

Basic Properties of GT transitions & β^- decay “Expected” in r-Process Nuclei

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**Understanding of r-process on the basis of Nuclear Physics
Kyoto, Yukawa, May. 22-24, 2019**



Neptune driving Waves
波を操る海神ネプチューン

Neptune=弱い相互作用
(weak interaction)



Powerful Waves=強い相互作用
(strong interaction)

Neptune and the waves, or "steeds," he rides.

— Walter Crane, 1892

Neptune driving Waves
波を操る海神ネプチューン

Neptune=弱い相互作用
(weak interaction)

What are the properties of β^- decay
in $N \gg Z$ nuclei ?

Properties of GT transitions are deduced
using experimental data from CE reactions !

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Neptune=弱い相互作用
(weak interaction)

In β decay

Gamow-Teller (caused by $\sigma\tau$ operator)

Fermi (caused by τ operator)

are called "allowed transitions,"

They are the dominant transition processes !

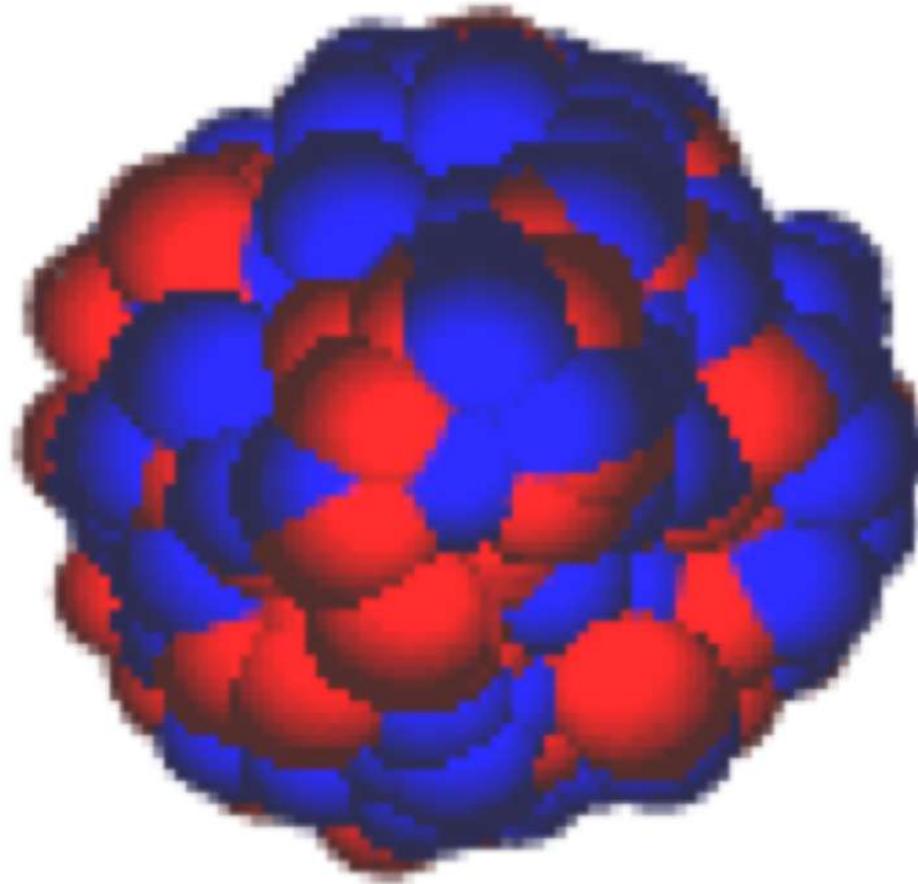
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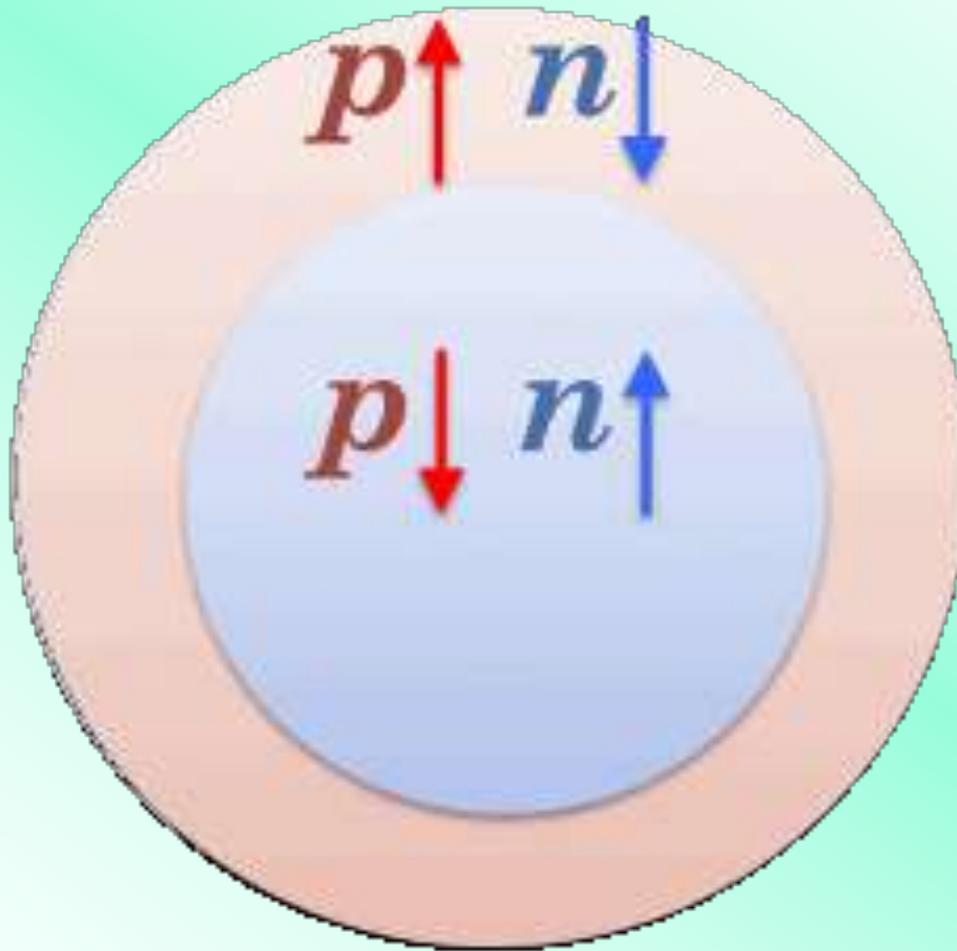
— Walter Crane, 1892

IV Giant Monopole Resonance (IVGMR)

by P. Adrich



IV Spin Monopole Mode



**Basic common understanding of β -decay and Charge-Exchange reaction in the study of GT transitions

β decays :

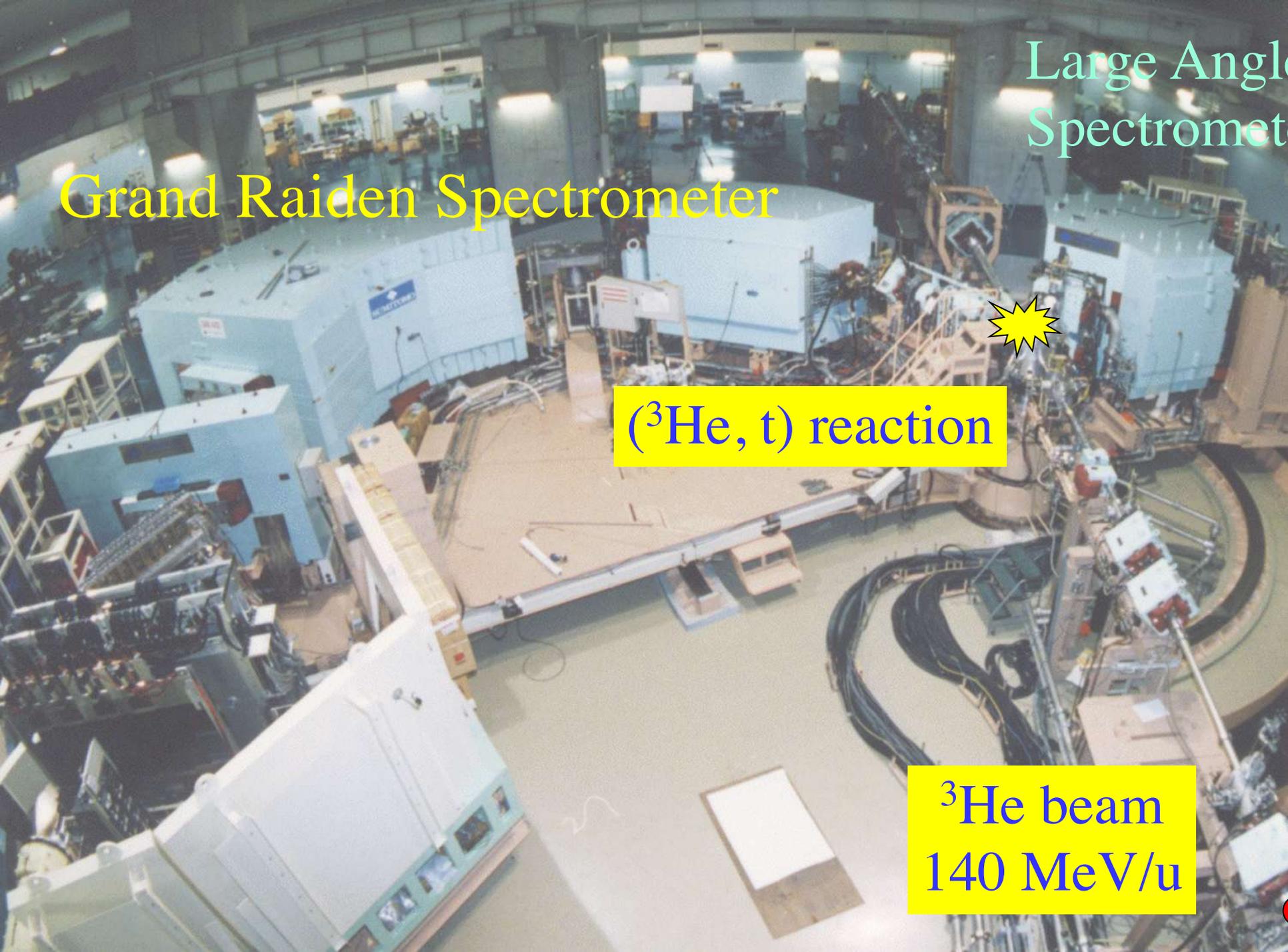
Absolute $B(\text{GT})$ values,

but usually the study is limited to low-lying states

(p, n) and $({}^3\text{He}, t)$ reaction at 0° :

Relative $B(\text{GT})$ values, but **Highly Excited States**

** Both are important for the study of GT transitions!



Large Angle
Spectrometer

Grand Raiden Spectrometer

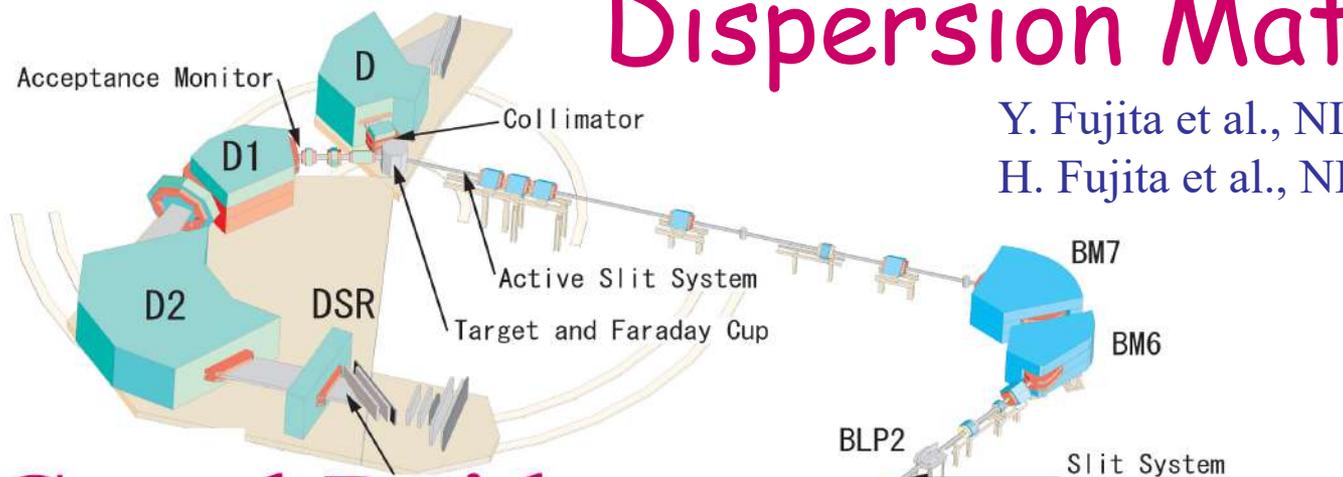
$(^3\text{He}, t)$ reaction

^3He beam
140 MeV/u



Dispersion Matching !

