

# Search for sterile neutrinos at reactors

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- 1. Introduction**
- 2. Sterile neutrino oscillations at reactors**
- 3. Summary**

**Based on OY, arXiv:1107.4766 [hep-ph]**

# 1. Introduction

## 1.1 $\nu$ oscillation

### Mass eigenstates

$$i \frac{d}{dt} \begin{pmatrix} \mathbf{v}_1 \\ \mathbf{v}_2 \end{pmatrix} = \begin{pmatrix} E_1 & 0 \\ 0 & E_2 \end{pmatrix} \begin{pmatrix} \mathbf{v}_1 \\ \mathbf{v}_2 \end{pmatrix}$$

$$E_j \equiv \sqrt{\vec{p}^2 + m_j^2}$$

### Flavor eigenstates

$$\begin{pmatrix} \mathbf{v}_\mu \\ \mathbf{v}_\tau \end{pmatrix} = U \begin{pmatrix} \mathbf{v}_1 \\ \mathbf{v}_2 \end{pmatrix}$$

$$U \equiv \begin{pmatrix} U_{\mu 1} & U_{\mu 2} \\ U_{\tau 1} & U_{\tau 2} \end{pmatrix}$$

### Probability of flavor conversion

$$P(\mathbf{v}_\mu \rightarrow \mathbf{v}_\tau) = \sin^2 2\theta \sin^2 \left( \frac{\Delta E L}{2} \right)$$

$$\Delta E = E_2 - E_1 \approx \frac{m_2^2 - m_1^2}{2E} = \frac{\Delta m^2}{2E}$$

## 1.2 Framework of 3 flavor $\nu$ oscillation

**Mixing matrix**

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

Functions of mixing angles  $\theta_{12}$ ,  $\theta_{23}$ ,  $\theta_{13}$ , and CP phase  $\delta$

## 1.3 Information we have obtained so far

$\nu_{\text{solar}}$  + KamLAND (reactor)



$$\theta_{12} \cong \frac{\pi}{6}, \Delta m_{21}^2 \cong 8 \times 10^{-5} \text{ eV}^2$$

$\nu_{\text{atm}}$  + K2K, MINOS (accelerators)



$$\theta_{23} \cong \frac{\pi}{4}, |\Delta m_{32}^2| \cong 2.5 \times 10^{-3} \text{ eV}^2$$

CHOOZ (reactor)  
+ T2K + MINOS + others



$$\theta_{13} \cong 0.14^{+0.02}_{-0.03}$$

# 1.4 Beyond the three flavor scenario

## ● accelerator $\nu$ anomaly LSND (1993-98, LANL)

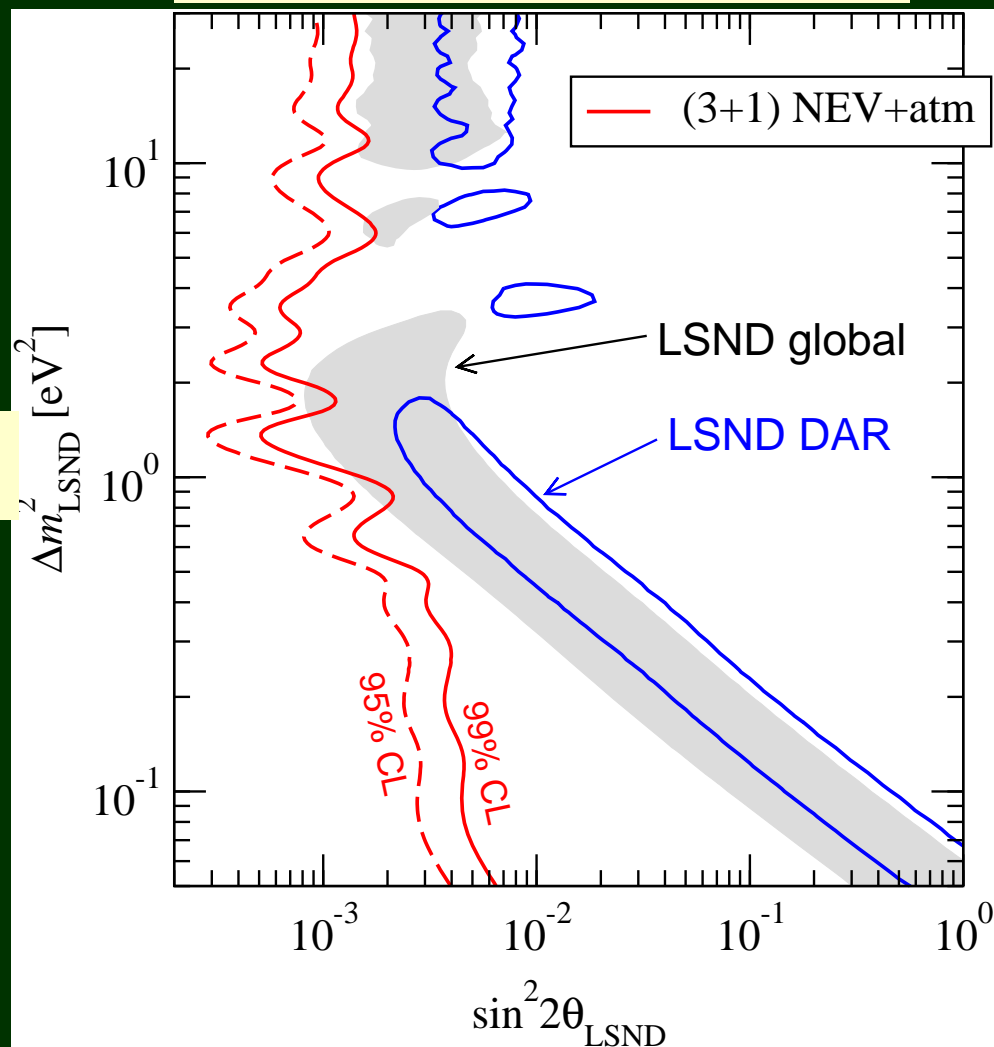
$$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$$

$$E_\nu \cong 50 \text{ MeV}$$

$$L \cong 30 \text{ m}$$

$$\Delta m^2 \cong \mathcal{O}(1) \text{ eV}^2$$
$$\sin^2 2\theta \cong \mathcal{O}(10^{-2})$$

Maltoni et al., hep-ph/0405172



# ● MiniBooNE (2002-, FNAL)

$E \sim 1\text{GeV}, L \sim 1\text{km},$

$(L/E)_{\text{MB}} = (L/E)_{\text{LSND}}$

The purpose of MB: to check LSND

In both cases, depending on energy ( $E > 475\text{ MeV}$  or  $E > 200\text{ MeV}$ ), the conclusion changes

$\nu$  mode (negative)

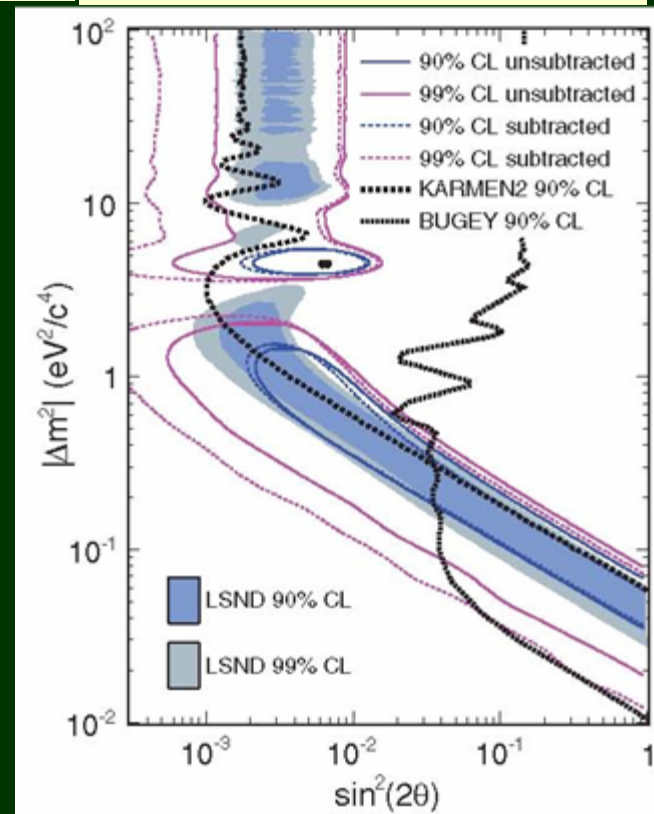
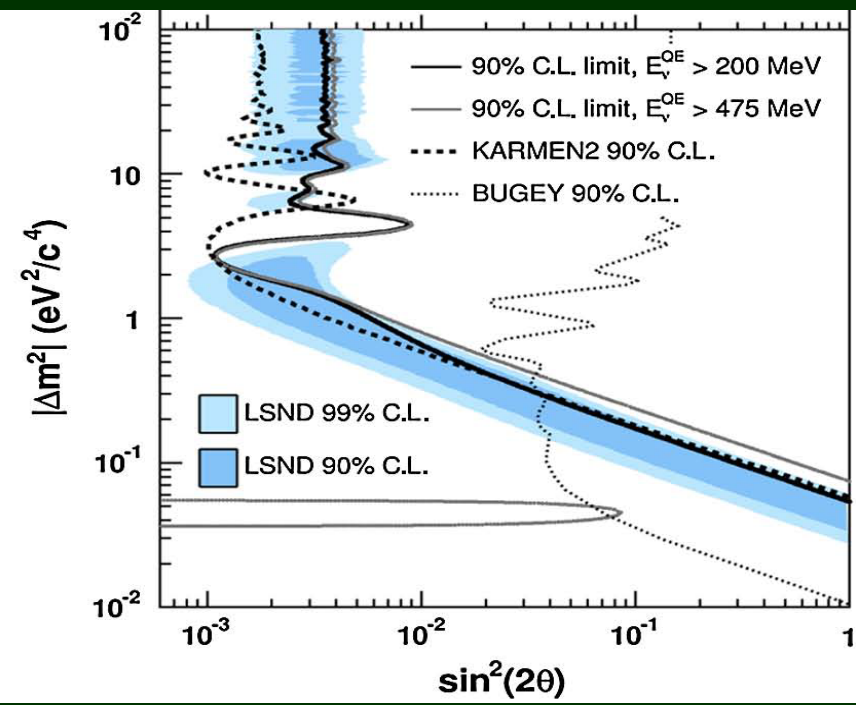
anti- $\nu$  mode (affirmative; No. of events is small)

$\nu_{\mu} \rightarrow \nu_e$

Aguilar-Arevalo et al., PRL 103, 111801 (2009)

$\bar{\nu}_{\mu} \rightarrow \bar{\nu}_e$

Aguilar-Arevalo et al., PRL 105, 181801 (2010)



# MiniBooNE's summary



The data is  
still  
confusing

R. Van der Water@Neutrino2010

mode	E<475MeV	E>475MeV
$\nu_{\mu} \rightarrow \nu_e$	An unexplained <b>3<math>\sigma</math> electron excess</b>	<b>Inconsistent w/ LSND @ 90%CL</b>
$\bar{\nu}_{\mu} \rightarrow \bar{\nu}_e$	A small <b>1.3<math>\sigma</math> electron excess</b>	<b>Consistent w/ LSND @ 99.4%CL</b>

## 1.5 $N_\nu=4$ schemes

Because of the hierarchy:  $\Delta m_{\text{sol}}^2 \ll \Delta m_{\text{atm}}^2 \ll \Delta m_{\text{LSND}}^2$

$N_\nu=3$  schemes can't explain LSND.

