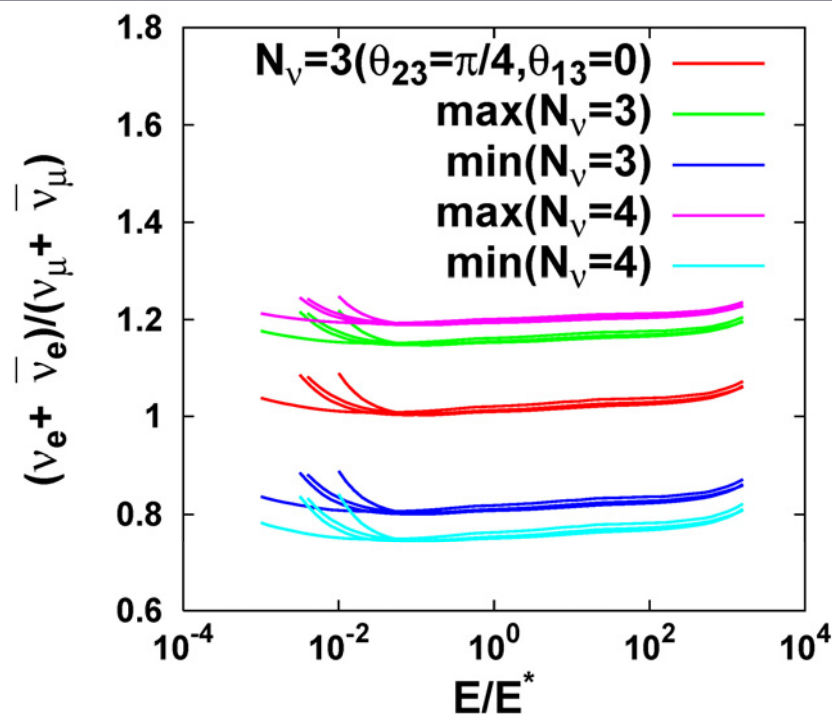
4 curves (energy dependence of  $\rho$ ,  $\gamma$ ) corresponding to uncertainties by Lipari et al.

No energy losses

- $(\alpha=2), (\beta_1=1, \beta_2=2)$
- - -  $(\alpha=2), (\beta_1=0.7, \beta_2=2)$
- · - · -  $(\alpha=2), (\beta_1=1, \beta_2=2.4)$
- $(\alpha=2.4), (\beta_1=1, \beta_2=2)$

