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# *Jet-Fluid String Formation and Decay in High-Energy Heavy-Ion Collisions*

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- Introduction
- Jet-Fluid String (JFS) model
- Results
- Summary



# Hadronization Mechanism at RHIC

- *High  $p_T$ : Indep. Frag. of Jet Partons (E.g. Hirano-Nara)*
  - Explains  $p_T$  spectrum when E-loss is included.
  - ✗ Elliptic Flow  $v_2$  is small at high  $p_T$  ← *This Talk*
- *Medium  $p_T$ : Recombination (E.g. Duke-Osaka-Nagoya)*
  - Explains Baryon Puzzle and Quark Number Scaling of  $v_2$
  - ✗ Entropy decreases in “ $n \rightarrow 1$ ” process
- *Low  $p_T$ : Equil. Fluid Hadronization (E.g. Hirano-Gyulassy)*
  - Explains  $p_T$  spec. and  $v_2$  at low  $p_T$
  - ✗ Results depends on the Freeze-Out Conditions

*QGP Signals are understood separately,  
and they are not necessarily consistent.  
→ Further Ideas are required !*

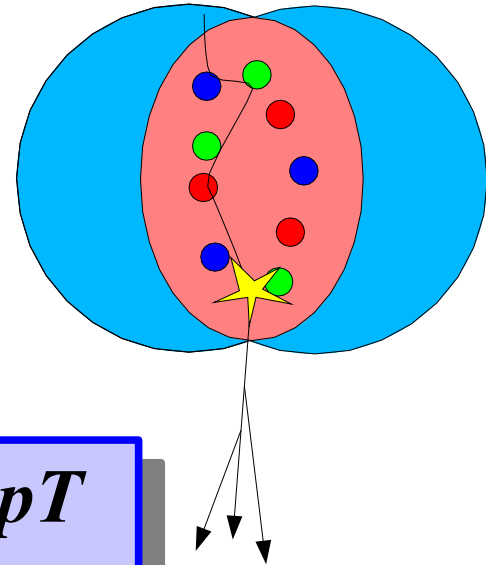


# How can we get large $v_2$ at high $p_T$ ?

- Quark Recombination → Combined Objects have larger  $v_2$

$$f(p, \varphi) = (1 + 2 v_2(p/2) \cos \varphi) \times (1 + 2 v_2(p/2) \cos \varphi) \\ \approx 1 + 2 \times 2 v_2(p/2) \cos \varphi$$

- Energy Loss in QGP generates  $v_2$ 
  - Large/Small suppression in  $y/x$  directions



*Plausible Hadronization giving large  $v_2$  at high  $p_T$*

- *Combination of several partons*
- *Large Energy Loss*
  - *Jet parton picks up Fluid parton and forms a string (Jet-Fluid String)*

# Jet-Fluid String Formation and Decay

**Jet production:** pQCD(LO)  $\times$  K-factor (PYTHIA6.3, K=1.8, *pp* fit)

$$\sigma_{jet} = K \sigma_{jet}^{pQCD(LO)}$$

**Jet propagation in QGP**

3D Hydro + Simplified GLV 1st order formula  $\times C$

(Hirano-Nara, NPA743('04)305, Hirano-Tsuda, PRC 66('02)054905. Web version!

Gyulassy-Levai-Vitev, PRL85('00)5535)

$$\frac{dE}{d\tau} = 3\pi\alpha_s^3 F_{color} C (\tau - \tau_0) \log\left(\frac{2E_0}{\mu^2 L}\right)$$

**Jet-Fluid String formation**

Fluid parton breaks color flux,  
according to string spectral func.

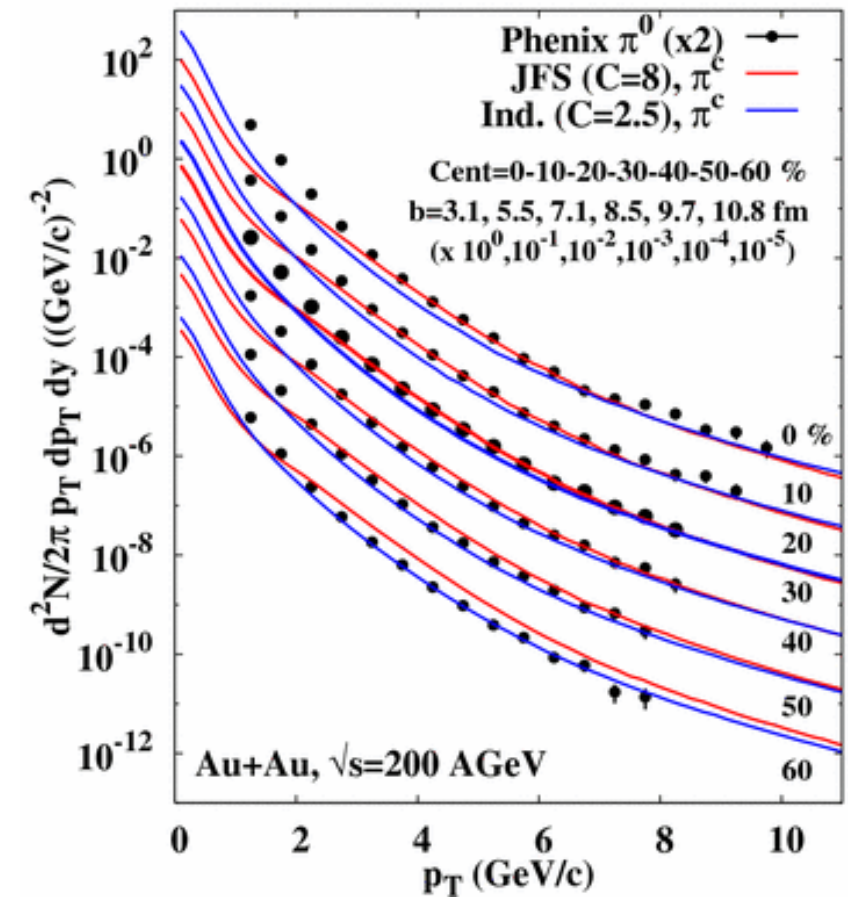
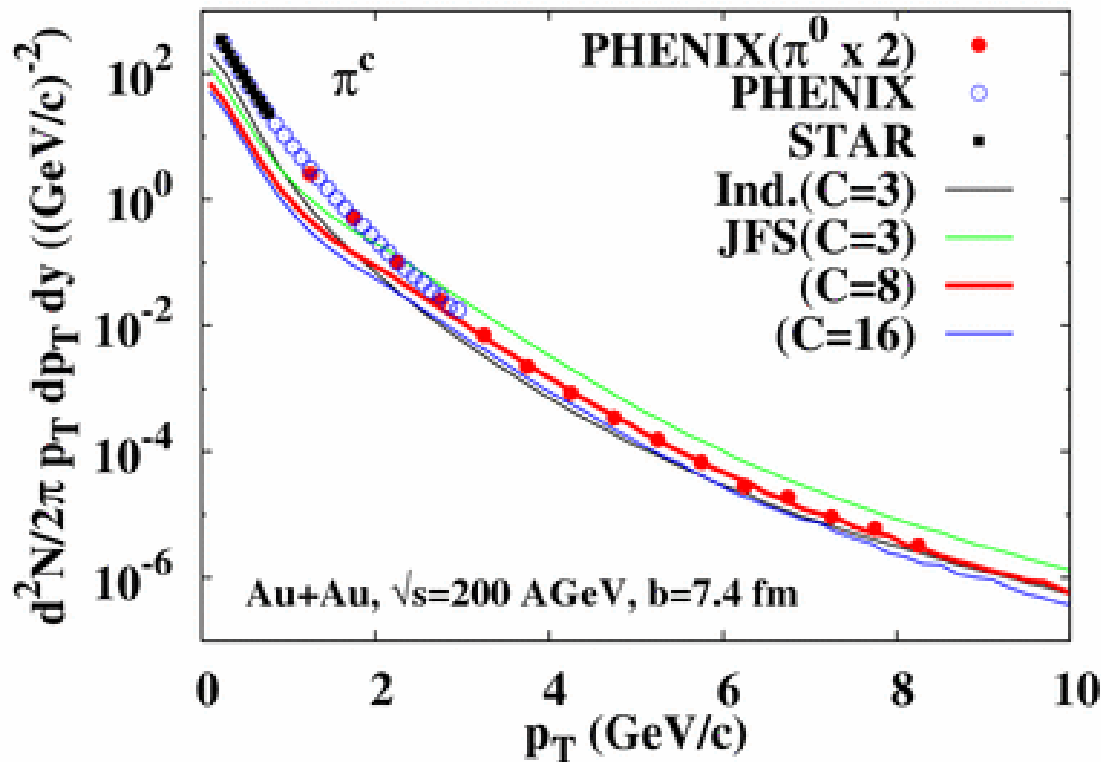
$$P(\sqrt{s}) \propto \Theta(\sqrt{s} - \sqrt{s_0}) \quad (\sqrt{s_0} = 2 \text{ GeV})$$