Y. Fujita et al., NIM B 126 ('99) 274.
H. Fujita et al., NIM A 484 ('02) 17.



Grand Raiden

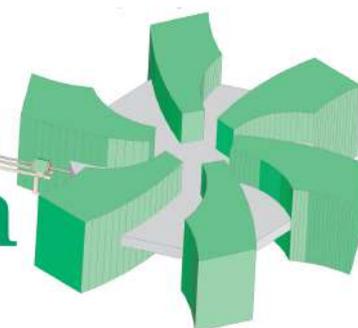
$\Delta E = 25 - 30 \text{ keV}$

Slit System
for Achromatic Beam

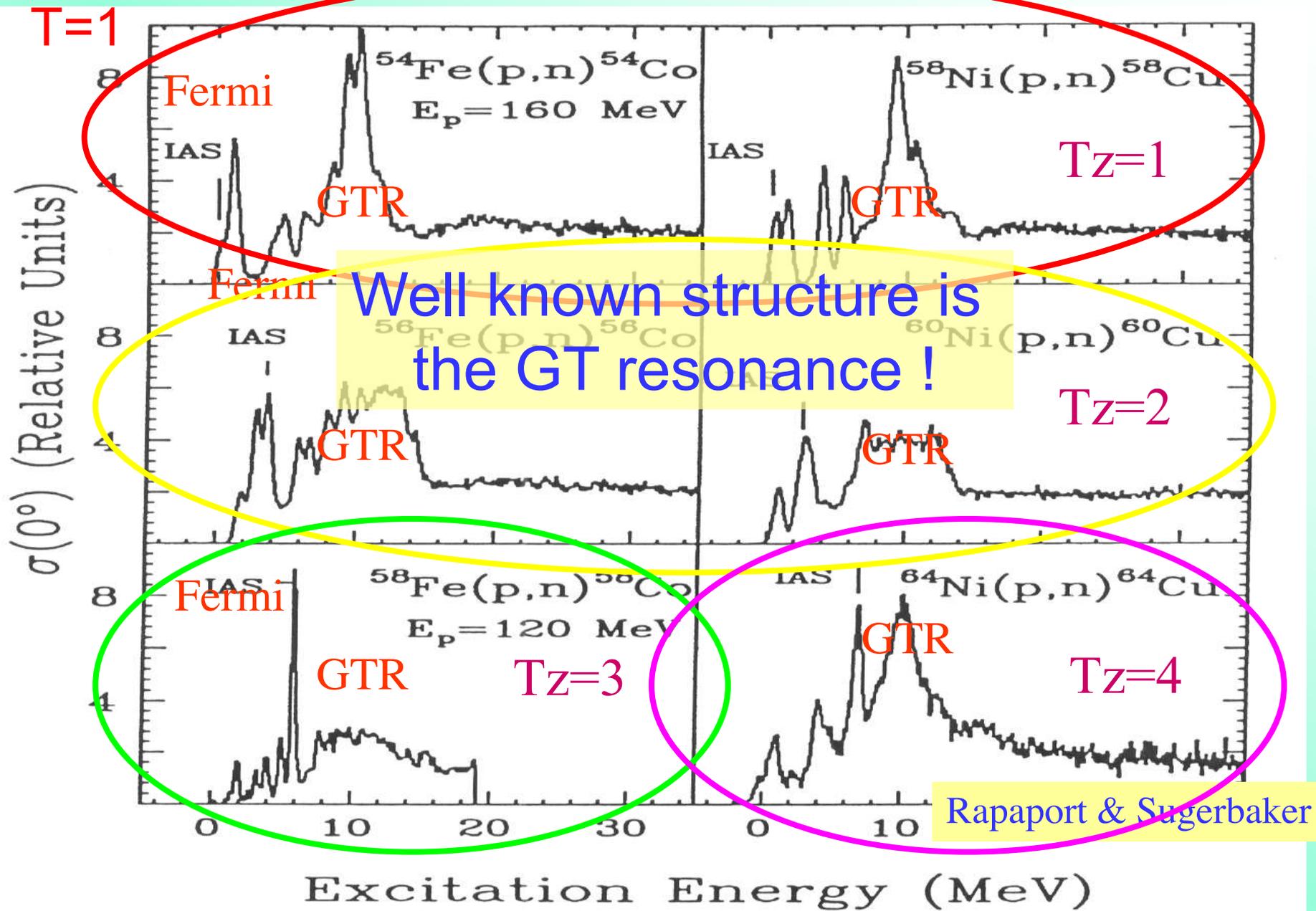
WS Beam Line

$E = 420 \text{ MeV}, \Delta E = 150 \text{ keV}$

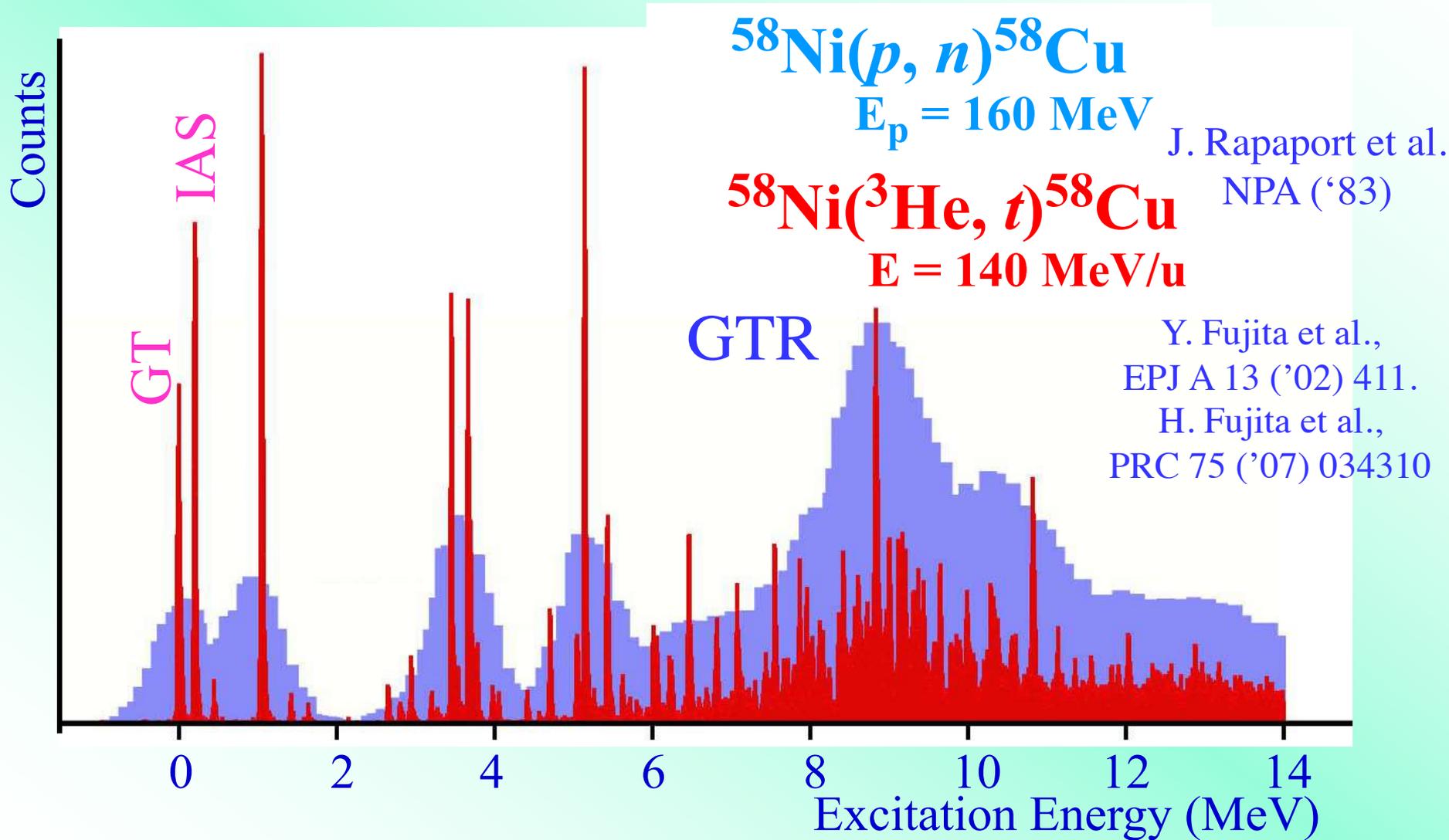
Ring Cyclotron



(p, n) spectra for Fe and Ni Isotopes



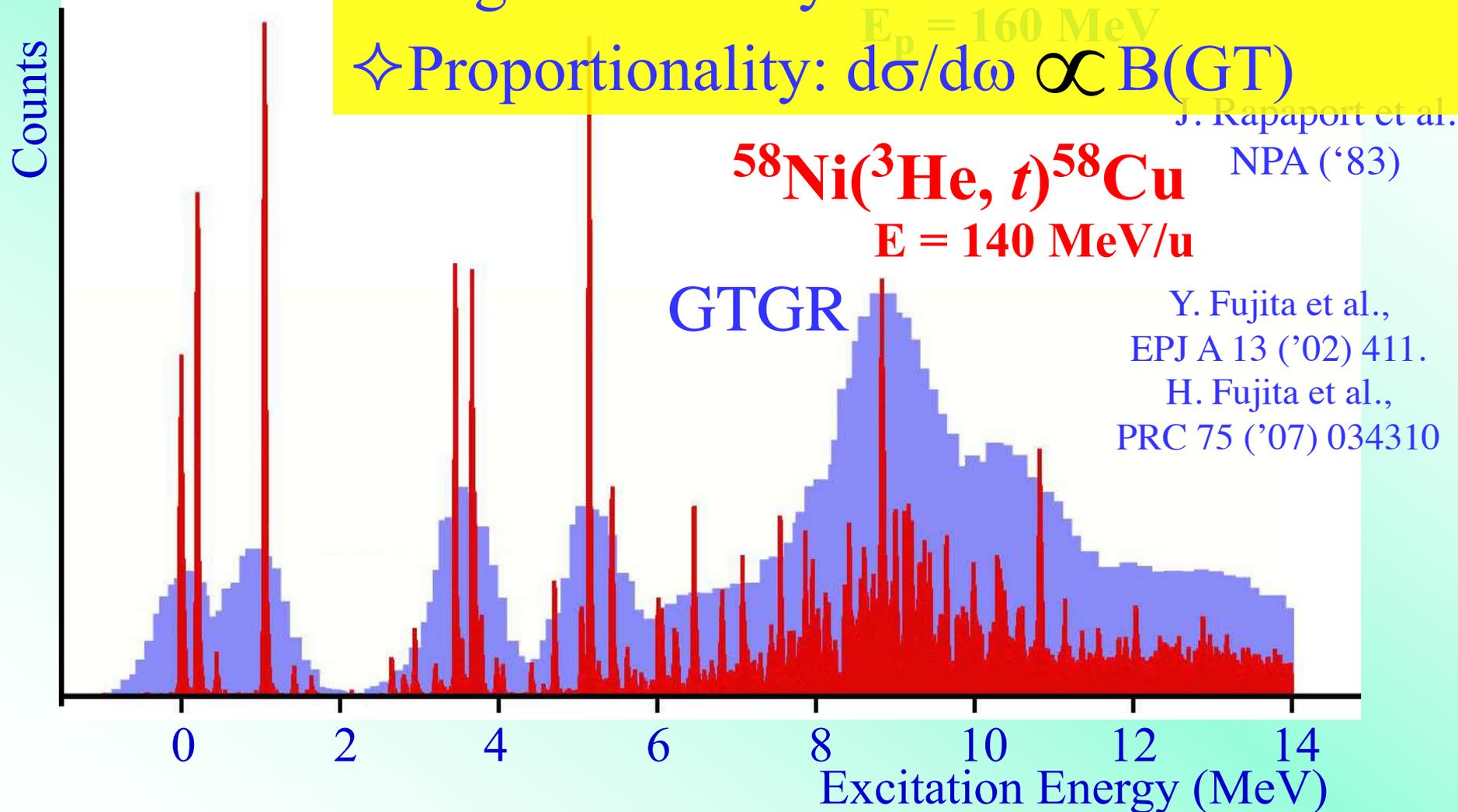
Comparison of (p, n) and ($^3\text{He}, t$) 0° spectra



Comparison of (p, n) and ($^3\text{He}, t$) 0° spectra

✧ High selectivity for GT excitations.

✧ Proportionality: $d\sigma/d\omega \propto B(\text{GT})$



Gamow-Teller transitions

Mediated by $\sigma\tau$ operator (axial isovector-operator)

$$\Delta S = -1, 0, +1 \quad \text{and} \quad \Delta T = -1, 0, +1$$

($\Delta L = 0$, no change in radial w.f.)

→ no change in spatial w.f.

Accordingly, transitions among $j_>$ and $j_<$ configurations

$$j_> \rightarrow j_>, \quad j_< \rightarrow j_<., \quad j_> \leftrightarrow j_<$$

example $d_{5/2} \rightarrow d_{5/2}$, $d_{3/2} \rightarrow d_{3/2}$, $d_{5/2} \leftrightarrow d_{3/2}$

Note that Spin and Isospin are
unique quantum numbers in atomic nuclei !

→ GT transitions are sensitive to Nuclear Structure !

→ GT transitions in each nucleus are UNIQUE !

β decay & Nuclear CE reaction

$$*\beta\text{-decay GT tra. rate} = \frac{1}{t_{1/2}} = f \frac{\lambda^2}{K} B(\text{GT})$$

$$B(\text{GT}) : \text{reduced GT transition strength} \\ \propto (\text{matrix element})^2 = |\langle f | \sigma \tau | i \rangle|^2$$

*Nuclear (CE) reaction rate (cross-section)
= reaction mechanism

⊗ operator

⊗ structure

$$= (\text{matrix element})^2$$

*At intermediate energies ($100 < E_{\text{in}} < 500$ MeV)

→ $d\sigma/d\omega(q=0)$: proportional to $B(\text{GT})$

β decay & Nuclear CE reaction

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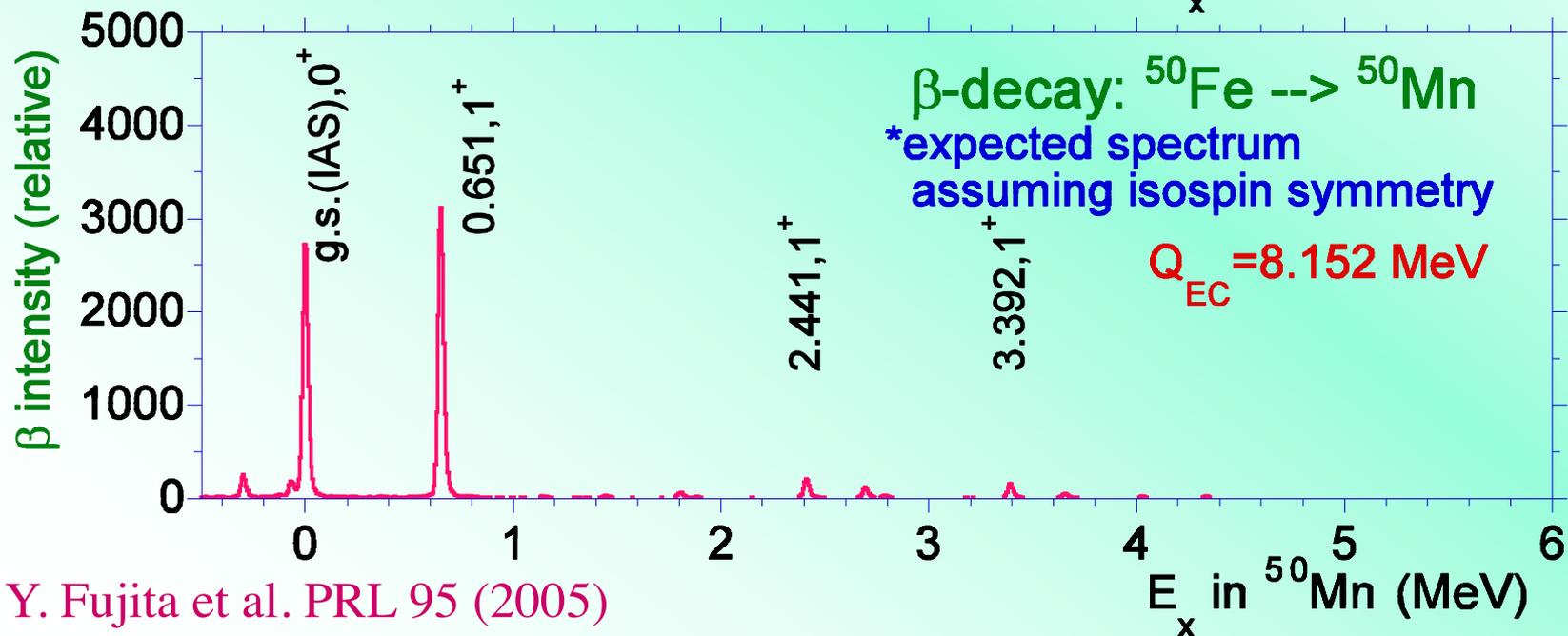
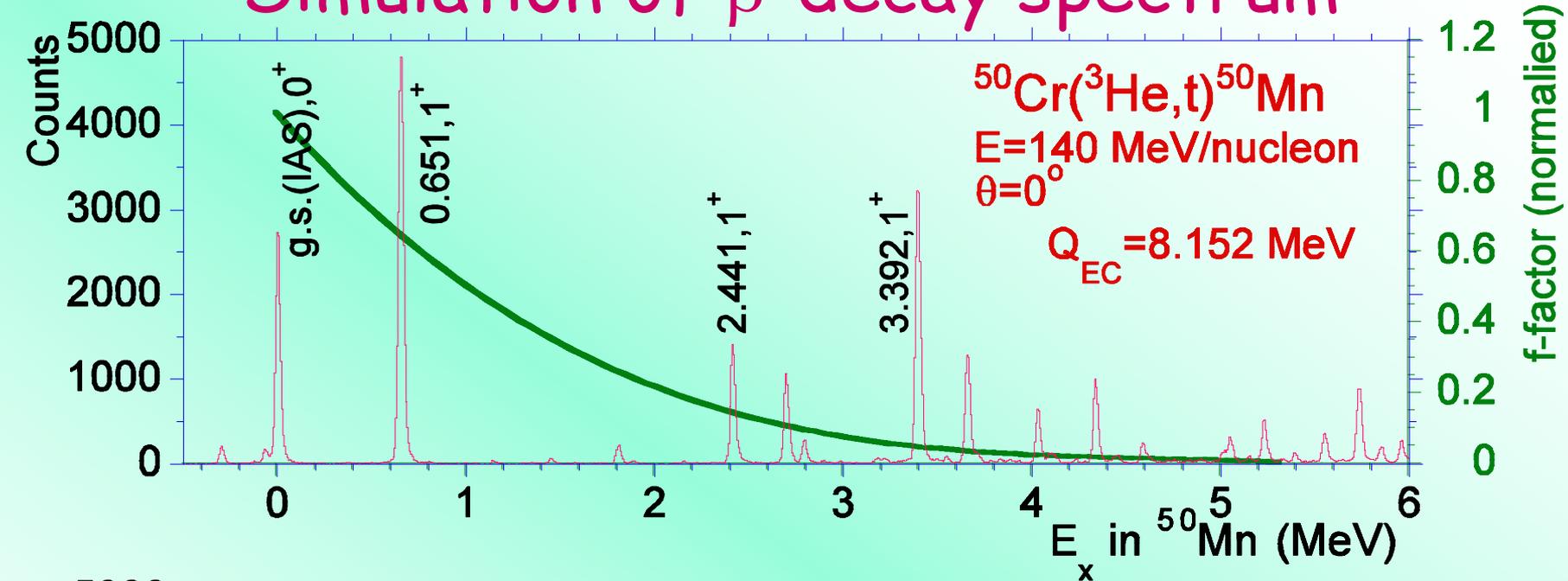
\otimes structure

$= (\text{matrix element})^2$

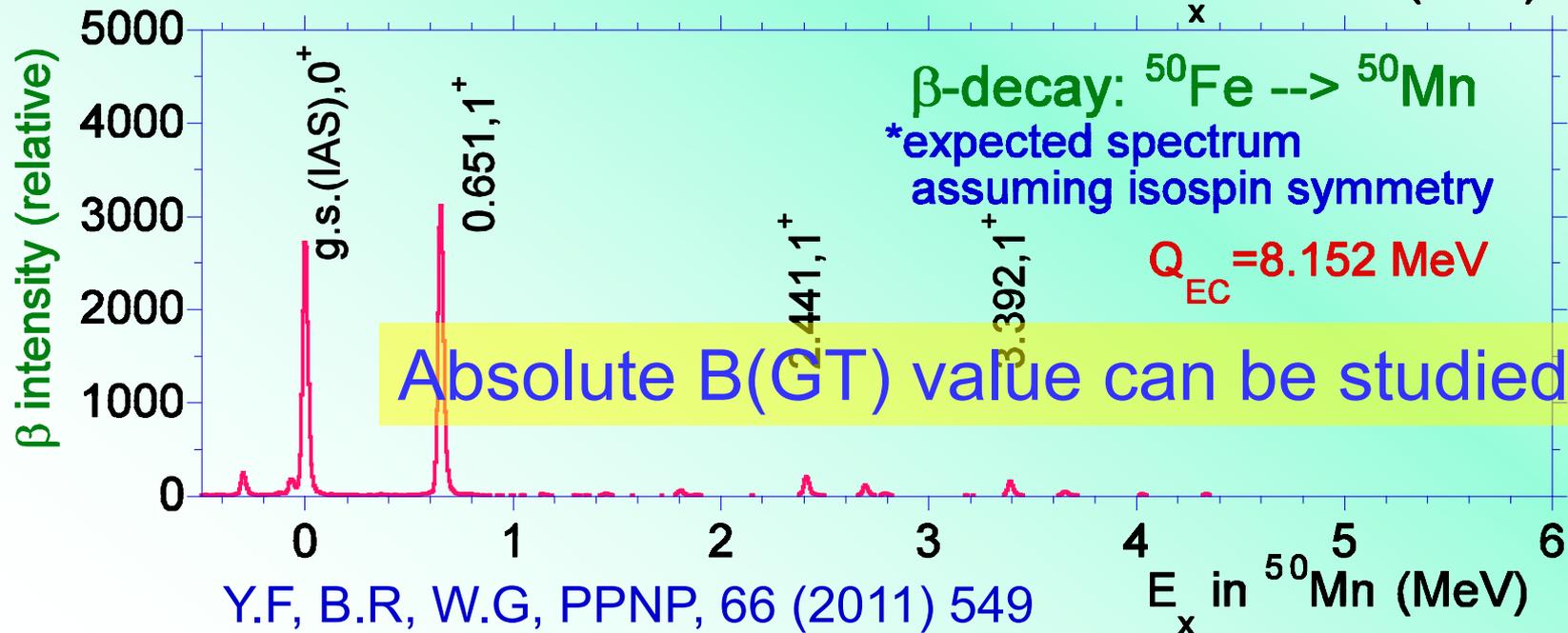
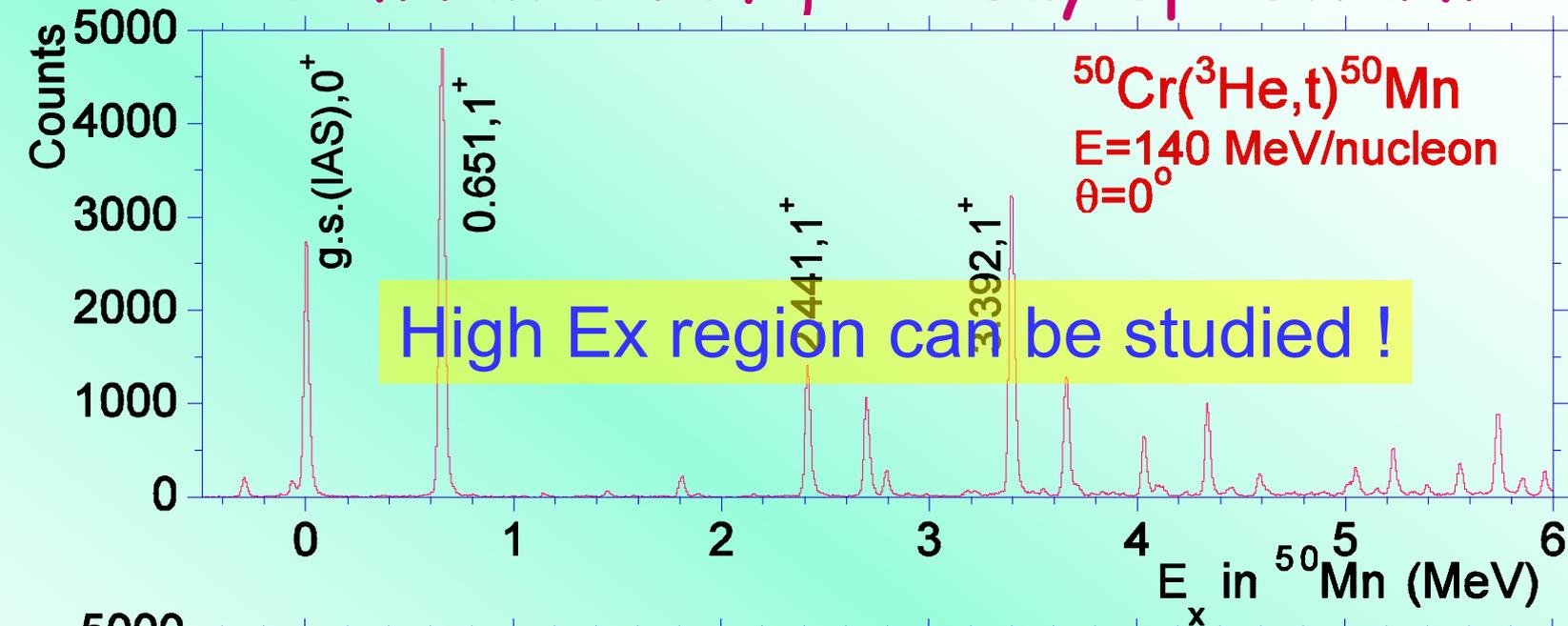
*At intermediate energies ($100 < E_{\text{in}} < 500$ MeV)

$\rightarrow d\sigma/d\omega(q=0)$: proportional to $B(\text{GT})$

Simulation of β -decay spectrum



Simulation of β -decay spectrum



****GT transitions in each nucleus are
UNIQUE!**

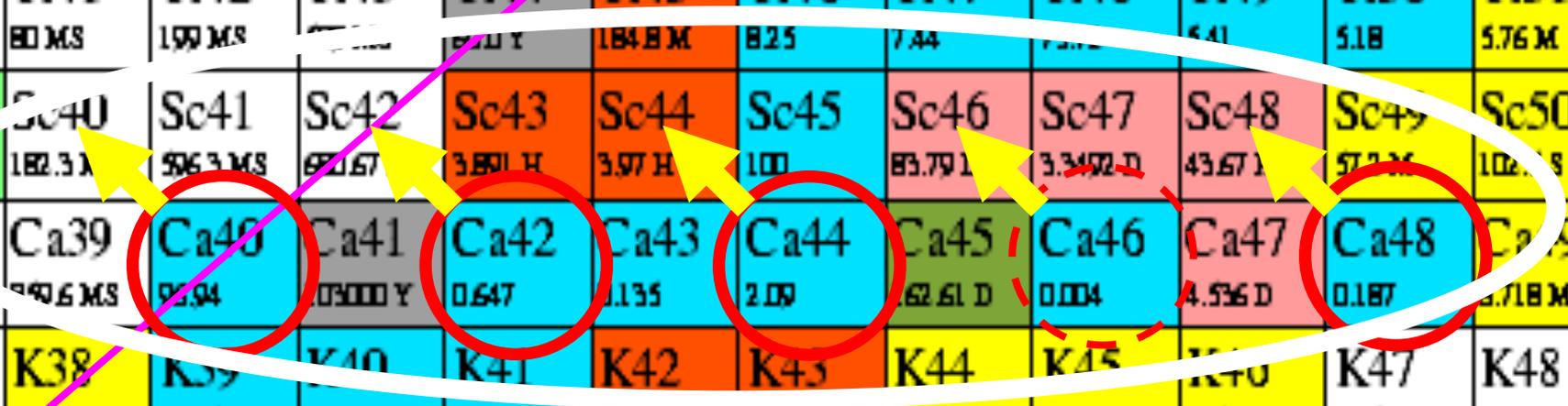
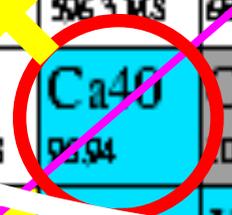
- Ca isotopes -

