
Probing the QCD Critical Point in Core Collapsing Compact Stars

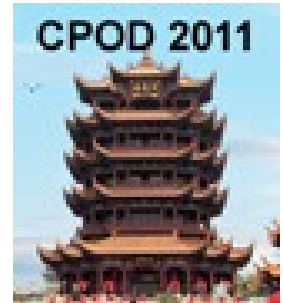
Akira Ohnishi (YITP)

in collaboration with H. Ueda, T.Z.Nakano (Kyoto U.),
M. Ruggieri (YITP → Catania), K. Sumiyoshi (Numazu CT)

7th Int. workshop on

“Critical Point and Onset of Deconfinement”

CCNU, Wuhan, China, Nov.7-11, 2011

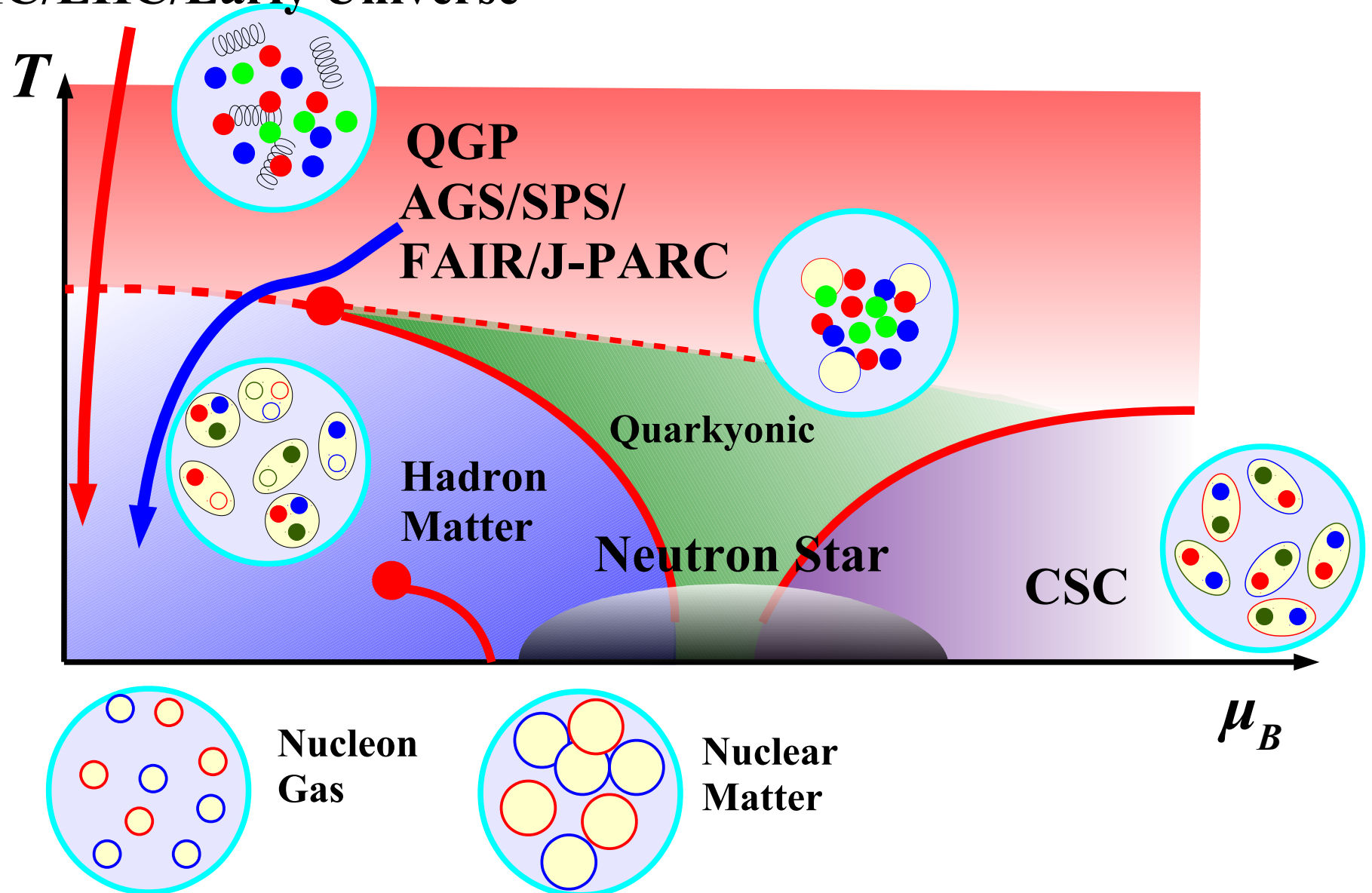


- Introduction
- QCD phase diagram in asymmetric nuclear matter
- Critical Point sweep during black hole formation
- Summary

*AO, H. Ueda, T.Z.Nakano, M. Ruggieri, K. Sumiyoshi,
PLB 704 ('11)284 [arXiv:1102.3753].*

QCD Phase Diagram

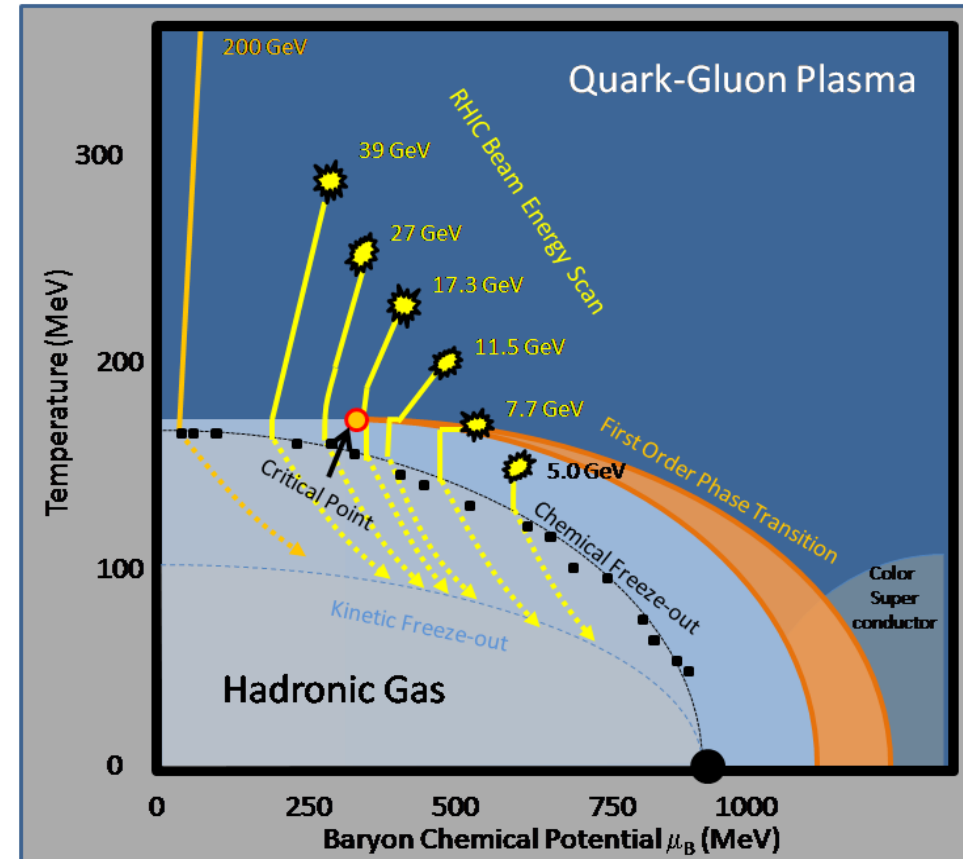
RHIC/LHC/Early Universe



Critical Point Search

- **Physics of QCD phase diagram**
connects the birth of our universe and the final form of materials,
and is probed in laboratory.
- **Critical Point is a Corner Stone of the phase diagram,**
and is accessible if $\mu_{CP} < 500$ MeV.

*Are there any other sites
where Hot and Dense matter
is formed ?
→ Compact Astrophysical
Phenomena !*



Quark Matter in Compact Stars

■ Neutron Star

E.g. N. Glendenning, "Compact Stars"; F. Weber, Prog.Part.Nucl.Phys.54('05)193

- Cold ($T \sim 0$), Dense ($\rho_B \sim 5 \rho_0$), Highly Asymmetric ($Y_p \sim (0.1-0.2)$)

■ Supernovae *T. Hatsuda, MPLA2('87)805; I. Sagert et al., PRL102 ('09) 081101.*

- Warm ($T \sim 20$ MeV), Dense ($\rho_B \sim 1.8 \rho_0$), mildly asym. ($Y_p \sim (0.3-0.4)$)

■ Neutron star merger

- Very dense, warm ($T \sim (10-20)$ MeV)

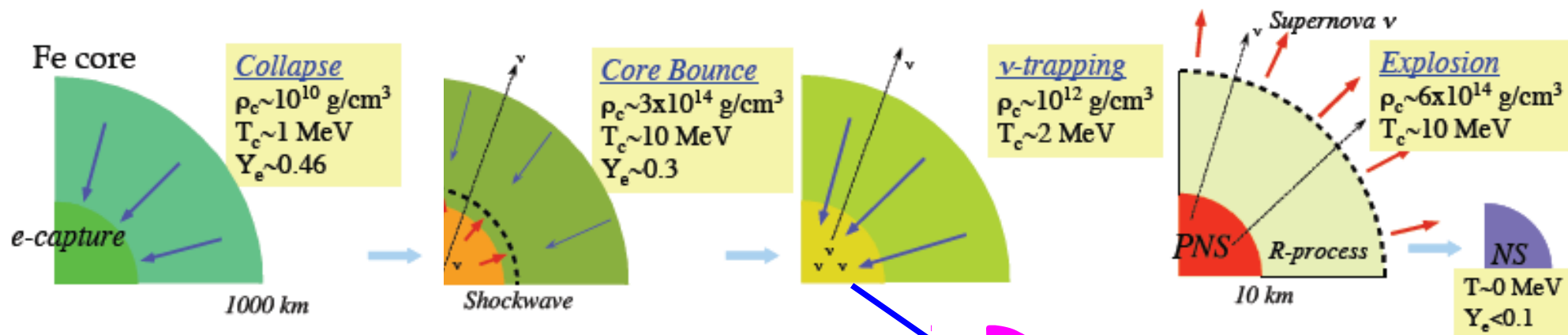
■ *Dynamical black hole formation*

K. Sumiyoshi, et al., PRL97('06) 091101;

K.Sumiyoshi, C.Ishizuka, AO, S.Yamada, H.Suzuki, ApJL690('09),L43

- Hot ($T \sim (70-90)$ MeV), Dense ($\rho_B \sim (4-5)\rho_0$),
and Asymmetric ($Y_p \sim (0.1-0.3)$)

