
Heavy Ion Collisions

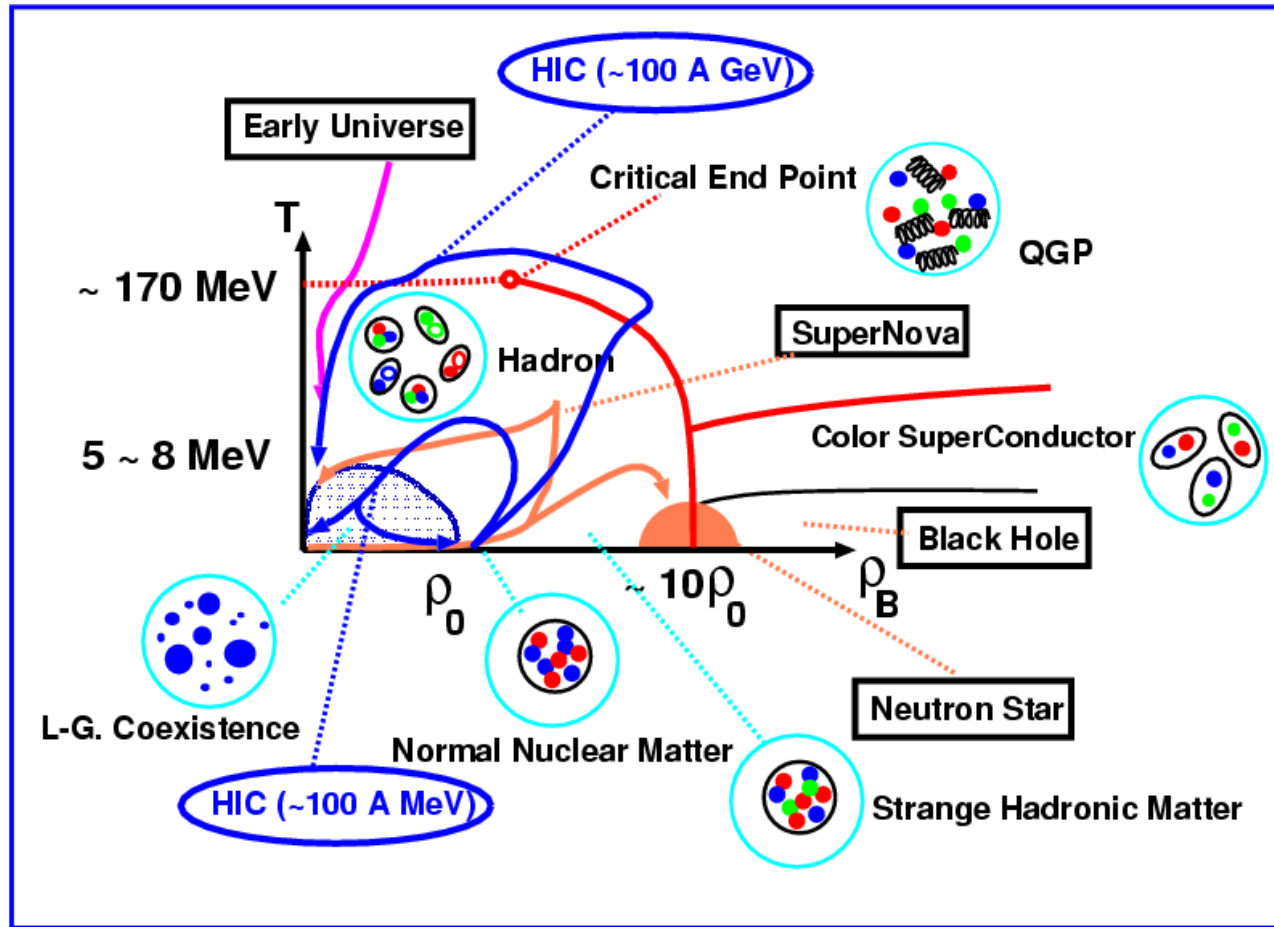
--- Past, Present, and Future ---

Seminar @ U. Tsukuba, 2007/10/18

Akira Ohnishi
Department of Physics, Faculty of Science,
Hokkaido University

- **Introduction**
- **HIC at $E_{\text{inc}} \sim 100 \text{ MeV/A}$**
- **HIC at $E_{\text{inc}} \sim (1-100) \text{ GeV/A}$**
- **HIC at RHIC**
- **Summary**

Hadronic Matter Phase Diagram



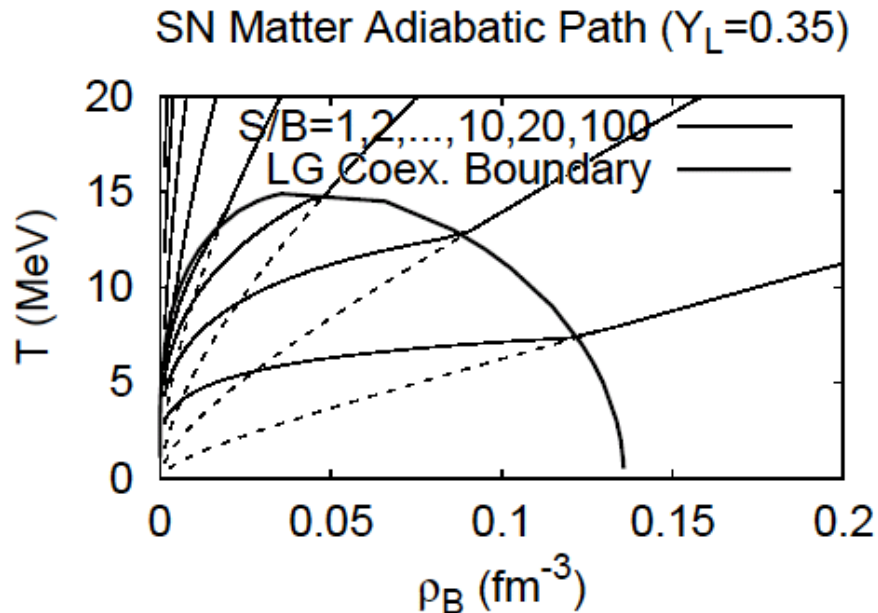
HIC (~ A few 100 A MeV) = Little Supernova
HIC (100+100 A GeV) = Little Big Bang

QCD 相転移=我々の宇宙の最後の真空相転移(菅沼談)

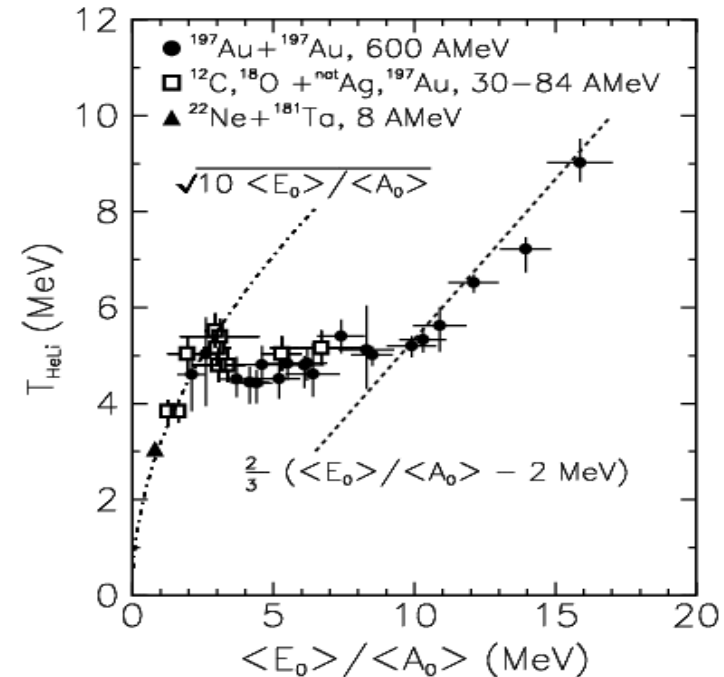
HIC at $E_{inc} \sim a \text{ few } 100 \text{ MeV}/A$

Physics of Fragmentation and Liquid-Gas Phase transition

- ◆ 低温では $\rho_B \sim (0.3-0.6) \rho_0$ において、 $dP/d\rho_B < 0$ (spinodal region)
 → 一様な核物質は不安定となり、液相と気相が共存する。



→ 重イオン反応という
 非平衡・非一様な状況で
 「相」の情報はみえるのか？



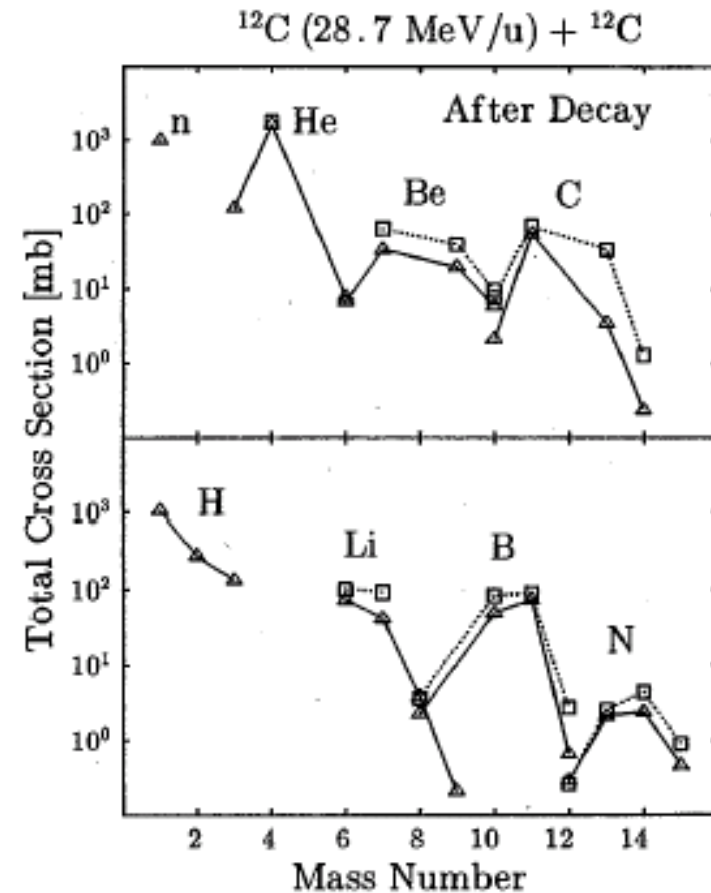
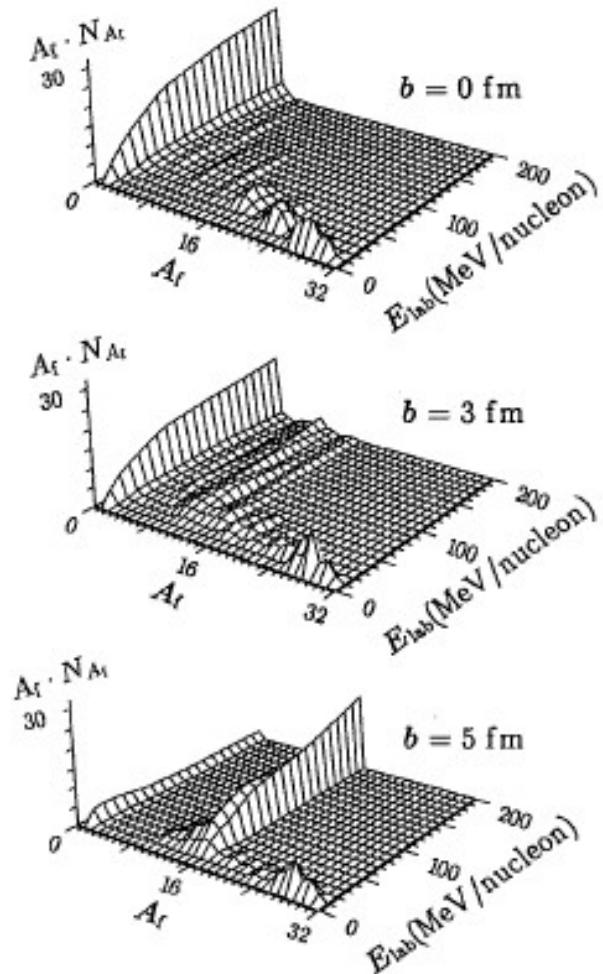
*J. Pochadzalla et al (GSI-ALLADIN collab.),
 PRL 75 (1995) 1040.*

$$Y_f \propto g_f \exp((B_f + Z\mu_p + N\mu_n)/T)$$

$$\rightarrow \frac{Y(^4\text{He})/Y(^3\text{He})}{Y(^7\text{Li})/Y(^6\text{Li})} \propto \exp(\Delta B/T)$$

Molecular Dynamics Study of Fragmentation

- Quantum Molecular Dynamics (QMD)
& Antisymmetrized Molecular Dynamics (AMD)
→ Reaction Dynamics, Mass & Isotope Dist.



Maruyama, Ohnishi, Horiuchi, PRC45('92)2355

Ono, Horiuchi, Maruyama, Ohnishi,
PTP87('92)1185

Molecular Dynamics Study of Fragmentation

● フラグメント分布を求める手続き

◆ Equation of Motion

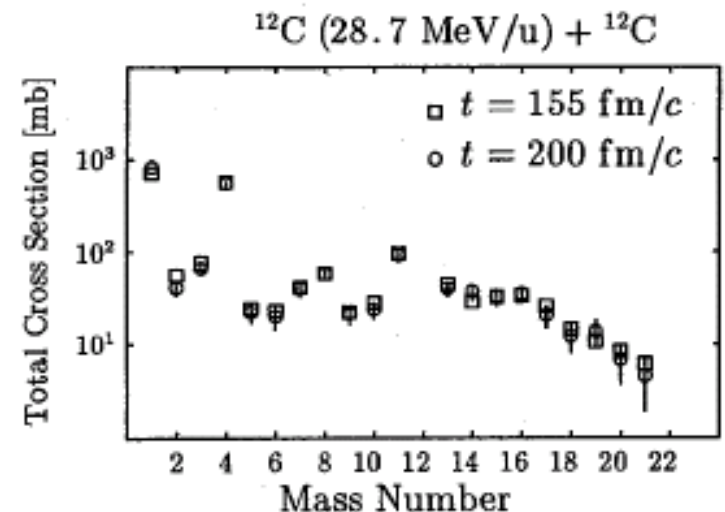
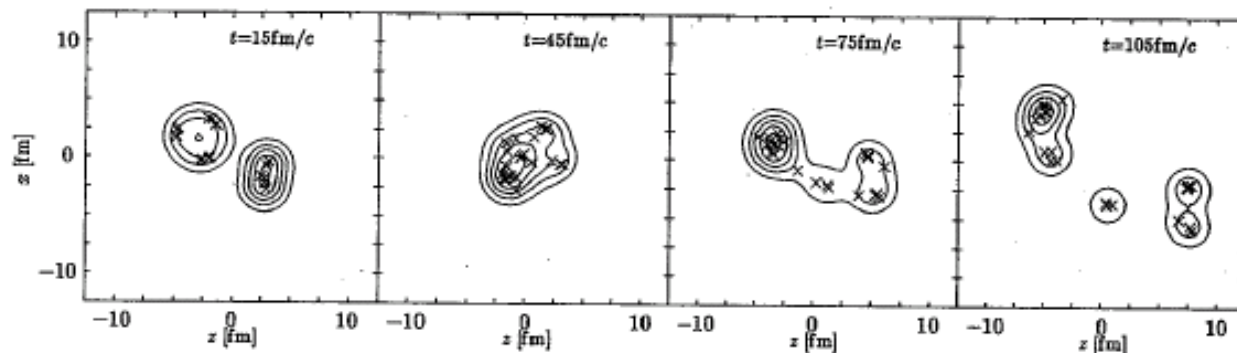
Gauss 波束の(反対称化)積波動関数+ 時間依存変分原理
→ (半古典的な)運動方程式

◆ クラスタ判定

終状態で位相空間の近い核子の集合を原子核と判定

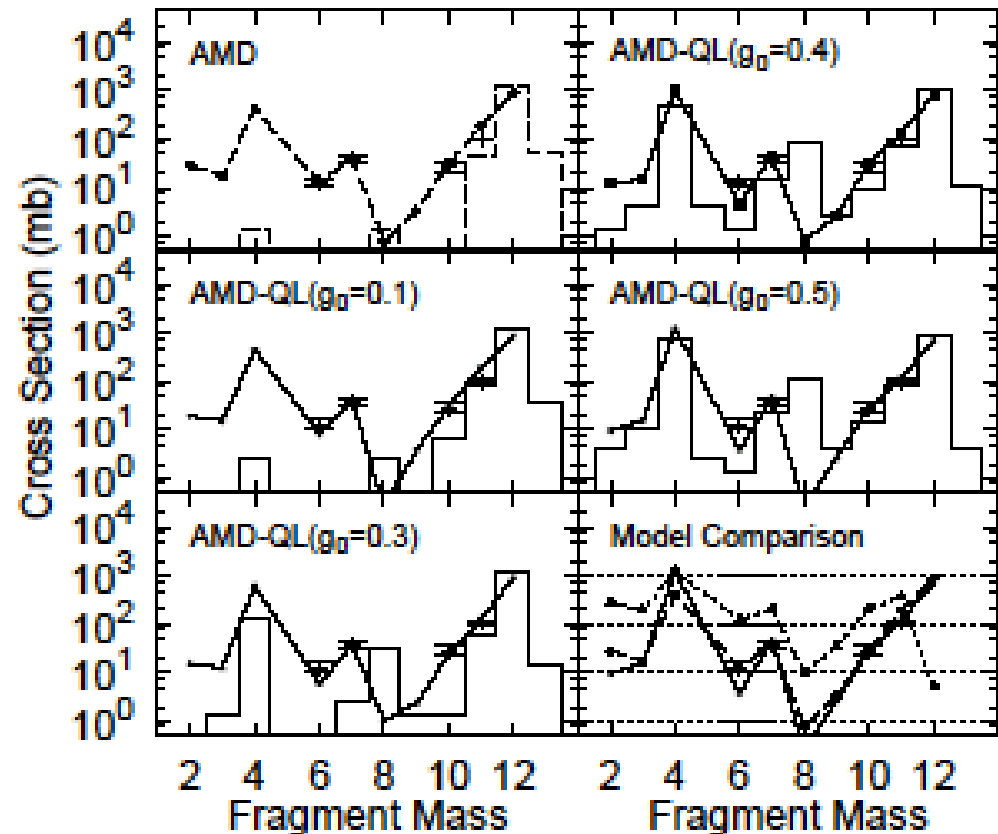
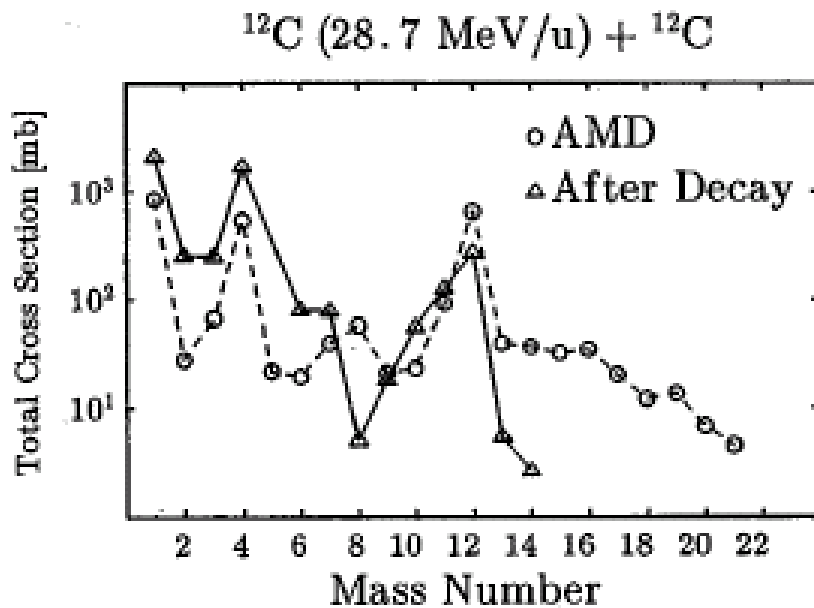
◆ 統計崩壊

原子核の励起エネルギーと角運動量から統計的に崩壊させる
(after burner)



Molecular Dynamics Study of Fragmentation

- 粒子シミュレーションでの時間スケール
 - ◆ 統計崩壊模型で与えられる時間スケールよりも長い
→ 古典的シミュレーションの問題点



p+ ^{12}C (45 MeV)