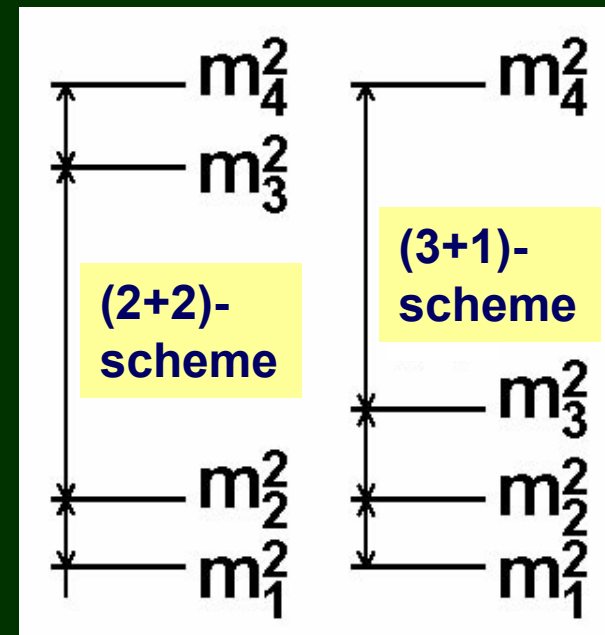
$N_\nu=4$  schemes may be able to explain all.

$$\Delta m_{21}^2 = \Delta m_{\text{sol}}^2, \Delta m_{32}^2 = \Delta m_{\text{atm}}^2, \Delta m_{43}^2 = \Delta m_{\text{LSND}}^2$$

LEP  $\rightarrow$  4<sup>th</sup>  $\nu$  has to be sterile

(2+2)-scheme is excluded by solar + atmospheric  $\nu$

$\rightarrow$  (3+1)-scheme will be discussed





# (3+1)-scheme

$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) = 1 - 4|U_{e4}|^2(1 - |U_{e4}|^2) \sin^2(\Delta m_{41}^2 L/4E)$$

$$P(\nu_\mu \rightarrow \nu_\mu) = 1 - 4|U_{\mu4}|^2(1 - |U_{\mu4}|^2) \sin^2(\Delta m_{41}^2 L/4E)$$

$$P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) = 4|U_{e4}|^2|U_{\mu4}|^2 \sin^2(\Delta m_{41}^2 L/4E)$$

$$\sin^2 2\theta_{\text{Bugey}} > 4|U_{e4}|^2(1 - |U_{e4}|^2) \cong 4|U_{e4}|^2$$

$$\sin^2 2\theta_{\text{CDHSW}} > 4|U_{\mu4}|^2(1 - |U_{\mu4}|^2) \cong 4|U_{\mu4}|^2$$

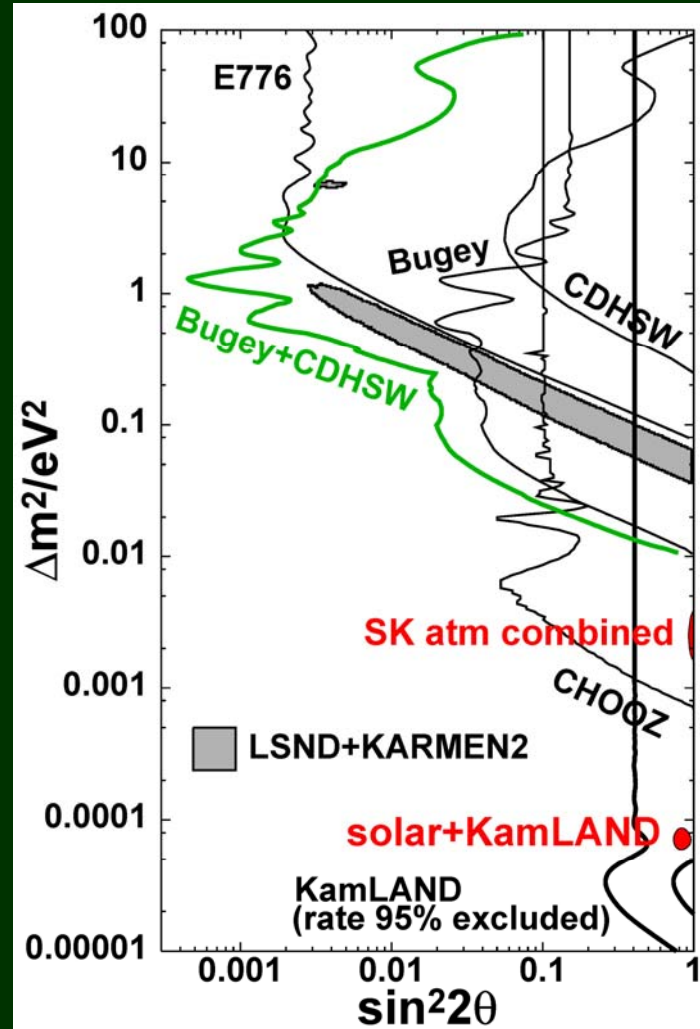
$$\sin^2 2\theta_{\text{LSND}} = 4|U_{e4}|^2|U_{\mu4}|^2$$

$U_{\alpha 4}$  : an element of 4x4 mixing matrix

$$\sin^2 2\theta_{\text{LSND}}(\Delta m^2) < \frac{1}{4} \sin^2 2\theta_{\text{Bugey}}(\Delta m^2) \sin^2 2\theta_{\text{CDHSW}}(\Delta m^2)$$

**must be satisfied** (Okada-OY,'97; Bilenky-Giunti-Grimus, '98)

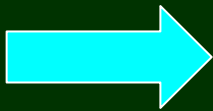
But there is no overlap between LSND and left side of Bugey+CDHSW



## 1.6 Reactor Anti-neutrino Anomaly

New prediction of the reactor  $\nu$  flux

T. A. Mueller et al., PRC83, 054615 (2011)



About +3% normalization shift  
with respect to old  $\nu$  spectrum

19 Experimental Results ( $L < 100\text{m}$ ) reexamined  
(ILL, Goesgen, Rovno, Krasnoyarsk, Bugey,  
Savannah River)

G. Mention et al, PRD83, 073006 (2011)

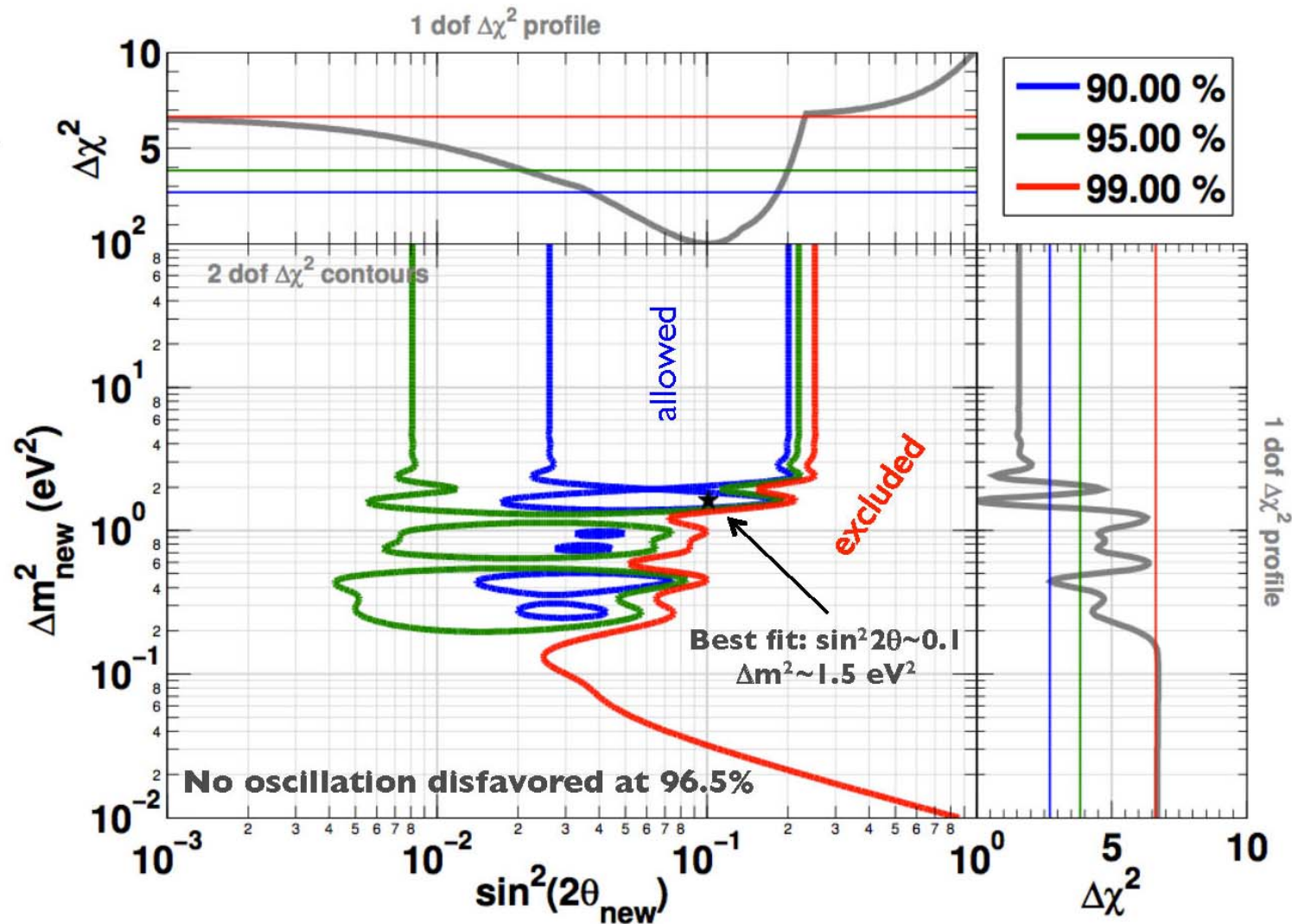


An affirmative result for  $\nu$   
oscillation at  $\Delta m^2 > 1\text{eV}^2$

# Allowed region with the new $\nu$ flux prediction

G. Mention et al, PRD83, 073006 (2011)

## Combined Reactor Rate+Shape contours



# New prediction of the reactor $\nu$ flux

→ (3+1)-scheme may fit to the data (LSND+MB+other short baseline expts.) better with new flux than before (with old flux).

