#### Systematic Study of Radial and Elliptic Flows in High-Energy Heavy-Ion Collisions

A. Ohnishi<sup>a</sup>, P.K. Sahu<sup>b</sup>, M. Isse<sup>a</sup>, N. Otuka<sup>c</sup>, and Y. Nara<sup>d</sup>

- <sup>a</sup> Div. of Phys., Grad. School of Sci., Hokkaido Univ., Sapporo 060-0810, Japan
- <sup>b</sup> Institute of Physics, Bhubaneswar, India
- <sup>c</sup> VBL, Hokkaido Univ., Sapporo, Japan
- <sup>d</sup> RIKEN-BNL Research Center, BNL, NY, USA

#### Our Refs.

- Y. Nara, N. Otuka, A. Ohnishi, T. Maruyama, Prog. Theor. Phys. Suppl. 129 (1997) 33.
- Y. Nara, N. Otuka, A. Ohnishi, K. Niita, S. Chiba, Phys. Rev. C 61 (2000), 024901. (JAM)
- P. K. Sahu, W. Cassing, U. Mosel and A. Ohnishi, Nucl. Phys. A672 (2000), 376. (RBUU, Flow)
- N. Otuka, P.K. Sahu, M. Isse, Y. Nara and A. Ohnishi, nucl-th/0102051 (RHIC, radial flow)
- P.K. Sahu, N. Otuka, N. Ohnishi, Pramana-J. Phys., in press; nucl-th/0206010 (RHIC, v2)

### Contents

- $\star$  Hydrodynamical Signals of QGP at RHIC
  - ... Re-Hardening and Early Thermalization
- $\star$  Hadron-String Cascade Model from SIS to RHIC (JAM)
- $\star$  Hadronic Spectra from SIS to RHIC
- $\star$  Elliptic Flow from SIS to RHIC
- \* Summary

## $\star$ Hydrodynamical Signals of QGP at RHIC

- Proposed and Observed Signals of QGP
  - \* Anomalous  $J/\psi$  supression: Uncertain  $\sigma(hh)$
  - $\star$  Strangeness Enhancement: Uncertain  $\sigma(hh)$
  - \* Low-E Dilepton Enh.: Partial Chiral Restoration
  - $\star$  Softening of particle spectra: Hagedorn Gas
  - \* Jet Energy Loss: Dense Partonic Gas (not fixed yet ?)

← Clear Bulk/Hydrodynamical Signal is desired. → Strong Radial and Elliptic Flows at RHIC

#### • Observed "Re-Hardening" Signature

Nu Xu and M. Kaneta, NPA698(2002), 306; nucl-ex/0104021



Strong Radial Flow Appears at RHIC !

#### • Strong Elliptic Flow EOS,E895,E877,NA49,STAR



• Naive Expectations



If QGP is formed,

\* Pressure is expected to Grow Again (Bag Model).  $\rightarrow$  Larger Radial Flow

\* Thermalization Time would be Much Shorter (Free from Hadronic Formation Time,  $\tau \sim 1 \text{ fm/c}$ ).  $\rightarrow$  Larger Elliptic Flow In this work,

- \* We analyze radial and elliptic flows from SIS to RHIC energies systematically in a realistic dynamical hadron-string cascade model including mini-jet production (JAM).
- $\star$  We will show that Hadron Rapidity and  $m_{T}$  Spectra are well explained EXCEPT for very stiff proton and anti-proton  $m_{T}$  spectra at RHIC,
- \* and that Elliptic Flows are in the Range of Hadron-String Cascade when Mean Field Effects are included up to SPS energies, but we CANNOT explain Strong Elliptic Flow at MID-RAPIDITIES in RHIC.

### **\*** Hadron-String Cascade Model from SIS to RHIC

JAM (Jet Aa Microscopic transport model)

Y. Nara et al., PRC61('00), 024901.

DOF:  $h(B, B^*, M, M^* (m \le 2 \text{ GeV})) + s(\text{Strings}) + \text{Mini-Jet Partons}$ 

 $\sigma$ : Hadronic ( $hh \leftrightarrow hh$ ,  $hh \leftrightarrow h$ ) + Soft [1,2] + Hard [3]



[1] "DPM + Lund" (~ HIJING) + Phase Space (hh↔s, hh→hs, hh→ss, s→hhh...)
[2] Consituent Rescattering (~ RQMD) (c= (qq), q, q ch↔ ch, ch→ cs (c= (qq), q, q))
[3] Jetset: Pythia (Mini-Jet Production)

# $\star$ Hadronic Spectra from SIS to RHIC

• Rapidity and  $m_T$  Distributions (N. Otuka et al. nucl-th/0102051)



 $\checkmark$  Good EXCEPT FOR anti-proton (and proton) m<sub>T</sub> spectra at RHIC

 $Sep. 30\text{-}Oct.4,\ 2002,\ PANIC02$ 

• Decomposition to T and  $\beta$ 

$$\frac{d^2 N}{M_t dM_t dY d\phi} \propto \exp(-M_t/T'), \quad T'(M) = T + \frac{1}{2} M \beta^2$$



• Temperature and Radial Flow from SIS to RHIC



## $\star$ Elliptic Flow from SIS to RHIC

• Incident Energy Dependence (P.K.Sahu et al., nucl-th/0206010)



<sup>•</sup> Larger than Data up to SPS  $\rightarrow$  Mean Field Effects ?

• Mean Field Effects (M. Isse et al.)



(\* Stronger P<sub>t</sub> are introduced)

 $\gamma$  Mean Field Shifts V<sub>2</sub> Downwards

 $\rightarrow$  Upward Shift at RHIC cannot be explained by Hadronic Mean Field



• P<sub>T</sub> and Impact Parameter Dependence (P.K.Sahu et al., nucl-th/0206010)

#### • Where Do We Underestimate V $_2$ ? : Pseudo-Rapidity Dependence

 $(\mathrm{P.K.Sahu~et~al.,~nucl-th}/0206010)$ 



• Why Do We Underestimate V<sub>2</sub> ? : Time Dependence



F In Hadron-String Scenario,

Formation Time and Interaction Suppression before String Decay Make  $\mathsf{V}_2$  to Grow Later !

 $\rightarrow$  Almond Shape is Already Obscured due to Large  $\gamma$  !

# $\star$ Summary

- \* RHIC data show **RE-HARDENING and EARLY THERMALIZATION** at mid-rapidities.
- \* Hadron-String Gas CANNOT BE STIFFER again at Higher Energy Densities. (Reduction of Repul. Int./Increase of Hadronic DOFs)
- $\star$  In Hadron-String Scenario,
  - Re-Hardening Signature is TOO WEAK,
  - $\circ$  and Thermalization is TOO SLOW,
- $\star$  The above observations suggest the necessity of Extra Pressure Generation in the Early Stage of Collisions such as that from QGP formation at mid-rapidities for RHIC.
- $\star$  Several Theoretical Supports
  - Success of Hydrodynamical description of V2 at mid-rapidities (Hirano PRC65(2001)011901; P.F. Kolb et al., NPA696(2001)175.)
  - $\circ$  AMPT: Partonization of Strings + Parton Cascade

- $\star$  Problems to be solved
  - $\circ$  Multiple Scattering Scheme
  - Partonization: Initial Condition
  - $\circ$  Hadronization  $\cdots$  String/Parton Coalescence
  - Parton Cascade incl. Inelastic Scattering