Only g and light q (qbar) are considered.



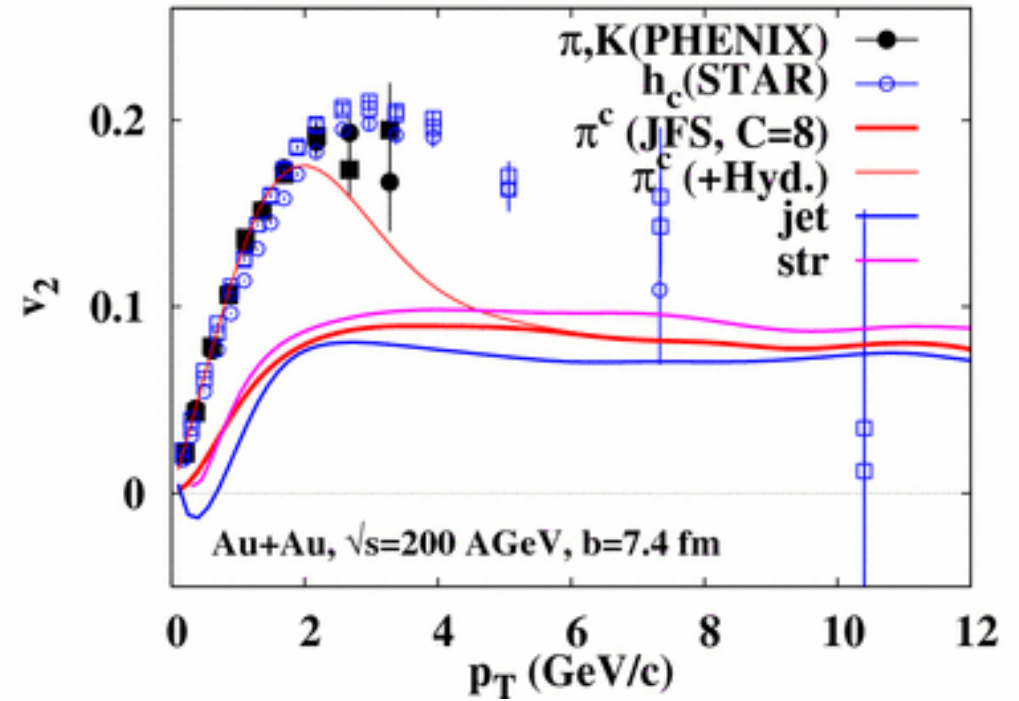
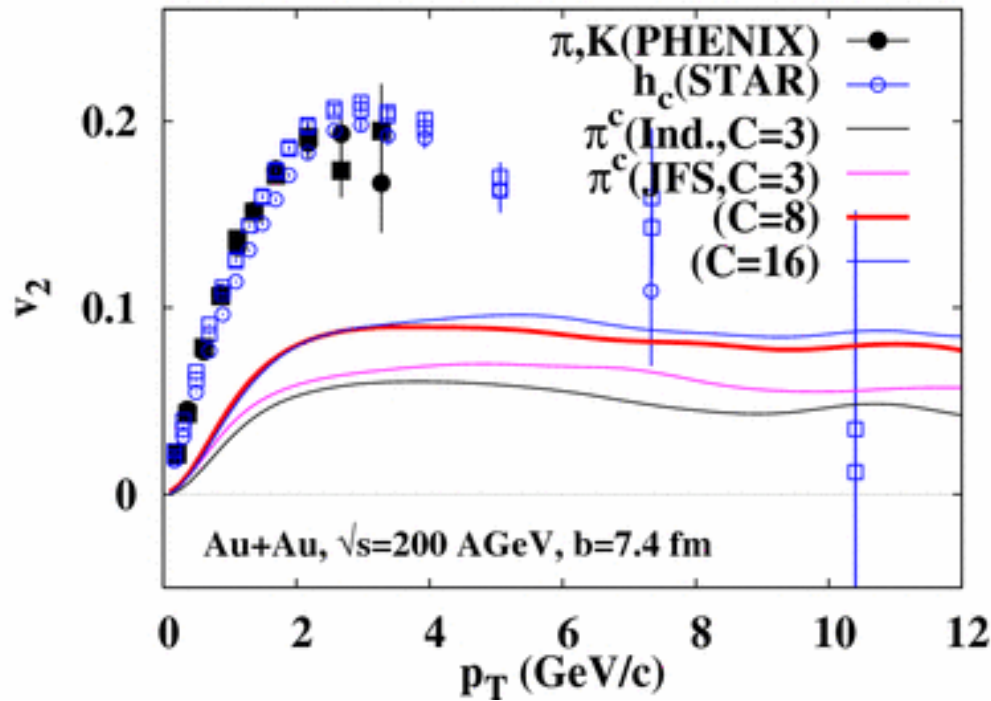
# Energy Loss Factor $C$ : $p_T$ Spectrum Fit