→ It is important to confirm sterile  $\nu$  oscillations

- A ten kilocurie scale anti- $\nu$  source ( $^{144}\text{Ce}$ ,  $^{106}\text{Ru}$ )  $\bar{\nu}_e \rightarrow \bar{\nu}_e$   
M. Cribier et al., arXiv:1107.2335

- A proposal for a  $\beta$ -beam  $\nu_e \rightarrow \nu_e$

Agarwalla-Huber-Link, JHEP 1001:071,2010

- $\nu$  oscillation experiments at a reactor with a small core → Present work arXiv:1107.4766 [hep-ph]

$$\bar{\nu}_e \rightarrow \bar{\nu}_e$$

# 1.7 Thermal Neutron Reactors vs Fast Neutron Reactors

Fuels must be distant  $\Rightarrow$  the volume must be larger

	Kinetic energy of neutron	Moderator	Coolant	Power density
Thermal Neutron Reactor (w/ H <sub>2</sub> O)	~0.02eV	H <sub>2</sub> O	H <sub>2</sub> O	~O(10MW/m <sup>3</sup> )
Fast Neutron Reactor	~2MeV	None	Na	~O(100MW/m <sup>3</sup> )

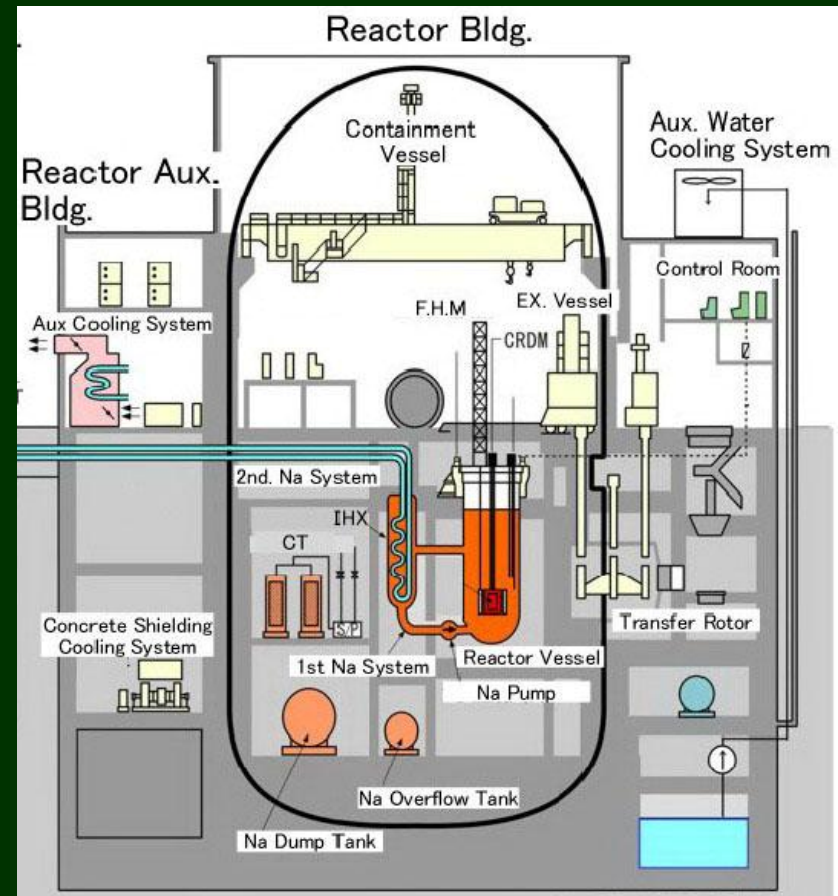
Fuels can be closer  $\Rightarrow$  the volume can be smaller

# Joyo Fast Research Reactor



Oarai,  
Ibaraki

Operated by JAEA  
 $P_{th} = 140\text{MW}$   
Frequent On/Off



## 2. Analysis of a reactor neutrino oscillation experiment with one reactor & two detectors

$$\chi^2 = \min_{\alpha's} \left\{ \sum_{A=N,F} \sum_{i=1}^n \frac{1}{(t_i^A \sigma_i^A)^2} [m_i^A - t_i^A(1 + \alpha + \alpha^A + \alpha_i) - \alpha_{\text{cal}}^A t_i^A v_i^A]^2 + \sum_{A=N,F} \left[ \left( \frac{\alpha^A}{\sigma_{\text{dB}}} \right)^2 + \left( \frac{\alpha_{\text{cal}}^A}{\sigma_{\text{cal}}} \right)^2 \right] + \sum_{i=1}^n \left( \frac{\alpha_i}{\sigma_{\text{Db}}} \right)^2 + \left( \frac{\alpha}{\sigma_{\text{DB}}} \right)^2 \right\}.$$

n=#(bin)=32

OY, arXiv:  
1107.4766  
[hep-ph]

$m_i^A$ : Measured numbers of events

$t_i^A$ : Theoretical prediction

$v_i^A$ : Variation due to energy calibration error

$$(t_i^A \sigma_i^A)^2 = \boxed{t_i^A} + \boxed{(t_i^A \sigma_{\text{db}}^A)^2}$$

statistical errors

systematic errors

In the present case  $\sigma_{\text{stat}} > \sigma_{\text{sys}}$ :  
statistical errors are more important



A=N:  
“near”  
detector

D<sub>1</sub>

—  
ν<sub>e</sub>

A=F: “far”  
detector

D<sub>2</sub>

## Assumed systematic errors

$\sigma_{\text{DB}}$ : correlated wrt detectors, correlated wrt bins = **3%**

$\sigma_{\text{Db}}$ : correlated wrt detectors, uncorrelated wrt bins = **2%**

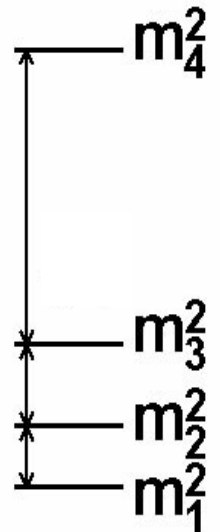
$\sigma_{\text{dB}}$ : uncorrelated wrt detectors, correlated wrt bins = **0.5%**

$\sigma_{\text{db}}$ : uncorrelated wrt detectors, uncorrelated wrt bins = **0.5%**

$\sigma_{\text{cal}}$ : energy calibration error for each bin = **0.6%**

## Formula for oscillation probability

$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) = 1 - \sin^2 2\theta_{14} \sin^2 \left( \frac{\Delta m_{41}^2 L}{4E} \right)$$



