

# Summary of WG1 (Theoretical Part)

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<http://physdep.okayama-u.ac.jp/nufact07/>



## Phenomenology with certain detectors

Terranova:  $\nu$  hierarchy from CP-blind observables w/ high density mag. det.  
Majumdar: Tri-bimaximal mixing

## Theoretical discussions on $\nu$ masses

Farzan: CP violation: Zero, maximal or between the two extremes  
Winter: extended quark-lepton complementarity

## Sterile $\nu$ scenario

Schwetz-Mangold: Sterile  $\nu$  oscillations after first MiniBooNE results  
Karagiorgi: Sterile  $\nu$  Oscillations and CP-Violation Implications for MiniBooNE

## New physics/Non-Standard Interactions

Agarwalla: New Physics searches with Beta Beams  
Ohlsson: Effects of NSI in MINOS  
Sugiyama: More on NSI at MINOS  
Ota: NSI in reactor and superbeam experiments

## Unitarity

Xing: Leptonic unitarity triangle in matter  
Kimura: CP Phase in  $\nu_{\mu} \rightarrow \nu_{\mu}$   
Lopez-Pavon: CP-violation from non-unitary leptonic mixing

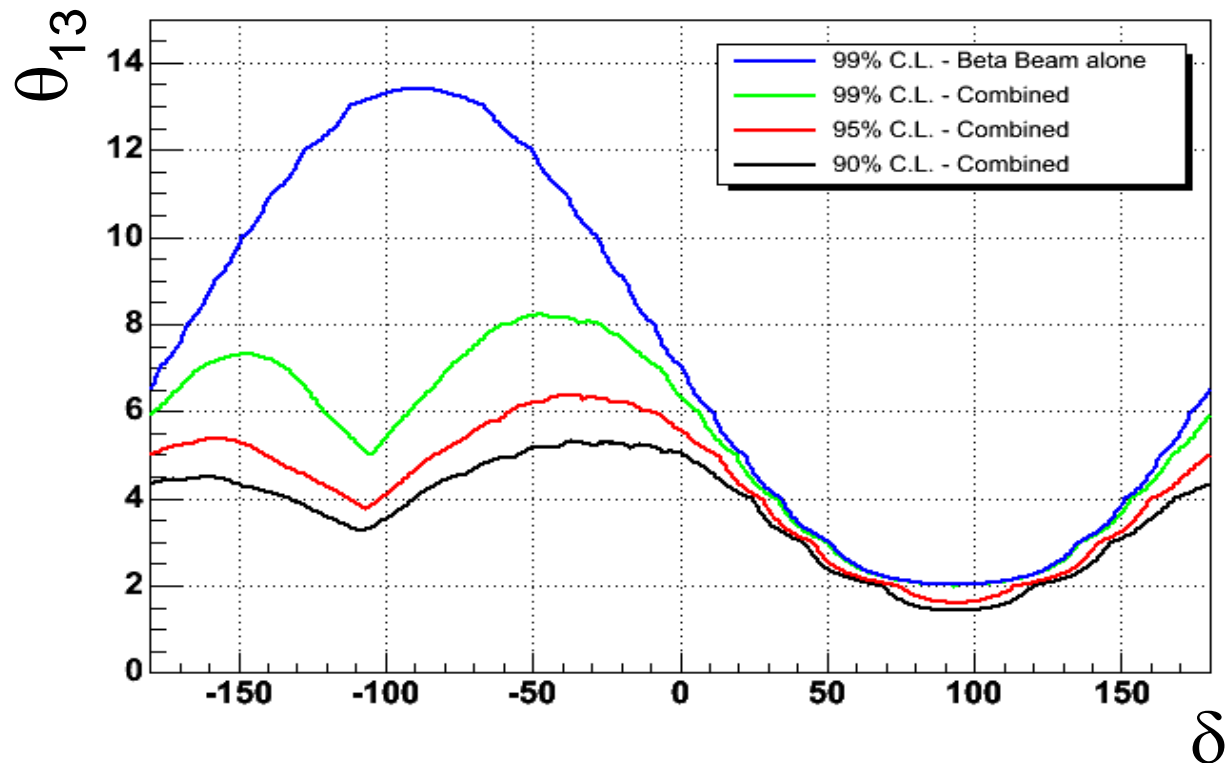
**Terranova** Combination of atmospheric + Beta Beam  
w/ charge ID by a magnetized iron detector

$$E_R = \pm \Delta m_{31}^2 L_{magic} \cos 2\theta_{13} / 4\pi$$

$$\Gamma_R = |\Delta m_{31}^2| L_{magic} \sin 2\theta_{13} / 2\pi$$

resonance occurs  
only for  $\nu$  (NH) or  
only for  $\bar{\nu}$  (IH)

→ mass hierarchy  
can be determined  
at 90% CL for  $\theta_{13}$   
> 4° (normal  
hierarchy  
negative  $\delta$ ).



Majumdar

## Tri-bimaximal mixing

$$\sin^2\theta_{23} = 1/2, \quad \sin^2\theta_{12} = 1/3, \quad \sin^2\theta_{13} = 0$$

Follows exactly from  $A_4$  symmetry

$$U = \begin{pmatrix} \sqrt{2/3} & \sqrt{1/3} & 0 \\ -\sqrt{1/6} & \sqrt{1/3} & \sqrt{1/2} \\ \sqrt{1/6} & -\sqrt{1/3} & \sqrt{1/2} \end{pmatrix}$$

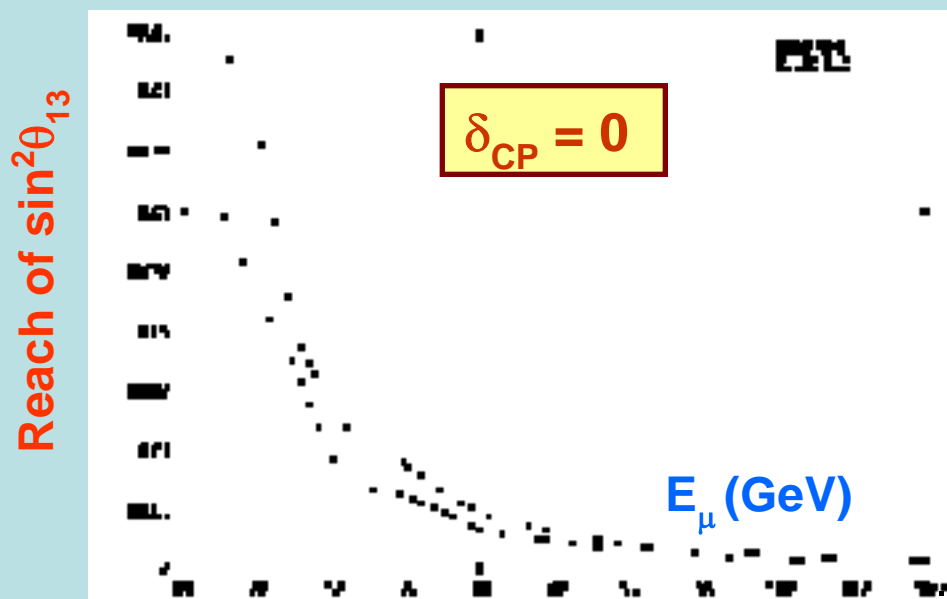
Some physics studies have been made for possible neutrino beams from Neutrino Factory with ICAL at INO as the End-detector.