Nuclear Chart *f*-shell Nuclei

		Co48	Co49	Co50	Co51	Co52	Co53	Co54	Co55	Co56	Co57
			<35 NS	44 MS	>200 NS	11.5 MS	>100 MS	195.28 MS	17.53 H	77.233 D	271.74 D
Fe45	Fe46	Fe47	Fe48	Fe49	Fe50	Fe51	Fe52	Fe53	Fe54	Fe55	Fe56
>350 NS	20 MS	27 MS	44 MS	70 MS	1.55 MS	205 MS	8.275 H	8.51 M	5.845	2.73 Y	91.754
Mn48	Mn49	Mn50	Mn51	Mn52	Mn53	Mn54	Mn55				
<10	382 MS	2.8529 MS	46.2 M	5.591 D	3740000 Y	312.11 D	100				
Cr47	Cr48	Cr49	Cr50	Cr51	Cr52	Cr53	Cr54				
21 MS	53 MS	90 MS	0.26 S	900 MS	21.56 H	42.3 M	4.345	27.7025 D	83.789	9.901	2.365
V42	V43	V44	V45	V46	V47	V48	V49	V50	V51	V52	V53
<55 NS	>800 MS	111 MS	547 MS	422.50 MS	32.6 M	15.9735 D	330 D	0.250	99.750	3.743 M	1.60 M
Ti41	Ti42	Ti43	Ti44	Ti45	Ti46	Ti47	Ti48	Ti49	Ti50	Ti51	Ti52
80 MS	199 MS	1.75	8.00 Y	184.8 M	8.25	7.44	7.315	5.41	5.18	5.76 M	1.7 M
Sc40	Sc41	Sc42	Sc43	Sc44	Sc45	Sc46	Sc47	Sc48	Sc49	Sc50	Sc51
182.3 M	506.3 MS	692.67	3.891 H	3.97 H	100	83.791	3.3072 D	43.671	57.2 M	102.5 S	12.4 S
Ca39	Ca40	Ca41	Ca42	Ca43	Ca44	Ca45	Ca46	Ca47	Ca48	Ca49	Ca50
99.6 MS	99.94	0.103000 Y	0.647	0.135	2.09	62.61 D	0.004	4.536 D	0.187	2.718 M	13.9 S
K38	K39	K40	K41	K42	K43	K44	K45	K46	K47	K48	K49
7.536 M	93.2581	0.0117	6.7302	12.380 H	22.3 H	22.13 M	17.3 M	105 S	17.90 S	6.8 S	1.26 S

GT transitions from Ca isotopes

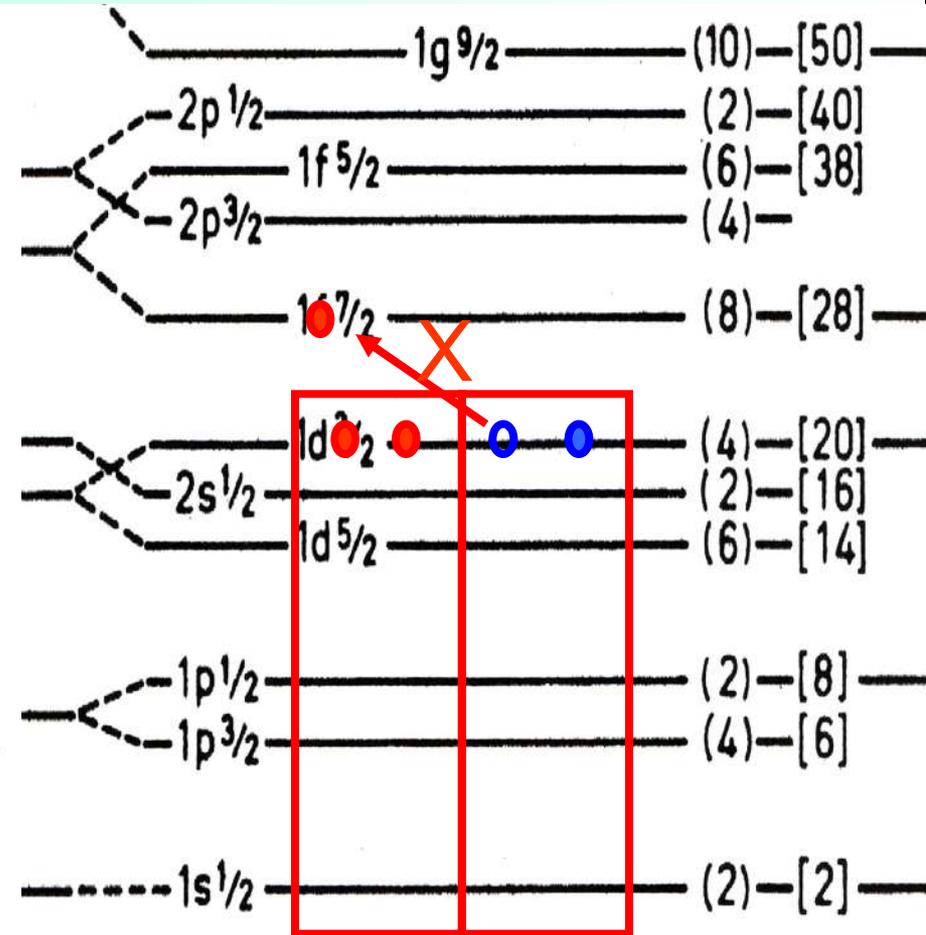
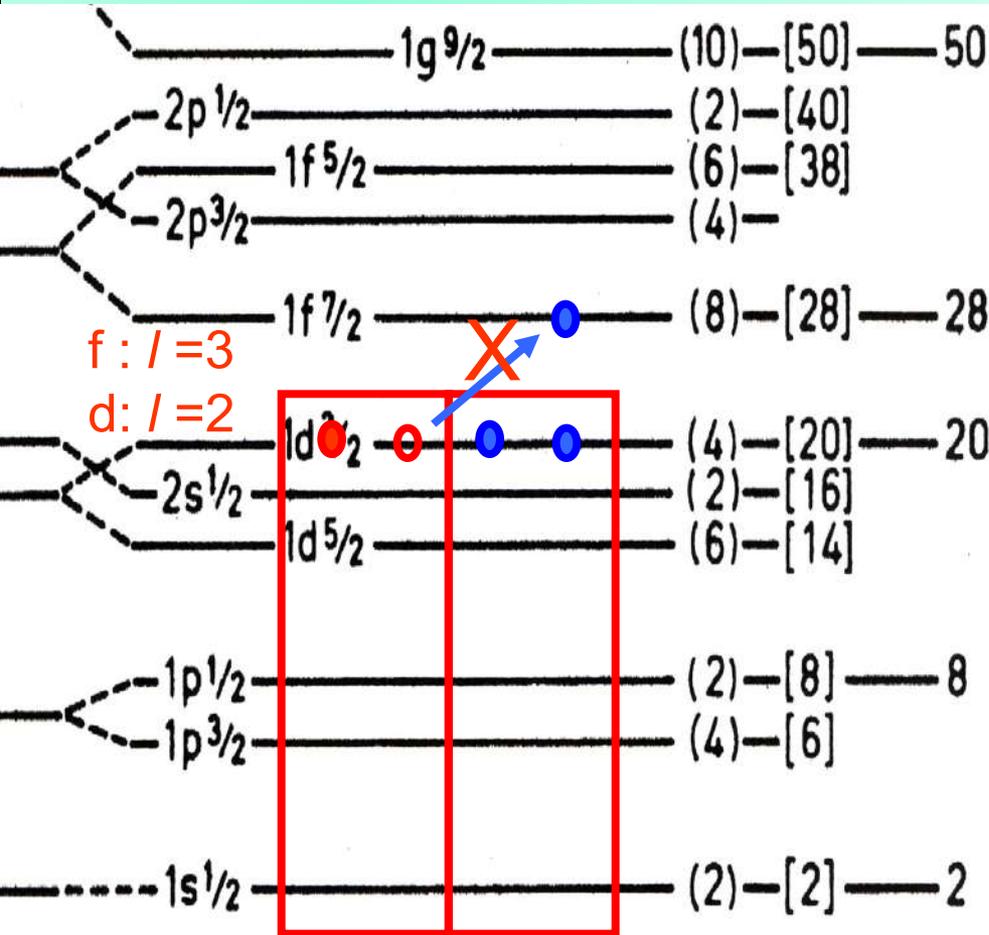
N=Z line



1p-1h Excitations in

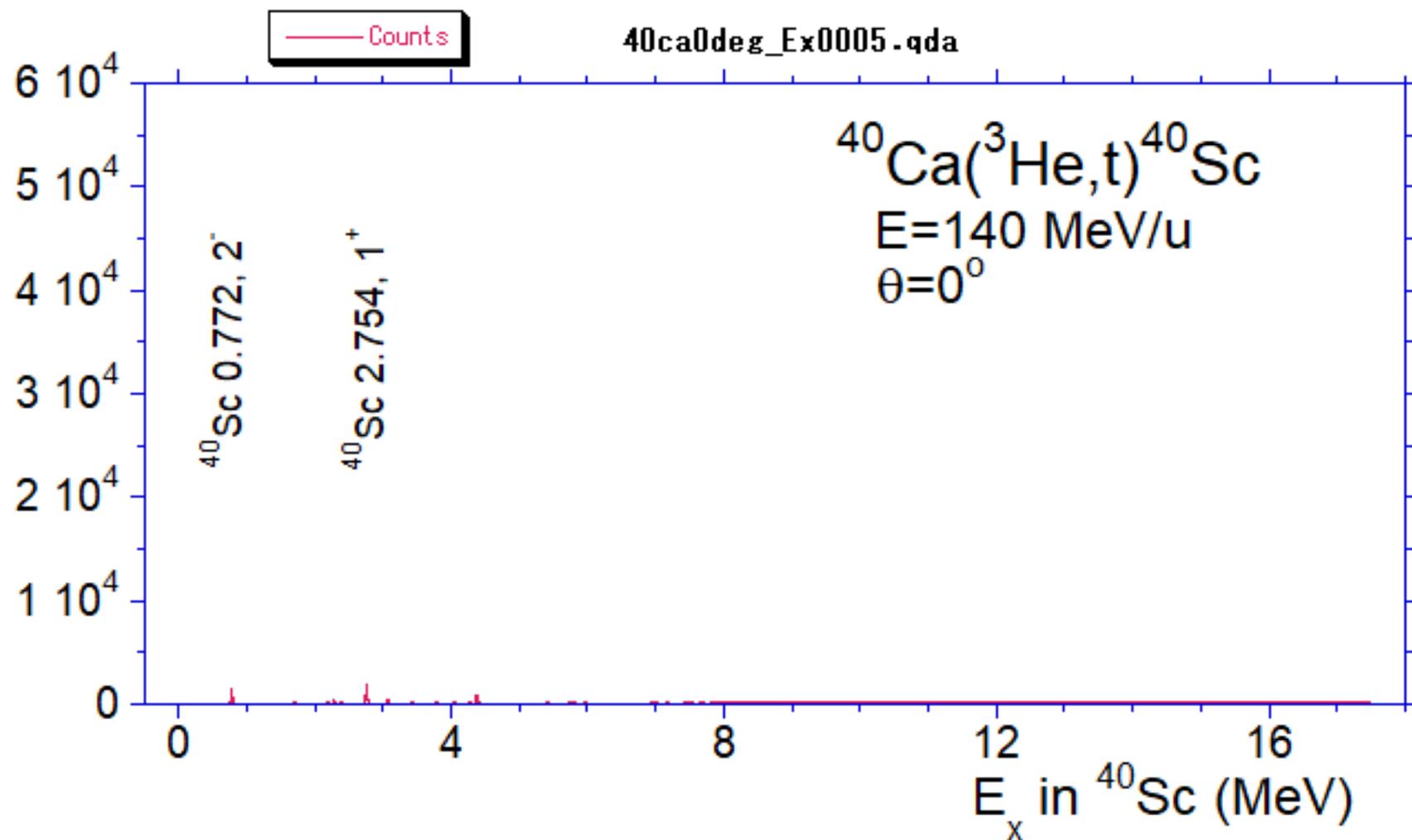
^{40}Ca : CE+ Reaction

^{40}Ca : CE- Reaction

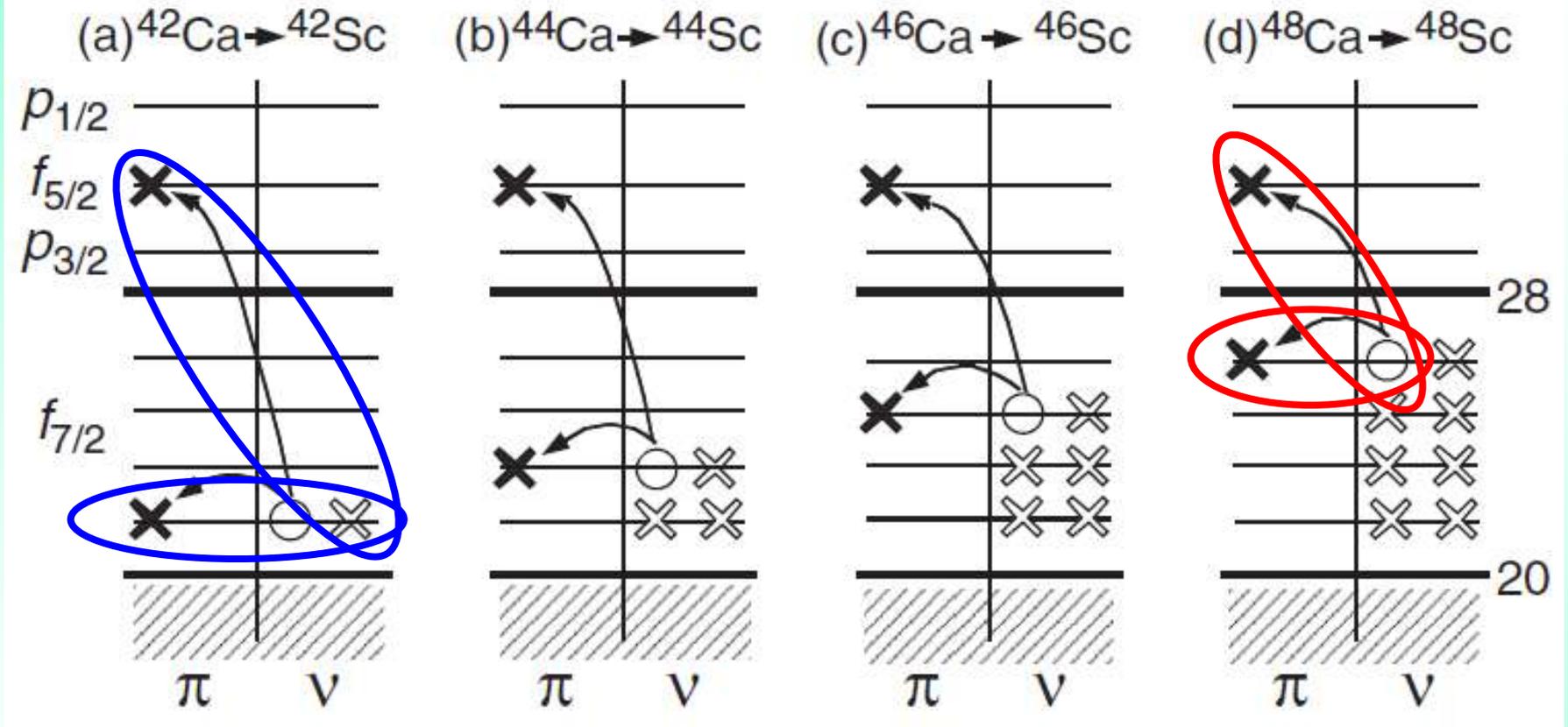


from ^4He , ^{16}O , ^{40}Ca : no GT transition is allowed!
 (no GT transition from LS-closed Doubly Magic Nuclei)

$^{40}\text{Ca}(^3\text{He},t)^{40}\text{Sc}$



GT Configurations in Sc isotopes



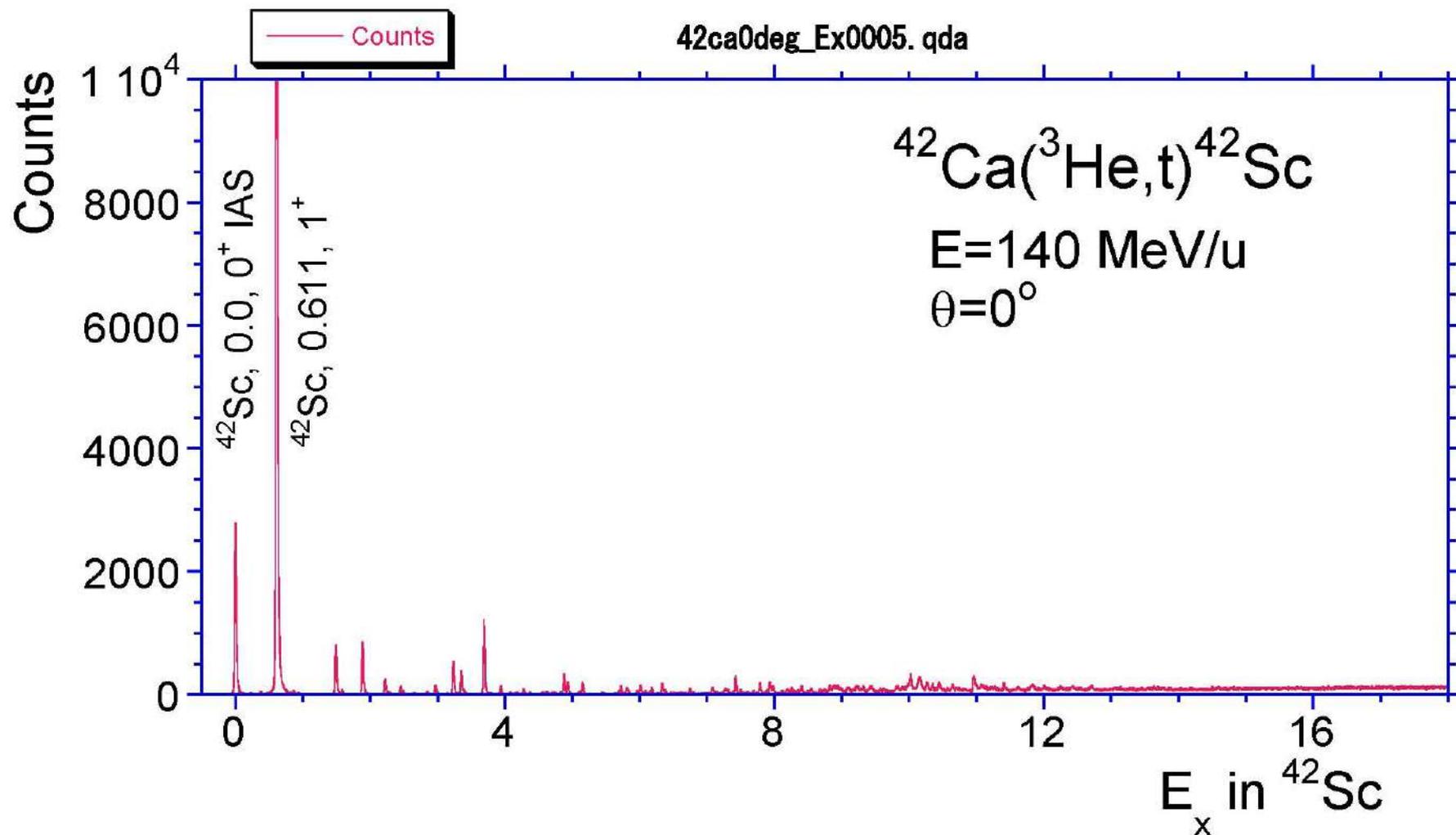
particle-particle
nature



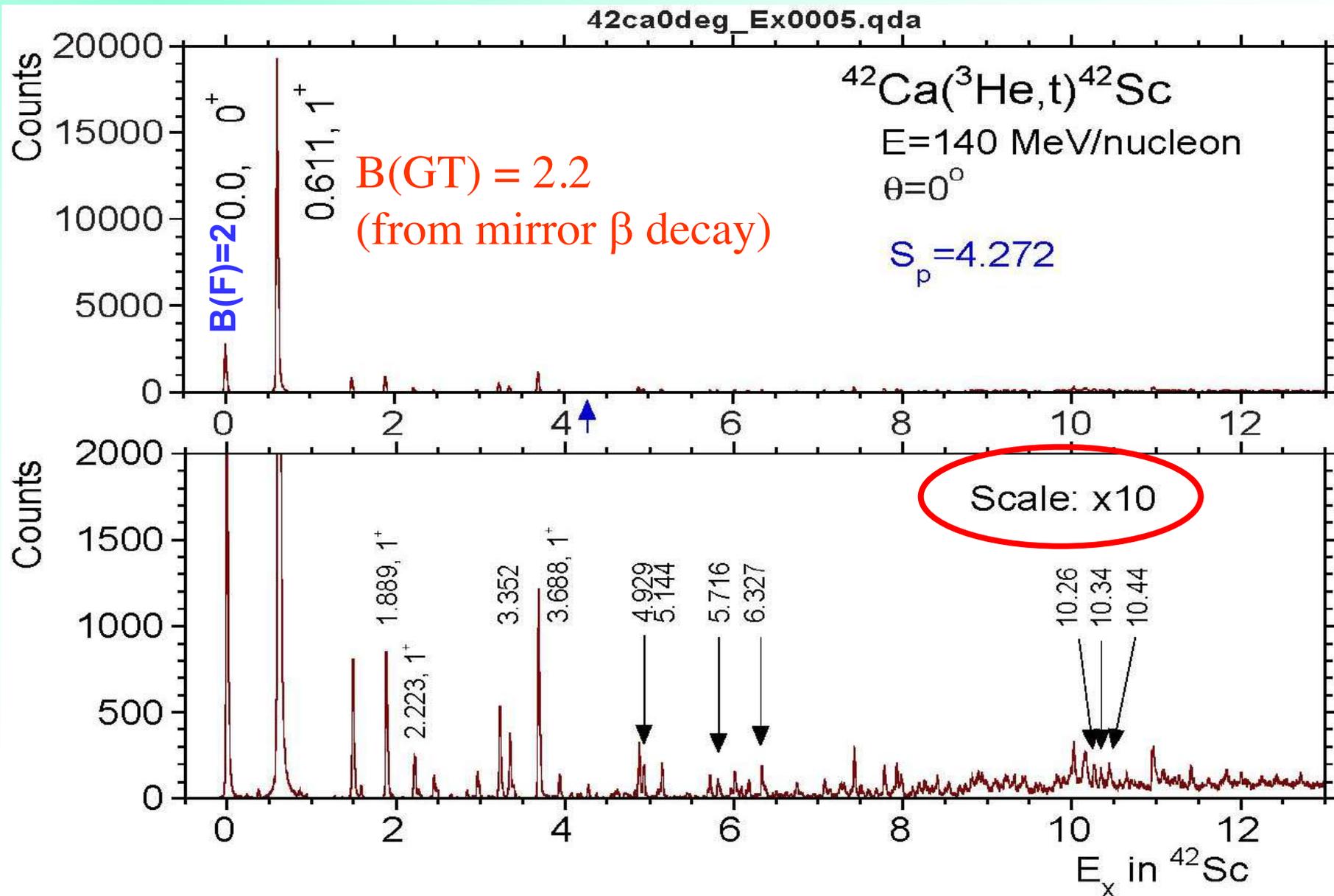
particle-hole
nature

particle-particle int. (attractive) \longrightarrow particle-hole int. (repulsive)

