

**Constraints on non-standard
interaction in ν propagation from
 ν_{atm} & T2KK long-baseline
experiment**

**Osamu Yasuda
Tokyo Metropolitan University**

Dec. 17, @Miami 2010

Ref: arXiv:1003.5554 [hep-ph]

In collaboration with Haruna OKI

1. Introduction

2. High energy behavior of ν_{atm} data & NSI

3. Sensitivity to NSI of propagation at T2KK

4. Conclusions

1. Introduction

Framework of 3 flavor ν oscillation

Mixing matrix

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

Functions of mixing angles θ_{12} , θ_{23} , θ_{13} , and CP phase δ

Information we have obtained so far:

ν_{solar} + KamLAND (reactor)

$$\theta_{12} \cong \frac{\pi}{6}, \Delta m_{21}^2 \cong 8 \times 10^{-5} \text{ eV}^2$$

ν_{atm} + K2K, MINOS (accelerators)

$$\theta_{23} \cong \frac{\pi}{4}, |\Delta m_{32}^2| \cong 2.5 \times 10^{-3} \text{ eV}^2$$

CHOOZ (reactor)

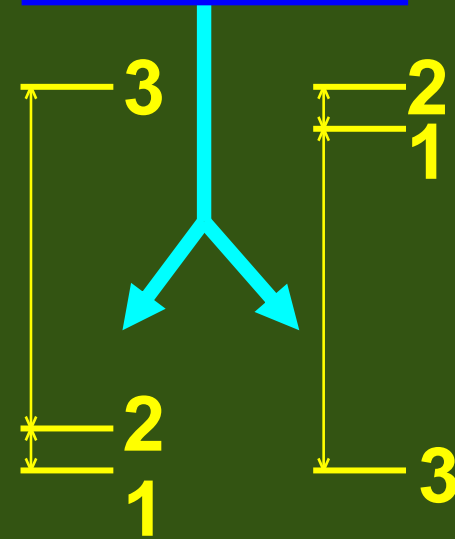
$$|\theta_{13}| \leq \sqrt{0.15/2}$$

$$U = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \simeq \begin{pmatrix} c_{12} & s_{12} & \epsilon \\ -s_{12}/\sqrt{2} & c_{12}/\sqrt{2} & 1/\sqrt{2} \\ s_{12}/\sqrt{2} & -c_{12}/\sqrt{2} & 1/\sqrt{2} \end{pmatrix}$$

- θ_{13} : only upper bound is known
- δ : undetermined

Next task is to measure θ_{13} , $\text{sign}(\Delta m^2_{31})$ and δ .

- Both mass hierarchies are allowed



normal hierarchy

$$\Delta m^2_{32} > 0$$

inverted hierarchy

$$\Delta m^2_{32} < 0$$

Future LBL exp. (on-going / under construction / proposed)

- (conventional) superbeam

T2K phase I (2009-, 0.75MW, $E \sim 1\text{GeV}$, $L=295\text{km}$)

T2K phase II (4MW+HK, $E \sim 1\text{GeV}$, $L=295\text{km}$)

T2KK (JAERI \rightarrow HK&Korea, $E \sim 1\text{GeV}$, $L=295\text{km}\&1000\text{km}$)

NOvA (FNAL \rightarrow Ash River (MN), $E \sim 2\text{GeV}$, $L=810\text{km}$)

LBNE (FNAL \rightarrow Homestake(SD), $E \sim 3\text{GeV}$, $L=1300\text{km}$)

SPL (CERN \rightarrow Frejus, $E \sim 0.25\text{GeV}$, $L=130\text{km}$)

- neutrino factory ($E_\nu \sim 25\text{GeV}$, $L \sim 3000\text{km}+7500\text{km}$)

- beta beam ($E_\nu=0.5-1.5\text{GeV}$, $L \sim 130\text{km}$)

Future reactor experiments ($E \sim 4\text{MeV}$, $L \sim 2\text{km}$)

Double CHOOZ (France) , Daya Bay (China), Reno (Korea)

\rightarrow With these experiments, θ_{13} , $\text{sign}(\Delta m_{31}^2)$
and δ are expected to be determined

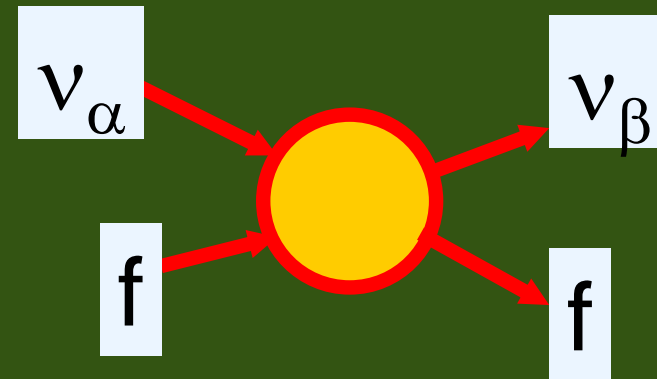
Motivation for research on **New Physics**

High precision measurements of ν oscillation in future experiments can be used to probe **physics beyond SM** by looking at deviation from $SM+m_\nu$ (like at B factories).