Gravitational Collapse of Heavy Star



Core collapse supernova (type II) Fe core collapse \rightarrow Core bounce

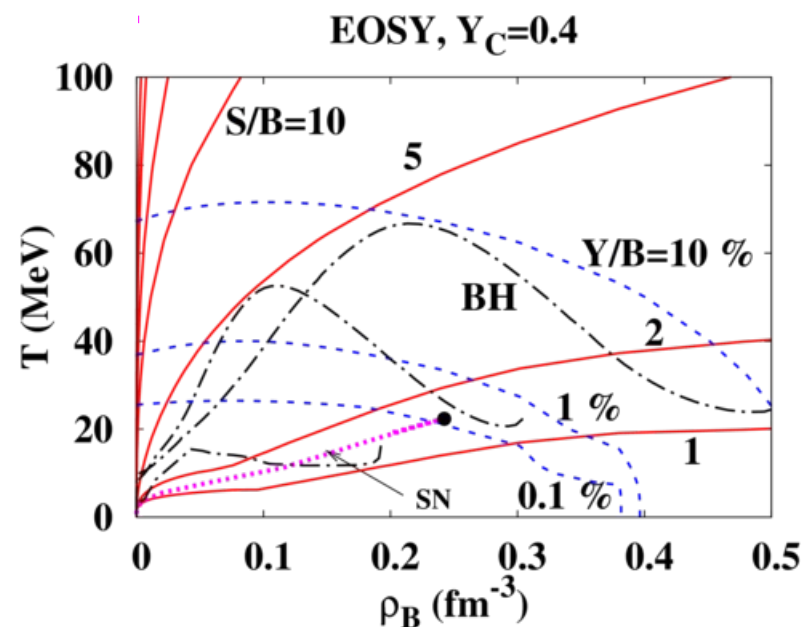
- \rightarrow ν trapping
- \rightarrow proto-neutron star + explosion of envelope

or \rightarrow Black Hole formation + Failed Supernova

M. Liebendorfer et al., ApJS 150('04)263
K. Sumiyoshi et al., PRL 97('06)091101

- Dynamical collapse with accretion.
- Hot and Dense nuclear matter is formed
 $T \sim (70-90) \text{ MeV}$, $\rho_B = 4 \rho_0$

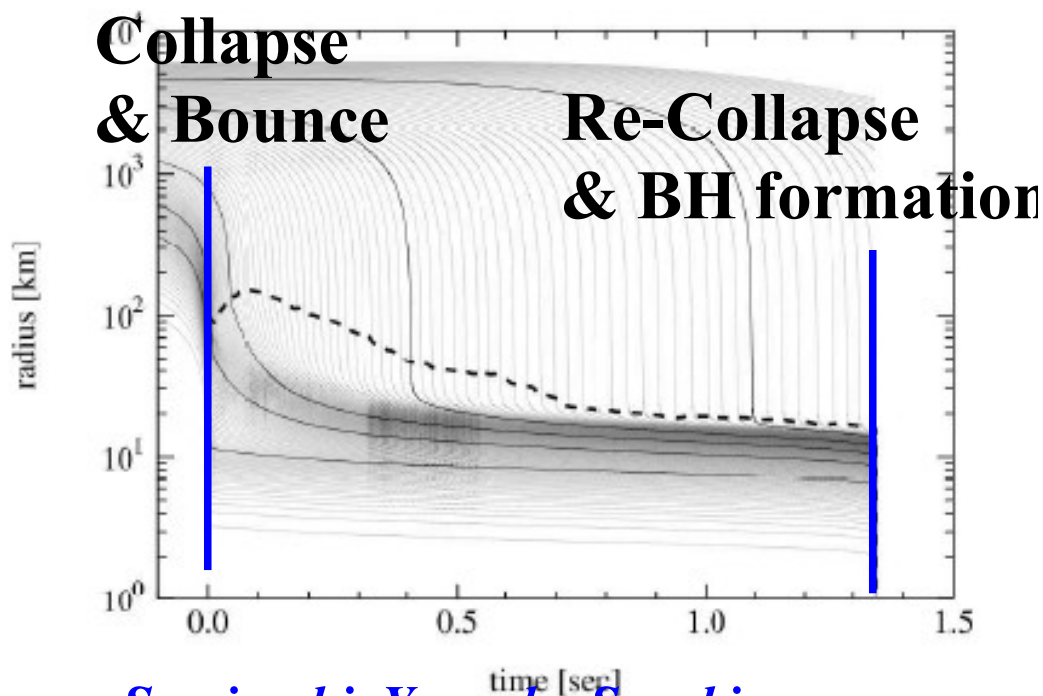
BH $T \sim (70-90) \text{ MeV}$
 $Y_e \sim (0.1-0.3)$



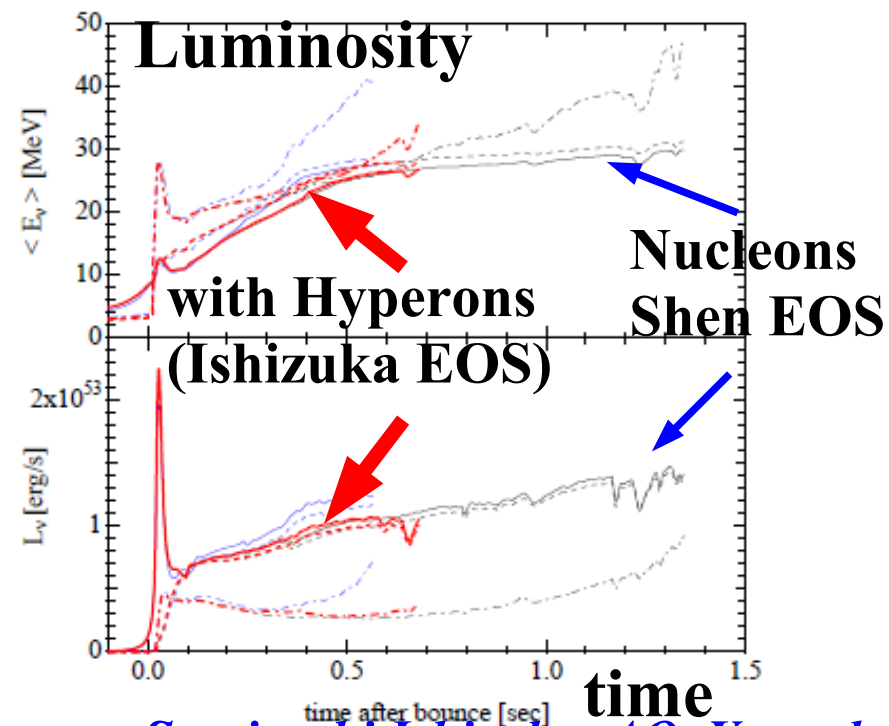
C. Ishizuka, AO, K. Tsubakihara, K. Sumiyoshi, S. Yamada, JPG 35('08) 085201; AO et al., NPA 835('10) 374.

Dynamical Black Hole Formation

- Gravitational collapse of heavy (e.g. $40 M_{\odot}$) progenitor would lead to BH formation.
 - Shock stalls, and heating by ν is not enough to take over strong accretion. → failed supernova
 - ν emission time $\sim (1-2)$ sec w/o exotic matter.
 - emission time is shortened by exotic dof (quarks, hyperons, pions).



Sumiyoshi, Yamada, Suzuki,
Chiba, PRL 97('06)091101.

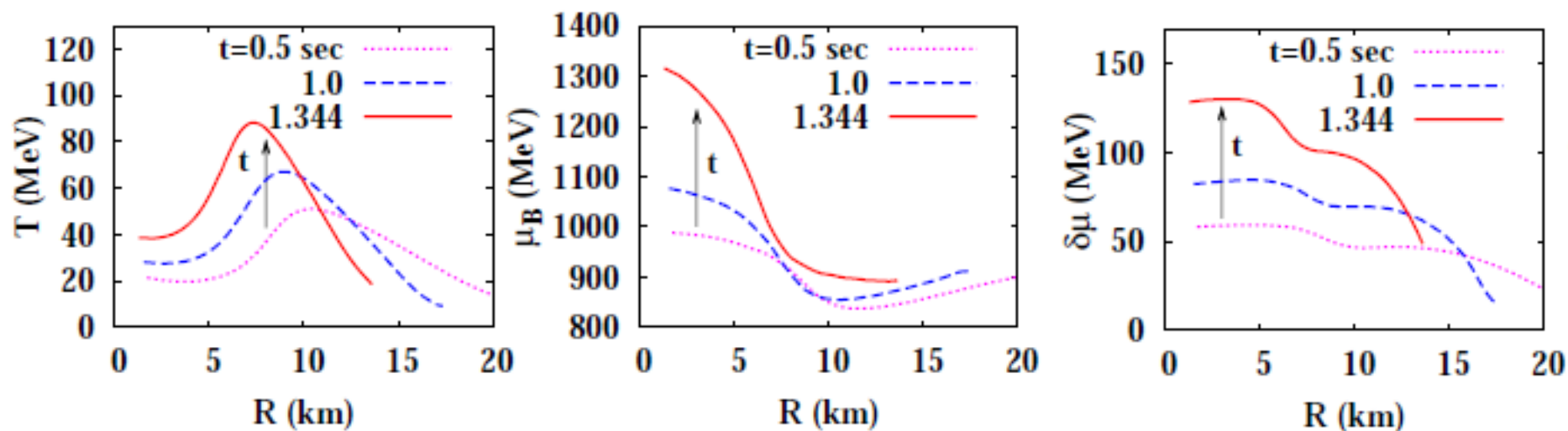


Sumiyoshi, Ishizuka, AO, Yamada,
Suzuki, ApJL 690('09)43.