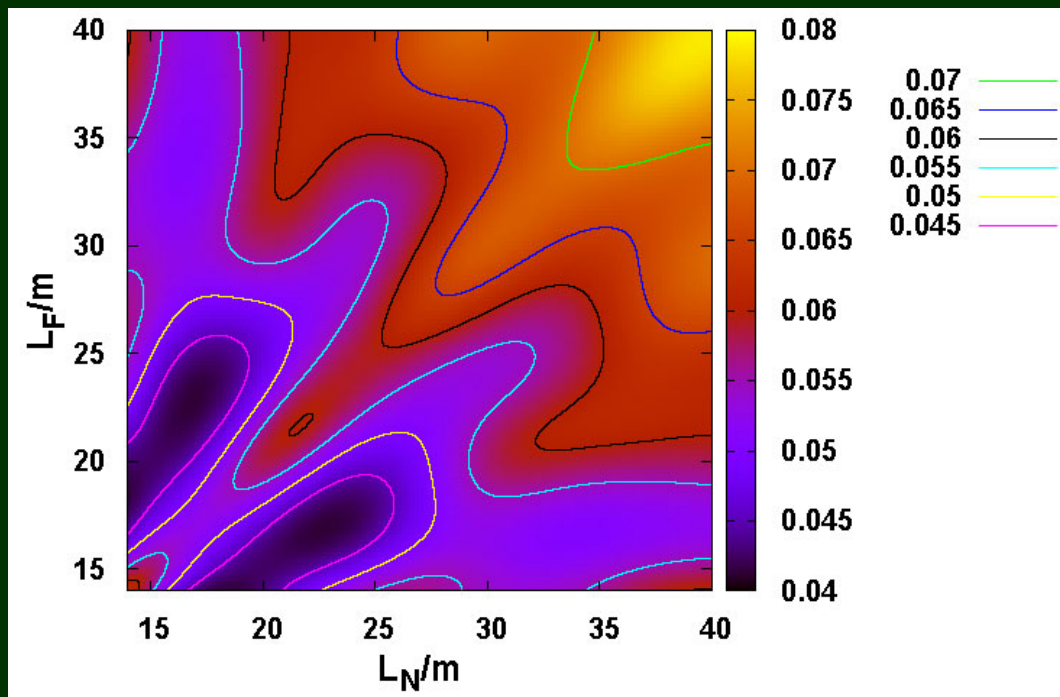


# (1) Conventional reactors (thermal neutron reactors)

## Assumed parameters (a la Bugey)

- Power: 2.8 GW
- Size of the core: Diameter=4m, Height=4m

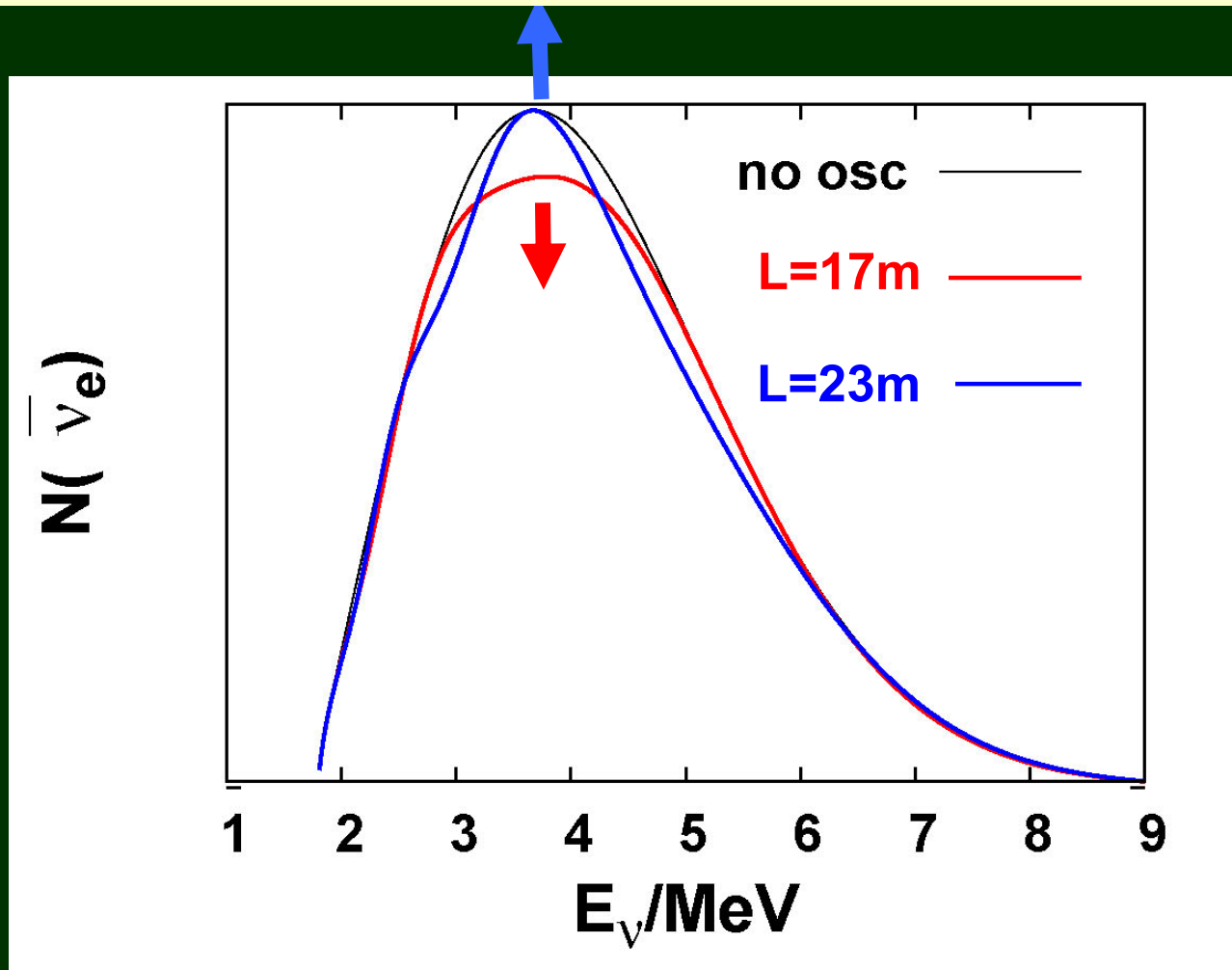
## Optimization w.r.t. baseline lengths $L_N$ , $L_F$ for $\Delta m^2=1\text{eV}^2$



**Optimized  
baseline  
lengths:  
 $L_N=17\text{m}$ ,  
 $L_F=23\text{m}$**

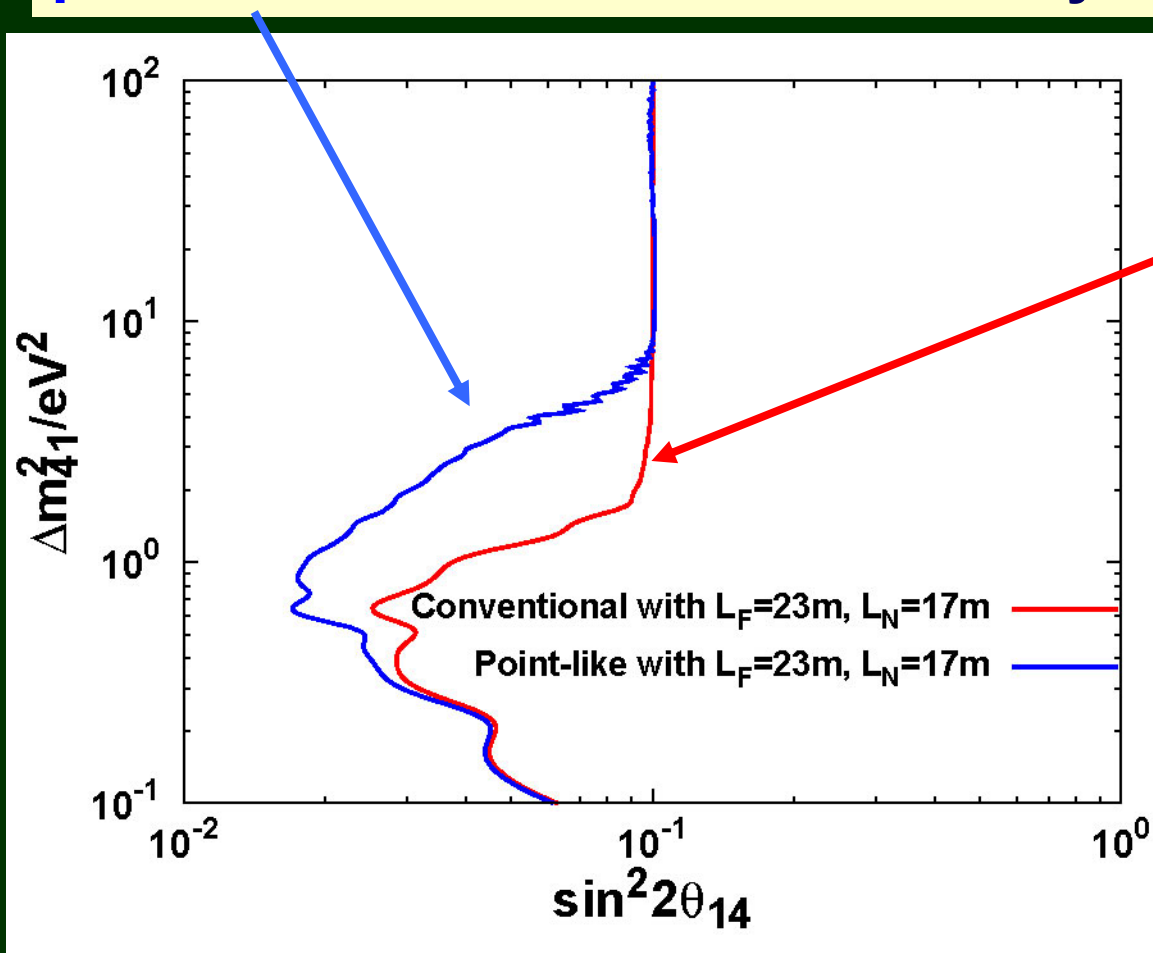
# The role of a “near” detector in the energy spectrum analysis for $\Delta m^2=1\text{eV}^2$

The difference at  $\langle E \rangle \sim 4\text{MeV}$  is most significant for  $L_N=17\text{m}$   $L_F=23\text{m}$



# Sensitivity of Conventional reactors to $\sin^2 2\theta_{14}$ at $L_N=17\text{m}$ $L_F=23\text{m}$

The case of a hypothetical reactor with a **point-like core**  $\rightarrow$  better sensitivity



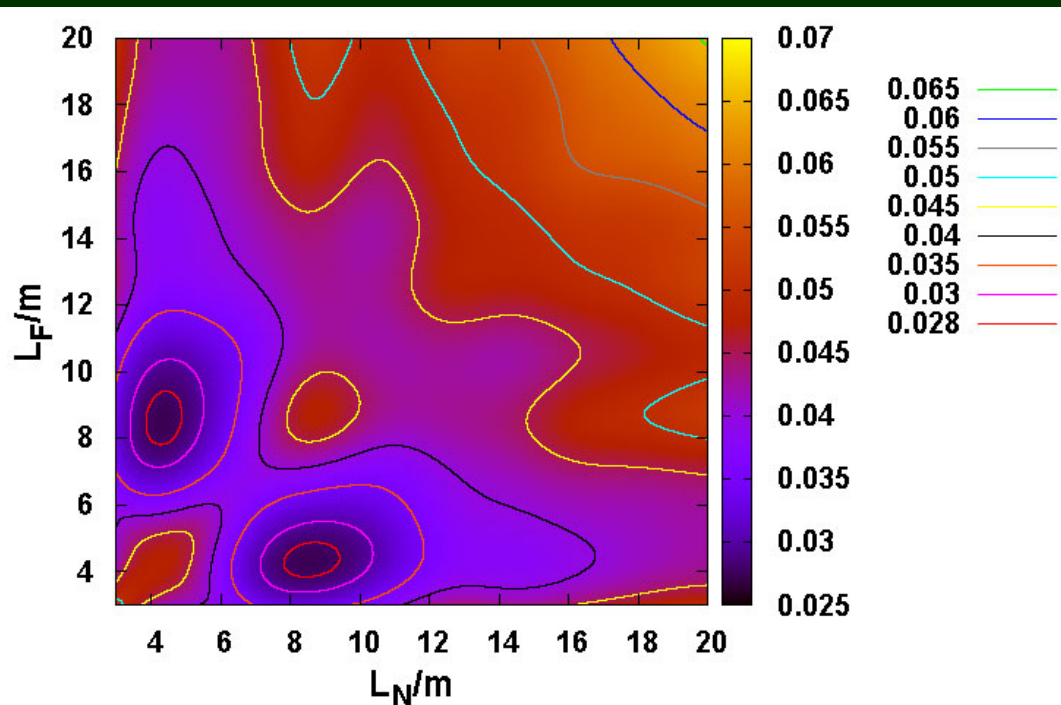
**Finite size effect**  
of a core  $\rightarrow$  poor  
sensitivity for  
 $\Delta m^2 \sim 2\text{eV}^2$