- For the same  $C \rightarrow dN_{JFS}(\text{high } p_T) > dN_{Ind}(\text{high } p_T)$
- $p_T$  spec. fit  $\rightarrow$  Ind. Frag.:  $C \approx (2.5-3)$ , JFS:  $C \approx 8$   
 $\rightarrow$  *Large Energy Loss is necessary / allowed in JFS*



# Elliptic Flow: $p_T$ Deps.

- High  $p_T$   $v_2$  :  $\sim 5\%$  in Ind. ( $C=3$ )  $\leftrightarrow$   $\sim 8\%$  in JFS ( $C=8$ )

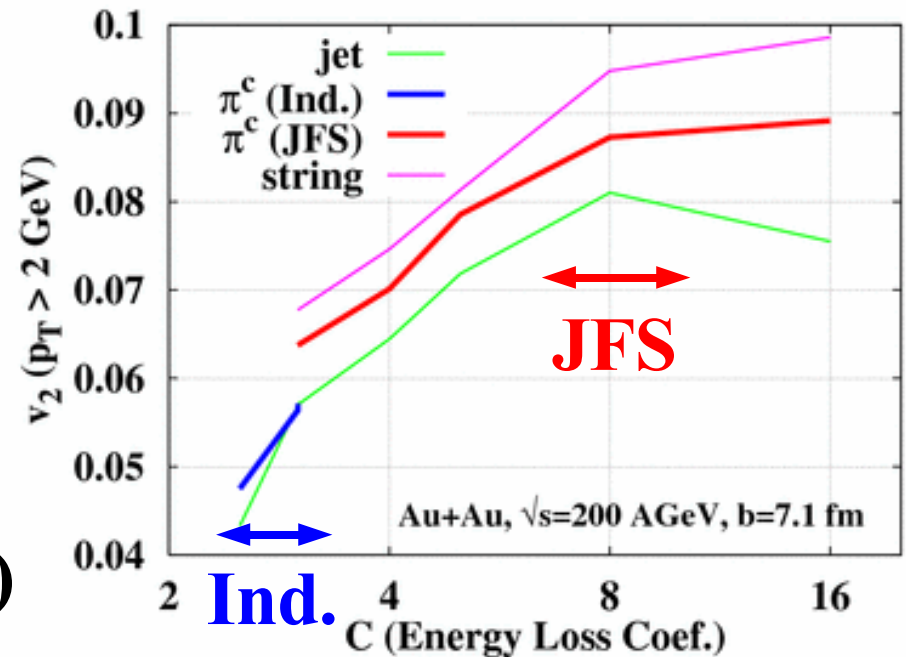


Origin of Large  $v_2 =$  *Large E-loss factor C* + *Fluid parton  $v_2$*



# Elliptic Flow: Parameter Deps.

- $v_2(\text{jet})$ : saturating behavior (large E-loss limit)  $\sim 8\%$
- $v_2(\text{string})$ : grows up to  $\sim 10\%$  larger than  $v_2(\text{jet, limit})$
- $v_2(\text{h})$ : string decay reduces  $v_2 \rightarrow v_2(\text{jet}) < v_2(\text{h}) < v_2(\text{string})$



*For  $p_T > 2\text{GeV}$  ( $p_T \approx 10\text{ GeV}$ )*

*Ind. Frag. with  $C = 2.5 \rightarrow v_2 \approx 5\%$  (4%)*

*Large E-loss factor  $C \rightarrow +3\%$*

*Fluid parton  $v_2 \rightarrow +1\%$*

*JFS with  $C = 8 \rightarrow v_2 \approx 9\%$  (8%)*



# Summary

- ***Jet-Fluid String (JFS) formation and decay*** is proposed as a mechanism to produce high  $p_T$  hadrons.
  - Effective to produce high  $p_T$  hadrons
  - Event-by-Event Energy-Mom. conservation  $\leftrightarrow$  Ind. Frag.
  - Entropy does not decrease, but increases.  $\leftrightarrow$  Reco.
- When we FIT  $p_T$  spectrum, ***large  $v_2$  emerges at high  $p_T$*** 
  - Large E-loss+fluid parton  $v_2$
- Problems and Homeworks
  - Mechanism of large E-loss
  - d+Au fit  $\rightarrow$  Cronin Effects
  - s-quarks, string spectral func.





# Comparison with Previous Works

- J. Casalderrey-Solana, E.V. Shuryak, hep-ph/0305160
  - Quarks, diquarks and gluons in QGP cut color flux ( $\sim$  JFS).
  - Large E-loss is generated by “phaleron”
  - *Large E-loss leads “surface emission”  $\rightarrow$  large  $v_2$*
- Recombination (Duke-Osaka-(Minnesota)-Nagoya)
  - Predicts large  $v_2$  ( $\sim 10$  %) at high-pT
    - Sharply edged density dist.  $\rightarrow$  E-loss  $\propto L \rightarrow v_2 \approx 10$  %
    - Woods-Saxon density dist.  $\rightarrow v_2 \approx 5$  %
  - Entropy problem:  $S(\text{QGP}) \approx S(\text{H})$  requires Res. and Strings
  - *Spectral Func.:  $\delta$  func.  $\leftrightarrow$   $\theta$  func. in JFS*

# *K-factor*

- **K-factor** → absolute value of  $\sigma_{\text{jet}}$

- **Experimental Data:**  $pp \rightarrow \pi^0$  @  $\sqrt{s_{\text{NN}}} = 200 \text{ GeV}$  (PHENIX)

$$\frac{1}{\sigma^{\text{exp}}} \frac{d^2 \sigma^{\text{exp}}}{2\pi p_T d p_T dy} = K \frac{\sigma^{\text{pQCD}(1st)}}{\sigma^{\text{exp}}} \frac{d^2 N^{\text{pQCD}(1st)}}{2\pi p_T d p_T dy} \quad A = K \frac{\sigma^{\text{pQCD}(1st)}}{\sigma^{\text{exp}}}$$