Two baseline lengths are considered

Possible signals for deviation from tri-bimaximality are studied

$\sin^2\theta_{13}$  reach  $\sim 0.001$  ( $\theta_{13} < 2^\circ$ ) at INO is obtained for  $E_\mu \sim 105$  GeV.

The effect of CP-violation and of mass hierarchy on  $\sin^2\theta_{13}$  reach is also studied.



- Zero Dirac phase
  - No CP-violation  $\equiv$  zero Dirac as well as Majorana phases; **Rephasing Invariants**;
  - $\delta = 0$  **but**  $\phi_1, \phi_2 \neq 0$ : **Conditions on  $m_\nu$** ;

- **Maximal  $\delta$ ;  $\mu - \tau$  reflection symmetry;**

$$\nu_e \rightarrow \xi_1 \nu_e^c, \quad \nu_\mu \rightarrow \xi_2 \nu_\tau^c, \quad \nu_\tau \rightarrow \xi_3 \nu_\mu^c,$$

- Arbitrary  $\delta$  between zero and maximal value: **Generalized  $\mu - \tau$  reflection symmetry.**

$$\nu_\alpha \rightarrow \sum_\beta P_{\alpha\beta}(\alpha, \phi) \nu_\beta^c \quad P(\alpha, \phi) = U_{23}(\alpha) \text{Diag}[1, 1, e^{i\phi}] U_{23}^T(\alpha)$$

- Relations between the phases of the **CKM** and **PMNS** matrix

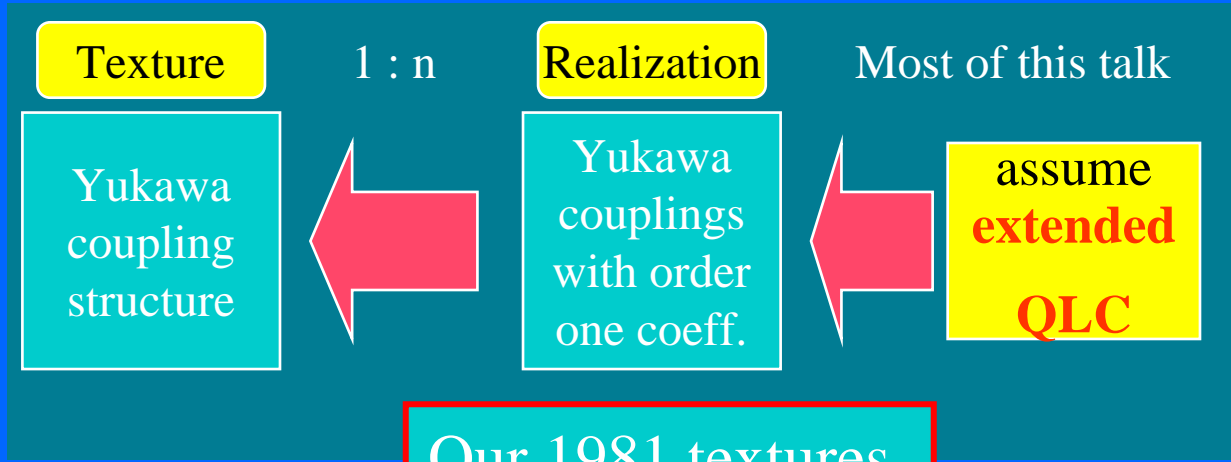
under certain conditions  $\rightarrow$

$$|\sin \theta_{13}| \simeq \frac{\sin \theta_C}{\sqrt{2}}$$

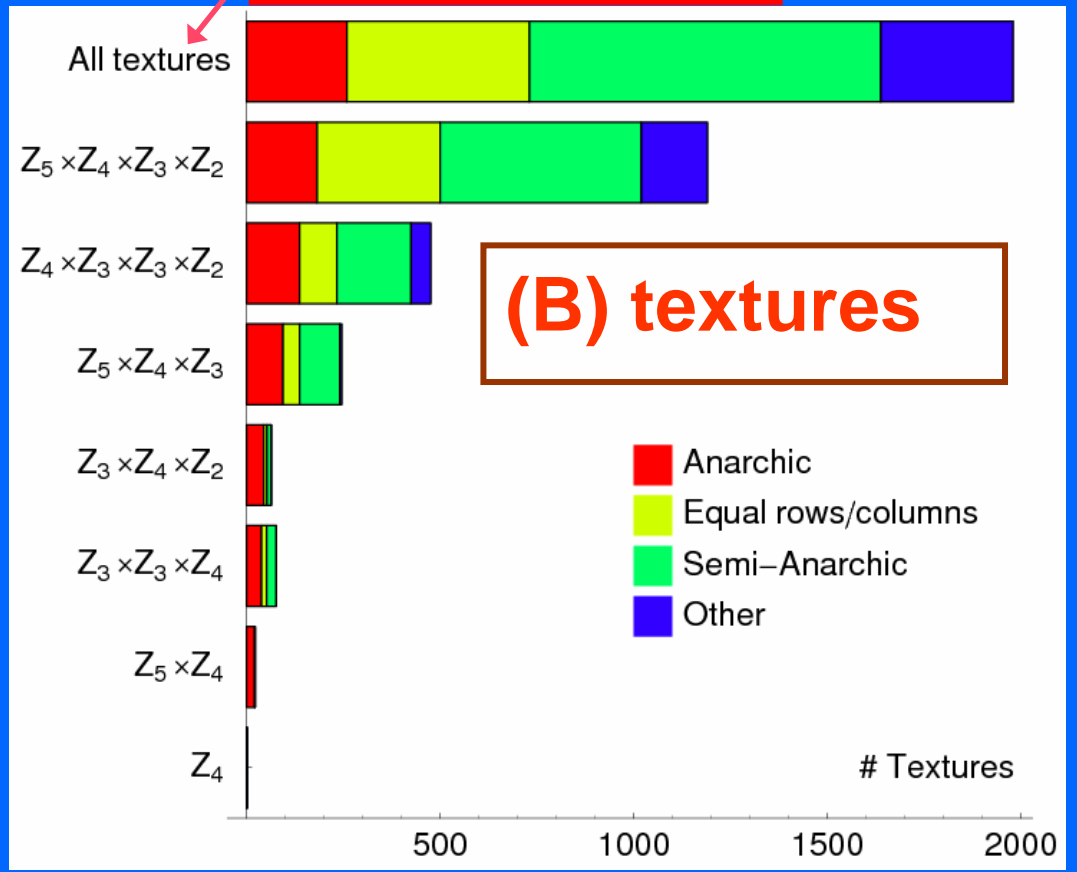
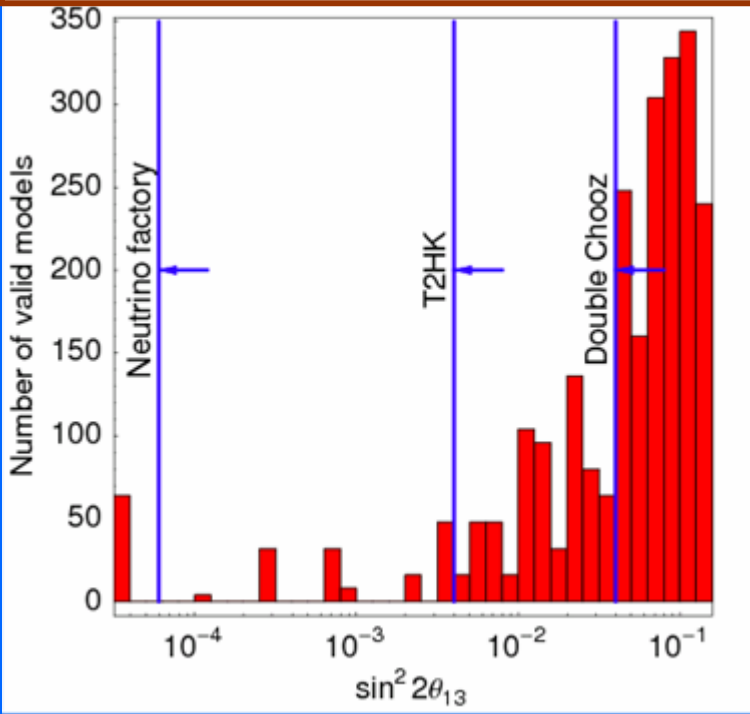
$$\sin \delta \approx \frac{|V_{ub}|}{\sin \theta_C} \sin \delta_{CKM}$$

