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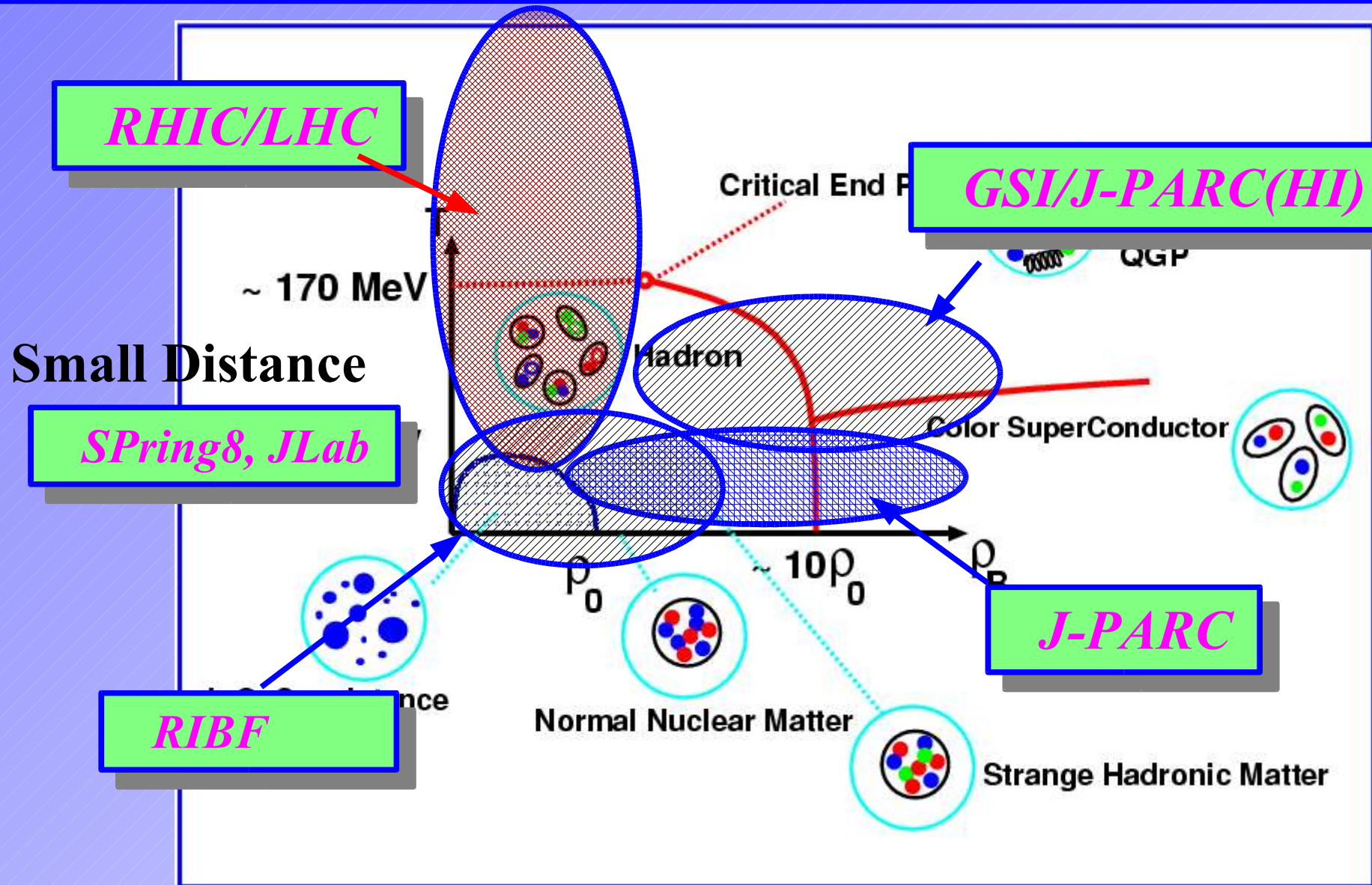
# *Jet-Fluid String Formation and Decay in High-Energy Heavy-Ion Collisions*

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in Collaboration with  
T.Hirano, M.Isse, Y.Nara, K.Yoshino**

- **Introduction**
- **Jet-Fluid String (JFS) model**
- **Results**
- **Summary**



# Hadronic Matter Phase Diagram



# *Physics of Hot Nuclear Matter*

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- Why is it interesting ?
  - Lattice QCD: We should see QCD phase transition !
  - Modification of Hadrons in Hot Medium
  - Close relation to Compact Astrophysical Objects
- How do we heat the Nucleus ?
  - Hot but Not Dense: High-Energy proton (light ion) induced Reaction, Absorption of  $pbar$ ,  $\pi^-$ , ....
  - Hot and/or Dense: **High-Energy Heavy-Ion Collisions**
- What do we want to know in High-E. HI Collisions ?
  - **Formation and Confirmation of QGP**
  - Hadron Properties in Hot Nuclear Matter
  - **Equation of State**



# *QGP Signals at RHIC*

- **High  $p_T$ : Jet Quenching**
  - *Independent* Fragmentation of Jet Partons which experienced Energy Loss in QGP.
  - *How about  $v_2$  at high  $p_T$  ?*
- **Medium  $p_T$ : Quark Number Scaling of  $v_2$** 
  - Quark Recombination suggests this scaling.
  - *Entropy reduces in “ $n \rightarrow 1$ ” process !*
- **Low  $p_T$ : Strong Elliptic Flow**
  - Hydrodynamics explains string rise of  $v_2$  at low  $p_T$ .
  - *Results depends on the later stages.*

*Signals are understood separately,  
and they are not necessarily consistent.  
→ Further Ideas are required !*

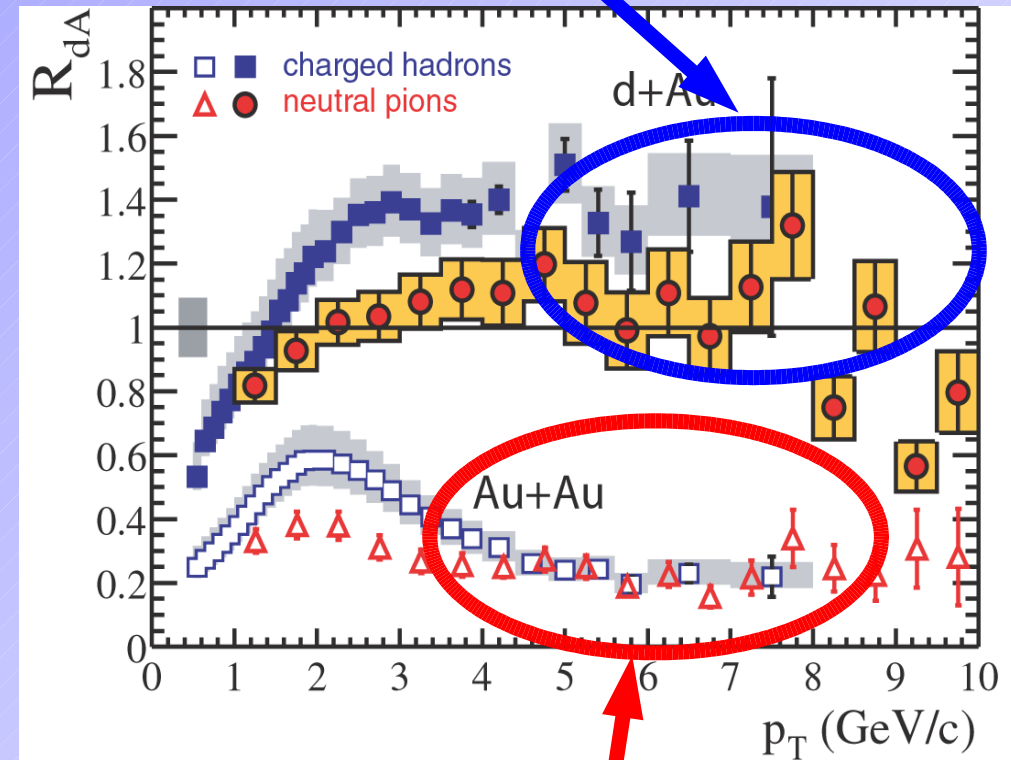


# Jet Quenching at RHIC (II)

Do we really see suppression of high energy particles at RHIC ?  
 → YES for Au+Au Collisions,  
 and NO for d+Au Collisions !