$\sigma^{\text{Exp.}} = 21.8 \text{ mb}$  (trigger)

$\sigma^{\text{pQCD}(1st)} = 9.9 \text{ mb}$

- **pythia6.3 fit:**

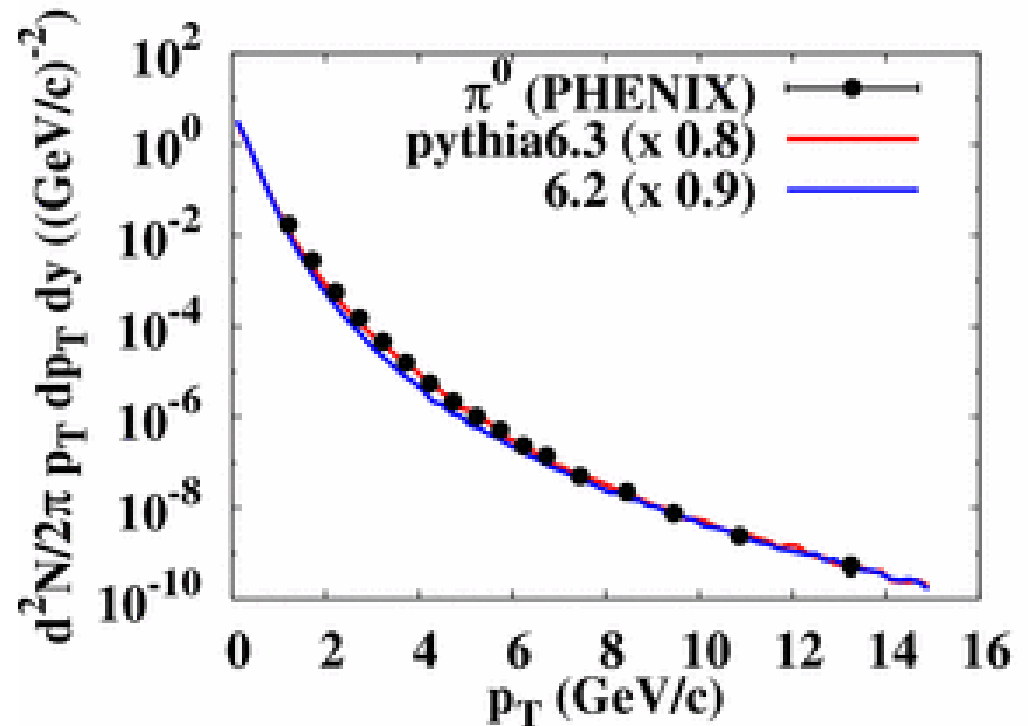
$A \approx 0.8 \rightarrow K = 1.8$

$(\sigma_{\text{jet}} (p_T^{\text{hard}} > 2 \text{ GeV}/c) \approx 17.5 \text{ mb})$

- **pythia6.2 fit:**

$A \approx 0.9 \rightarrow K = 2.0$

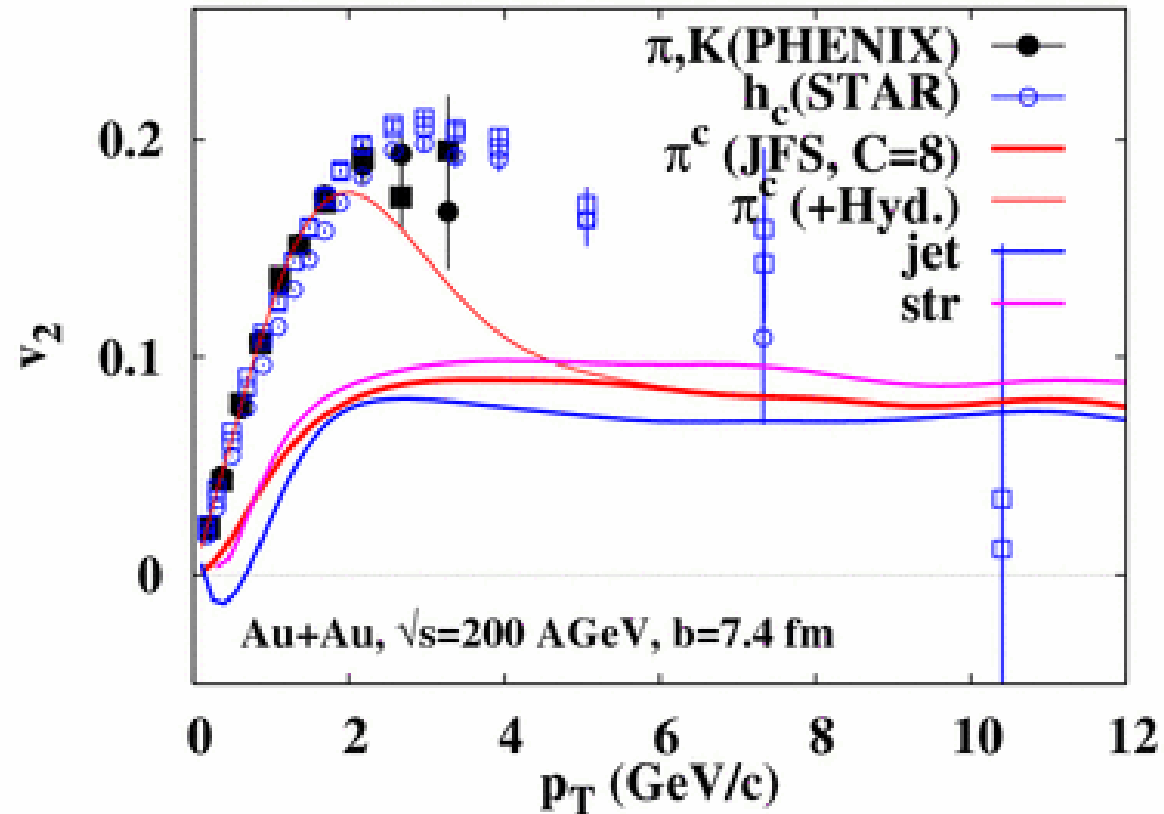
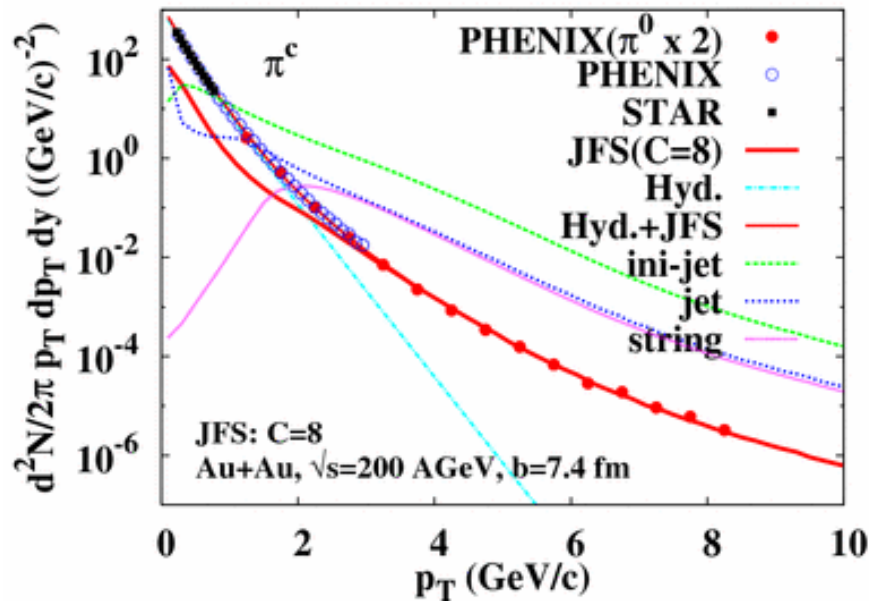
$(\sigma_{\text{jet}} \approx 19.6 \text{ mb})$