→ Research on **New Physics** is important.

Phenomenological **New Physics** considered in this talk: 4-fermi exotic interactions:

$$\mathcal{L}_{eff} = G_{NP}^{\alpha\beta} \bar{\nu}_\alpha \gamma^\mu \nu_\beta \bar{f} \gamma_\mu f'$$



neutral current
Non Standard
Interaction

● NSI in propagation (non-standard matter effect)

$$i \frac{d}{dt} \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \left[U \text{diag} \left(\frac{m_1^2}{2E}, \frac{m_2^2}{2E}, \frac{m_3^2}{2E} \right) U^{-1} + A \begin{pmatrix} 1 + \epsilon_{ee} & \epsilon_{e\mu} & \epsilon_{e\tau} \\ \epsilon_{\mu e} & \epsilon_{\mu\mu} & \epsilon_{\mu\tau} \\ \epsilon_{\tau e} & \epsilon_{\tau\mu} & \epsilon_{\tau\tau} \end{pmatrix} \right] \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix}$$

$A = 2^{1/2} G_F N_e$ $N_e = \text{electron density}$

NSI

● Constraints on $\epsilon_{\alpha\beta}$

Davidson et al., JHEP 0303:011,2003; Berezhiani, Rossi, PLB535 ('02) 207; Barranco et al., PRD73 ('06) 113001; Barranco et al., arXiv:0711.0698

Biggio et al., JHEP 0908, 090 (2009) w/o 1-loop arguments

related to each other by ν_{atm}

can be improved by ν_{atm}

$$\left(\begin{array}{l} |\epsilon_{ee}| \lesssim 4 \times 10^0 \\ |\epsilon_{e\mu}| \lesssim 3 \times 10^{-1} \\ |\epsilon_{e\tau}| \lesssim 3 \times 10^0 \\ |\epsilon_{\mu\mu}| \lesssim 7 \times 10^{-2} \\ |\epsilon_{\mu\tau}| \lesssim 3 \times 10^{-1} \\ |\epsilon_{\tau\tau}| \lesssim 2 \times 10^1 \end{array} \right)$$

2. High energy behavior of ν_{atm} data & NSI

- Standard case with $N_\nu=2$

$$1 - P(\nu_\mu \rightarrow \nu_\mu) \sim \sin^2 2\theta_{\text{atm}} \sin^2 \left(\frac{\Delta m_{\text{atm}}^2 L}{4E} \right) \propto \frac{1}{E^2}$$

- Standard case with $N_\nu=3$

$$1 - P(\nu_\mu \rightarrow \nu_\mu) \simeq \left(\frac{\Delta m_{31}^2}{2AE} \right)^2 \left[\sin^2 2\theta_{23} \left(\frac{c_{13}^2 AL}{2} \right)^2 + s_{23}^2 \sin^2 2\theta_{13} \sin^2 \left(\frac{AL}{2} \right) \right] \propto \frac{1}{E^2}$$

- Deviation of $1-P(\nu_\mu \rightarrow \nu_\mu)$ due to NSI contradicts with data

$$1 - P(\nu_\mu \rightarrow \nu_\mu) \simeq \mathbf{c}_0 + \frac{\mathbf{c}_1}{E} + \frac{c_{20}L^2 + c_{21} \sin^2(c_{22}L)}{E^2}$$

→ High ν_{atm} data gives constraints on NSI:

$$|\mathbf{c}_0| \ll 1, |\mathbf{c}_1| \ll 1$$

● with NSI

$$1 - P(\nu_\mu \rightarrow \nu_\mu) \simeq \mathbf{c}_0 + \frac{\mathbf{c}_1}{E} + \frac{c_{20}L^2 + c_{21} \sin^2(c_{22}L)}{E^2}$$

$$|\mathbf{c}_0| \ll 1 \rightarrow |\varepsilon_{e\mu}| \ll 1, |\varepsilon_{\mu\mu}| \ll 1, |\varepsilon_{\mu\tau}| \ll 1$$

$|\varepsilon_{\mu\tau}| \ll 1$: Already shown by Fornengo et al. PRD65, 013010, '02;
Gonzalez-Garcia&Maltoni, PRD70, 033010, '04; Mitsuka@nufact08

$|\varepsilon_{\mu\mu}| \ll 1$: Already shown from other expts. by Davidson et al.
JHEP 0303:011, '03

$|\varepsilon_{e\mu}| \ll 1$: New observation (analytical consideration only)

$$|\mathbf{c}_1| \ll 1 \rightarrow |\varepsilon_{\tau\tau} - |\varepsilon_{e\tau}|^2 / (1 + \varepsilon_{ee})| \ll 1$$