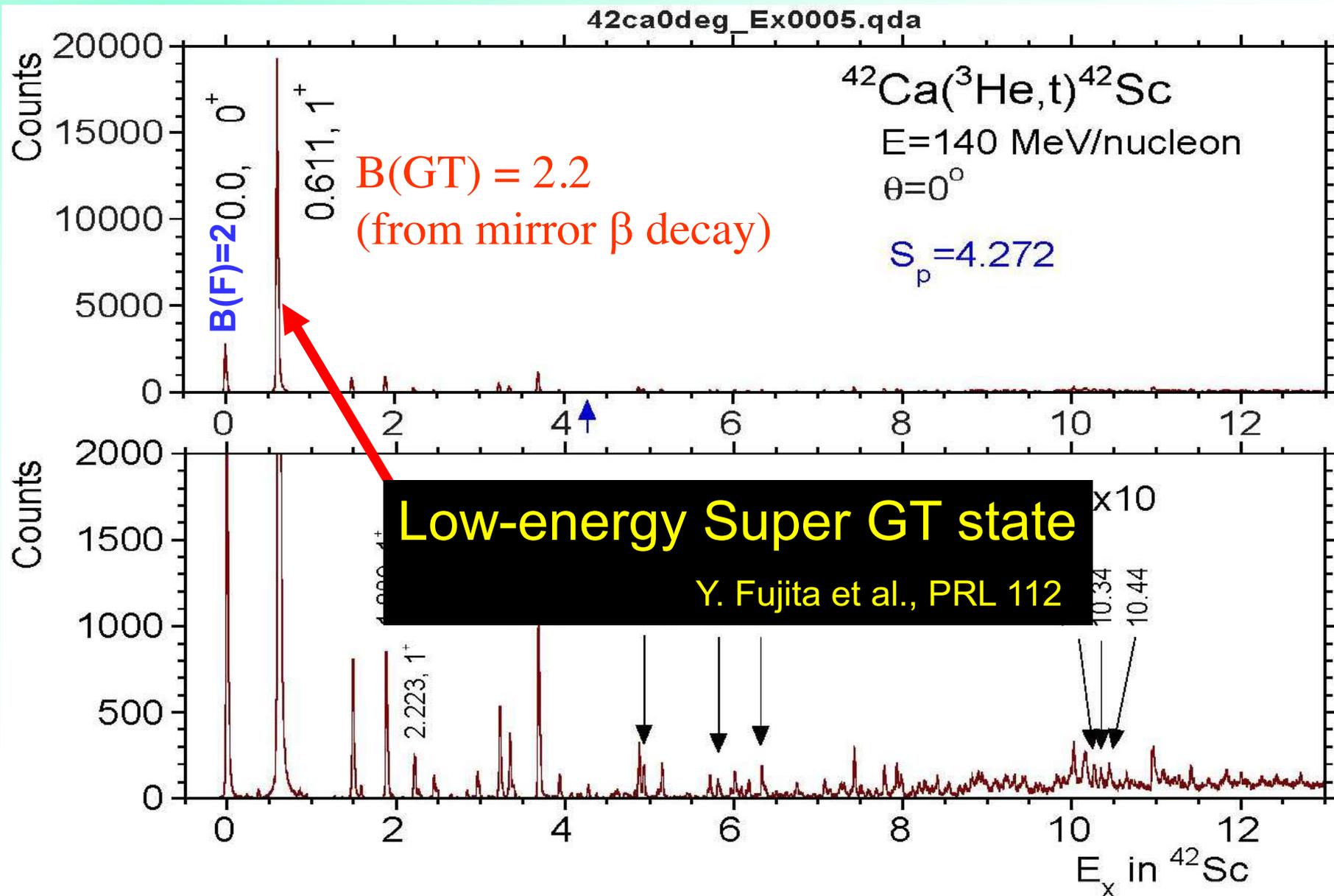
$^{42}\text{Ca}(^3\text{He},t)^{42}\text{Sc}$



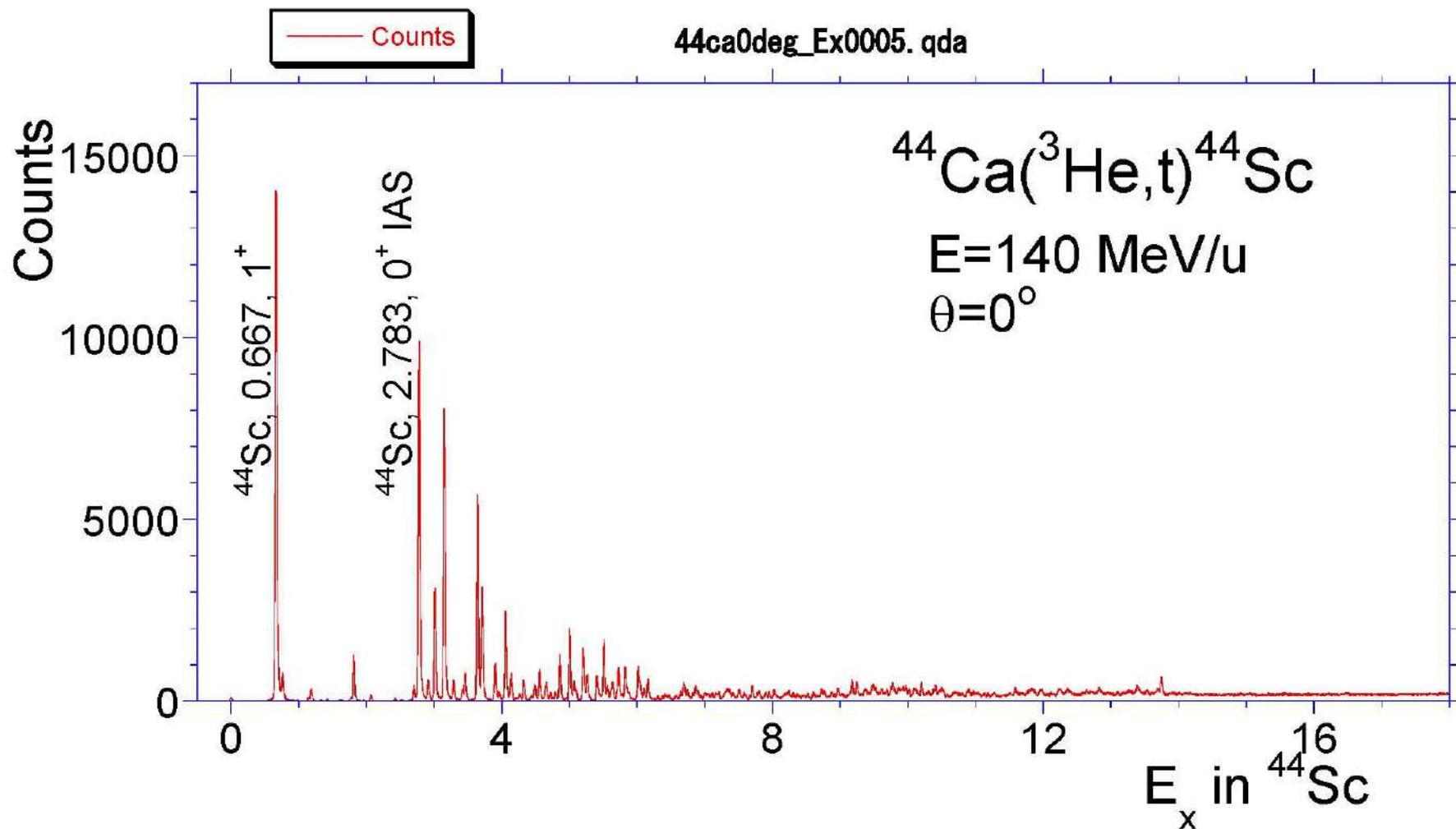
$^{42}\text{Ca}(^3\text{He},t)^{42}\text{Sc}$ in 2 scales



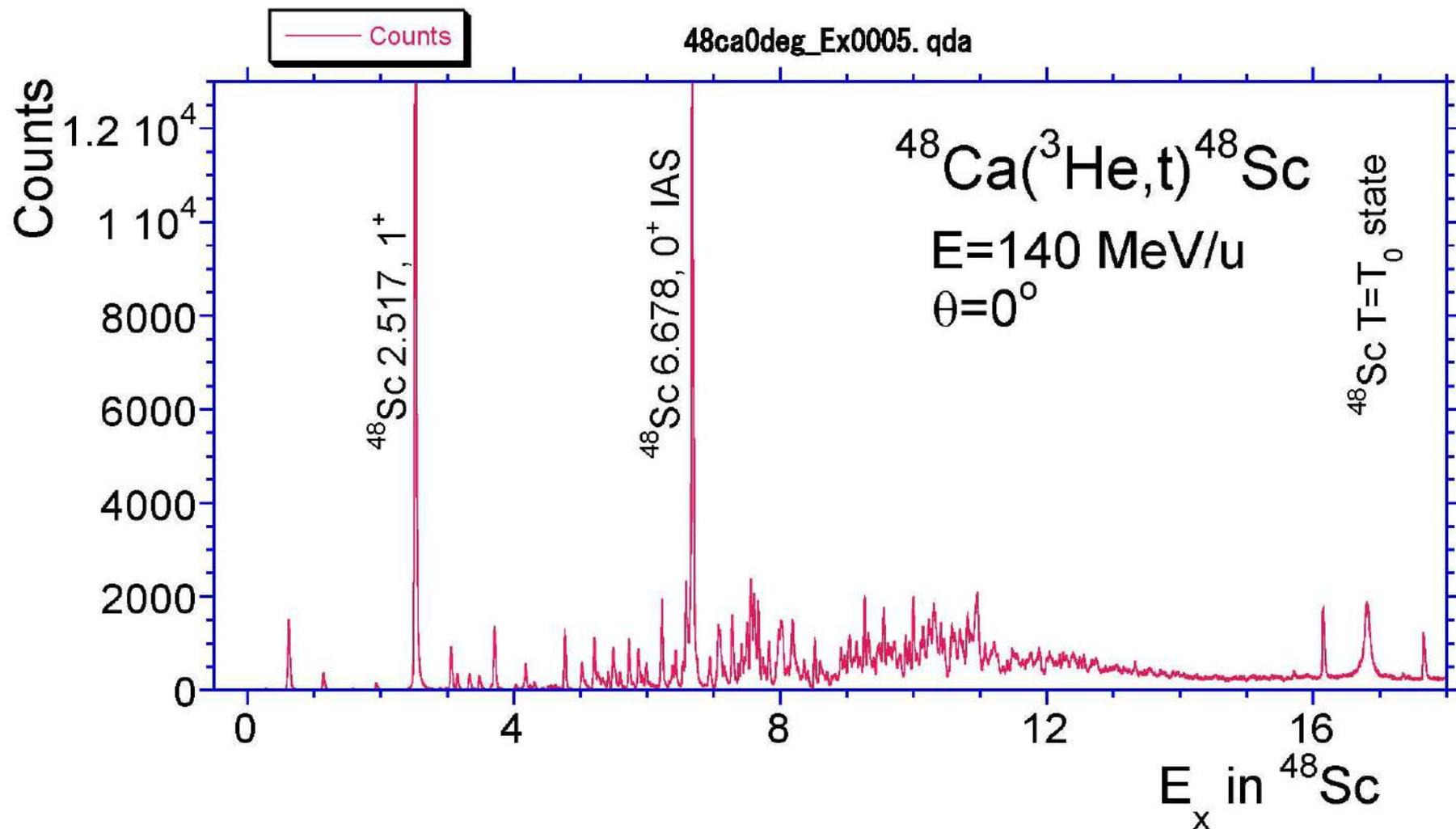
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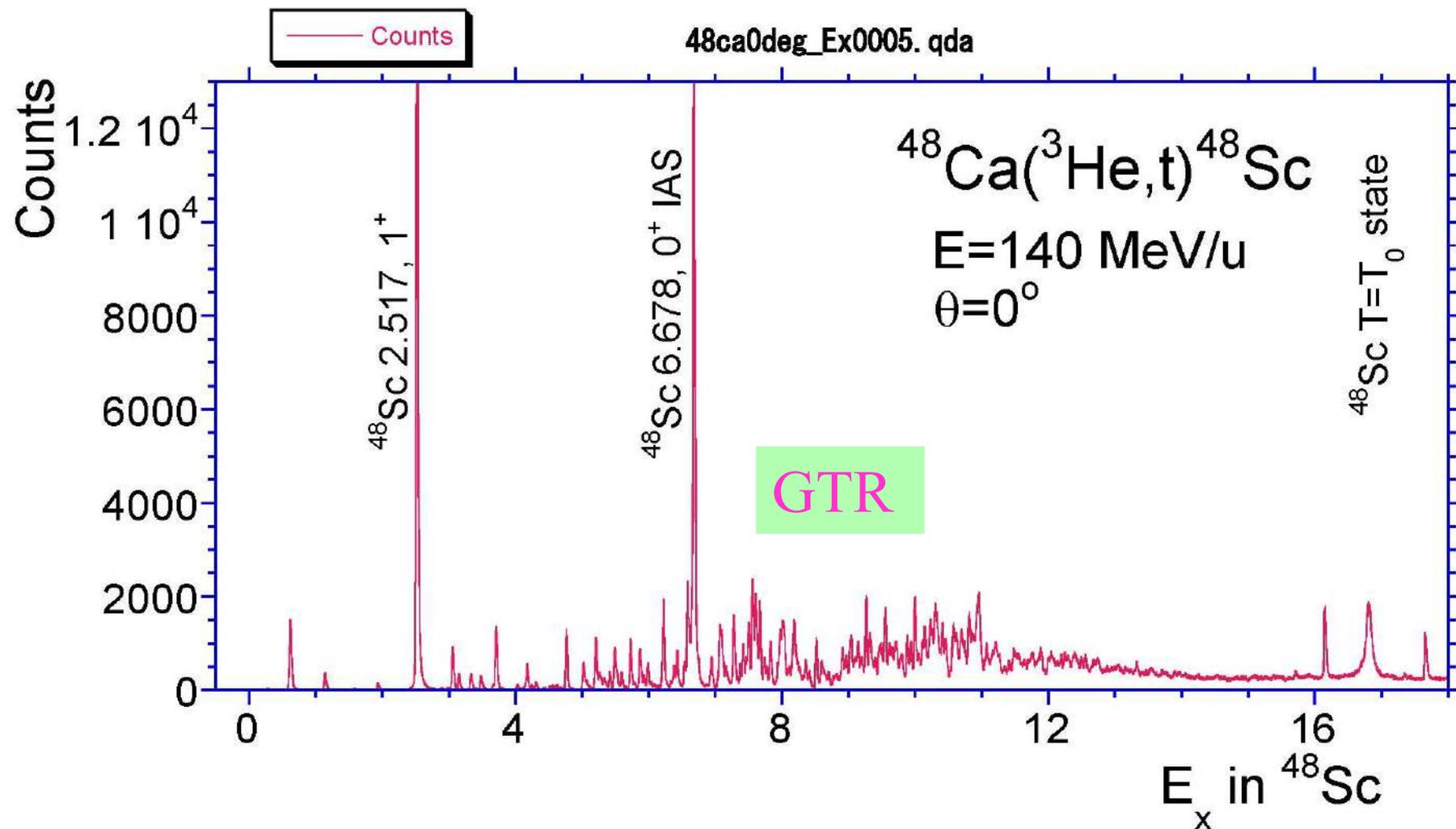
$^{44}\text{Ca}(^3\text{He},t)^{44}\text{Sc}$