# Combined with Low $p_T$ spectrum

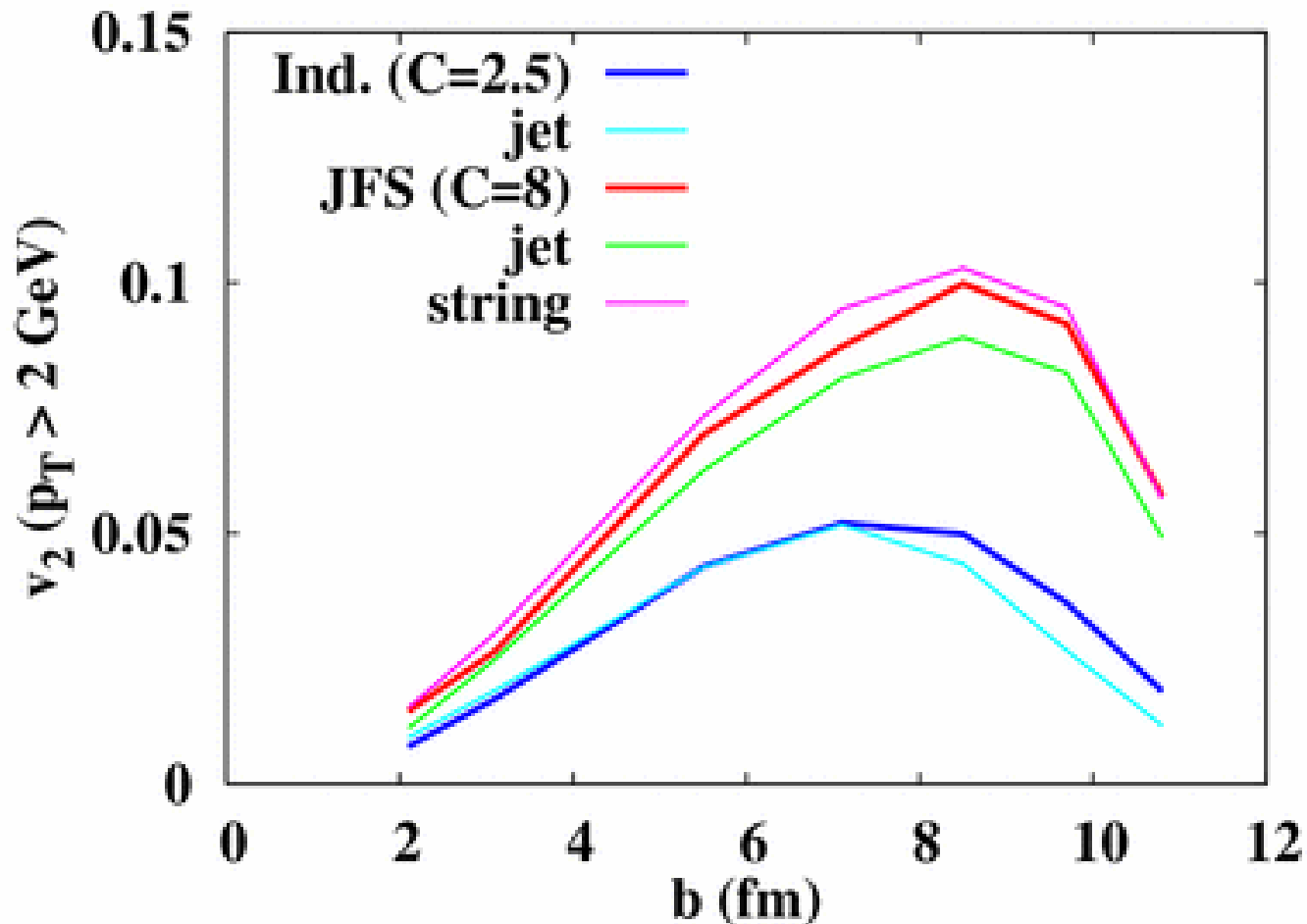
- Low  $p_T$  spectrum is assumed and combined.

$$E \frac{d^3 N_{Hyd}}{dp^3}(p_T) = A \exp(-p_T/T) (1 + B / (1 + (p_T/p_0)^8)) \quad v_2^{Hyd}(p_T) = 0.14 p_T$$