Thermal Condition during BH formation

- Quark-hadron and nuclear physicists are interested in (T, μ) !
 - Maximum $T \sim 90$ MeV (off-center)
(Heated by shock propagation)
 - Maximum $\mu_B \sim 1300$ MeV (center)
 - Maximum $\delta\mu = (\mu_n - \mu_p)/2 \sim 130$ MeV (center)

Can we reach CP ? What is the effects of $\delta\mu$?

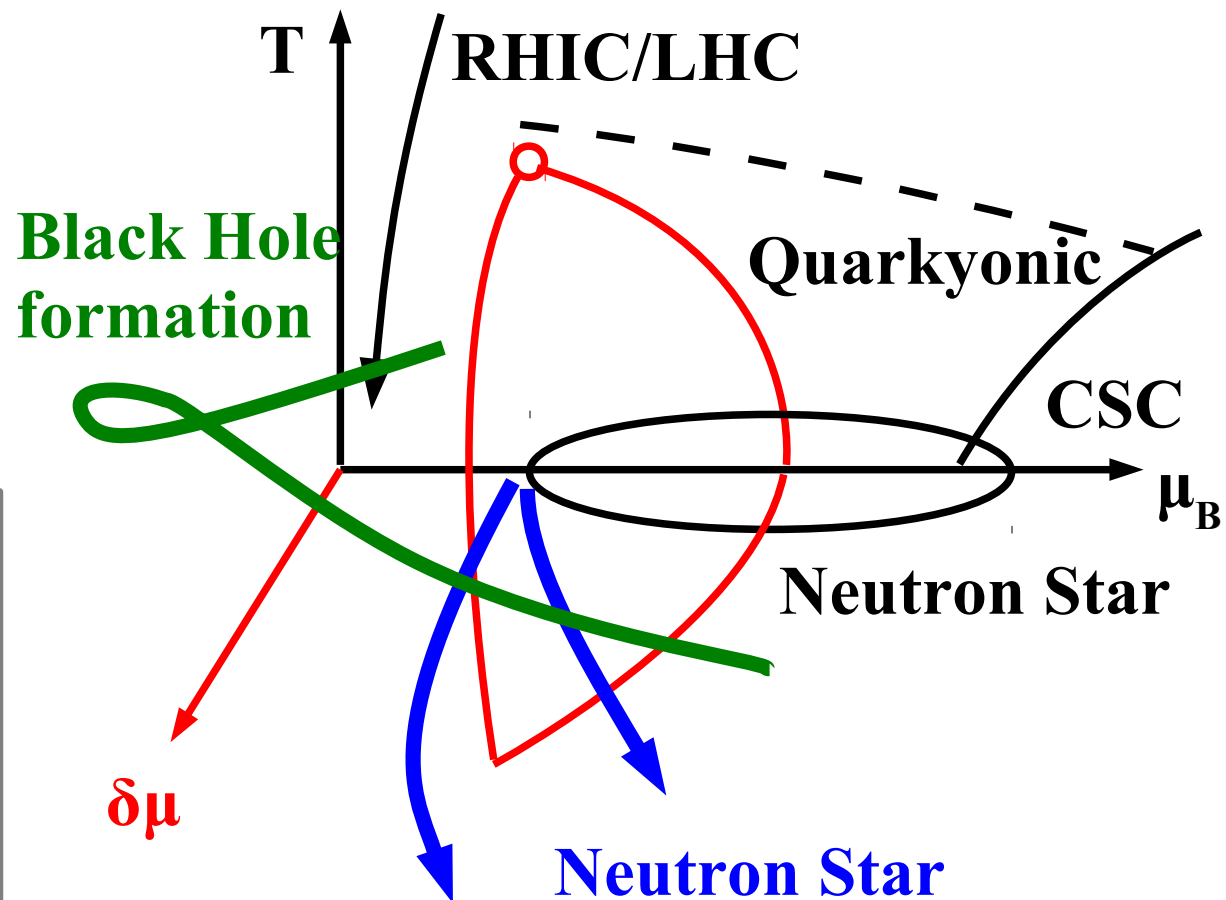


Nucleon+leptons+photon (Shen EOS), 40 Msun

AO, Ueda, Nakano, Ruggieri, Sumiyoshi, PLB704('11),284

QCD phase diagram in Compact Astrophys. Phen.

- Phase diagram probed in High-Energy Heavy-Ion Collisions
 - Hot & Dense *Symmetric* matter
 - Phase diagram probed in Compact Astrophysical Phenomena
 - Hot and/or Dense *Asymmetric* matter
- 3D phase diagram must be considered !
(c.f. P. Zhuang)



We compare the 3D phase diagram in effective models and thermal condition in Compact Stars

Model Details

■ BH formation calculation

Sumiyoshi, Yamada, Suzuki, Chiba, PRL 97('06)091101.

- **v radiation 1D (spherical) Hydrodynamics**
- **v transport is calculated exactly by solving the Boltzmann eq.**
- **Gravitational collapse of $40 M_{\odot}$ star**
- **Initial condition: WW95**
S.E.Woosley, T.A.Weaver, ApJS 101 ('95) 181
- **Shen EOS (npe μ)**

■ QCD effective models

- **NJL, PNJL, PNJL with 8 quark int., PQM**
- **$N_f=2$**
- **Vector coupling $\rightarrow G_v/G_s$ (g_v/g_s in PQM)=0, 0.2**

*Phase diagram
in (Isospin) Asymmetric Matter*

Chiral Effective Models

■ Approaches to Phase Diagram

● Lattice QCD:

Reliable at small μ ($\mu \ll T$), but has the sign problem at large μ

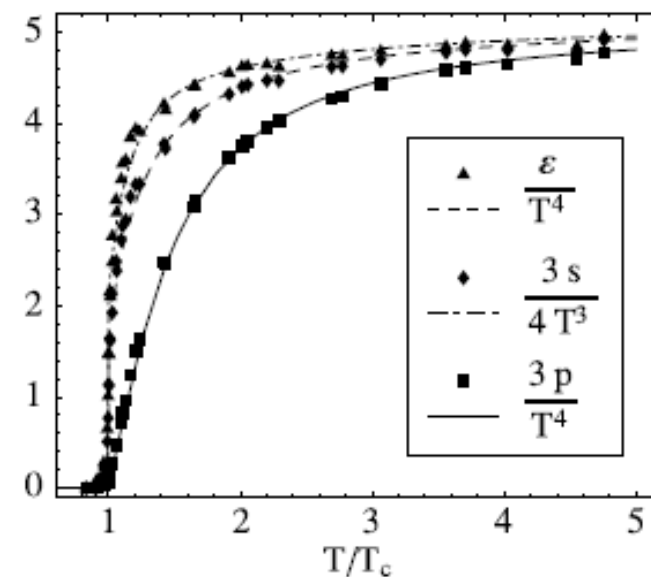
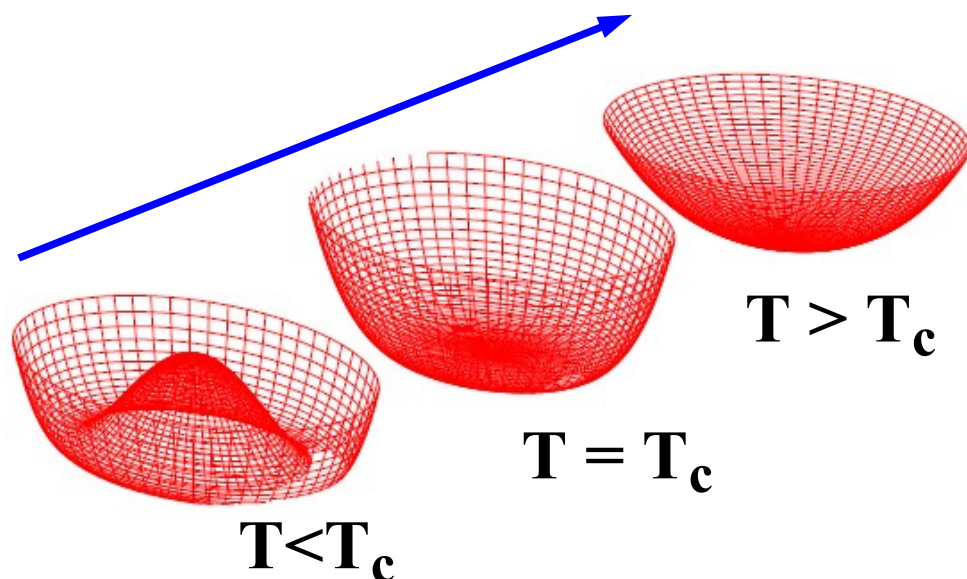
● Chiral Effective models: NJL, PNJL, PQM

Nambu, Jona-Lasinio ('61), Fukushima('03), Ratti, Thaler, Weise ('06),

B.J.Schafer, Pawłowski, Wambach ('07); Skokov, Friman, E.Nakano, Redlich('10)

Spontaneous breaking & restoration of chiral symmetry

Polyakov loop extension \rightarrow Deconf. transitions



Roessner et al.('07)

Chiral Effective Models ($N_f=2$)

■ Lagrangian (PQM, as an example)

$$L = \bar{q} \left[i \gamma^\mu \underline{D_\mu} - g_\sigma \underline{(\sigma + i \gamma_5 \tau \cdot \pi)} \right] q + \frac{1}{2} \partial^\mu \sigma \partial_\mu \sigma + \frac{1}{2} \partial^\mu \pi \cdot \partial_\mu \pi$$

q-Pol. quark-meson

$$- \underline{U_\sigma(\sigma, \pi)} - \underline{U_\Phi(\Phi, \bar{\Phi})}$$

chiral Polyakov

$$F_{\text{eff}} \equiv \Omega/V = U_\sigma(\sigma, \pi=0) + U_\Phi(\Phi, \bar{\Phi}) + \underline{F_{\text{therm}}} + \underline{U_{\text{vac}}(\sigma, \Phi, \bar{\Phi})}$$

particle exc. q zero point

■ Polyakov loop effective potential from Haar measure

$U_\Phi \sim -\log(\text{Haar Measure})$ (Fit lattice data to fix parameters).