## (2) A fast neutron reactor

### Assumed parameters

- Power: 0.14 GW
- Size of the core: Diameter=0.8m, Height=0.5m

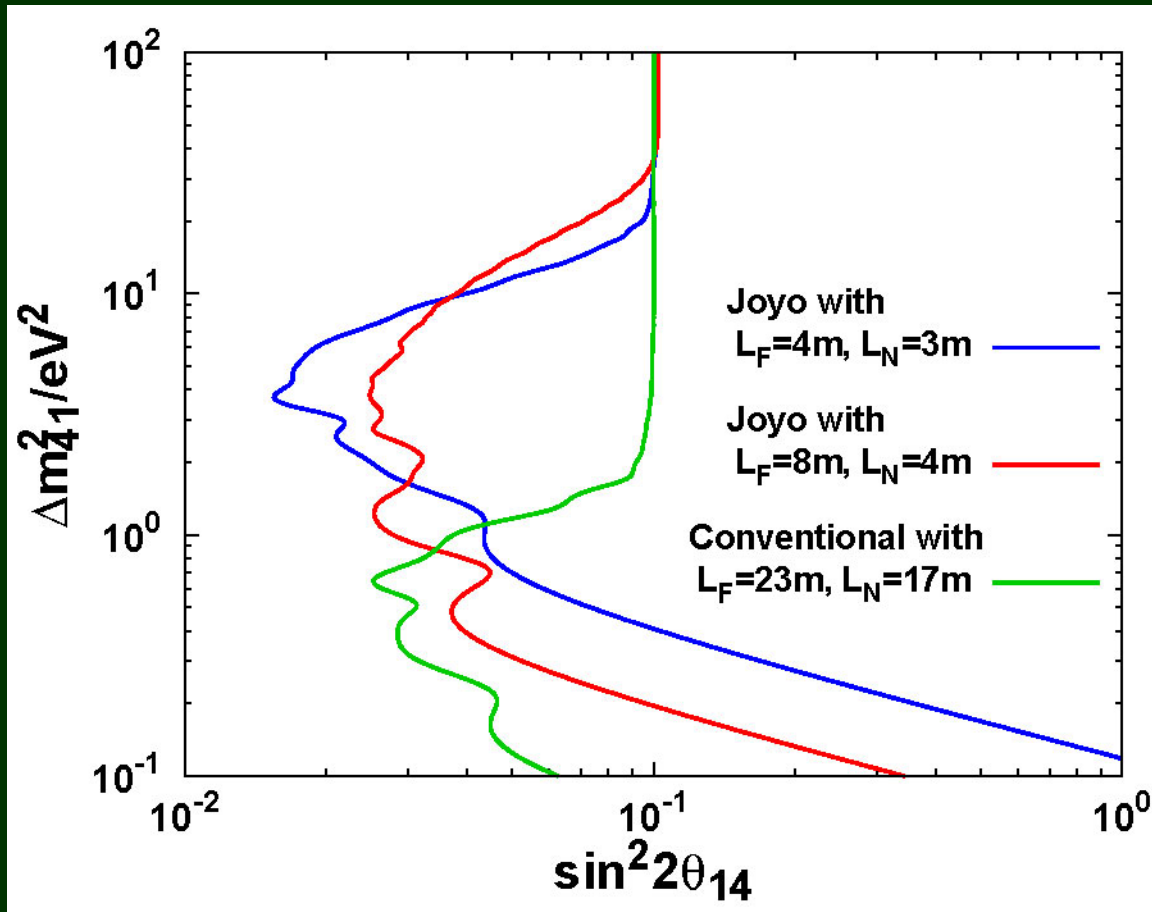
Optimization w.r.t. baseline lengths  $L_N$ ,  $L_F$  for  $\Delta m^2=1\text{eV}^2$



**Optimized  
baseline  
lengths:  
 $L_N=4\text{m}$   
 $L_F=8\text{m}$**

## Sensitivity of Joyo to $\sin^2 2\theta_{14}$ at $L_N=4\text{m}$ , $L_F=8\text{m}$

- Less power is compensated by closer distance
- A reactor with a small core prevents smearing effect



# A Study of Reactor $\nu$ Monitoring at Experimental Fast Reactor JOYO

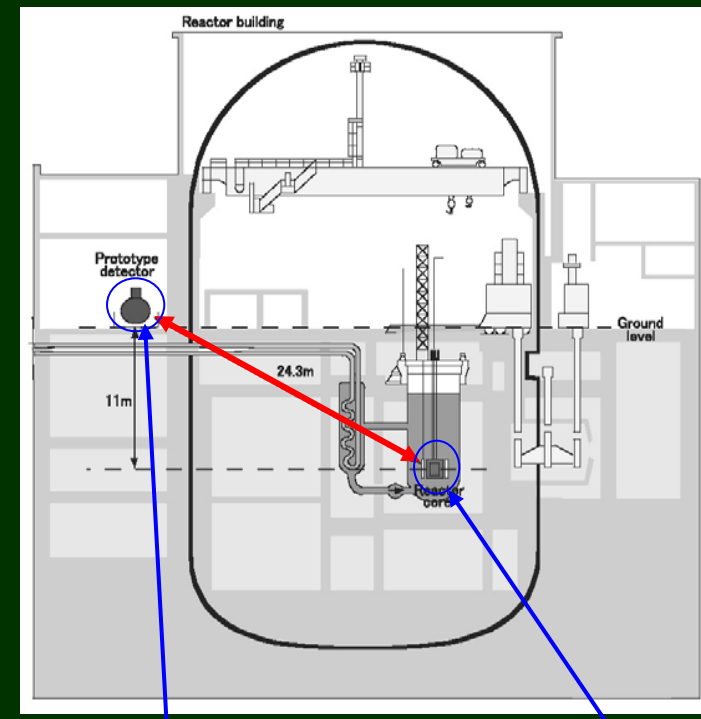
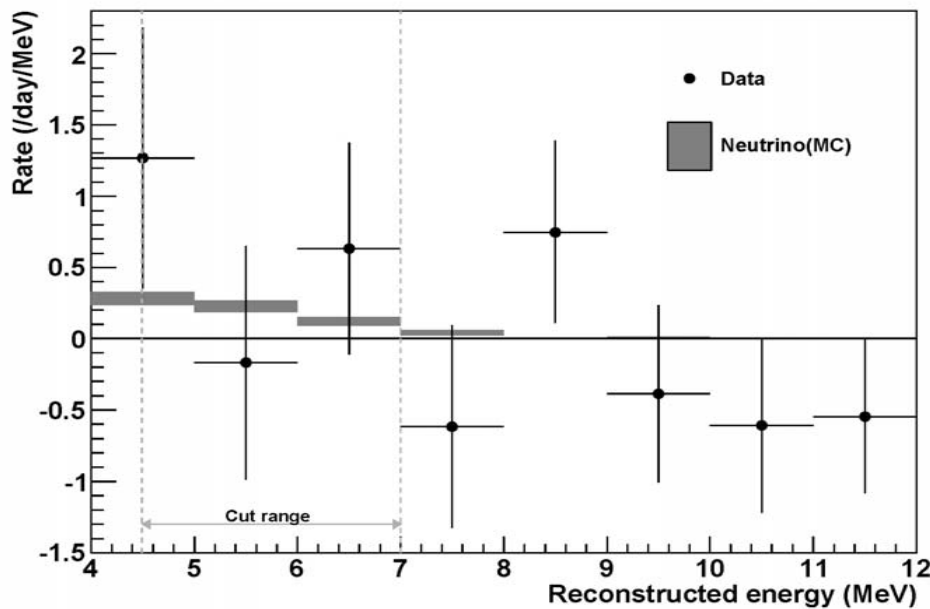
H.Furuta et al., arXiv:1108.2910v1 [hep-ex]

$L=24.3\text{m}$ ; about 150  $\nu p \rightarrow e^+n$  reactions/day

The measured  $\nu$  event rate from reactor on-off comparison was  $1.11 \pm 1.24(\text{stat.}) \pm 0.46(\text{syst.})$  events/day.

The statistical significance of the measurement was not enough.

Their motivation: to detect  $\nu$  from a fast reactor (not motivated by  $\nu_s$ )



Prototype detector

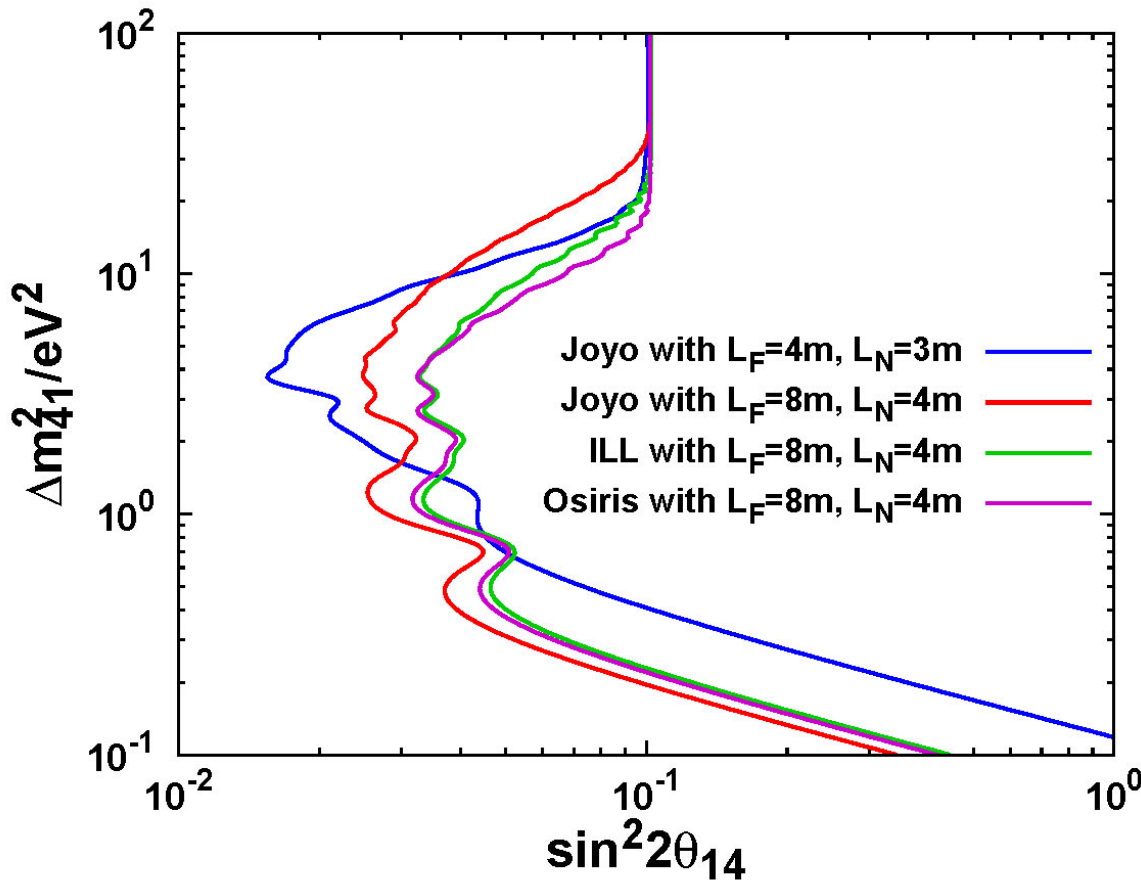
Reactor core

### 3. Summary (1)

- Because of the recent re-evaluation of the reactor  $\nu$  flux, scenarios of sterile  $\nu$  oscillations with  $\Delta m^2 \sim O(1\text{eV}^2)$  are reviving.
- To get a useful information from the spectrum analysis of reactor  $\nu$  for  $\Delta m^2 > 1\text{eV}^2$ , a reactor with a small core is necessary to avoid the smearing effect.
- Fast neutron reactors have a small core in general, and measurements of  $\nu$  from a fast neutron reactor Joyo may be able to offer a test of LSND/MiniBooNE.
- A preliminary experiment to measure  $\nu$  from Joyo has been performed, but not sufficient significance of the signals was obtained. → More developments are needed.

