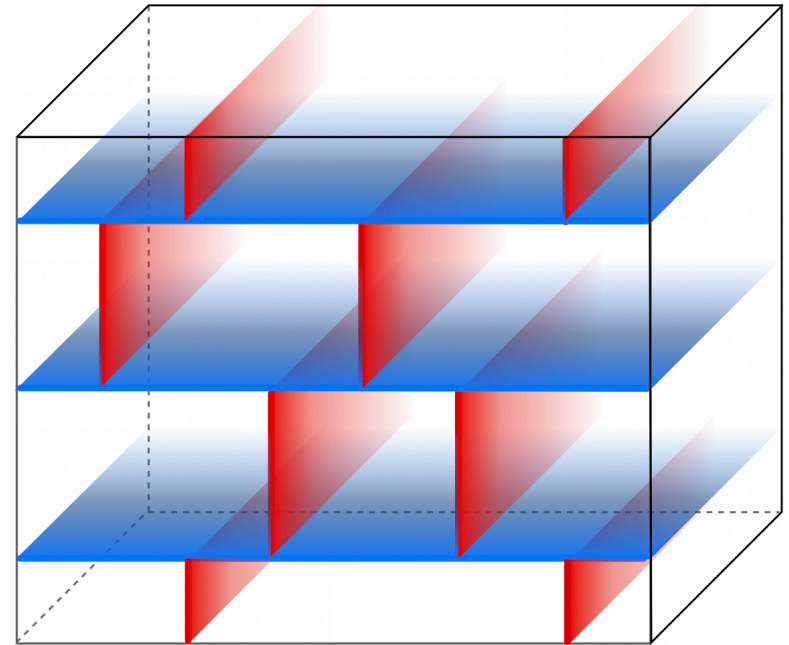


The amazing Super-Maze

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Nejc Ceplak, Shaun Hampton and Nick Warner



JOHN TEMPLETON

FOUNDATION

Agence Nationale de la Recherche
ANR



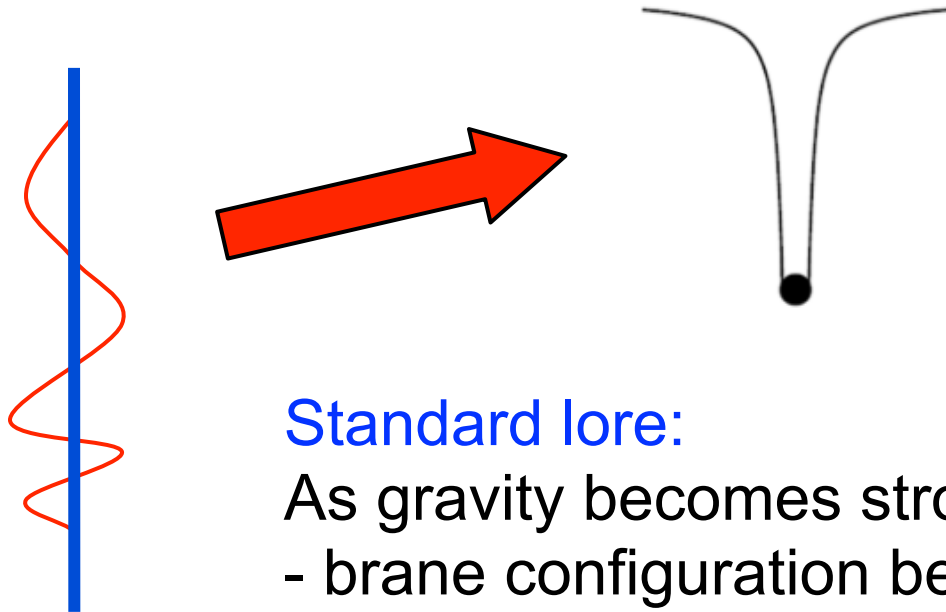
An amazing success of String Theory

Count Black Hole Microstates (branes + strings)

Correctly match B.H. entropy !!!