Already shown by
Friedland-Lunardini,
PRD72:053009, '05

- Summary of the constraints on $\epsilon_{\alpha\beta}$

To a good approximation, we are left with 3 independent variables ϵ_{ee} , $|\epsilon_{e\tau}|$, $\arg(\epsilon_{e\tau})$:

$$A \begin{pmatrix} 1 + \epsilon_{ee} & \epsilon_{e\mu} & \epsilon_{e\tau} \\ \epsilon_{\mu e} & \epsilon_{\mu\mu} & \epsilon_{\mu\tau} \\ \epsilon_{\tau e} & \epsilon_{\tau\mu} & \epsilon_{\tau\tau} \end{pmatrix}$$

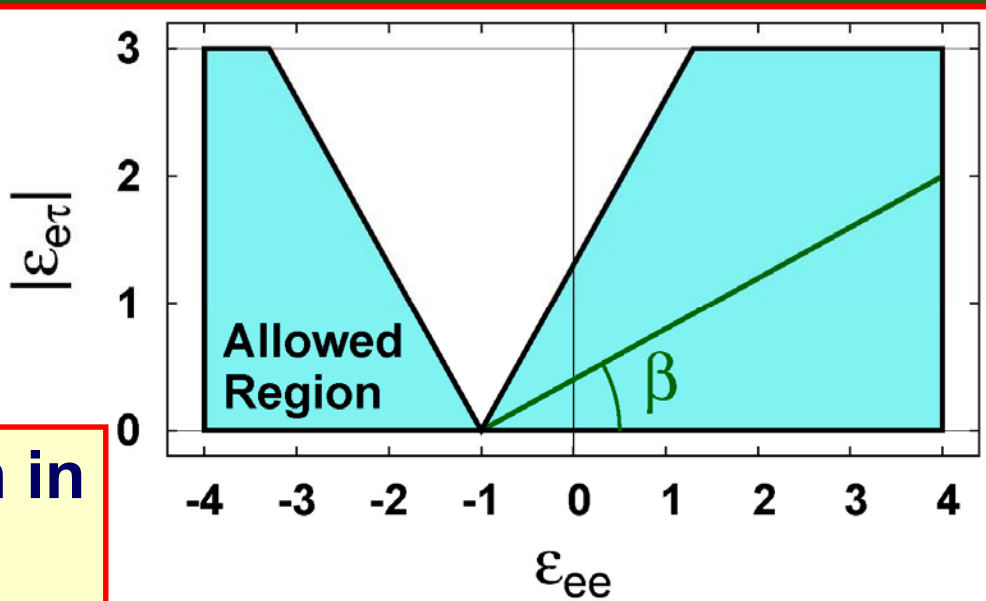


$$A \begin{pmatrix} 1 + \epsilon_{ee} & 0 & \epsilon_{e\tau} \\ 0 & 0 & 0 \\ \epsilon_{e\tau}^* & 0 & |\epsilon_{e\tau}|^2 / (1 + \epsilon_{ee}) \end{pmatrix}$$

Furthermore, ν_{atm} data implies

$$\tan\beta = |\epsilon_{e\tau}| / (1 + \epsilon_{ee}) < 1.3$$

Friedland-Lunardini,
PRD72:053009,'05



Allowed region in
(ϵ_{ee} , $|\epsilon_{e\tau}|$)

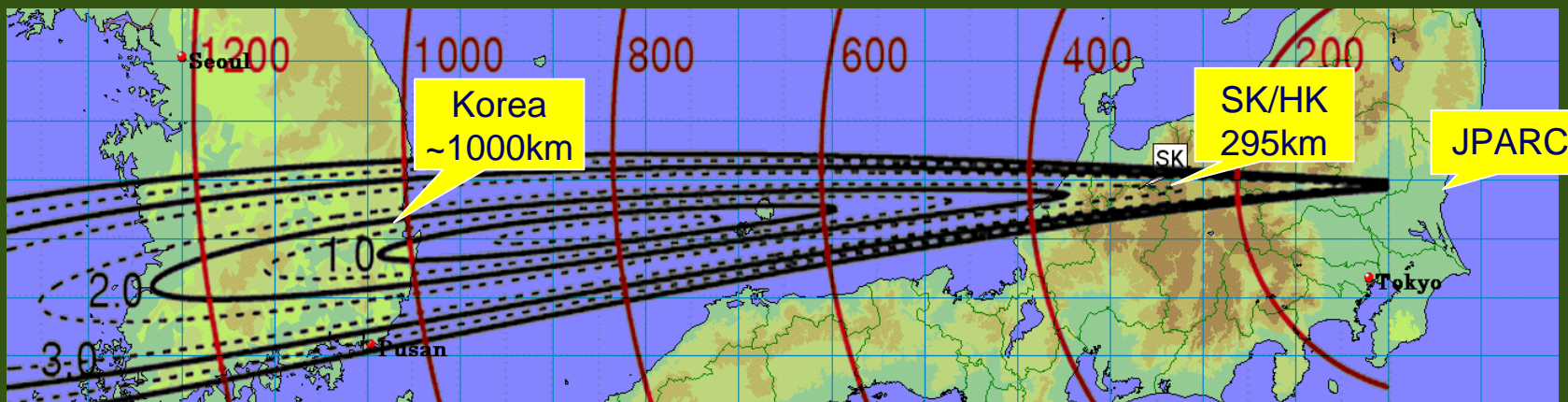
3. Sensitivity to NSI of propagation at T2KK