# Winter

## Bottom-up approach:



### (A) prediction for $\theta_{13}$



### (B) textures

# Sterile neutrino scenario

$$\Delta m_{\text{sol}}^2 \sim 10^{-4} \text{ eV}^2$$

$$\Delta m_{\text{atm}}^2 \sim 10^{-3} \text{ eV}^2$$

$$\Delta m_{\text{LSND}}^2 \sim O(1) \text{ eV}^2$$

→ at least one  $\nu_s$  is required

LSND( $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ ): affirmative

MiniBOONE( $\nu_\mu \rightarrow \nu_e$ ): negative

difference between  $\nu$  & anti- $\nu$  may offer a promising fit

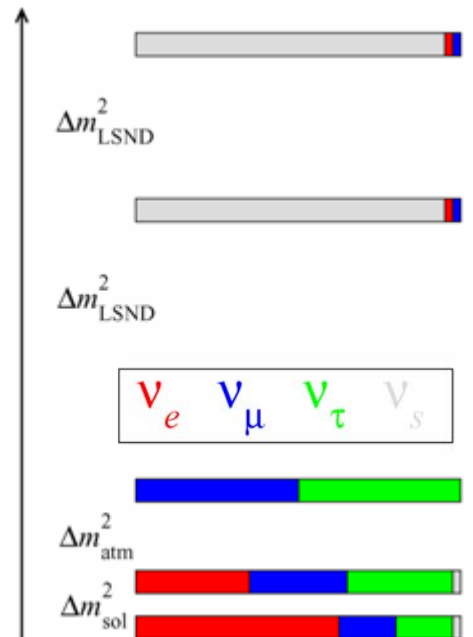
(3+2)-scheme w/ CP phase  $\delta$

$$\begin{aligned}
 P_{\nu_\mu \rightarrow \nu_e} &= 4 |U_{e4}|^2 |U_{\mu4}|^2 \sin^2 \phi_{41} \\
 &+ 4 |U_{e5}|^2 |U_{\mu5}|^2 \sin^2 \phi_{51} \\
 &+ 8 |U_{e4} U_{\mu4} U_{e5} U_{\mu5}| \sin \phi_{41} \sin \phi_{51} \cos(\phi_{54} - \delta)
 \end{aligned}$$