Zero Gravity

One Particular Microstate at **Finite Gravity**:



Standard lore:

As gravity becomes stronger,

- brane configuration becomes smaller
- horizon develops and engulfs it
- recover standard black hole

Susskind
Horowitz, Polchinski
Chen, Maldacena, Witten

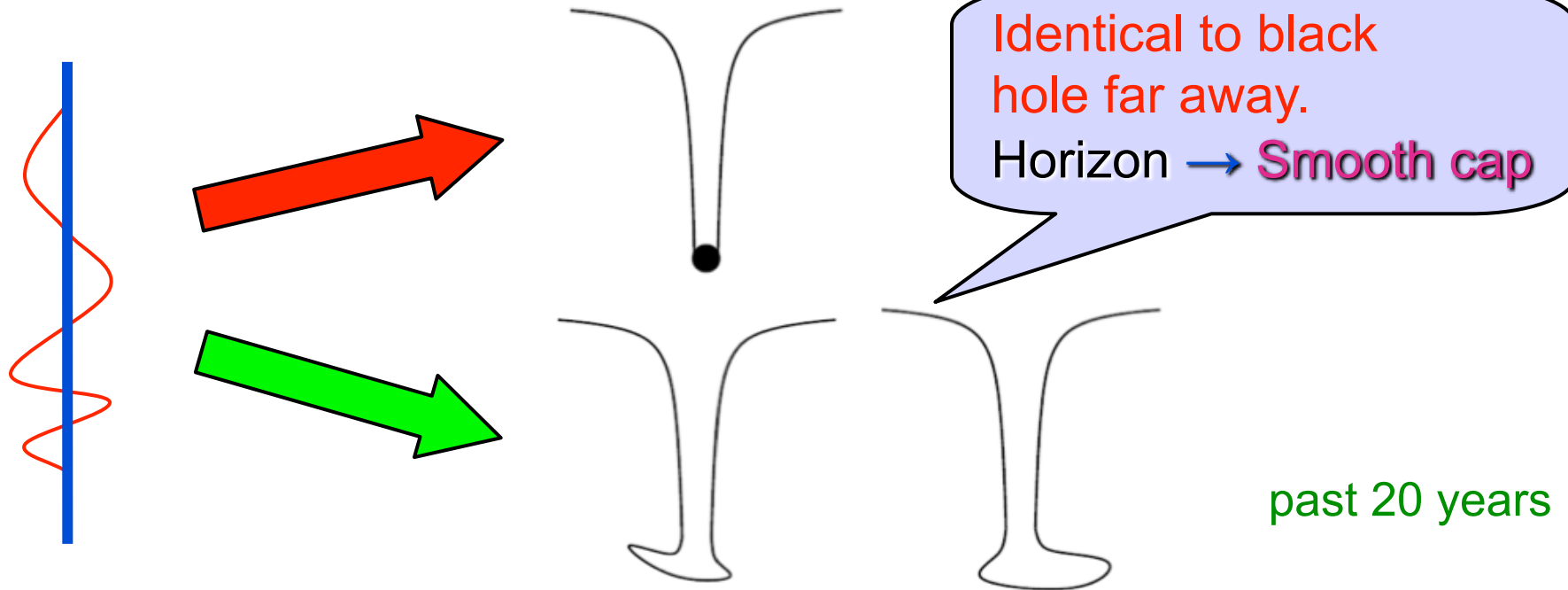
An amazing success of String Theory

Count Black Hole Microstates (branes + strings)

Correctly match B.H. entropy !!!