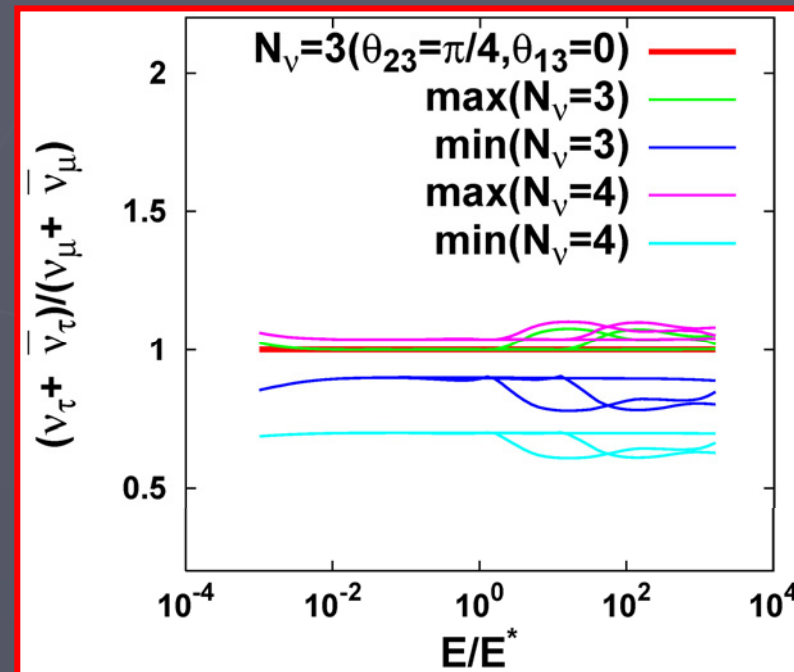
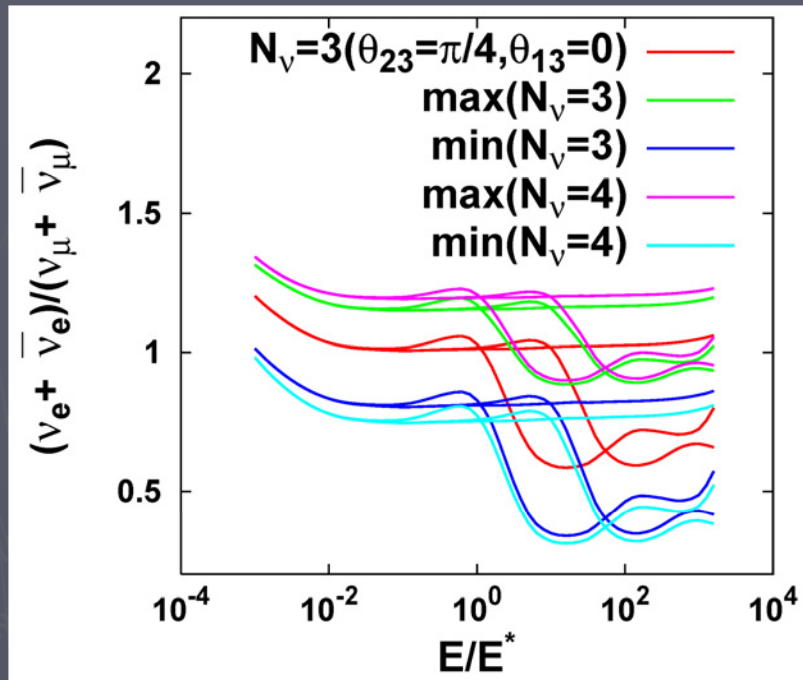
$\mu/\tau$  ratio is less energy dependent (to 1<sup>st</sup> order in small parameters)

$$F(\nu_\tau)/F(\nu_\mu) = c_{34}^2 \geq 0.67$$



3 curves (muon energy loss)  
corresponding to  
uncertainties by Lipari et al.

Donini-OY '07



- Energy dependence gives us hint on the uncertainties
- $\mu/\tau$  ratio is less energy dependent

$$F(\nu_\tau)/F(\nu_\mu) = c_{34}^2 \geq 0.67$$

(to 1<sup>st</sup> order in small parameters)

## Statistics of expected events


For a typical galactic source, ten years of running at a km<sup>3</sup> water equivalent detector:

e,  $\mu$  events  $\sim O(100)$

P. Lipari, astro-ph/0605535

$\tau$  events  $\sim O(30)$

$$N_e/N_\mu (N_\nu = 3) \simeq 1.0_{-0.2}^{+0.14}(\text{osc})_{-0.58}^{+0}(\mu \text{ damp}) \pm 0.14(\text{stat})$$


$$N_e/N_\mu (N_\nu = 4; \theta_{34} = 35^\circ) \sim 0.75 \quad {}_{-0.4}^{+0}(\mu \text{ damp}) \pm 0.11(\text{stat})$$

$$N_\tau/N_\mu (N_\nu = 3) \simeq 0.30_{-0.03}^{+0}(\text{osc})_{-0.02}^{+0}(\mu \text{ damp}) \pm 0.08(\text{stat})$$

$$N_\tau/N_\mu (N_\nu = 4; \theta_{34} = 35^\circ) \sim 0.2 \quad {}_{-0.01}^{+0}(\mu \text{ damp}) \pm 0.06(\text{stat})$$

$\mu/\tau$  ratio suffers from theoretical uncertainty less than e/ $\tau$  ratio, but statistics is not sufficient.

A possible way out:

To increase the detector volume in the future?