Hirata, Nara, Ohnishi, Harada, Randrup, 1999

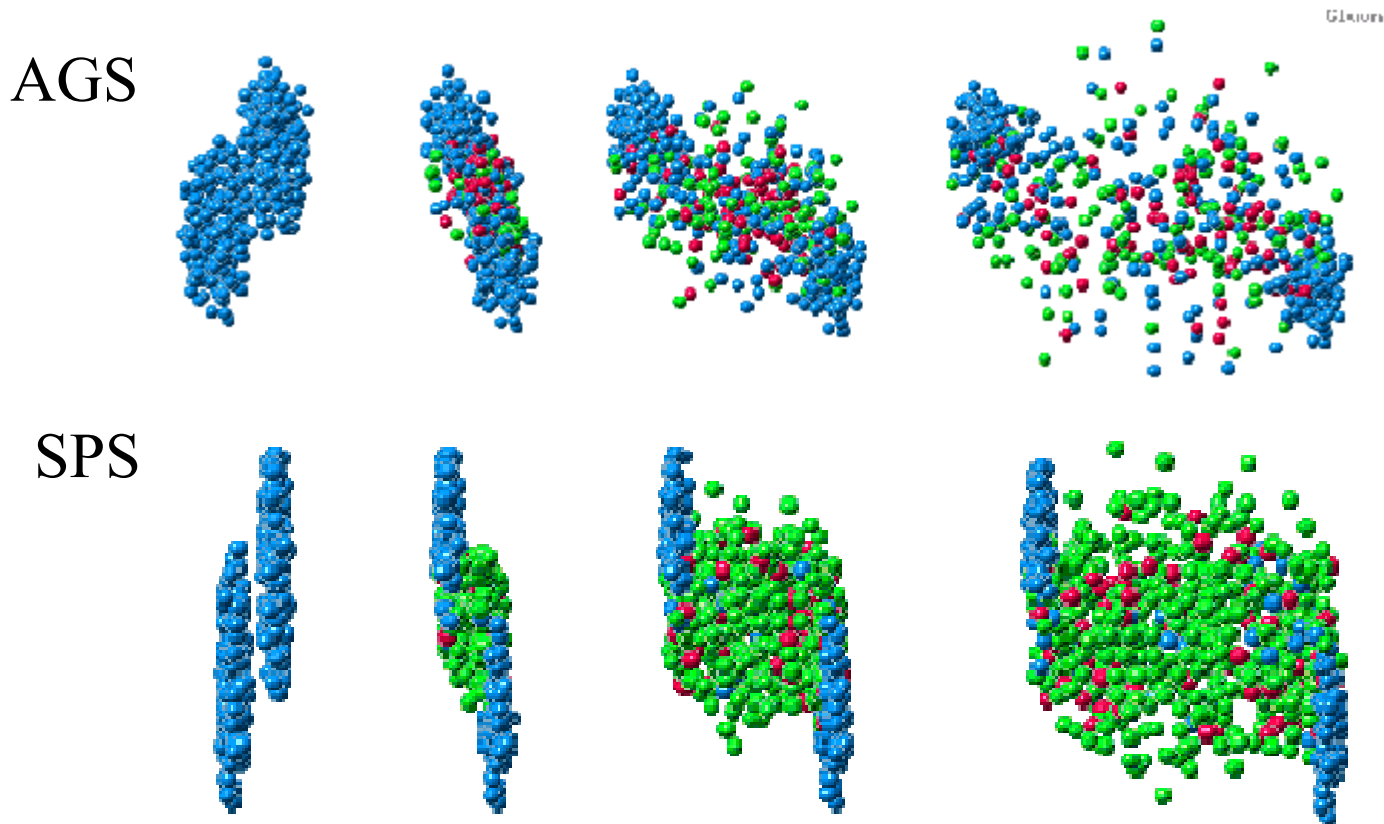
Ono et al., 1992

Lessons from HIC @ 100 A MeV

- フラグメントの起源
 - まず質量数の大きな励起した原子核が作られ、その「統計的」崩壊により多くの原子核が作られる。
 - ◆ 「大きな原子核の高い励起状態の状態数 ~ 位相空間」
 - 短い時間スケールでの系の励起エネルギー分布は古典的なシミュレーションでよく説明可能であろう。
 - ◆ 基底状態フラグメント放出、低エネルギーでの核子放出には、エネルギー集中が必要 → 統計崩壊モデルとの組み合わせが必要。
- 反応・崩壊の時間スケールが近い場合の問題点
 - ◆ 軽イオン(d, t, 3He , ...)、中間質量片(IMF)生成は比較的短時間でおこる
 - 量子揺らぎ、Coalescence 過程、軽イオン自体の輸送等をあらわに取り入れる必要がある。
 - ◆ 時間スケールをそのまま信頼できないだろう例(東大関連の仕事)
 - Penta Quark の崩壊幅、超新星での Pasta 状態生成時間(おそらく古典シミュレーションより短い時間でおこる。結論は問題なし)

Heavy-Ion Collisions at $E_{\text{inc}} \sim (1-100) A \text{ GeV}$

- Study of Hot and Dense Hadronic Matter
→ Particle Yield, Collective Dynamics (Flow), EOS,



JAMming on the Web, linked from <http://www.jcprg.org/>

Collective Flow and EOS: Old Problem ?

- **1970's-1980's: First Suggestions and Measurement**
 - **Hydrodynamics suggested the Existence of Flow.**
 - **Strong Collective Flow suggests Hard EOS**
- **1980's-1990's: Deeper Discussions in Wider E_{inc} Range**
 - **Momentum Dep. Pot. can generate Strong Flows.**
 - **E_{inc} deps. implies the importance of Momentum Deps.**
 - **Flow Measurement up to AGS Energies.**
- **2000's: Extention to SPS and RHIC Energies**
 - **EOS is determined with Mom. AND Density Dep. Pot. ?**

Old but New (Continuing) Problem !

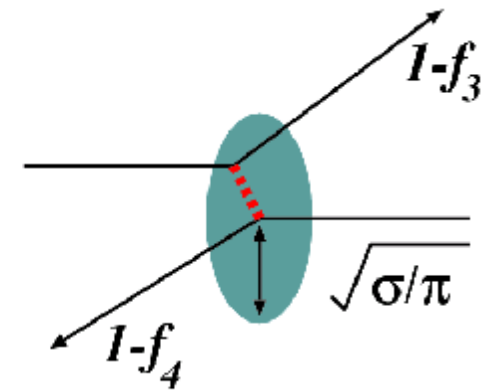
Mean Field Dynamics + Two-Body Collision

- **BUU Equation** (Bertsch and Das Gupta, Phys. Rept. 160(88), 190)
 - Time-Dependent Hartree-Fock Eq. を Wigner 変換 → Vlasov Eq.
 - Pauli blocking を導入した Boltzmann 方程式の衝突項を導入
 - 低エネルギーで重要な平均場理論と
高エネルギー(>100 A MeV) で支配的なカスケード過程を統合
 - どのような粒子自由度を導入すべきか？

$$\frac{\partial f}{\partial t} + v \cdot \nabla_r f - \nabla U \cdot \nabla_p f = I_{coll}[f]$$

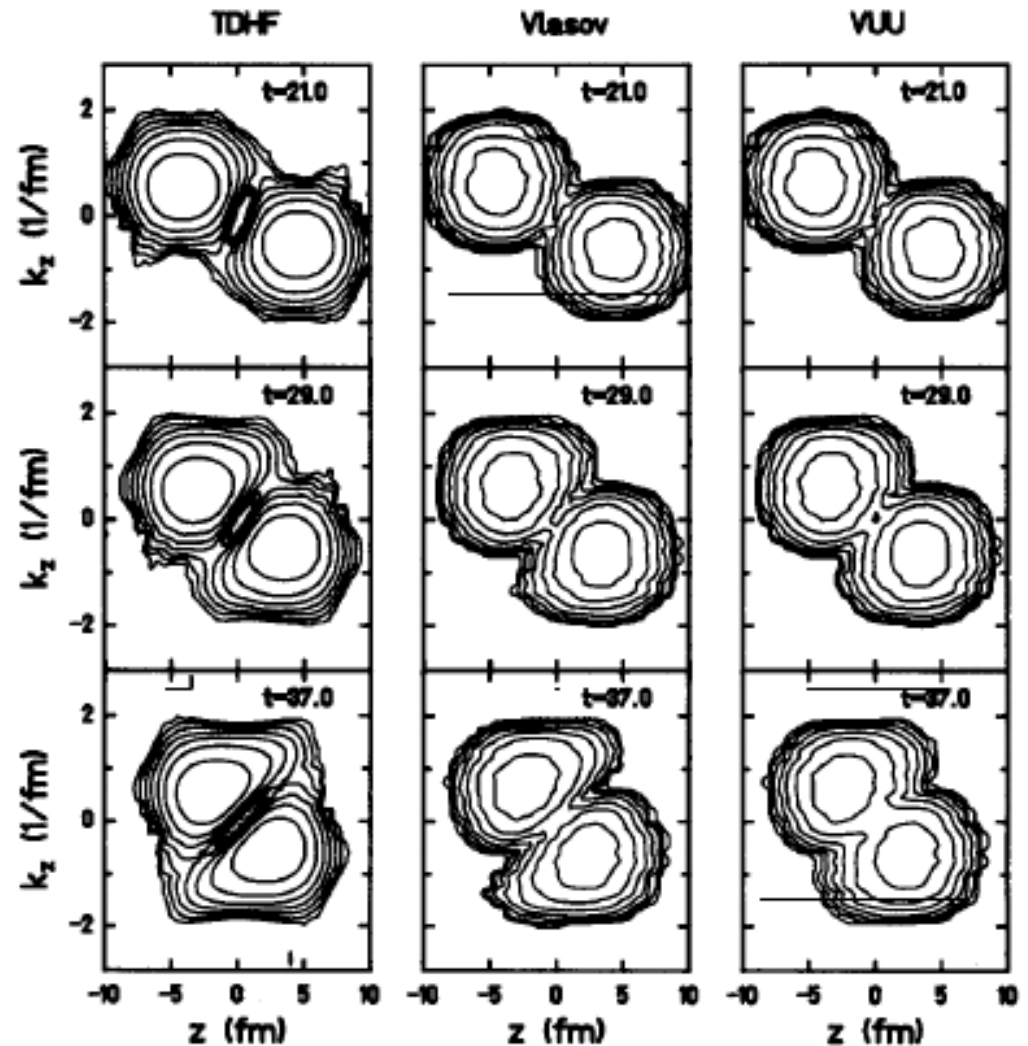
$$I_{coll}[f] = -\frac{1}{2} \int \frac{d^3 p_2 d\Omega}{(2\pi\hbar)^3} v_{12} \frac{d\sigma}{d\Omega}$$

$$\times [f f_2 (1-f_3)(1-f_4) - f_3 f_4 (1-f)(1-f_2)]$$



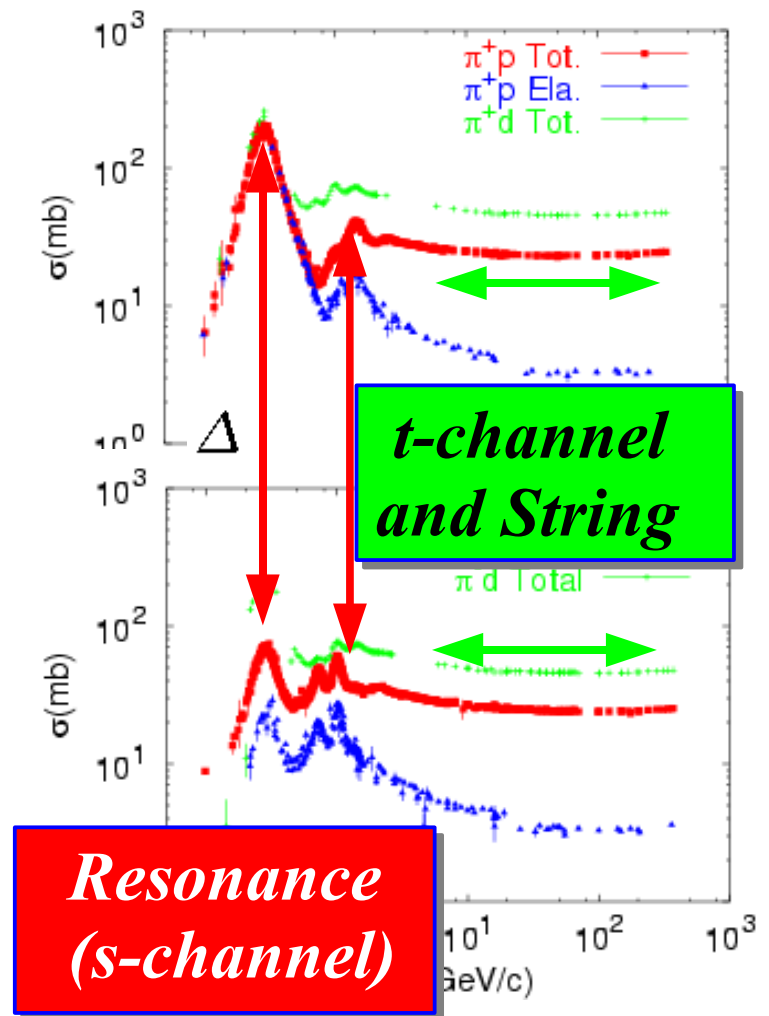
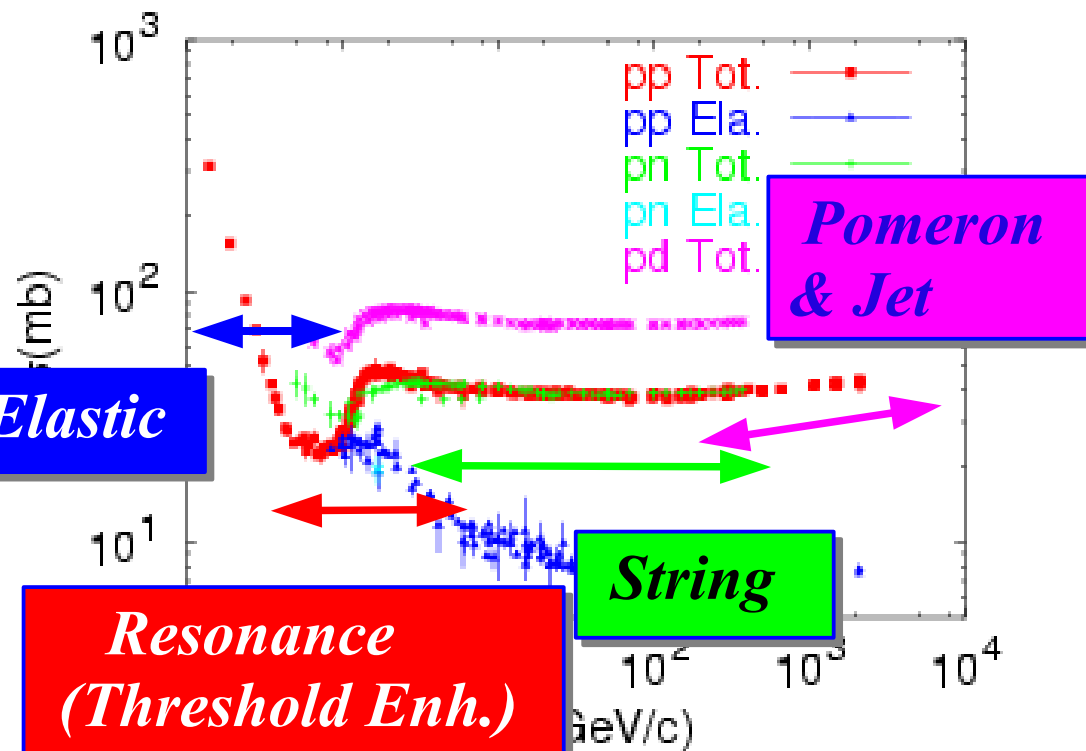
Comparison of TDHF, Vlasov and BUU(VUU)

- Ca+Ca, 40 A MeV
(Cassing-Metag-Mosel-Niita, Phys. Rep. 188 (1990) 363).



Hadron-Hadron Cross Sections

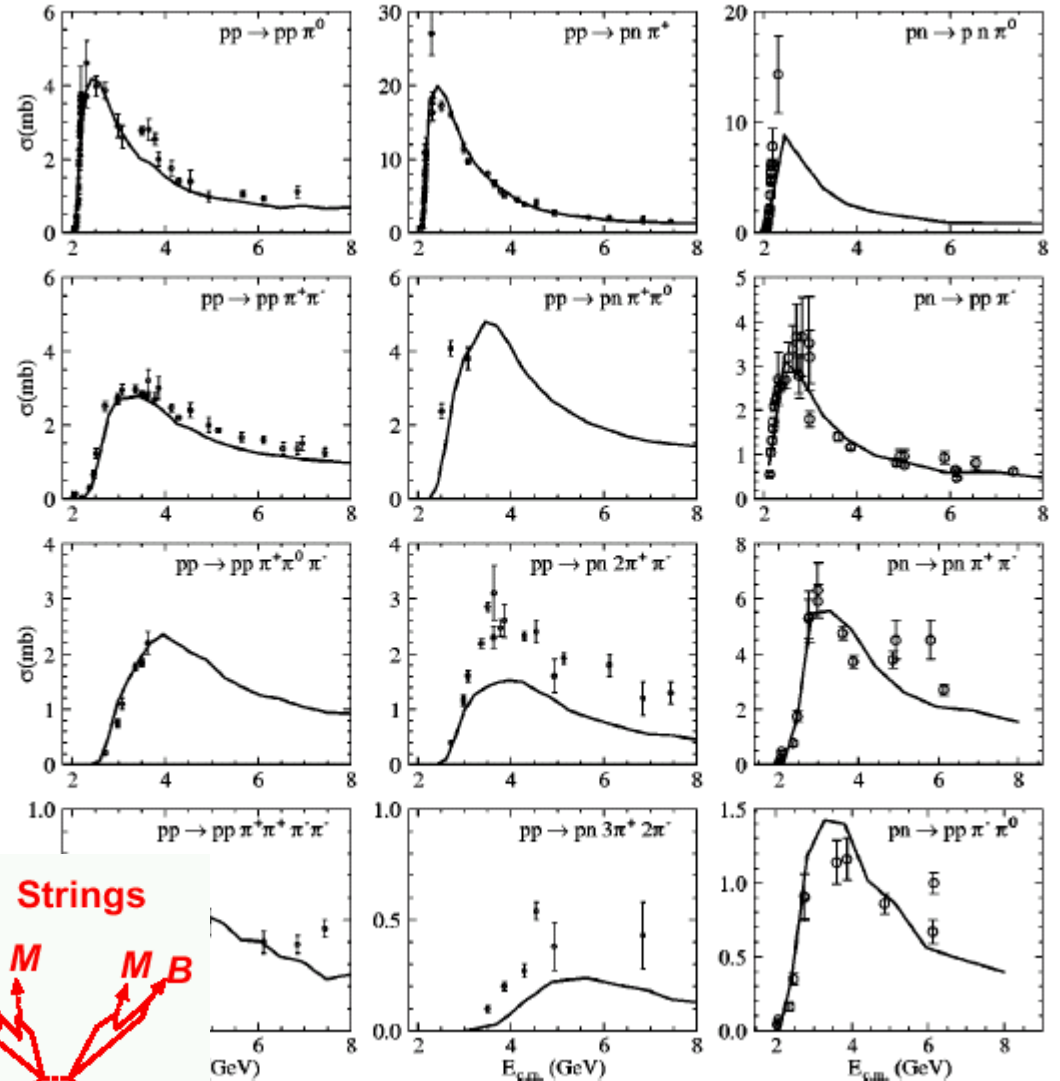
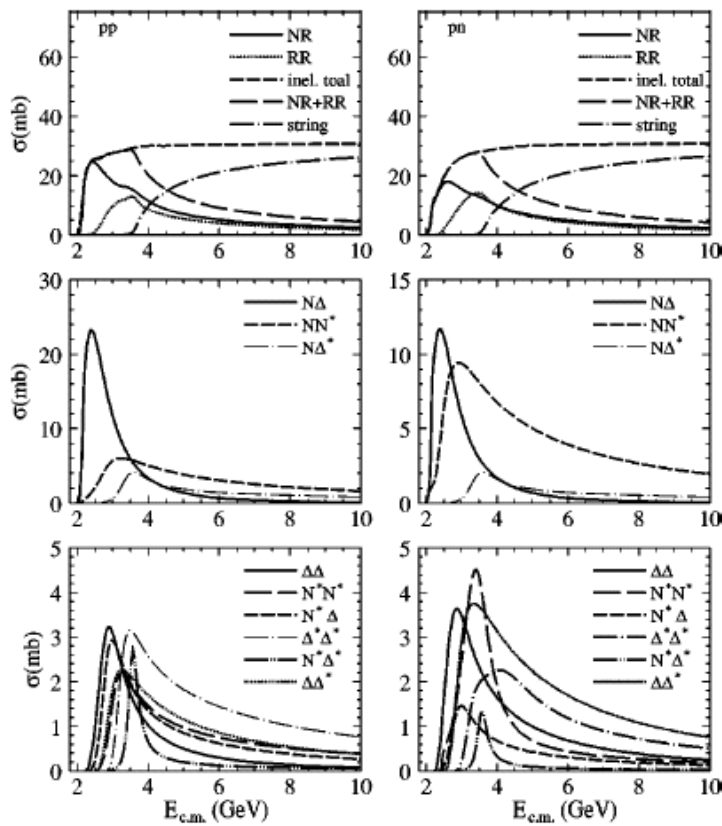
From Particle Data Group



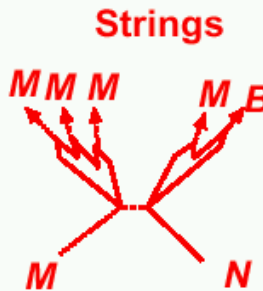
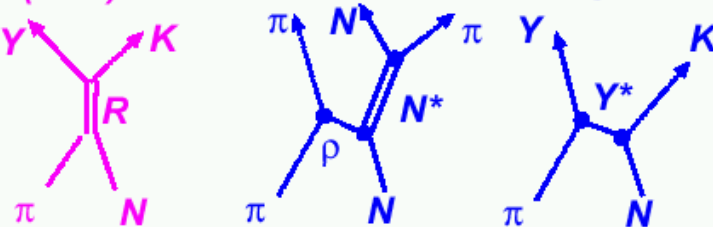
Exclusive Cross Sections in JAM

Nara, Otuka, AO, Niita, Chiba (JAM), PRC 61 (2000), 024901.