T2KK proposal with baselines $L=295\text{km}$, 1050km
→ $L=1050\text{km}$ is sensitive to the matter effect

	$ \Delta m^2_{31} L/4E$	$ \Delta m^2_{21} L/4E$	$AL/2$
$L=295\text{km}$	~ 1	~ 0.04	~ 0.06
$L=1050\text{km}$	~ 5	~ 0.1	~ 0.3



dependence on A & Δm^2_{21} at $L=1050\text{km}$ is non-negligible



Outline of our Analysis

$$A \equiv \sqrt{2}G_F n_e$$

Our ansatz

$$i \frac{d}{dt} \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \left\{ U^{-1} \text{diag} \left(\frac{m_1^2}{2E}, \frac{m_2^2}{2E}, \frac{m_3^2}{2E} \right) U + A \begin{pmatrix} 1 + \epsilon_{ee} & 0 & \epsilon_{e\tau} \\ 0 & 0 & 0 \\ \epsilon_{e\tau}^* & 0 & 1 + \epsilon_{ee} \end{pmatrix} \right\} \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix}$$

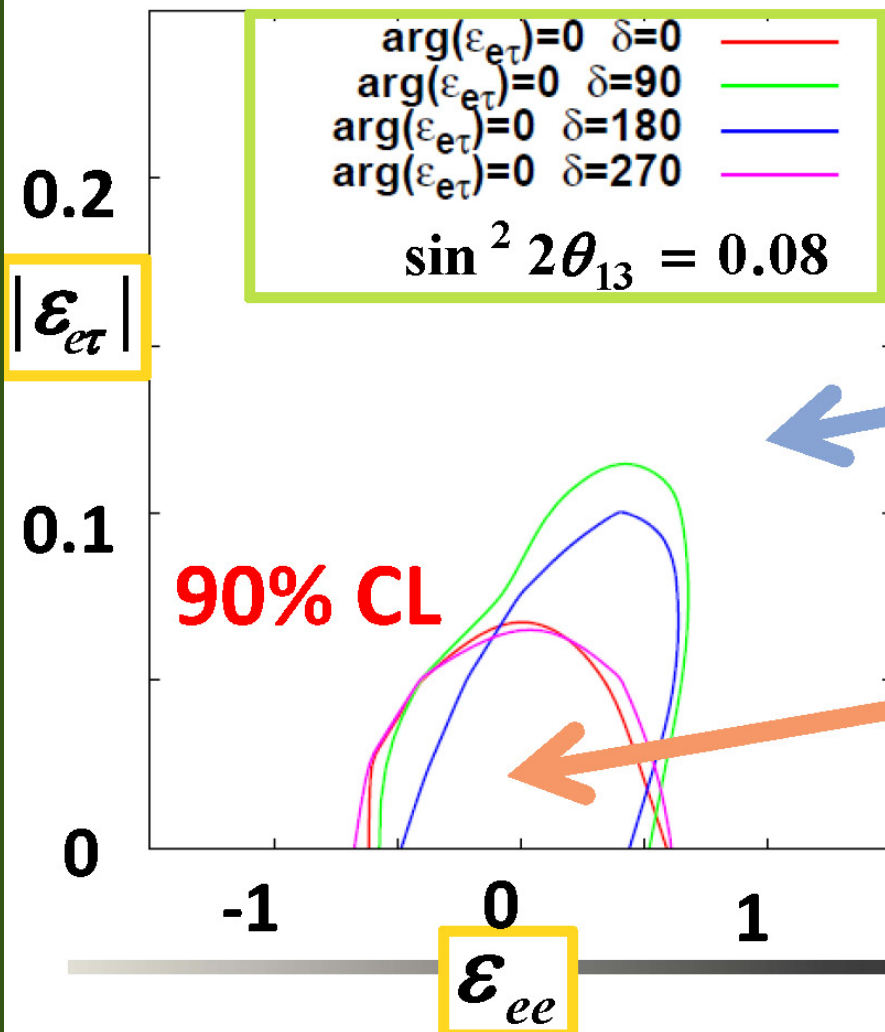
Black : standard **Red : non-standard**

$$\Delta\chi^2(\text{NSI}) = \min_{\text{std parameters}} \sum_i \frac{\left(N_i^0(\text{NSI}) - N_i(\text{std}) \right)^2}{\sigma_i^2} + \Delta\chi_{\text{prior}}^2$$