## 4. Conclusions

- **(3+1)-scheme without LSND constraint** predicts flavor ratio of HE cosmic  $\nu$  which could be in principle distinguished from 3 flavor case.
- **$\mu/\tau$  ratio** suffers relatively less from theoretical uncertainties, and could play an important role to look for signatures of **sterile  $\nu$** .
- Information from **energy spectrum** could be also important to check theoretical uncertainties.
- Statistics from one source is not sufficient to get signatures of sterile  $\nu$ , but if we can **increase the detector volume** in the future, then we may be able to say something about **sterile  $\nu$** .

The background is a dark blue-grey color with a faint, light-colored topographic map overlay. The map features contour lines and a compass rose in the lower-left quadrant. The compass rose has a needle pointing towards the top-left and is marked with 'N' for North, 'E' for East, 'S' for South, and 'W' for West. A dollar sign (\$) is also visible near the compass rose.

**Backup slides**

LSND( $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ ): affirmative  
 MiniBOONE( $\nu_\mu \rightarrow \nu_e$ ): negative

with one more  $\nu_s$   
 difference between  
 $\nu$  & anti- $\nu$  may offer  
 a promising fit

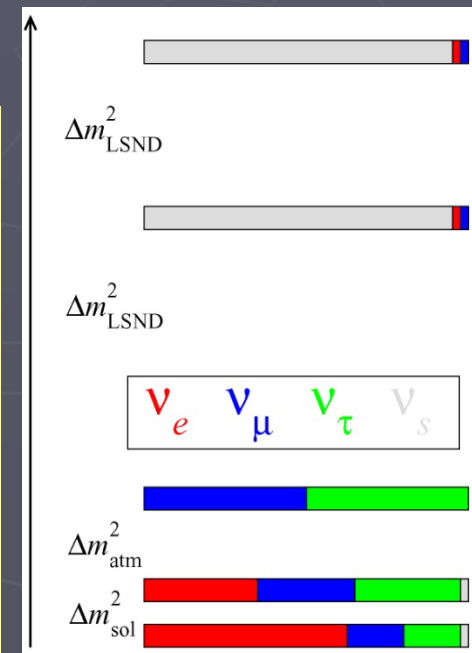
(3+2)-scheme with CP phase  $\delta$

$$\begin{aligned}
 P_{\nu_\mu \rightarrow \nu_e} &= 4 |U_{e4}|^2 |U_{\mu4}|^2 \sin^2 \phi_{41} \\
 &+ 4 |U_{e5}|^2 |U_{\mu5}|^2 \sin^2 \phi_{51} \\
 &+ 8 |U_{e4} U_{\mu4} U_{e5} U_{\mu5}| \sin \phi_{41} \sin \phi_{51} \cos(\phi_{54} - \delta)
 \end{aligned}$$

with the definitions

$$\phi_{ij} \equiv \frac{\Delta m_{ij}^2 L}{4E},$$

$$\delta \equiv \arg(U_{e4}^* U_{\mu4} U_{e5} U_{\mu5}^*) .$$





Schwetz-Mangold@nufact07

$$\phi_{54}^{best} = 1.64 \pi$$

$$\Delta m_{41}^2 = 0.89 \text{ eV}^2$$

$$\Delta m_{51}^2 = 6.49 \text{ eV}^2$$

$$\chi_{\min}^2 = 94.5 / (107 - 7)$$

Karagiorgi@nufact07

$$\chi^2/ndf = 146.7/156$$

gof=69%

$$\phi_{54}^{best} = 1.74 \pi$$

- (3+2) schemes

- offer the possibility of CP violation to reconcile LSND and MiniBooNE,

- but there is tension between appearance and disappearance data ( $3\sigma$ ,  $4\sigma$  for MB300)

$\bar{\nu}_e \rightarrow \bar{\nu}_e$  : Bugey  $\nu_\mu \rightarrow \nu_\mu$  : CDHSW

So from the global fit, (3+2) is probably not a promising scheme...