Ground State Hadrons, Resonances, and Strings

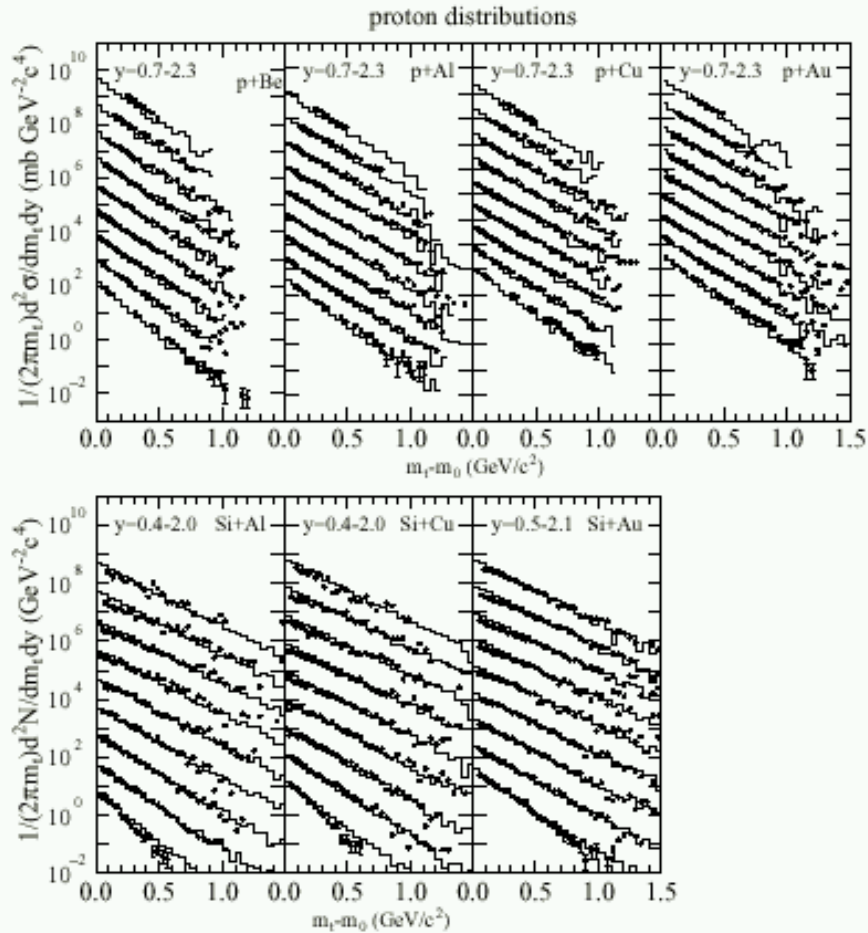


s-channel **t-channel** **u-channel**
R (or S) Form. **Reggeon Exch.** **Baryon Exch.**

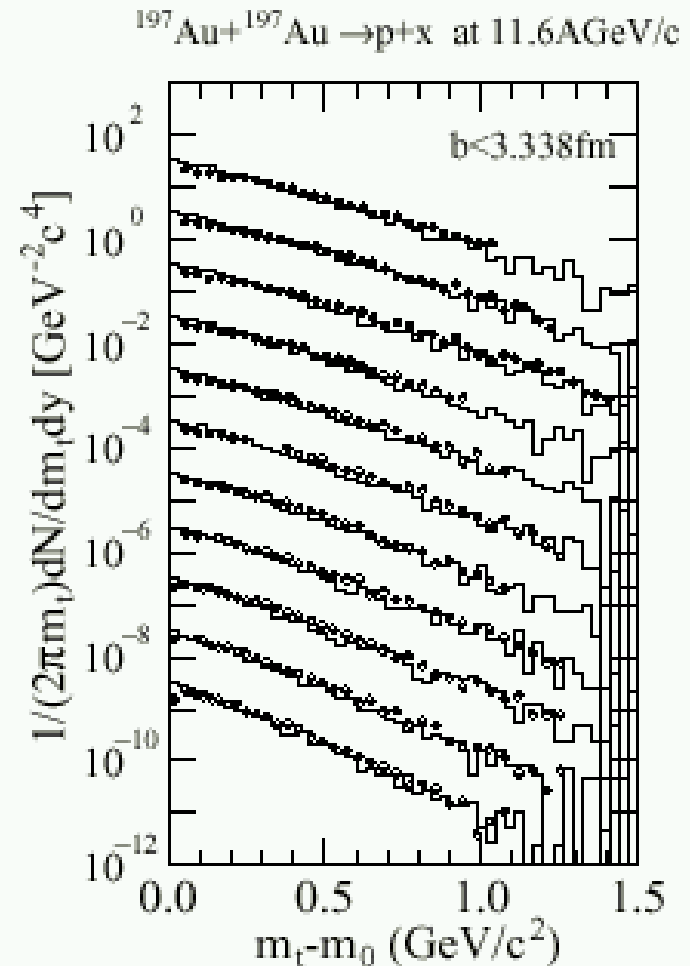


JAM Results @ AGS Energy

• p-A collisions



• Au+Au Collision



***JAM explains AA collisions as well as pA collisions:
→ Good Elementary Cross Sections for MM, MN and NN***

Mean Field and Particle DOF Effects @ AGS

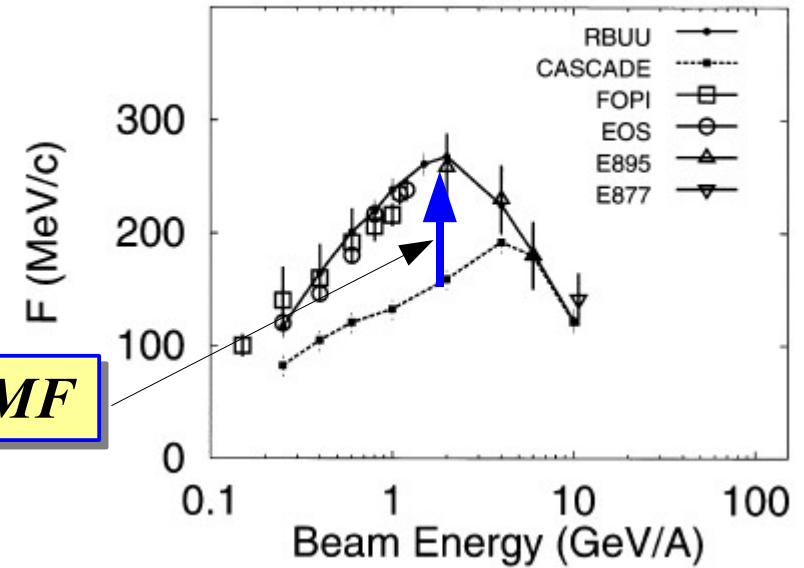
- Mean Field Effects at AGS
→ Visible but small for p_T spectrum

Sahu, Cassing, Mosel, Ohnishi, 2000

P.K. Sahu et al. / Nuclear Physics A 672 (2000) 376–386

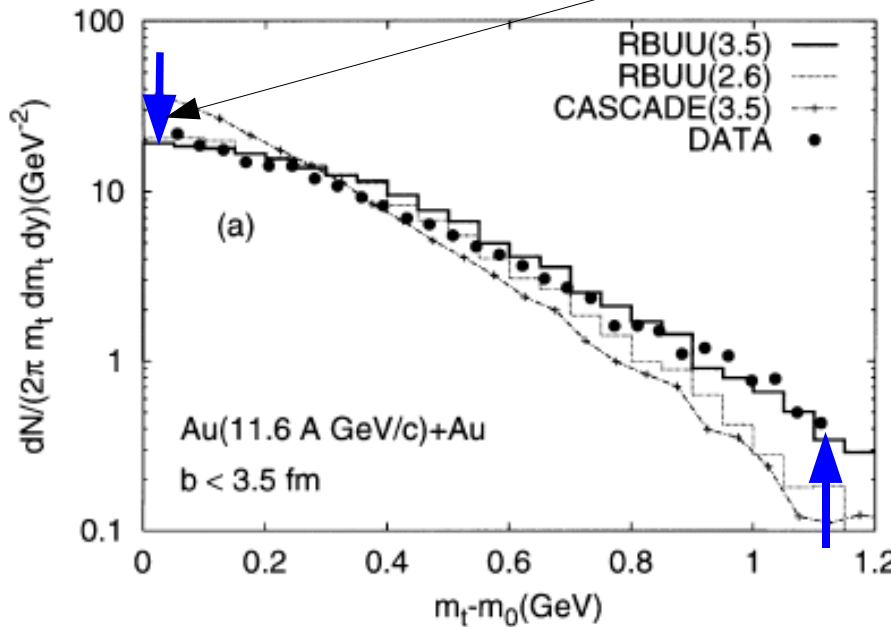
Essential for Flow

- Particle DOF Effects
→ Seen at high p_T



P.K. Sahu et al. / Nuclear Physics A 672 (2000) 376–386

Repulsive MF



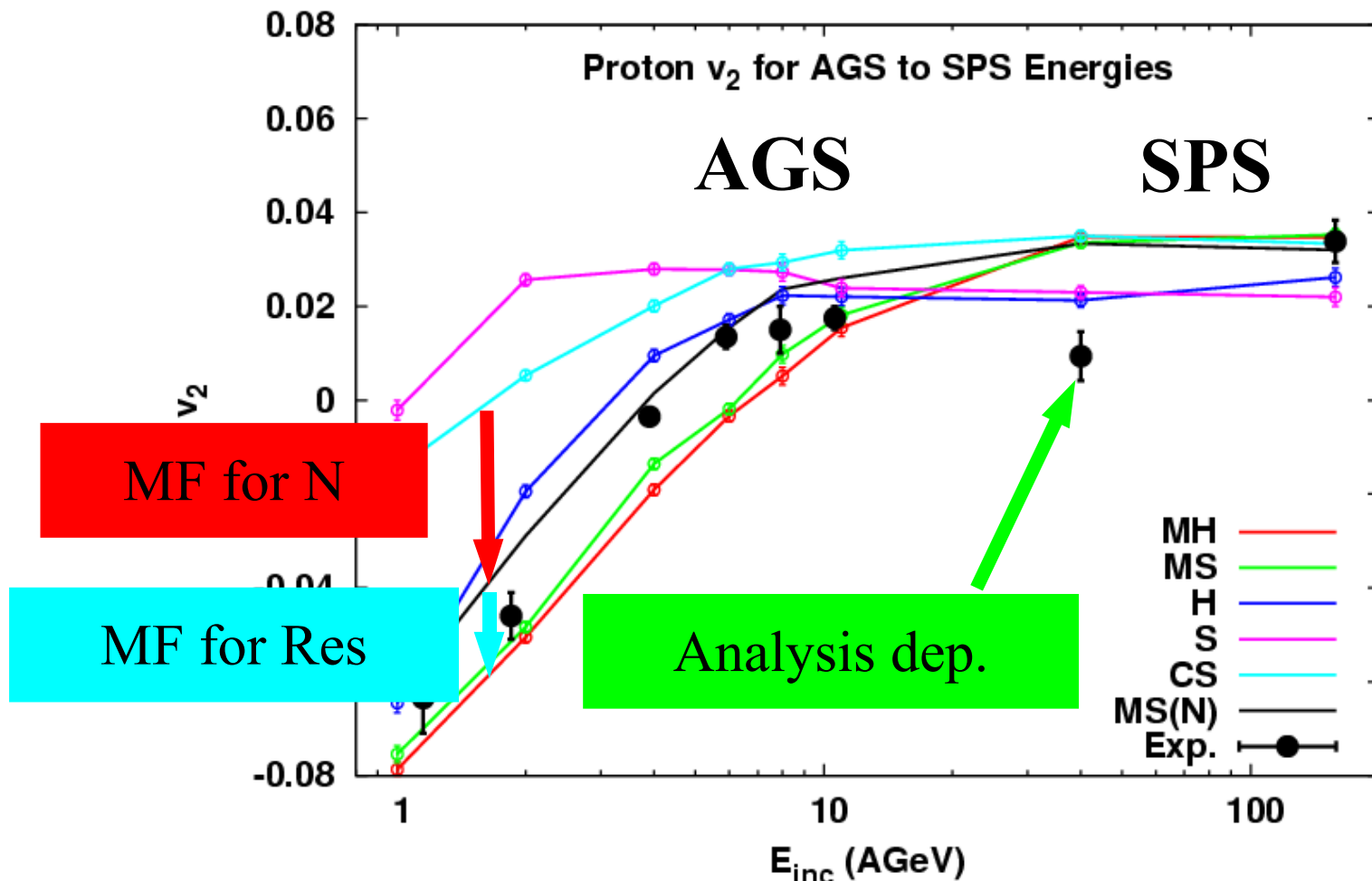
Switching $\sqrt{s} = 3.5$ GeV
(JAM fit)

Switching $\sqrt{s} = 2.6$ GeV
(HSD default)

Elliptic Flow from AGS to SPS

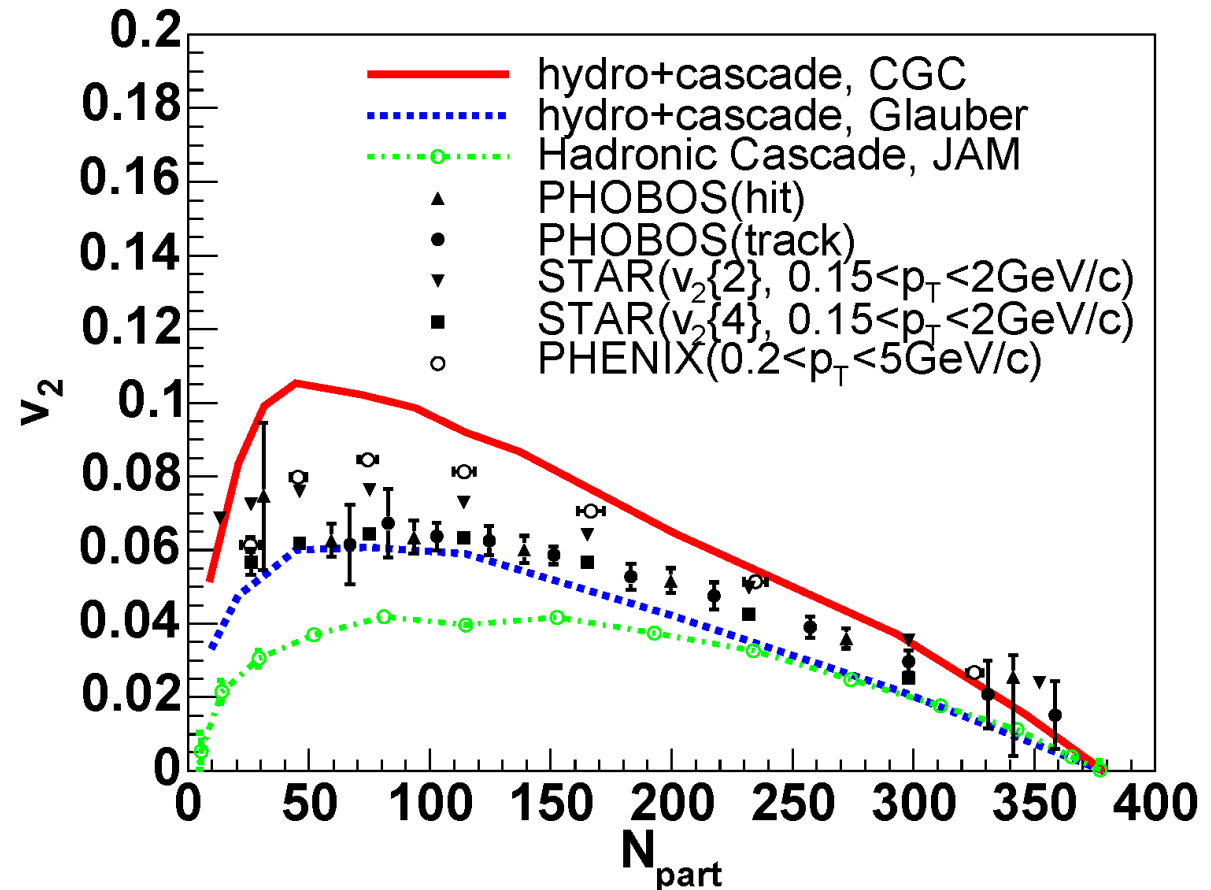
Isse, AO, Otuka, Sahu, Nara, PRC 72 (2005), 064908

- JAM-MF with p dep. MF explains proton v_2 at 1-158 A GeV
 - v_2 is not very sensitive to K (incompressibility)
 - Data lies between MS(B) and MS(N)



Cascade vs Hydro @ RHIC: Au+Au

- Comparison of v_2 as a function of N_{part}
 - Cascade predict smaller v_2 in peripheral collisions
 - Data lies between hydro results with two different initial condition CGC (Color Glass Condensate) and Glauber type initial condition.



*Hydro is better,
CGC may be realized
in central collisions.*

Lessons from AGS and SPS Energy HIC

- 粒子生成の主要過程
 - ◆ 1 A GeV Energy → 共鳴粒子生成 + 共鳴崩壊
 - ◆ 10 A GeV Energy (AGS) → 2共鳴ハドロン生成、ストリング生成+崩壊
 - ◆ 100 A GeV Energy (SPS) → ストリング生成+崩壊
- 必要な自由度の輸送を取り入れる必要性
 - ◆ pT スペクトルに直接的に影響を与える。
 - ◆ あらわな自由度を取り入れない場合
 - formation time 等を導入して相互作用の強さ(圧力)を調整(量子論的な「漸近領域に達する時間」だけではないだろう)
- RHICエネルギーでのハドロン輸送モデルの失敗
 - ◆ SPS エネルギーまでで成功している formation time を使うと、反応初期での相互作用が小さすぎる
 - 遅い熱平衡化時間、小さな楕円フロー(特に high pT)

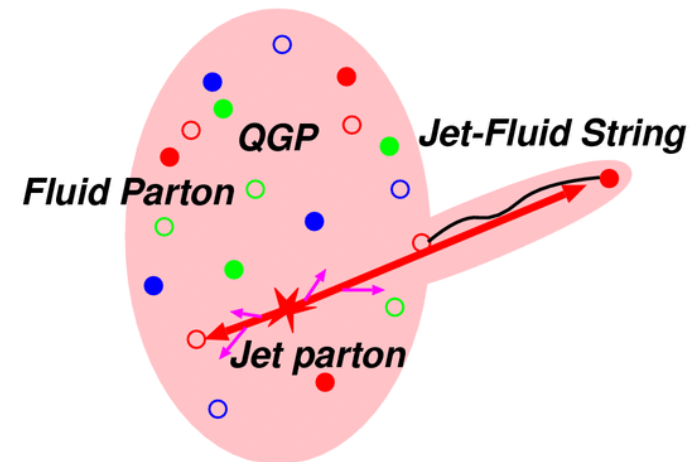
Jet-Fluid String 模型における粒子相関

東大理、阪大理^A、北大理^B、フランクフルト大^C
平野哲文、一瀬昌嗣^A、水川零^B、奈良寧^C、大西明^B、吉野公二^B

Hadron correlations in Jet-Fluid String model

T.Hirano, M.Isse^A, R. Mizukawa^B, Y.Nara^C, A. Ohnishi^B, K.Yoshino^B
U. Tokyo, Osaka U.^A, Hokkaido U.^B, Frankfurt U.^C

- Introduction
- High p_T でのハドロン化模型
- JFSでのハドロン相関
- まとめ



Isse, Hirano, Mizukawa, AO, Yoshino, Nara, nucl-th/0702068

High p_T ハドロン生成

- GSI, AGS, SPS → 共鳴ハドロン、ストリング生成と破砕

Nara et al., PRC61('00),024901; Isse et al., PRC72('05),064908.