$$R_{AB}(p_T) = \frac{d^2 N / dp_T d\eta}{T_{AB} d^2 \sigma^{pp} / dp_T d\eta}$$

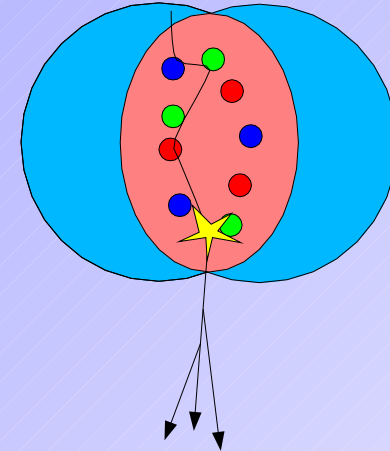
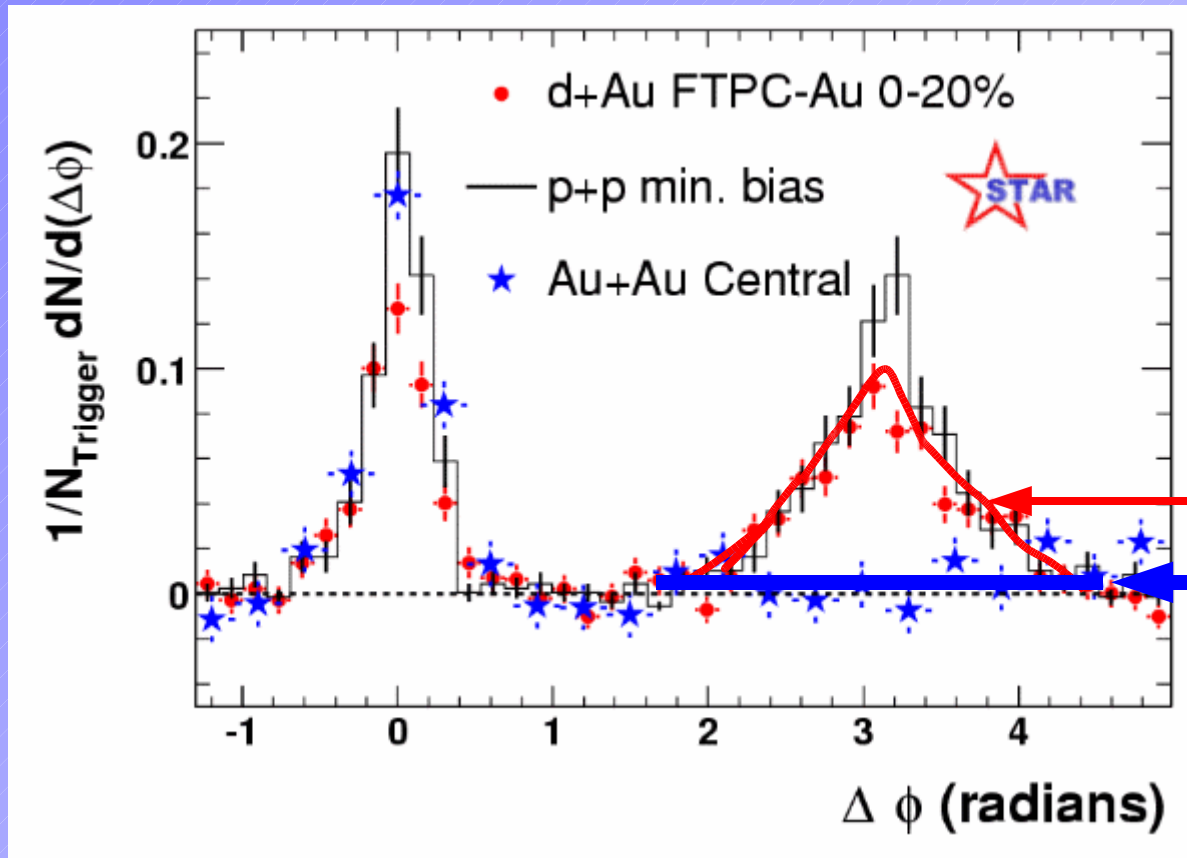
## d + Au: Initial State Effects



*High Energy Particles are suppressed in Au + Au Collisions but NOT suppressed in d + Au Collisions at RHIC compared to p+p collisions !*

**Au + Au:  
Initial State  
+ Final State Effects**

# Jet Quenching at RHIC (III)



**d + Au: Backward Peak**

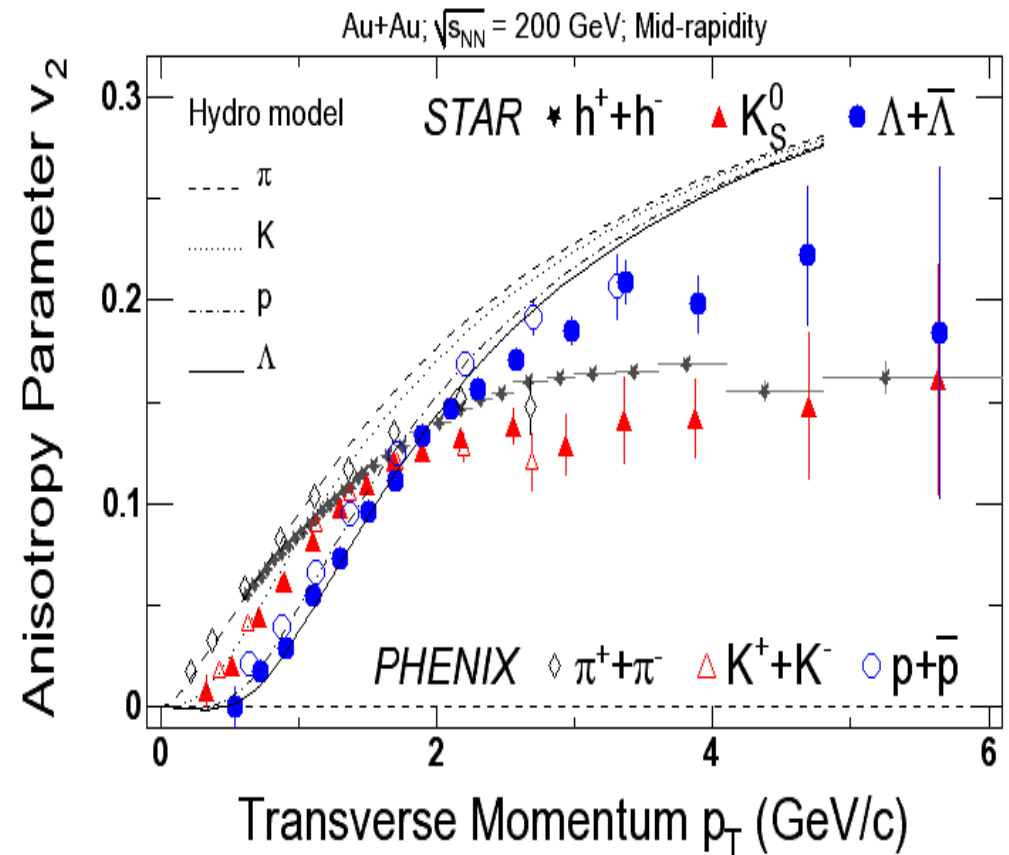
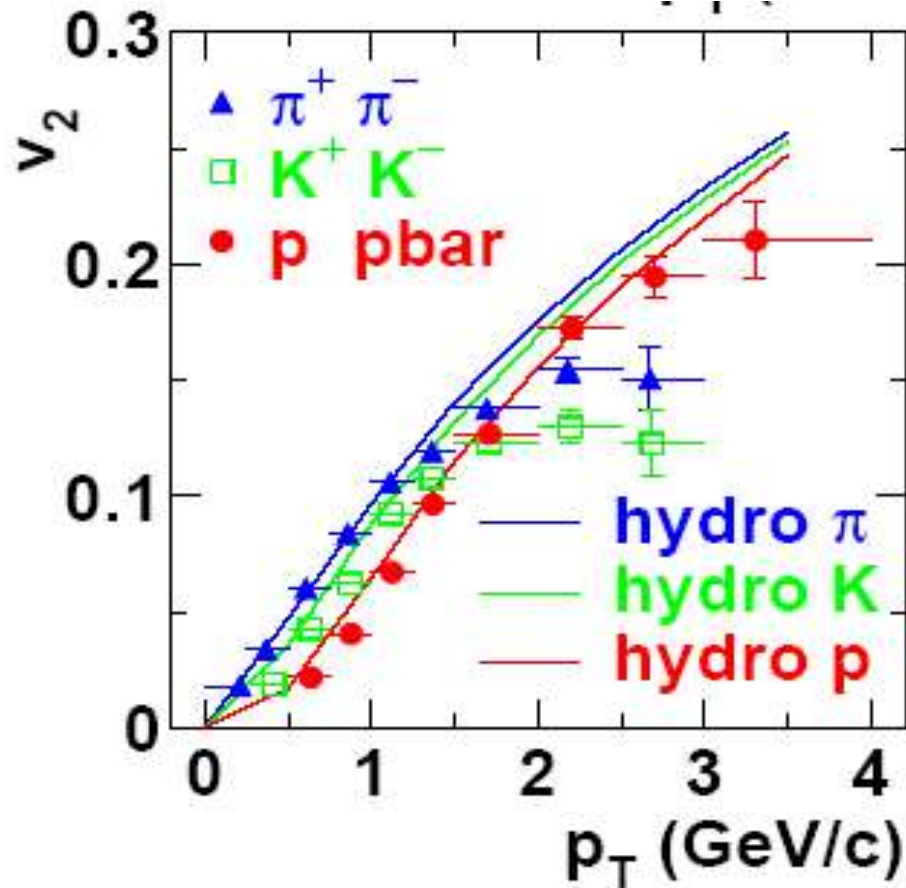
**Au + Au:  
No Backward Peak**