$^{48}\text{Ca}(^3\text{He},t)^{48}\text{Sc}$



$^{48}\text{Ca}(^3\text{He},t)^{48}\text{Sc}$



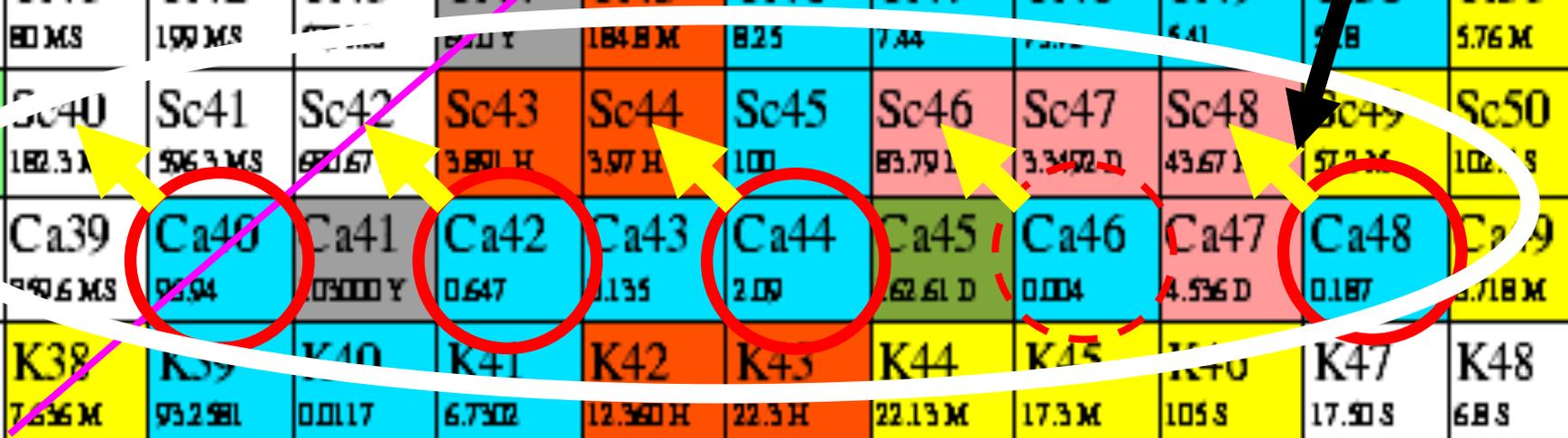
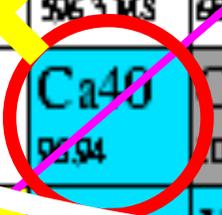
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Sc40	Sc41	Sc42	Sc43	Sc44	Sc45	Sc46	Sc47	Sc48	Sc49	Sc50	Sc51	
182.3 M	506.3 MS	6.2167	3.891 H	3.97 H	100	83.791	3.3072 D	43.671	57.2 M	102.0 S	12.4 S	
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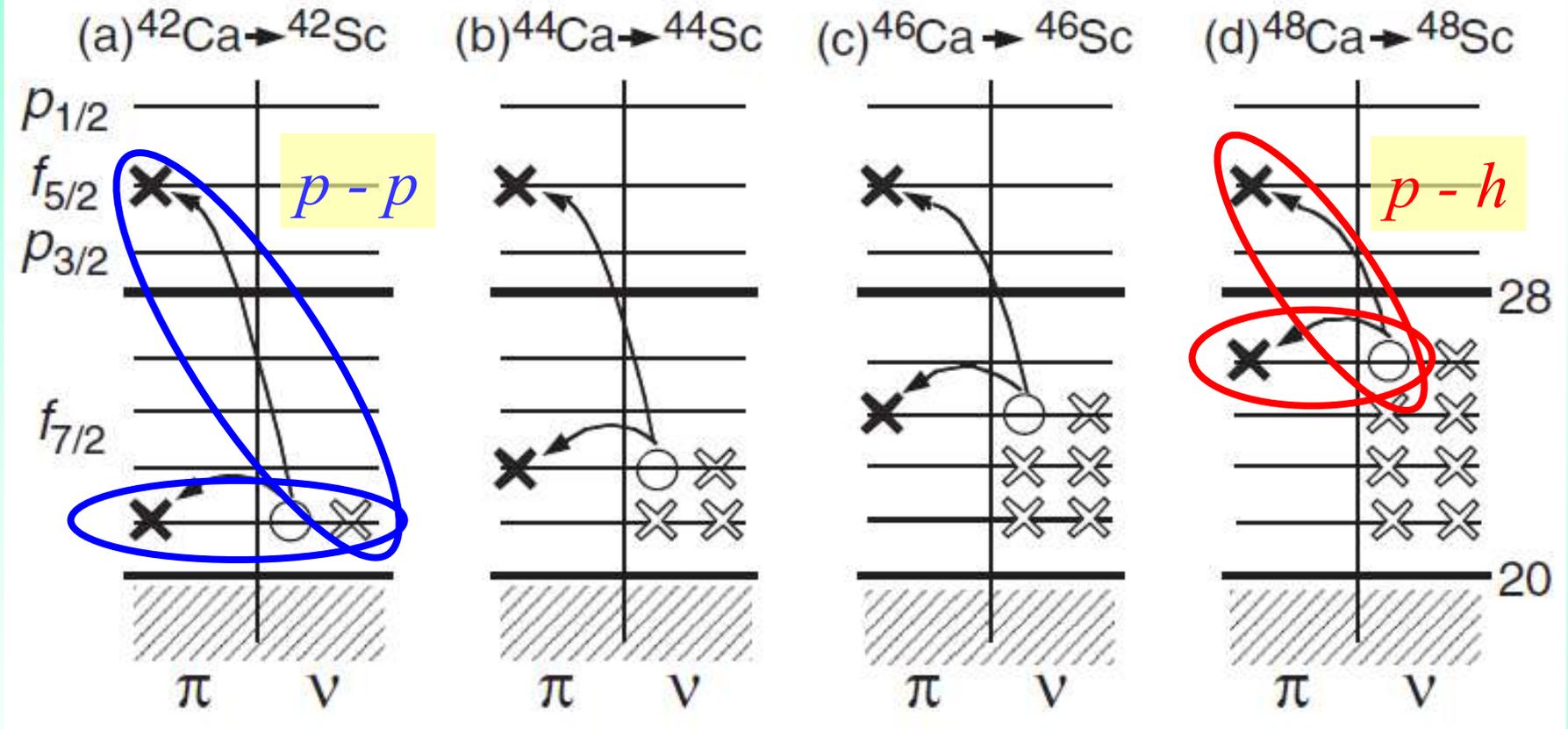
GT transitions from Ca isotopes

N=Z line

Transition in the β^- direction!



GT Configurations in Sc isotopes



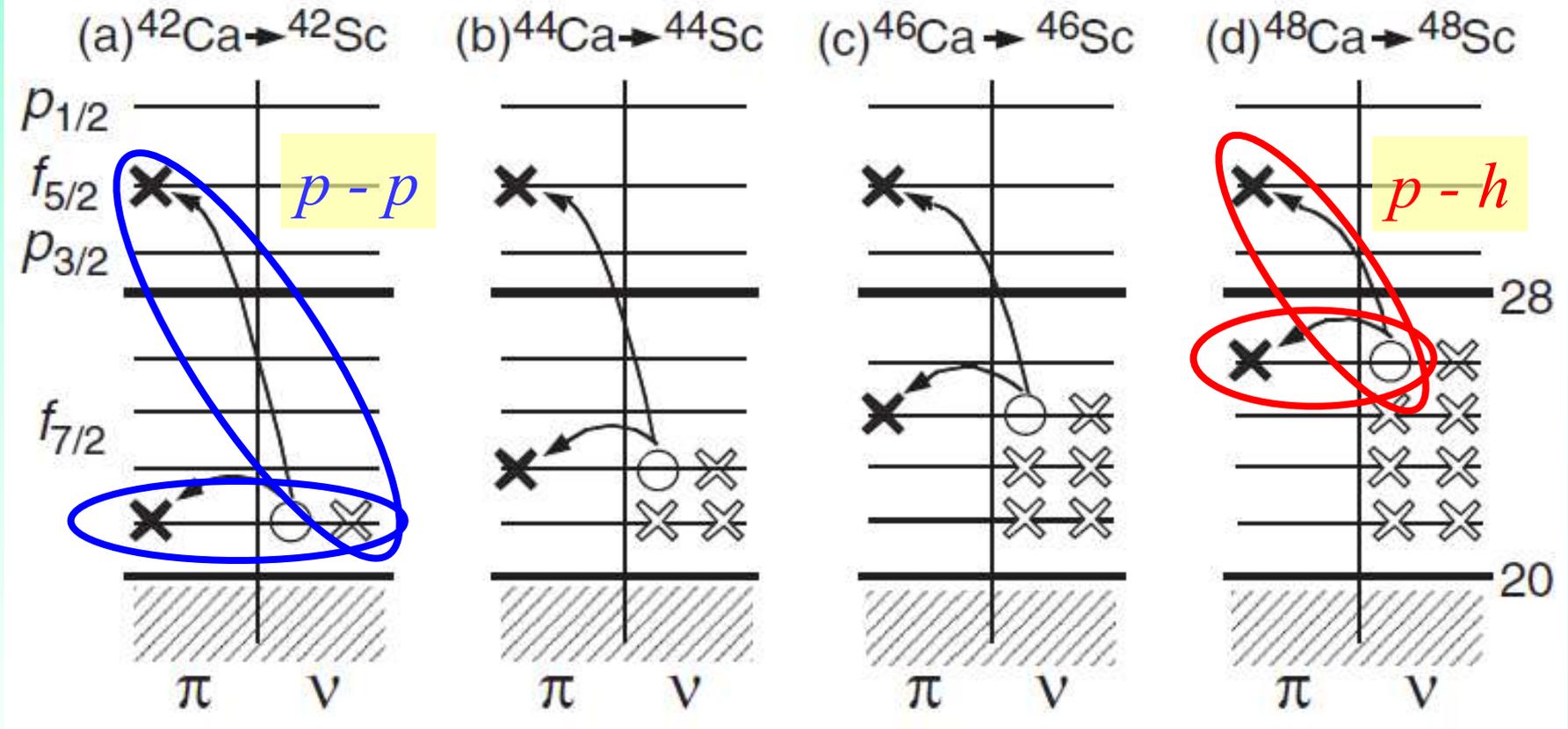
particle-particle int. (attractive) \longrightarrow

particle-hole int. (repulsive)

Low-energy
Super GT state
Is formed !

Gamow-Teller
Resonance
Is formed !

GT Configurations in Sc isotopes



particle-particle int. (attractive)

particle-hole int. (repulsive)

Low-energy
Super GT state
Is formed !

Gamow-Teller
Resonance
Main Player:
Isovector interaction !

Role of Residual Int. (repulsive case)

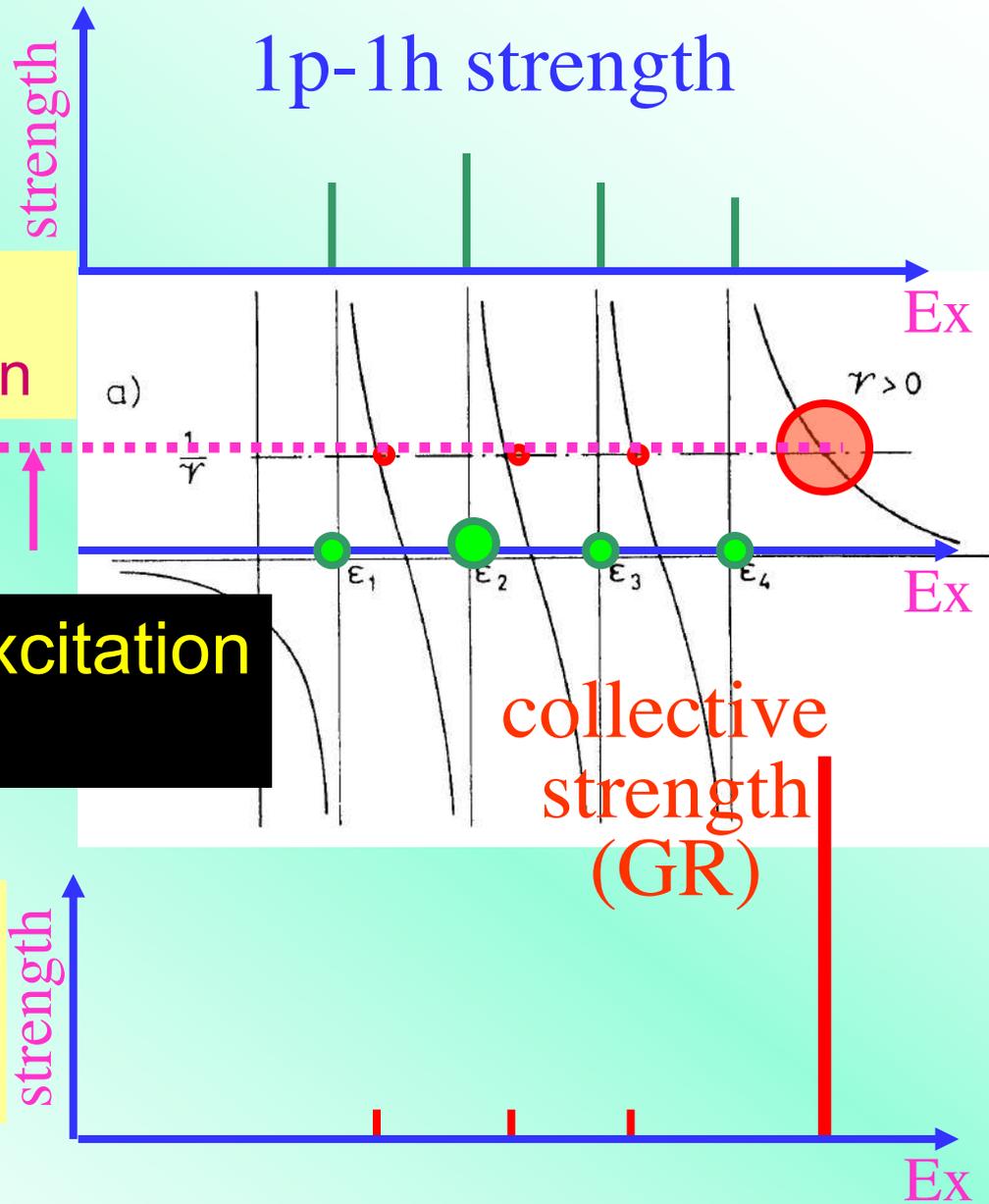
Single particle-hole strength distribution

Graphical solution of the RPA dispersive eigen-equation

positive = repulsive

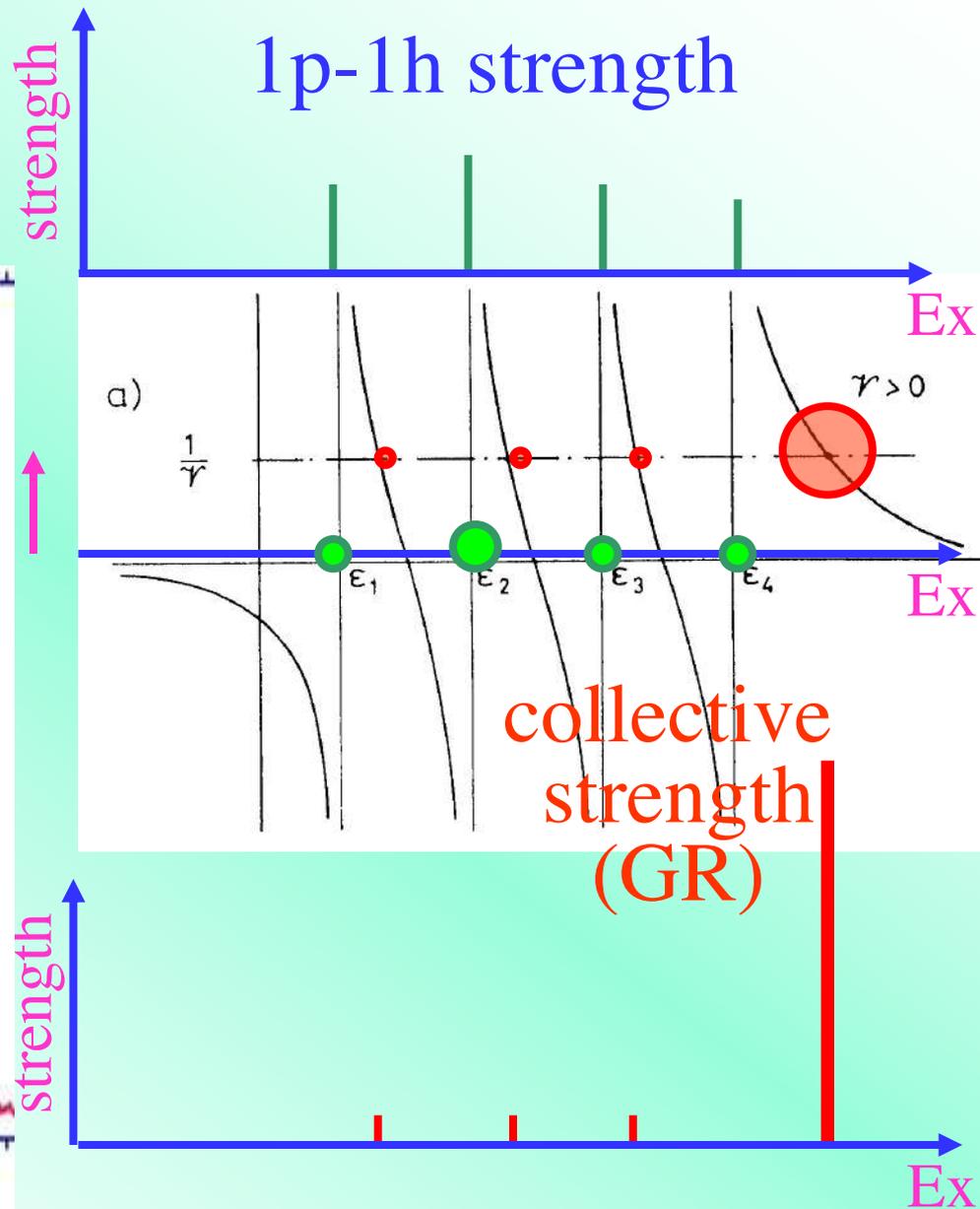
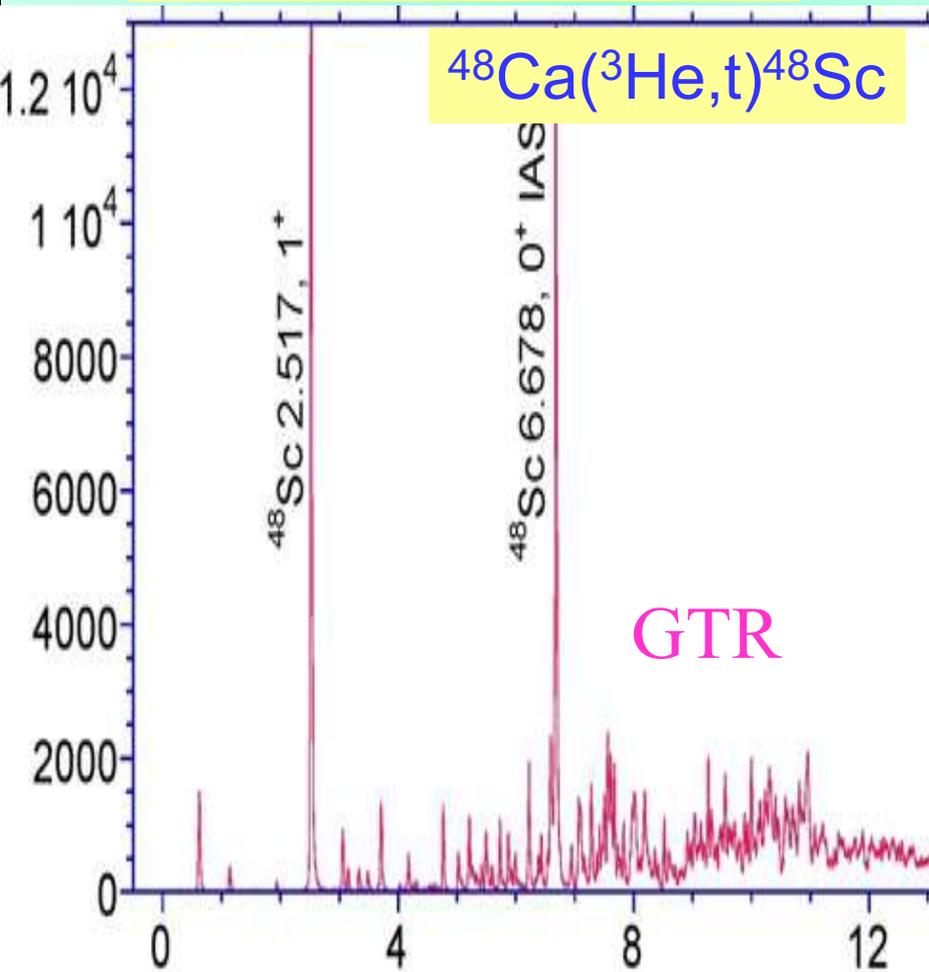
$p - h$ configuration + IV excitation = repulsive

Collective excitation formed by the repulsive residual interaction

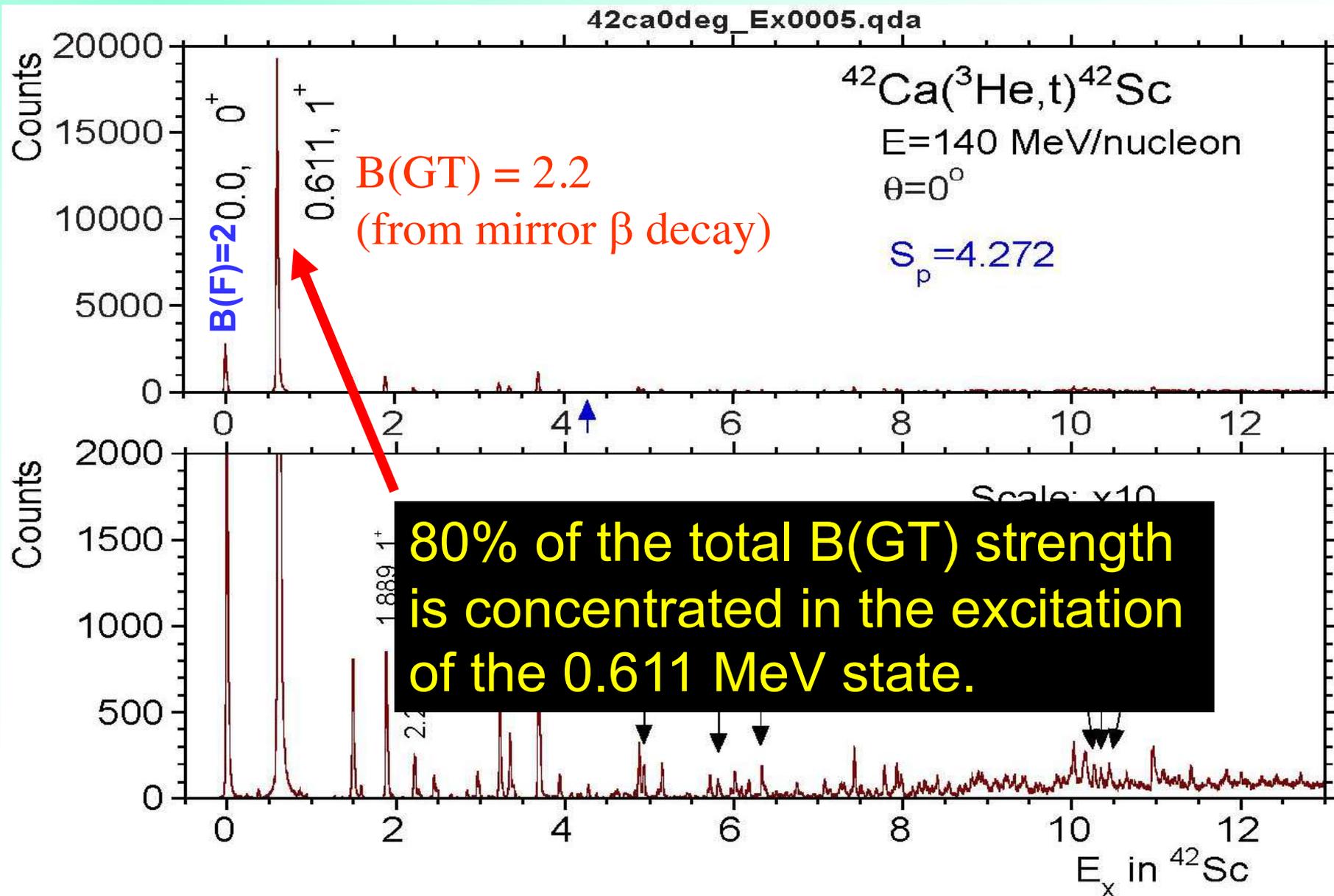


Role of Residual Int. (repulsive)

