

Phenomenological approach to dense hyperon mixed matter EOS

Akira Ohnishi (YITP, Kyoto Univ.)

YIPQS Long-term workshop

Dynamics and Correlations in Exotic Nuclei (DCEN2011)

20th September - 28th October, 2011

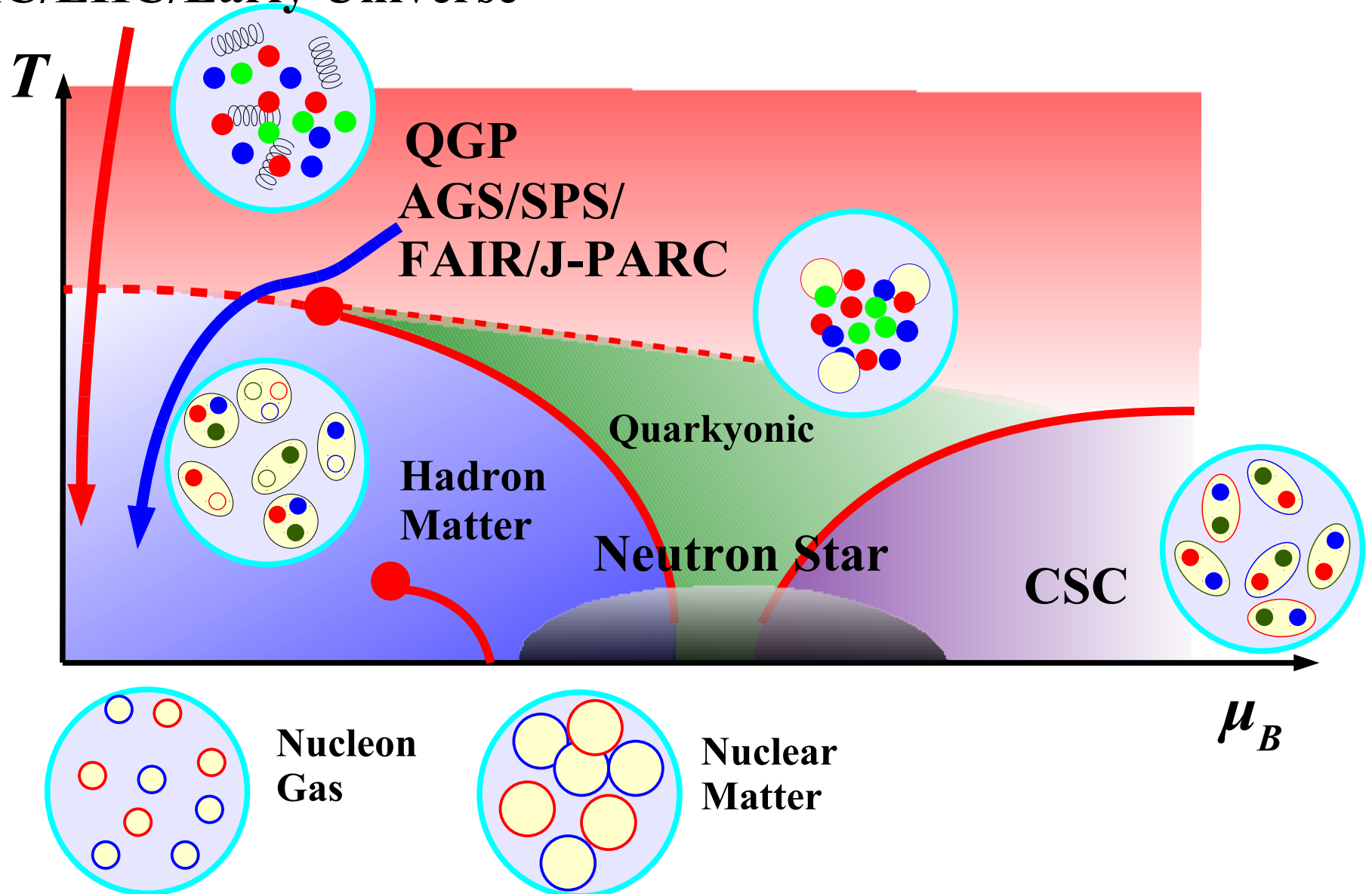
Yukawa Institute for Theoretical Physics, Kyoto, Japan

- Introduction
- Relativistic Mean Field for Hypernuclei and Hyperonic Matter
- Do hyperons survive in $1.97 M_{\odot}$ neutron star ?
- Summary

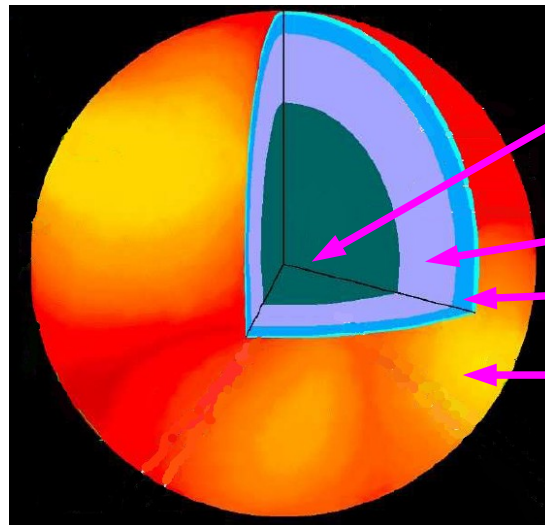


QCD Phase Diagram

RHIC/LHC/Early Universe



Neutron Star Composition

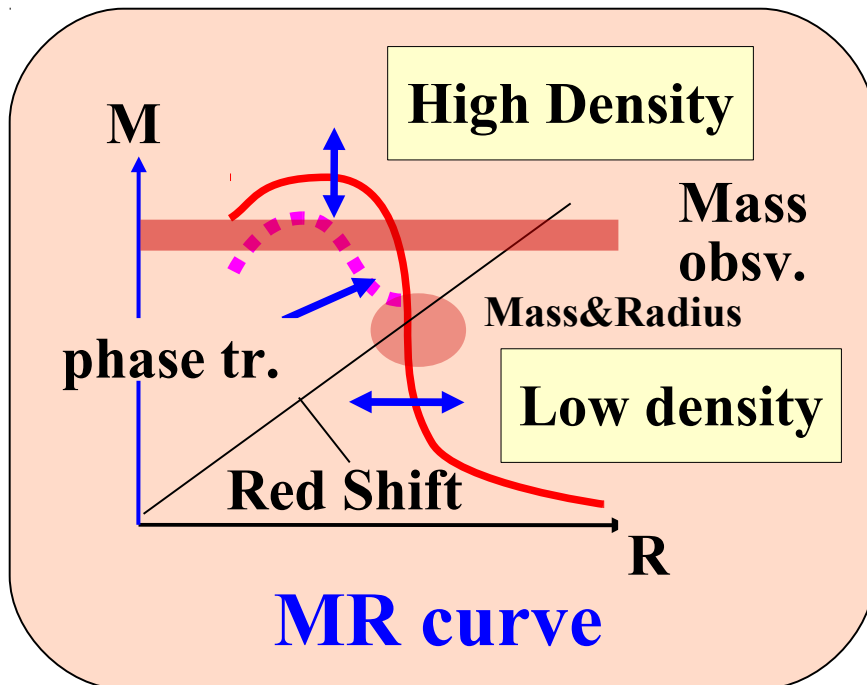


Hyperons, mesons, quarks

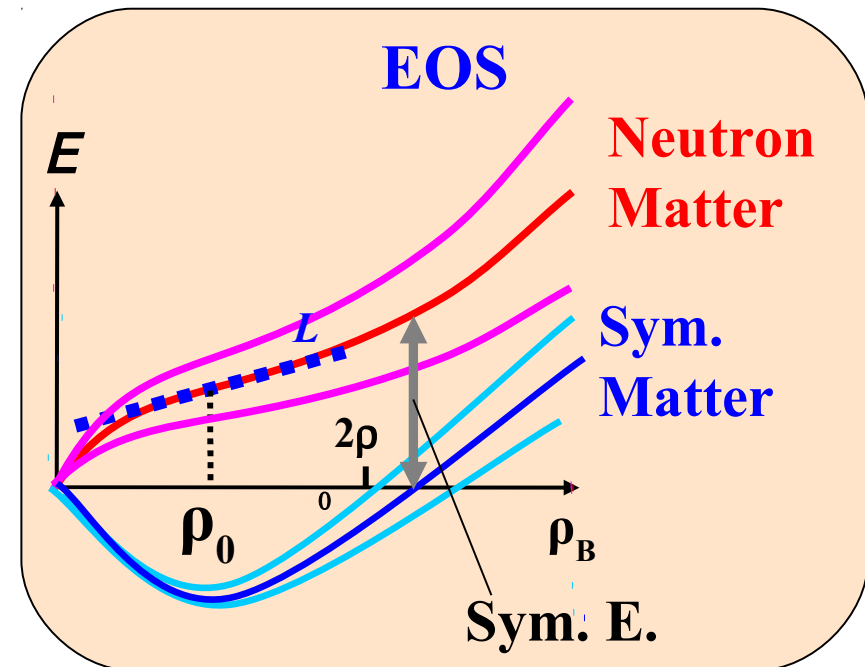
Asym. nuclear matter+elec.+ μ

Nuclei+neutron gas+elec.

Nuclei + elec.

