New physics effects in long baseline experiments

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Contents

Introduction New Physics in v oscillation Summary

Based on:
N. Kitazawa, H. Sugiyama, OY, hep-ph/0606013
OY, arXiv:0704.1531 [hep-ph]

1. Introduction

Framework of 3 flavor v oscillation

Mixing matrix

$$\begin{pmatrix} v_{e} \\ v_{\mu} \\ v_{\mu} \\ v_{\tau} \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix} \begin{pmatrix} v_{1} \\ v_{2} \\ v_{3} \end{pmatrix}$$

Functions of mixing angles $\theta_{12}, \theta_{23}, \theta_{13}, \text{ and CP}$ phase δ

Information we have obtained so far:

 v_{solar} +KamLAND (reactor)

v_{atm}+K2K,MINOS(accelerators) →

$$\theta_{12} \cong \frac{\pi}{6}, \Delta m_{21}^2 \cong 8 \times 10^{-5} eV^2$$

$$\theta_{23} \cong \frac{\pi}{4}, |\Delta m_{32}^2| \cong 2.5 \times 10^{-3} \, eV^2$$

CHOOZ (reactor)

Mixing matrix has been roughly determined:

$$U = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{T1} & U_{T2} & U_{T3} \end{pmatrix} \cong \begin{pmatrix} C_{12} & S_{12} & 0 \\ -S_{12}/\sqrt{2} & C_{12}/\sqrt{2} & 1/\sqrt{2} \\ S_{12}/\sqrt{2} & -C_{12}/\sqrt{2} & 1/\sqrt{2} \end{pmatrix}$$
$$\theta_{12} \cong \pi/6$$

However,

θ₁₃ :only upper bound is known
 δ :undetermined

Next task is to measure θ_{13} , sign(Δm_{31}^2) and δ

Most realistic way to measure θ_{13} , sign(Δm_{31}^2) and δ is long baseline experiments by accelerators or reactors.



hierarchy

 $\Delta m_{32}^2 > 0$

hierarchy

 $\Delta m_{32}^2 < 0$

Both

hierarchies

are allowed

mass

Future LBL experiments

To perform precise measurements of θ_{13} and δ , one has to have a lot of numbers of events to reduce statistical errors.

→We need high intensity beams

Candidates for high intensity beam in the future:

(conventional) superbeam

neutrino factory

 μ in a storage ring

beta beam

RI in a storage ring

$$\begin{array}{c} \mathbf{n} & \left\{ \begin{matrix} \pi^{+} \rightarrow \mu^{+} + \mathbf{v}_{\mu} \\ \pi^{-} \rightarrow \mu^{-} + \mathbf{v}_{\mu} \end{matrix} \right. \begin{matrix} \mathbf{v}_{\mu} \rightarrow \mathbf{v}_{e} \\ \overline{\mathbf{v}}_{\mu} \rightarrow \overline{\mathbf{v}}_{e} \end{matrix} \\ \left\{ \begin{matrix} \mu^{+} \rightarrow \mathbf{e}^{+} + \mathbf{v}_{e} + \mathbf{v}_{\mu} \end{matrix} \right. \begin{matrix} \mathbf{v}_{e} \rightarrow \mathbf{v}_{\mu} \\ \mu^{-} \rightarrow \mathbf{e}^{-} + \mathbf{v}_{e} + \mathbf{v}_{\mu} \end{matrix} \\ \left\{ \begin{matrix} \mathbf{e} & \mathbf{v}_{e} \rightarrow \mathbf{v}_{\mu} \\ \mathbf{v}_{e} \rightarrow \overline{\mathbf{v}}_{\mu} \end{matrix} \right. \\ \left\{ \begin{matrix} \mathbf{e} & \mathbf{e}^{-} & \mathbf{e}^{-} & \mathbf{v}_{e} \end{matrix} \right. \end{matrix} \\ \left\{ \begin{matrix} \mathbf{e} & \mathbf{e}^{-} & \mathbf{e}^{-} & \mathbf{v}_{e} \end{matrix} \right. \end{matrix} \\ \left\{ \begin{matrix} \mathbf{e} & \mathbf{e}^{-} & \mathbf{e}^{-} & \mathbf{v}_{e} \end{matrix} \right. \end{matrix} \\ \left\{ \begin{matrix} \mathbf{e} & \mathbf{e}^{-} & \mathbf{e}^{-} & \mathbf{v}_{e} \end{matrix} \right. \end{matrix} \\ \left\{ \begin{matrix} \mathbf{e} & \mathbf{e}^{-} & \mathbf{e}^{-}$$

Example of expected sensitivity and time scale (FERMILAB-FN-0778-AD-E (=hep-ex/0509019))





Sept. 2005 ~ Sept. 2006 http://www.hep.ph.ic.ac.uk/iss/

Evaluate the physics case for the facility
Study options for the accelerator complex and neutrino detection systems

Physics Group Y. Nagashima
 Detector Group A. Blondel
 Accelerator Group M. Zisman

Theory Subgroup S.F. King
 Phenomenology Subgroup OY
 Experiment Subgroup K. Long
 Muon Subgroup L. Roberts

Deviation from SM with massive neutrinos (test of unitarity, probe of NP) was the main issue.