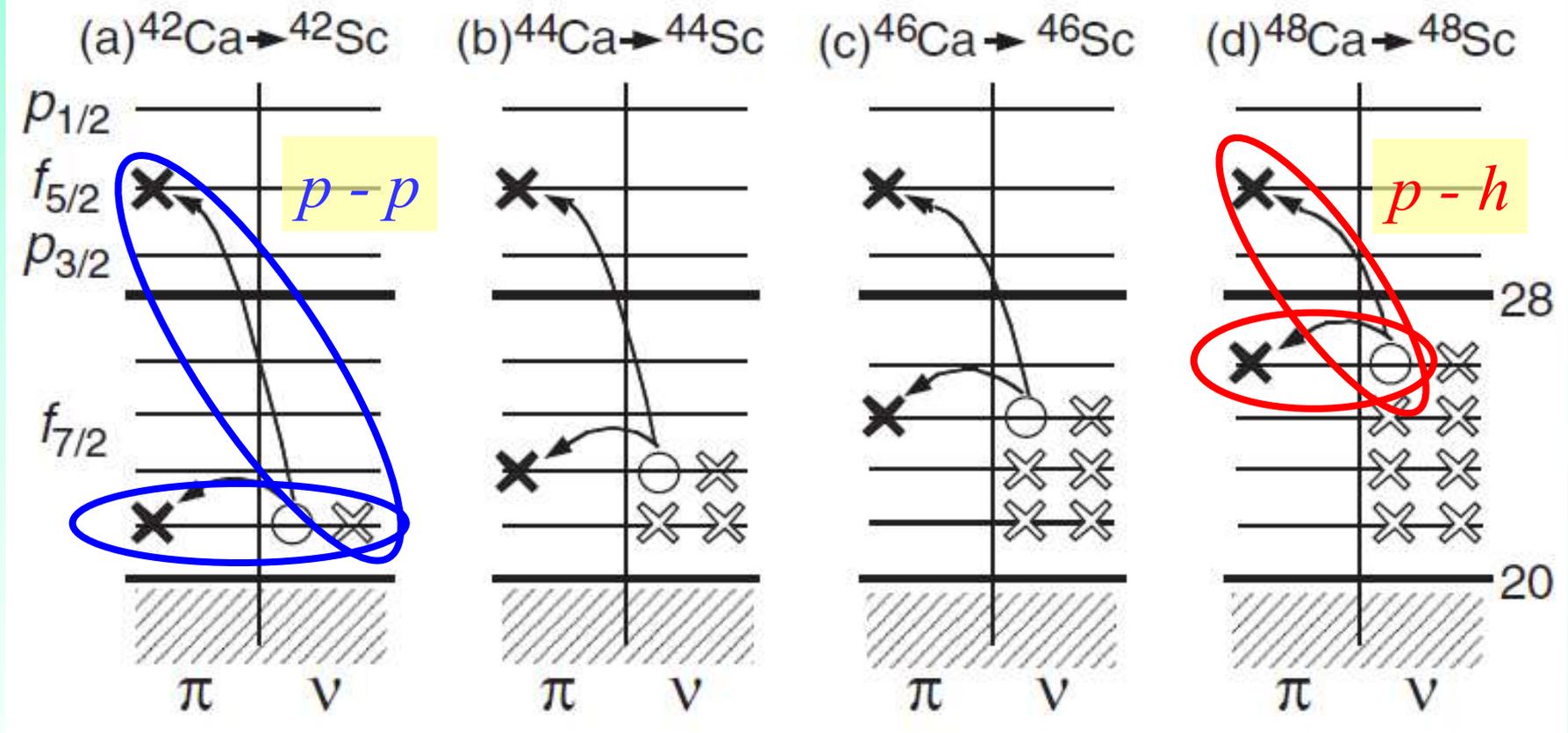
GTR is formed by the
IV-type Repulsive
residual interaction



$^{42}\text{Ca}(^3\text{He},t)^{42}\text{Sc}$ in 2 scales



GT Configurations in Sc isotopes



particle-particle int. (attractive)



particle-hole int. (repulsive)

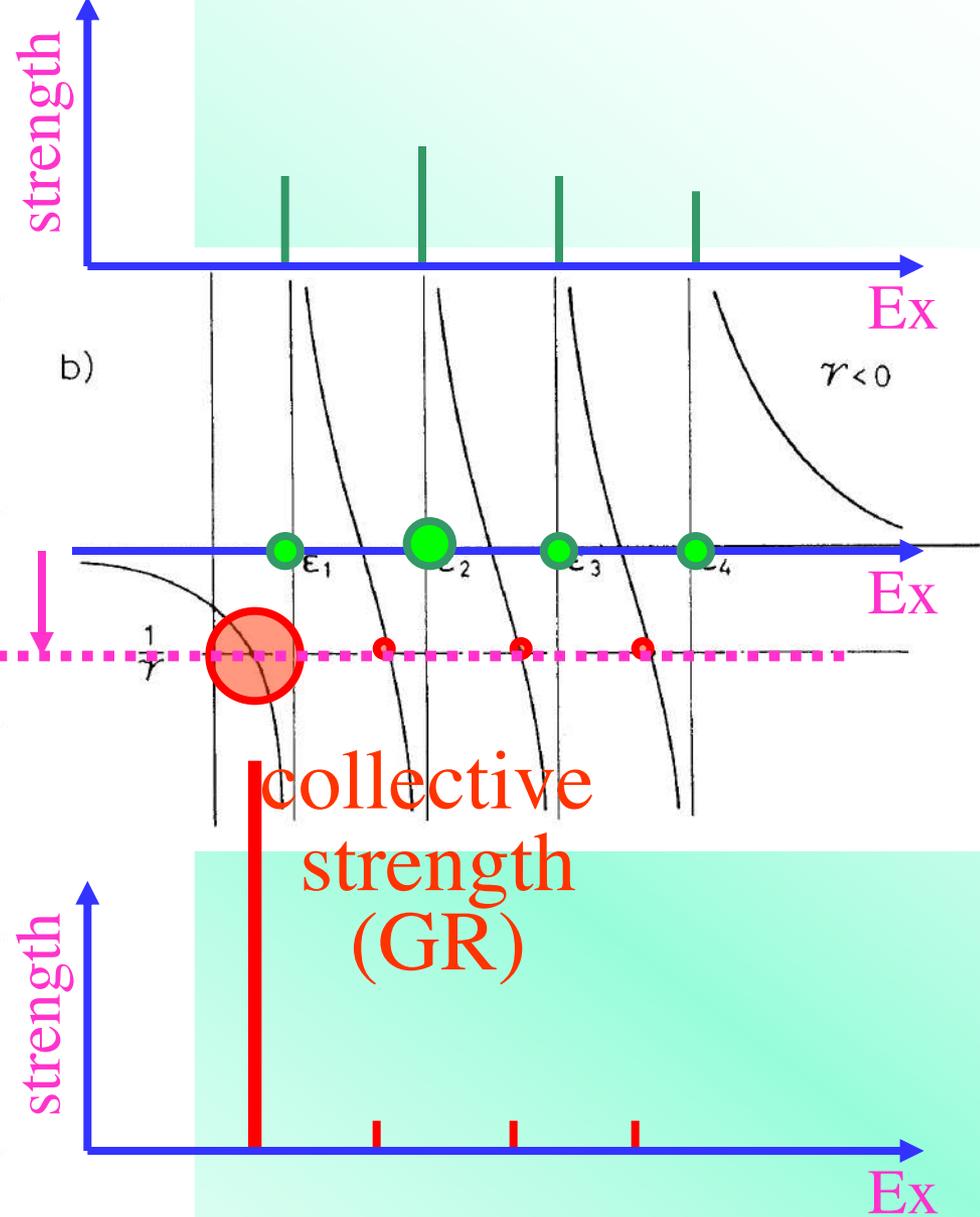
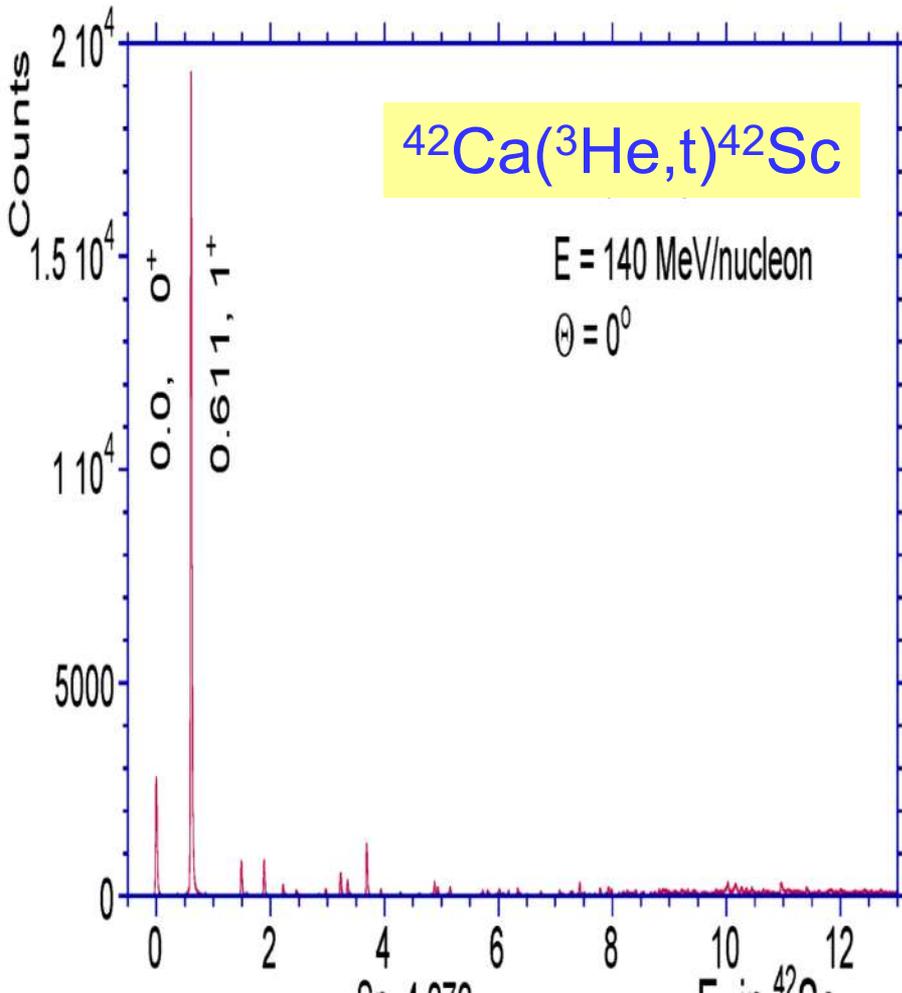
Low-energy Super GT state
Main Player:
Isoscalar interaction !

Gamow-Teller Resonance Is formed !

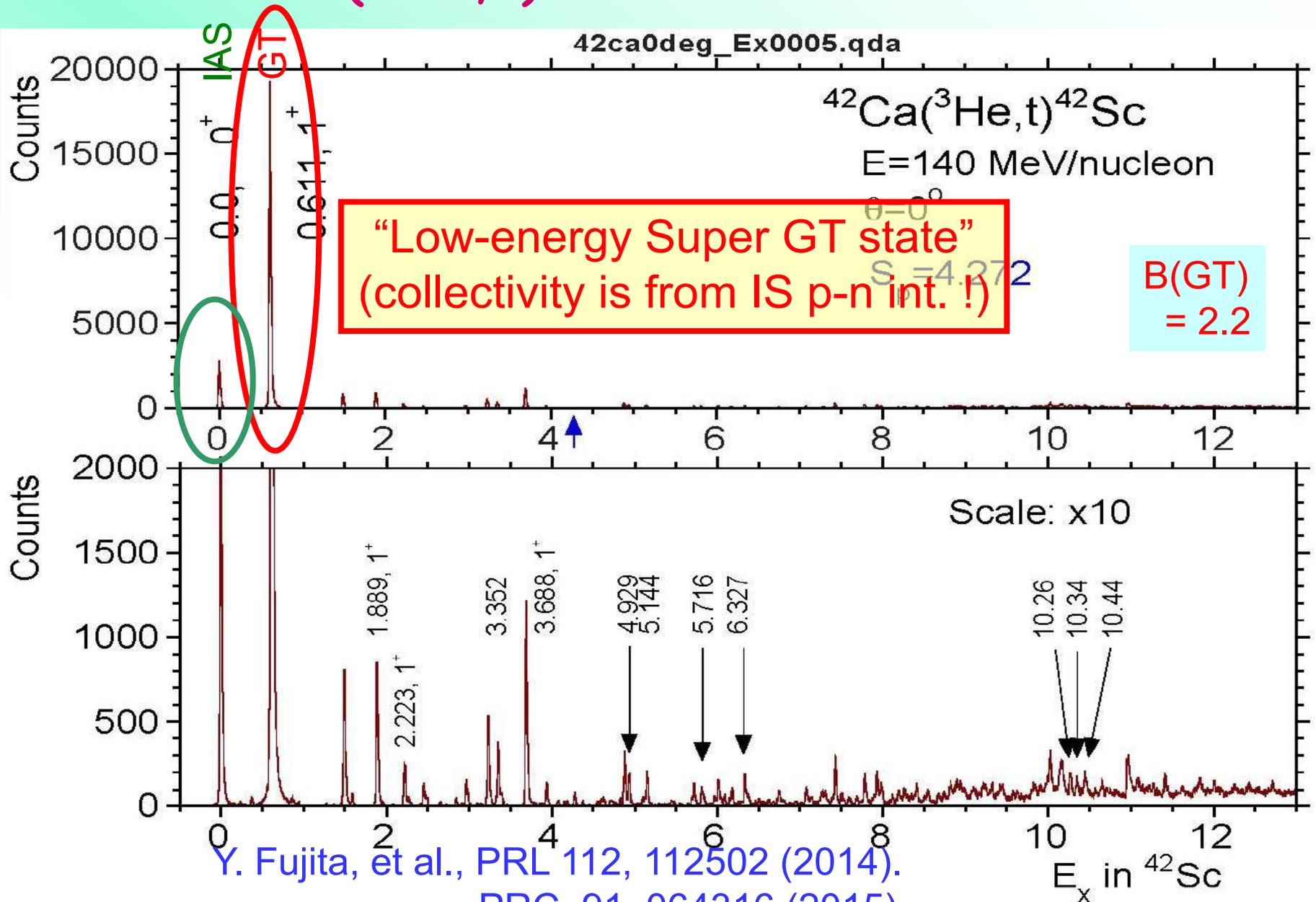
Role of Residual Int. (attractive)

Bai, Sagawa, Colo et al., PRC 90 ('14)

Collective excitation formed by the attractive IS residual interaction

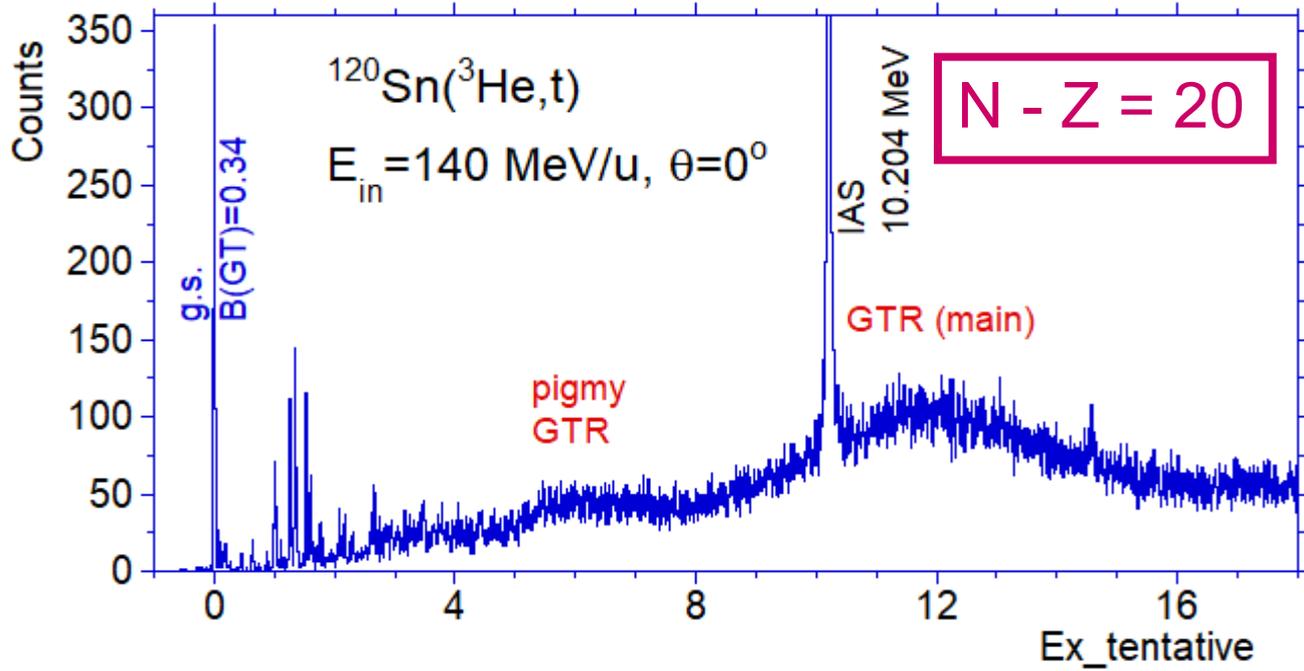
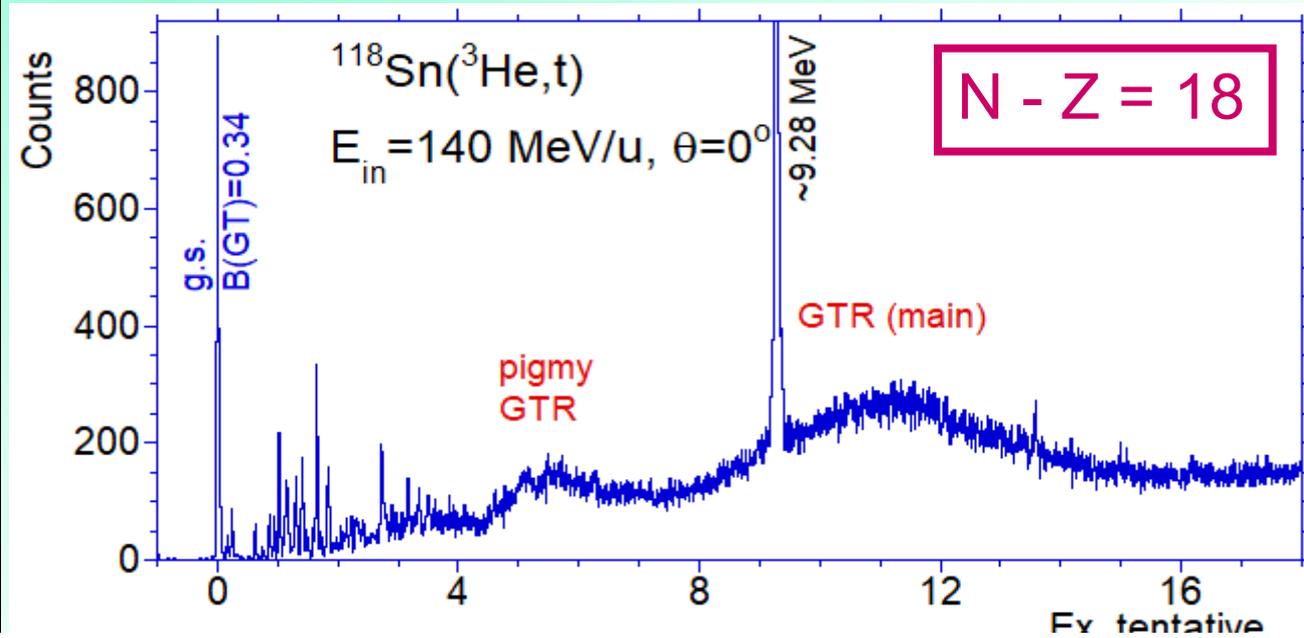