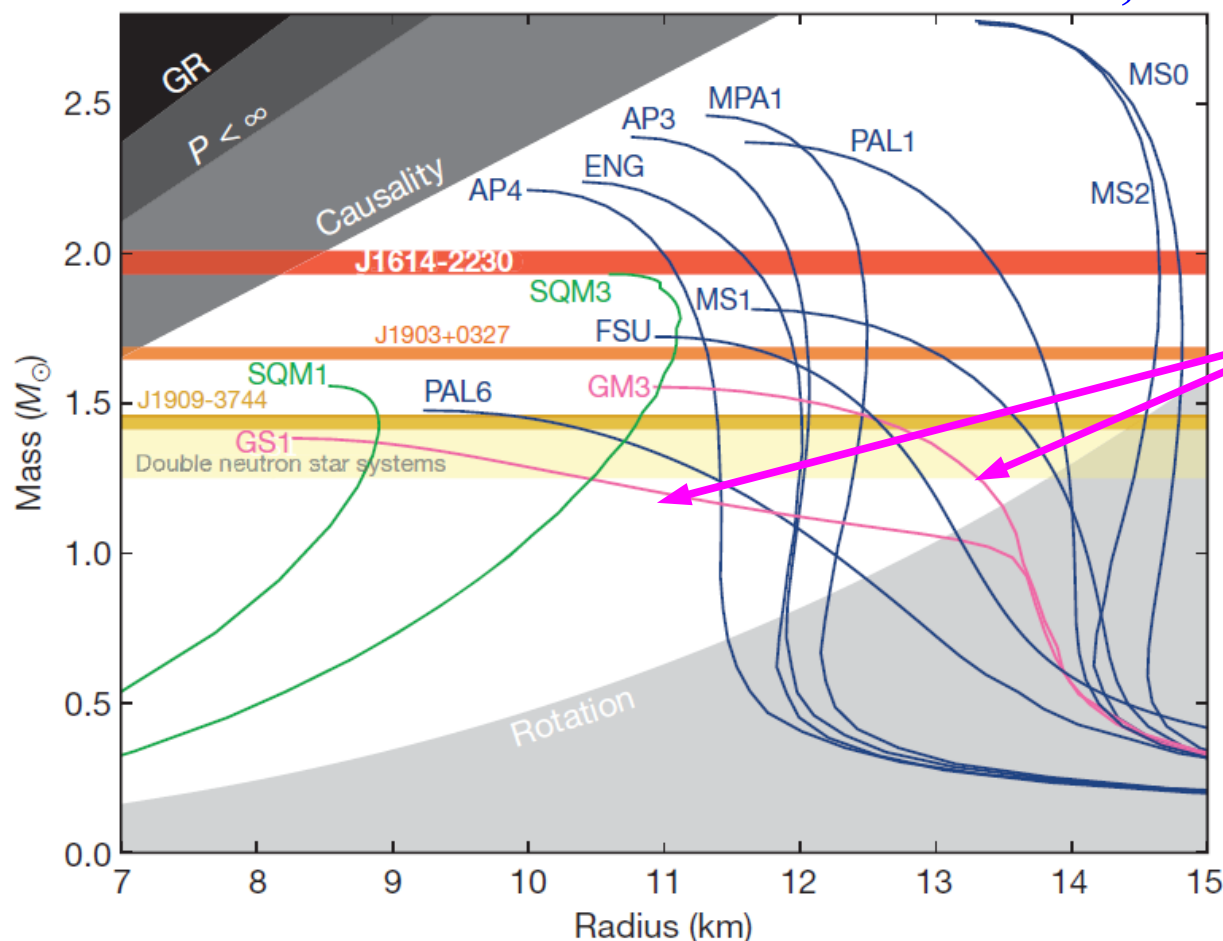


TOV eq.



$1.97 \pm 0.04 M_{\odot}$ Neutron Star

Demorest et al., *Nature* 467 (2010) 1081 (Oct.28, 2010).



**EOS with
Strange Hadrons**

signature. We calculate the pulsar mass to be $(1.97 \pm 0.04)M_{\odot}$, which rules out almost all currently proposed²⁻⁵ hyperon or boson condensate equations of state (M_{\odot} , solar mass). Quark matter can support a star this massive only if the quarks are strongly interacting and are therefore not 'free' quarks¹².

Hyperons in Dense Matter

- **Hyperons are HOT now !**
 - **What makes NS matter core ? Nucleons ? Quarks ? Hyperons ?**
 - **How can we suppress hyperon appearance in NS ?
or How can hyperonic matter be so stiff ?
or Which inter-quark interaction supports $1.97 M_{\odot}$ NS ?**

*We stick to hyperonic matter (rather than quark matter),
and discuss possible mechanism
to stiffen the EOS at high density.*

*Dense Nuclear Matter EOS
with Hyperon Admixture*

Theories/Models for Nuclear Matter EOS

■ Ab initio Approaches to Nuclear Matter

→ LQCD, Variational, GFMC, BHF(G-Matrix), DBHF, ...

- LQCD-MC: Not (yet) applicable to cold dense matter, $A \leq 4$
SC-LQCD: Nuclear matter does not bound

- Variational, BHF: Need phen. 3-body repulsion to reproduce saturation point.

- GFMC: Limited to be $A \leq 12$.

- DBHF: Good, but E/A is not enough. Not yet extensively investigated.

→ Not easy to handle, Not yet satisfactory for phen. purposes

■ Mean Field Models (~ Nuclear Density Functional approach)

- Skyrme Hartree-Fock(-Bogoliubov)

- ◆ Nuclear Mass is very well explained (HFB, Total B.E. $\Delta E \sim 0.6$ MeV)
- ◆ Causality is violated at very high densities.

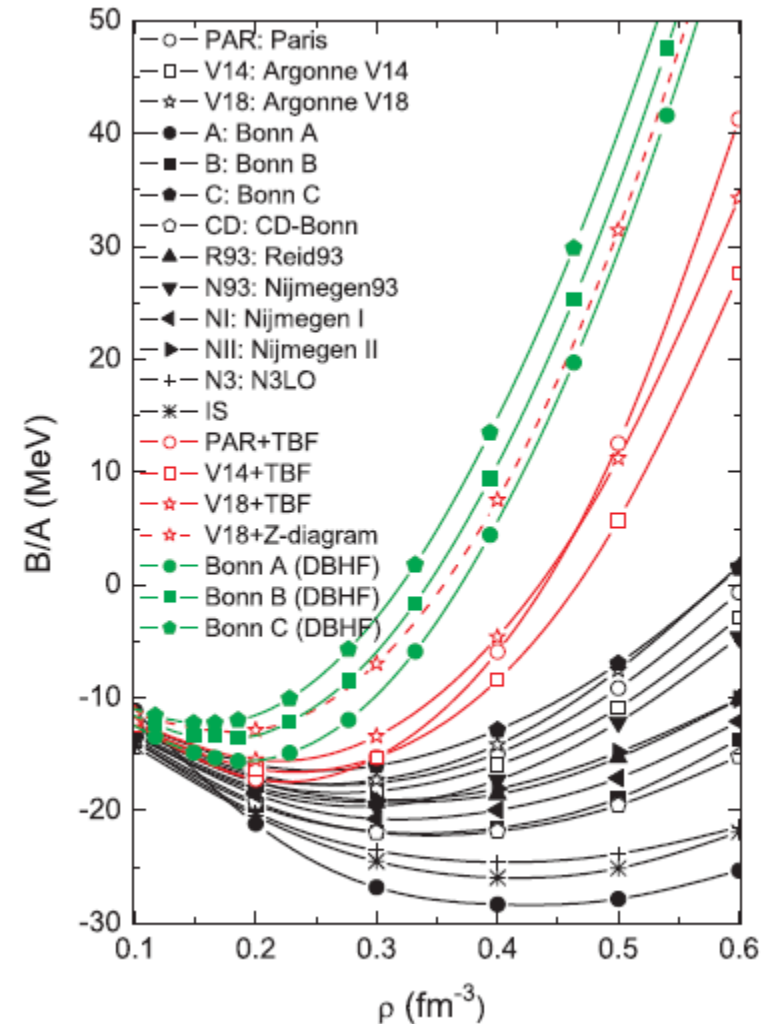
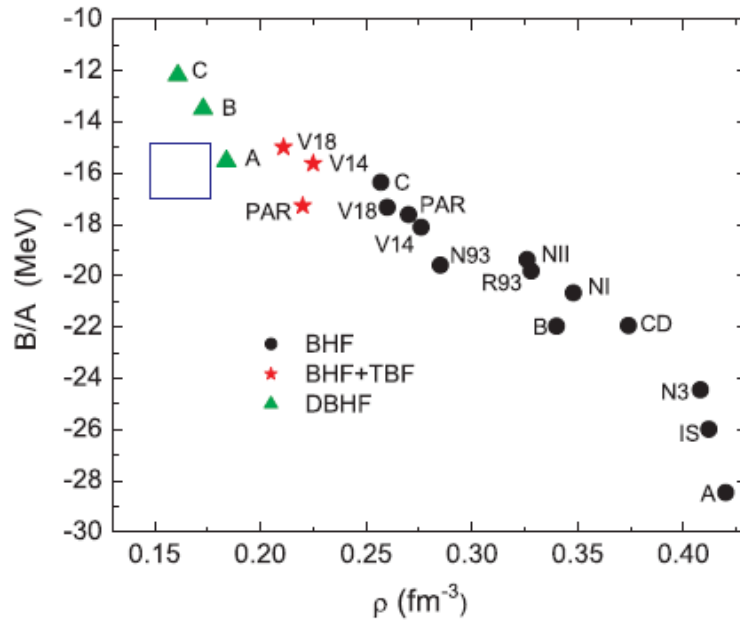
- Relativistic Mean Field