### 3. Summary (2)

- There exist in France a couple of experimental thermal neutron reactors with a small core. → **Nucifer project**



**ILL** (Institut Laue-Langevin near Grenoble) research reactor

Power=58 MW,  
Diameter=40cm,  
Height=80cm

**Osiris** (in the French Atomic Energy Commission (CEA) centre at Saclay)

Power=70 MW,  
Size=57cmx57cmx60cm

Great if the detectors are placed very closed to a reactor!



**Backup slides**

# (2+2)-scheme

$$\eta_s \equiv |\mathbf{U}_{s1}|^2 + |\mathbf{U}_{s2}|^2 \rightarrow \mathbf{0}$$

$$\mathbf{v}_{\text{atm}} : \mathbf{v}_\mu \rightarrow \mathbf{v}_s \text{ (100\%)}$$

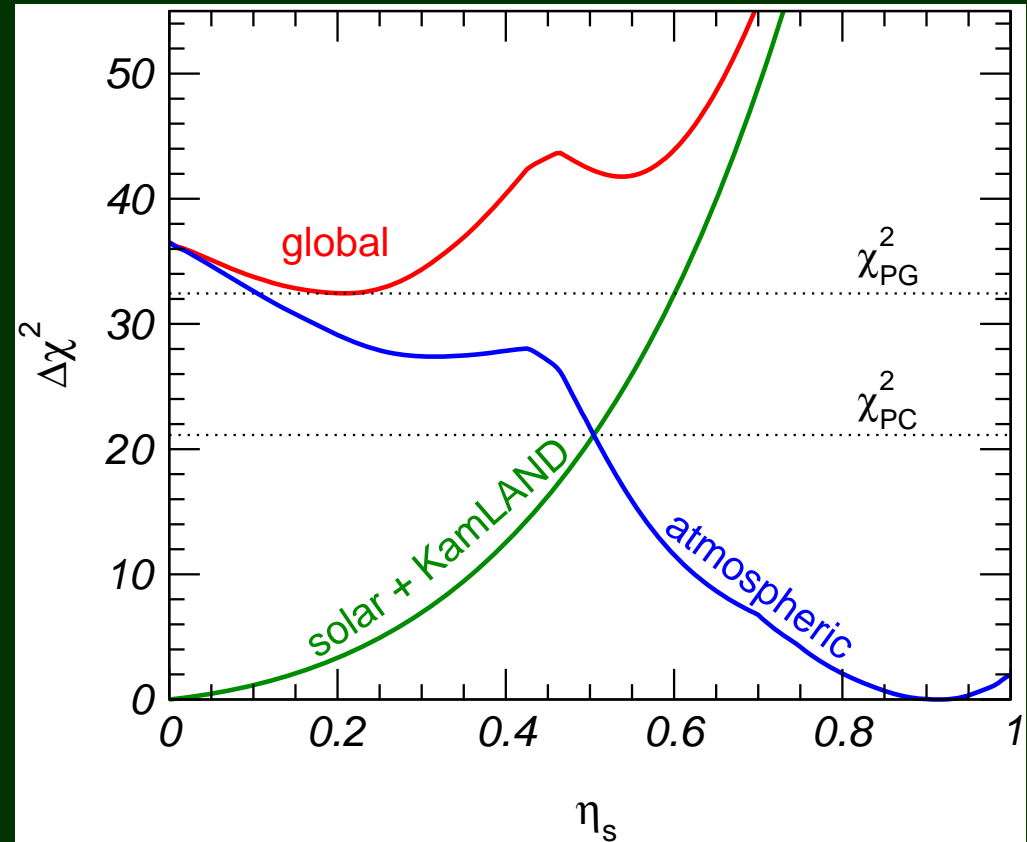
Strongly disfavored by  
SK  $\nu_{\text{atm}}$  data

$$\eta_s \equiv |\mathbf{U}_{s1}|^2 + |\mathbf{U}_{s2}|^2 \rightarrow \mathbf{1}$$

$$\mathbf{v}_{\text{sol}} : \mathbf{v}_e \rightarrow \mathbf{v}_s \text{ (100\%)}$$

Strongly disfavored by  
SNO  $\nu_{\text{sol}}$  data

Maltoni et al., hep-ph/0405172



PC: parameter consistency test  
PG: parameter goodness-of-fit test

For any value of  $|\mathbf{U}_{s1}|^2 + |\mathbf{U}_{s2}|^2$ , fit to sol+atm data is bad.

# (3+2)-scheme

LSND( $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ ): affirmative  
 MiniBOONE( $\nu_\mu \rightarrow \nu_e$ ): negative

**difference between  $\nu$  & anti- $\nu$  may offer a promising fit**

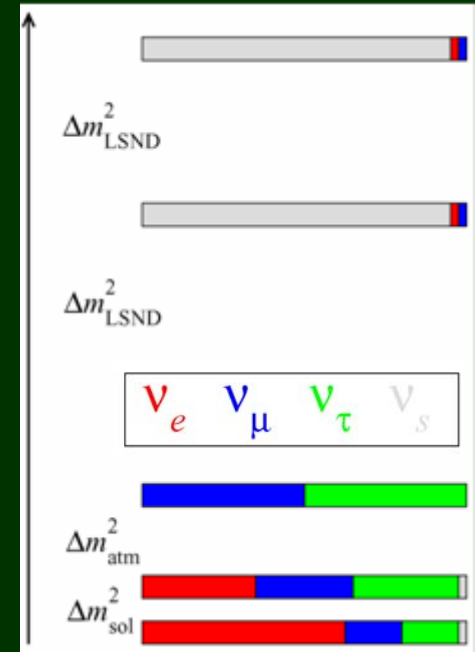
## (3+2)-scheme w/ CP phase $\delta$

$$\begin{aligned}
 P_{\nu_\mu \rightarrow \nu_e} &= 4 |U_{e4}|^2 |U_{\mu4}|^2 \sin^2 \phi_{41} \\
 &+ 4 |U_{e5}|^2 |U_{\mu5}|^2 \sin^2 \phi_{51} \\
 &+ 8 |U_{e4} U_{\mu4} U_{e5} U_{\mu5}| \sin \phi_{41} \sin \phi_{51} \cos(\phi_{54} - \delta)
 \end{aligned}$$

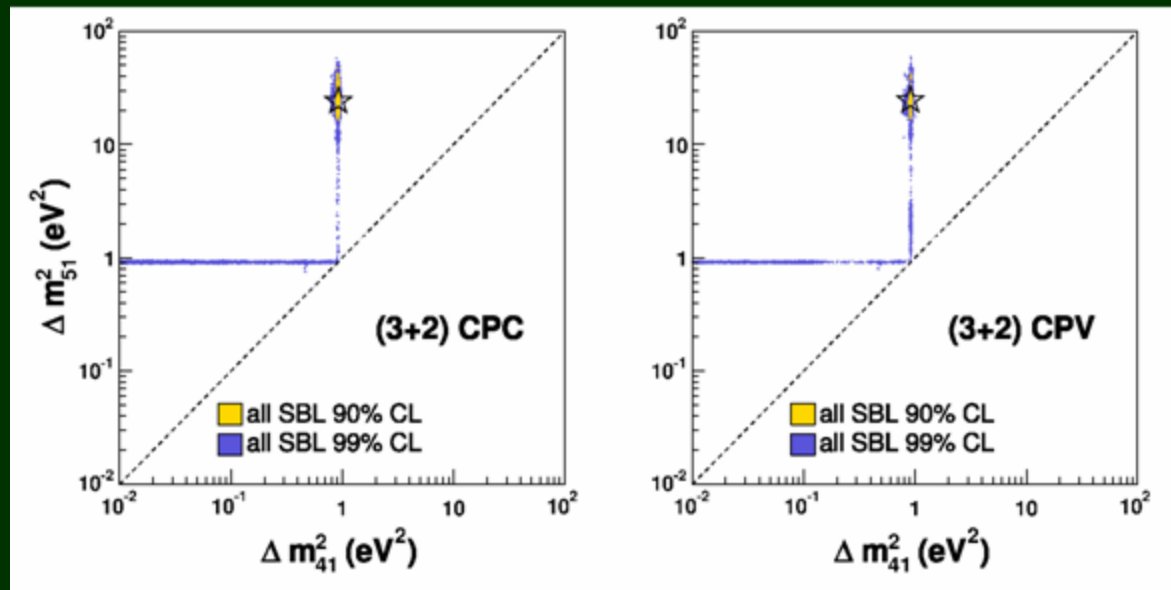
with the definitions

$$\phi_{ij} \equiv \frac{\Delta m_{ij}^2 L}{4E},$$

$$\delta \equiv \arg(U_{e4}^* U_{\mu4} U_{e5} U_{\mu5}^*)$$



**(3+2)-scheme  
gives slightly  
better fit than  
(3+1) between  
MB & LSND**



Data Sets	PG (%)
APP vs. DIS	0.26
APP (no BNB-MB( $\nu$ )) vs. DIS (no CDHS + ATM)	36.4
APP (no BNB-MB( $\nu$ )) vs. DIS (no CDHS)	0.58
APP (no BNB-MB( $\nu$ )) vs. DIS (no ATM)	0.82
APP (no BNB-MB( $\nu$ )) vs. DIS	0.10
APP vs. DIS (no CDHS + ATM)	15.7
APP vs. DIS (no CDHS)	0.76
APP vs. DIS (no ATM)	1.4

TABLE VII: Comparison of compatibility between appearance (APP) and disappearance (DIS) experiments, within a (3+2) CP-violating scenario. The BNB-MB( $\nu$ ) data set, CDHS data set, and atmospheric constraints (ATM) are removed from the fits as specified in order to establish the source of tension between appearance and disappearance experiments. See text for more details.