■ Vector coupling is not known well \rightarrow Comparison of $g_v/g_s=0, 0.2$

$$L_V = -g_v \bar{q} \gamma_\mu (\omega^\mu + \tau \cdot R^\mu) q - \frac{1}{4} \omega_{\mu\nu} \omega^{\mu\nu} - \frac{1}{4} R_{\mu\nu} \cdot R^{\mu\nu} + \frac{1}{2} m_\omega^2 \omega_\mu \omega^\mu + \frac{1}{2} m_\rho^2 R_\mu R^\mu$$

■ 8 Fermi interaction

T. Sasaki, Y. Sakai, H. Kouno, M. Yahiro ('10)

$$G_{\sigma 8} \left[(\bar{q}q)^2 + (\bar{q}i\gamma_5\tau q)^2 \right]^2$$

Isospin chemical potential

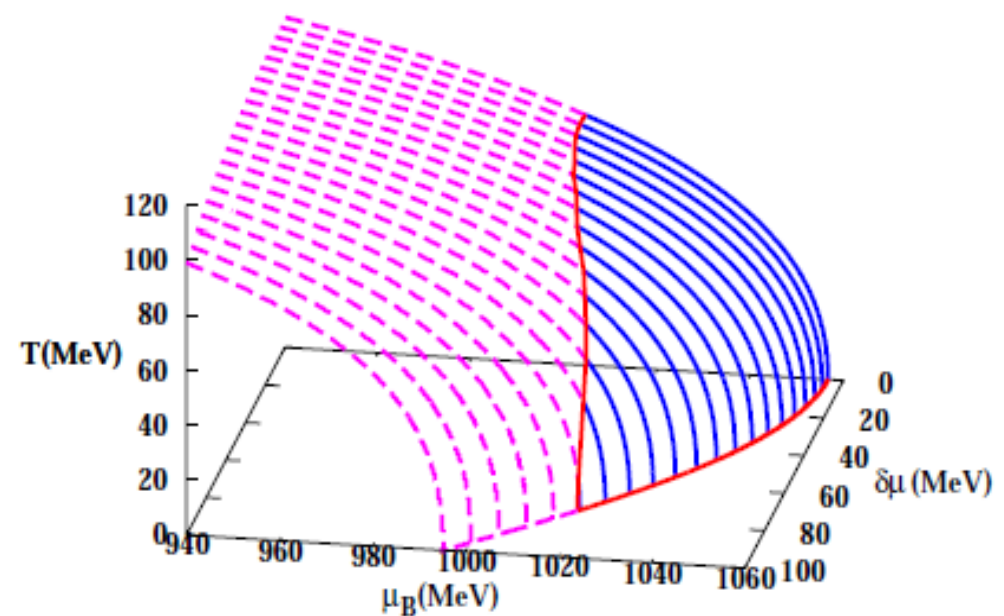
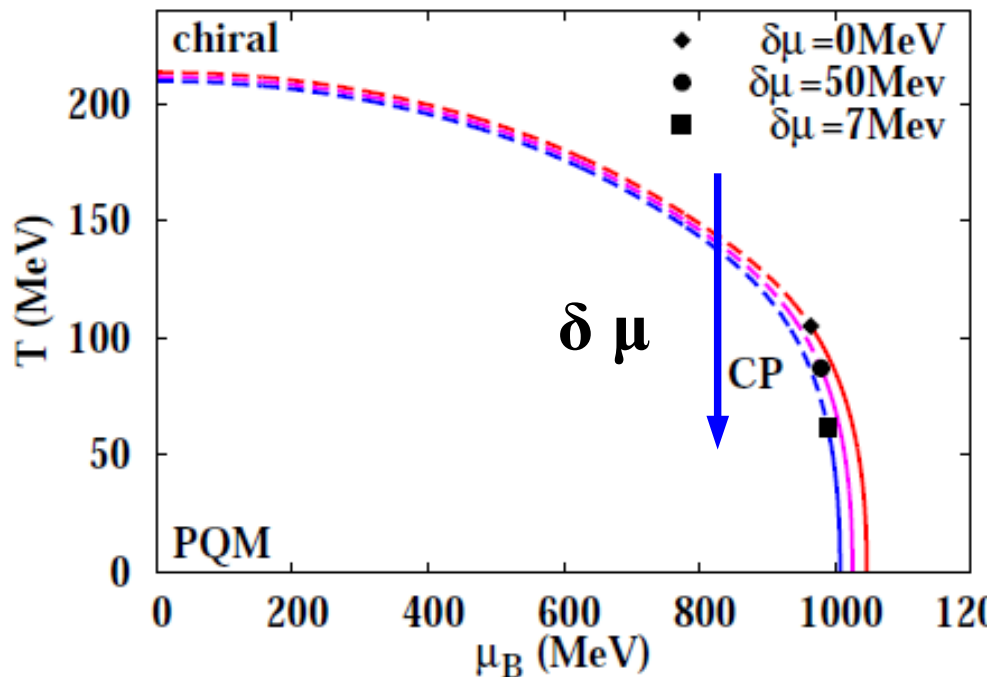
■ Isospin chemical potential $\delta\mu$

$$\delta\mu = (\mu_d - \mu_u)/2 = (\mu_n - \mu_p)/2 \rightarrow \mu_d = \mu_q + \delta\mu, \mu_u = \mu_q - \delta\mu$$

● Finite $\delta\mu \rightarrow$ (Isospin) Asymmetric matter $N_u \neq N_d$

\rightarrow Smaller “Effective” number of flavors

\rightarrow Weaker phase transition \rightarrow smaller T_{CP}

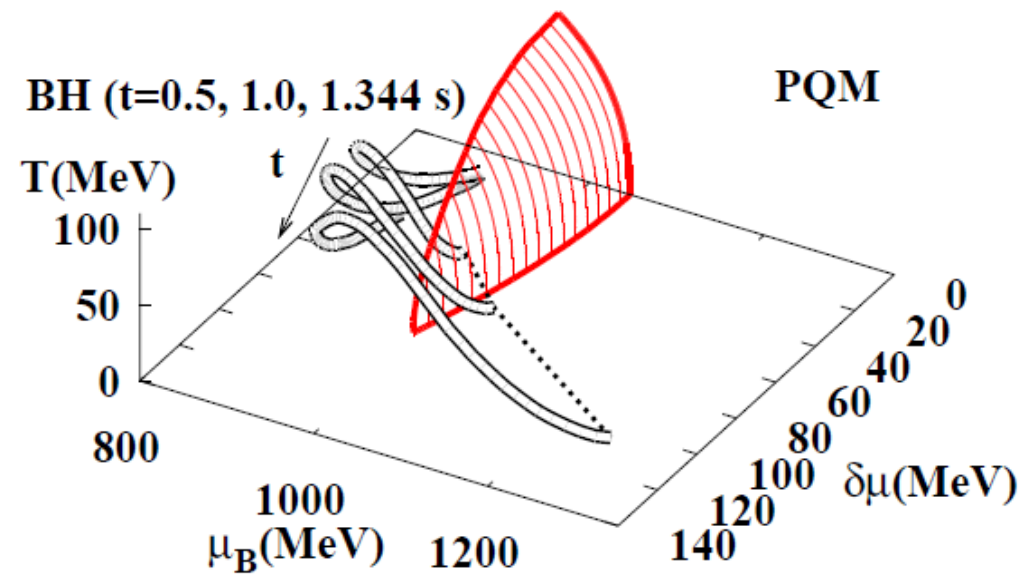
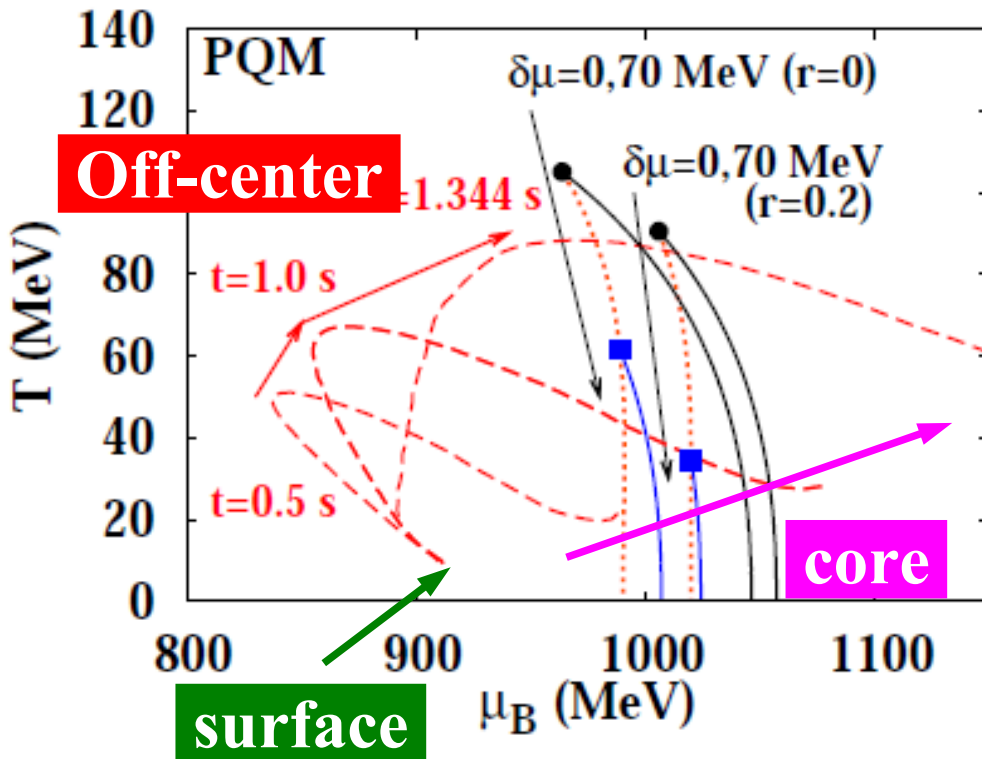