with the definitions

$$\phi_{ij} \equiv \frac{\Delta m_{ij}^2 L}{4E},$$

$$\delta \equiv \arg(U_{e4}^* U_{\mu4} U_{e5} U_{\mu5}^*).$$



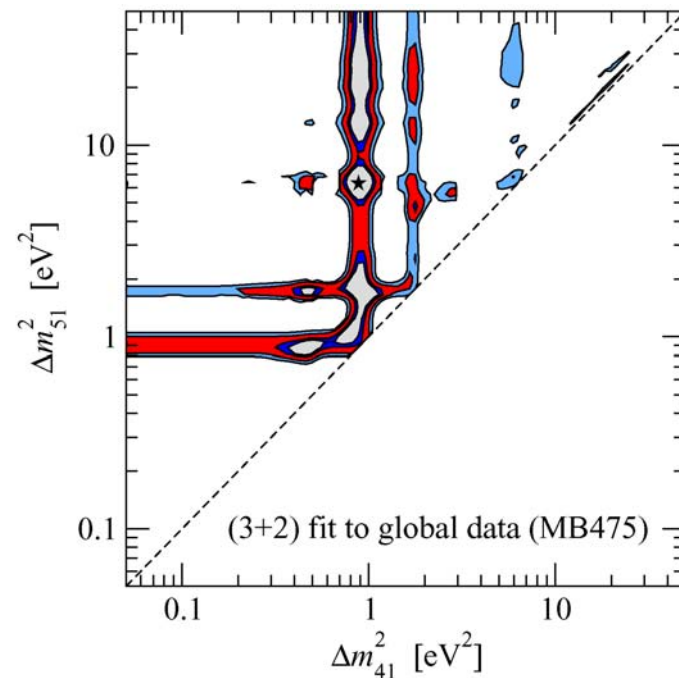
# Schwetz-Mangold

$$\Delta m_{41}^2 = 0.89 \text{ eV}^2$$

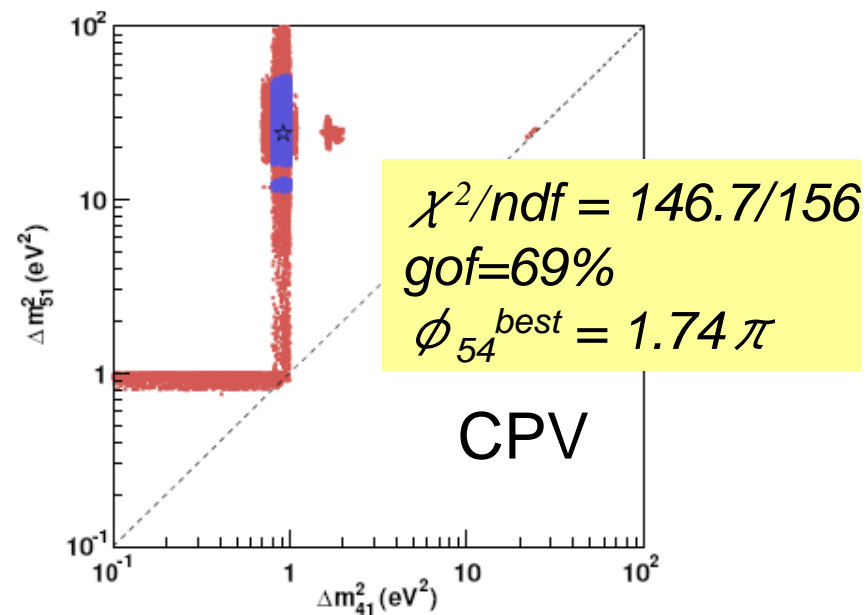
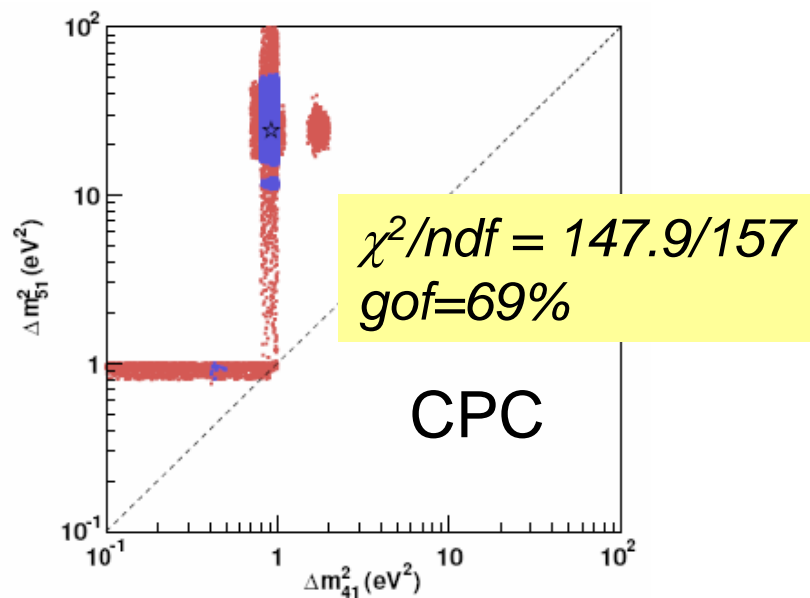
$$\Delta m_{51}^2 = 6.49 \text{ eV}^2$$

$$\chi_{\min}^2 = 94.5 / (107 - 7)$$

$$\phi_{54}^{\text{best}} = 1.64 \pi$$



# Karagiorgi





- (3+2) schemes
  - offer the possibility of CP violation to reconcile LSND and MiniBooNE,
  - but there is tension between appearance and disappearance data ( $3\sigma$ ,  $4\sigma$  for MB300)

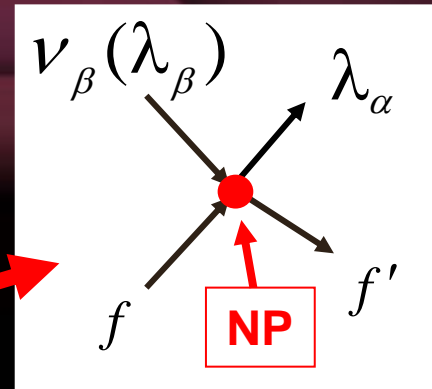
**The two works basically agree, but some details (comparison between CPC & CPV, inclusion of low energy data, etc.) have to be worked out in future.**

# New Physics/Non-Standard Interaction

## New Physics involving charged leptons

If either of the particles with flavor  $\alpha$  and  $\beta$  in the NP interaction is charged lepton, then

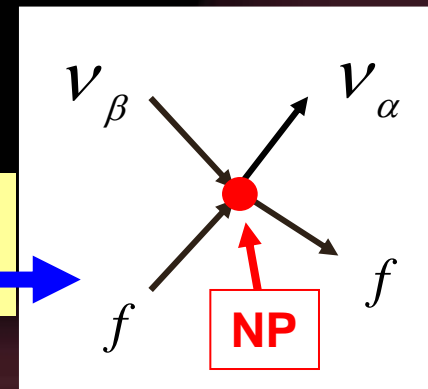
- New Physics at source and detector:  
Agarwalla, Ota, Lopez-Pavon



## New Physics with neutral current

If the particles with flavor  $\alpha$  and  $\beta$  in the NP interaction are both neutrinos, then

- New Physics in propagation (matter effect):  
Ohlsson, Sugiyama, Ota



$$\begin{pmatrix} A & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

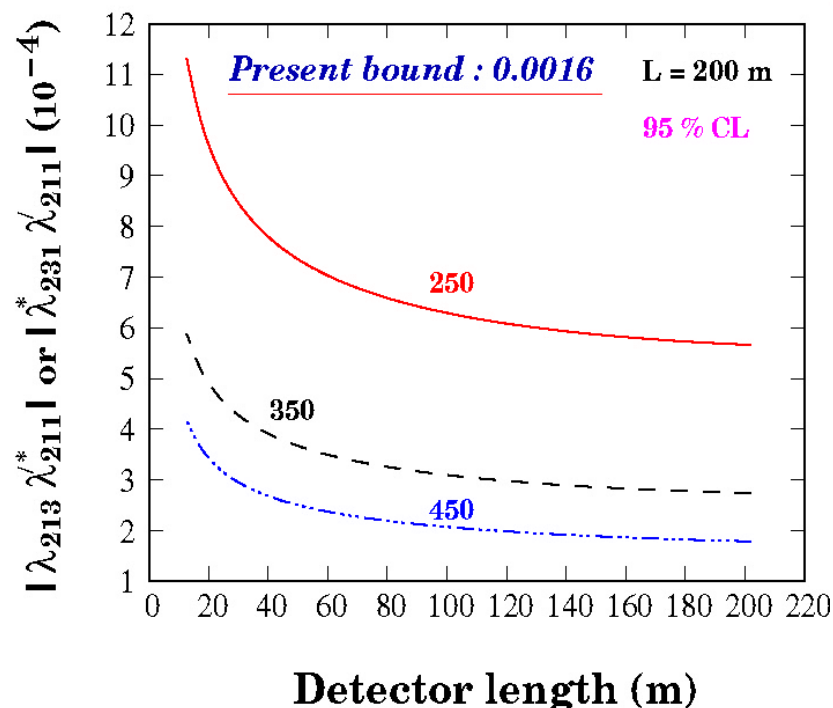
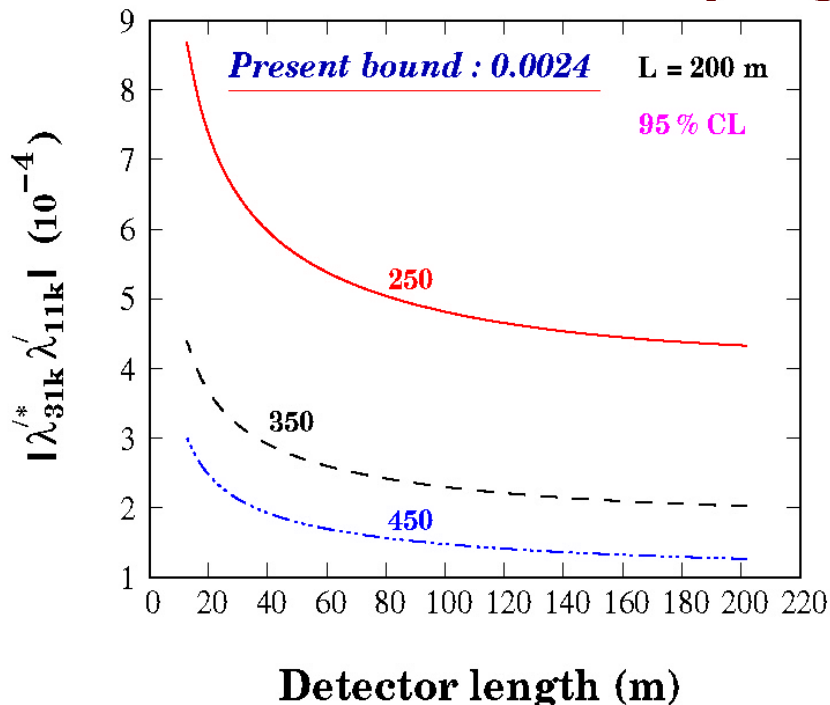