**STAR (nucl-ex/0306024)**

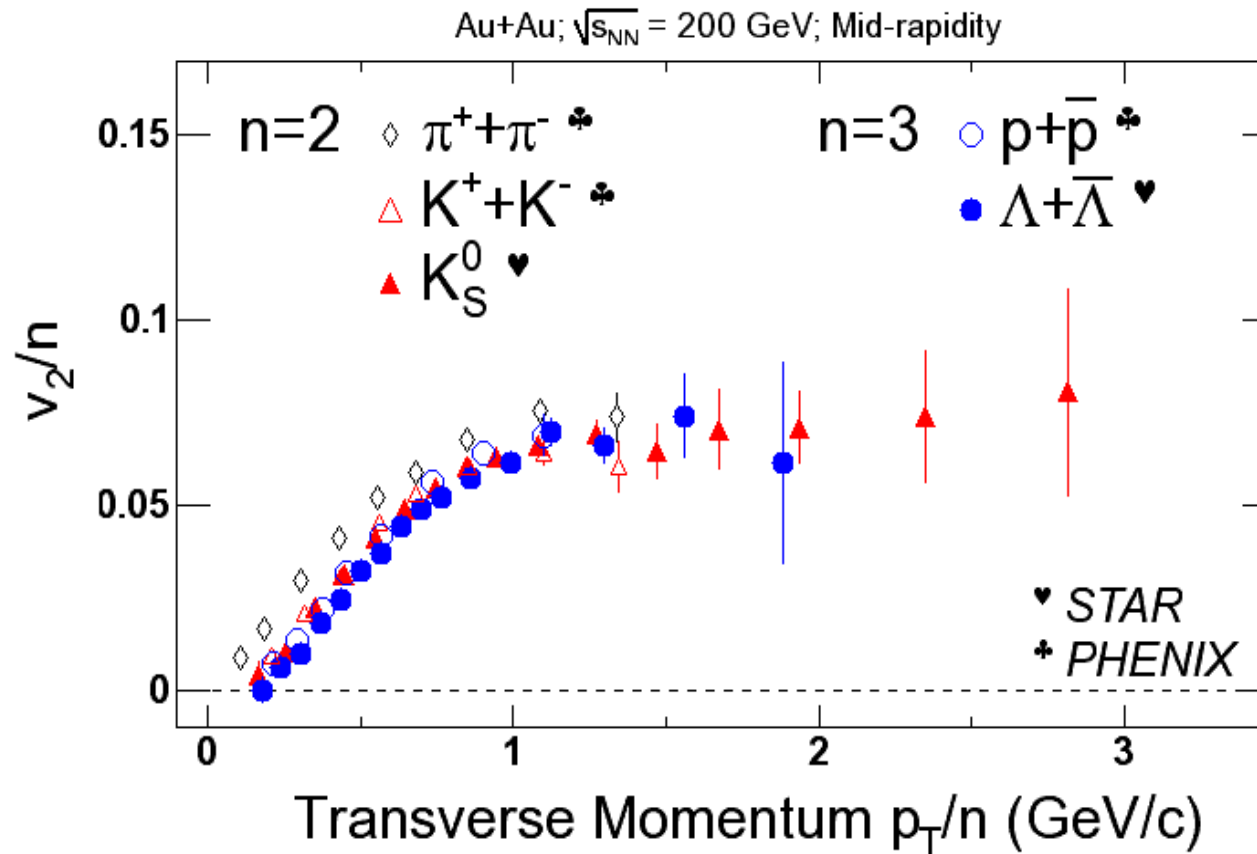
*Jet Energy Loss also lead  
to reduction of back-to-back correlation*



# by Esumi, Matter03



*Low Momentum : Hydrodynamical calc.  
with Early Thermalization  
High Momentum : Reduction from Hydro. calc.*



## Coalescence (Recombination) Picture

$$v_2^{Hadron}(P_T) = n v_2^{Parton}(P_T/n)$$

*Recombination Picture seems to work well  
... Parton Elliptic Flow*



# How can we get large $v_2$ at high $p_T$ ?

## ■ Essence in Quark Recombination Model

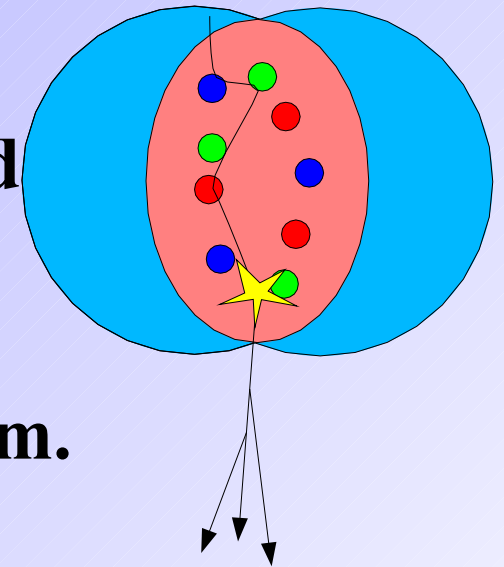
→ When two or three quarks make an object, that object will have an momentum anisotropy of their sum.

$$f(\varphi) = (1 + 2 v_2(q) \cos \varphi) \times (1 + 2 v_2(q) \cos \varphi) \\ \approx 1 + 2 \times 2 v_2(q) \cos \varphi$$

## ■ Elliptic Flow of High $p_T$ particles is generated by the Energy Loss in QGP.

→ **Larger Energy Loss gives Larger  $v_2$**

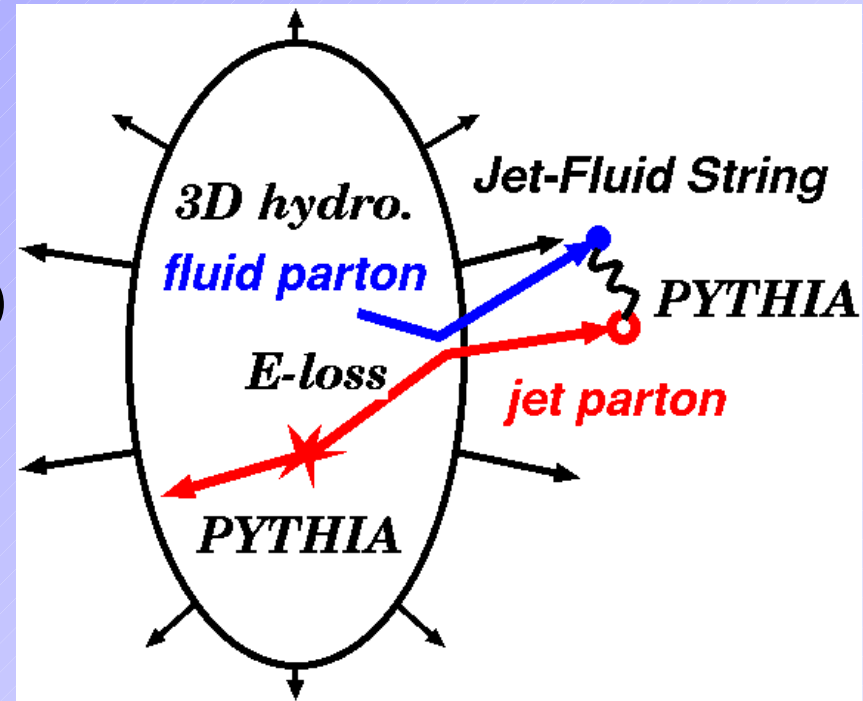
but they are not consistent with  $p_T$  spectrum.



*Let's consider a possibility  
of New Hadronization Scheme  
to generate Larger  $v_2$  at high  $p_T$   
by combining the above two ideas !*

# Jet-Fluid String Formation and Decay

- Jet parton picks up a fluid parton **to make a color singlet object.**  
↔ Independent Fragmentation  
(No explicit color flux specified)
- Color singlet string will **break up into many (several) hadrons.**  
→ Entropy does not decrease.  
↔ Quark Recombination
- Momenta of jet and fluid partons are **positively correlated.**  
→ String will have large  $p_T$  and  $v_2$ .



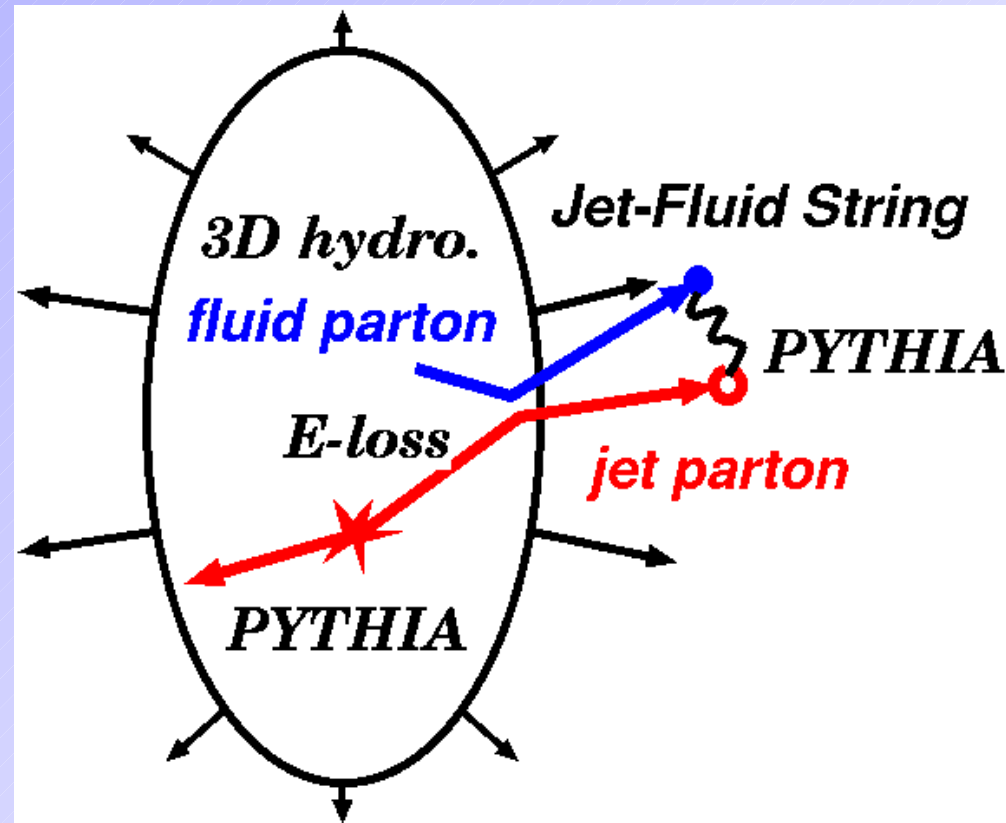
*Can we understand  $p_T$  spectrum and  $v_2$  consistently ?*



# Model Details (1)

## Model Components

- (Mini-)Jet Production: Pythia
- Parton Energy Loss in QGP:  
GLV first order formula  
+ 3D Hydrodynamics results
- String formation Prob.:  
Use parameterized form
- String Fragmentation: Pythia