- ◆ Relativistic, Meson-Baryon coupling, Meson self-energies
- ◆ Successful in describing pA scattering (Dirac Phenomenology)

Bruckner-Hartree-Fock

Self-consistent treatment of Effective interaction (G-matrix) in the Bruckner Theory and Single particle energy from G-matrix

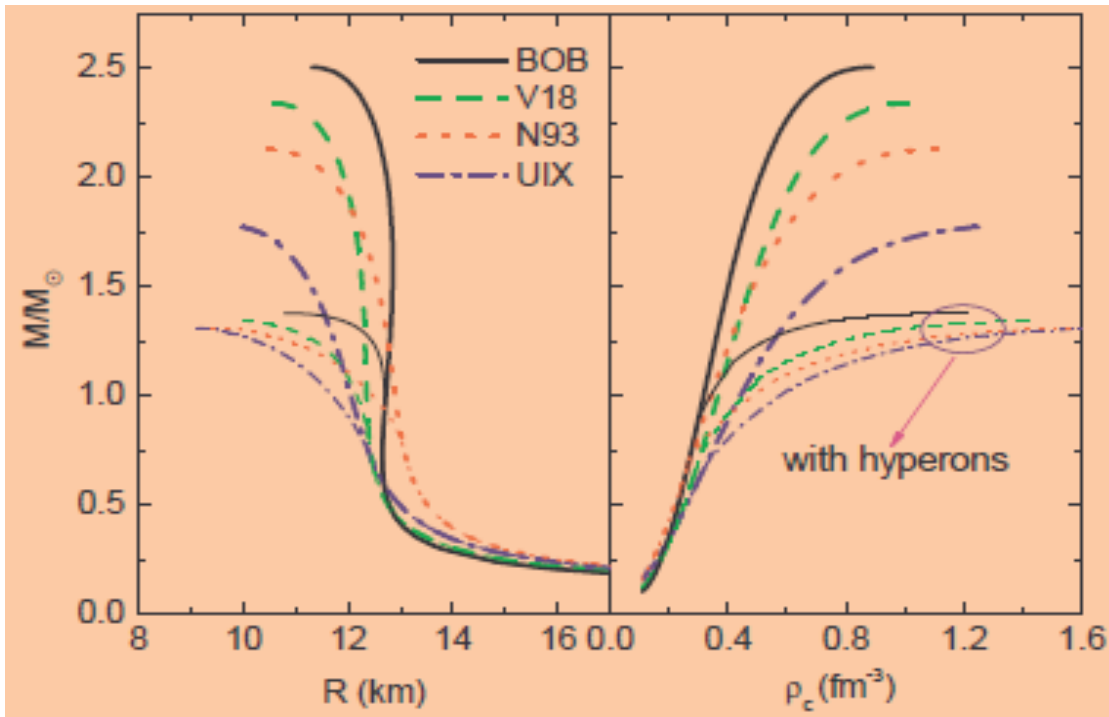
- Need 3-body force to reproduce saturation point.
 - FY type 2 π exchange + phen. or Z-diagram



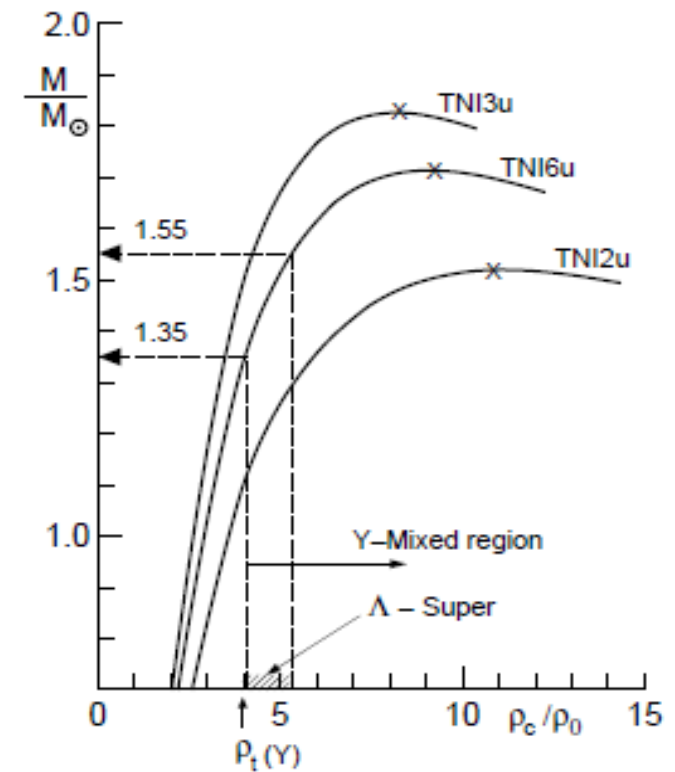
Z.H.Li, U. Lombardo, H.-J. Schulze, W. Zuo, L. W. Chen, H. R. Ma, PRC74('06)047304.

Bruckner-Hartree-Fock theory with Hyperons

- Microscopic G-matrix calculation with realistic NN, YN potential and microscopic (or phen.) 3N force (or 3B force).
 - Interaction dep. (V18, N93, ...) is large → Need finite nuclear info.
E.Hiyama, T.Motoba, Y.Yamamoto, M.Kamimura / M.Tamura et al.
 - NS collapses with hyperons w/o 3BF.



*H.J.Schulze, A.Polls, A.Ramos, I.Vidana,
PRC73('06),058801.*



*S. Nishizaki, T. Takatsuka,
Y. Yamamoto, PTP108('02)703.*

Relativistic Mean Field

Effective Lagrangian of Baryons and Mesons + Mean Field App.

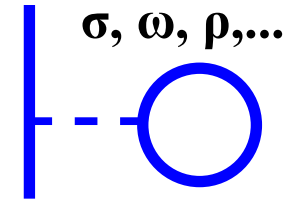
B.D.Serot, J.D.Walecka, Adv.Nucl.Phys.16 ('86), 1

$$L = L_B^{\text{free}} + L_M^{\text{free}} + L_{BM} + L_M^{\text{Int}}$$

$$L_M^{\text{Int}} = -U_\sigma(\sigma) + \frac{1}{4}c_\omega(\omega_\mu\omega^\mu)^2 + \dots$$

$$L_{BM} = -\sum_{B,S} g_{BS} \bar{\Psi}_B \varphi_S \Psi_B - \sum_{B,V} g_{BV} \bar{\Psi}_B \gamma^\mu V_\mu \Psi_B$$

$$L_B^{\text{free}} = \bar{\Psi}_B (i \gamma^\mu \partial_\mu - M_B) \Psi_B, \quad L_M^{\text{free}} = \sum_S \left[\frac{1}{2} \partial^\mu \varphi_S \partial_\mu \varphi_S - \frac{1}{2} m_S^2 \varphi_S^2 \right] + \sum_V \left[-\frac{1}{4} V_{\mu\nu} V^{\mu\nu} + \frac{1}{2} V_\mu V^\mu \right]$$



- **Baryons and Mesons: B=N, Λ, Σ, Ξ, ..., S=σ, ζ, ..., V=ω, ρ, φ, ...**

- **Based on Dirac phenomenology & Dirac Bruckner-Hatree-Fock**

E.D. Cooper, S. Hama, B.C. Clark, R.L. Mercer, PRC47('93),297

R. Brockmann, R. Machleidt, PRC42('90),1965

- **Large scalar (att.) and vector (repl.) → Large spin-orbit pot.
Relativistic Kinematics → Effective 3-body repulsion**

- **Non-linear terms of mesons → Bare 3-body and 4-body force**

Boguta, Bodmer ('77), NL1:Reinhardt, Rufa, Maruhn, Greiner, Friedrich ('86), NL3:

Lalazissis, Konig, Ring ('97), TM1 and TM2: Sugahara, Toki ('94), Brockmann, Toki ('92)

RMF is a phenomenological MODEL !