H. Ueda, et al, in preparation

*Critical Point sweep
during black hole formation*

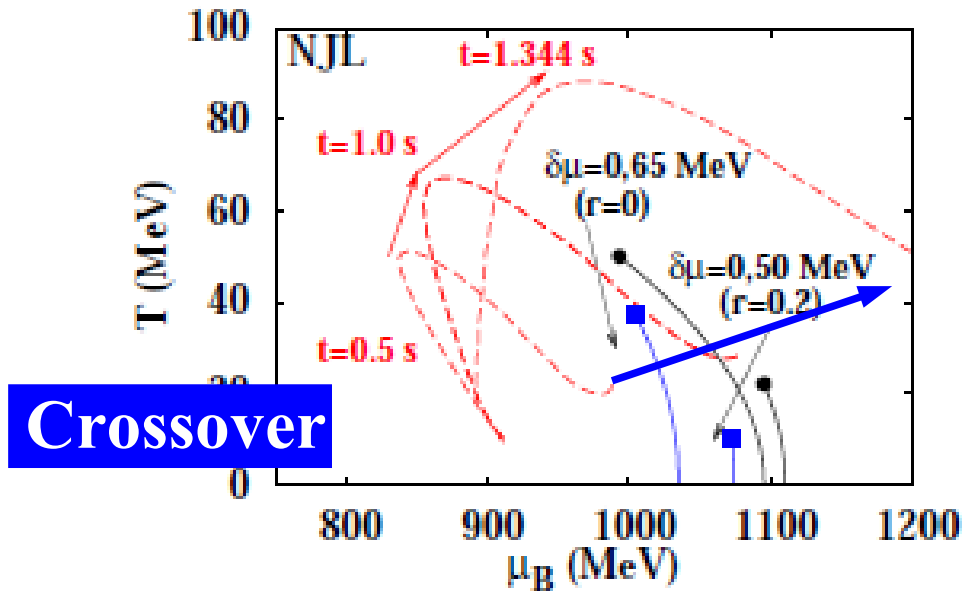
How is quark matter formed during BH formation ?

- Highest μ_B just before horizon formation ~ 1300 MeV
 $>$ QCD transition μ (1000-1100 MeV)
 \rightarrow *Quark matter is formed before BH formation*
- Core evolves below CP, Off-center goes above CP
 \rightarrow *CP sweep*

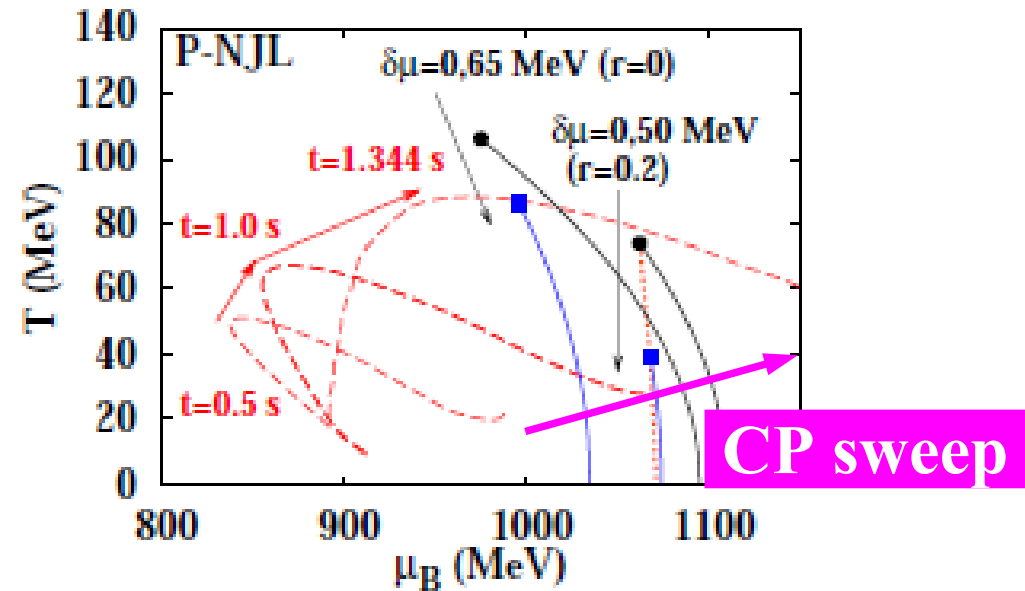


How is quark matter formed during BH formation ?

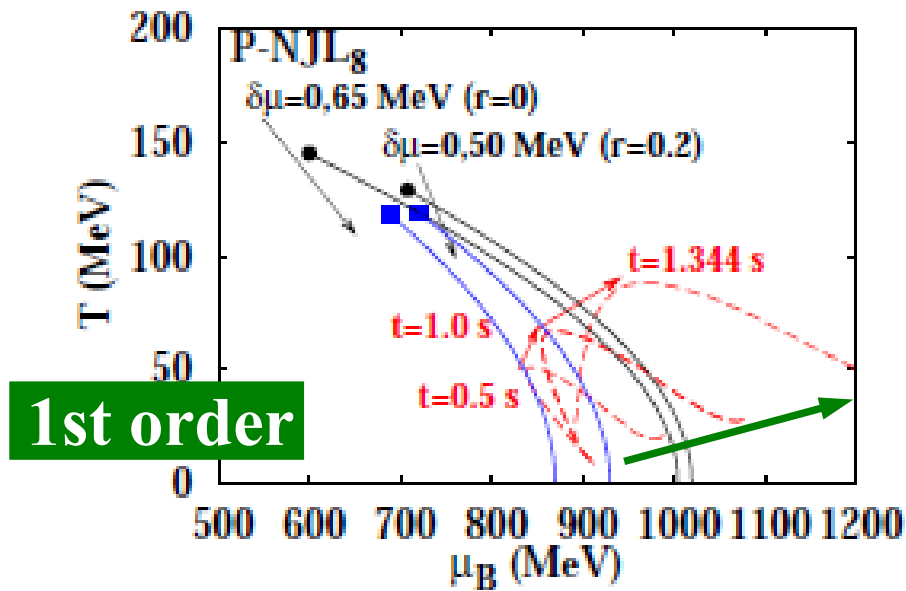
- Model dependence to form quark matter → Three ways