# Model Details (2)

## ■ Relevant Model Parameters

- Jet production: K-factor

$$\sigma_{jet} = K \sigma_{jet}^{pQCD(1st\ order)}$$

(c.f. JAM  $\rightarrow$  K=3)

- Energy Loss

$$\frac{dE}{d\tau} = 3 \pi \alpha_s^3 F_{color} C (\tau - \tau_0) \log\left(\frac{2 E_0}{\mu^2 L}\right)$$

(c.f. Hydro+Jet model C  $\approx$  2.7)

- Parameterized String Formation Probability

$$P(\sqrt{s}) \propto \Theta(\sqrt{s} - \sqrt{s_0}) s^{-n/2}$$

(This should be evaluated by pQCD matrix element + string level density)

Current Choice:  $\sqrt{s_0} = 1.0$  GeV,  $n = 1$



# *K-factor*

- **K-factor** → absolute value of  $\sigma_{\text{jet}}$

- **Experimental Data:**  $pp \rightarrow \pi^0$  @  $\sqrt{s_{\text{NN}}} = 200 \text{ GeV}$  (PHENIX)

$$\frac{1}{\sigma^{\text{exp}}} \frac{d^2 \sigma^{\text{exp}}}{2\pi p_T d p_T dy} = K \frac{\sigma^{\text{pQCD}(1st)}}{\sigma^{\text{exp}}} \frac{d^2 N^{\text{pQCD}(1st)}}{2\pi p_T d p_T dy} \quad A = K \frac{\sigma^{\text{pQCD}(1st)}}{\sigma^{\text{exp}}}$$

$\sigma^{\text{Exp.}} = 21.8 \text{ mb}$  (trigger)

$\sigma^{\text{pQCD}(1st)} = 9.9 \text{ mb}$

- **pythia6.3 fit:**

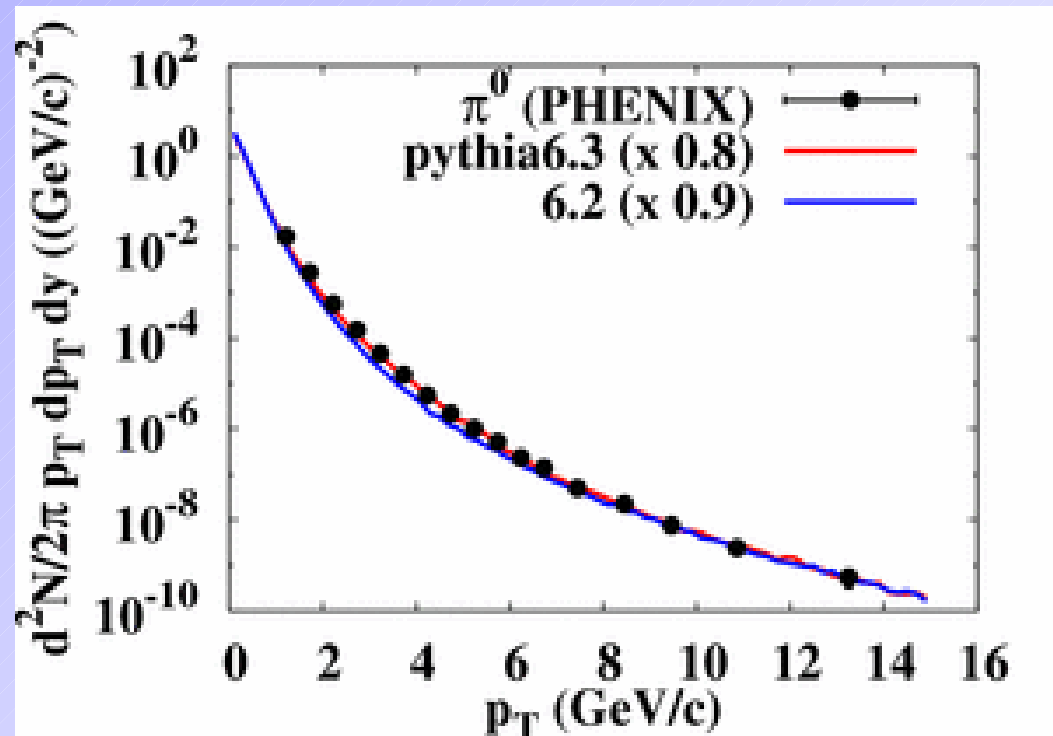
$A \approx 0.8 \rightarrow K = 1.8$

$(\sigma_{\text{jet}} (p_T^{\text{hard}} > 2 \text{ GeV}/c) \approx 17.5 \text{ mb})$

- **pythia6.2 fit:**

$A \approx 0.9 \rightarrow K = 2.0$

$(\sigma_{\text{jet}} \approx 19.6 \text{ mb})$



# Energy Loss Factor (1)

- Additional Factor for Energy Loss → High  $p_T$  hadron yield
- Exp. Data:  $p_T$  spectra of  $\pi$  in Au+Au (PHENIX, STAR)

$$\frac{d^2 N^{Exp.}}{2\pi p_T dp_T dy} = N_{jet} \frac{1}{N_{jet}} \frac{d^2 N^{JFS}(C)}{2\pi p_T dp_T dy}$$

→ Determining  $N_{jet}$  is important !

$N_{coll} = 373$  @  $b=7.4$  fm (PHENIX estimate)

$\sigma_{jet}^{NN} = 17.5$  mb (pp fit pythia 6.3),  $\sigma_{tot}^{NN} = 47.4$  mb (JAM)

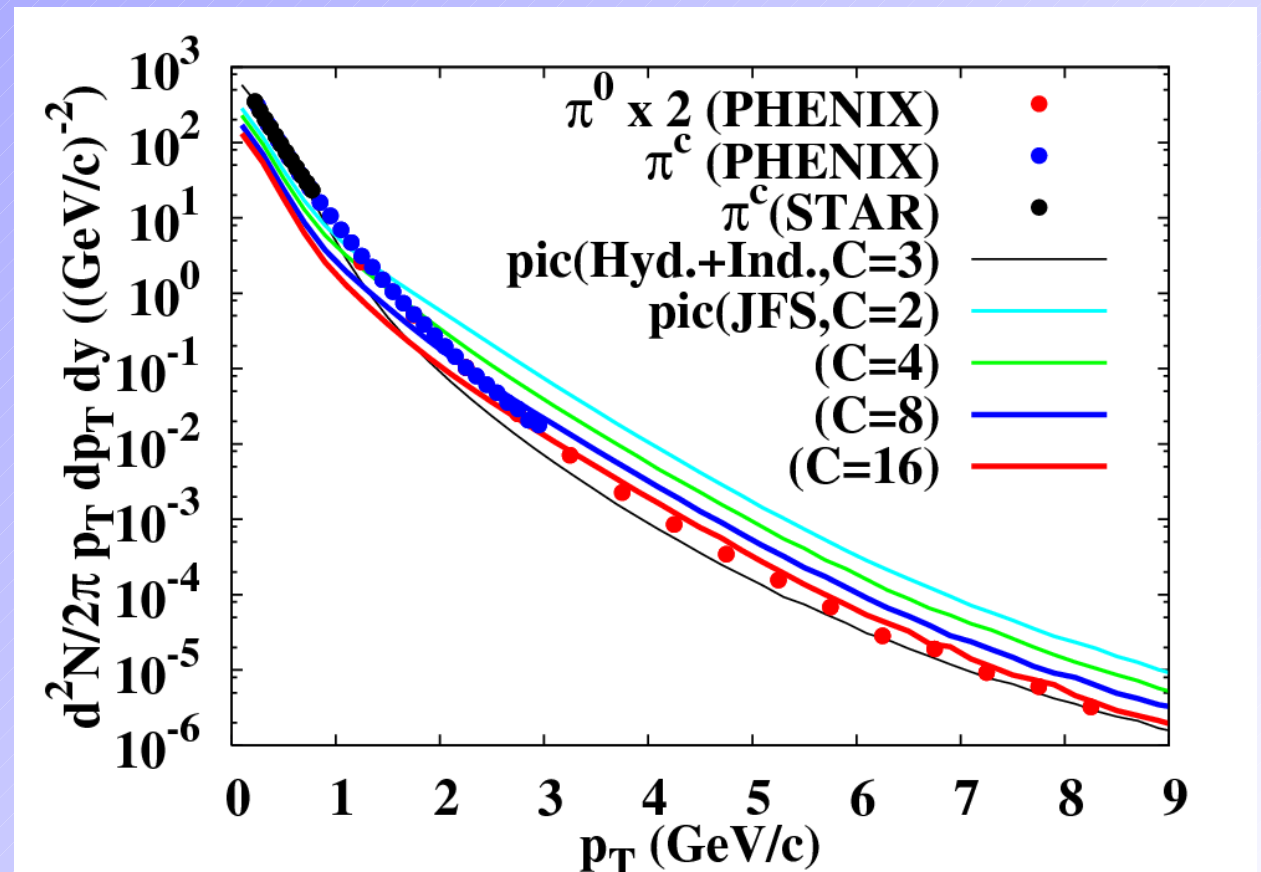
$$N_{jet} = \sigma_{jet}^{NN} \int d^2 r_T T_A(r_T + b/2) T_B(r_T - b/2) = \frac{\sigma_{jet}^{NN}}{\sigma_{tot}^{NN}} N_{coll}$$