$$\Delta\chi_{\text{prior}}^2 \equiv \frac{(\sin^2 2\theta_{23} - \sin^2 2\theta_{23}^{\text{best}})^2}{(\delta \sin^2 2\theta_{23})^2} + \frac{(\Delta m_{31}^2 - \Delta m_{31}^{2\text{best}})^2}{(\delta \Delta m_{31}^2)^2} + \frac{(\sin^2 2\theta_{13} - \sin^2 2\theta_{13}^{\text{best}})^2}{(\delta \sin^2 2\theta_{13})^2}$$

$\Delta\chi^2 > 4.6$: Deviation of NSI from νSM is significant compared with errors (at 90% CL of 2 degrees of freedom $\epsilon_{ee}, |\epsilon_{e\tau}|$)

Sensitivity to ϵ_{ee} , $|\epsilon_{e\tau}|$



Marginalized over θ_{13} ,
 θ_{23} , $|\Delta m_{31}^2|$, $\text{sign}(\Delta m_{31}^2)$

- Outside of the curves :
Effects of NSI can be distinguished from the standard case.
- Inside of the curves :
Effects of NSI are not significant.

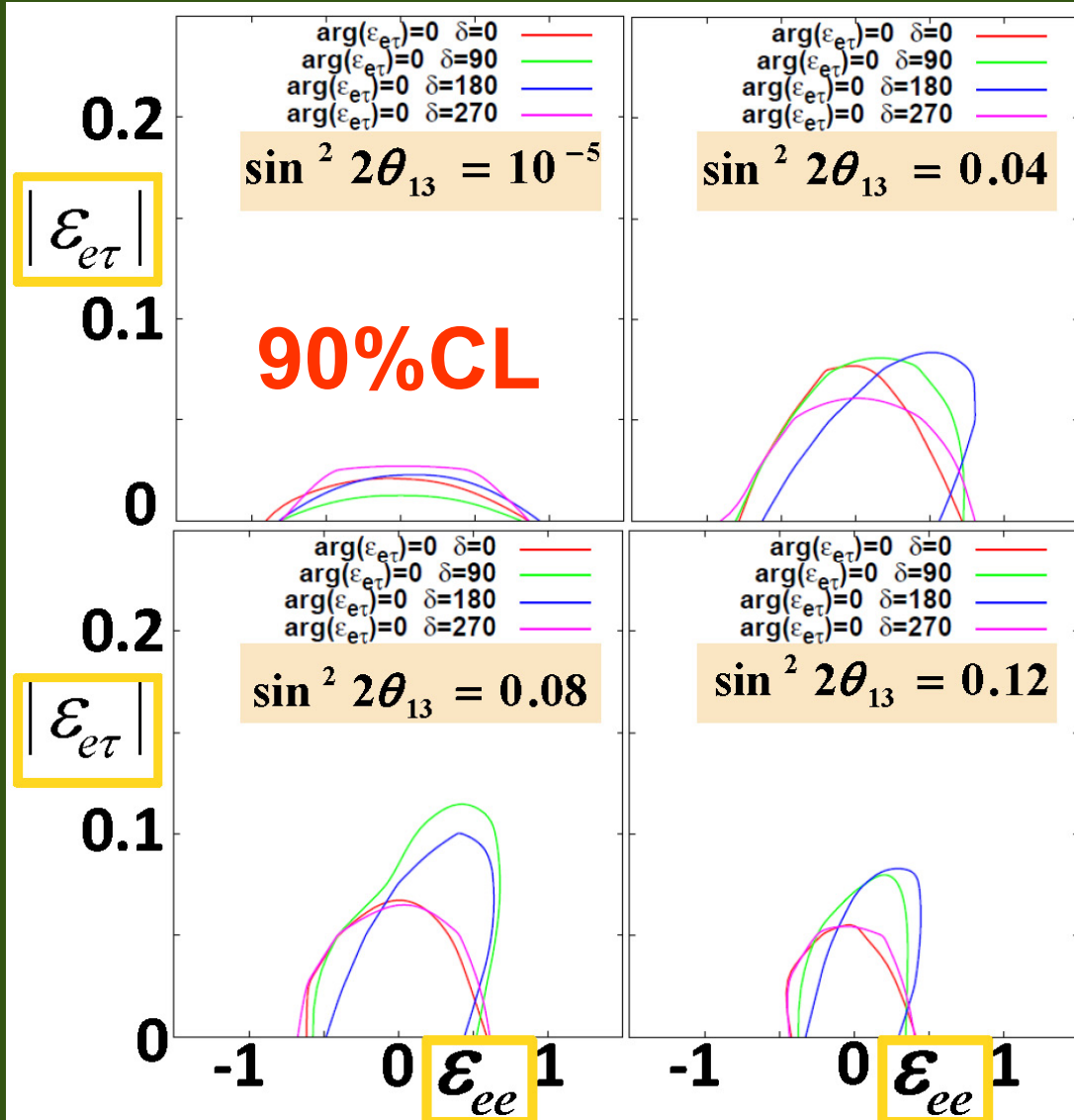
- **Dependence on phases δ and $\arg(\epsilon_{e\tau})$**