Final report: http://www.hep.ph.ic.ac.uk/~longkr/UKNF/Scoping-study/ISS-wwwsite/WG1-PhysPhen/Planning-drafts/Report/Current/PhysReport.pdf It will appear on arXiv soon.

2. New Physics in \nu oscillation

2.1 New Physics in v oscillation

Just like at B factories, high precision measurements of ν oscillation can be used also to probe physics beyond SM by looking at from deviation from SM+massive ν

Here we study phenomenologically new physics which is described by 4-fermi exotic interactions:

$$\mathcal{L}_{eff} = G_{NP}^{\alpha\beta} \bar{\nu}_{\alpha} \gamma^{\mu} \nu_{\beta} \bar{f} \gamma_{\mu} f' \qquad \mathcal{L}_{NP} = G_{N}^{\alpha\beta} \bar{\nu}_{\alpha} \gamma^{\mu} \ell_{\beta} \bar{f} \gamma_{\mu} f'$$





(1) Effects of New Physics at source and detector Deviation from the standard form is small: Grossman (PLB359:141,1995) $|(U^{s}-1)_{\alpha\beta}| < O(10^{-2}), |(U^{d}-1)_{\alpha\beta}| < O(10^{-2})$

(2) New Physics effects in propagation

1. Constraints from various v experiments: Davidson et al (JHEP 0303:011,2003)



2. Constraints from atmospheric neutrinos: Friedland-Lunardini (Phys.Rev.D72:053009,2005)

$$\begin{split} \mathcal{E}_{ee}, \mathcal{E}_{e\tau}, \mathcal{E}_{\tau\tau} &\sim \mathbf{O(1)} \text{ are consistent with } v_{atm} \text{ data, provided} \\ \epsilon_{\tau\tau} &\sim \frac{|\epsilon_{e\tau}|^2}{1+\epsilon_{ee}} \quad 0 \leq |\epsilon_{e\tau}| \lesssim 1+\epsilon_{ee} \quad -1 \lesssim \epsilon_{ee} \lesssim 1.5 \end{split}$$

Since the parameters $\mathcal{E}_{\alpha\beta}$ can be of O(1) only for New Physics in propagation, we will consider only NP in propagation here.

NP effects in propagation becomes important when baseline L is larger

because oscillation probability $\propto \sin^2 \left(\text{something} \times \varepsilon_{\alpha\beta} AL \right)$ where AL ~ L/2000km $A \equiv \sqrt{2}G_F N_e$

Experiments with a longer baseline are advantageous

Here we will discuss MINOS (L=730km)

2.2 Analytical formula for the oscillation probability in matter with New Physics

(1)For the standard 3 flavor case, analytical formula for the oscillation probability in matter is known: Kimura, Takamura and Yokomakura (PLB537:86,2002)

(2) KTY formalism to more general cases (e.g., NP etc.) was discussed: OY arXiv:0704.1531 [hep-ph] In particular, in the limit $\Delta m_{21}^2 \rightarrow 0$, $P(v_{\mu} \rightarrow v_{e})$ can be obtained analytically with

$$\mathcal{A} = \mathbf{A} \begin{pmatrix} 1 + \mathbf{\mathcal{E}}_{ee} & 0 & \mathbf{\mathcal{E}}_{e\tau} \\ 0 & 0 & 0 \\ \mathbf{\mathcal{E}}_{e\tau}^* & 0 & \mathbf{\mathcal{E}}_{\tau\tau} \end{pmatrix}$$
$$A \equiv \sqrt{2}G_F N_e$$
$$\mathbf{\mathcal{E}}_{e\tau} = \mathbf{\mathcal{E}}_{e\tau} \sim \mathbf{O}(1)$$