$$T_A(r_T) = \int dz \rho(r_T, z)$$



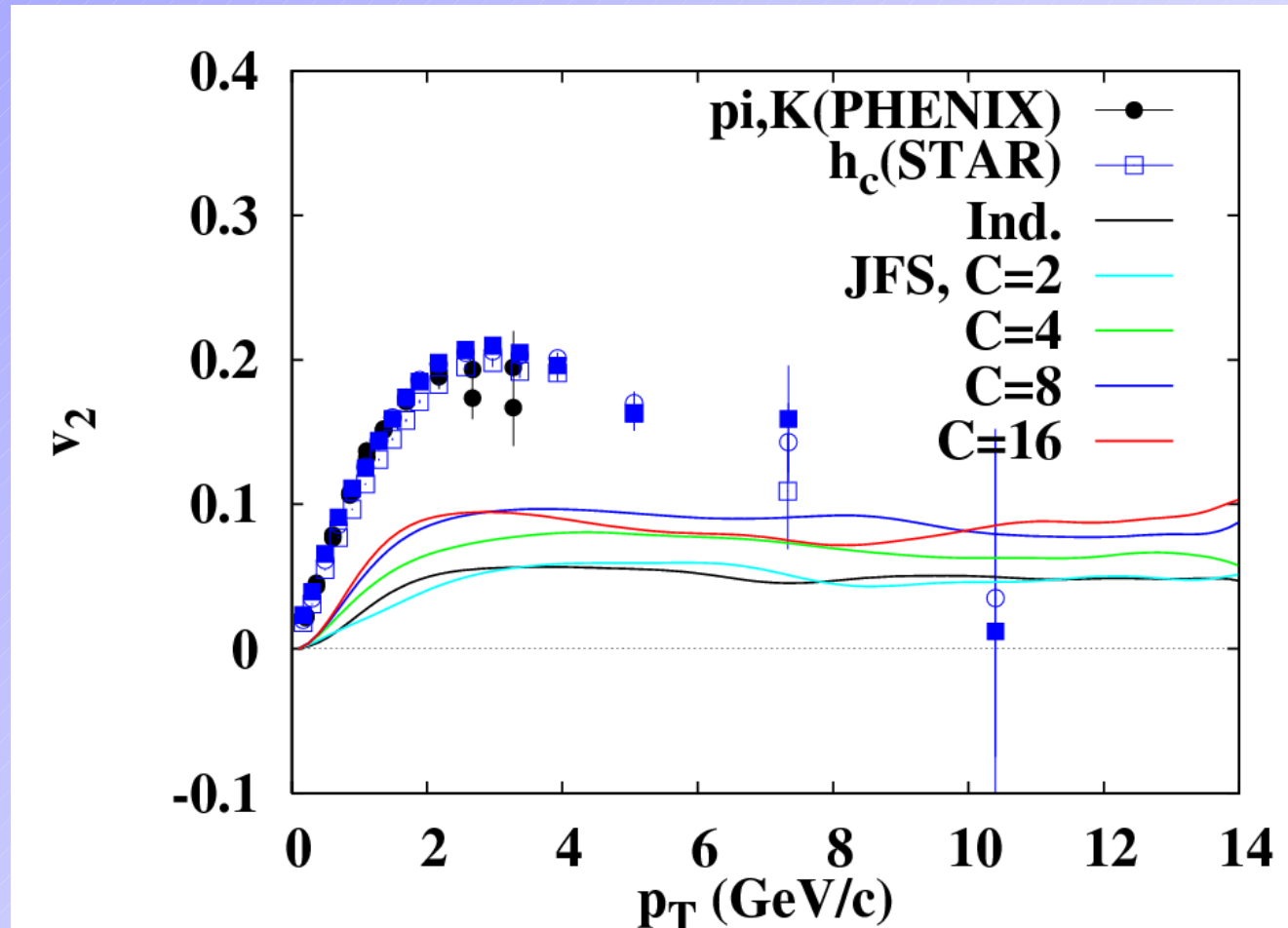
# Energy Loss Factor (2)

- Comparison with pion pT spectrum in Au+Au @ RHIC  
Ind. Frag.:  $C \approx 3$ , JFS:  $C > 8$   
→ Large Energy Loss is allowed in JFS



# Elliptic Flow

- JFS with large energy loss factor,  $C$   
→ Enhanced Elliptic Flow ( $\sim 10\%$ ) is generated even at high  $p_T$  ( $\sim 10$  GeV/c).
- Independent Frag.  
→  $v_2 \sim 5\%$  at high  $p_T$



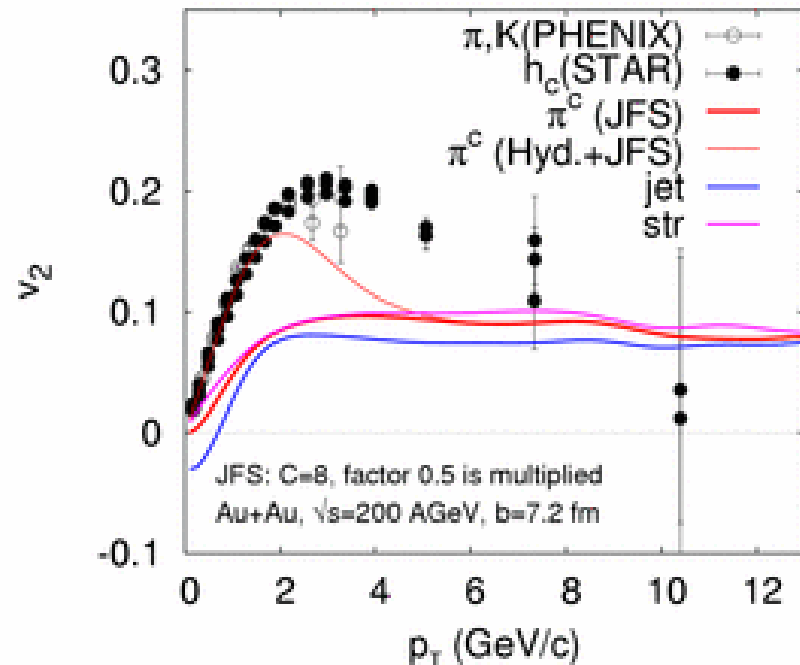
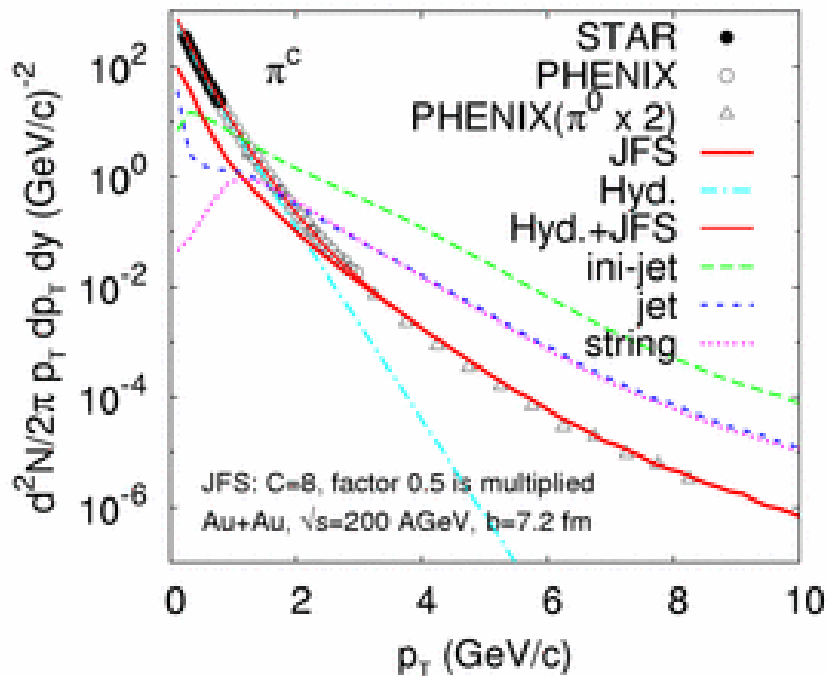


# Combined with Low $p_T$ spectrum

- Low  $p_T$  spectrum is assumed and combined.

$$F^{Hyd}(p_T) = A \exp(-p_T/T) (1 + B / (1 + (p_T/p_0)^\delta))$$

$$v_2^{Hyd}(p_T) = 0.13 p_T$$



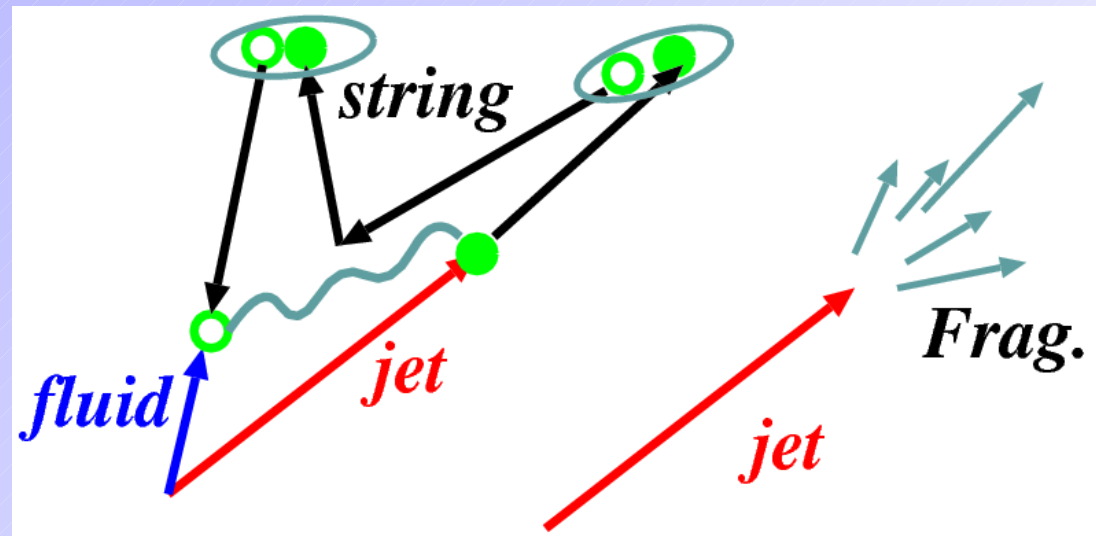
# Discussion

## ■ Mechanism to produce high $p_T$ hadrons in JFS

- Jet and Fluid partons are correlated in momentum  
→ large transverse VELOCITY ( $p_T$ ) of formed Strings
- Relative momentum is relatively small  
→ Smaller number of hadrons with high  $p_T$  are formed

↔ Independent Frag. (Large no. of Low  $p_T$  hadrons)

- Allowed large energy loss and Momentum anisotropy correlation of jet-fluid makes  $v_2$  larger.