$$P(\nu_\mu \rightarrow \nu_e) \cong P_0(\nu_\mu \rightarrow \nu_e) \Big|_{\Delta m_{21}^2=0} + \Delta m_{21}^2 P_1(\nu_\mu \rightarrow \nu_e)$$

**Function of
 $\delta + \arg(\epsilon_{e\tau})$**

**Approximately
function of
 $\arg(\epsilon_{e\tau})$ only**

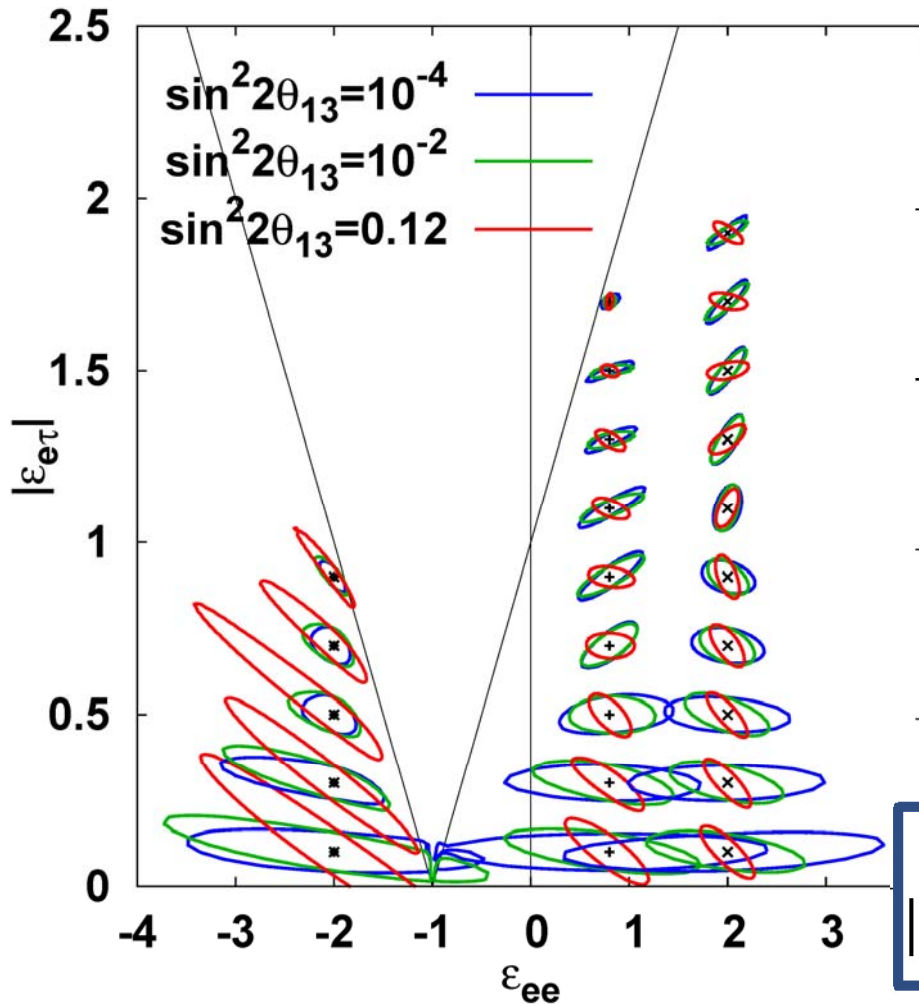
Sensitivity to ϵ_{ee} , $|\epsilon_{e\tau}|$ for various θ_{13}



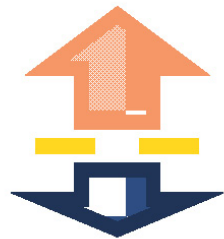
regions depend on
 $\theta_{13}, \delta, \arg(\epsilon_{e\tau})$

$$\begin{array}{l}
 |\epsilon_{ee}| < 4 \\
 |\epsilon_{e\tau}| < 3 \\
 \downarrow \\
 |\epsilon_{ee}| \gtrsim 1 \\
 |\epsilon_{e\tau}| \gtrsim 0.2
 \end{array}$$

Precision of ϵ_{ee} , $|\epsilon_{e\tau}|$



$|\epsilon_{e\tau}| \geq 0.5$
 $\epsilon_{ee}, |\epsilon_{e\tau}|$
 determined
 separately