- RHICでの標準描像 = pQCD + E-loss + 独立破砕

$$\begin{aligned} \frac{dN^{AA}(b)}{dy d^2 p_T} &= \int d\mathbf{r}_T t_A(\mathbf{r}_T - b/2) t_B(\mathbf{r}_T + b/2) && \text{Geometry} \\ &\times K \sum_{abcd} \int dx_a dx_b d^2 k_a d^2 k_b f_{a/A} f_{b/B} \frac{d\sigma^{ab \rightarrow cd}}{d\hat{t}} && \text{pQCD} \times \text{K-fac.} \\ &\times D(E_c - \Delta E_c(\mathbf{r}_T); c \rightarrow h) && \text{E-loss} + \text{Indep. Frag.} \end{aligned}$$

→ しかし問題は残っている (high p_T での v_2 など)

→ RHICではストリング破砕は必要ないのか？

Hirano et al., PLB636('06)299 (afterburner improves v_2 in Hydro+Jet)

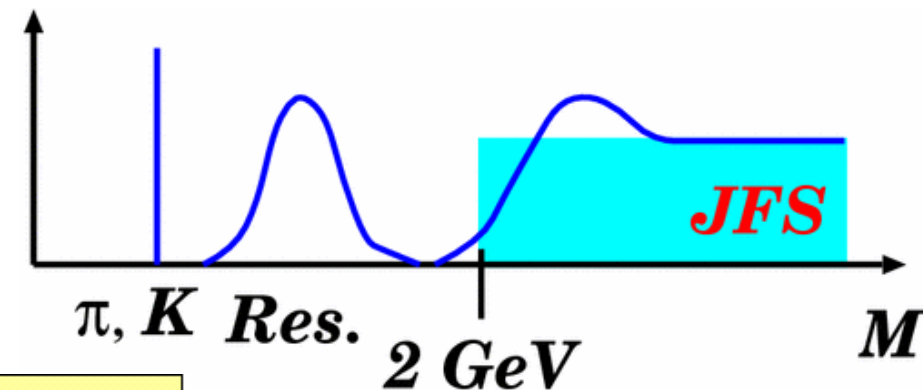
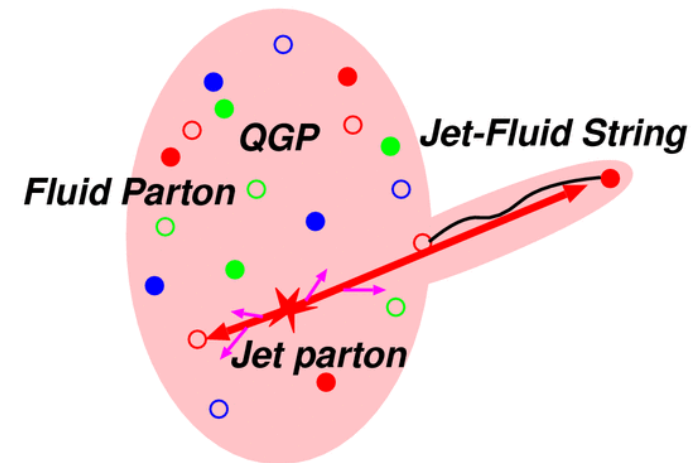
Sahu et al. Pramana 67 ('07)257 (cascade → low p_T data except for v_2)

Parton Cascade (Kinder-Geiger) (Parton cluster → hadrons)

Jet-Fluid String formation and decay: Model

Isse, Hirano, Mizukawa, AO, Yoshino, Nara, nucl-th/0702068

- ミニジェット生成=pQCD (PYTHIA 6.4)
- QGP中のパートン伝播
 - ◆ 3次元流体模型
Hirano-Nara, PRL91('03), 082301;
PRC69('04),034908
Hirano,Tsuda, PRC66('02),054905
 - ◆ GLV エネルギー損失× factor (C)
Gyulassy-Levai-Vitev, PRL85('00), 5535.
- スtring生成・破砕
 - ◆ "スペクトル"関数 Θ ($\sqrt{s} - 2 \text{ GeV}$)



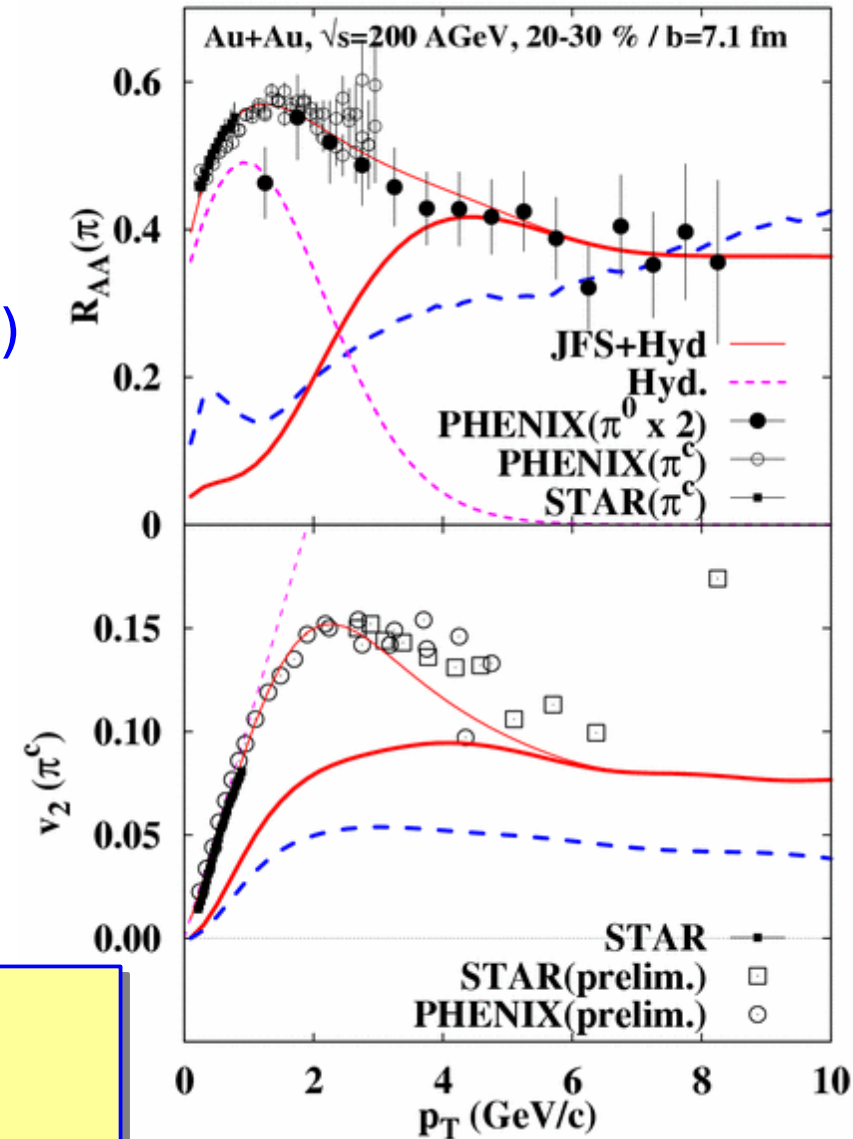
$$D(j \rightarrow h) = \int d^3 k_f f_f(k_f, T, u_\mu, \mathbf{x}(\tau_f)) \\ \times S(s = (k_j + k_f)^2) D(\text{String}(\sqrt{s}, k_j, k_f) \rightarrow h)$$

Jet-Fluid String formation and decay: Results

Isse, Hirano, Mizukawa, AO, Yoshino, Nara, nucl-th/0702068

- 高い high p_T ハドロン生成率
→ 大きなエネルギー損失が必要
 - ◆ R_{AA} fit → E-loss fac. $C = (6-8)$
 $C = (2-3)$ in Hydro+Jet (Hirano-Nara)
- 大きなエネルギー損失
+ 流体パートンの v_2
→ high p_T での大きな v_2
 - ◆ $v_2 \sim 8\%$ @ $p_T > 6$ GeV/c
 $v_2 \sim (3-5)\%$ in Indep. Frag.

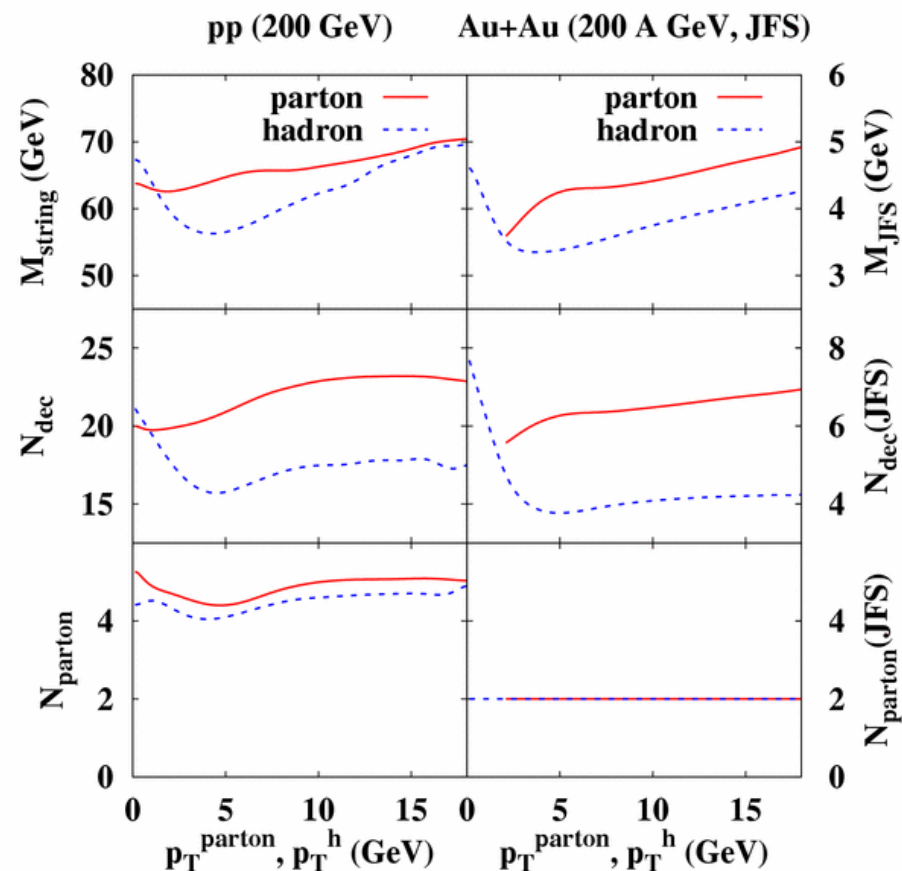
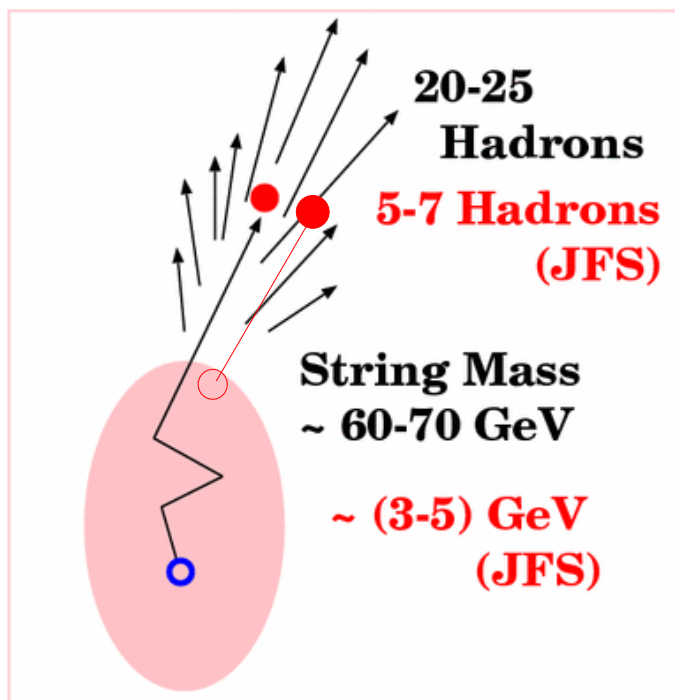
High p_T で R_{AA} を説明する E-loss で
 v_2 データをほぼ説明
→ なぜ high p_T ハドロンが作られやすい?



独立破碎模型との比較

独立破碎模型(IF)

- ppでは IF ~ ストリング破碎
→ 重いストリング(60-70 GeV)が
多くのハドロン(20-25)に崩壊
- AAでの IF @ p_T (After E-loss)
~ pp でのストリング破碎 @ p_T

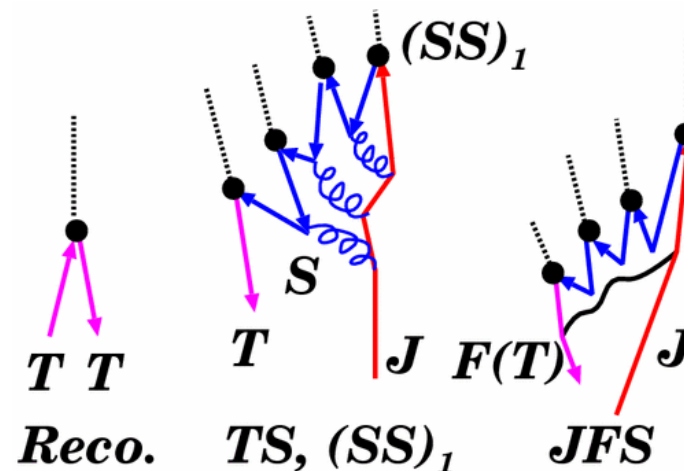


ジェットパートンの独立破碎
~ 重いストリングの崩壊
→ AA衝突のジェット破碎段階で
これほど重いストリングが作られるか？

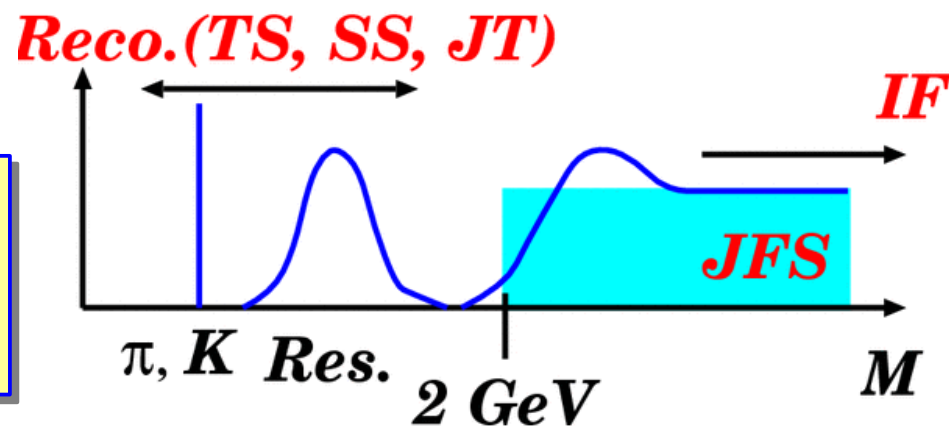
High p_T 領域での再結合模型との比較

- **TT(T) \rightarrow med. pT**
Nonaka et al., PRC69('04),031902
- **JT \rightarrow med. pT (soft-hard)**
Greco-Ko-Levai, PRC68('03),034904
- **TS \rightarrow med. pT, $(SS)_1 \rightarrow$ high pT**
Hwa-Yang, PRC70('04)024905
- **TT(T) \rightarrow Res. \rightarrow med./low pT**
Greco-Ko, PRC70('04)024901

T: Thermal (Fluid) parton
J: Jet parton
S: Shower parton

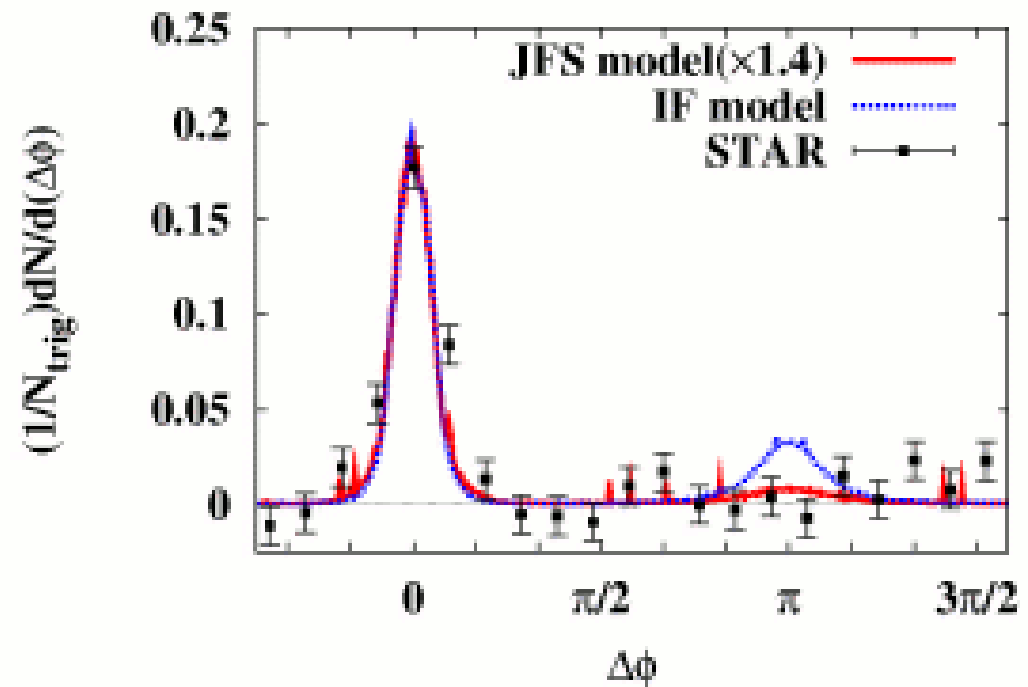


- T +”part of Jet”によるハドロン生成
- π の直接生成より共鳴崩壊が有利
 \rightarrow JFSの描像と無矛盾

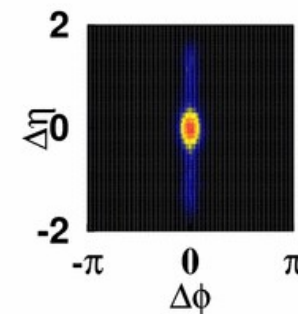
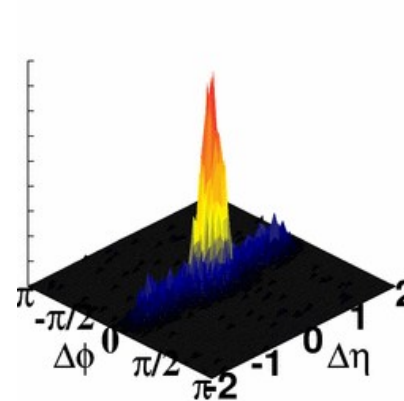
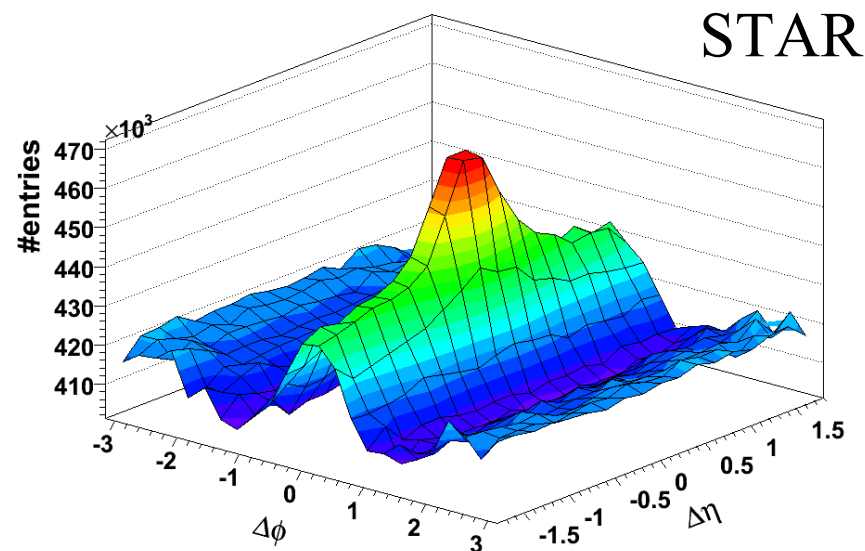


ハドロンの方角角相関

- Au+Au衝突での後方相関の消失 = QGP生成の強いシグナル
 - ◆ Hydro + Jet model Hirano & Nara, PRL (2003)
 - R_{AA} を説明する E-loss では後方相関の抑制が十分でない
 - ジェットの変化する散乱効果を取り入れると説明可能
 - ◆ Jet “absorption” model Drees, Feng, Jia, PRC71('05), 034909
 - ジェットパートンが $\exp(-\alpha L)$ の確率で「吸収」
 - エネルギー損失との関係は？
 - ◆ JFS
 - R_{AA} を説明する E-loss により、後方相関は消失



- Jet-Ridge structure
→ 横に狭く、縦に広い相関
(narrow $\Delta\phi$ + wide $\Delta\eta$ corr.)
 - ◆ JFS では見えない
 - ◆ Chiu and Hwa: 早い時点で Jet により熱せられた広い η の範囲の流体 parton が coalesce
 - ◆ Shuryak: エネルギーを失った jet parton が流体中の「非平衡成分」として現れる
 - ◆ Wong: Jet のエネルギー損失時に放出された radiation が平衡に達する前の広い η 分布を持つ bulk parton に大きな p_T を与えてハドロン化
→ radiation の p_T を拡大すると、弱いが ridge 構造を出す



$p_T(\text{rad. G}) \times 5$

水川

Lessons from RHIC physics (until now...)