**Karagiorgi, Djurcic, Conrad, Shaevitz,  
Sorel, Phys.Rev.D80:073001,2009.**

**But tension also  
exists between (3+2)-  
scheme and  
disappearance data**

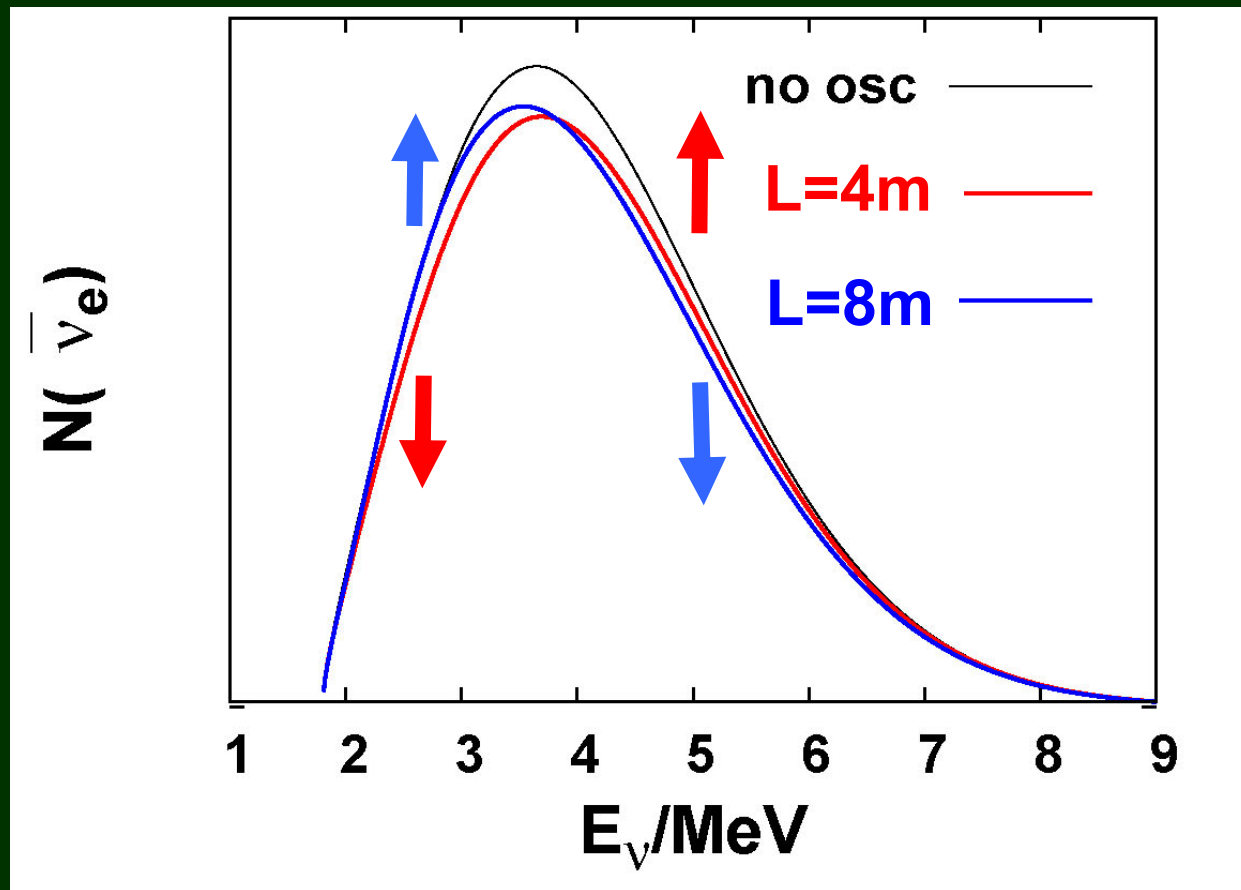
$$v_i^A = \lim_{\alpha_{\text{cal}}^A \rightarrow 0} \frac{1}{\alpha_{\text{cal}}^A t_i^A} \left[ \frac{N_p T}{4\pi L_A^2} \int dE \int_{(1+\alpha_{\text{cal}}^A)E_i}^{(1+\alpha_{\text{cal}}^A)E_{i+1}} dE' R(E_e, E') \epsilon(E) F(E) \sigma(E) - t_i^A \right]$$

$$t_i^A \equiv \frac{N_p T}{4\pi L_A^2} \int dE \int_{E_i}^{E_{i+1}} dE' R(E_e, E') \epsilon(E) F(E) \sigma(E)$$

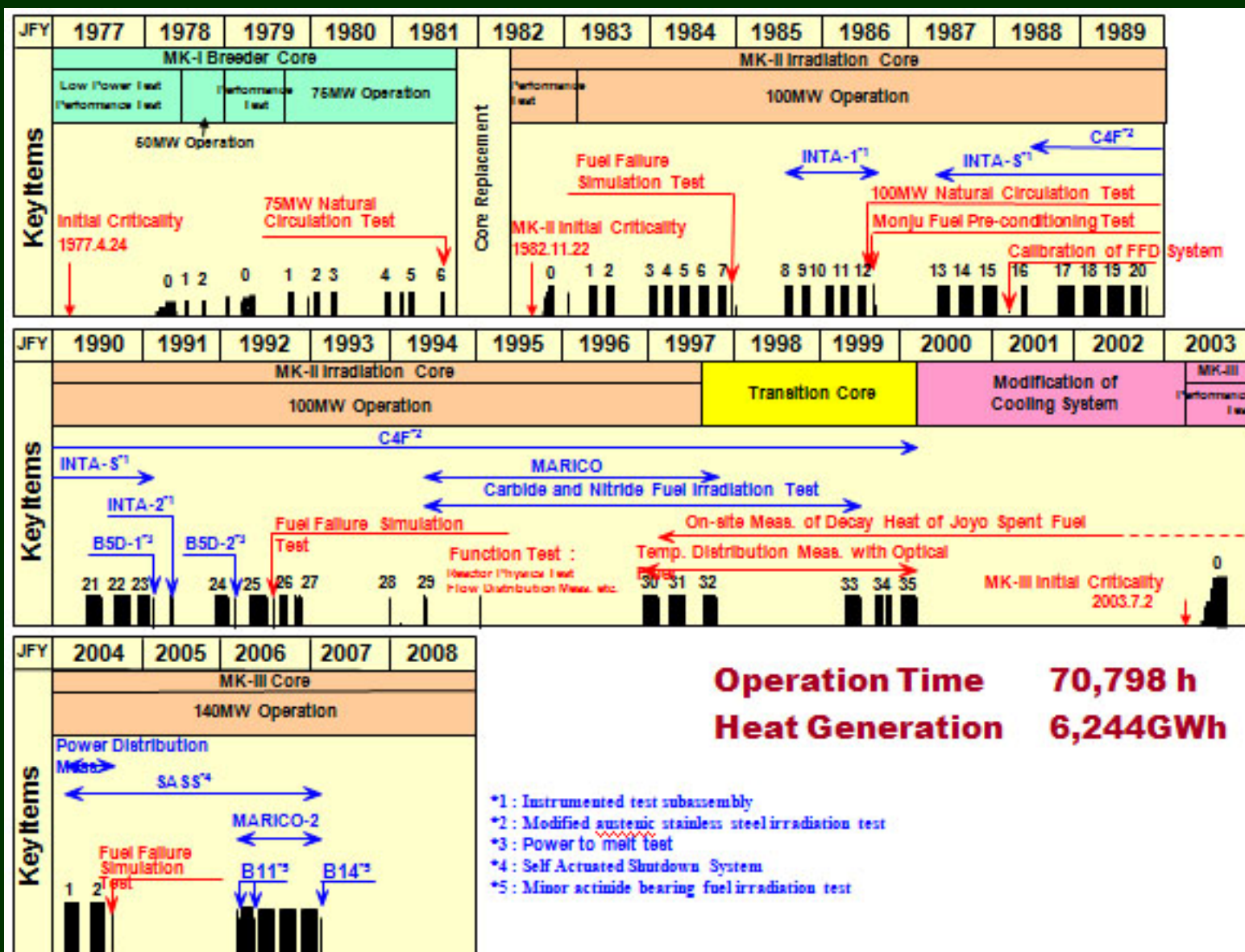
In Eqs. (4) and (5),  $N_p$  is the number of target protons in the detector,  $T$  denotes the exposure time,  $L_A$  is the baseline for the detector  $A$ ,  $F(E)$  is the flux of  $\bar{\nu}_e$ , and  $\sigma(E)$  is the cross section of the inverse  $\beta$  decay  $\bar{\nu}_e + p \rightarrow n + e^+$ .  $E$  is the energy of the incident  $\bar{\nu}_e$  and it is related to the positron energy  $E_e$  and the masses  $m_n$ ,  $m_p$  of a neutron and a proton by  $E = E_e + m_n - m_p = E_e + 1.3$  MeV.  $E'$  is the measured positron energy and we will assume that the energy resolution is given by  $8\%/\sqrt{E}$ , i.e.,  $R(E_e, E') = R(E - m_n + m_p, E')$  is a Gaussian function which describes the energy resolution and is given by  $R(E_e, E') = (1/\sqrt{2\pi}\sigma) \exp[-(E_e - E')^2/2\sigma^2]$ , where  $\sigma = 0.08\sqrt{(E_e + m_e)/\text{MeV}} = 0.08\sqrt{(E - 0.8/\text{MeV})/\text{MeV}}$ . Our strategy is to *assume no*

# The role of a “near” detector in the energy spectrum analysis for $\Delta m^2=1\text{eV}^2$

Asymmetry at  $\langle E \rangle \sim (4 \mp 1)\text{MeV}$  is most significant for  $L_N=4\text{m}$   $L_F=8\text{m}$



# Operation history of Joyo



# How to measure Pu/U ratio by $\nu$

(simplified discussion)

$$\begin{cases} P_{th} = q(n_U + n_{Pu}) \\ N_{\nu} = an_U + bn_{Pu} \end{cases}$$

$$\rightarrow \frac{n_{Pu}}{n_U} = \frac{1 - ar}{br - 1}; \quad r = \frac{P_{th}}{qN_{\nu}}$$

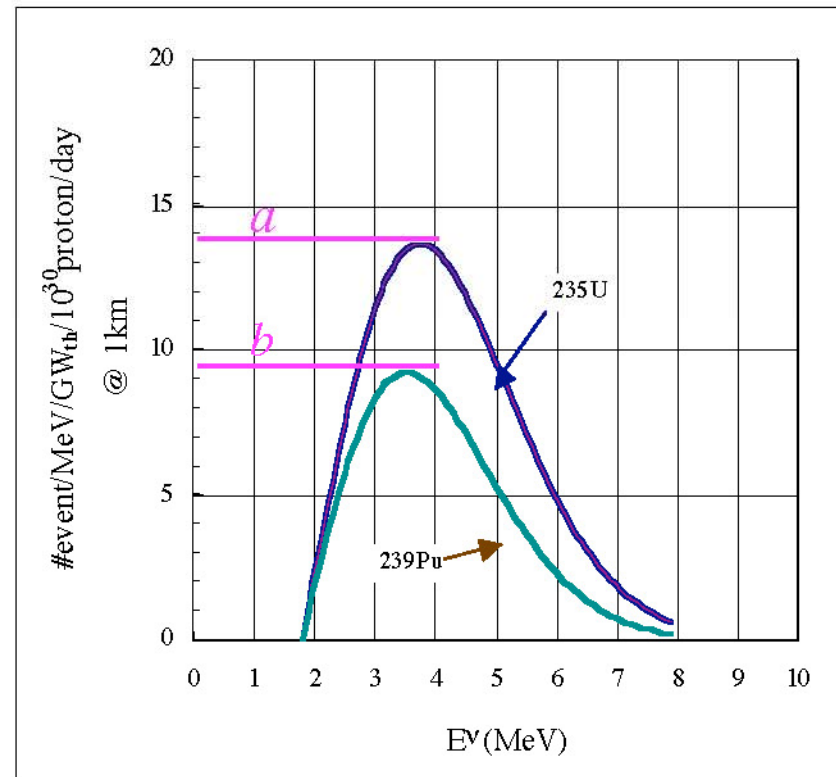
$n_U, n_{Pu}$ : Fission rate of U and Pu