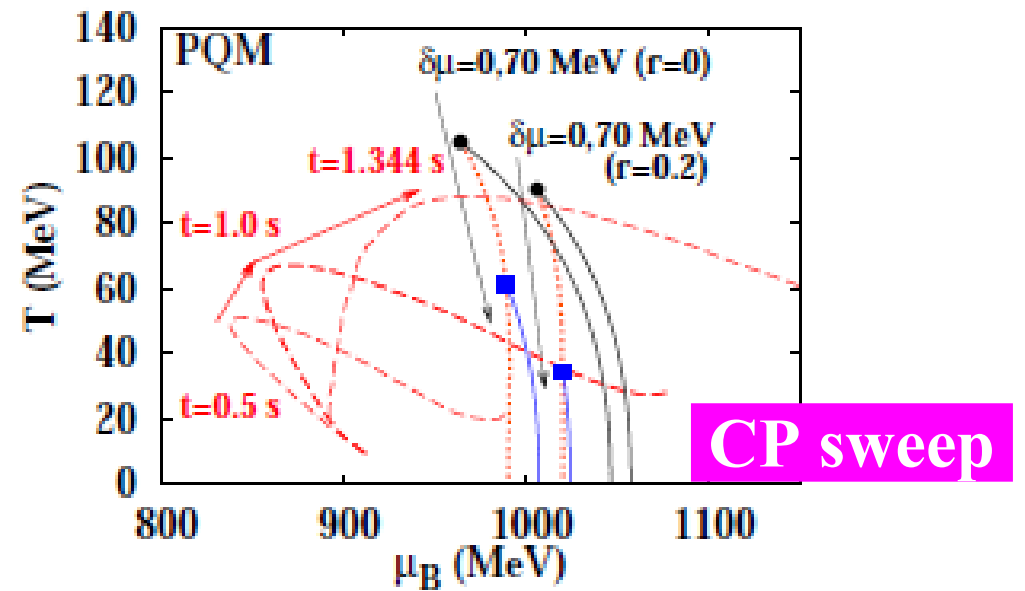
Crossover



CP sweep



1st order



CP sweep

Swept Region of Phase Diagram during BH formation

■ CP location in Symmetric Matter

- Lattice QCD

$$\mu_{CP} = (400-900) \text{ MeV}$$

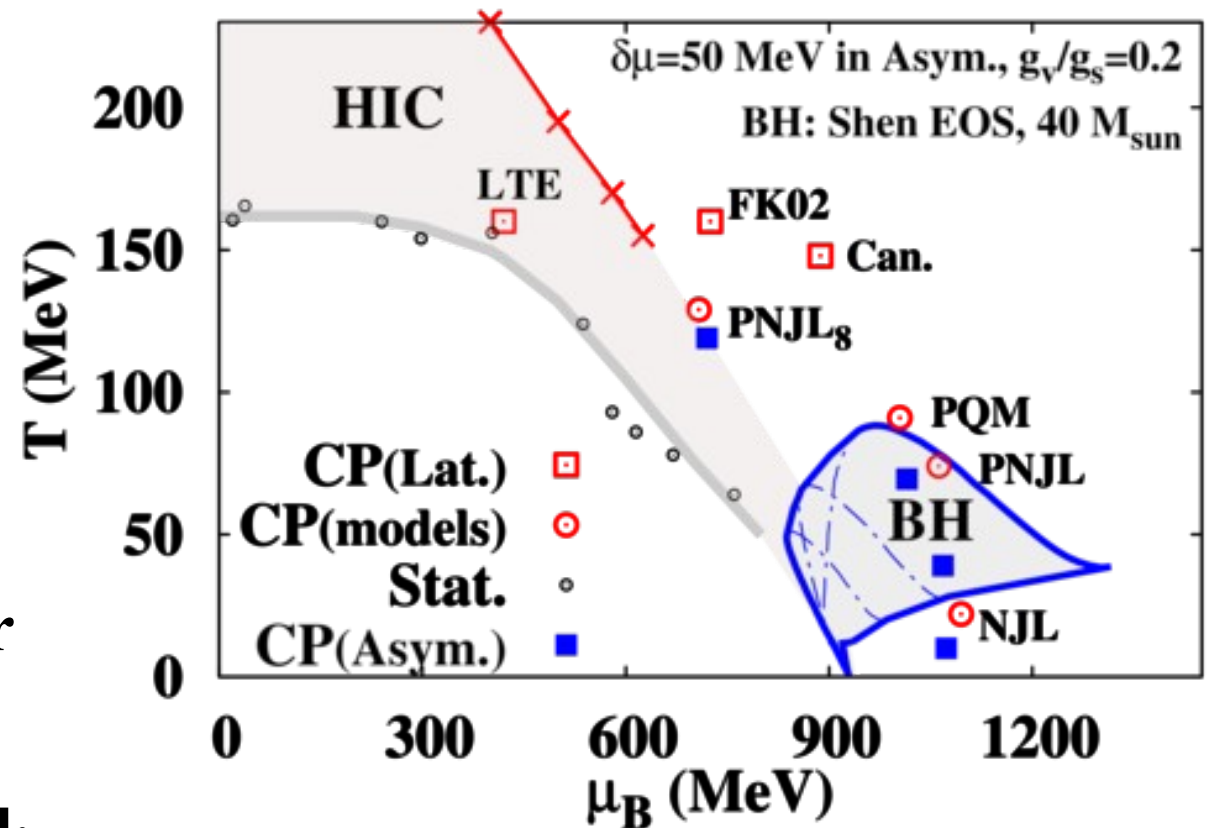
- Effective models

$$\mu_{CP} = (700-1050) \text{ MeV}$$

■ CP in Asymmetric Matter (E.g. $\delta\mu=50 \text{ MeV}$)

- T_{CP} decreases at finite $\delta\mu$.

→ Accessible (T, μ_B) region during BH formation



(Stephanov plot)

M.A.Stephanov, Prog.Theor.Phys.Suppl.153 ('04)139;
FK02:Z. Fodor, S.D.Katz, JHEP 0203 (2002) 014
LTE:S. Ejiri et al., Prog.Theor.Phys.Suppl. 153 (2004) 118;
Can: S. Ejiri, PRD78 (2008) 074507
Stat.:A. Andronic et al., NPA 772('06)167

How about Neutron Stars ?

■ Contraction of Proto-Neutron Star

- (T, μ_B) are not enough at 1 sec after bounce of $15 M_{\odot}$ star collapse
- Larger (T, μ_B) is expected in long time evolution (~ 20 sec) or heavier proto-neutron stars.

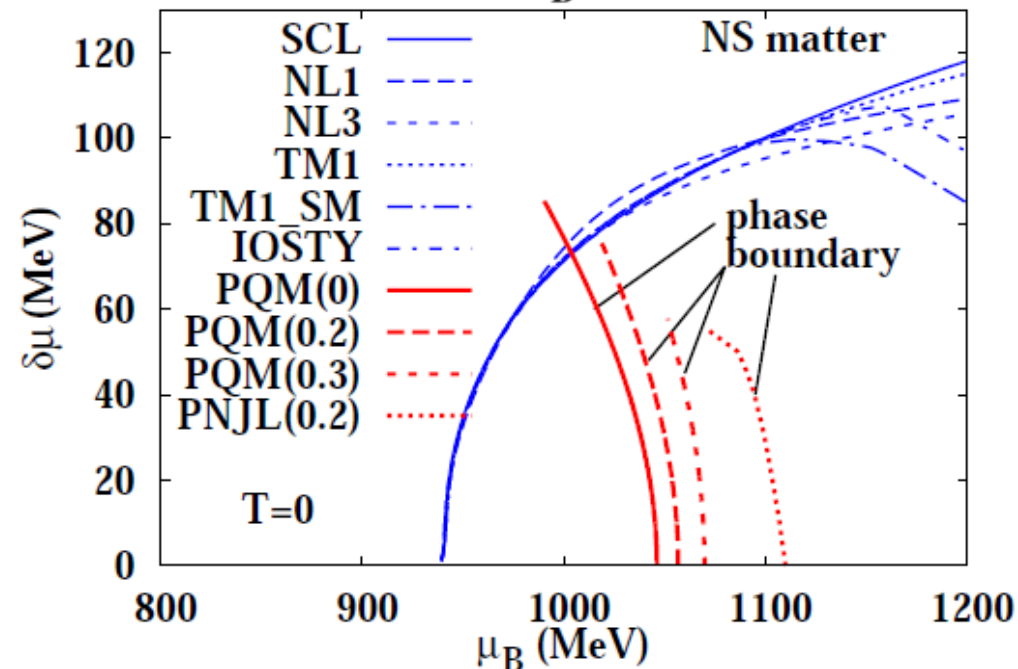
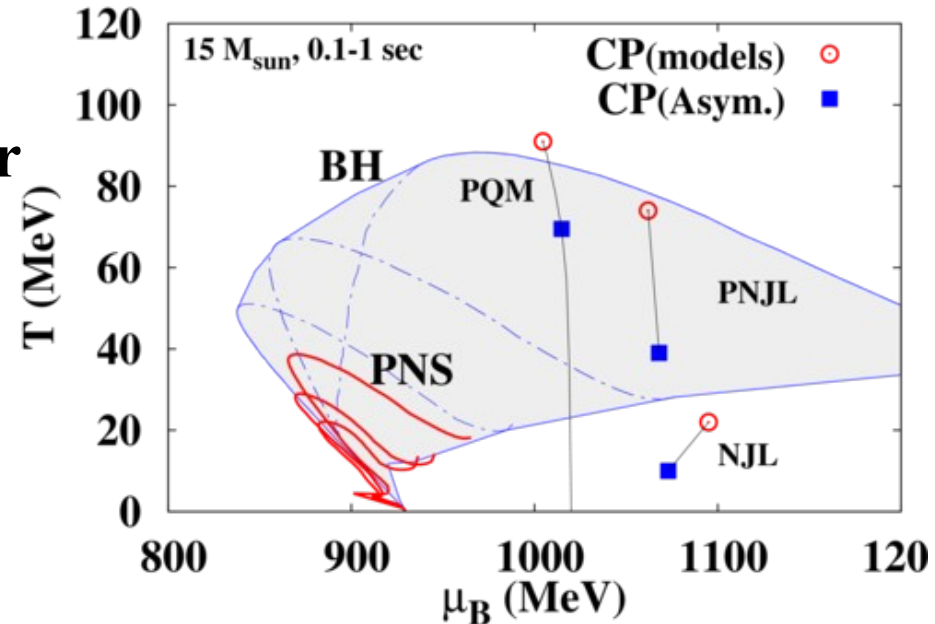
K. Sumiyoshi et al. ApJ 629 ('05) 922;

J. A. Pons et al., ApJ 513 ('99) 780;

J. A. Pons et al., ApJ 553 ('01) 382.

■ Cold Neutron Star

- max. $\delta \mu \sim 100$ MeV
- Possibility of cross over in NS



H. Ueda et al., in preparation

Discussion

■ How can we observe the phase transition signal ?

- ν spectrum ? Gravitational waves ?

Supernova: Second peak in ν & $\bar{\nu}$ emission

Hatsuda('87), Sagert et al.('09)

■ How frequent do dynamical BH formation take place ?

- Less frequent than SN ($< 20 M_{\odot}$), but should be in collapse of heavy stars ($> 40 M_{\odot}$).

C.L.Fryer, ApJ 522('99)413; E.O'Connor, C.D.Ott, ApJ 730('11)70

■ Strangeness may reduce $\delta\mu$ in hadronic / quark matter

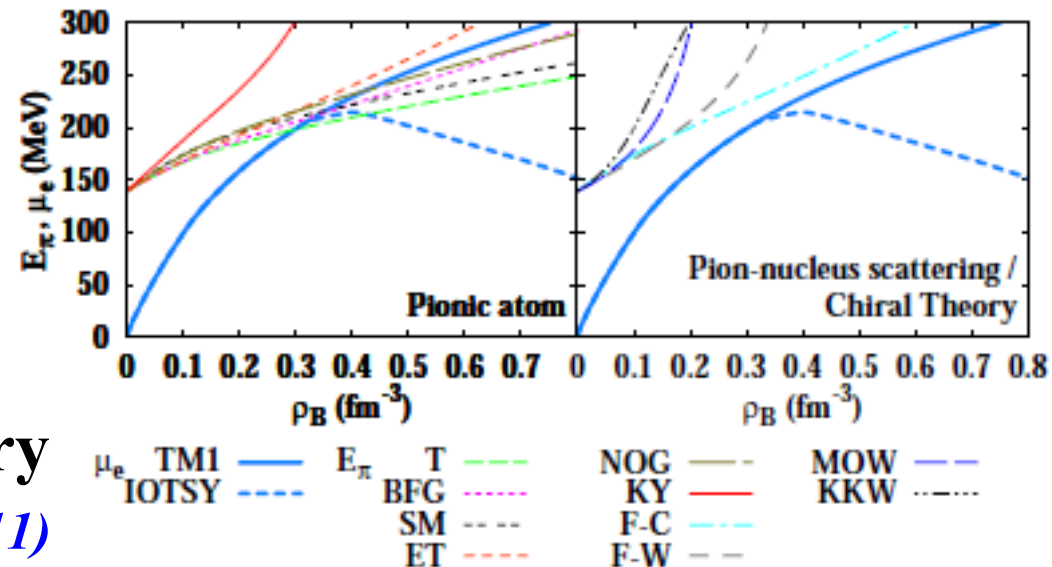
- No s-wave π cond. in NS

AO, D. Jido, T. Sekihara,

K. Tsubakihara, PRC80('09)038202.

■ Hadron-Quark EOS is necessary

E.g. Steinheimer, Schramm, Stocker('11)



Summary and Discussion

- **Critical Point temperature is expected to be reduced in asymmetric nuclear matter.**
- **Black hole formation processes produce hot (~ 90 MeV) and dense ($\mu_B \sim 1300$ MeV) matter, and we expect the formation of baryon rich quark matter.**
- **Since the temperature and asymmetry ($\delta\mu \sim 130$ MeV) are high, we have a possibility that CP is swept during BH formation.**
- **Construction of Hadron-Quark matter EOS with CP and its application to BH formation are desired.
(c.f. J. Steinheimer; D. Blaschke)**

Thank you for your attention !