$$A \begin{pmatrix} 1 + \epsilon_{ee} & \epsilon_{e\mu} & \epsilon_{e\tau} \\ \epsilon_{e\mu}^* & \epsilon_{\mu\mu} & \epsilon_{\mu\tau} \\ \epsilon_{e\tau}^* & \epsilon_{\tau\mu}^* & \epsilon_{\tau\tau} \end{pmatrix}$$

$$\mathcal{L}_{\lambda'} = \lambda'_{ijk} \left[ \tilde{d}_L^j \bar{d}_R^k \nu_L^i + (\tilde{d}_R^k)^* (\bar{\nu}_L^i)^c d_L^j \right] + h.c.$$

■ We consider a  $\beta$ -beam experiment with **CERN-INO** baseline.  $\mathcal{R}$  interactions may obstruct a clean extraction of the mixing angle  $\theta_{13}$  or determination of the **mass hierarchy** unless the bounds on the  $\lambda'$  couplings are tightened

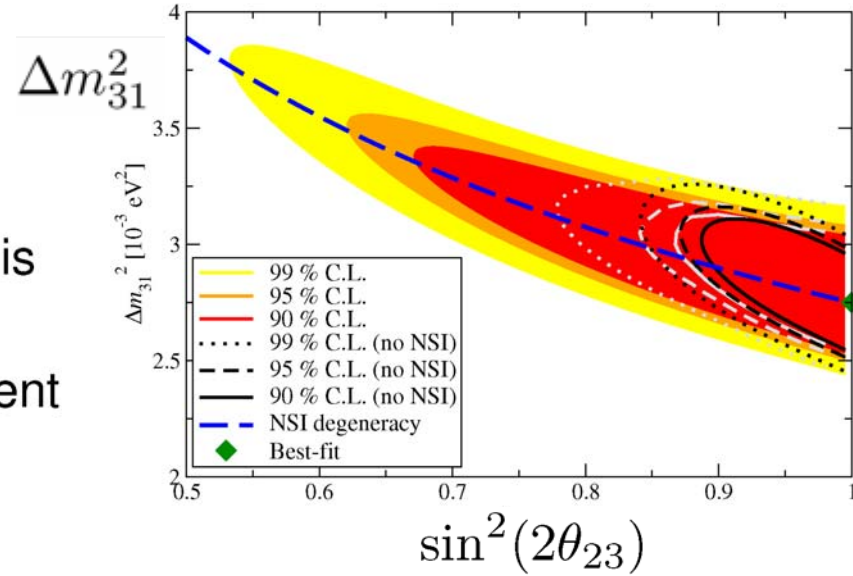
■ one might see a clean signal of new physics and **put tighter constraints on the  $\lambda'$  couplings**



# Ohlsson

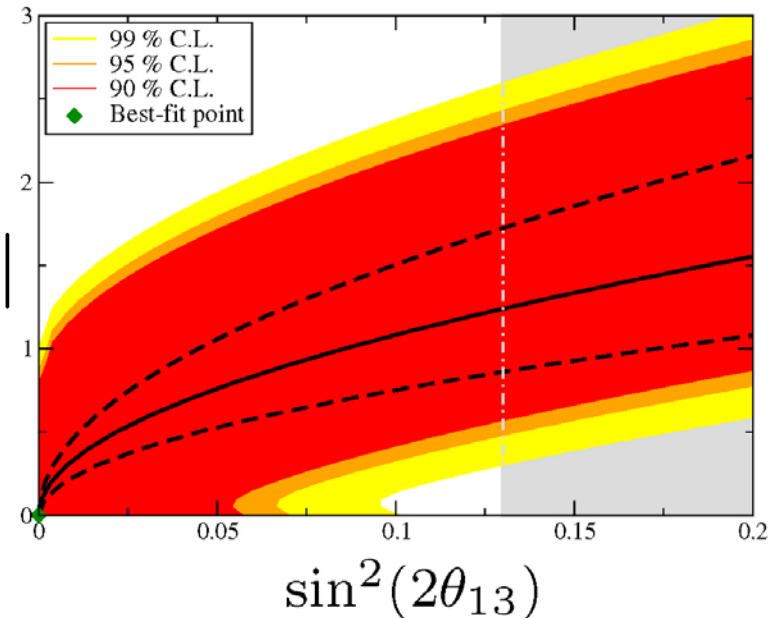
$$\mathbf{A} \begin{pmatrix} 1 + \epsilon_{ee} & 0 & \epsilon_{e\tau} \\ 0 & 0 & 0 \\ \epsilon_{e\tau}^* & 0 & \epsilon_{\tau\tau} \end{pmatrix}$$

- Allowed region in the  $\sin^2(2\theta_{23}) - \Delta m_{31}^2$  plane is extended to smaller values of  $\sin^2(2\theta_{23})$  and larger values of  $\Delta m_{31}^2$  if NSI effects are present
- Possible bounds on the NSI parameter  $\epsilon_{e\tau}$  depending on the value of  $\theta_{13}$
- Better upper bound on  $\sin^2(2\theta_{13})$  than CHOOZ only for small values of  $|\epsilon_{e\tau}|$



$$|\epsilon_{e\tau}|$$

$\sin^2(2\theta_{13}) = 0.07$	$-2.16 < \epsilon_{e\tau} < -1.31$	90 % C.L.
	$-0.60 < \epsilon_{e\tau} < 0.41$	
$\sin^2(2\theta_{13}) = 0$	$-0.69 < \epsilon_{e\tau} < 0.8$	90 % C.L.