- **Baryon one-loop approximation (Hartree approximation) makes RMF a phenomenological model.**
 - **We need DATA and AB INITIO results.**
 - **Saturation point (ρ_0 and $E/A(\rho_0)$) from mass formula**
 - **Nuclear binding energies**
 - **U_v and U_s from DBHF results**
 - **$P(\rho_B)$ from heavy-ion data**
 - **Λ separation energy from single Λ hypernuclear data**
 - **$\Lambda\Lambda$ bond energy from double Λ hypernuclear data**
 - **Σ atomic shift**
 - **Σ and Ξ potential depth from quasi-free production data**
 - ***Pure neutron matter EOS from ab initio calculations (not used here)***

RMF models

■ Variety of the RMF models

→ MB couplings, meson masses, meson self-energies

- σN , ωN , ρN couplings are well determined
→ almost no model deps. in Sym. N.M. at low ρ

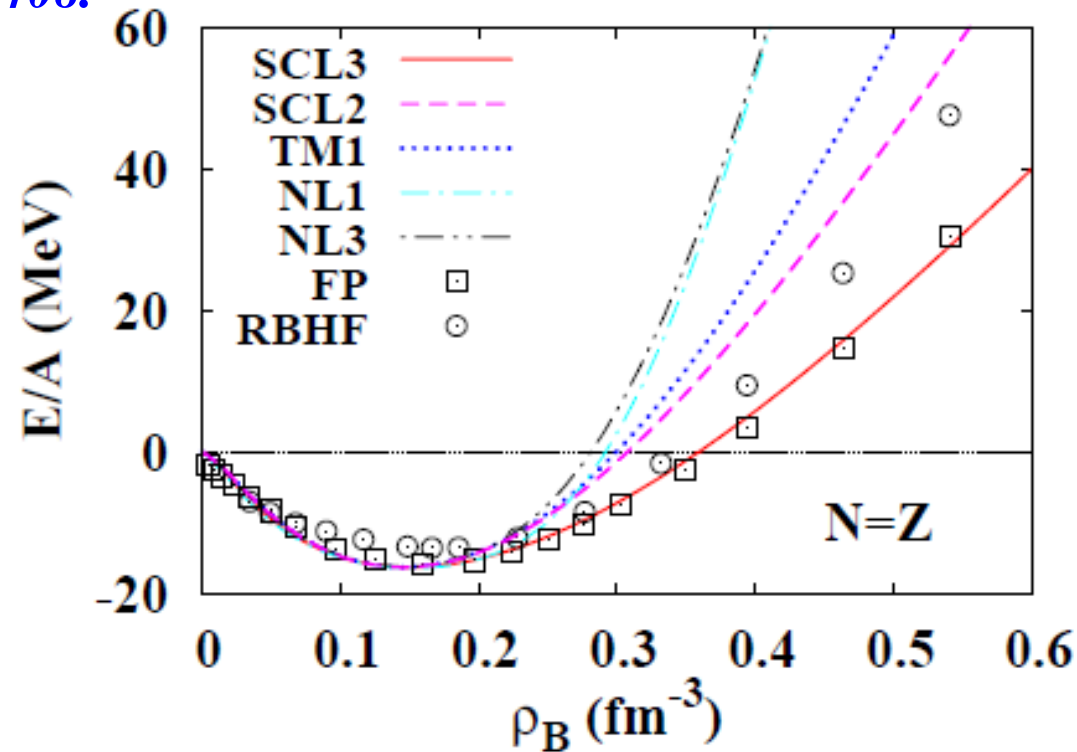
- ω^4 term is introduced to simulate DBHF results of vector pot.

*TM1&2: Y. Sugahara, H. Toki, NPA579('94)557;
R. Brockmann, H. Toki, PRL68('92)3408.*

- σ^3 and σ^4 terms are introduced to soften EOS at ρ_0 .

*J. Boguta, A.R. Bodmer NPA292('77)413,
NL1: P.-G. Reinhardt, M. Rufa, J. Maruhn,
W. Greiner, J. Friedrich, ZPA323('86)13.
NL3: G.A. Lalazissis, J. Konig, P. Ring,
PRC55('97)540.*

→ Large differences are found at high ρ



K. Tsubakihara, H. Maekawa, H. Matsumiya, AO, PRC81('10)065206.

Choice of $U_\sigma(\sigma)$

■ Logarithmic σ potential

K. Tsubakihara, AO, PTP 117 (2007) 903.

K. Tsubakihara, H. Maekawa, H. Matsumiya, AO, PRC81('10) 065206.

$$U_\sigma = -\frac{a_\sigma}{2} \log \det(M M^\dagger) + \frac{b_\sigma}{2} \text{tr}(M M^\dagger) \\ - d_\sigma (\det M + \det M^\dagger) - \frac{c_\sigma}{4} \text{tr}(M + M^\dagger)$$

$$M = \text{Meson matrix} = [\lambda^a (\sigma^a + i \pi^a)] / \sqrt{2}$$

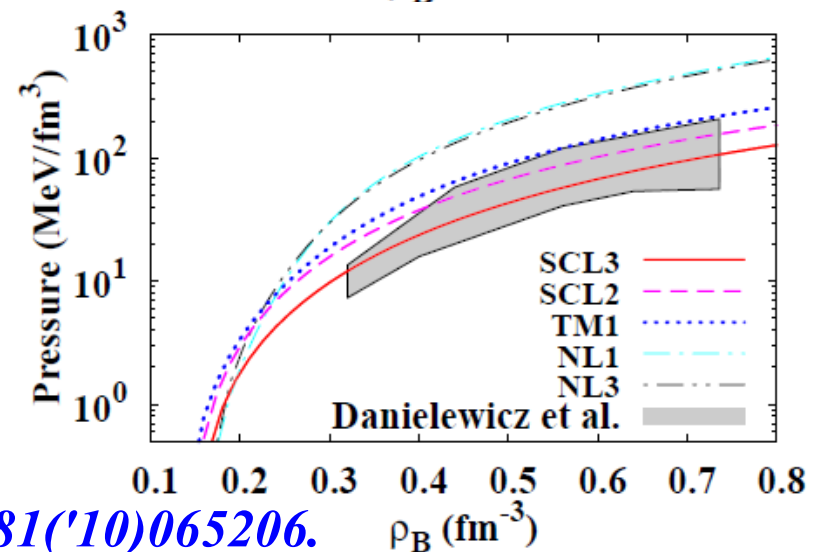
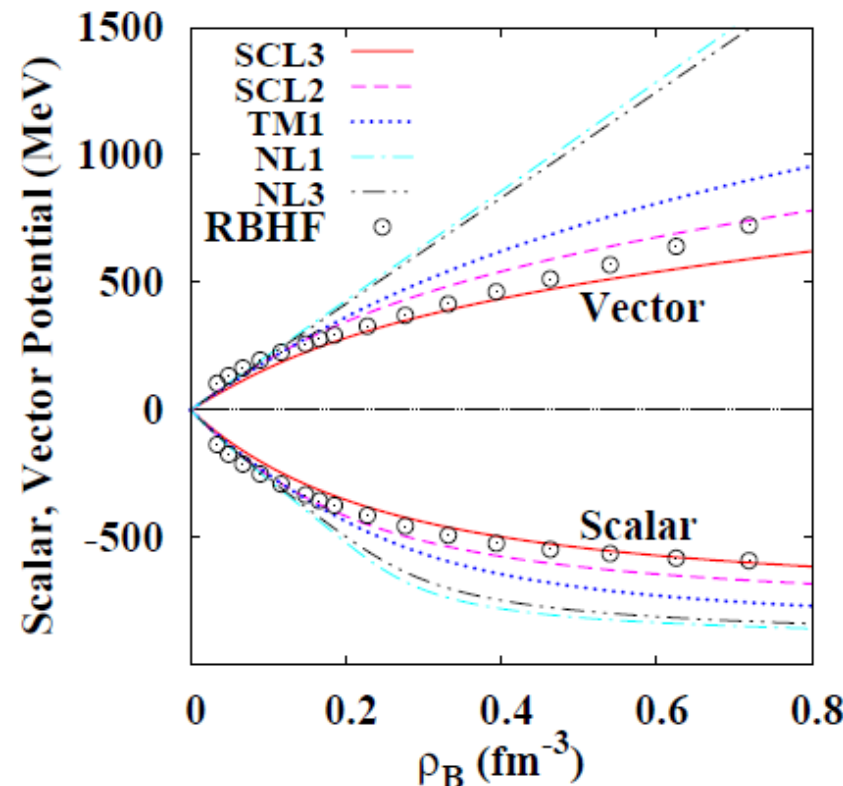
- **No chiral collapse, No instability at large σ**
- **Log σ term appears from coupling to dilaton (scale anomaly)**
E. K. Heide, S. Rudaz, and P. J. Ellis, NPA571('94)713
or from strong coupling limit of lattice QCD
N. Kawamoto, J. Smit, NPB 190 ('81)100.
- **det σ term (KMT interaction) represents $U(1)_A$ anomaly**
M. Kobayashi, T. Maskawa, PTP44('70)1422; M. Kobayashi, H. Kondo, T. Maskawa, PTP 45('71)1955; G. 't Hooft, PRD 14 ('76)3432.

Vector potential in RMF

- Vector potential from ω dominates at high density !

$$U_v(\rho_B) = g_\omega \omega \sim \frac{g_\omega^2}{m_\omega^2} \rho_B$$

- Dirac-Bruckner-Hartree-Fock shows suppressed vector potential at high ρ_B .
R. Brockmann, R. Machleidt, PRC42('90)1965.
- Collective flow in heavy-ion collisions suggests pressure at high ρ_B .
P. Danielewicz, R. Lacey, W. G. Lynch, Science298('02)1592.
- Self-interaction of $\omega \sim c_\omega (\omega_\mu \omega^\mu)^2$
→ DBHF results & Heavy-ion data



K. Tsubakihara, H. Maekawa, H. Matsumiya, AO, PRC81('10)065206.

RMF with Hyperons (Single Λ hypernuclei)

■ RMF for Λ hypernuclei

$x \sim 1/3$: R. Brockmann, W. Weise, PLB69('77)167; J. Boguta and S. Bohrman, PLB102('81)93.

$x \sim 2/3$: N. K. Glendenning, PRC23('81)2757, PLB114('82)392;

Tensor: Y. Sugahara, H. Toki, PTP92('94)803; H. Shen, F. Yang, H. Toki, PTP115('06)325;

J. Mares, B. K. Jennings, PRC49('94)2472.

ρ -dep. coupling: H. Lenske, Lect. Notes Phys. 641('04)147; C. M. Keil, F. Hofmann, H. Lenske, PRC 61('00)064309.