$^{42}\text{Ca}(^3\text{He},t)^{42}\text{Sc}$ in 2 scales



Y. Fujita, et al., PRL 112, 112502 (2014).
 PRC 91, 064316 (2015).

GT transitions in $^A\text{Sn} \rightarrow ^A\text{Sb}$ CE reactions



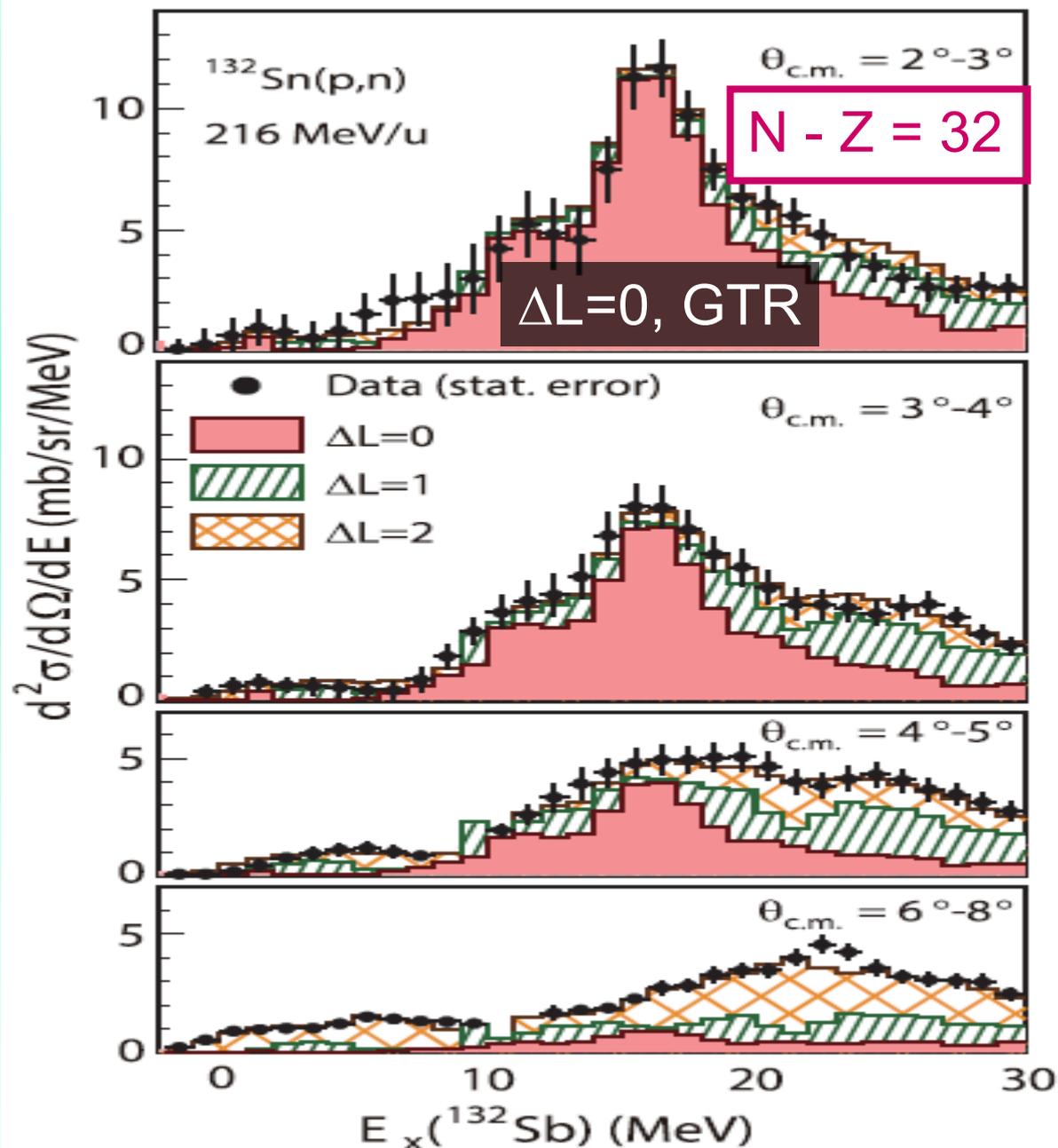
Scenario

- A) In $N \gg Z$ nuclei, GT ex. has $p-h$ nature.
- B) In $p-h$ configurations, IV-type int. is active.
- C) Due to the repulsive nature of IV residual interaction, the GT strength is pushed up.
- D) With increasing $N-Z$, the GT strength is pushed up more.

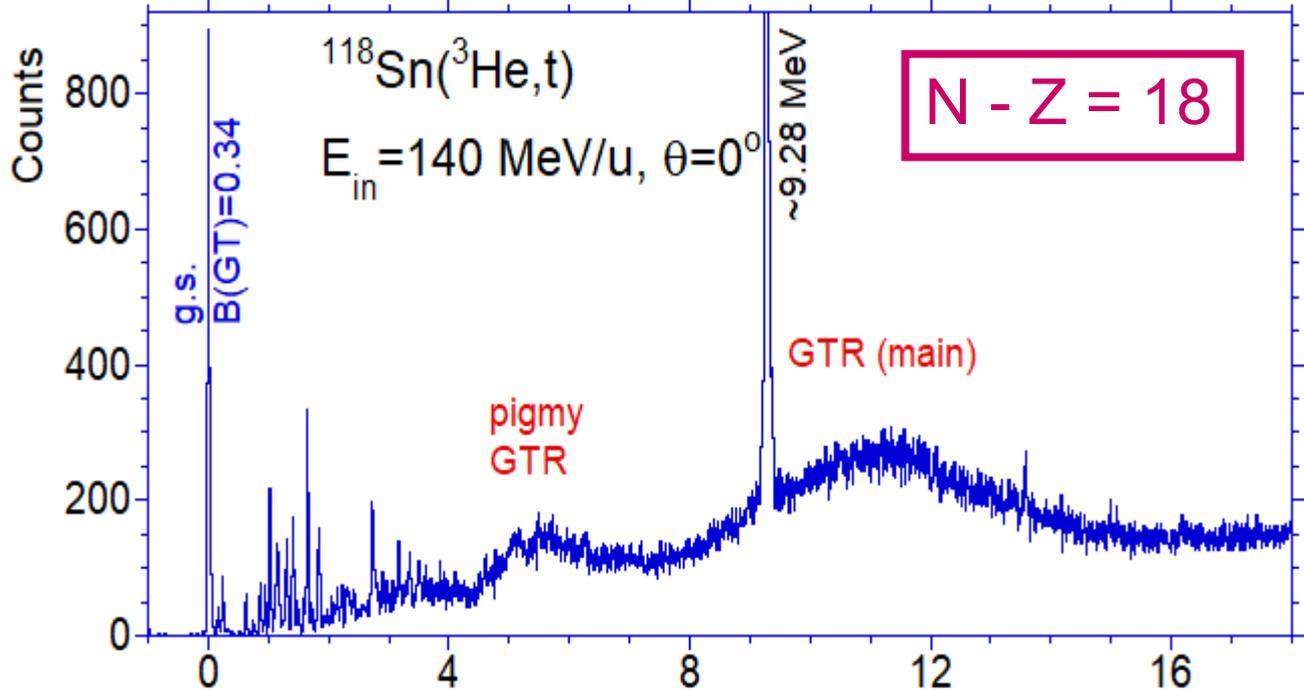
$^{132}\text{Sn}(p, n)^{132}\text{Sb}$ @ RIBF RIKEN (Angular-dis. Ana.)

The result of MDA
(Multi-Pole Decomp. Ana.)
shows that GTR is
at $E_x \sim 16.3$ MeV
width $\Gamma \sim 4.7$ MeV.

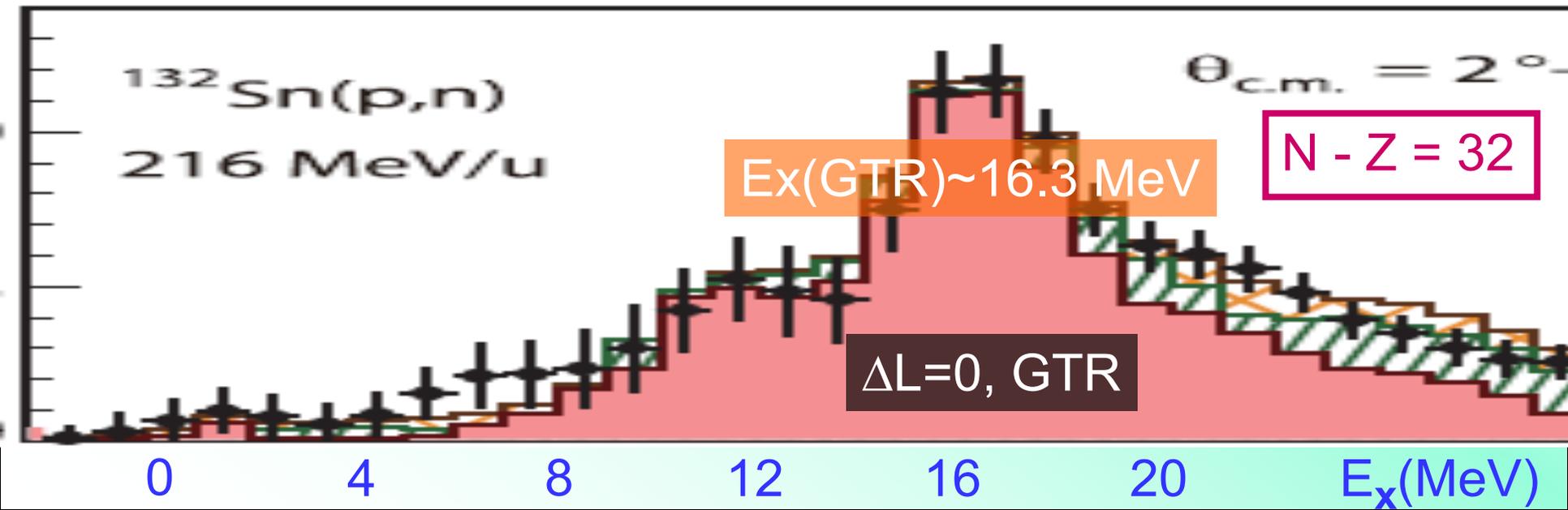
J. Yasuda et al.,
PRL 121, 132501 (2018)



GT transitions in $^A\text{Sn} \rightarrow ^A\text{Sb}$ CE reactions



Ikeda Sum Rule
 $B(\text{GT}) \sim 3(N - Z)$



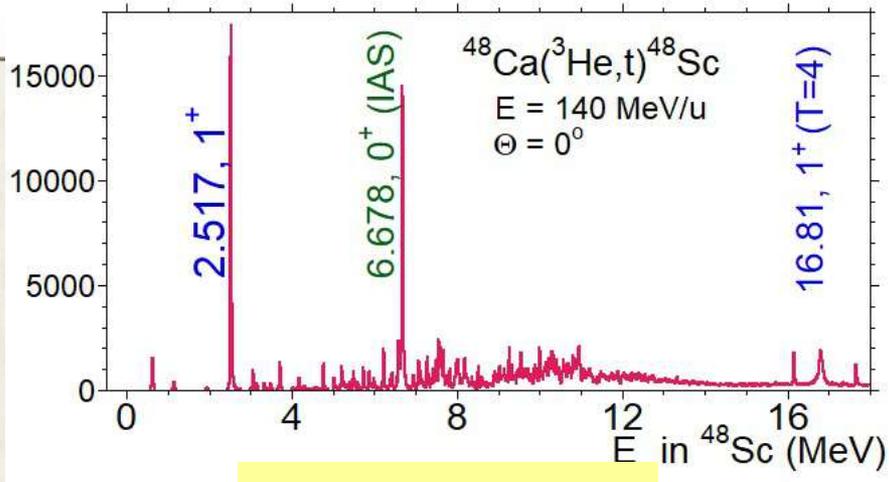
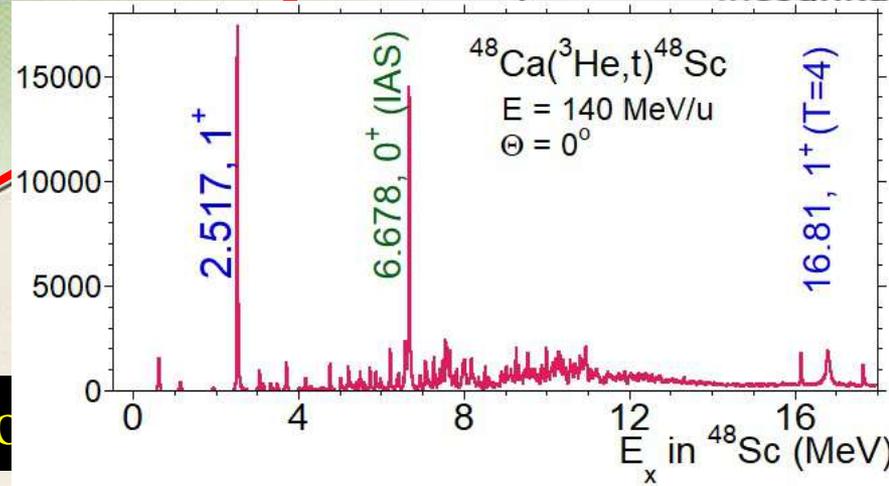
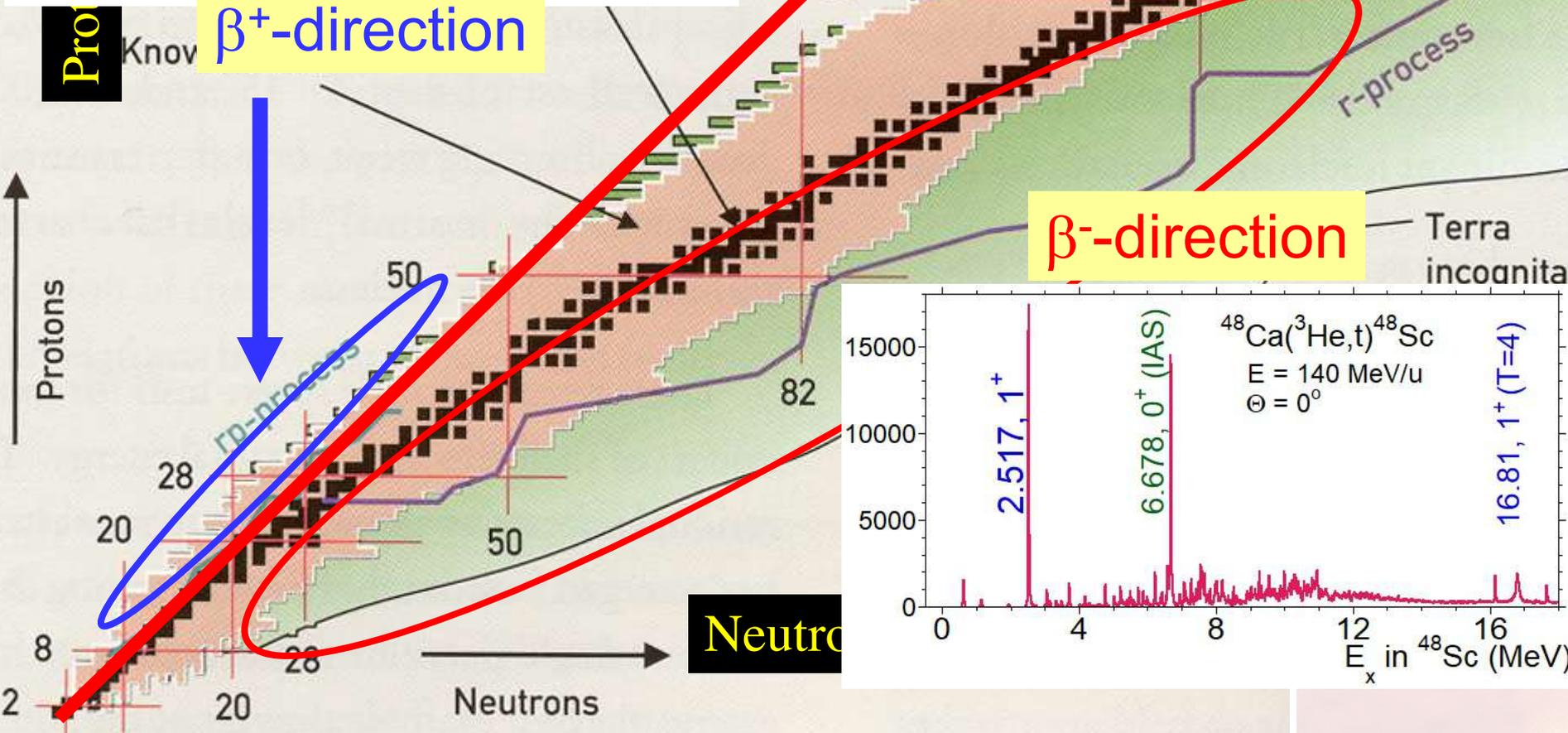
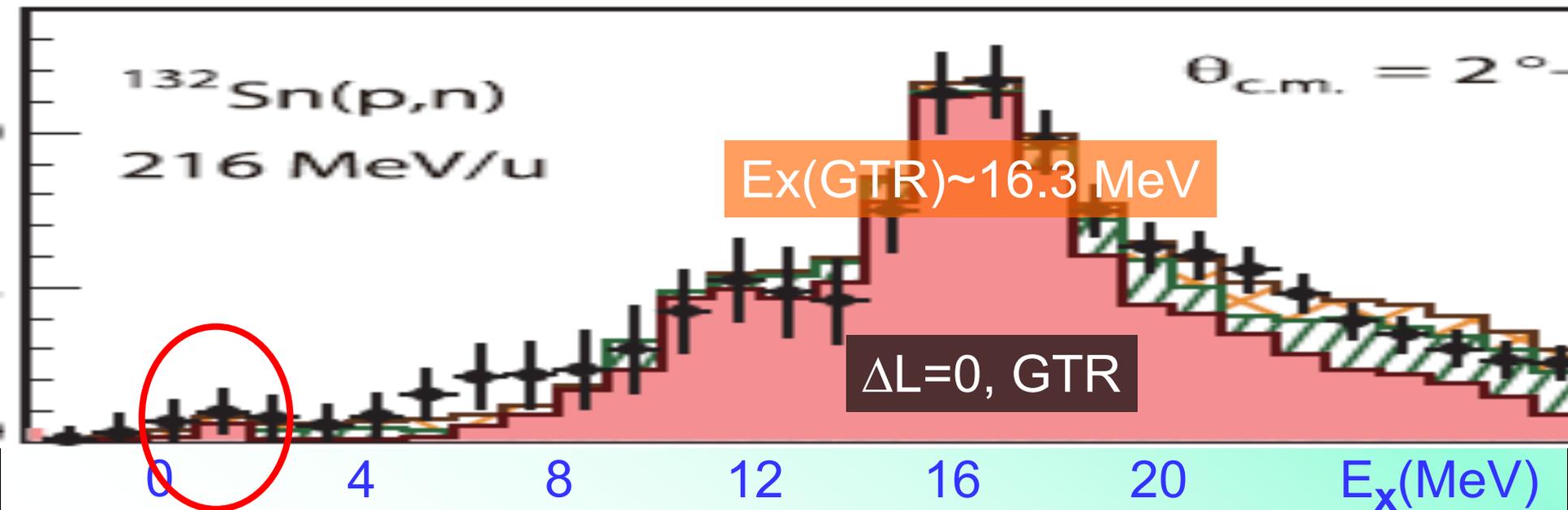
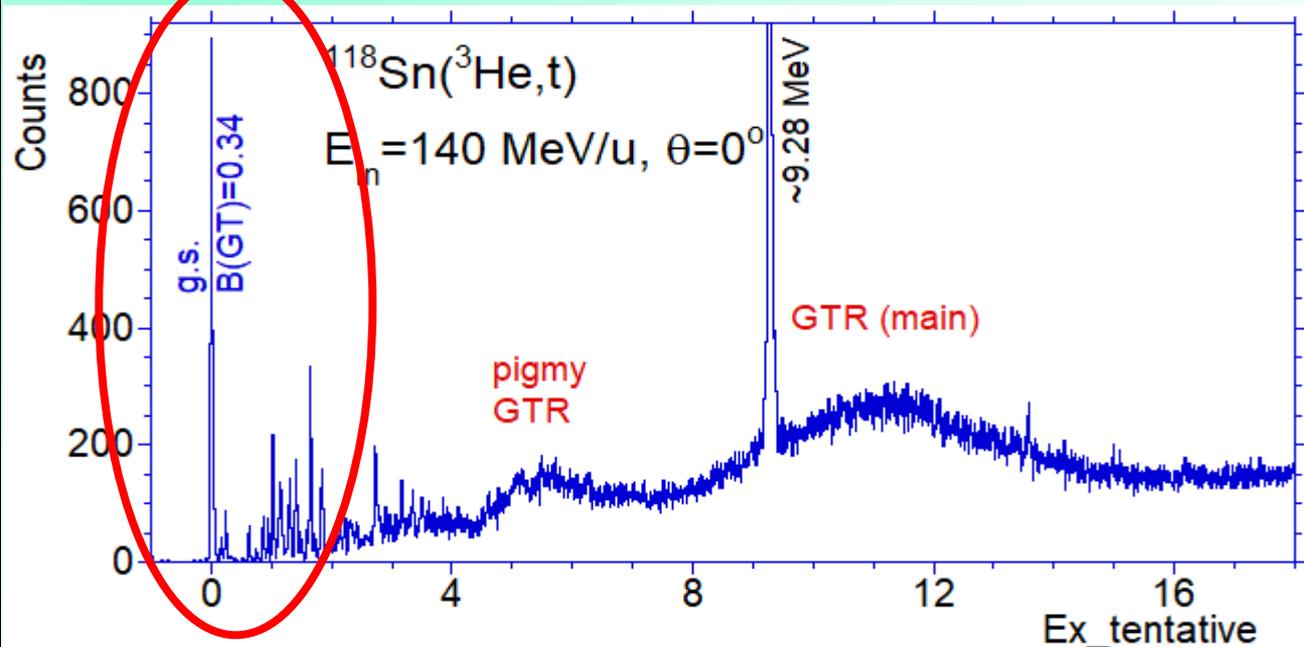