Sugiyama

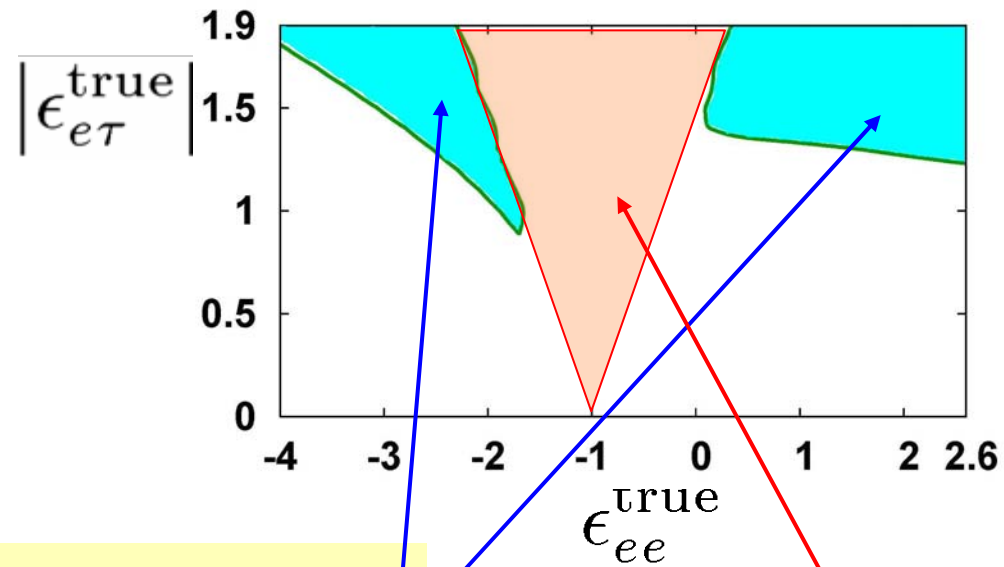
$$\mathbf{A} \begin{pmatrix} 1 + \epsilon_{ee} & 0 & \epsilon_{e\tau} \\ 0 & 0 & 0 \\ \epsilon_{e\tau}^* & 0 & \epsilon_{\tau\tau} \end{pmatrix}$$

$\nu_e$  appearance in MINOS

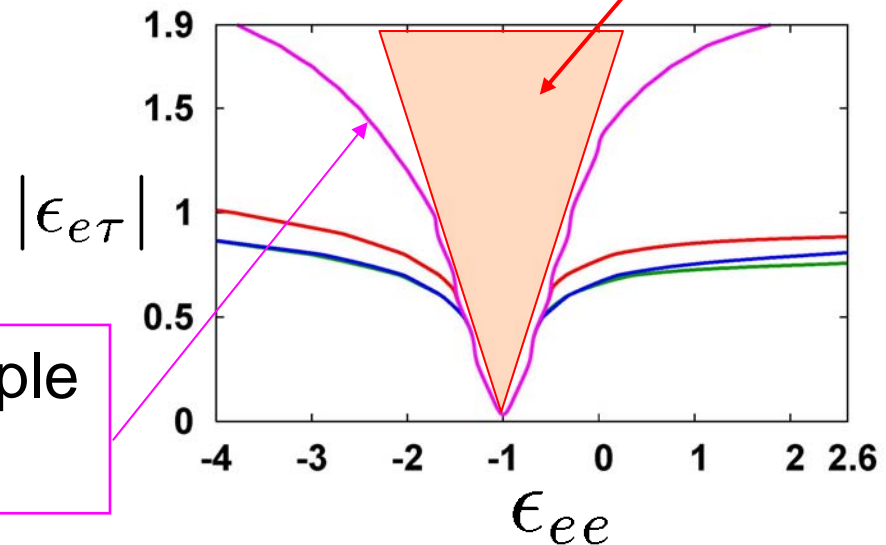
● If MINOS finds  $\nu_e$  appearance, and if true values exist within the light blue region, we **can exclude**  $\epsilon_{ee} = \epsilon_{e\tau} = 0$

● If MINOS does not find  $\nu_e$  appearance, constraints on  $\epsilon$  does **not improve much**.