Zero Gravity

One Particular Microstate at **Finite Gravity**:



In an **ideal world**: Track **each and every** BH microstate from zero-gravity regime to fully-backreacted solution

20 years of microstate geometries

Nick's review talk

- Huge number of smooth horizonless solutions
 - Bubbling geometries, superstrata
 - Largest class of solutions to Einstein's equations ever
 - Many features of **typical** microstates (mass gap)
 - $S \sim (Q_1 Q_5)^{1/2} (Q_p)^{1/4} < S_{\text{BH}} \sim (Q_1 Q_5 Q_p)^{1/2}$ Mayerson, Shigemori '20
- Link with D1-D5 states that count BH entropy ?
 - Only known for a few (messy holographic procedure)
 - Hard to build fractional momentum carriers
Bena, Martinec, Turton, Warner '16; Shigemori '21, '22
 - **Painful reality**: we have **not** succeeded to track typical D1-D5 Strominger-Vafa microstates to **finite gravity**

**Do not pray to the saint who
does not help you !**

Romanian proverb

Instead of D1-D5 look at D2-D4 (or F1-NS5 in type IIA)

One F1 inside N_5 NS5 branes $\rightarrow N_5$ little strings.

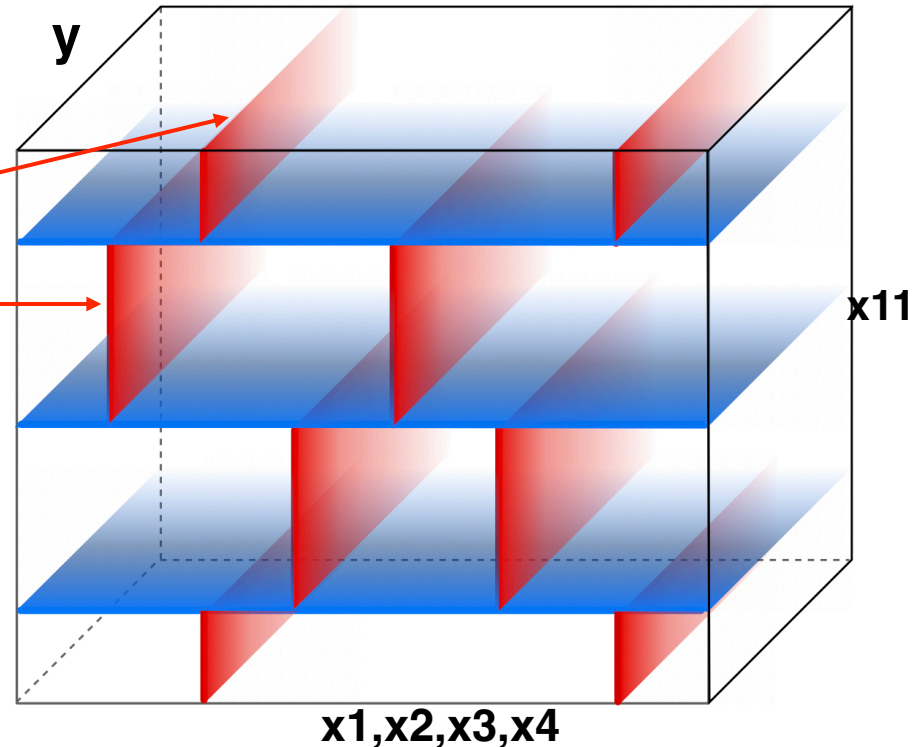
Dijkgraaf, Verlinde, Verlinde

- Visible as **M2 brane strips** in M-theory
- **Total** $N_1 N_5$ independent **momentum carriers**
- each has **4 oscillation directions** (T^4) + **4 fermionic partners**