SU(3) or SU(6) (ζ, φ): J. Schaffner, C. B. Dover, A. Gal, C. Greiner, H. Stoecker, PRL71('93)1328; Schaffner et al., Ann.Phys.235('94)35; J. Schaffner, I. N. Mishustin, PRC 53('96)1416.

Chiral SU(3) RMF: K. Tsubakihara, H. Maekawa, H. Matsumiya, AO, PRC81('10)065206.

- Sep. E. of Λ is well fitted by $U_{\Lambda} \sim -30 \text{ MeV} \sim 2/3 U_N$

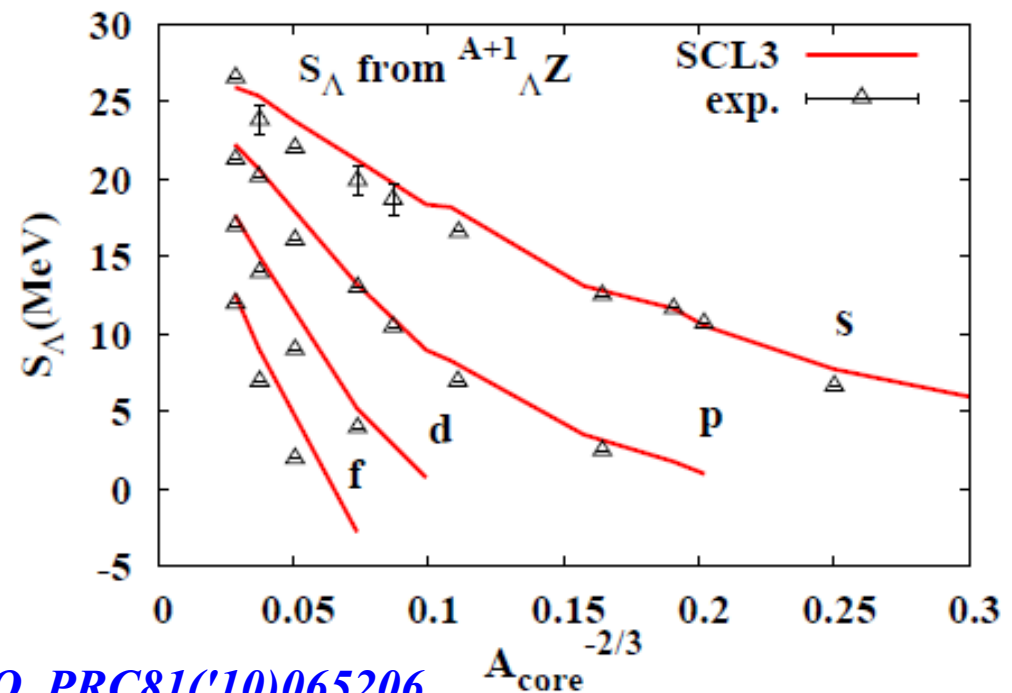
- Coupling with mesons

$$x_M = g_{M\Lambda} / g_{MN}$$

quark counting: $x_{\sigma} \sim 2/3$

π exchanges: $x_{\sigma} \sim 1/3$

→ Which is true ?



K. Tsubakihara, H. Maekawa, H. Matsumiya, AO, PRC81('10)065206.

RMF with Hyperons (Double Λ hypernuclei)

■ Nagara event $\Delta B_{\Lambda\Lambda} \sim 1.0$ MeV (weakly attractive)

● TM & NL-SH based RMF

H. Shen, F. Yang, H. Toki, PTP115('06)325.

Model 1: $x_\sigma = 0.621$, $x_\omega = 2/3$ (no ζ , φ)

Model 2: $R_\zeta = g_{\zeta\Lambda} / g_{\sigma N} = 0.56-0.57$, $R_\varphi = g_{\varphi\Lambda} / g_{\omega N} = -\sqrt{2/3}$

● Chiral SU(3) RMF

K. Tsubakihara, H. Maekawa, H. Matsumiya, AO, PRC81('10)065206.

SU(3)f for vector coupling

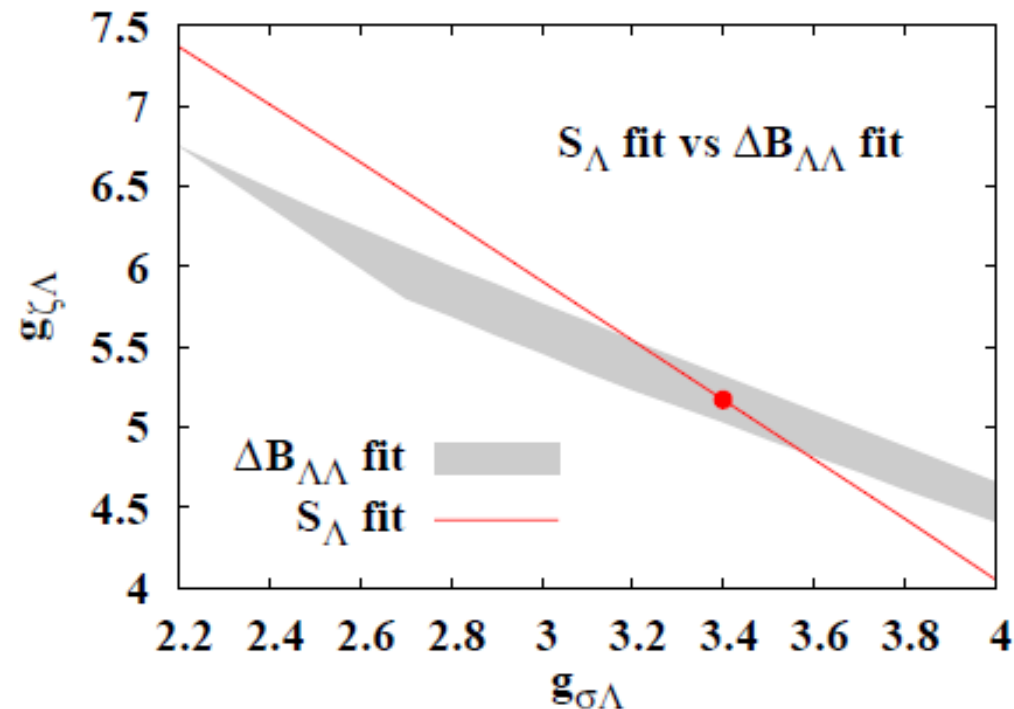
$x_\omega = 0.64$, $R_\varphi = 0.504$

Det. (KMT) int. mixes σ and ζ

M. Kobayashi, T. Maskawa, PTP44('70)1422;

G. 't Hooft, PRD14('76)3432.

→ $x_\sigma = 0.335$, $R_\zeta = 0.509$



Hyperon Composition in Dense Matter

■ Hyperon start to emerge at $(2-3)\rho_0$ in Neutron Star Matter !

■ Hyperon composition in NS is sensitive to Hyperon potential.

● $U_\Lambda \sim -30$ MeV: Well-known

● $U_\Xi \sim -(12-15)$ MeV

(K^-, K^+) reaction, twin hypernuclei

P. Khaustov et al. (E885), PRC61('00)054603;

S. Aoki et al., PLB355('95)45.

● $U_\Sigma \sim -30$ MeV (Old conjecture)

→ Σ^- appears prior to Λ

● $U_\Sigma > 0$ (repulsive) → No Σ in NS

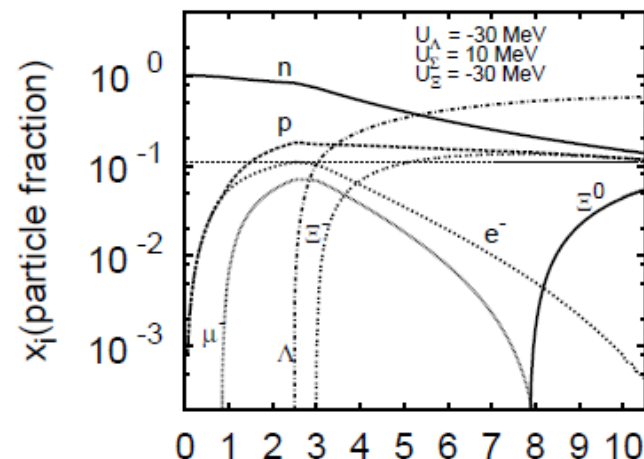
Σ atom (phen. fit), QF prod.