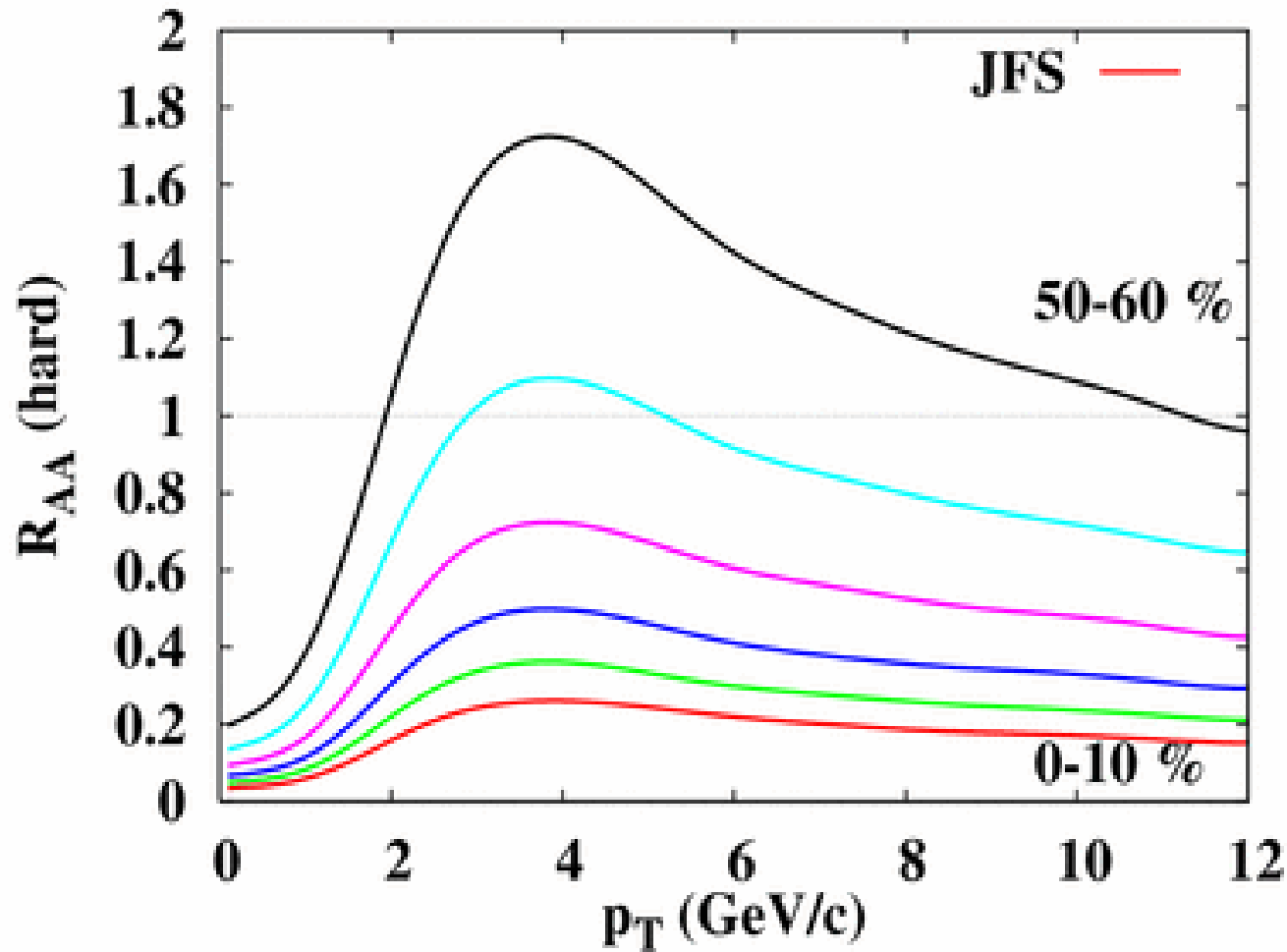
# *Elliptic Flow: Centrality Deps.*

- Ind. (C=3):  $v_2 \sim 5\%$  at  $b \approx 7$  fm
- JFS (C=8):  $v_2 \sim 10\%$  at  $b \approx 8.5$  fm



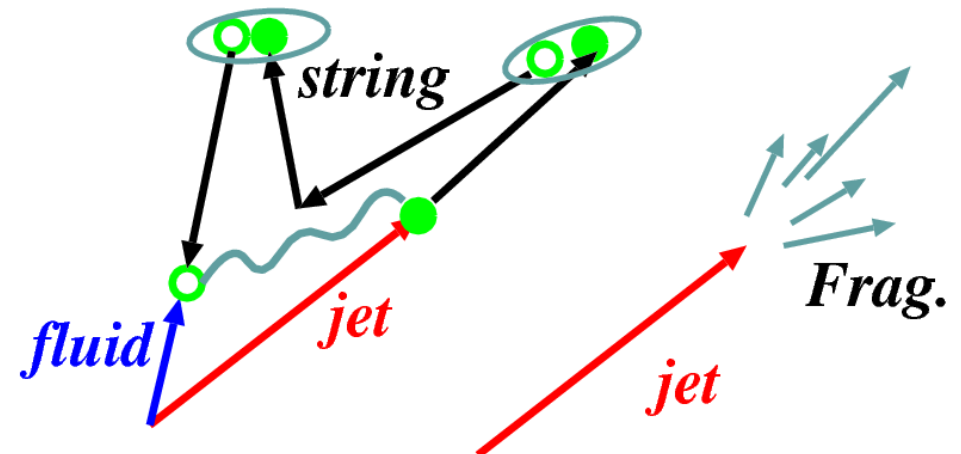
# Nuclear Modification Factor

## ■ Centrality Deps.



# Discussion

- Mechanism to produce high  $p_T$  hadrons in JFS
  - String Decay from Lorenz boosted fluid
  - Relative momentum is relatively small
    - Smaller number of hadrons with high  $p_T$  are formed
- ↔ Independent Frag. (Large no. of Low  $p_T$  hadrons)



# Energy Loss Factor

- Additional Factor for Energy Loss → High  $p_T$  hadron yield
- Exp. Data:  $p_T$  spectra of  $\pi$  in Au+Au (PHENIX, STAR)

$$\frac{d^2 N^{Exp.}}{2\pi p_T dp_T dy} = N_{jet} \frac{1}{N_{jet}} \frac{d^2 N^{JFS}(C)}{2\pi p_T dp_T dy}$$

→ Determining  $N_{jet}$  is important!

$N_{coll} = 373$  @  $b=7.4$  fm (PHENIX estimate)

$\sigma_{jet}^{NN} = 17.5$  mb (pp fit pythia 6.3),  $\sigma_{tot}^{NN} = 47.4$  mb (JAM)

$$N_{jet} = \sigma_{jet}^{NN} \int d^2r T_A(r_T + b/2) T_B(r_T - b/2) = \frac{\sigma_{jet}^{NN}}{\sigma_{tot}^{NN}} N_{coll}$$

$$T_A(r_T) = \int dz \rho(r_T, z)$$



# Further Problems

- Very large energy loss is required to explain  $p_T$  spectrum.
  - $C \approx 8$  in JFS  $\leftrightarrow C \approx 2.7$  in Hydro+Jet model (Hirano-Nara)
- Is it possible to justify this large energy loss ?
- Elliptic flow at medium  $p_T$  is underestimated.
  - Fluid-Fluid String would be necessary to consider.
- Large baryon yield at medium  $p_T$  may not be explained.
  - Three parton string ? (Jet-Fluid-Fluid, Fluid-Fluid-Fluid)
- String formation probability should be evaluated in pQCD matrix element + string level density.
- Strange hadrons