$$S = 2\pi \sqrt{\frac{4+2}{6} N_1 N_5 N_p}$$

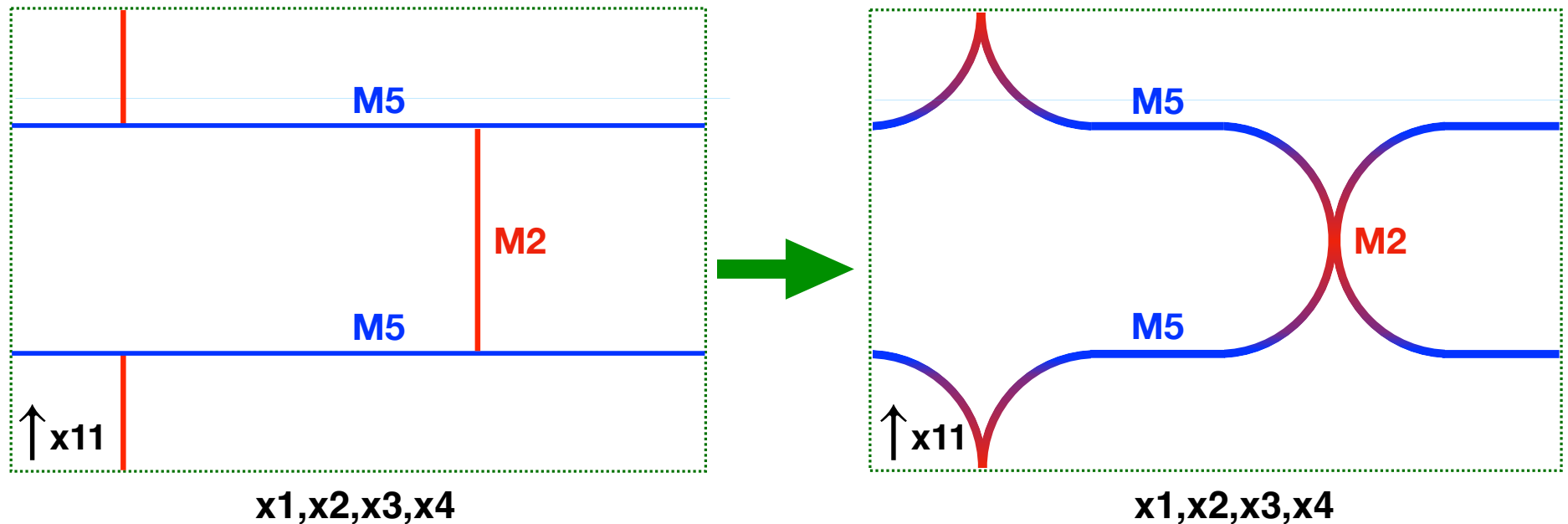
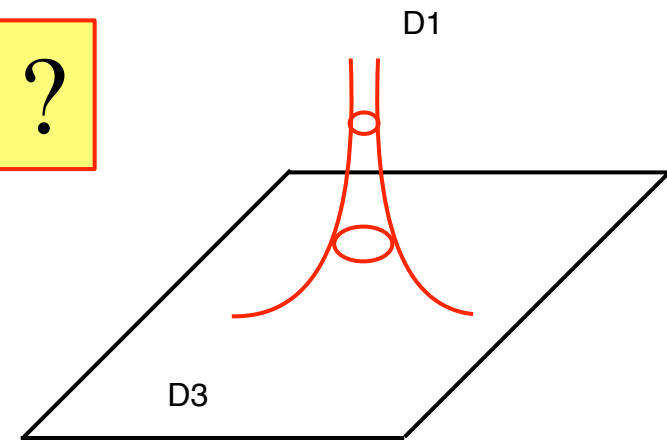
M2 along y, 11
M5 along y, 1234
P along y