S. Balberg, A. Gal, NPA625('97)435;

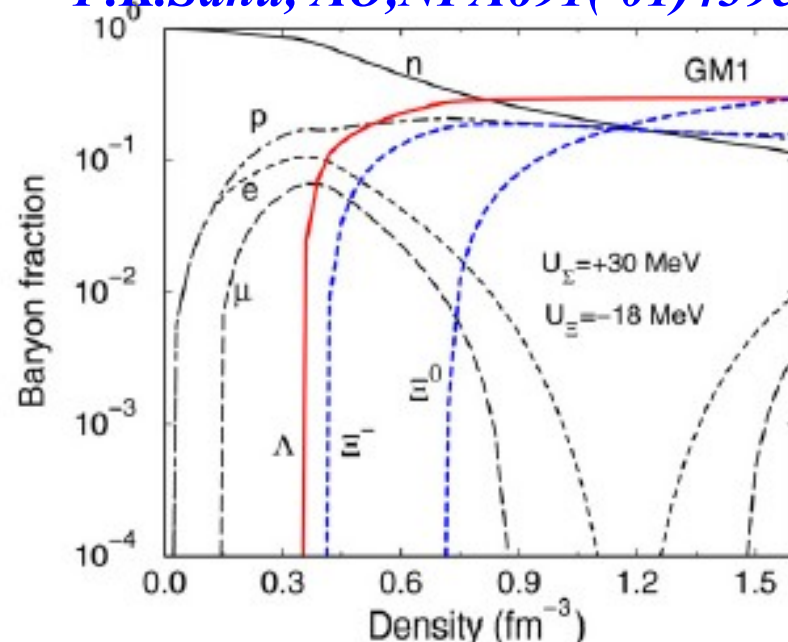
H. Noumi et al., PRL89('02)072301;

T. Harada, Y. Hirabayashi, NPA759('05)143;

M. Kohno et al. PRC74('06)064613.



P.K.Sahu, AO, NPA691('01)439c



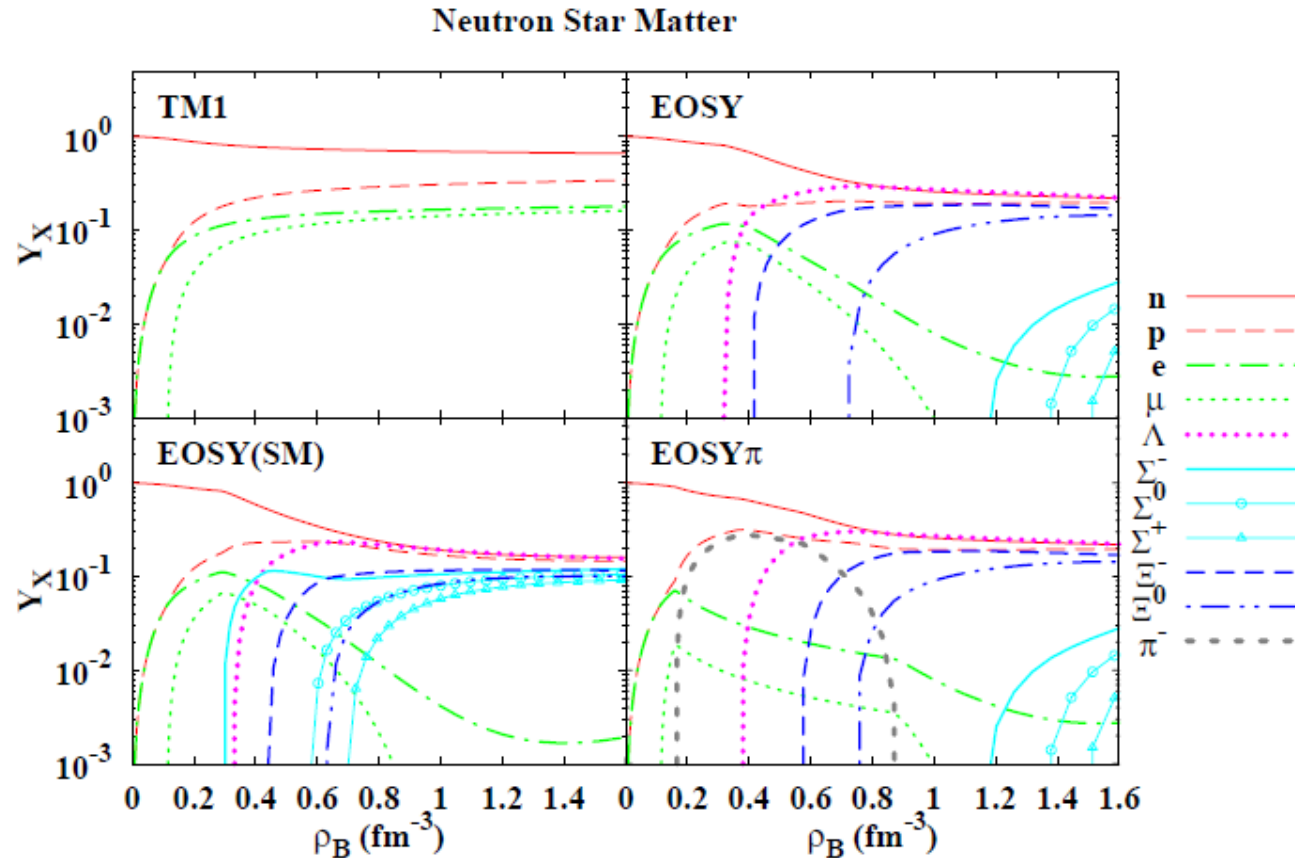
J. Schaffner-Bielich, NPA804('08)309.

Hyperon Composition in Dense Matter

■ Comparison of Hyperon Composition

- $U_{\Sigma} = -30$ MeV, $U_{\Xi} = -28$ MeV \rightarrow SU(3) sym. matter at $\rho_B \sim 10 \rho_0$
Schaffner, Mishustin ('94)
- $U_{\Sigma} = +30$ MeV, $U_{\Xi} = -15$ MeV \rightarrow Σ baryons are strongly suppressed.
C. Ishizuka, AO, K. Tsubakihara, K. Sumiyoshi, S. Yamada, JPG35('08)085201.

\rightarrow Does Σ play no role in NS ?



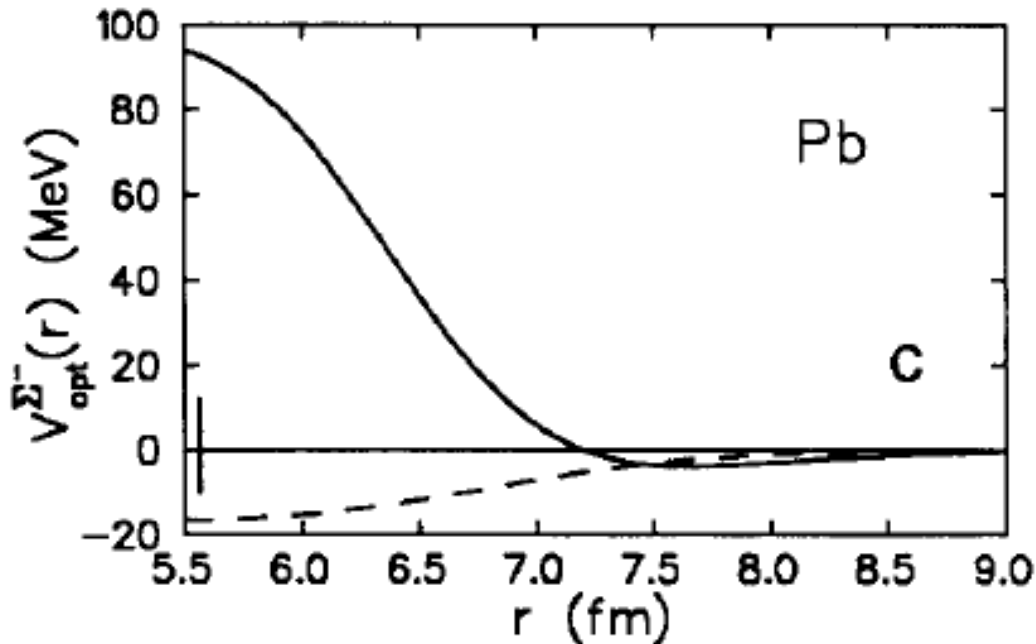
Σ^- atom data

- Σ^- atom data suggested repulsion in the interior of nuclei !

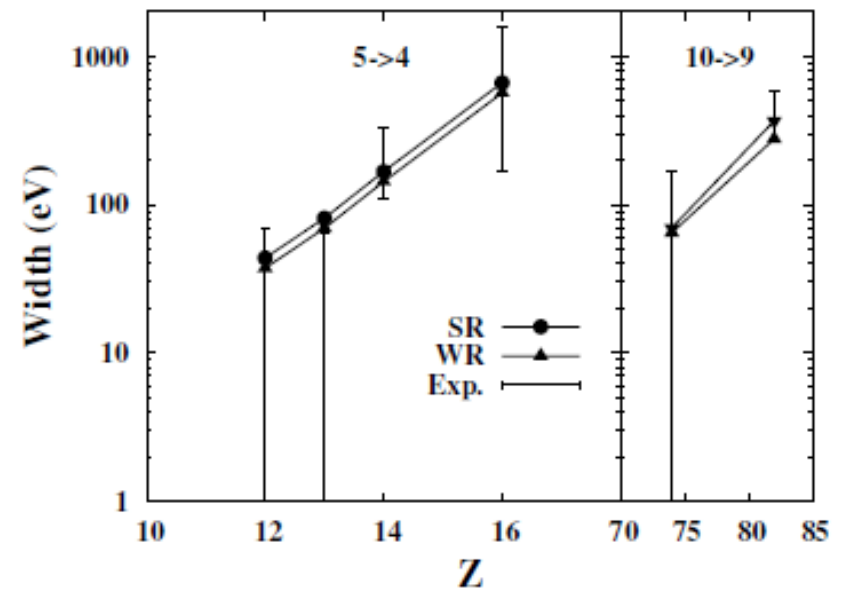
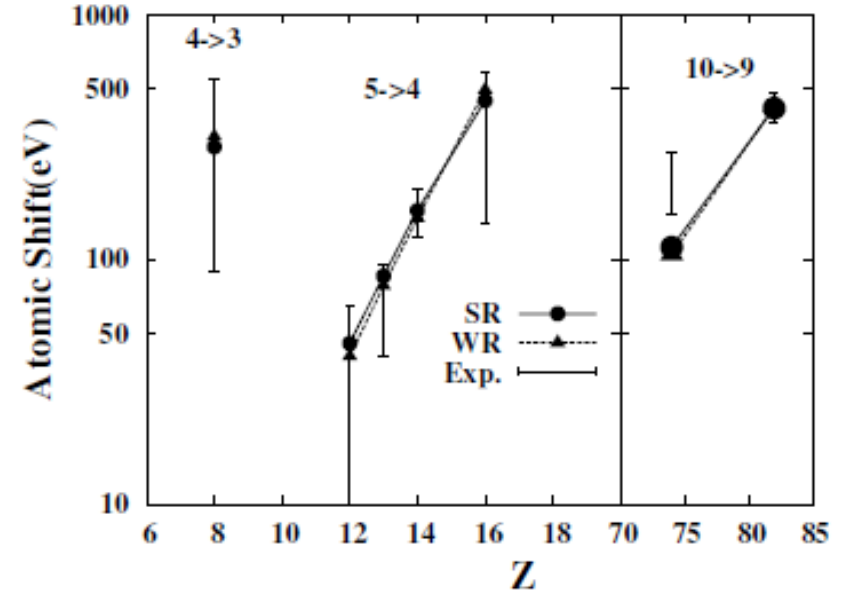
C.J.Batty, E.Friedman, A.Gal, PLB335('94)273

Batty's DD potential is very repulsive inside nuclei.