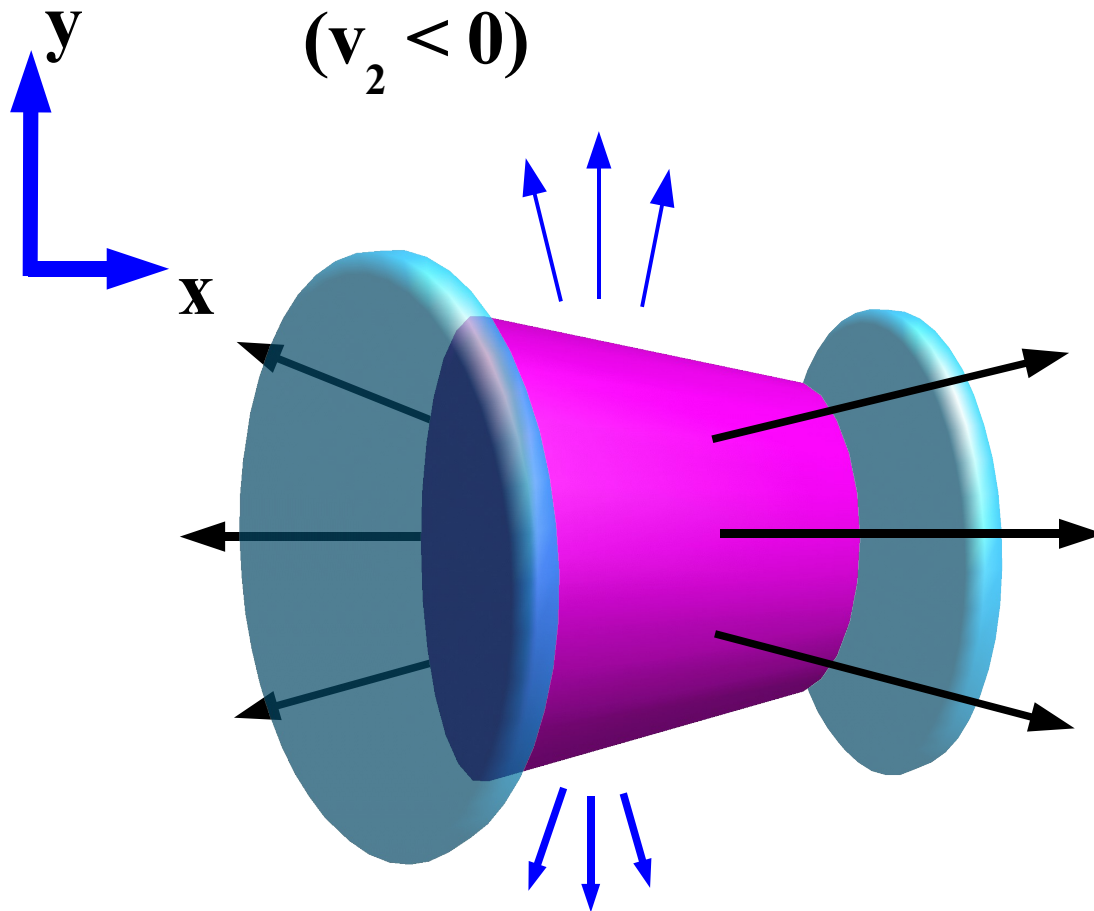




# *Elliptic Flow*

## Out-of-Plane Flow

$$(v_2 < 0)$$



## ★ What is Elliptic Flow ?

- Anisotropy in P space

## ★ Hydrodynamical Picture

- Sensitive to the Pressure

Anisotropy in the Early Stage

- Early Thermalization is

Required for Large  $v_2$

## In-Plane Flow

$$(v_2 > 0)$$

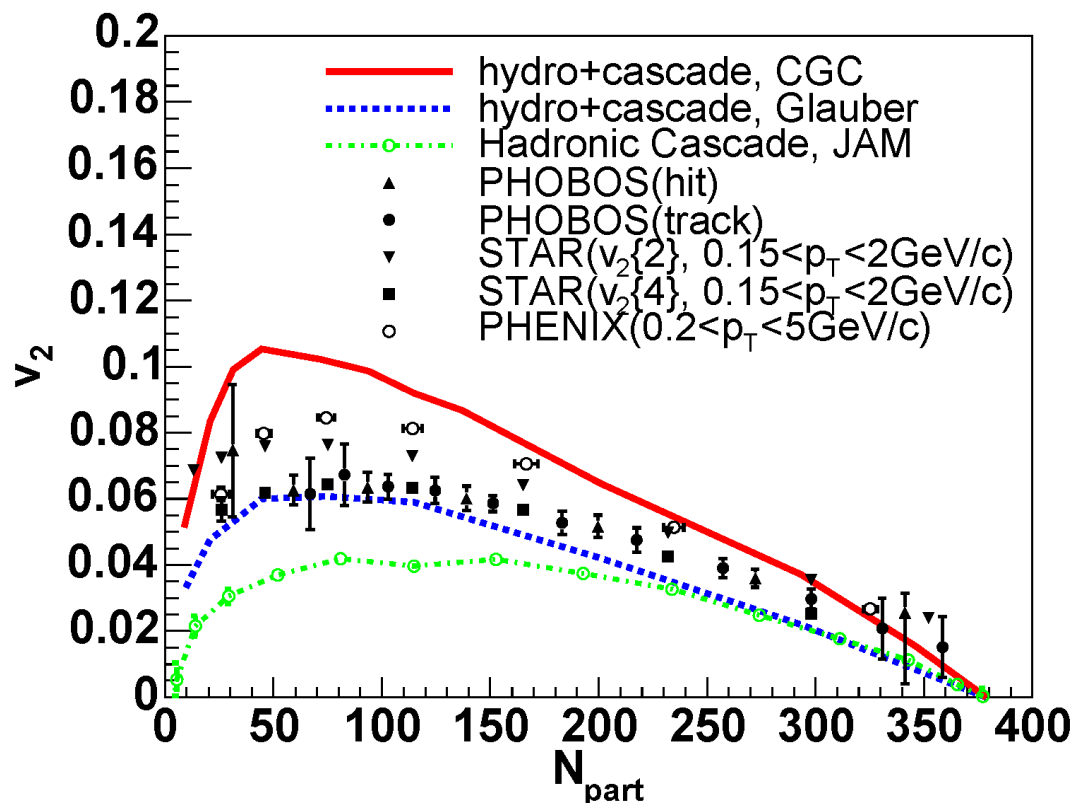
$$v_2 \equiv \left\langle \frac{p_x^2 - p_y^2}{p_x^2 + p_y^2} \right\rangle = \langle \cos 2\phi \rangle$$