# Summary

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- A new mechanism to produce high  $p_T$  hadrons (Jet-Fluid String formation and decay) is proposed.
  - This would be better than Indep. Frag. where Energy-Momentum conservation is satisfied only in average.
  - Low  $p_T$  hadrons are suppressed than in Indep. Frag.
  - Entropy does not decrease, but increases.
- When we FIT  $p_T$  spectrum (roughly), large  $v_2$  is found to be generated.
  - Easy to form high  $p_T$  hadrons, and then large energy loss is required to explain  $p_T$  spectrum data.
  - Momentum anisotropy correlation of jet-fluid is expected to help.



# Further Problems

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- Very large energy loss is required to explain  $p_T$  spectrum.
  - $C > 8$  in JFS  $\leftrightarrow C \approx 2.7$  in Hydro+Jet model (Hirano-Nara)

Is it possible to justify this large energy loss ?
- Elliptic flow at medium  $p_T$  is underestimated.  
→ Fluid-Fluid String would be necessary to consider.
- Large baryon yield at medium  $p_T$  may not be explained.  
→ Three parton string ? (Jet-Fluid-Fluid, Fluid-Fluid-Fluid)
- String formation probability should be evaluated  
in pQCD matrix element + string level density.  
→ Yoshino's Master thesis ?
- and Many.



# High-Energy Heavy-Ion Collision Experiments

Heavy-ion physicists wanted to create QGP for a long time ..

**LBL-Bevalac:**

**800 A MeV**

**GSI-SIS:**

**1-2 A GeV**

**BNL-AGS (1987-):**

**10 A GeV**

**CERN-SPS (1987-):**

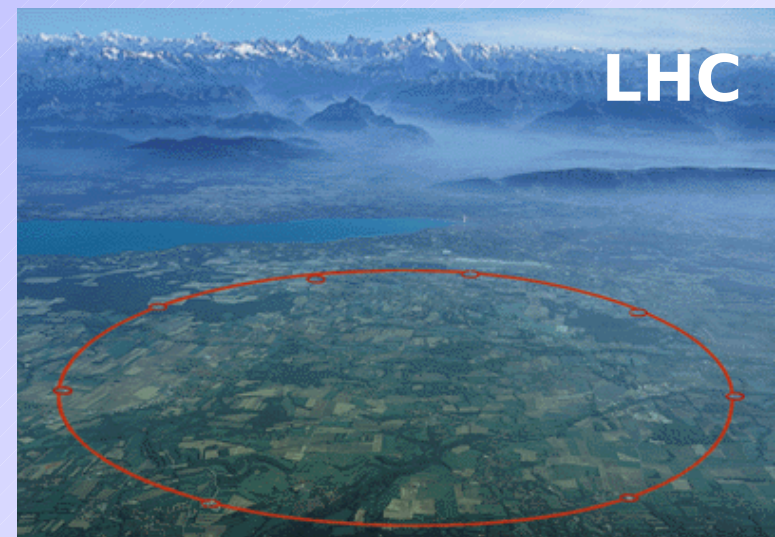
**160 A GeV**

**BNL-RHIC (2000-):**

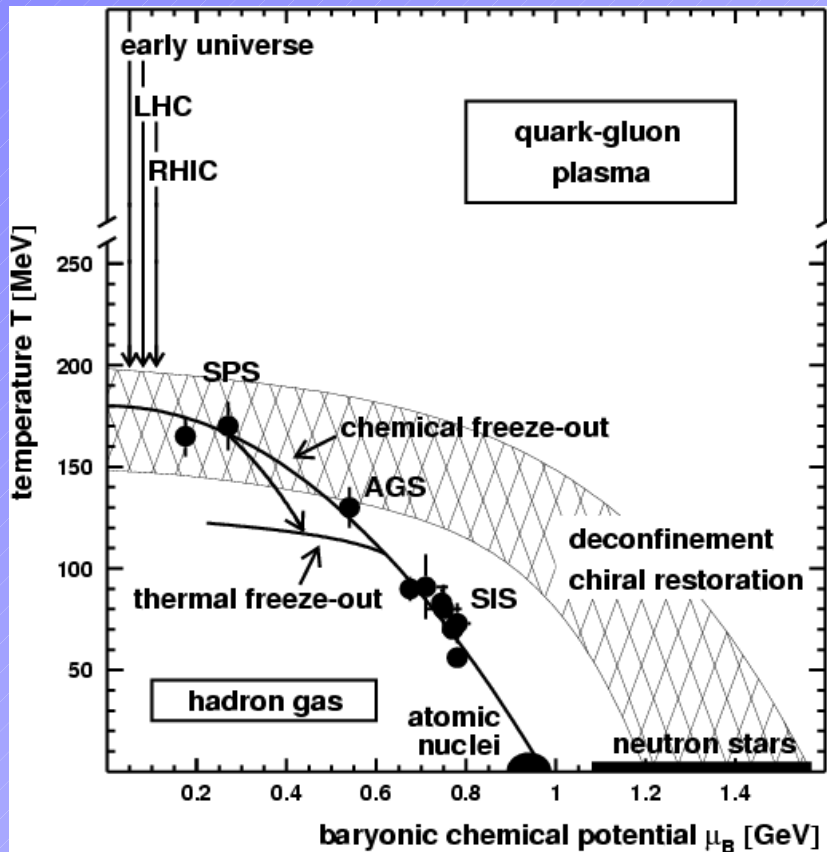
**100+100 A GeV**

**CERN-LHC (2007(?)-):**

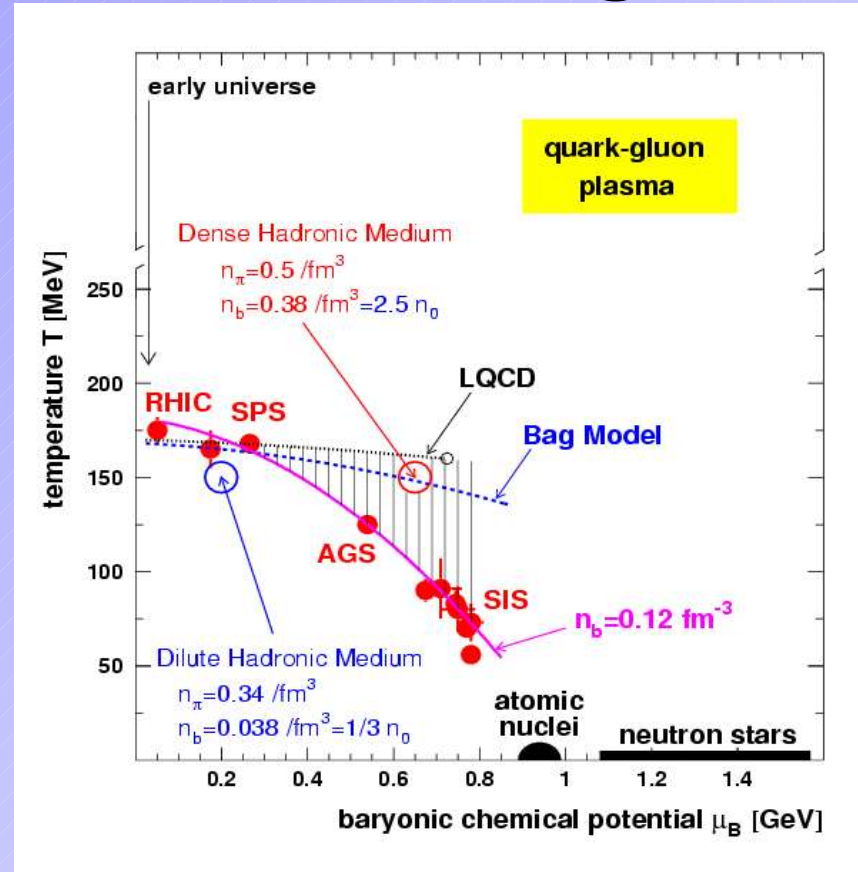
**3 + 3 A TeV**



# Experimentally Estimated Phase Diagram



1998 (J. Stachel et al.)