zero-coupling picture

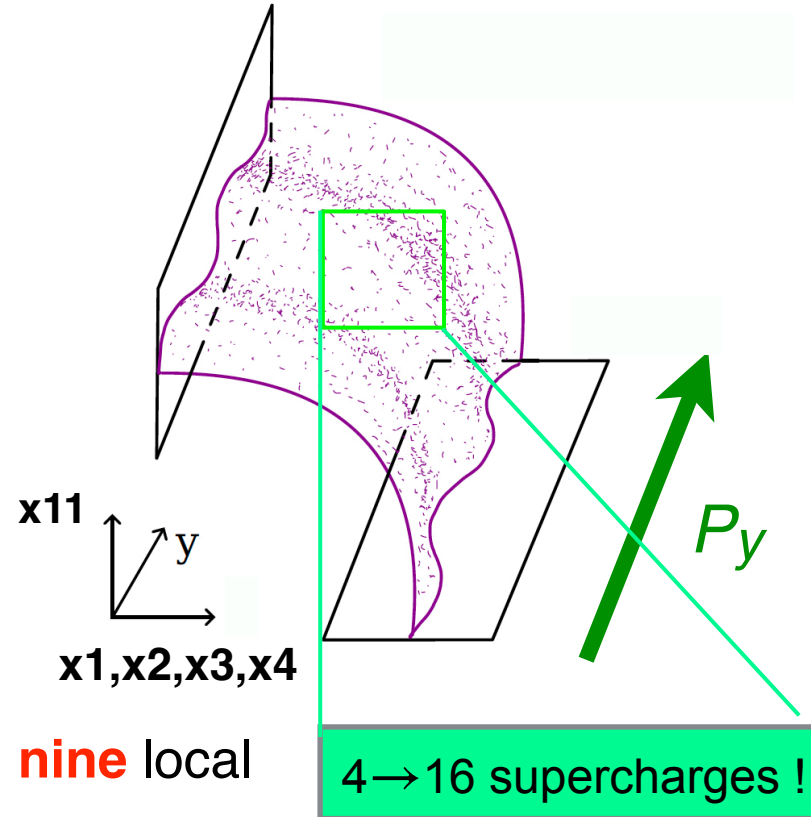
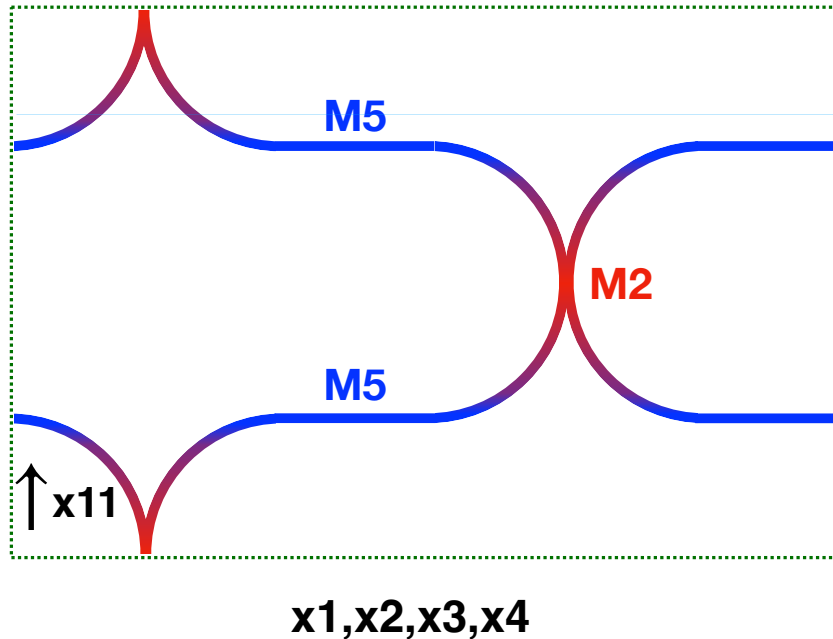


What about finite coupling ?

- Reminder:
Callan-Maldacena spike formed by D1 pulling on an orthogonal D3
- M2 branes also pull on the M5 branes