(1) Exact formula for oscillation probability in matter with standard 3 flavor neutrinos Kimura, Takamura and Yokomakura (PLB537:86,2002)

$$\begin{split} i\frac{d}{dt} \begin{pmatrix} \nu_{e} \\ \nu_{\mu} \\ \nu_{\tau} \end{pmatrix} &= \left(U\mathcal{E}U^{-1} + \mathcal{A} \right) \begin{pmatrix} \nu_{e} \\ \nu_{\mu} \\ \nu_{\tau} \end{pmatrix} \quad \mathcal{E} \equiv \begin{pmatrix} E_{1} & 0 & 0 \\ 0 & E_{2} & 0 \\ 0 & 0 & E_{3} \end{pmatrix} \quad \mathcal{A} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \mathcal{L} \equiv \sqrt{2}G_{F}N_{e} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

Problem: Obtain the values of
$$\tilde{X}_{j}^{\alpha\beta} \equiv \tilde{U}_{\alpha j}\tilde{U}_{\beta j}^{*}$$

which appear in diagonalization of
 $U\mathcal{E}U^{-1} + \mathcal{A} \equiv \tilde{U}\begin{pmatrix} \tilde{E}_{1} & 0 & 0\\ 0 & \tilde{E}_{2} & 0\\ 0 & 0 & \tilde{E}_{3} \end{pmatrix}\tilde{U}^{-1}$
 $\mathcal{A} \equiv \sqrt{2}G_{F}N_{e}\begin{pmatrix} 1 & 0 & 0\\ 0 & 0 & 0\\ 0 & 0 & 0 \end{pmatrix}$

Solution: Trivial 3 identities solve it Xing-Zhang PLB618:131,2005; OY arXiv:0704.1531 [hep-ph]

$$\begin{cases} \delta_{\alpha\beta} = \left[\tilde{U}\tilde{U}^{-1}\right]_{\alpha\beta} = \sum_{j}\tilde{U}_{\alpha j}\tilde{U}_{\beta j}^{*} = \sum_{j}\tilde{X}_{j}^{\alpha\beta} \\ \left[U\mathcal{E}U^{-1} + \mathcal{A}\right]_{\alpha\beta} = \left[\tilde{U}\tilde{\mathcal{E}}\tilde{U}^{-1}\right]_{\alpha\beta} = \sum_{j}\tilde{U}_{\alpha j}\tilde{E}_{j}\tilde{U}_{\beta j}^{*} = \sum_{j}\tilde{E}_{j}\tilde{X}_{j}^{\alpha\beta} \\ \left[\left(U\mathcal{E}U^{-1} + \mathcal{A}\right)^{2}\right]_{\alpha\beta} = \left[\tilde{U}\tilde{\mathcal{E}}^{2}\tilde{U}^{-1}\right]_{\alpha\beta} = \sum_{j}\tilde{U}_{\alpha j}\tilde{E}_{j}^{2}\tilde{U}_{\beta j}^{*} = \sum_{j}\tilde{E}_{j}^{2}\tilde{X}_{j}^{\alpha\beta} \\ \left(\frac{1}{\tilde{E}_{1}}\frac{1}{\tilde{E}_{2}}\frac{1}{\tilde{E}_{3}}\right) \begin{pmatrix}\tilde{X}_{1}^{\alpha\beta} \\ \tilde{X}_{2}^{\alpha\beta} \\ \tilde{X}_{3}^{\alpha\beta} \end{pmatrix} = \begin{pmatrix}\left[U\mathcal{E}U^{-1} + \mathcal{A}\right]_{\alpha\beta} \\ \left[(U\mathcal{E}U^{-1} + \mathcal{A})^{2}\right]_{\alpha\beta} \end{pmatrix} \end{cases}$$
 Simultaneous linear eqs.: easily solved

(2) Analytical formula for the oscillation probability in matter with New Physics in the limit $\Delta m_{21}^2 \rightarrow 0$

OY arXiv:0704.1531 [hep-ph]