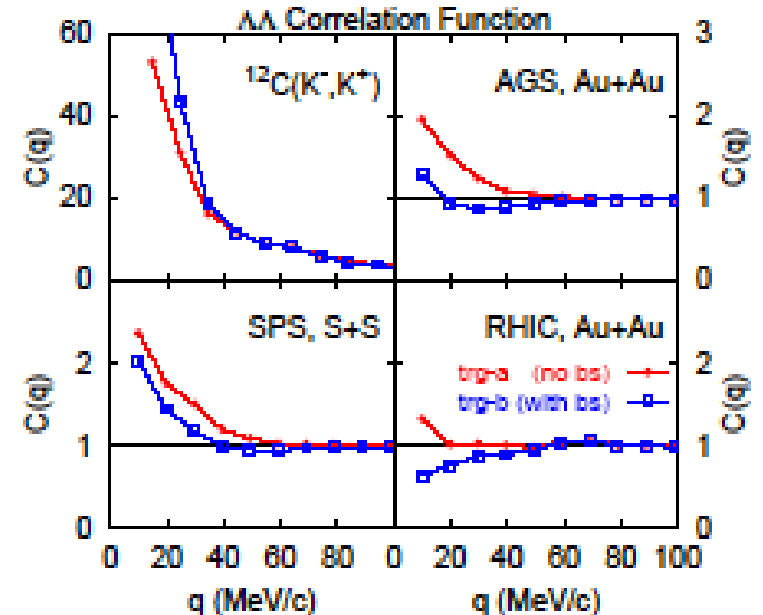
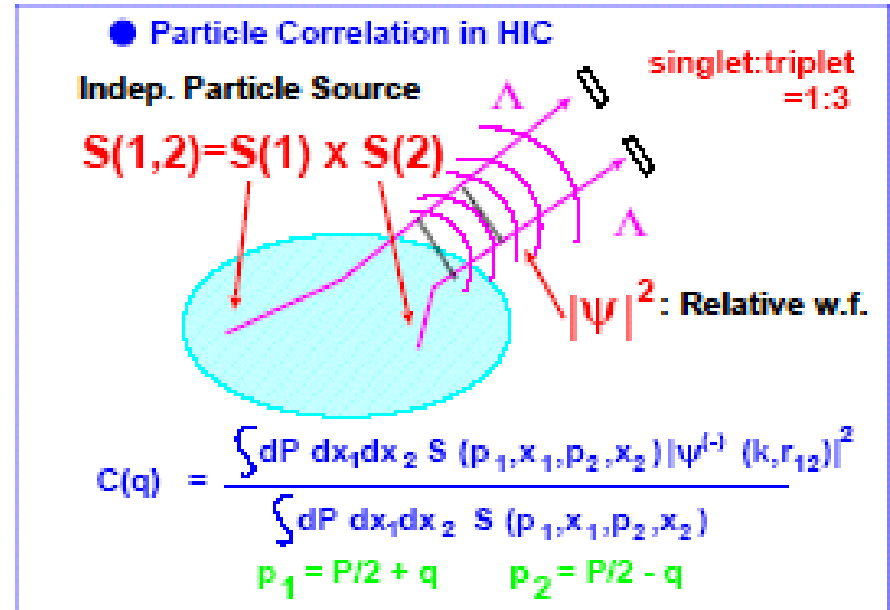
- 分かったこと → jet parton が局所熱平衡に達した bulk quark-gluon matter 中をエネルギーを失いながら伝播し、parton が再結合してハドロンを作る。
 - ◆ jet parton は媒質中でエネルギーを失ってからハドロン化
 - ◆ bulk 部分が完全流体によりうまく記述できる (SPS energy までは、流体モデルは「アイデア」を与えるが、定量的には粒子シミュレーションに勝てなかった。)
 - ◆ 中間 pT 領域で baryon が meson より多く、 v_2 も大きい。
- 分かりつつあること → QCD 物性
 - ◆ jet は流体への feed back や流体 parton との再結合により、より低い pT ハドロンの分布にも影響を与える。
- よく分かっていないこと
 - ◆ 初期条件、速い熱平衡化、jet の失われたエネルギーの行き先、jet 起源で十分な量の baryon を作る方法, viscous hydro の輸送係数.....

Heavy-Ion Collisions – Past, Present, Future --

- 重イオン反応は相図の広い範囲を実験室で探る唯一の手段
- ただし非平衡・非一様な現象なので輸送現象を扱う動力学が必要
 - ◆ SPS まで → ハドロン・string 輸送、RHIC → Hydro, Jet,
- 正しい自由度での動力学を作らないと現象は記述できない
- 多くの粒子は「崩壊」から作られる
 - ◆ 励起した大きな原子核の崩壊 → fragments
 - ◆ resonance, string の崩壊 → hadrons
 - ◆ jet, fluid の「崩壊」 → hadrons
- 古典的な輸送モデルでは「時間スケール」が大きな問題
 - ◆ (基底状態の) fragment 生成はきわめて「量子論的」な過程
 - ◆ Resonance, string 崩壊は、端点の古典力学を追うよりも、量子論的な理論による崩壊を取り入れることが望ましい。
 - ◆ fragment 生成で(量子論的) coalescence は比較的重要な役割を持つ

Near Future --- $\Lambda\Lambda$ correlation ---

- Longstanding problem in hadron spectroscopy: Does H ($S=-2$, $B=2$) dibaryon below $\Lambda\Lambda$ threshold ?
- RHIC may solve this problem.
 - If $\Lambda\Lambda$ bound, continuum w.f. must be orthogonal to b.s.w.f and must have a node around the scattering length.
 - Source size at RHIC may be comparable to the scattering length, and w.f. are suppressed in the source, IFF $\Lambda\Lambda$ bounds. (Int. between $\Lambda\Lambda$ is attractive.)



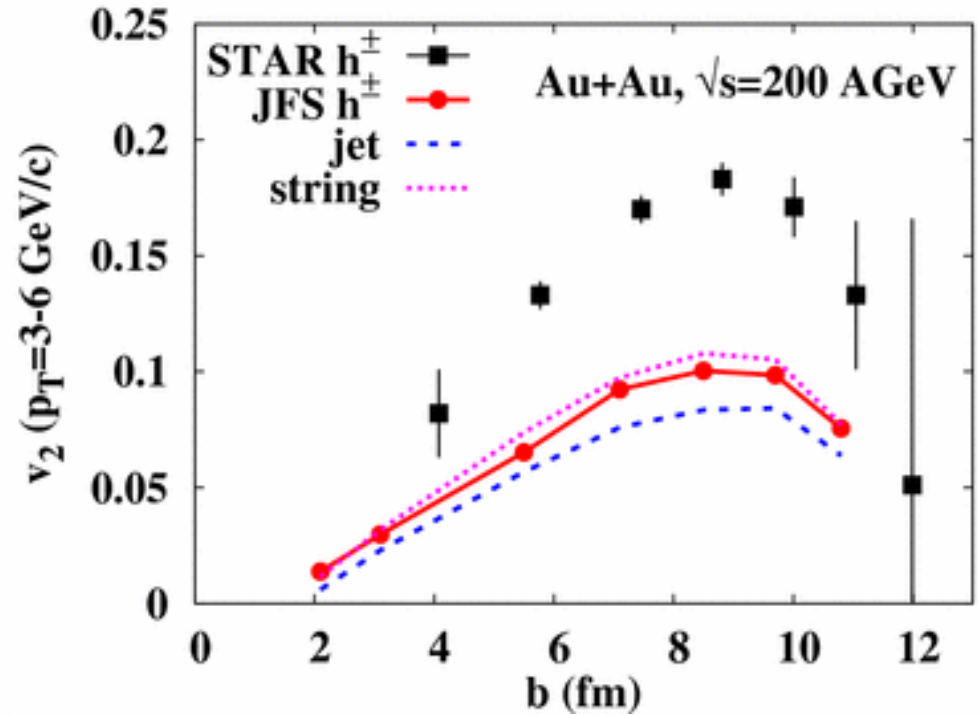
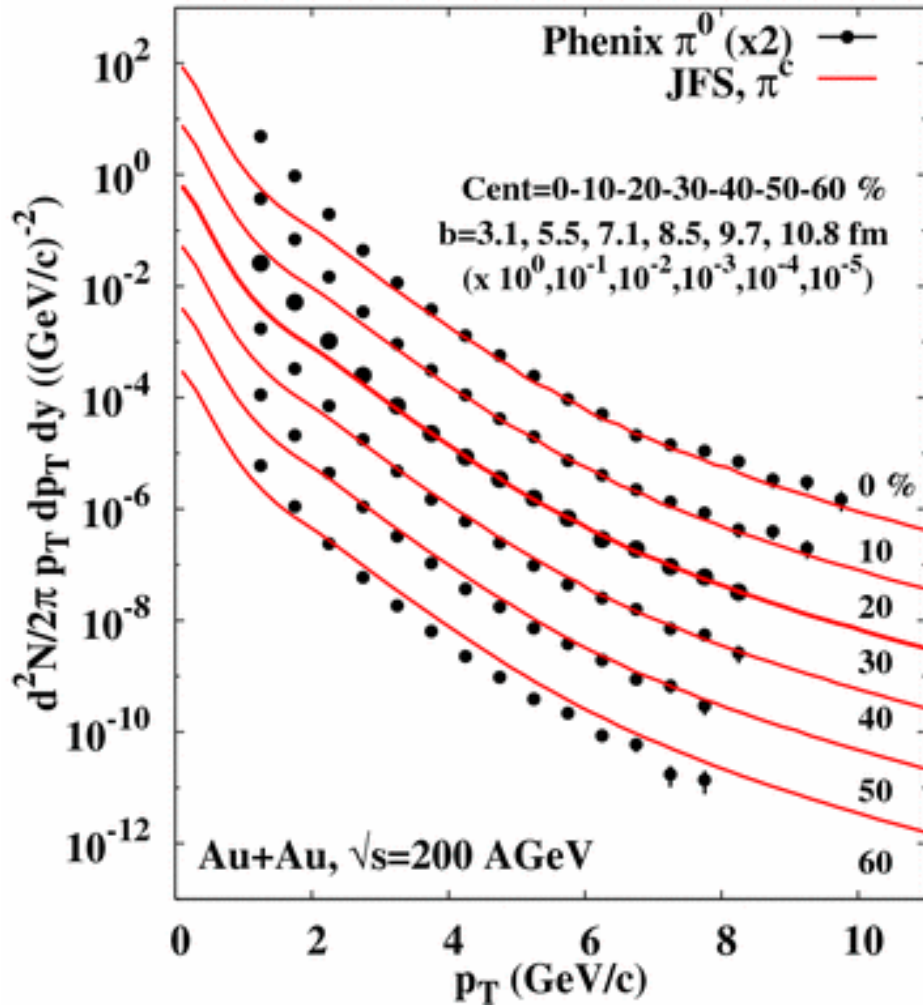
Ohnishi et al., NPA 670 (2000), 297c [arXiv:nucl-th/9903021]

Future HIC Physics

- **LHC & RHIC II: High p_T Parton DOF becomes more important**
 - **Viscous Fluid ? (smaller coupling but larger density)**
 - **Feedback of Jet E-loss to Fluid (c.f. In supernovae, matter is hit by neutrinos and shock may revive.)**
 - **Jet-Jet interaction**
 - **Color Glass Condensate would be more clearly seen.**
- **FAIR: Competition of Hadronic EOS & QCD phase transition**
 - **25-30 GeV/A \rightarrow Highest density matter may be formed.**
 - **Coex. of hadronic and quark matter \rightarrow Very small sound velocity**
 - **Critical End Point search**
 - \rightarrow **Can we distinguish the first order transition and cross over ?**
- **RIBF, RIA,**
 - **EOS of neutron rich matter, Fragmentation (Level density, Low E mode,),**

Backups

Centrality Dependence

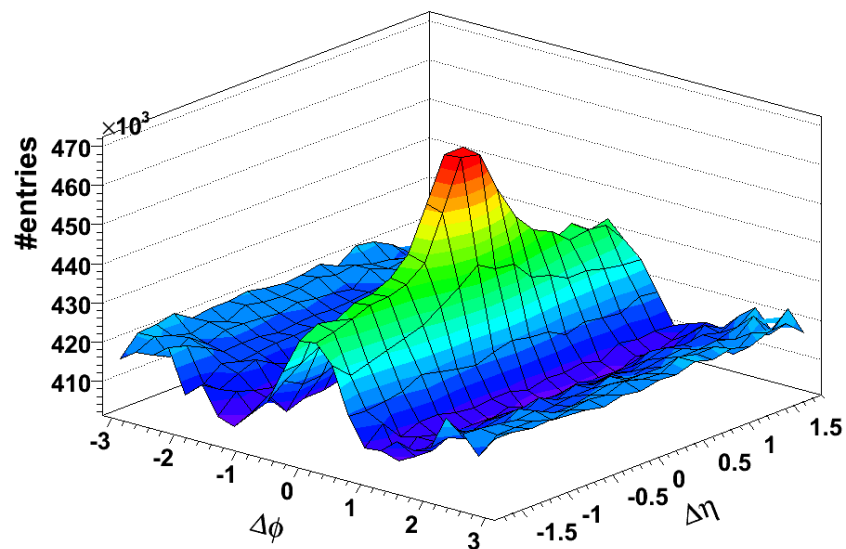


ジェット・リッジ構造

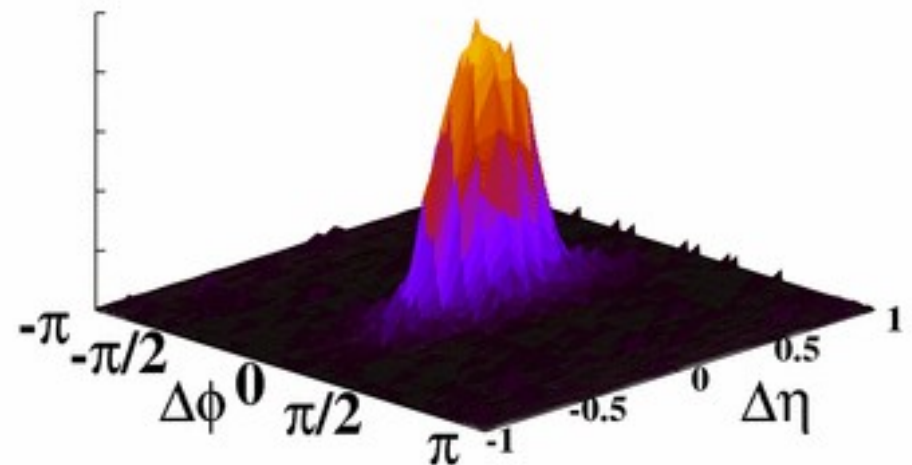
But, ...

- JFS模型において、リッジ構造は見られていない (理由の分析は今後)

Data

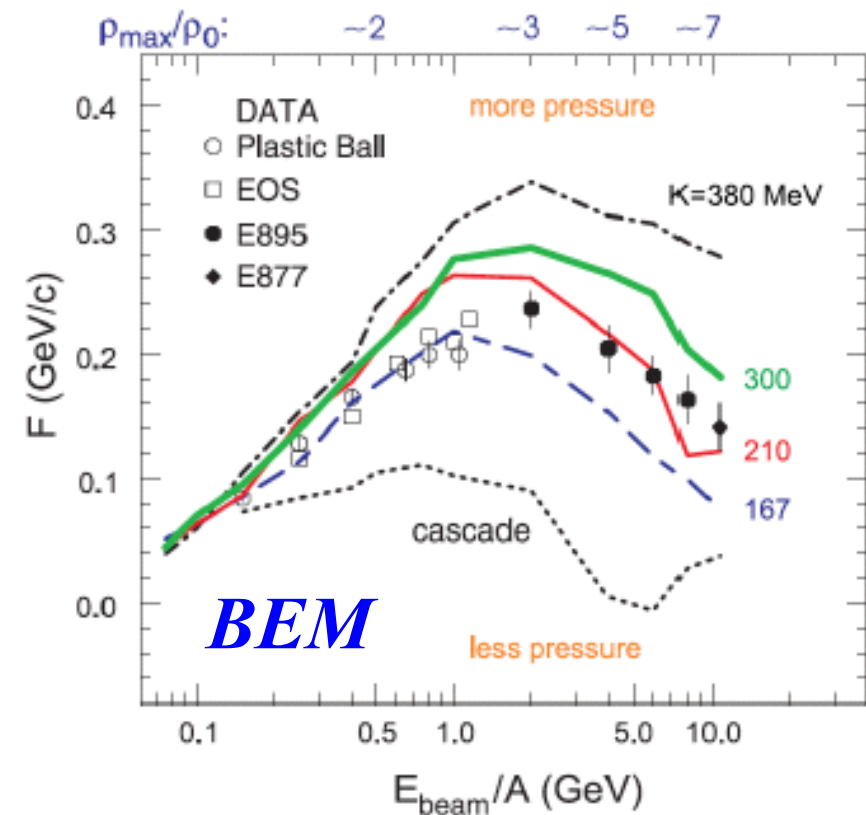
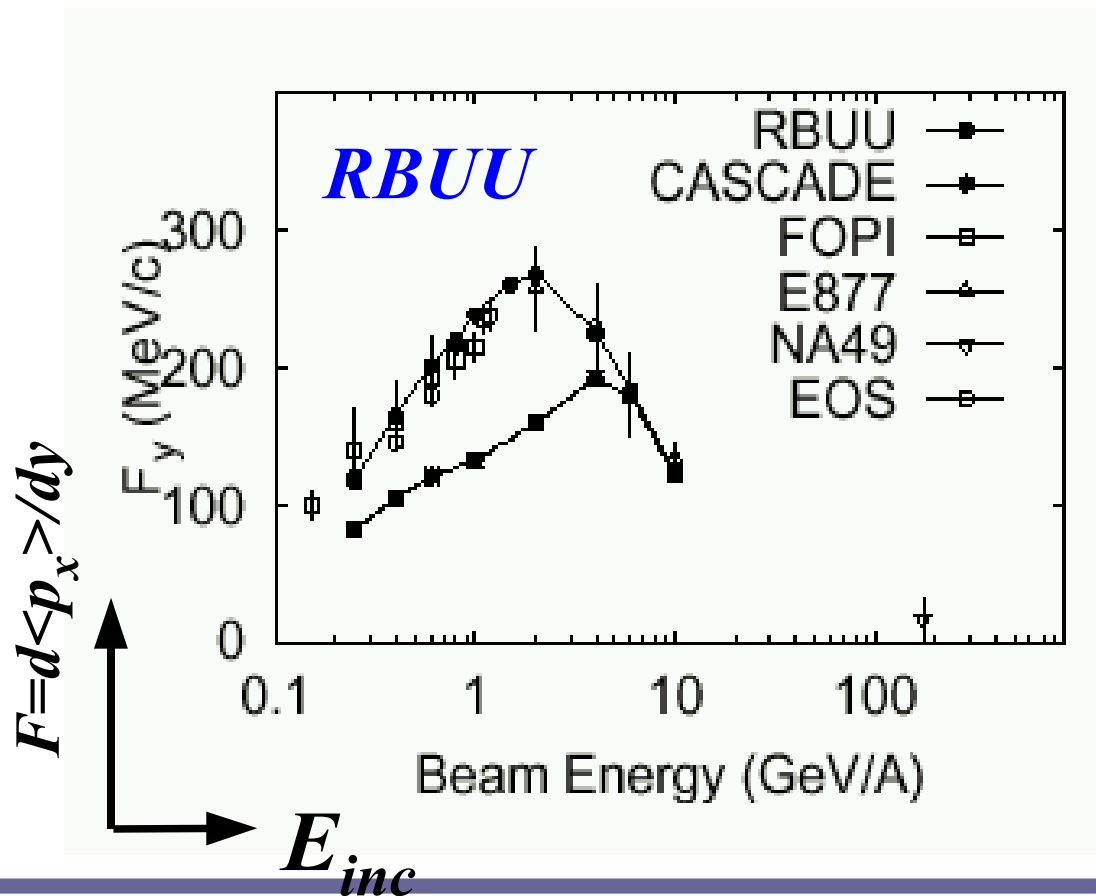


JFS



Side Flow at AGS Energies

- Relativistic BUU (RBUU) model: $K \sim 300 \text{ MeV}$
(Sahu, Cassing, Mosel, AO, Nucl. Phys. A672 (2000), 376.)
- Boltzmann Equation Model (BEM): $K=167\sim 210 \text{ MeV}$
(P. Danielewicz, R. Lacey, W.G. Lynch, Science 298(2002), 1592.)

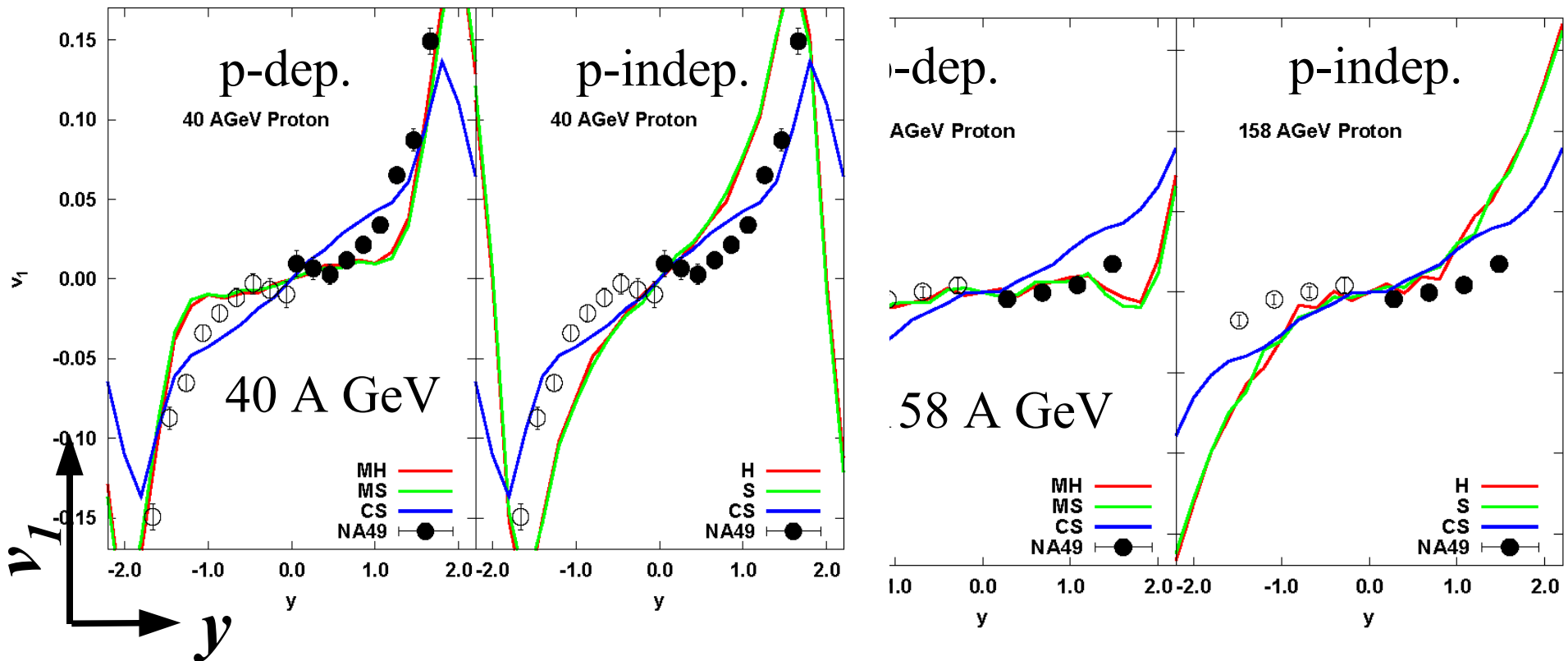


Directed flow v_1 at SPS

Isse, AO, Otuka, Sahu, Nara, PRC 72 (2005), 064908

• JAM-RQMD/S

- ◆ p-dep. (indep.) MF suppresses (enhances) v_1 . $v_1 = \langle \cos \phi \rangle = \langle p_x / p_T \rangle$
- ◆ “Wiggle” behavior appears with p-dep. MF at 158 A GeV.