Collaborators

T.Z.Nakano (Kyoto U./YITP),

H. Ueda (Kyoto U.), M. Ruggieri (YITP)

K. Sumiyoshi (Numazu), K. Tsubakihara (Hokkaido U.),

C. Ishizuka (Tokyo U. of Sci.),

S. Yamada (Waseda), H. Suzuki (Tokyo U. Sci.),

Questions and Conclusion

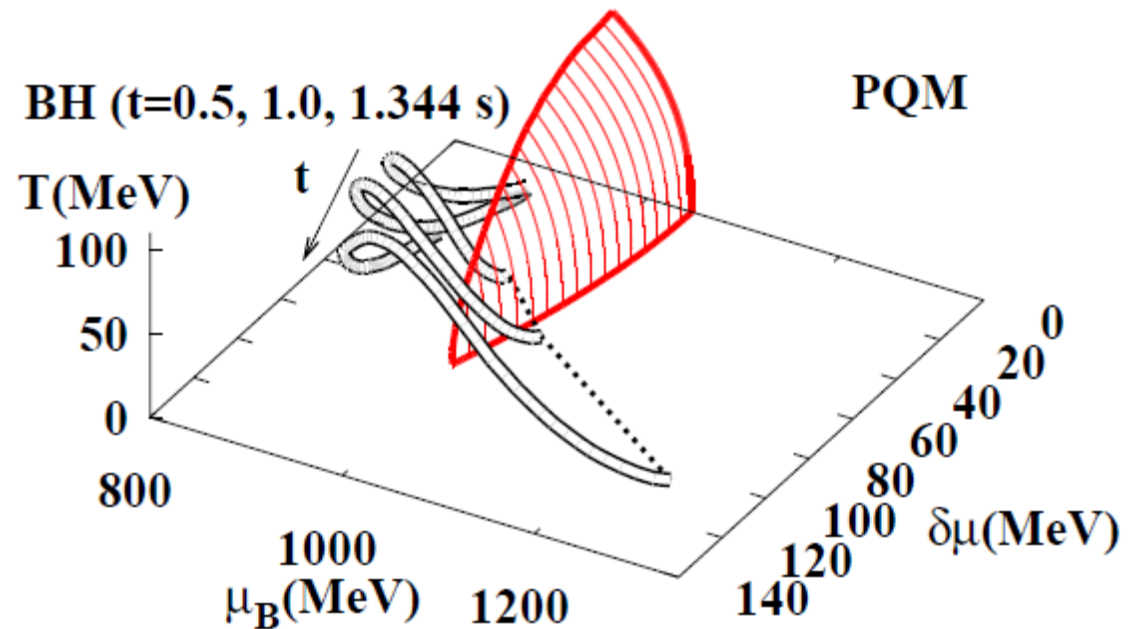
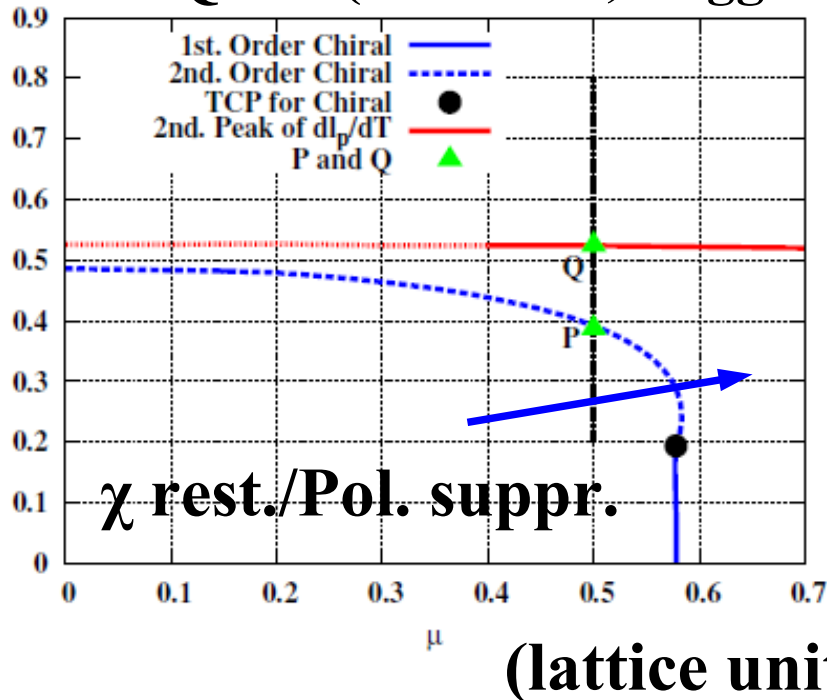
■ Does Quarkyonic matter exist in QCD with $N_c=3$?

→ There is χ restored & Polyakov loop suppressed region at low T and large μ in Strong Coupling Lattice QCD

■ Is there any site where Quarkyonic matter is formed ?

→ During the dynamical black hole formation, CP may be swept and quarkyonic matter may be formed.

P-SC-LQCD (NLO+LO, staggered)



Quarkyonic matter

■ Do χ and Z_{N_c} transitions deviate at large μ ?

● Large N_c : Yes

L. McLerran, R. D. Pisarski, NPA796 ('07)83

● Effective Models: Yes and No

◆ Yes, in PNJL with some parameter set

L. McLerran, K. Redlich, C. Sasaki, NPA824('09)86; H. Abuki et al. ('08); Y. Sakai et al. ('10); D. Blaschke et al. ('11)

◆ No, with FRG or phen. inputs

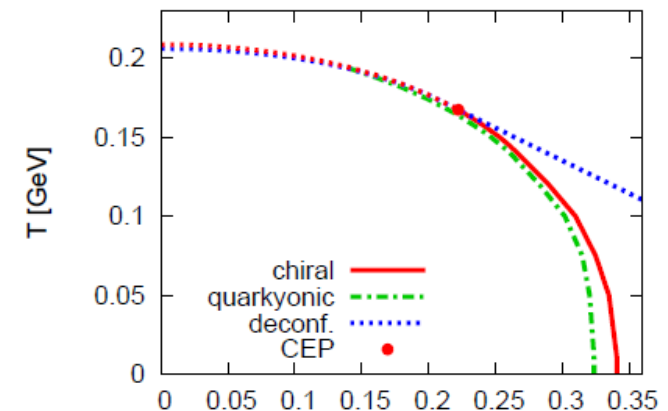
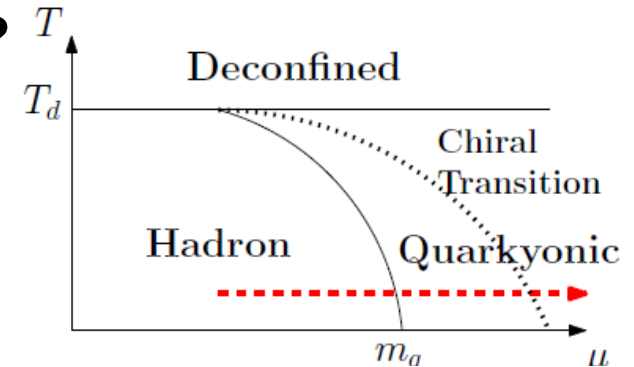
T. K. Herbst, J. M. Pawłowski, B. J. Schaefer, PLB 696 ('11)58 (PQM-FRG), K. Fukushima, PLB 695('11)387 (PNJL+Stat.)

■ QCD with $N_c=3$: Difficult

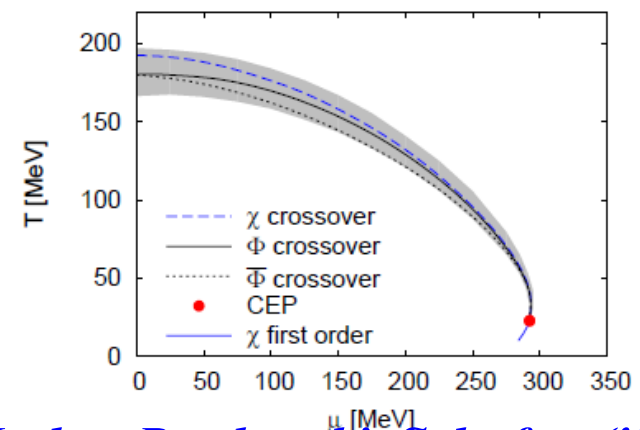
● AC, Taylor expansion, ... $\rightarrow \mu/T < 1$

● QCD-FRG: Not yet

● *SC-LQCD: This work*



McLerran, Redlich, Sasaki ('09)



Herbst, Pawłowski, Schaefer, ('11)

Strong Coupling Lattice QCD

- SC-LQCD has been a successful tool from the beginning of the lattice QCD formulation !
 - Pure Yang-Mills theory → **Confinement**
Area Law (Wilson ('74)), S.C. Expansion (Munster ('81)),
Finite T Pol. loop eff. action (Langelage, Münster, Philipsen ('08)), ..
 - With fermion → **SSB and restoration of Chiral Symmetry**
SSB [Kawamoto, Smit ('81)]
meson mass [Kluberg-Stern, Morel, Petersson ('83)],
Chiral restoration [Damgaard, Kawamoto, Shigemoto('84)],
phase diagram [Bilic, Karsch, Redlich ('92), Fukushima ('04),
Kawamoto, Miura, AO, Ohnuma ('07), de Forcrand, Fromm ('10)],
Finite coupling [Miura, Nakano, AO, Kawamoto ('09-'11)]
 - Combination → **Chiral and Polyakov loop dynamics**
Chiral Polyakov Dynamics [Ilgenfritz, Kripfganz ('85),
Gocksch, Ogilvie ('85), Fukkushima('03), Nakano, Miura, AO('11),
Miura, Nakano, AO, Kawamoto('11)]