# $v_2(\text{Centrality})$ @RHIC 200GeV, Au+Au

- カスケード模型 JAM は、周辺衝突になるにつれて (図の左側)、小さくなってしまふ。
- 実験値は、流体模型+カスケードに CGC または Glauber 近似を仮定したものの中に位置する。

⇒ 流体描像が妥当  
⇒ 部分的に CGC



# Relativistic Hydrodynamics

## ■ EOM: Conservation Laws

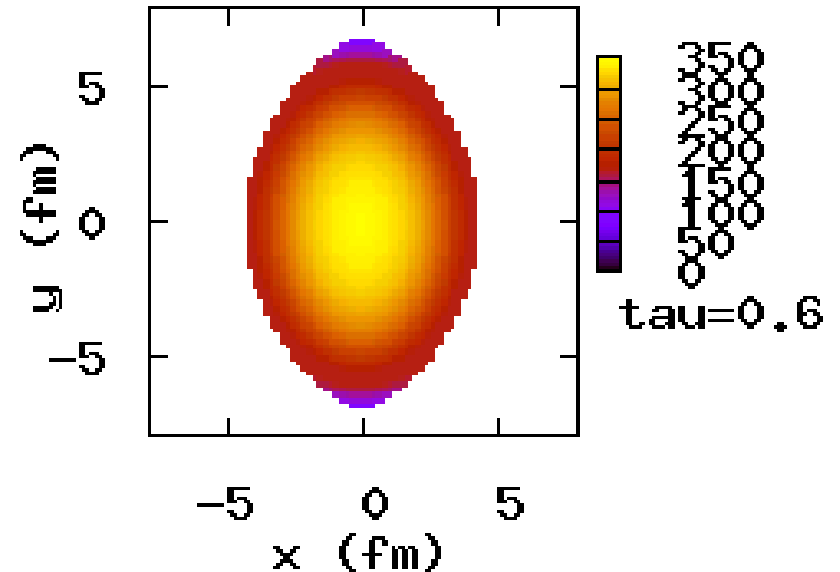
$\partial_\mu T^{\mu\nu} = 0$  Energy Momentum Conservation

$\partial_\mu n_i u^\mu = 0$  Conservation of Charge (Baryon, Strangeness, ...)

$$T^{\mu\nu} = (e + P)u^\mu u^\nu - P g^{\mu\nu}$$

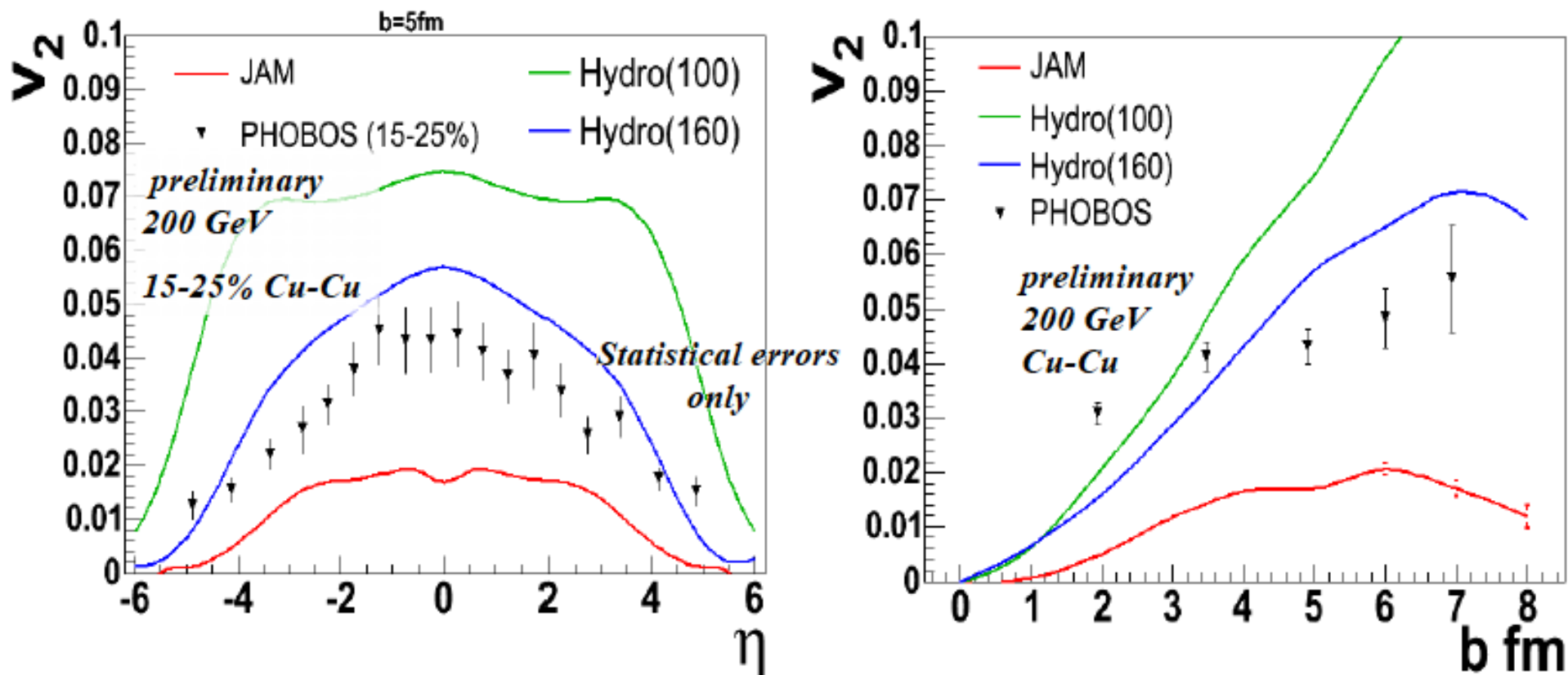
$e$  : energy density,  $P$ : pressure,

$u^\mu$  : four velocity  $\gamma(1, \mathbf{v})$ ,  $n_i$  : number density



T. Hirano, Y. Nara,  
Nucl. Phys. A743, 305 (2004)  
T. Hirano, K. Tsuda,  
Phys. Rev. C 66, 054905(2002)

# Compared to JAM Model



**Cu-Cu more like Hydro than JAM hadron string cascade model**

*Here JAM uses a 1 fm/c formation time. Hydro (160) has kinetic freezeout temperature at 160 MeV*

$v_2$  は、両模型の違いが顕著。

流体模型でも  $T^{\text{th}}$  ( $\Leftrightarrow$  Freeze out の早さ) で違いがある。