excluded above the purple line for  $\delta + \arg[\epsilon_{e\tau}] = -\pi/2$



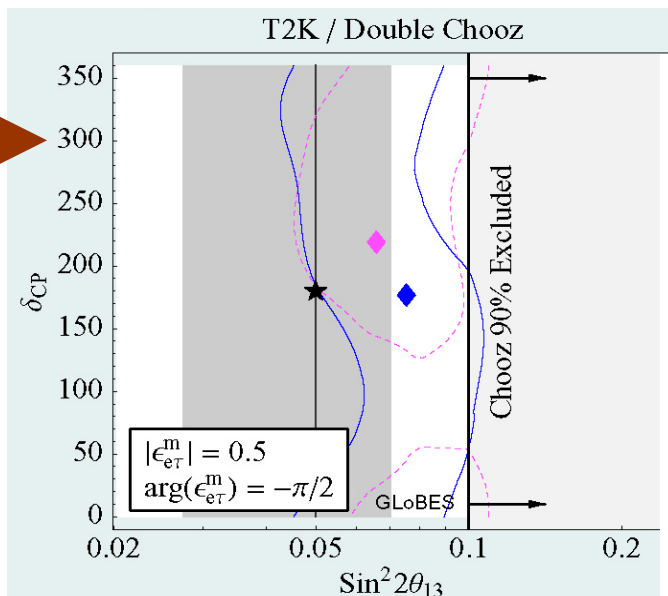
excluded by  $\nu_{atm}$  & K2K



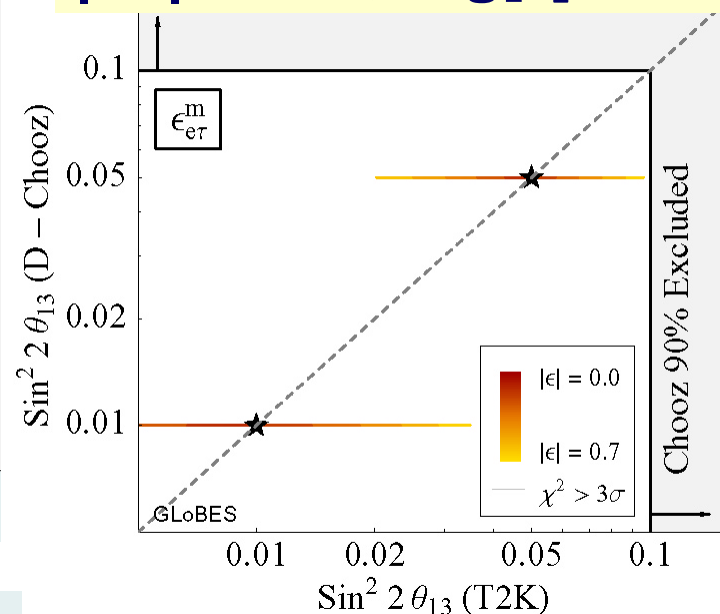
Ota

Mismatch

Best fit points for reactor & T2K don't agree

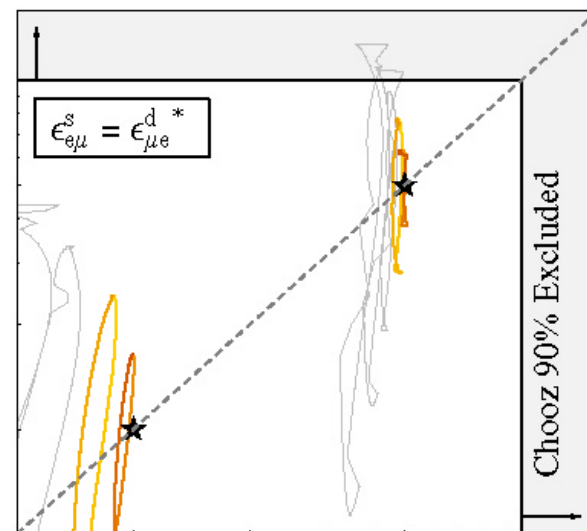
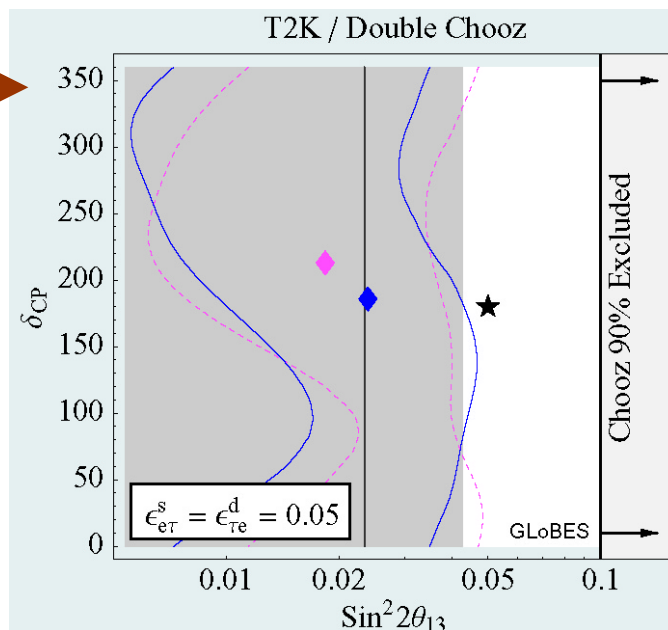


$|\epsilon^m| = 0-0.7, \arg[\epsilon] = 0-2\pi$



Offset

Best fit points for two agree but miss the true point

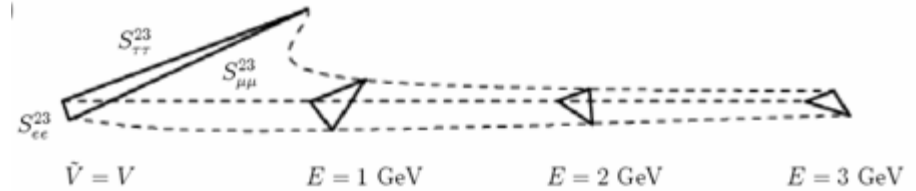


$|\epsilon^{s,d}| = 0-0.1, \arg[\epsilon] = 0-2\pi$

Discovery reach : depends on arg[epsilon]

# Xing

◆ Testing the unitarity of lepton flavor mixing is an important task in the era of precision measurements. A way to explore new physics.



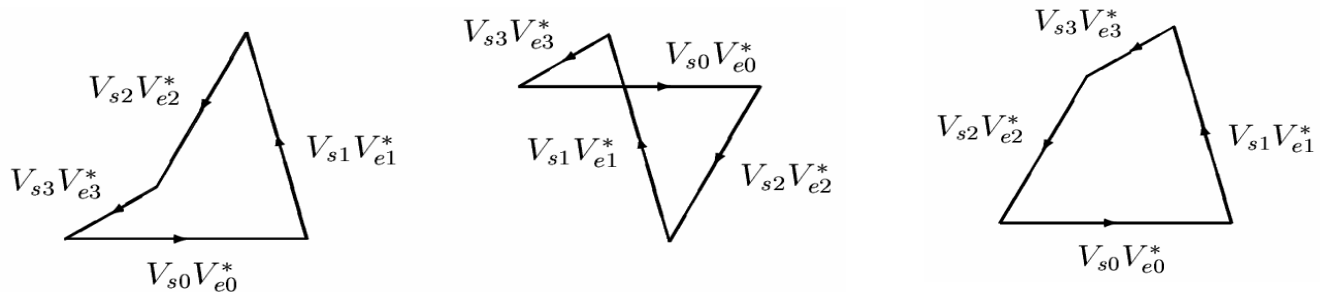
$$\begin{aligned} \tilde{V}_{\mu 1} \tilde{V}_{\tau 1}^* &= \frac{(\hat{\Delta}_{21} + A)\Delta_{31}}{\tilde{\Delta}_{21}\tilde{\Delta}_{31}} V_{\mu 1} V_{\tau 1}^* + \frac{(\hat{\Delta}_{11} + A)\Delta_{32}}{\tilde{\Delta}_{21}\tilde{\Delta}_{31}} V_{\mu 2} V_{\tau 2}^* \\ \tilde{V}_{\mu 2} \tilde{V}_{\tau 2}^* &= \frac{(\hat{\Delta}_{32} + A)\Delta_{21}}{\tilde{\Delta}_{32}\tilde{\Delta}_{21}} V_{\mu 2} V_{\tau 2}^* + \frac{(\hat{\Delta}_{22} + A)\Delta_{31}}{\tilde{\Delta}_{32}\tilde{\Delta}_{21}} V_{\mu 3} V_{\tau 3}^* \\ \tilde{V}_{\mu 3} \tilde{V}_{\tau 3}^* &= \frac{(\hat{\Delta}_{13} + A)\Delta_{23}}{\tilde{\Delta}_{13}\tilde{\Delta}_{23}} V_{\mu 3} V_{\tau 3}^* + \frac{(\hat{\Delta}_{33} + A)\Delta_{21}}{\tilde{\Delta}_{13}\tilde{\Delta}_{23}} V_{\mu 1} V_{\tau 1}^* \end{aligned}$$

◆ In realistic seesaw models, the  $3 \times 3$  MNS matrix is non-unitary.

Natural seesaw: unitarity violation  $\sim < 10^{-24}$

Unnatural seesaw: unitarity violation  $\sim < 10^{-2}$

◆ The existence of sterile neutrinos would violate the unitarity of the  $3 \times 3$  MNS matrix (at a detectable level?)



# Kimura

Independent determination of  $\delta$  from  $\nu_\mu \rightarrow \nu_\mu$   
→ Test of unitarity

General feature on CP dependence

$$P_{\mu e} = A_{\mu e} \cos \delta + B_{\mu e} \sin \delta + C_{\mu e}$$
$$P_{\mu\mu} = A_{\mu\mu} \cos \delta + C_{\mu\mu}$$

Magnitude of each coefficient

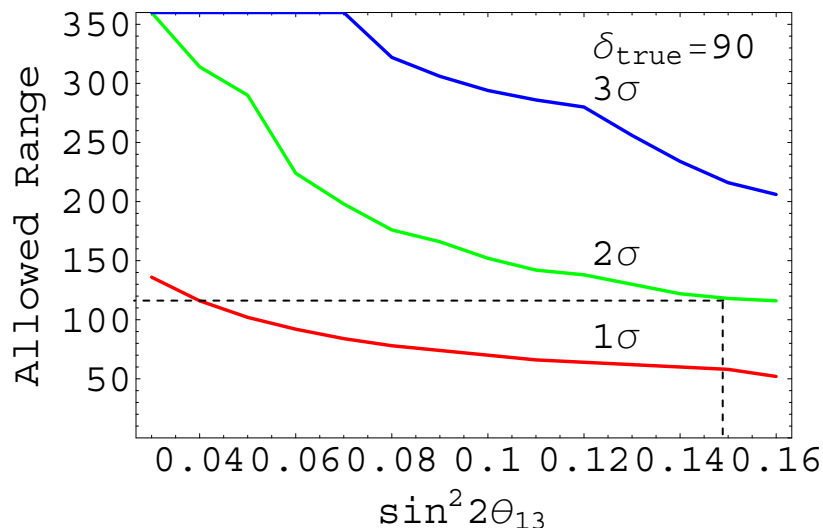
$$A_{\mu\mu} = -A_{\mu e} = O(\alpha s_{13})$$