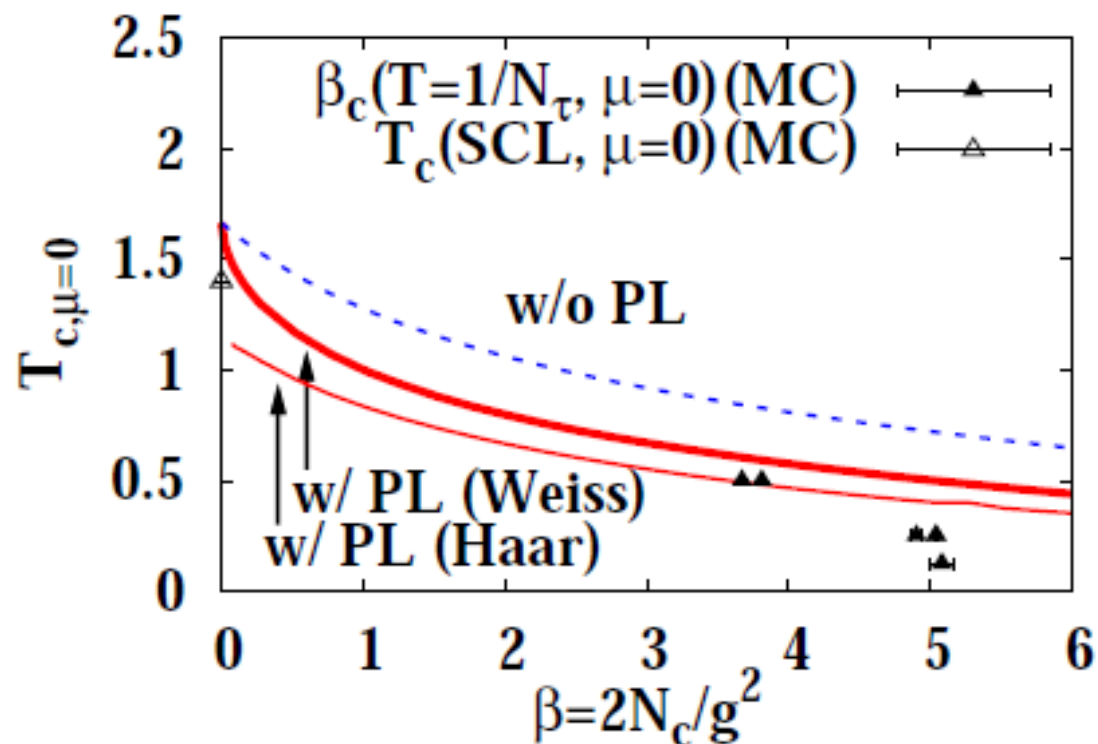
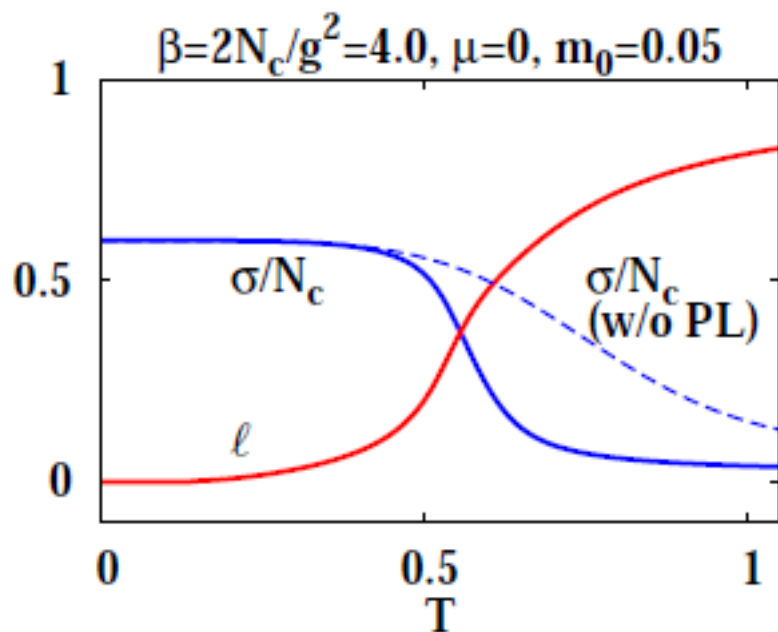
Does SC-LQCD show quarkyonic matter ?

P-SC-LQCD at $\mu=0$

T. Z. Nakano, K. Miura, *AO, PRD 83 (2011), 016014 [arXiv:1009.1518 [hep-lat]]*

- P-SC-LQCD reproduces $T_c(\mu=0)$ in the strong coupling region ($\beta = 2N_c/g^2 \leq 4$)

MC data: SCL (Karsch et al. (MDP), de Forcrand, Fromm (MDP)), $N_\tau=2$ (de Forcrand, private), $N_\tau=4$ (Gottlieb et al. ('87), Fodor-Katz ('02)), $N_\tau=8$ (Gavai et al. ('90))



Lattice Unit

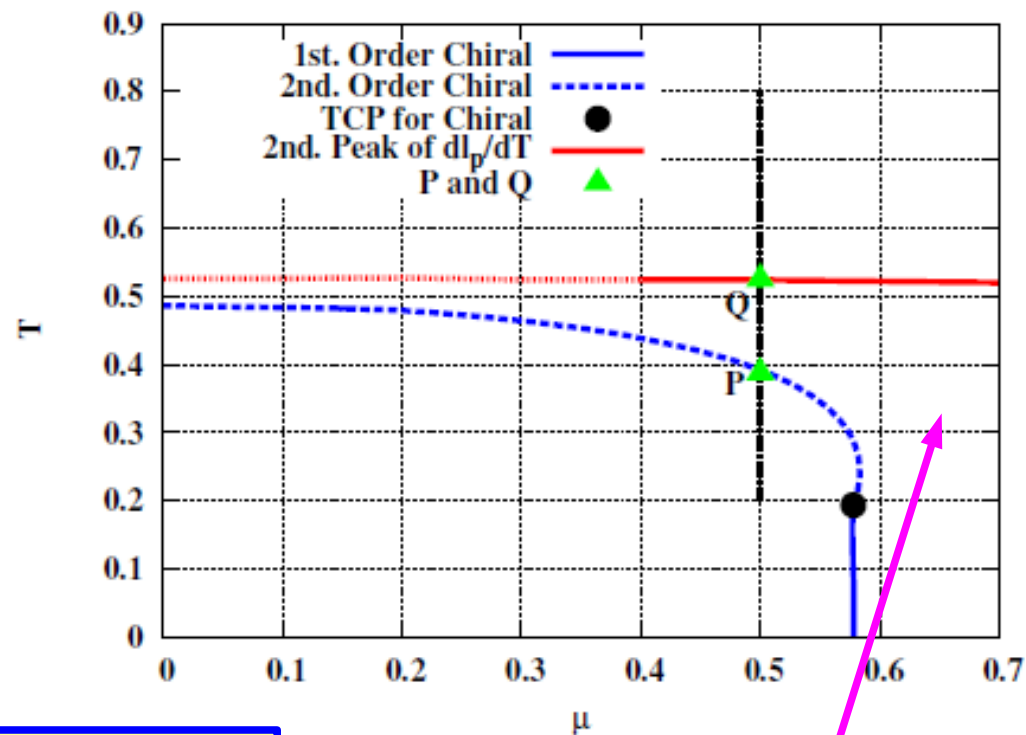
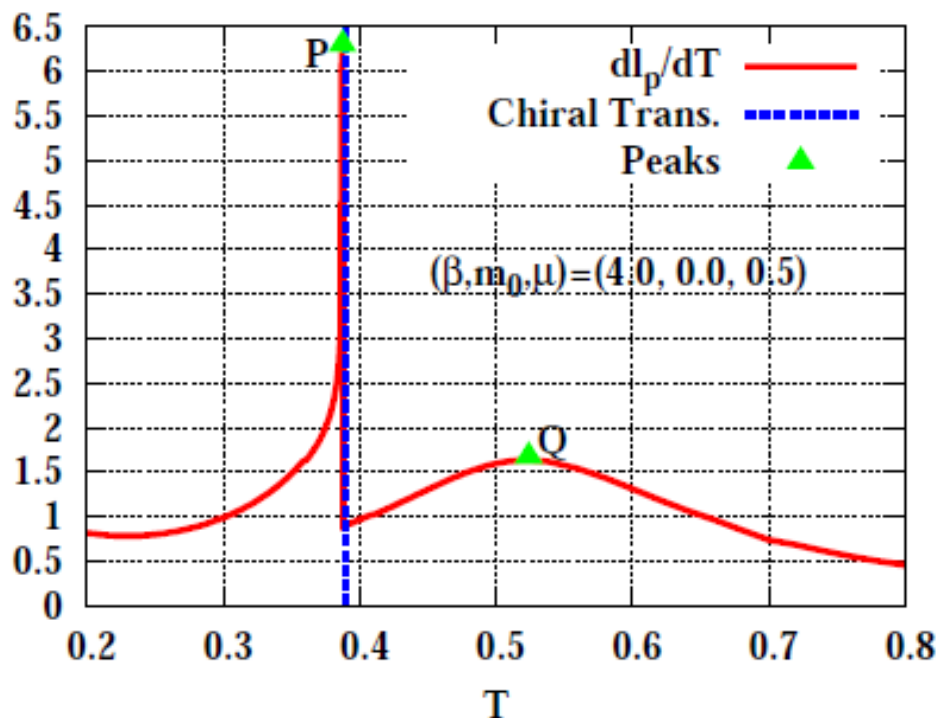
Phase diagram in P-SC-LQCD

K. Miura, T.Z. Nakano, AO, N. Kawamoto,

PoS LATTICE2010 (2010), 202 [arXiv:1012.1509 [hep-lat]] ; in prep.

and predicts the existence of the “Quarkyonic-like” matter

dl_p/dT has two peaks: Chiral-induced & Z_{N_c} -induced.



“Q” depends only weakly on μ and m_0 .
 $\rightarrow Z_{N_c}$ -induced peak

Quarkyonic-like
 (χ restored,
 Pol. loop suppressed.)