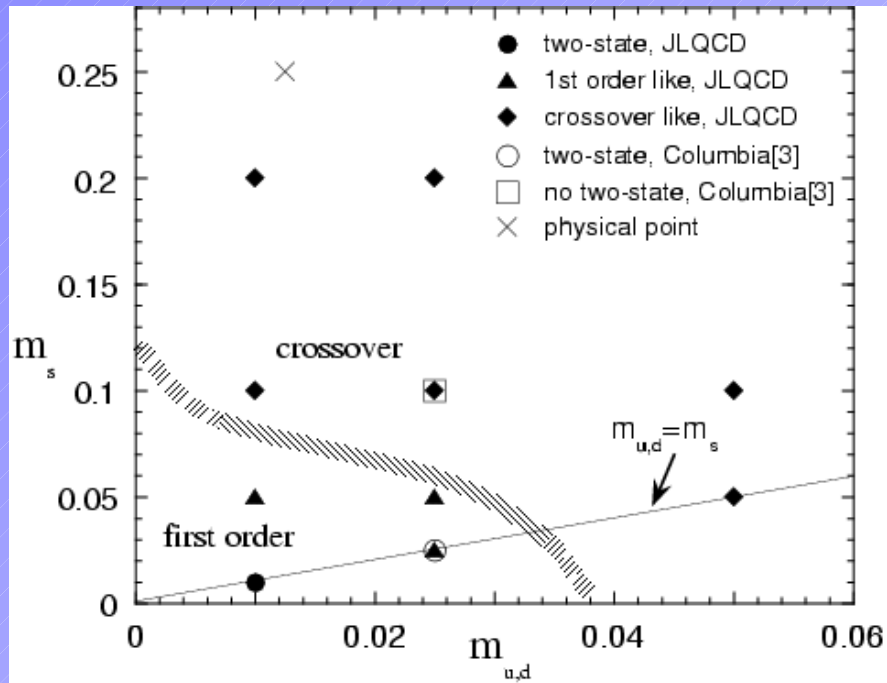
2002 (Braun-Munzinger et al. J. Phys. G28 (2002) 1971.)

*Chem. Freeze-Out Points are very Close to Expected QCD Phase Transition Boundary*

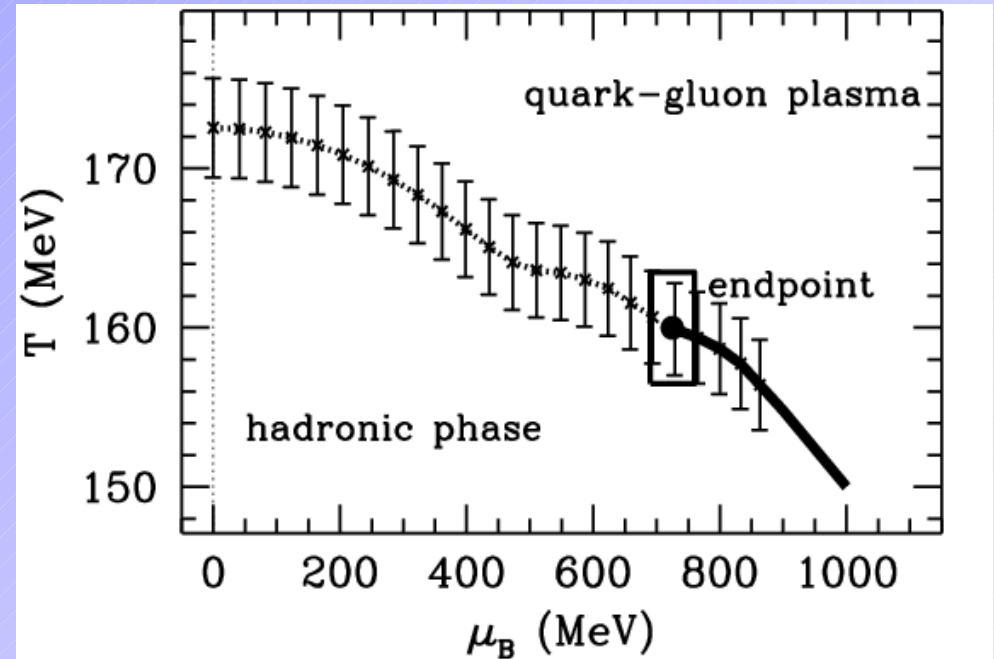


# Theoretically Expected QCD Phase Diagram

## Zero Chem. Pot.



## Finite Chem. Pot.



JLQCD Collab. (S. Aoki et al.),  
Nucl. Phys. Proc. Suppl. 73 (1999)  
459.

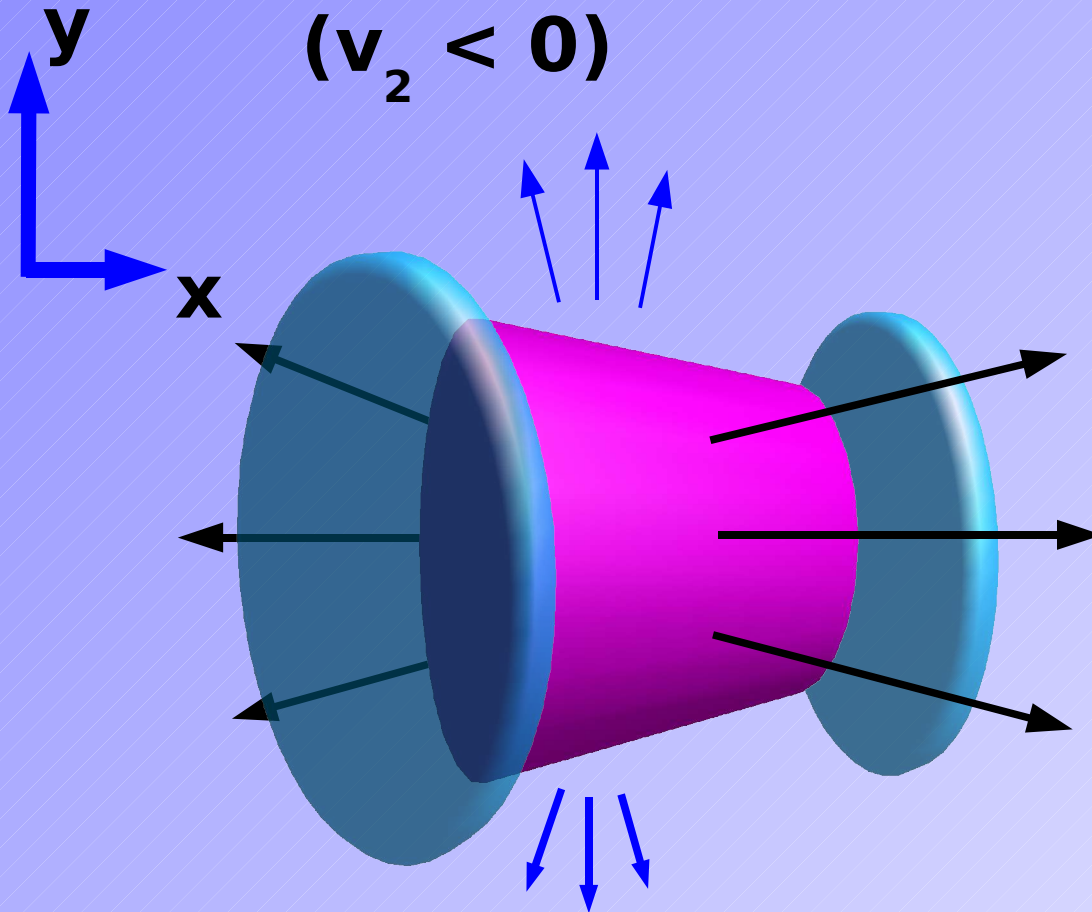
Finite  $\mu$  : Fodor & Katz,  
JHEP 0203 (2002), 014.

*Zero Chem. Pot. : Cross Over*  
*Finite Chem. Pot.: Critical End Point*



# Elliptic Flow (I)

**Out-of-Plane Flow**  
( $v_2 < 0$ )



- ★ What is Elliptic Flow ?
  - Anisotropy in P space
- ★ Hydrodynamical Picture
  - Sensitive to the Pressure Anisotropy in the Early Stage
  - Early Thermalization is Required for Large  $v_2$

**In-Plane Flow**  
( $v_2 > 0$ )

$$v_2 \equiv \left\langle \frac{p_x^2 - p_y^2}{p_x^2 + p_y^2} \right\rangle = \langle \cos 2\phi \rangle$$