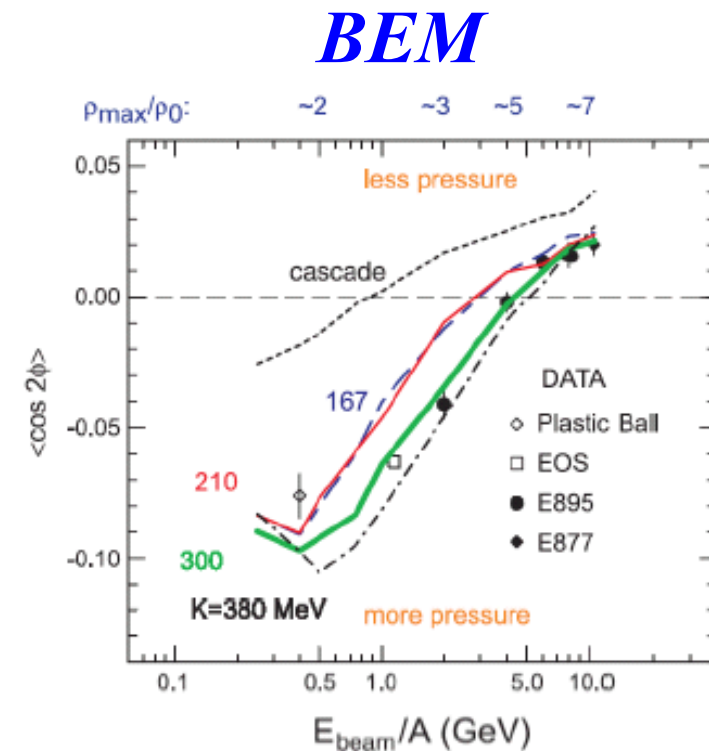
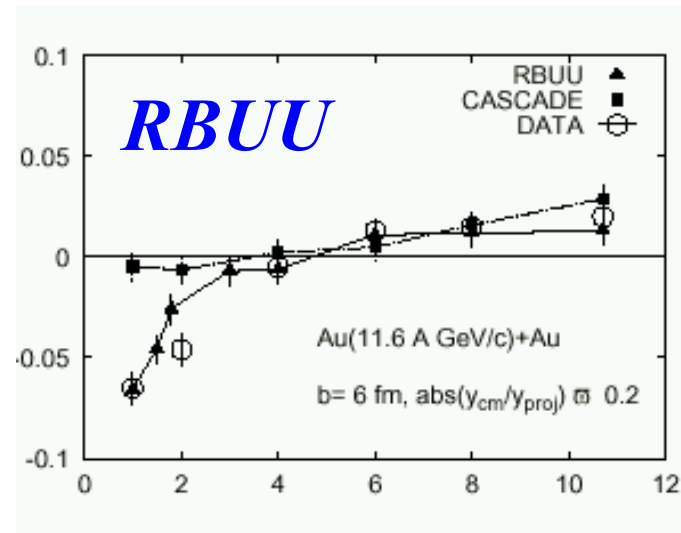
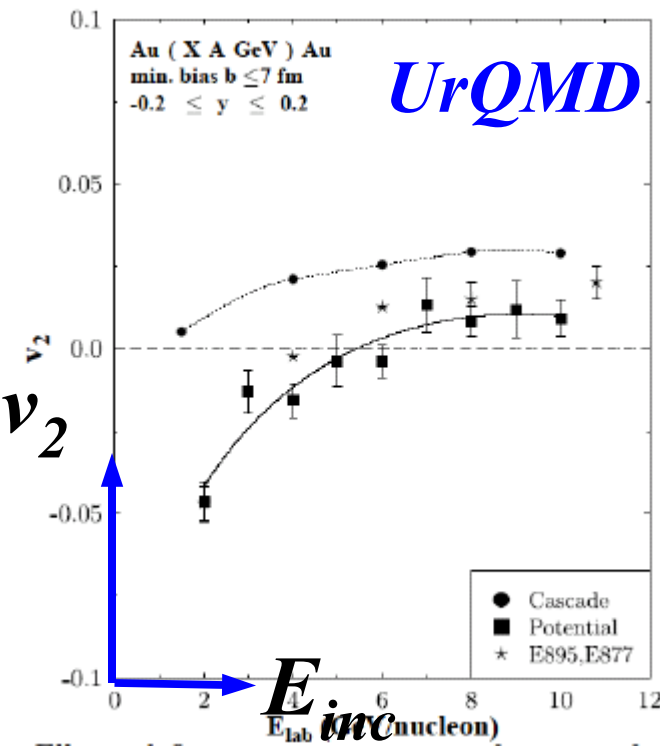
Elliptic Flow at AGS

- Strong Squeezing Effects at low E (2-4 A GeV)

- ◆ UrQMD: Hard EOS (S.Soff et al., nucl-th/9903061)

- ◆ RBUU (Sahu-Cassing-Mosel-AO, 2000): $K \sim 300$ MeV

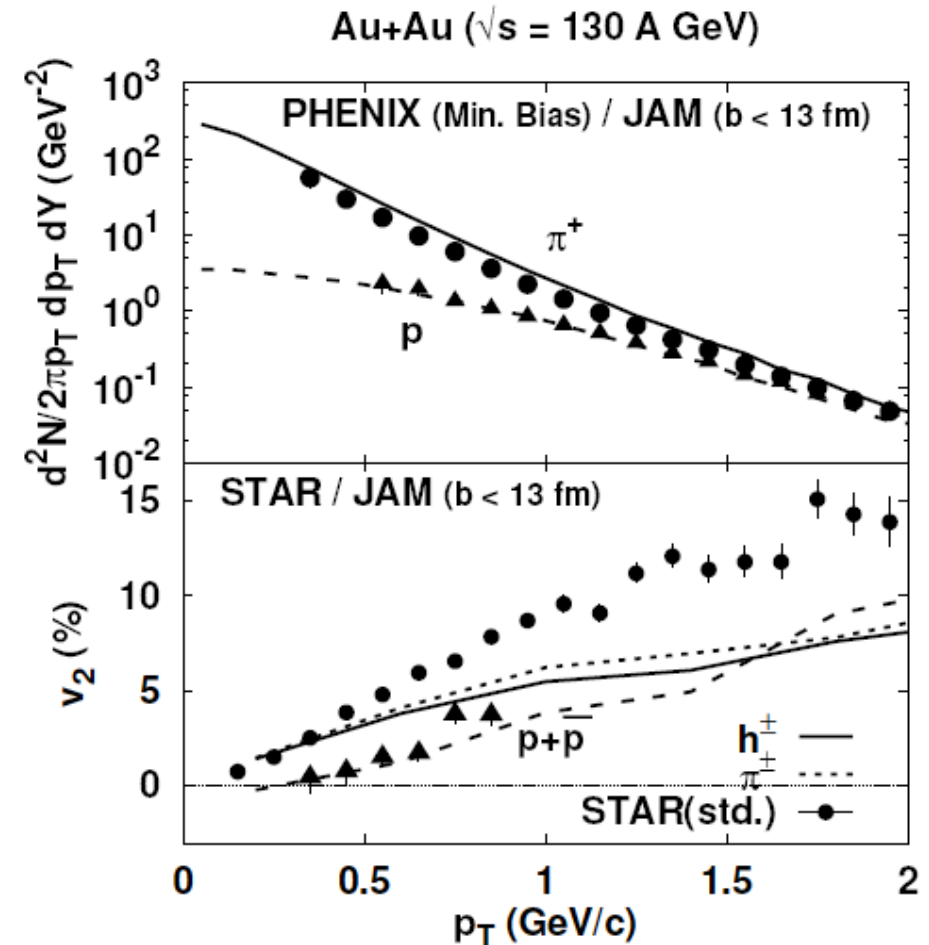
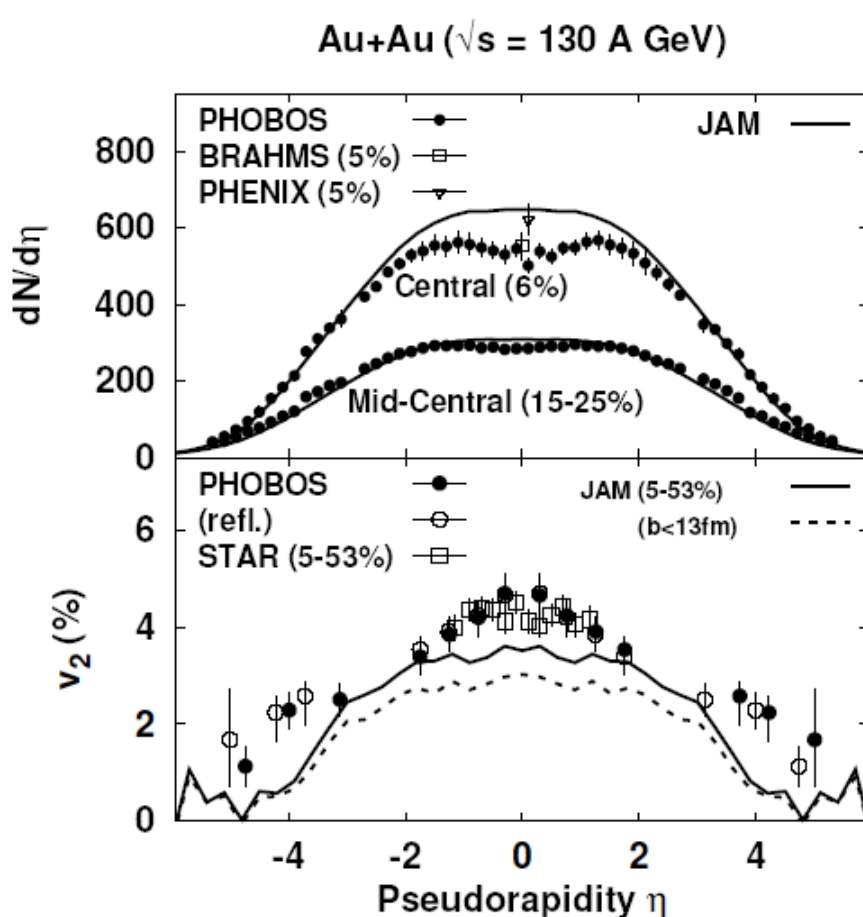
- ◆ BEM(Danielewicz2002): $K = 167 \rightarrow 300$ MeV



Elliptic Flow in Hadron-String Cascade (I)

Hadron-String Cascade (JAM) @ RHIC

- Hadron Yield is reasonably explained up to 2 GeV/c (10-20 % error)
- v_2 is underestimated (20-30 % (integrated), 50 % ($p_T > 1$ GeV))



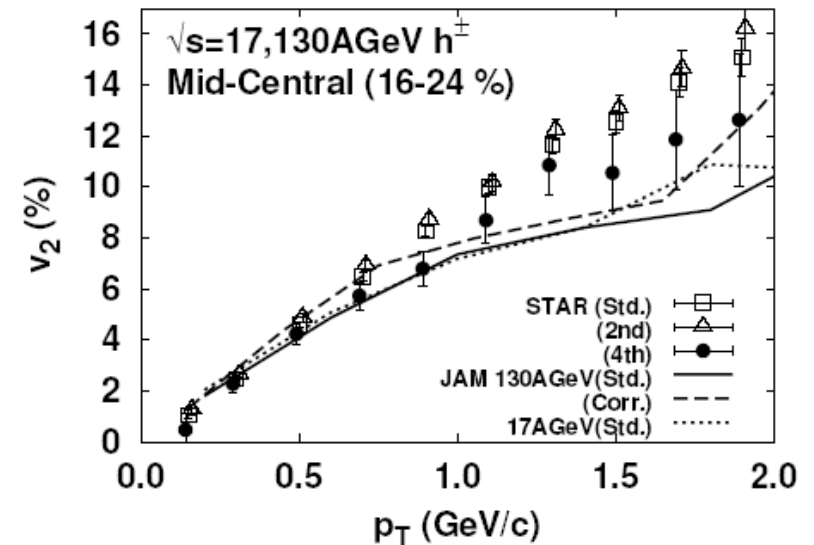
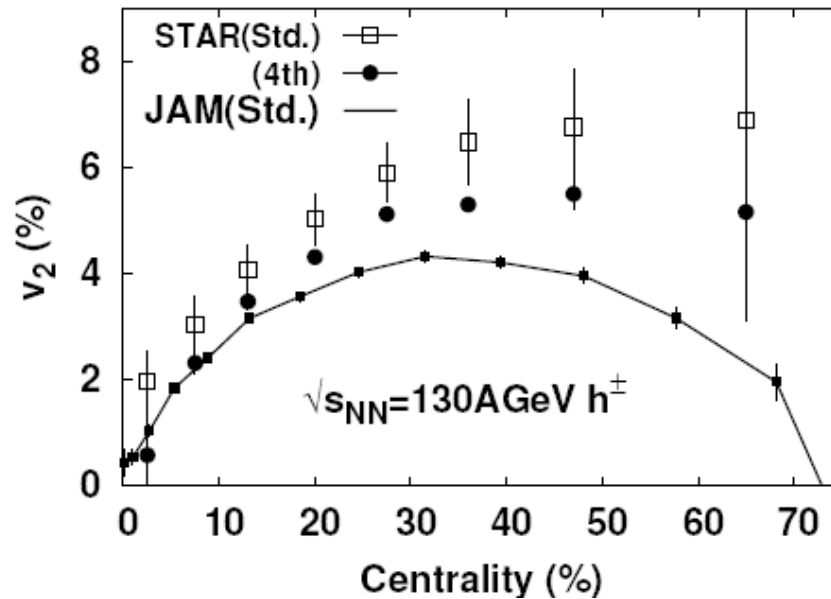
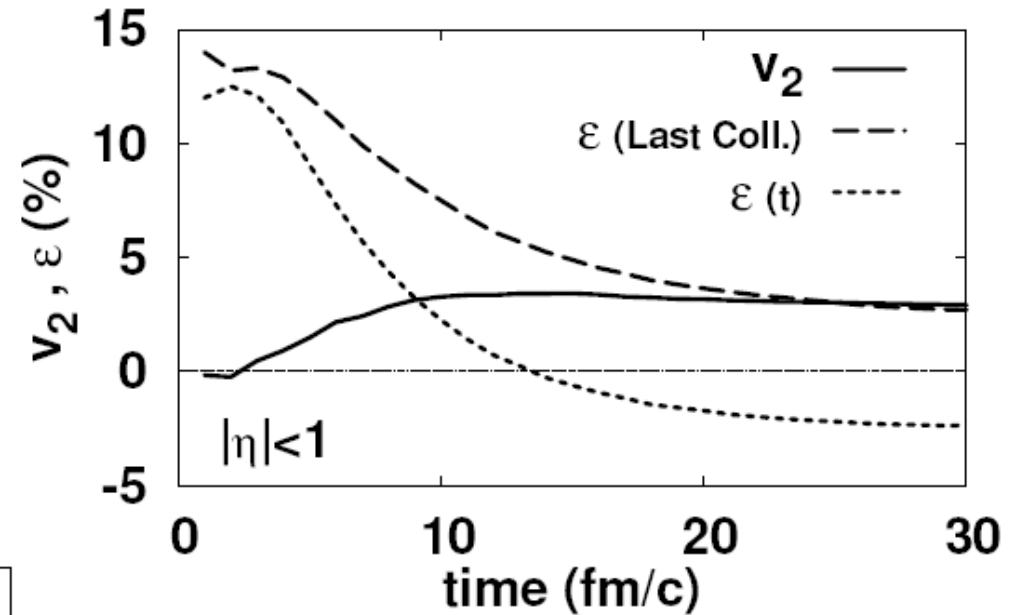
Elliptic Flow in Hadron-String Cascade (II)

Why do we underestimate v_2 in Hadron-String Cascade ?

- v_2 growth time is long (~ 10 fm/c), due to hadron formation time ($\tau \sim 1$ fm/c).
 \rightarrow much longer than hydro

Sahu-Isse-AO-Otuka-Phatak 2006

Au+Au, $\sqrt{s_{NN}} = 130$ GeV, $b < 13$ fm



Predictions of Cu+Cu Collisions @ RHIC (I)

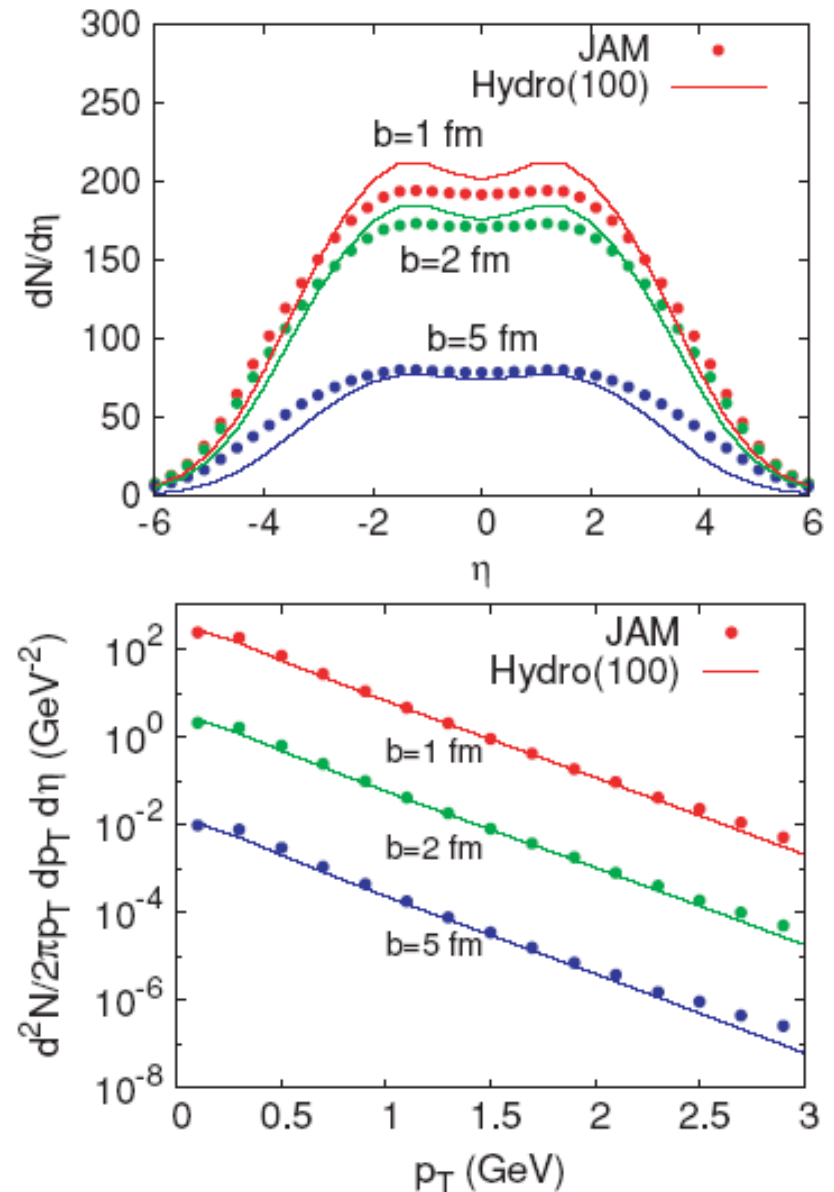
- Single particle spectra

- Cascade (JAM) and Hydro predict almost the same single particle spectra

$$dN/d\eta, d^2N/p_T dp_T d\eta$$

- Surprising ?