→ No Σ baryon in dense matter.



J.Mares, E.Friedman, A.Gal, B.K.Jennings, NPA594('95)311.



K.Tsubakihara, H.Maekawa, AO, EPJA33('07)295.

Σ^- atom in RMF

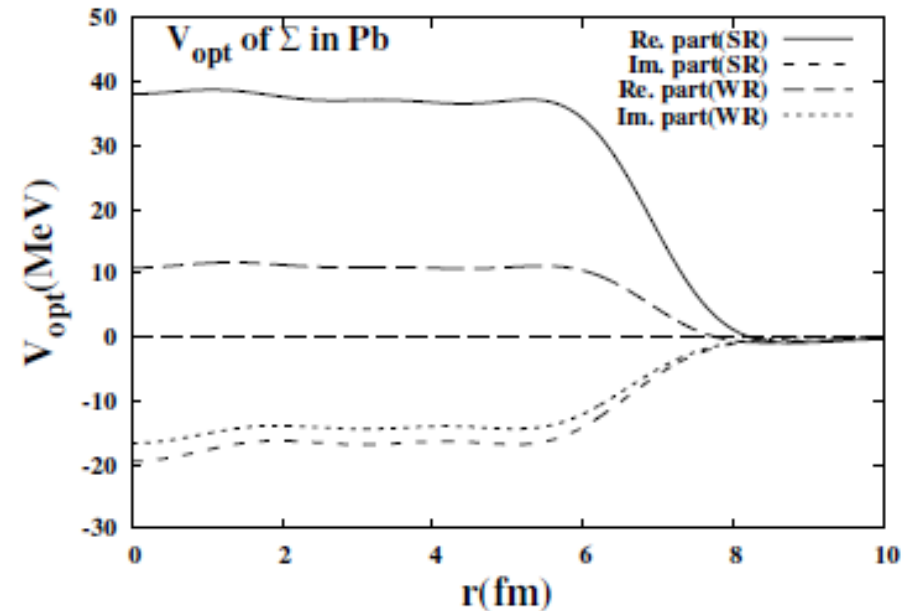
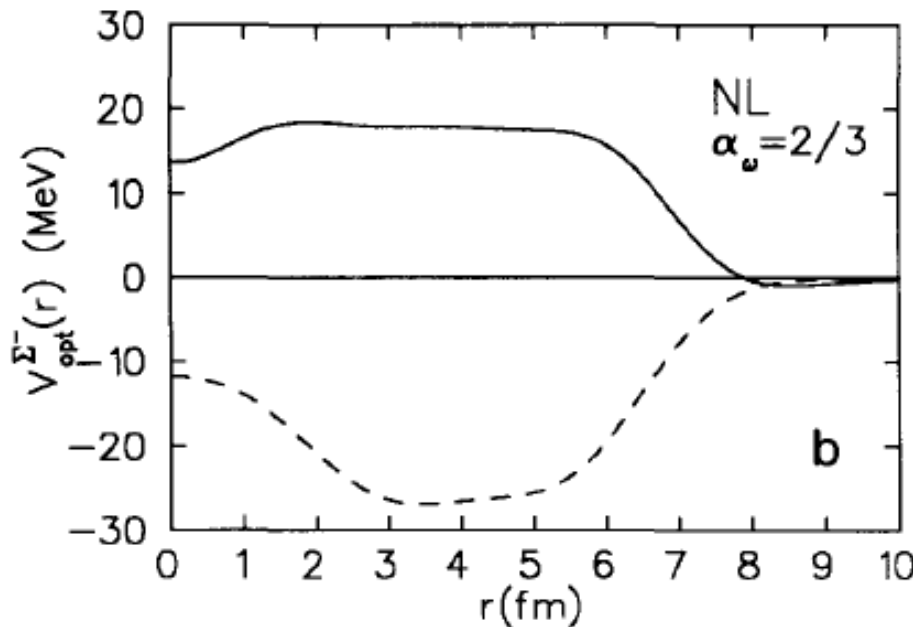
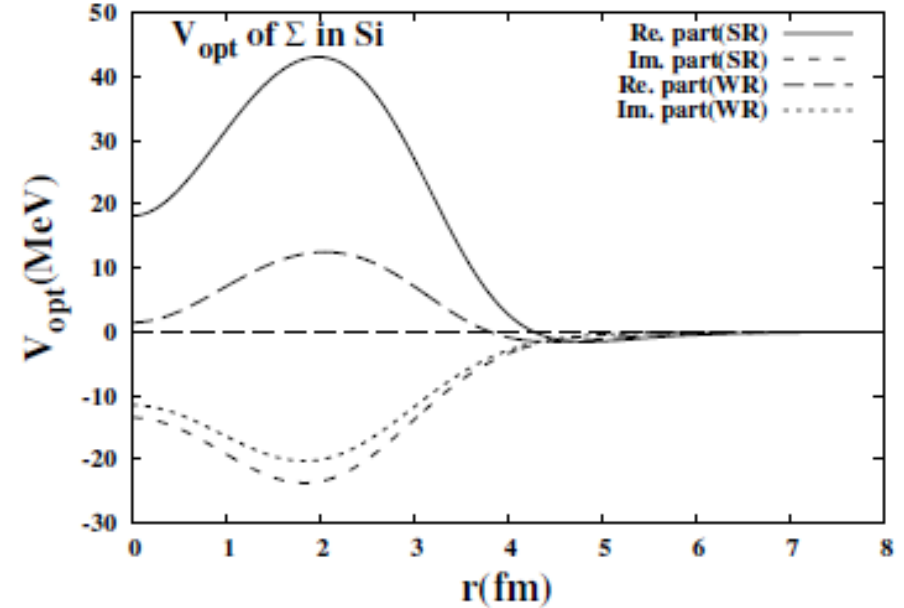
■ RMF fit of Si and Pb Σ^- atom

$$\alpha_\omega = g_{\omega\Sigma} / g_{\omega N} \sim 2/3(\text{M}), 0.69(\text{T})$$

$$\alpha_\rho = g_{\rho\Sigma} / g_{\rho N} \sim 2/3(\text{M}), 0.434(\text{T})$$

J.Mares, E.Friedman, A.Gal, B.K.Jennings, NPA594('95)311; Tsubakihara et al.('10)

- Much smaller $g_{\rho\Sigma}$ than naïve SU(3) ($g_{\rho\Sigma} / g_{\rho N} = 2$), which has been applied in some of previous works.