Except that the spike is a *furrow* carrying momentum waves along y



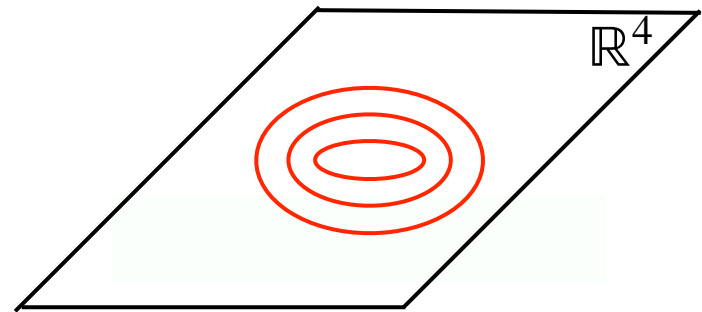
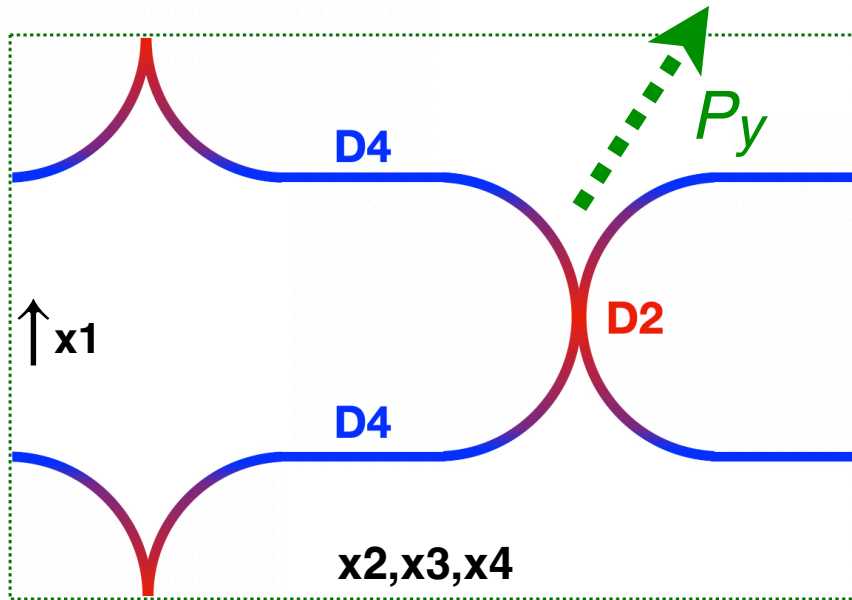
Zoom in on the furrow carrying momentum: **nine** local brane charges: $M2_{x_{11},y}$ $M5_{y,x_1,x_2,x_3,x_4}$ P_y

$M2_{x_1,x_{11}}$ $M5_{x_{11},y,x_2,x_3,x_4}$ $M2_{x_1,y}$ $M5_{x_{11},x_1,x_2,x_3,x_4}$ $P_{x_{11}}$ P_{x_1}

4 → 16 supercharges !

Smoking gun of smooth horizonless solutions

How would these solutions look like ?



spherically symmetric in \mathbb{R}^4 (x_5, x_6, x_7, x_8)
 same **spacetime $SO(4)$** symmetry as BH

$SO(4)$ invariant solutions:

momentum carried by **waves** on fractionated strings (inside T^4) =

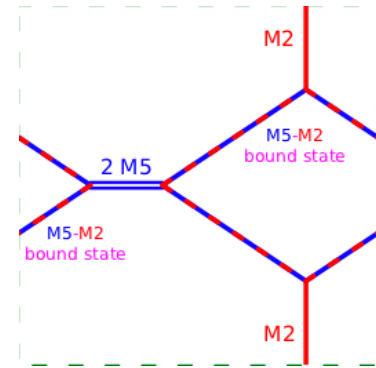
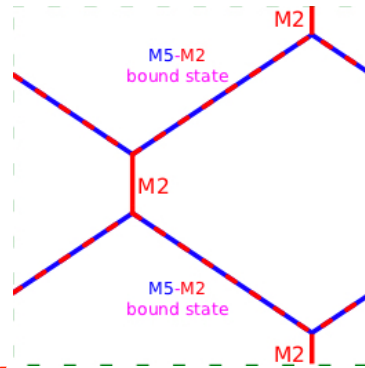
$$\text{bosonic d.o.f. : } S_{\text{bosonic}} = 2\pi\sqrt{\frac{4}{6}N_1N_5N_p}$$

$$+ 2 \text{ fermionic d.o.f. preserving } SO(4) \Rightarrow S_{SO(4) \text{ invariant}} = 2\pi\sqrt{\frac{5}{6}N_1N_5N_p}$$

$$\text{Remaining 2 fermionic d.o.f. break } SO(4) \Rightarrow S_{SO(4) \text{ breaking}} = 2\pi\sqrt{\frac{1}{6}N_1N_5N_p}$$

How will the $SO(4)$ -invariant solution look like ?