$q$ : Energy release per fission  
(~200MeV)

$P_{th}$ : Thermal power

$N_{\nu}$ : # of  $\nu$

$a, b$ : # of  $\nu$  generation per U, Pu fission  
( $a/b \sim 1.5$ )

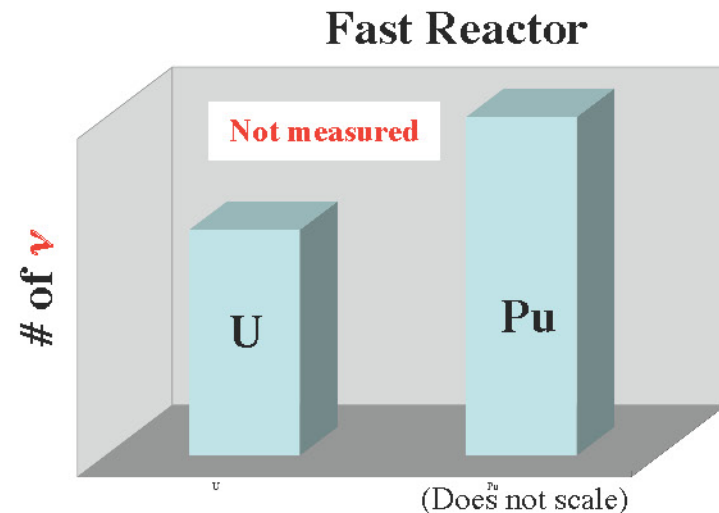
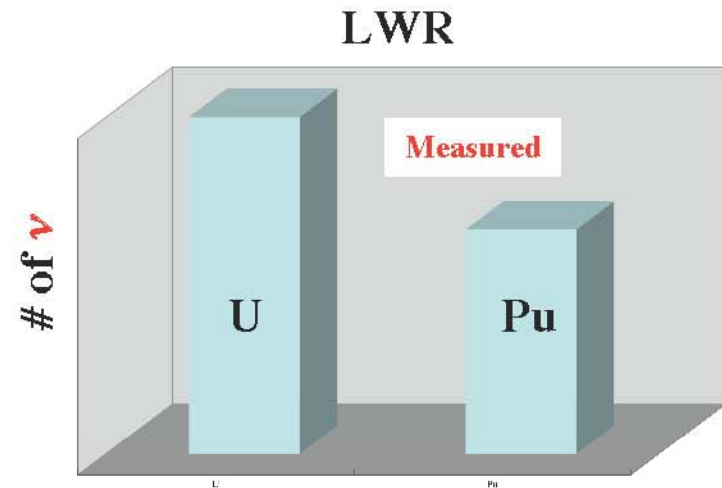




# Why Joyo?

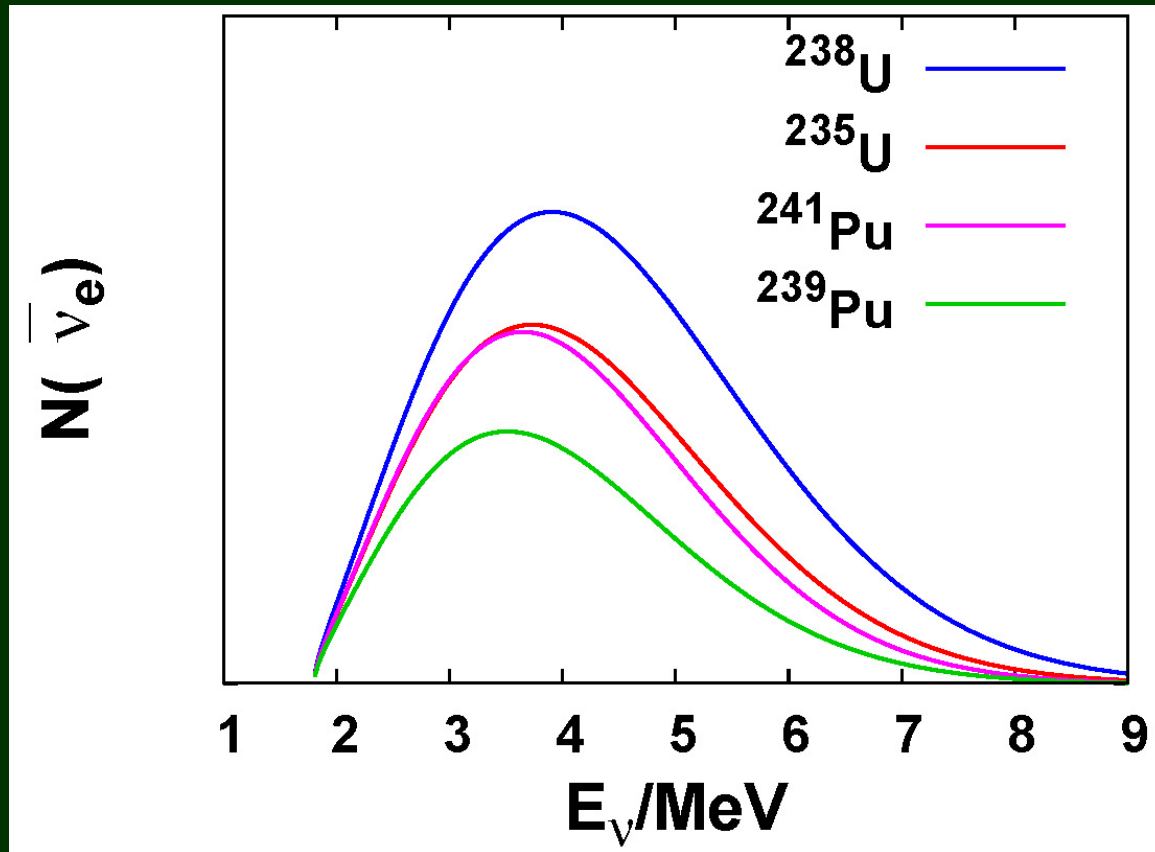
- \* Practical Reason:  
Research Reactor is easier to access.
- \* Scientific Interest:  
 $\nu$  from fast reactor has not been measured.
- \* Technological Interest  
 $\nu$  spectrum from U and Pu can be measured separately by combining with the data from Light Water Reactor

However, the thermal power is small (1/20 of San-Onofre) and it is challenging to detect  $\nu$  at Joyo.



# Composition of Thermal Neutron Reactor & Fast Neutron Reactor

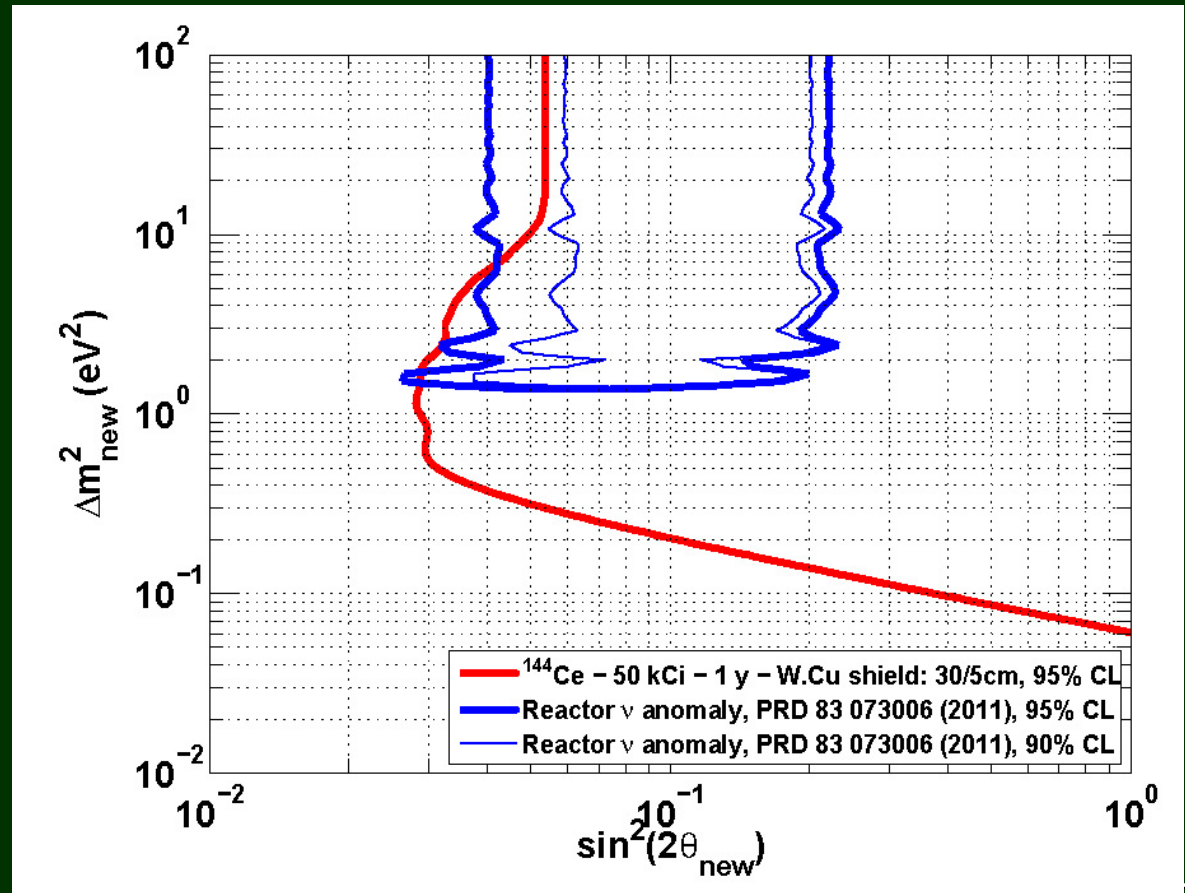
	$^{235}\text{U}$	$^{239}\text{Pu}$	$^{238}\text{U}$	$^{241}\text{Pu}$
Thermal Neutron Reactor (w/ $\text{H}_2\text{O}$ )	53.8%	32.8%	7.8%	5.6%
Fast Neutron Reactor	37.1%	51.3%	7.3%	4.3%



# A ten kilocurie scale anti- $\nu$ source ( $^{144}\text{Ce}$ , $^{106}\text{Ru}$ )

Cribier et al., arXiv:1107.2335v1 [hep-ex]

anti- $\nu$  source placed in a liquid scintillator detector (e.g., KamLAND)



# Proposal of a $\beta$ -beam

Agarwala-Huber-Link,  
JHEP 1001:071,2010