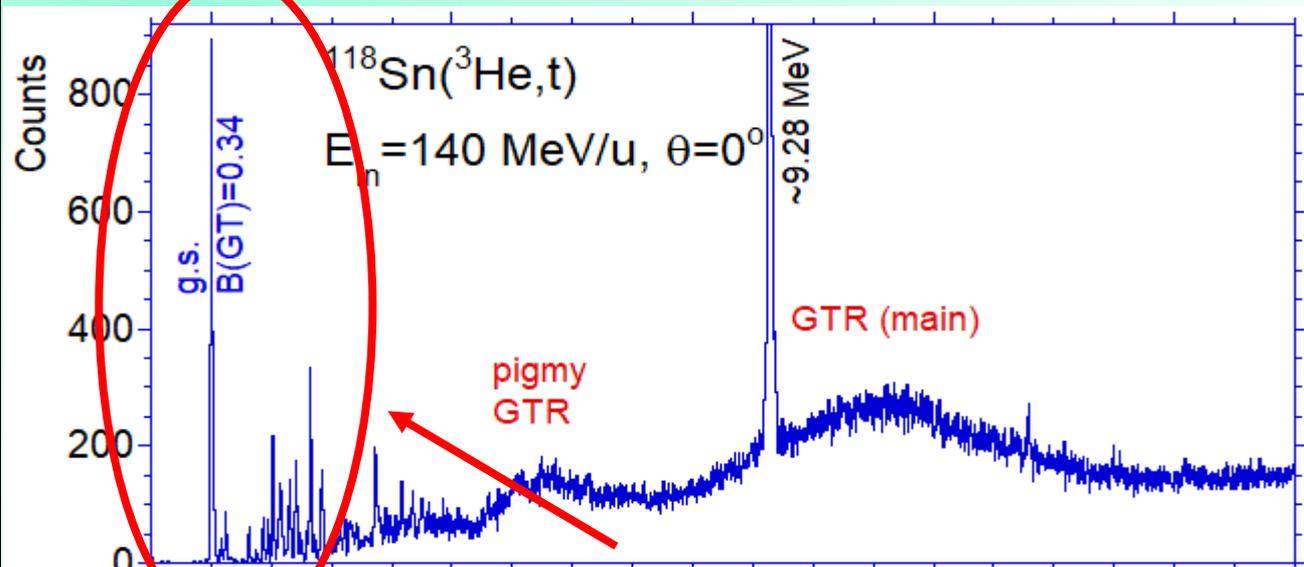
Chart Landscape



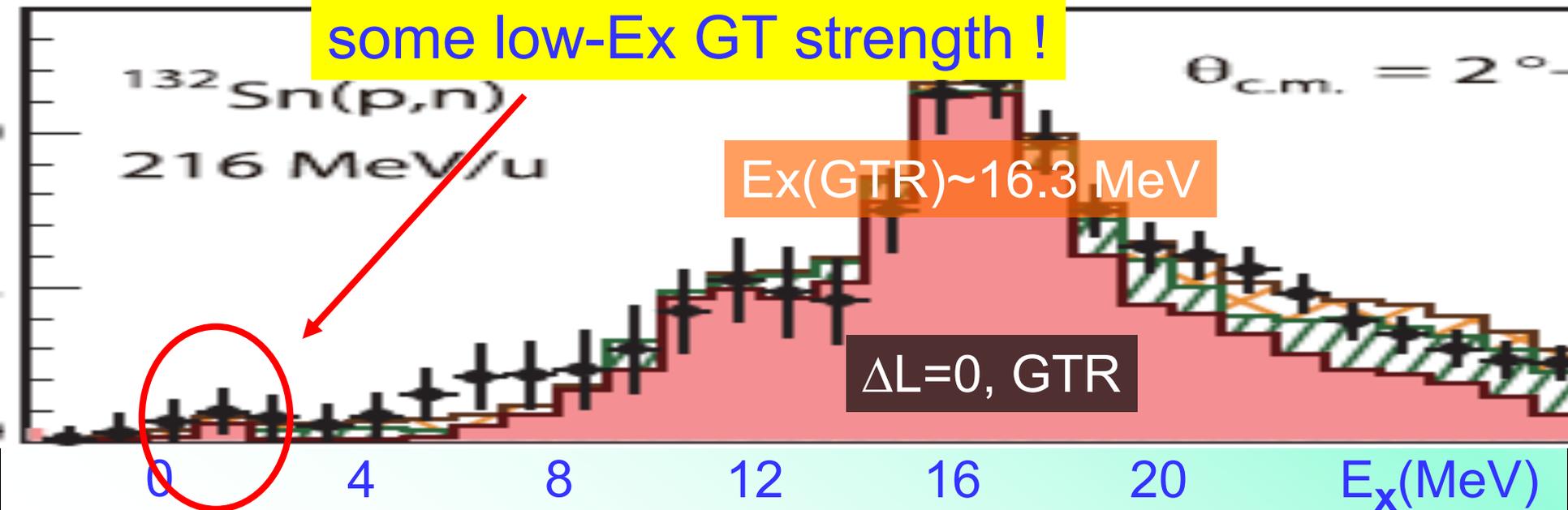
GT transitions in ${}^A\text{Sn} \rightarrow {}^A\text{Sb}$ CE reactions



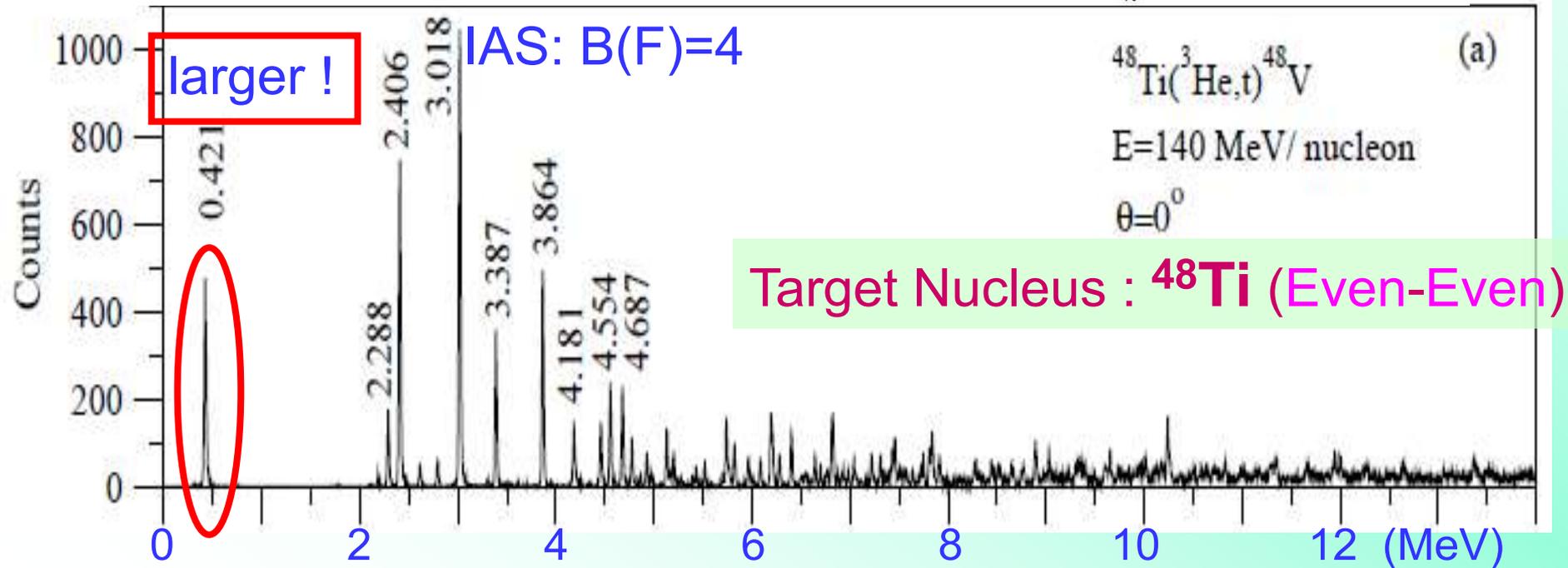
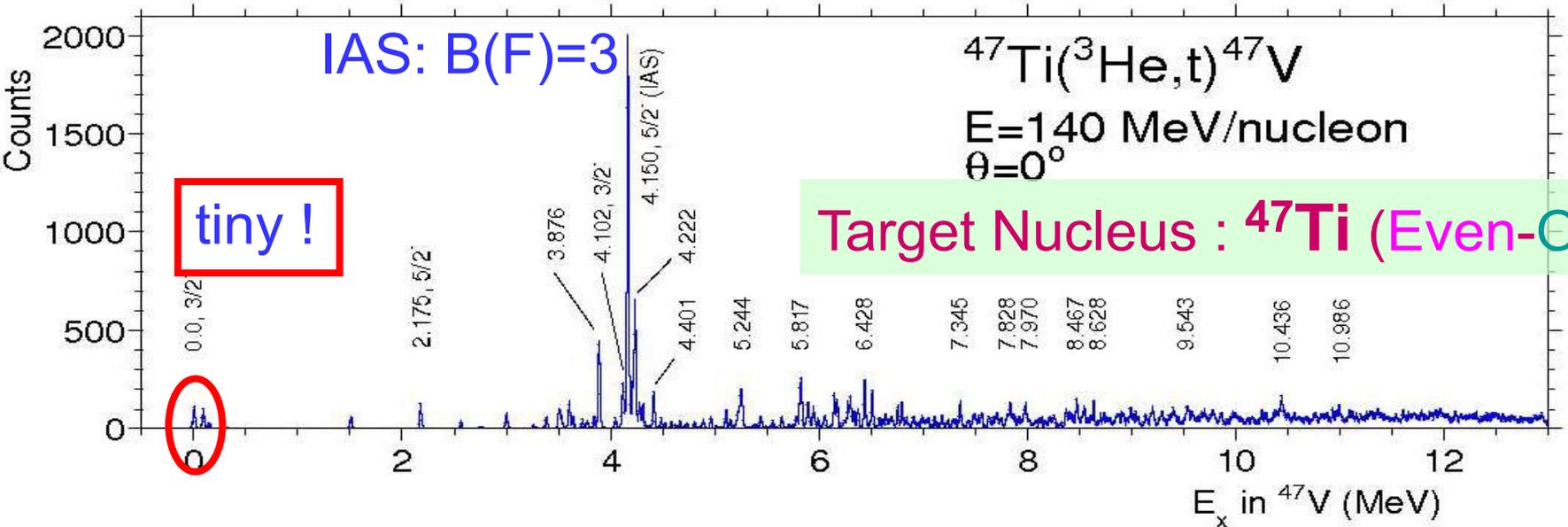
GT transitions in $^A\text{Sn} \rightarrow ^A\text{Sb}$ CE reactions



There always remains some low-Ex GT strength !



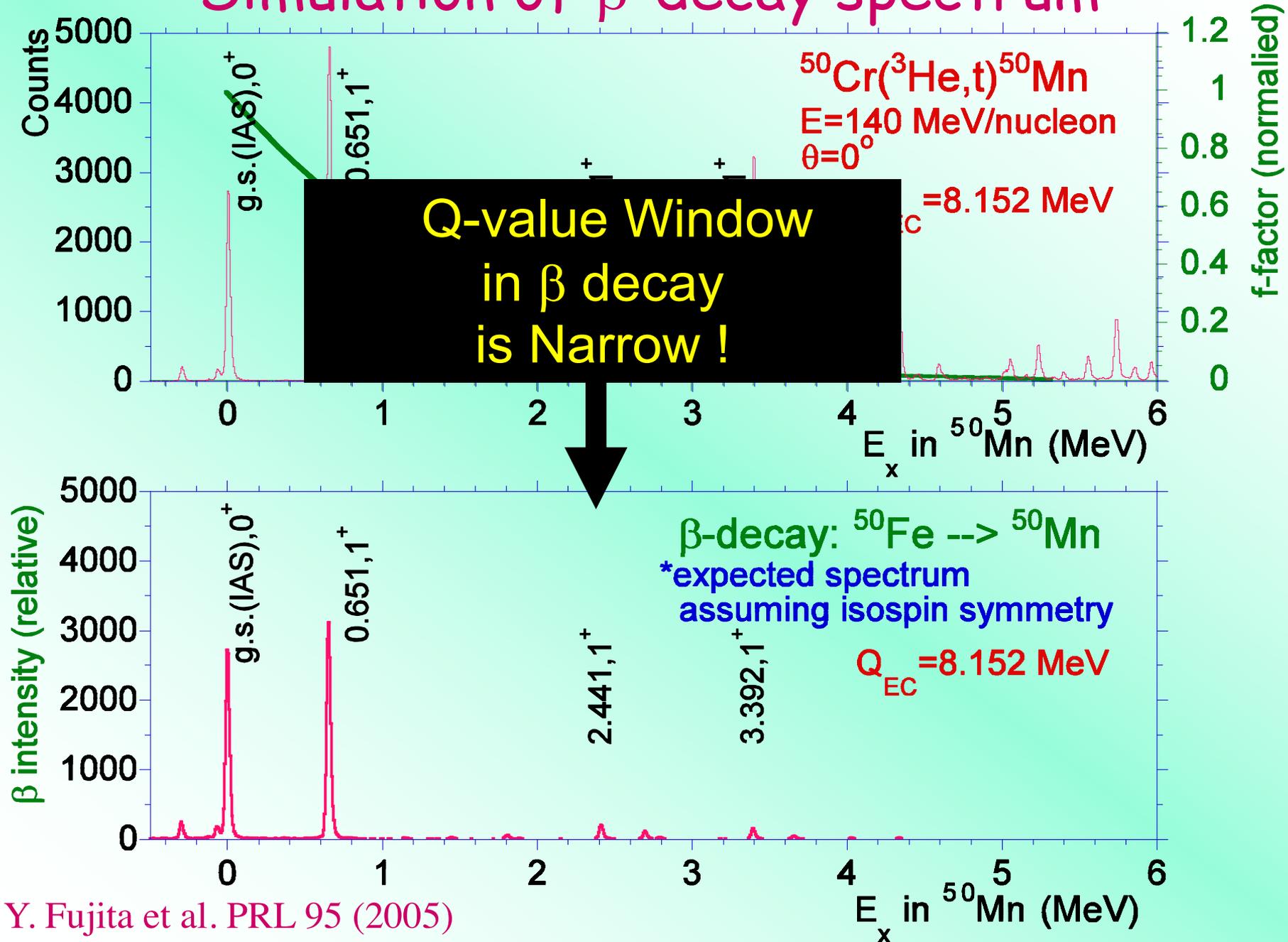
Low-Ex GT strength: Even-Odd vs. Even-Even



Interpretation of CE results into β^- decay results

*** Q-value limitation

Simulation of β -decay spectrum



Interpretation of CE results into β^- decay results

*** Q-value limitation

GTR region usually makes no contribution !

Fermi transition cannot make contribution !

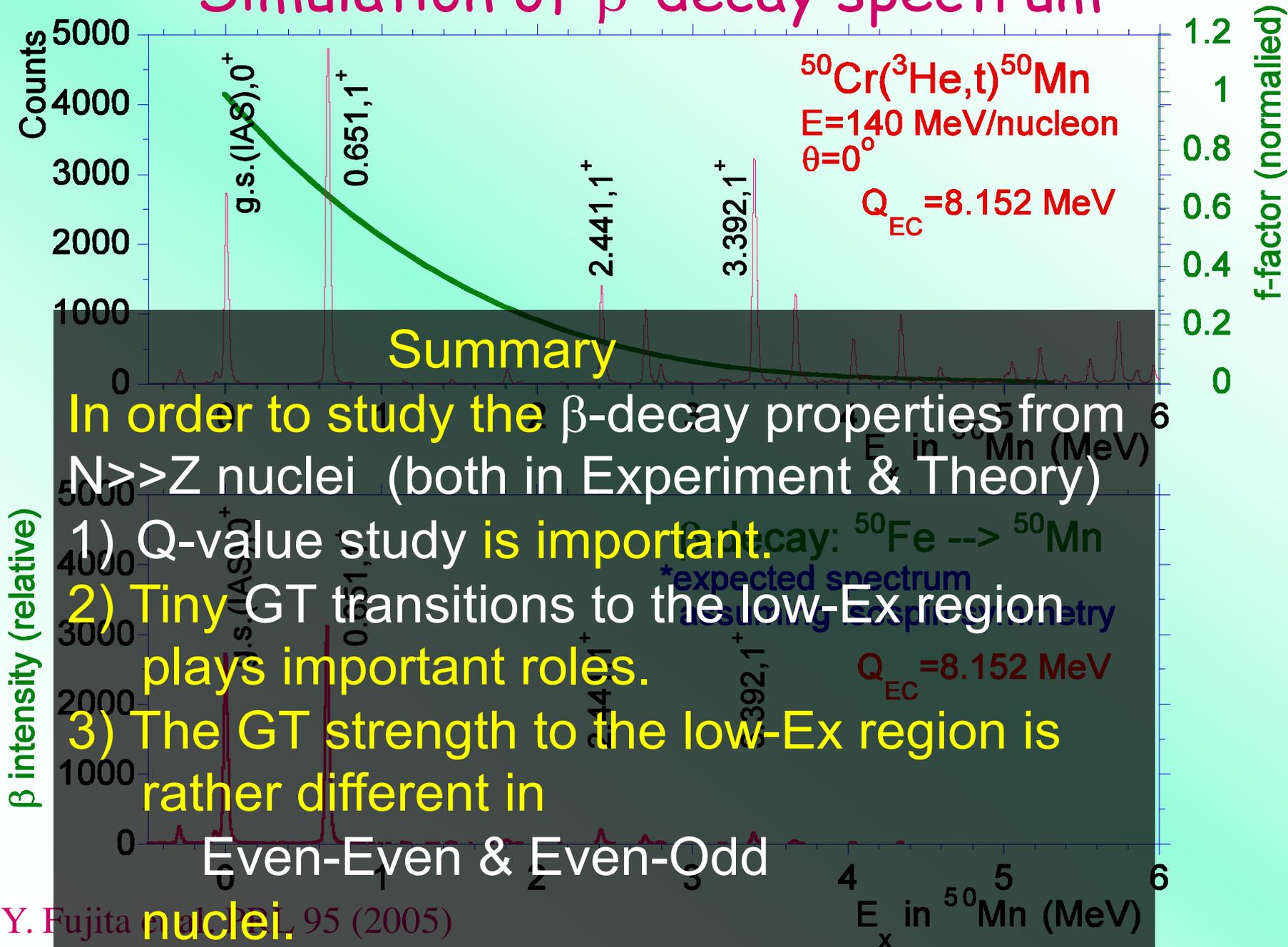
[Y. Fujita et al. PPNP 66 (2011) 549]

*** GT transitions to the low-Ex region although weak, have large weight.

*** GT transitions to the low-Ex region: different in Even-Even & Even-Odd nuclei !

→ T1/2 can be largely different !

Simulation of β -decay spectrum





End of publicity