- **2-charge** - Monge-Ampère *cohomog-3* at least Lunin 07
- **3-charge**: at least *cohomog-4*
- smeared on $T^3 \Rightarrow$ **string web**:
- **Horizonless** \Leftrightarrow **16-susy locally**
- Geometric transition \Rightarrow Bubbles on internal dimensions
- Expectation: **backreaction** will make bubbles **large** *irrespective* of T^4 size at infinity
- Differs from BH only by T^4 **KK modes**:
- Asympt. $\mathbb{R}^{4,1} \times S^1 \times T^4$: **exponentially-decaying**
- Asympt. $AdS_3 \times S^3 \times T^4$: **high-dimension operators**
 - **Dimension** depends on T^4 moduli. **SUSY ?**
 - **Visible** at free-orbifold point ?
 - Can CFT distinguish different supermaze solutions ?



How will the generic solution look like ?

- Generic microstates will contain
 - $SO(4)$ breaking modes + T^4 dependent modes
- 2-charge systems:
 - when $SO(4)$ breaking modes are present, smearing on T^4 does not lose information Kanitscheider, Taylor, Skenderis
 - If **only T^4 dependent modes** present, smearing **erases** information \Rightarrow **singular**, small horizon
- 3-charge story ?
 - superstrata with $SO(4)$ -breaking (++) strands capture **some** smeared T^4 dependent modes: **(00) strands**
- A. Could the presence of $SO(4)$ -breaking modes in generic solution allow T^4 smearing without info loss ?
- B. Would T^4 -dependent information be lost upon smearing even when $SO(4)$ -breaking modes exist ?

DVV microstates

$$S = S_{\text{BH}}$$

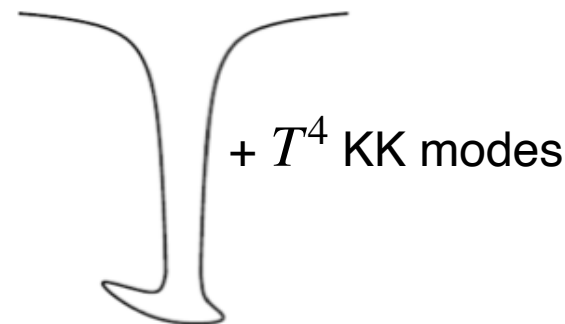
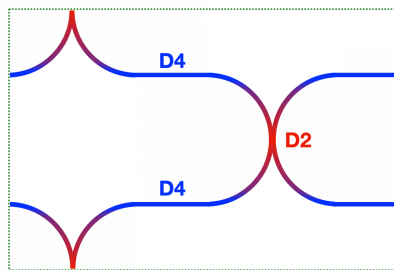
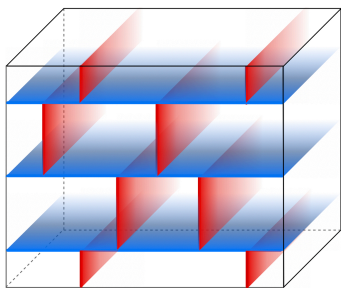
SUPERMAZE

branes pull & merge
16 susy locally !

New Microstate
Geometries

$$S = S_{\text{BH}}$$

Effective coupling (g_s)



- Build supergravity solution !
- Holographic dual to supermaze? T^4 -dependent modes?
 $\langle \Psi_{\text{supermaze}} | \mathcal{O}_{T^4\text{-dependent}} | \Psi_{\text{supermaze}} \rangle \neq 0$
- Most generic beast: is 6D sugra enough? or one needs 10D?
- Flat space: supermaze fields decay exponentially.
Universal ?