$$P(\nu_{\mu} \rightarrow \nu_{e}) = -4\operatorname{Re}\left(\tilde{X}_{1}^{\mu e} \tilde{X}_{2}^{\mu e*}\right) \sin^{2}\left(\frac{\Lambda_{-L}}{2}\right) - 4\operatorname{Re}\left(\tilde{X}_{2}^{\mu e} \tilde{X}_{3}^{\mu e*}\right) \sin^{2}\left(\frac{\Lambda_{+L}}{2}\right) \\ -4\operatorname{Re}\left(\tilde{X}_{1}^{\mu e} \tilde{X}_{3}^{\mu e*}\right) \sin^{2}\left[\frac{(\Lambda_{+} - \Lambda_{-})L}{2}\right] \\ -8\operatorname{Im}\left(\tilde{X}_{1}^{\mu e} \tilde{X}_{2}^{\mu e*}\right) \sin\left(\frac{\Lambda_{-L}}{2}\right) \sin\left(\frac{\Lambda_{+L}}{2}\right) \sin\left[\frac{(\Lambda_{+} - \Lambda_{-})L}{2}\right] \\ \overline{\Lambda_{\pm}} = \frac{1}{2}\left[\Delta E_{31} + \frac{A(1 + \epsilon_{ee})}{\cos^{2}\beta}\right] \pm \frac{1}{2}\sqrt{\left[\Delta E_{31}\cos 2\theta_{13}^{\prime\prime\prime} - \frac{A(1 + \epsilon_{ee})}{\cos^{2}\beta}\right]^{2} + (\Delta E_{31}\sin 2\theta_{13}^{\prime\prime\prime})^{2}} \\ \widetilde{X}_{1}^{\mu e} = \frac{-1}{\Lambda_{-}(\Lambda_{+} - \Lambda_{-})}\left[\xi + \eta e^{\frac{i(\arg(\epsilon_{e\mu}) + \partial)}{2}} - \Lambda_{+}\zeta\right] \\ \widetilde{X}_{2}^{\mu e} = \frac{1}{\Lambda_{+}\Lambda_{-}}\left[\xi + \eta e^{\frac{i(\arg(\epsilon_{e\mu}) + \partial)}{2}} - (\Lambda_{+} + \Lambda_{-})\zeta\right] \\ \widetilde{X}_{3}^{\mu e} = \frac{1}{\Lambda_{+}(\Lambda_{+} - \Lambda_{-})}\left[\xi + \eta e^{\frac{i(\arg(\epsilon_{e\mu}) + \partial)}{2}} - \Lambda_{-}\zeta\right] \\ \operatorname{Tan} \beta = \frac{|\epsilon_{e\tau}|}{1 + \epsilon_{ee}}\left[\epsilon_{\tau\tau} = \frac{|\epsilon_{e\tau}|^{2}}{1 + \epsilon_{ee}}\right] \frac{\theta_{13}^{\prime\prime\prime} = \sin^{-1}|e^{-i\arg(\epsilon_{e\mu})}U_{e3}\cos\beta + U_{\tau3}\sin\beta|}{e^{-i\arg(\epsilon_{e\mu})}U_{e3}\cos\beta + U_{\tau3}\sin\beta|}$$

Features of the probability (in the limit $\Delta m_{21}^2 \rightarrow 0$) A) It depends only on $\arg(\epsilon_{e\tau})+\delta$.

→ This is approximately the case also for $\Delta m_{21}^2 \neq 0$. B) Each term gives a large contribution (See Fig. below). → Interpretation of behavior of probability is difficult.



2.3 Implications of NP for ongoing experiments

MINOS (2005-)

Major channel is disappearance $(\nu_{\mu} \rightarrow \nu_{\mu})$ but appearance $(\nu_{\mu} \rightarrow \nu_{e})$ can be also measured

Baseline L=730km is larger than K2K, so matter effect at MINOS plays a more important role than at K2K





For some values of \mathcal{E}_{ee} , $\mathcal{E}_{e\tau}$, $\mathcal{E}_{\tau\tau} \sim O(1)$ within the allowed region, there is enhancement in the channel $v_{\mu} \rightarrow v_{e}$ which cannot be explained only by the standard oscillation scenario with θ_{13}



$\begin{array}{l} \textbf{MINOS} \\ \textbf{(1) In case MINOS observes } \nu_{e} \textbf{ events: If values of} \\ \varepsilon_{ee} \textbf{ and } \varepsilon_{e\tau} \textbf{ lie in the colored region, then} \\ \textbf{MINOS can verify existence of NP} \end{array}$

region where MINOS can prove (ε_{ee} , $\varepsilon_{e\tau}$) \neq (0,0) for each θ_{13}



In these cases, number of appearance events becomes so large (> 70) that it cannot be explained only by θ_{13} which would yield (<50 events)



3. Summary

- New Physics in V oscillation (during propagation) was discussed in the case where the ε_{αβ} parameters are of O(1). This kind of search of New Physics is complementary to those at LHC and ILC.
- The analytical formula was obtained for $P(v_{\mu} \rightarrow v_{e})$ in the presence of NP (in propagation) in the limit $\Delta m_{21}^{2} \rightarrow 0$.
- At ongoing MINOS, if values of ε_{ee} and ε_{eτ} lie in a certain region, then MINOS can verify existence of NP. If no ν_e events are observed at MINOS, then a constraint is slightly improved in the (ε_{ee}, | ε_{eτ} |) plane.
 Many more works yet have to be done (analysis for future intense LBL; global analysis of NP in production, propagation, detection, etc.)