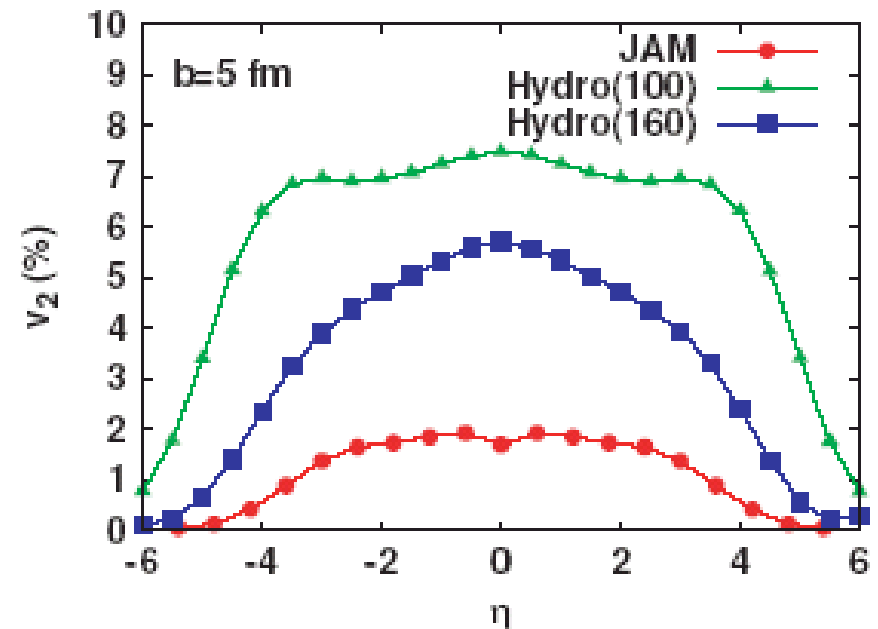
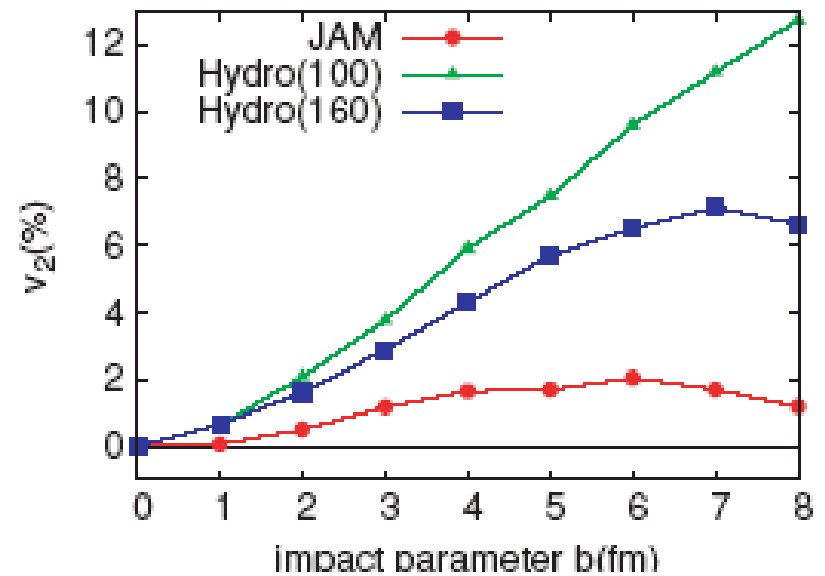
- Initial Cond. of Hydro is tuned to fit $dN/d\eta$ (~ Energy per rapidity)
- Cascade use fitted σ_{NN}
- Thermalization is expected at Low p_T (long time before particle production)
→ Coincidence may not be surprising



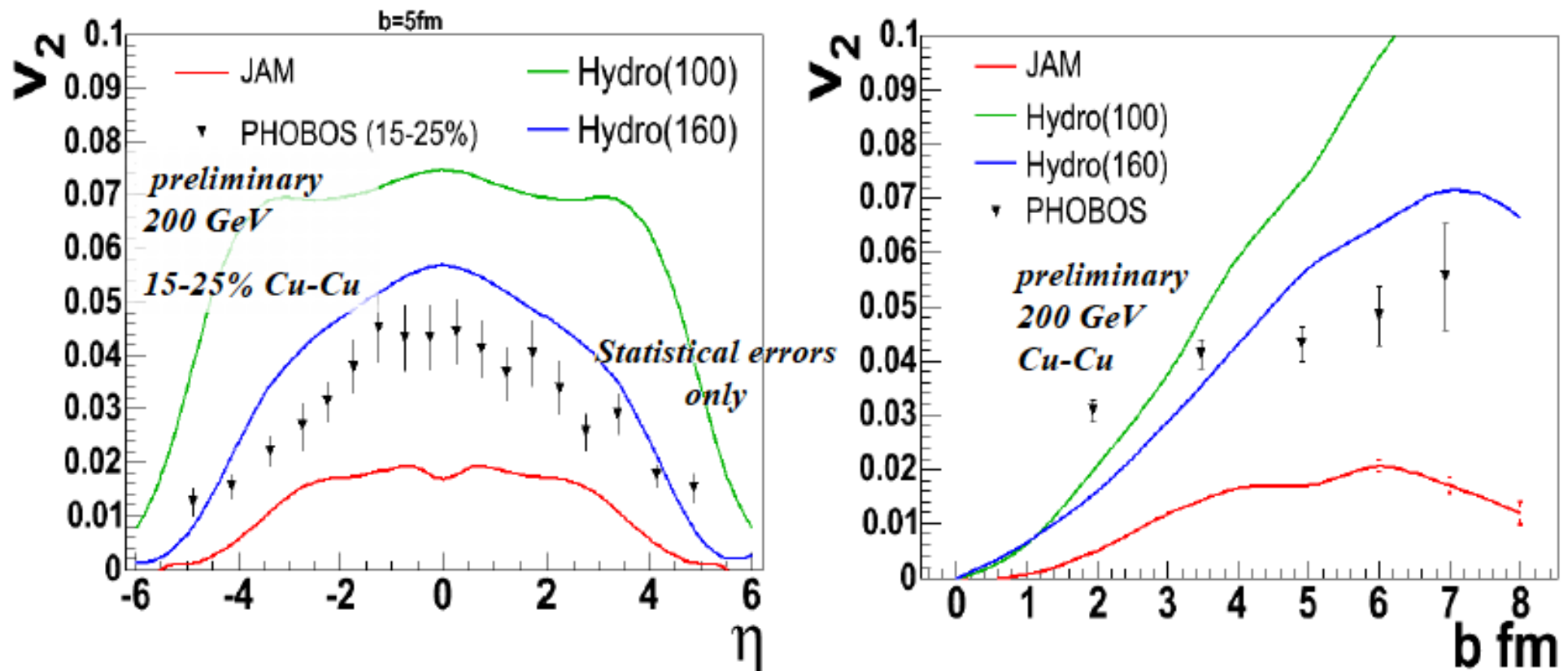
Hirano, Isse, Nara, AO, Yoshino, Phys. Rev. C 72(2005), 041901

Predictions of Cu+Cu Collisions @ RHIC (II)

- Calculations were done **BEFORE** the data are opened to public.
- Cascade and Hydro predict very different Elliptic Flow !
 - ◆ Cascade: small v_2
→ Small int. in the early stage
 - ◆ Hydro: large v_2
→ Strong int. after $\tau = \tau_0 \sim 0.6$ fm/c
- T^{th} dependence
 - ◆ $T^{th} = 160$ MeV $\sim T_c = 170$ MeV
→ short time of expansion in the hadron phase
 - ◆ $T^{th} = 100$ MeV $< T_c = 170$ MeV
→ long time of expansion



Compared to JAM Model

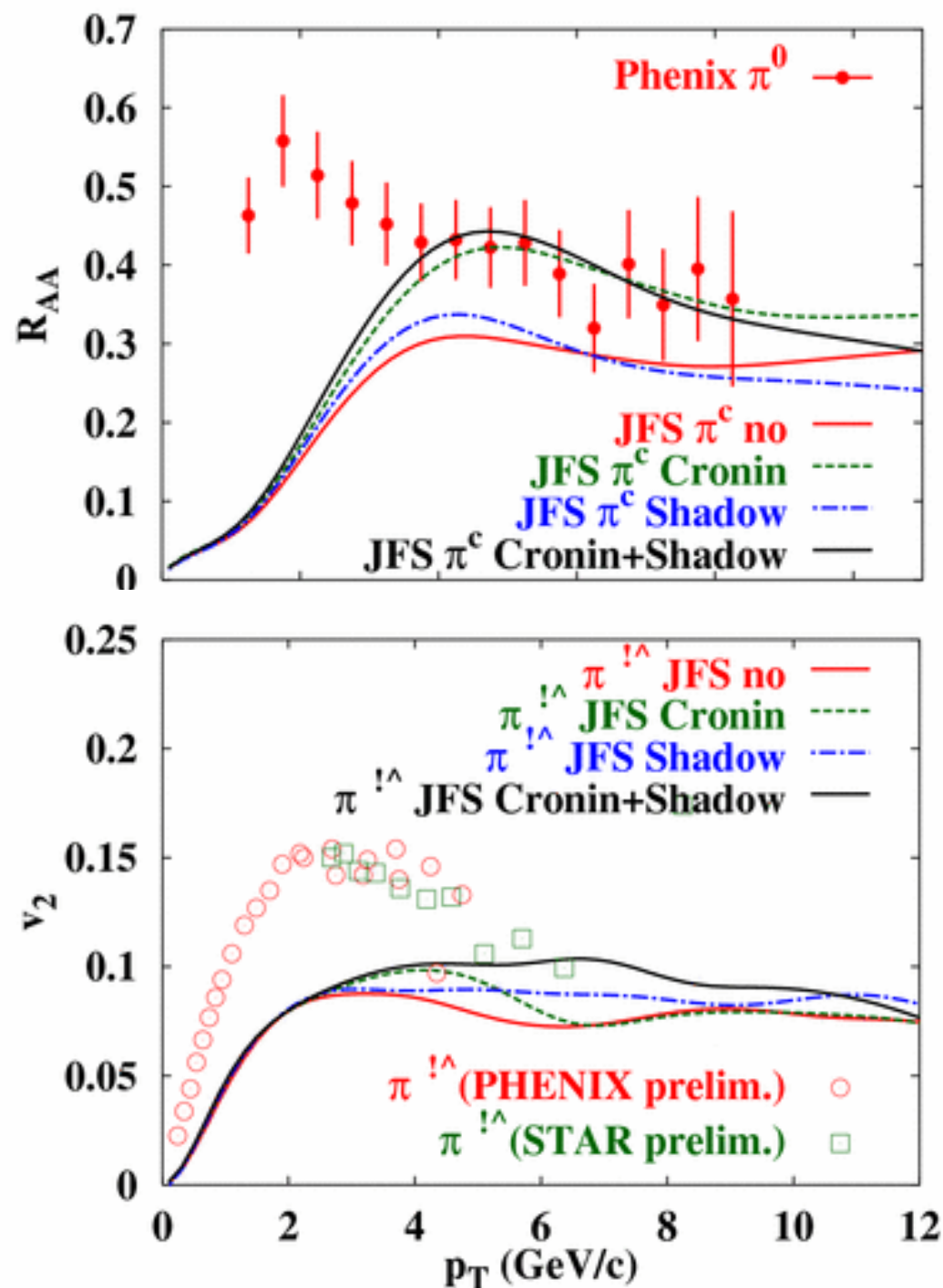


Cu-Cu more like Hydro than JAM hadron string cascade model

Here JAM uses a 1 fm/c formation time. Hydro (160) has kinetic freezeout temperature at 160 MeV

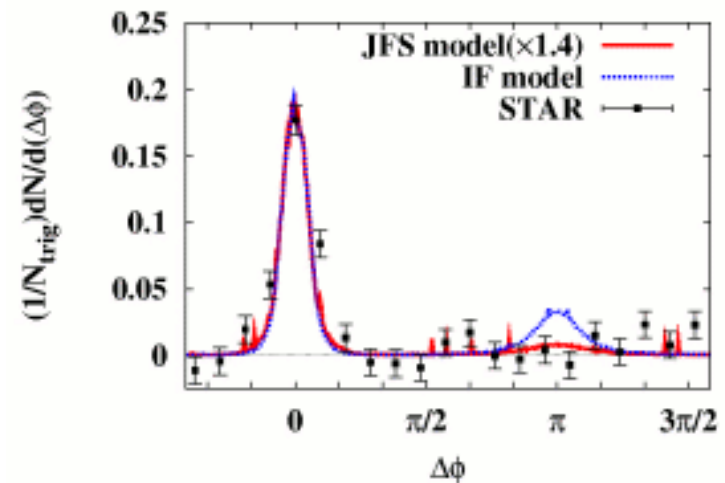
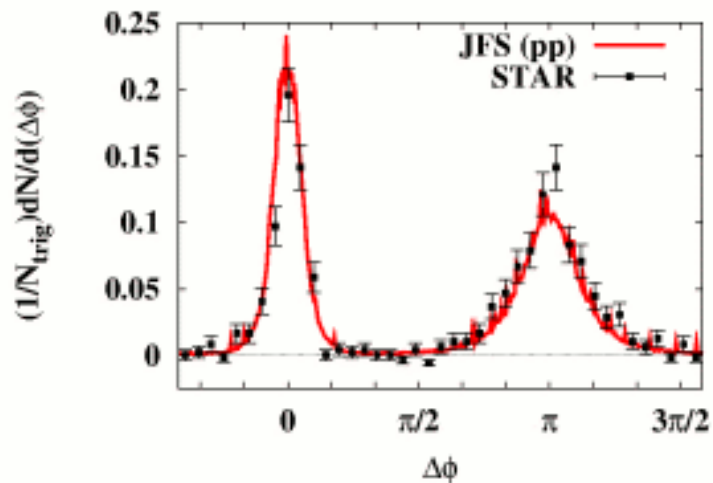
Cronin and Shadowing Effects

- Standard (EKS, ...)
Cronin+Shadow
enh. med. $p_T R_{AA}$
and suppr. high $p_T R_{AA}$.



Two Hadron Correlation

- pp衝突の correlationは pythia で説明できる
- Au+Au衝突を見ると、
 - ◆ IF modelでは180°相関の消失が不完全
 - ◆ JFS modelでは180°相関の消失を定性的には再現



AMD (Antisymmetrized Molecular Dynamics)

Ono-Horiuchi-Maruyama-AO, 1992

- **Gaussian Approximation for single particle wave function**

$$|\Psi\rangle = A \prod |\psi_i\rangle, \quad \psi_i = \phi(r; Z_i) \chi(\sigma, \tau), \quad Z = \sqrt{\nu} D + \frac{i}{2\hbar\sqrt{\nu}} K$$
$$\phi(r; Z) = \left(\frac{2\nu}{\pi}\right)^{3/4} \exp(-\nu(r - Z/\sqrt{\nu})^2 + Z^2/2) \propto \exp(-\nu(r - D)^2 + iK \cdot (r - D)/\hbar)$$

- **Time-dependent Variational Principle \rightarrow Equations of Motion**

$$L = \frac{\langle \Psi | i\hbar \partial / \partial t - H | \Psi \rangle}{\langle \Psi | \Psi \rangle} \quad \frac{d}{dt} \frac{\partial L}{\partial (d\bar{Z}_i/dt)} - \frac{\partial L}{\partial \bar{Z}_i} = 0 \quad \rightarrow \quad i\hbar C_{i\alpha, j\beta} \frac{dZ_i}{dt} = \frac{\partial H}{\partial \bar{Z}_i}$$

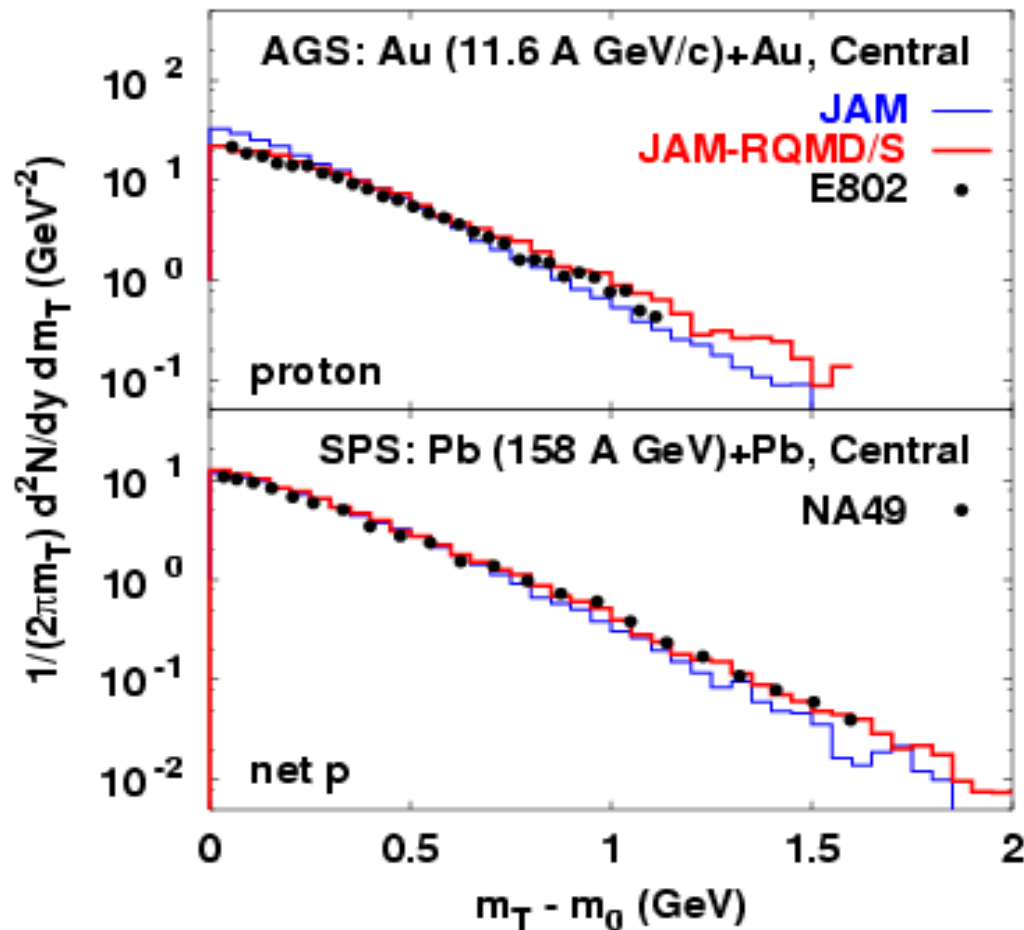
- **Ignoring Antisymmetrization**

\rightarrow **Quantum Molecular Dynamics EOM (= Classical EOM)**

$$C = \delta \quad \rightarrow \quad \frac{dD_i}{dt} = \frac{\partial H}{\partial K_i}, \quad \frac{dK_i}{dt} = -\frac{\partial H}{\partial D_i}$$

Classical-type EOM is obtained through Gaussian + TDVP

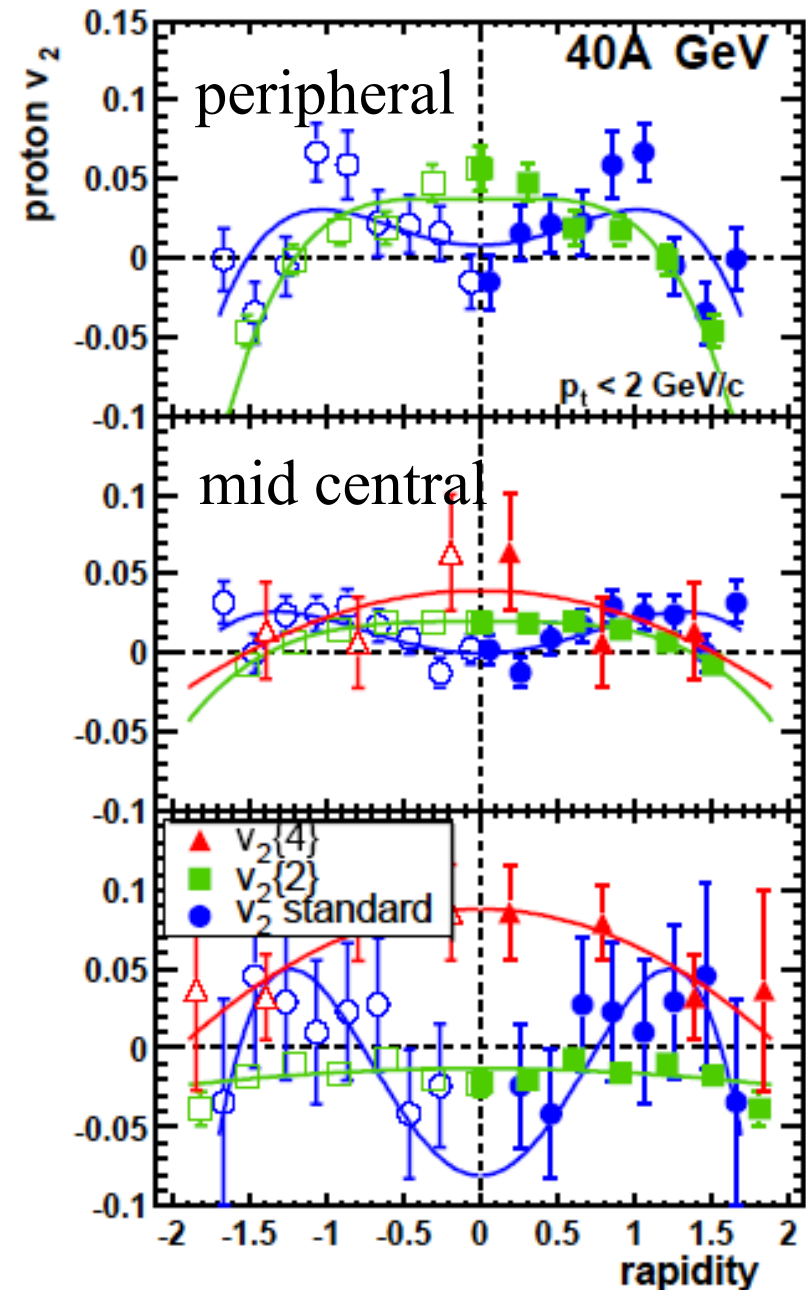
Mean Field Effects in Mt Spectrum



Mean Field affects
the Mt Spectra
even at SPS energy.

Dip of V_2 at 40 A GeV: Phase Transition ?

- Dip of V_2 at 40 A GeV may be a signal of QCD phase transition at high baryon density. (Cassing et al.)
- However, the data is too sensitive to the way of the analysis (reaction plane/two particle correlation).
- We have to wait for better data.



Flow and EOS; to be continued

- In addition to the ambiguities in in-medium cross sections, Res.-Res. cross sections, we have model dependence.