ϵ_{ee} not determined
 $|\epsilon_{e\tau}|$ determined (if > 0.1)

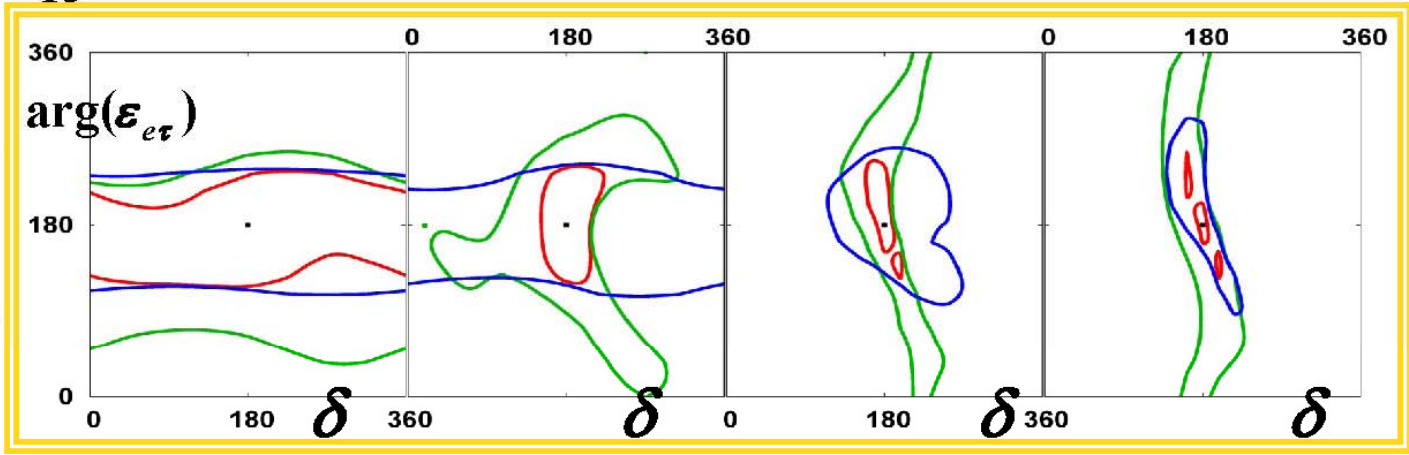
Sensitivity to δ and $\arg(\epsilon_{e\tau})$

Kamioka+Korea ———
 Kamioka ———
 Korea ———

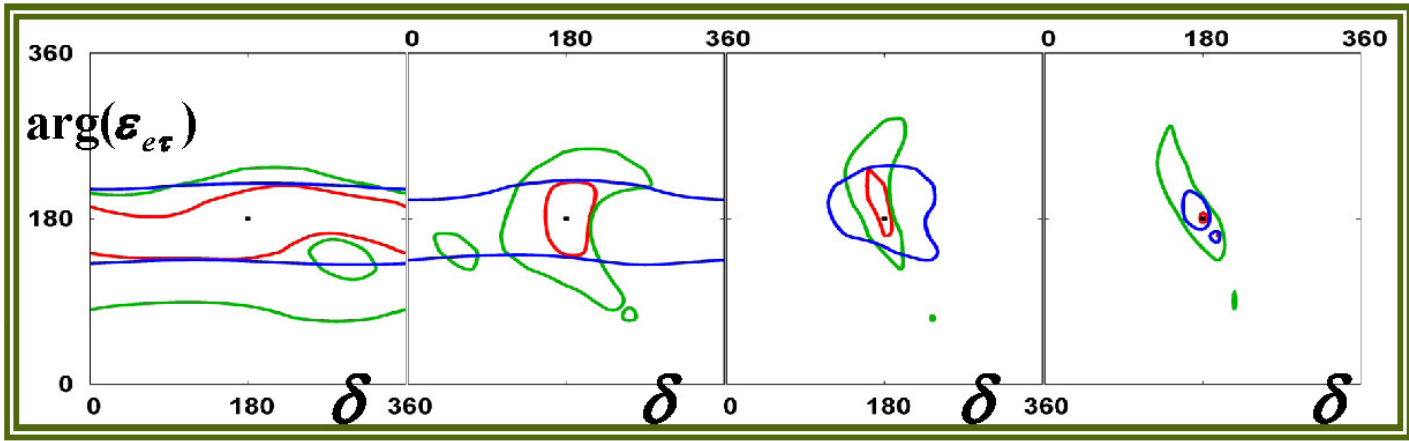
● Correlation of measured $\arg(\epsilon_{e\tau})$ and δ