$$\alpha = \Delta m_{21}^2 / \Delta m_{31}^2$$

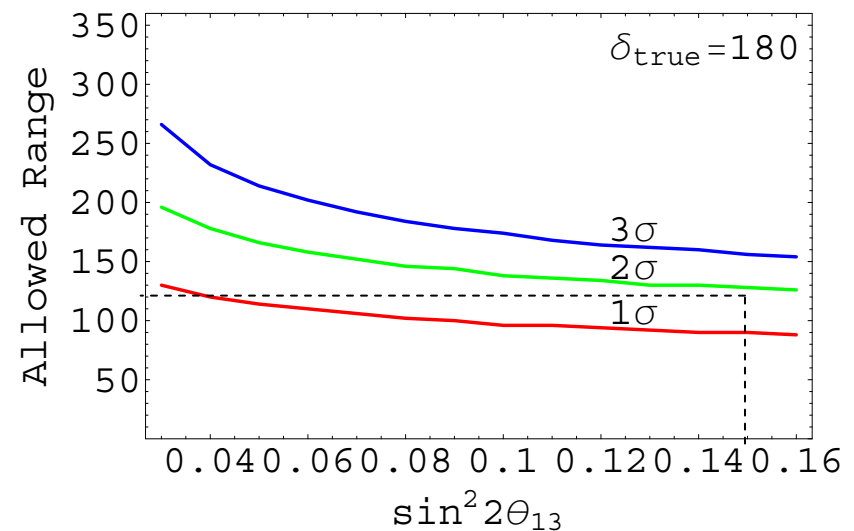
4MW JPARC beam, 500kt WC Detector,  
E=0.4-10 GeV and L=295km, 5000km,  
10 years run

3 flavor unitarity is assumed

Allowed range of CP phase



Allowed range of CP phase





# Lopez-Pavon

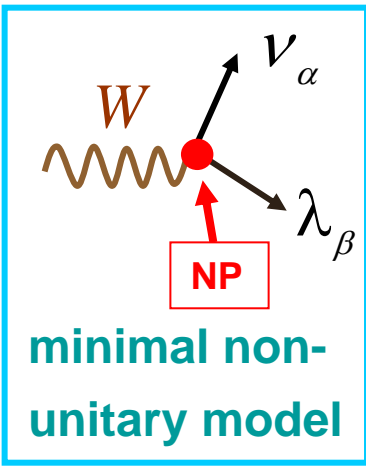
## Unitarity of the leptonic mixing matrix

$U \rightarrow N$  (non-unitary)

$NN^\dagger - 1$ : deviation from unitarity

$$|NN^\dagger| \approx \begin{pmatrix} 0.994 \pm 0.005 & < 7.1 \cdot 10^{-5} & < 1.6 \cdot 10^{-2} \\ < 7.1 \cdot 10^{-5} & 0.995 \pm 0.005 & < 1.0 \cdot 10^{-2} \\ < 1.6 \cdot 10^{-2} & < 1.0 \cdot 10^{-2} & 0.995 \pm 0.005 \end{pmatrix} \quad 90\% \text{ C.L.}$$

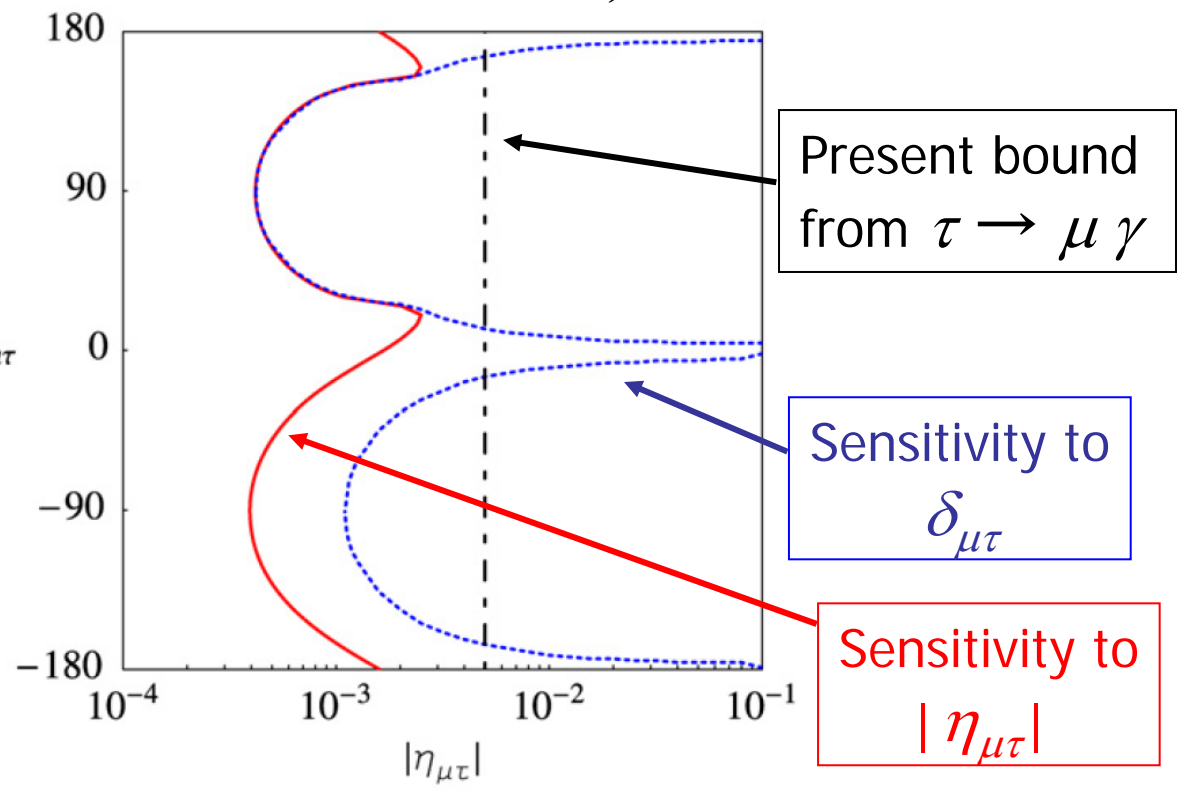
mostly from rare decays



Phase of N

$$V_\mu \leftrightarrow V_\tau$$

For non-trivial  $\delta_{\mu\tau}$ , one order of magnitude improvement for  $|\eta_{\mu\tau}|$



## Future problems toward nufact08

After the ISS report is finished, there are still a lot of problems ahead of us:

- Predictions of various schemes on deviation from SM+massive  $\nu$
- Quantitative discussions on determination of small quantities such as  $\theta_{13}$ ,  $\pi/4 - \theta_{23}$ , and parameters of new physics and/or non-unitarity (correlations of errors, degeneracies, dependence on the beam energy and the baseline, etc.)
- Test of leptonic unitarity
- Other strong physics case for future LBL
- Many more .....