- ◆ **RBUU** (*e.g. Sahu, Cassing, Mosel, AO, Nucl. Phys. A672 (2000), 376.*)

- In RMF, Strong cut-off for meson-N coupling in RMF
→ Smaller EOS dep.

- ◆ **Scalar potential interpretation in BUU**

Larionov, Cassing, Greiner, Mosel, PRC62,064611('00), Danielewicz, NPA673,375('00)

$$\varepsilon(\mathbf{p}, \rho) = \sqrt{[m + U_s(\mathbf{p}, \rho)]^2 + \mathbf{p}^2} = \sqrt{m^2 + \mathbf{p}^2} + U(\mathbf{p}, \rho)$$

- Due to the Scalar potential nature, EOS dependence is smaller.

- ◆ **Scalar/Vector Combination** *Danielewicz, Lacey, Lynch, Science 298('02), 1592*

$$\varepsilon(p, \rho) = m + \int_0^p dp' v^*(p', \rho) + \tilde{U}(\rho), \quad v^*(p, \rho) = \frac{p}{\sqrt{p^2 + [m^*(p, \rho)]^2}}$$

- Relatively Strong EOS dependence even at high energy

- ◆ **JAM-RQMD/S** *Isse, AO, Otuka, Sahu, Nara, PRC 72 (2005), 064908*

- Similar to the Scalar model BUU

Results of Parton Cascade

- Unexpectedly high parton cross sections of $\sigma = 5-6$ mb have to be assumed in parton cascades in order to reproduce the elliptic flow.

ZI-WEI LIN AND C. M. KO

PHYSICAL REVIEW C 65 034904

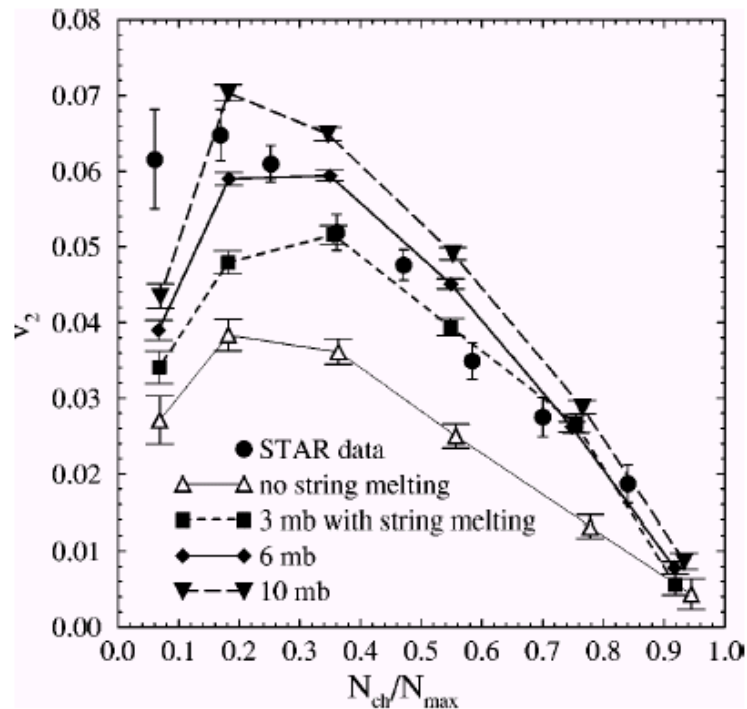


FIG. 3. Impact parameter dependence of elliptic flow at 130 A GeV. The data from the STAR collaboration [7] are shown by filled circles, while the theoretical results for different partonic dynamics are given by curves.

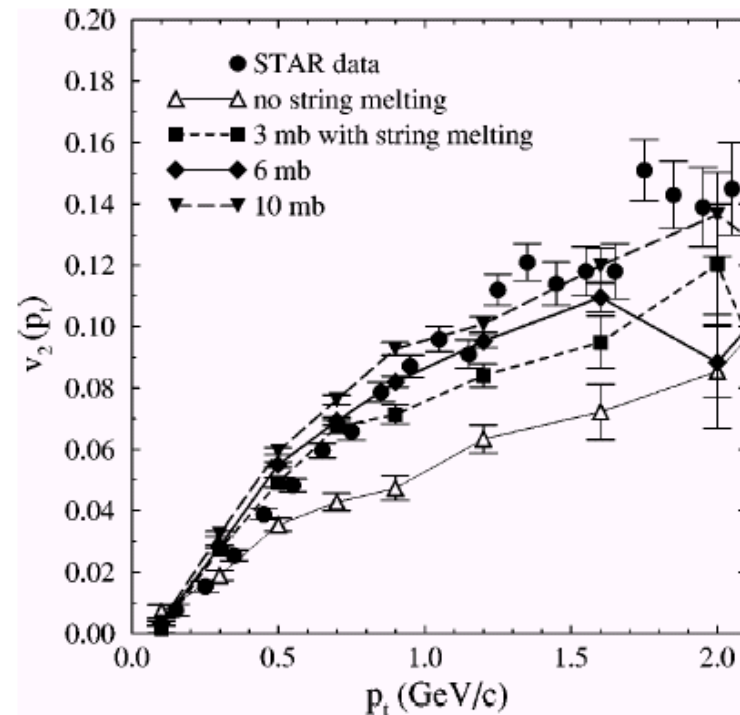


FIG. 4. Transverse momentum dependence of elliptic flow at 130 A GeV. Circles are the STAR data for minimum-bias Au+Au collisions [7], and curves represent the minimum-bias results for charged particles within $\eta \in (-1.3, 1.3)$ from the AMPT model.

Initial Conditions in Hydro

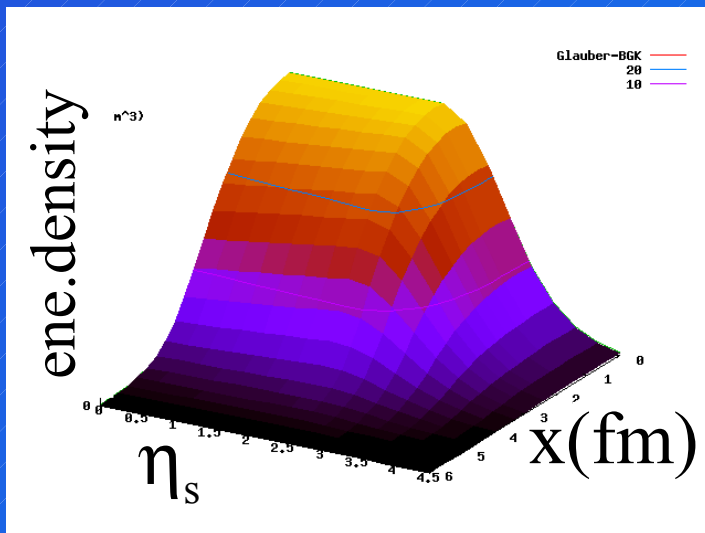
Glauber-BGK type

[Reference Initial Condition]
Transverse profile:

Entropy density
 $\propto a\rho_{\text{part}} + b\rho_{\text{coll}}$

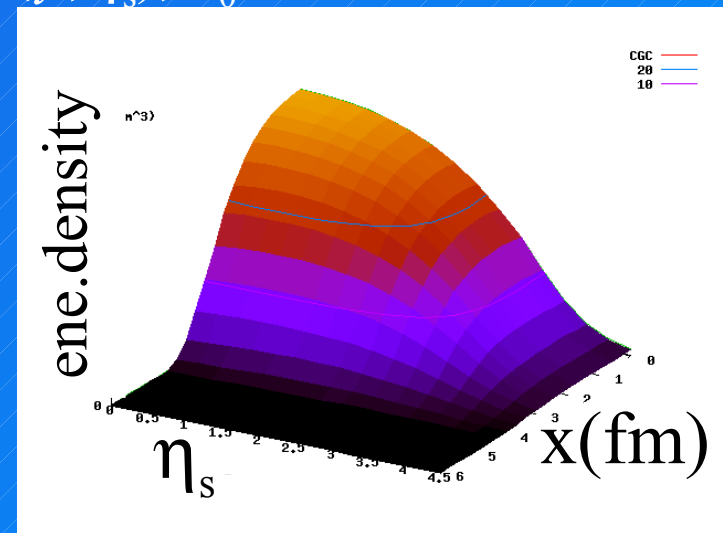
Longitudinal Profile:

Brodsky-Gunion-Kuhn triangle



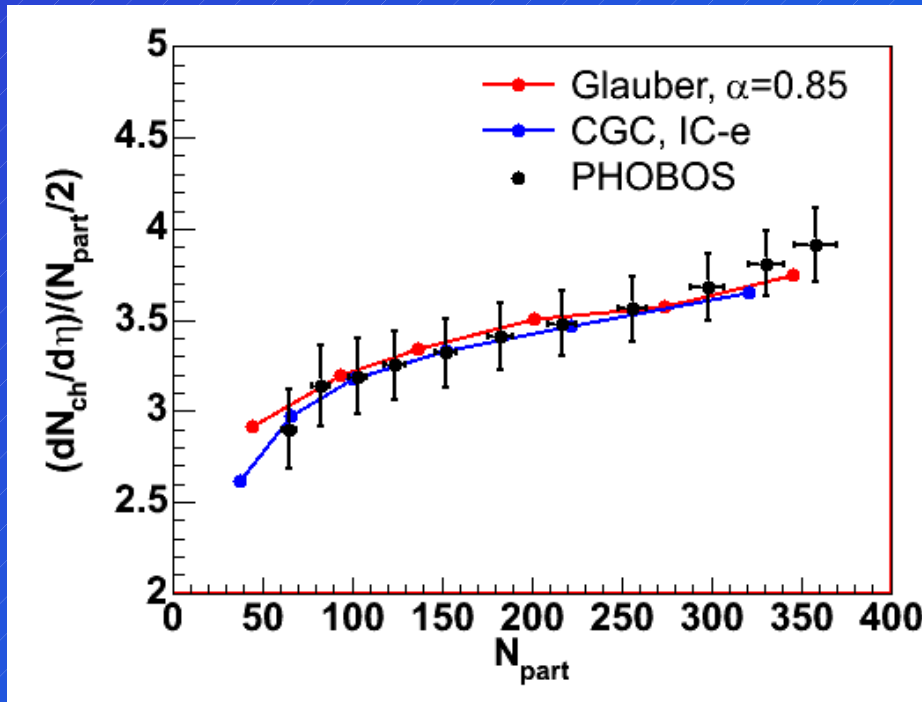
Color Glass Condensate

- Unintegrated gluon distribution a.l.a. Kharzeev, Levin, and Nardi
- Gluon production via k_T factorization formula
- Count deposited energy in dV at (τ_0, x, y, η_s) , $\tau_0 = 0.6\text{fm}/c$

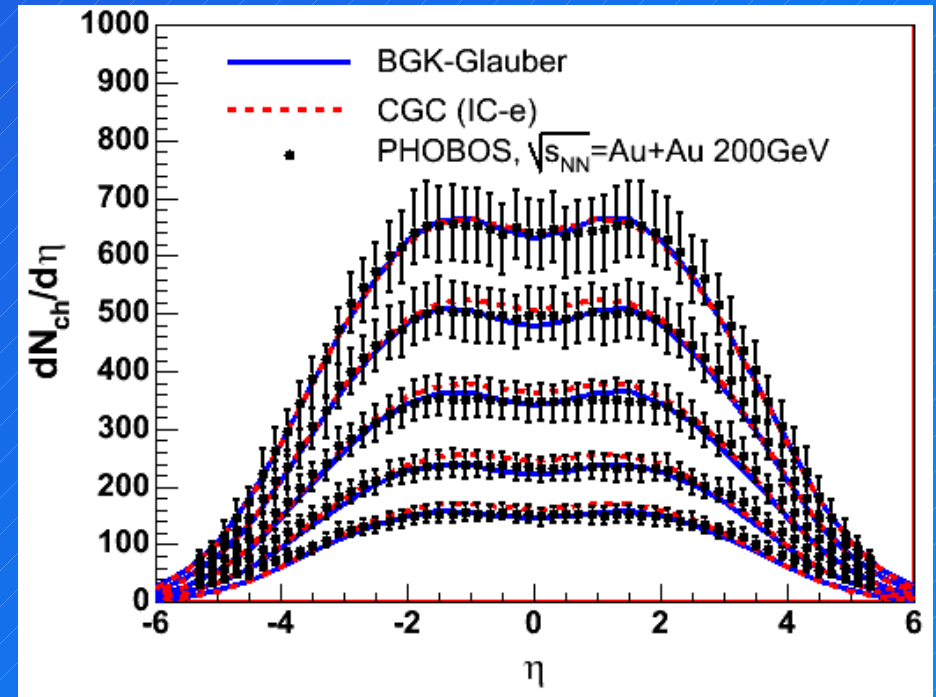


Two Hydro Initial Conditions Which Clear the “First Hurdle”

Centrality dependence

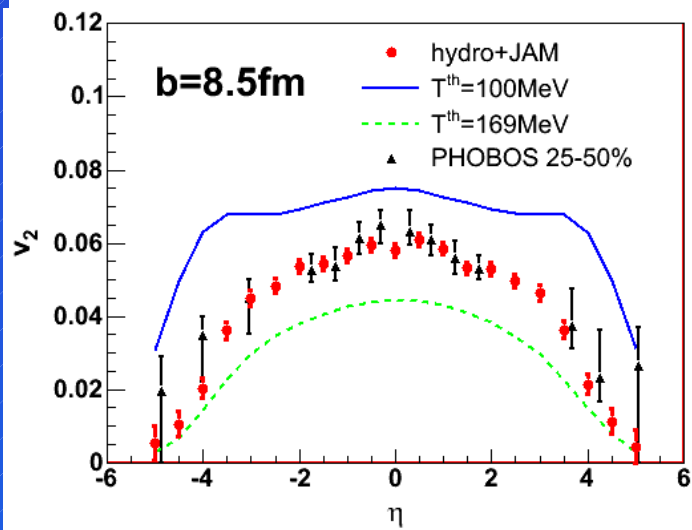
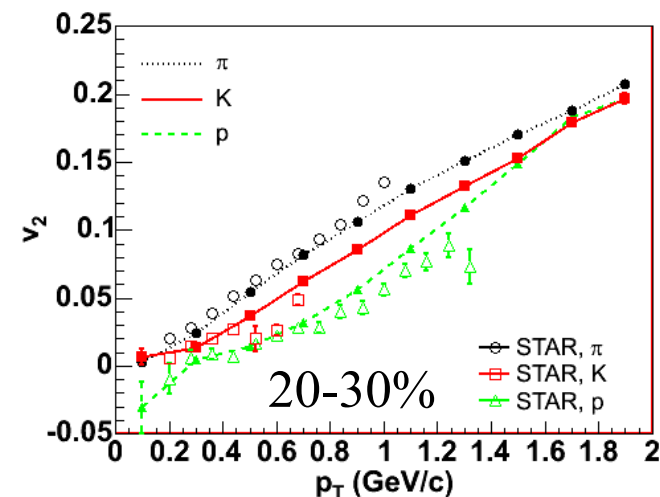
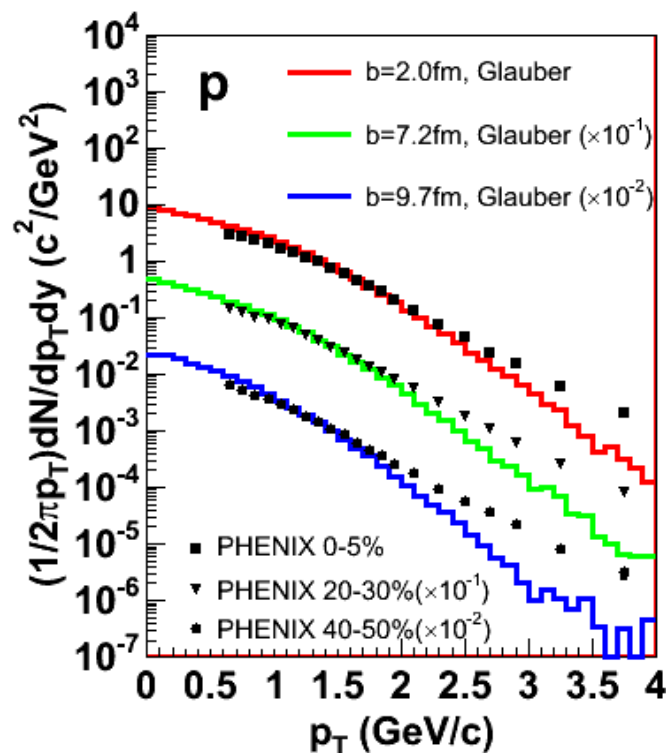
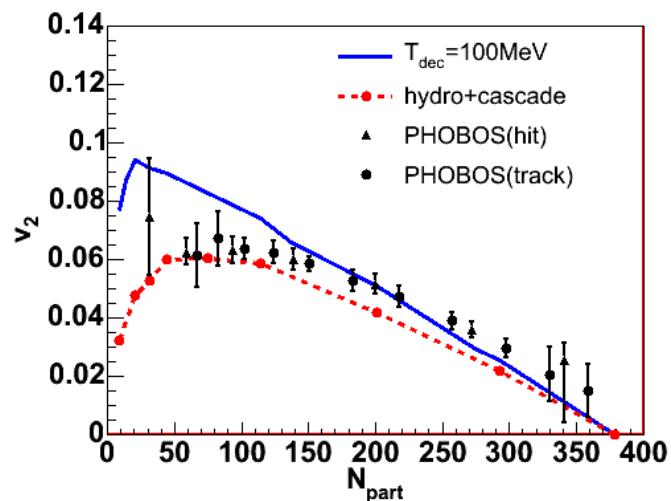


Rapidity dependence



1. CGC model Kharzeev, Levin, and Nardi
 Matching I.C. via $e(x, y, \eta)$ Implemented in hydro by TH and Nara
 2. Glauber model (as a reference)
- $N_{part} : N_{coll} = 85\% : 15\%$

Highlights from Glauber + QGP Fluid + Hadron Gas Model



Good agreement for bulk
($p_T < \sim 1.5\text{GeV}/c$)

→ What happens to the CGC case?

Recombination and Fragmentation

Fries, Muller, Nonaka, Bass, PRL90, 202303(2003); PRC68,044902 (2003)

- **Successes: quark number scaling, baryon/meson ratio**
→ $v_2 \sim 0.10$ at high- p_T .

$$f(p, \varphi) = (1 + 2 v_2(p/2) \cos \varphi) \times (1 + 2 v_2(p/2) \cos \varphi)$$
$$\approx 1 + 2 \times 2 v_2(p/2) \cos \varphi$$

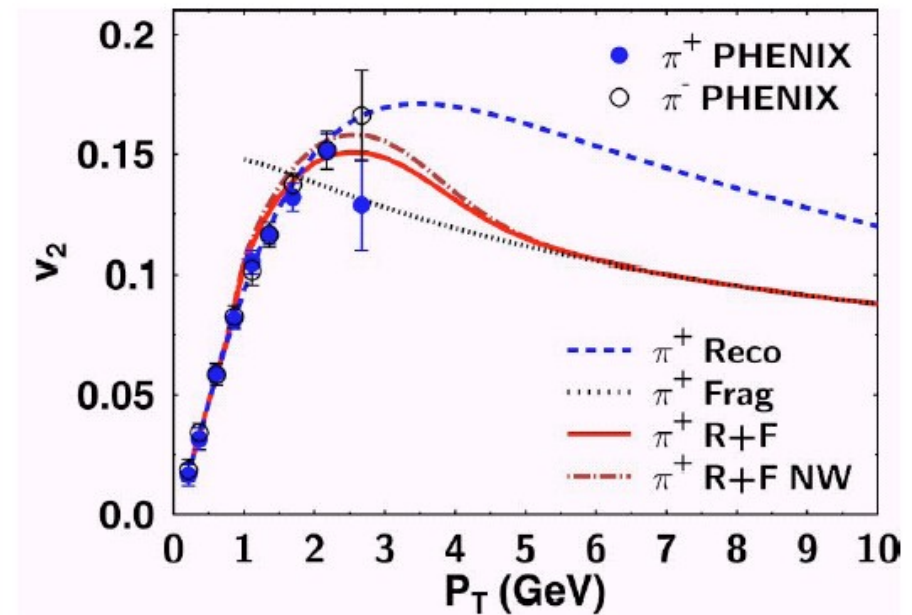
- **Problems: Sharply edged density dist. (Hard Sphere)**

$$\ell(b) = \sqrt{R_A^2 - (b/2)^2}$$

→ $E\text{-loss} \propto \ell \rightarrow v_2 \sim 0.10$

- ◆ **Woods-Saxon density distribution**

→ $v_2 \sim 0.05$: Half of H.S.



Unsolved (or Newly Found) Problems at RHIC

- **Mach Cone / Color Cerenkov**
 - ♦ Many low p_T particles are observed along the Quenched Jet (Angle from Jet = 120 deg.)
- **J/ ψ Production Mechanism**
 - ♦ With the expected absorption ratio at SPS, J/ ψ yield @ RHIC is underestimated.
- **Baryon(Hyperon)-Hadron azimuthal angle correlation**
 - ♦ Around the high p_T baryon angle, many hadrons are observed as in the case of jet production \rightarrow Baryons are also formed in jets.
- **High p_T v_2 problem**
 - ♦ With the energy loss explaining p_T spectrum, elliptic flow is calculated to be too small at high p_T .
- **And Many....**

Impact Parameter Dependence

- Mid- p_T v_2 ($3 < p_T < 6$ GeV/c) in JFS is larger than the “Strong E-loss Limit” with Woods-Saxon profile in Independent Fragmentation, but still smaller than Data.