$\sin^2 2\theta_{13} = 10^{-4} \quad 10^{-3} \quad 10^{-2} \quad 0.12$

$\epsilon_{ee} = 0.8$
 $|\epsilon_{e\tau}| = 0.2$



$\epsilon_{ee} = 0.8$
 $|\epsilon_{e\tau}| = 0.4$



● If $(\epsilon_{ee}, |\epsilon_{e\tau}|, s_{13})$ are large, we can determine $\arg(\epsilon_{e\tau}), \delta$

4. Summary (1)

- We provided an analytical argument on the oscillation probability for high energy atmospheric neutrinos that $|\epsilon_{\mu\alpha}| \ll 1$ & $|\epsilon_{\tau\tau} - |\epsilon_{e\tau}|^2 / (1 + \epsilon_{ee})| \ll 1$ must hold.

$$A \begin{pmatrix} 1 + \epsilon_{ee} & \epsilon_{e\mu} & \epsilon_{e\tau} \\ \epsilon_{\mu e} & \epsilon_{\mu\mu} & \epsilon_{\mu\tau} \\ \epsilon_{\tau e} & \epsilon_{\tau\mu} & \epsilon_{\tau\tau} \end{pmatrix}$$



$$A \begin{pmatrix} 1 + \epsilon_{ee} & 0 & \epsilon_{e\tau} \\ 0 & 0 & 0 \\ \epsilon_{e\tau}^* & 0 & |\epsilon_{e\tau}|^2 / (1 + \epsilon_{ee}) \end{pmatrix}$$

- Deviation of $1 - P(\nu_\mu \rightarrow \nu_\mu)$ from the standard case in high energy ν_{atm} data gives strong constraints on **Non Standard Interaction**.

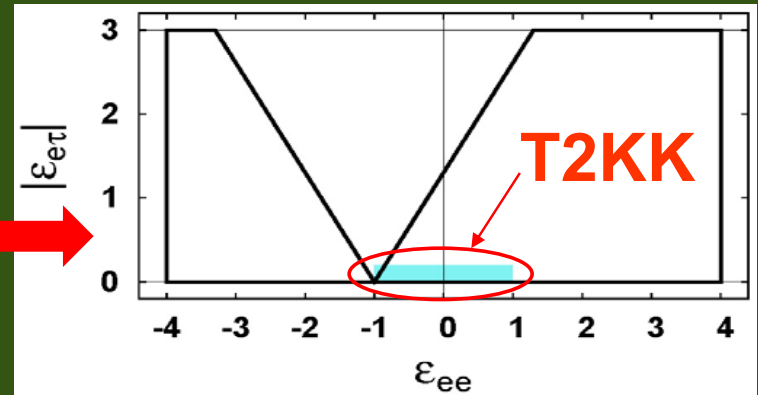
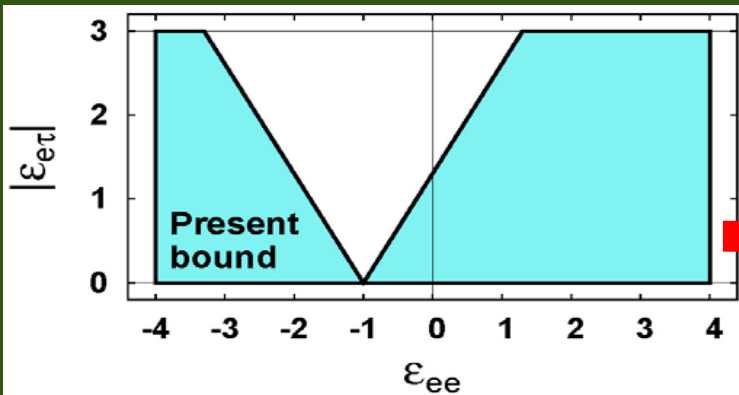
→ It would be great if we can constrain/determine c_0, c_1, c_{2j} ($j=0,1,2$) in high energy ν_{atm} data:

$$1 - P(\nu_\mu \rightarrow \nu_\mu) \simeq c_0 + \frac{c_1}{E} + \frac{c_{20}L^2 + c_{21} \sin^2(c_{22}L)}{E^2}$$

Is it possible at SK, IceCube, HK?

4. Summary (2)

- We studied phenomenologically sensitivity to **NSI** in propagation of the T2KK proposal.
- Under the assumptions $\epsilon_{e\mu} = \epsilon_{\mu\mu} = \epsilon_{\mu\tau} = 0$ & $\epsilon_{\tau\tau} = |\epsilon_{e\tau}|^2 / (1 + \epsilon_{ee})$, we found that T2KK can restrict the **NSI** parameters: $|\epsilon_{ee}| \lesssim 1$, $|\epsilon_{e\tau}| \lesssim 0.2$



- If ϵ_{ee} , $|\epsilon_{e\tau}|$ and s_{13} are large, then T2KK can determine ϵ_{ee} , $|\epsilon_{e\tau}|$, δ and $\arg(\epsilon_{e\tau})$ separately.