# Elliptic Flow (II)

## ★ What is the Origin of Elliptic Flow ?

- **Hydrodynamics**

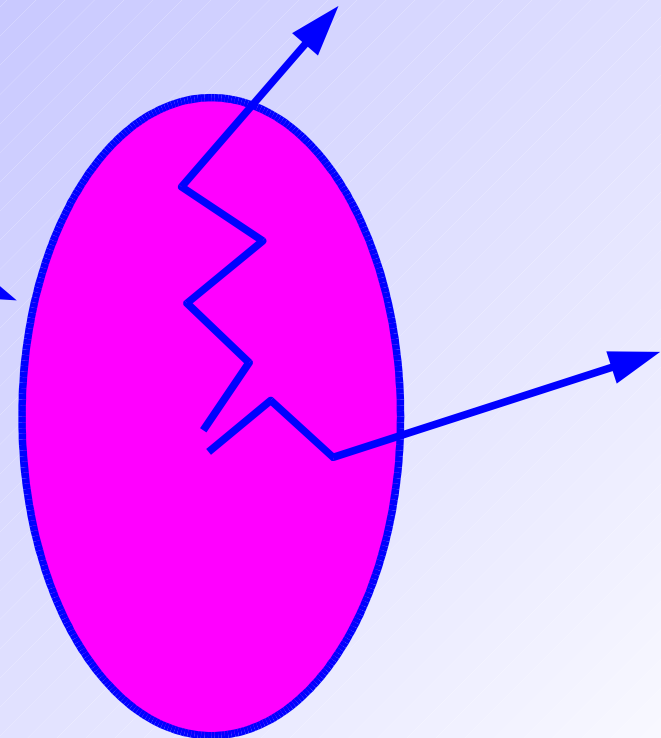
- **Jet Energy Loss**

- **Coalescence**

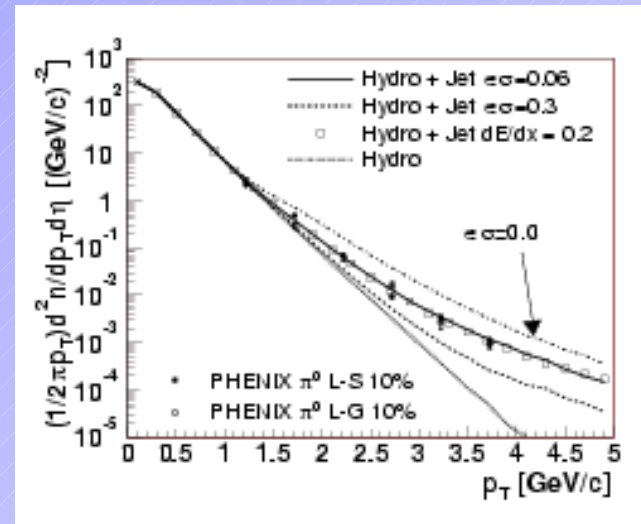
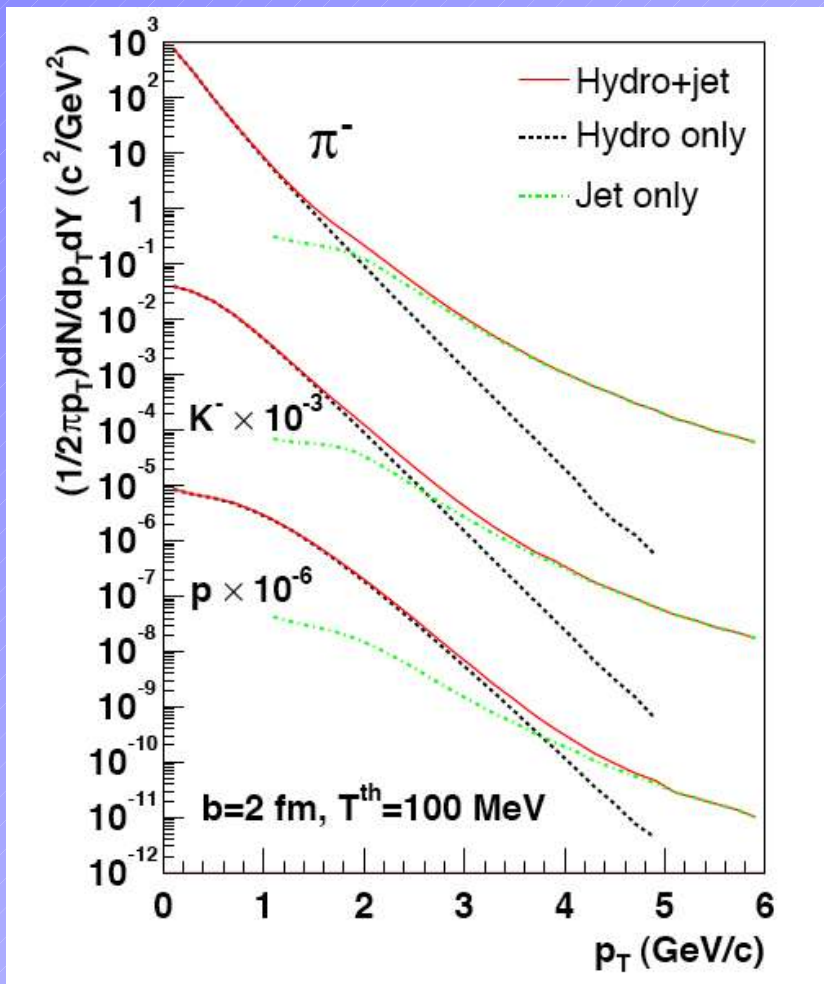
Hydro+Jet  
(Hirano and Nara)

Fragmentation  
& Recombination  
Fries, Nonaka, ...

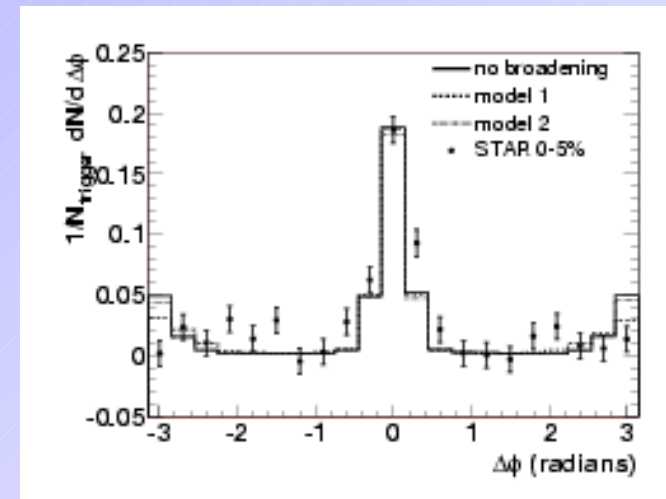
$$\begin{aligned} f(\phi) &\simeq f_1(\phi) f(\phi) \\ &\propto (1 + 2v_2 \cos \phi) \times (1 + 2v_2 \cos \phi) \\ &= 1 + 2 \times 2v_2 \cos \phi \end{aligned}$$



# Hydro + Jet Model (Hirano and Nara)



**PRC66 ( 2002) 041901.**



**PRL 91 (2003)082301.**

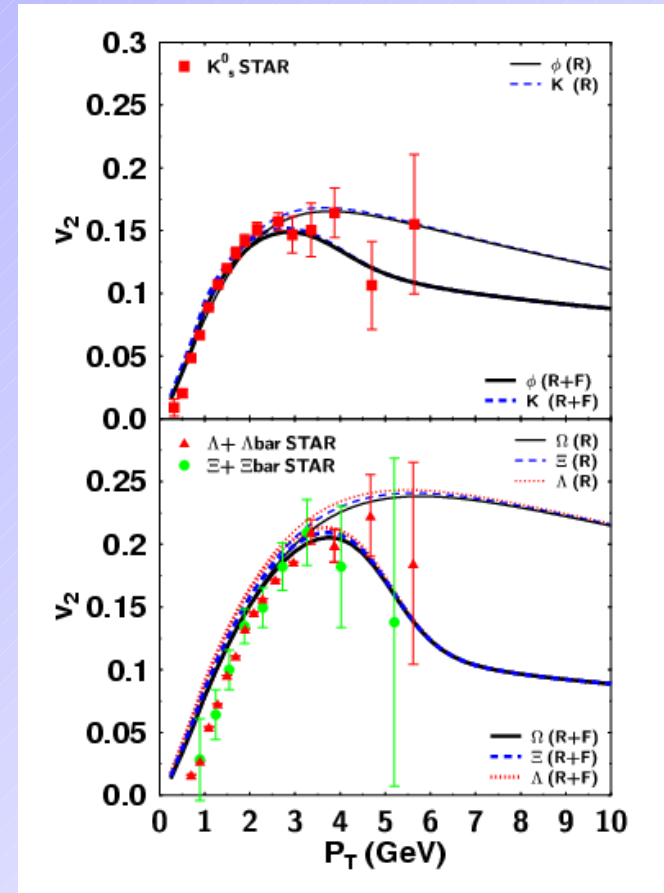
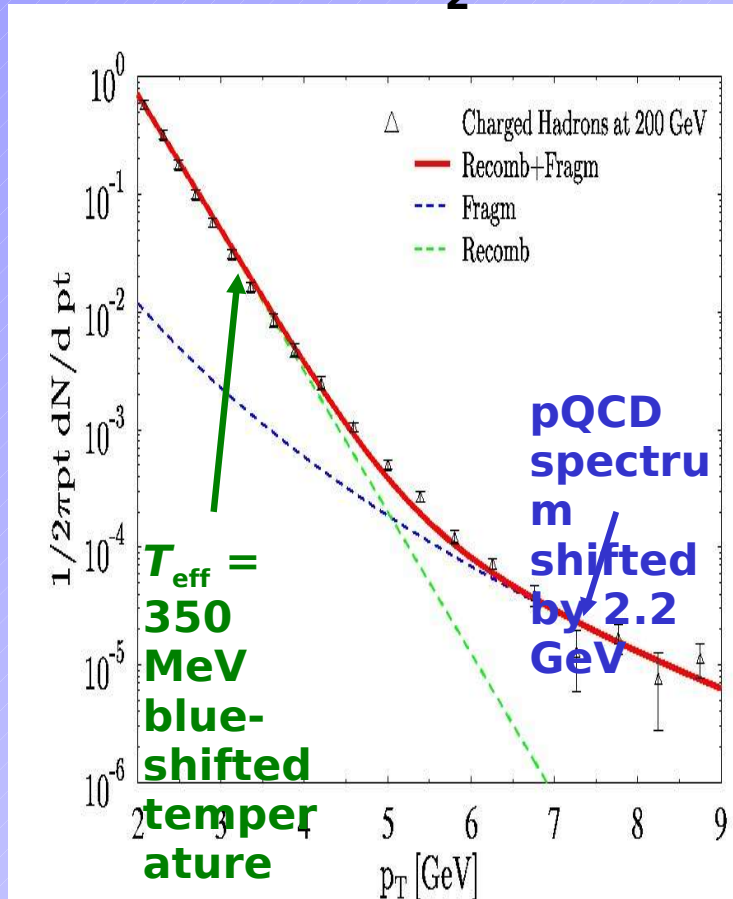
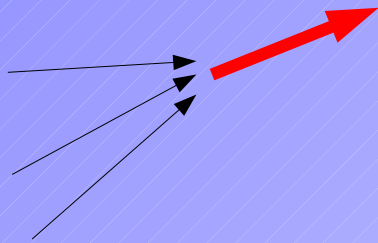
*Heavy-Particles are affected by Hydro. Flow until Larger  $P_T$*



# Fragmentation and Recombination

## (Duke U. Group)

Recombination Enhances Intermed.  
 $P_T$  Hadrons and Baryon  $V_2$ .



Fries et al. PRL 90 (2003), 202303, Nonaka et al., nucl-th/0308051