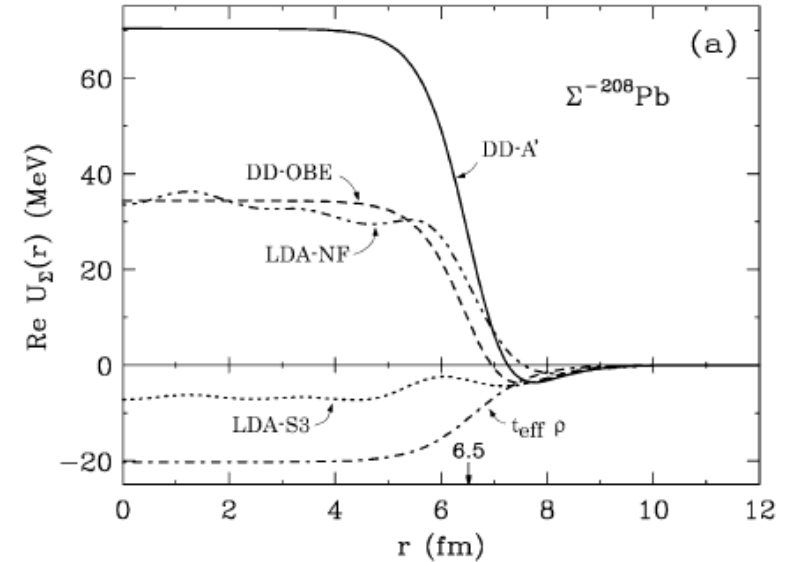


Σ atom and Neutron Star

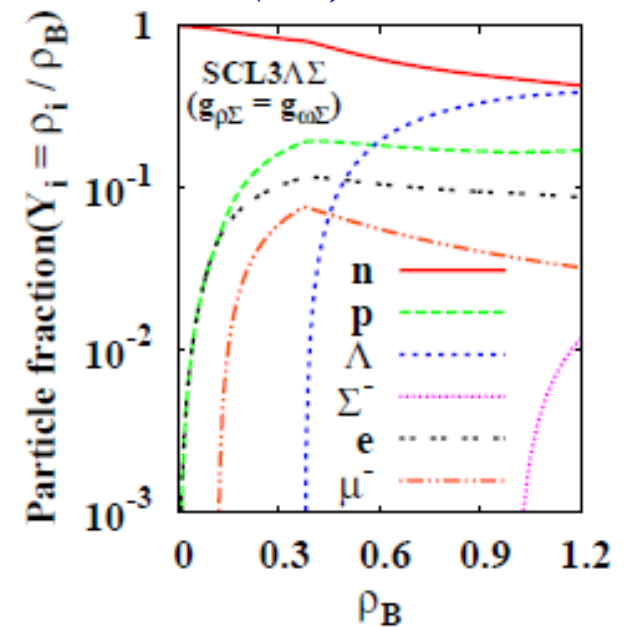
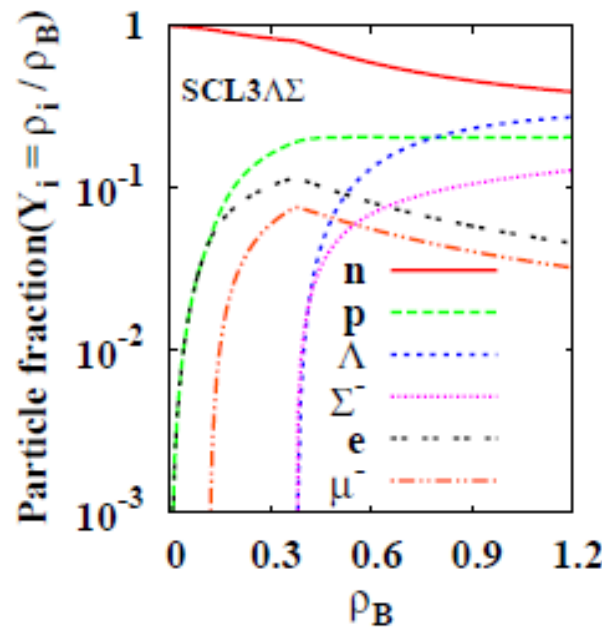
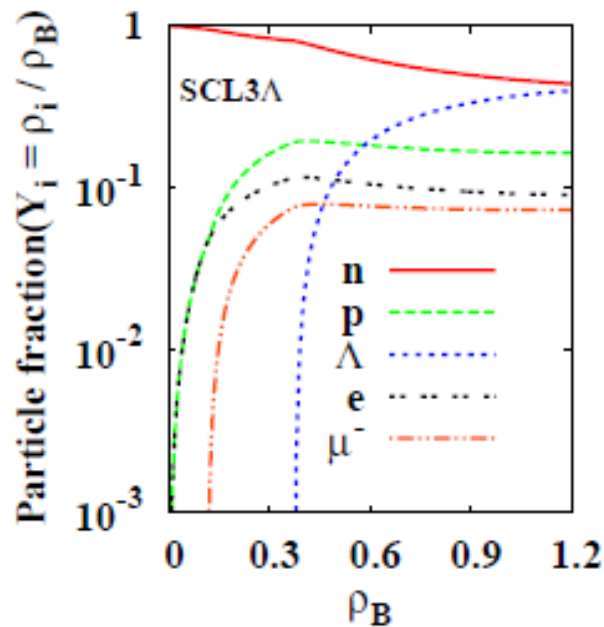
■ Σ may not feel *very* repulsive potential in neutron star....

- ρ^γ -type fit \rightarrow very repulsive
- RMF fit \rightarrow small isovector potential

\rightarrow QF prod. may support the latter.
 Σ^- would appear in NS.



*T. Harada, Y. Hirabayashi,
 NPA767('06)206*

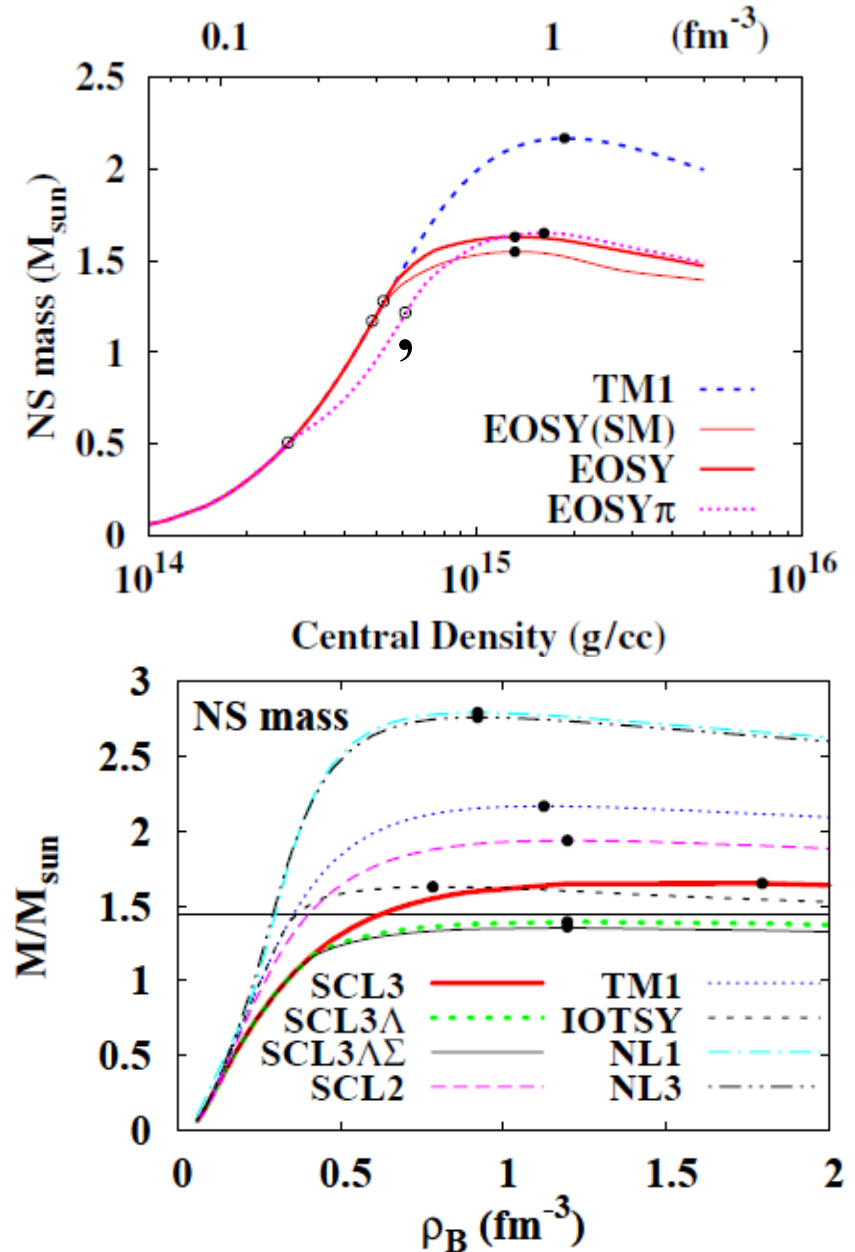


K. Tsubakihara, H. Maekawa, H. Matsumiya, AO, PRC81('10)065206.

Ohnishi @ DCEN2011, Sep.20-Oct.28, 2011, YITP, Kyoto, Japan

Neutron Star Mass

- Large fraction of hyperons softens EOS at $\rho_B > (0.3-0.4) \text{ fm}^{-3}$
 - NS star max. mass red. $\sim 1 M_{\text{sun}}$.
 - RMF generally predicts stiff EOS at high density. (Scalar attraction saturation, or Z-graph in NR view.)
 - Some of RMF with Y do not support $1.44 M_{\text{sun}}$.
- Additional Repulsion at high ρ ?
 - Vector mass mod. \rightarrow stronger repulsion at high ρ .
M. Naruki et al., PRL96('06)092301.
 - Another term such as $NN\omega\sigma$.



C. Ishizuka, AO, K. Tsubakihara, K. Sumiyoshi, S. Yamada, JPG35('08)085201.

K. Tsubakihara, H. Maekawa, H. Matsumiya, AO, PRC81('10)065206.

RMF is a phenomenological MODEL !

- **Baryon one-loop approximation (Hartree approximation) makes RMF a phenomenological model.**
 - **We need DATA and AB INITIO results.**
- ● **Saturation point (ρ_0 and $E/A(\rho_0)$) from mass formula**
- ● **Nuclear binding energies**
- ● **U_v and U_s from DBHF results**
- ● **$P(\rho_B)$ from heavy-ion data**
- ● **Λ separation energy from single Λ hypernuclear data**
- ● **$\Lambda\Lambda$ bond energy from double Λ hypernuclear data**
- ● **Σ atomic shift**
- ● **Σ and Ξ potential depth from quasi-free production data**
 - *Pure neutron matter EOS from ab initio calculations (not used here)*
- △ ● **Neutron Star Max. Mass $\sim 1.40 M_\odot$, a little smaller $1.44 M_\odot$.**

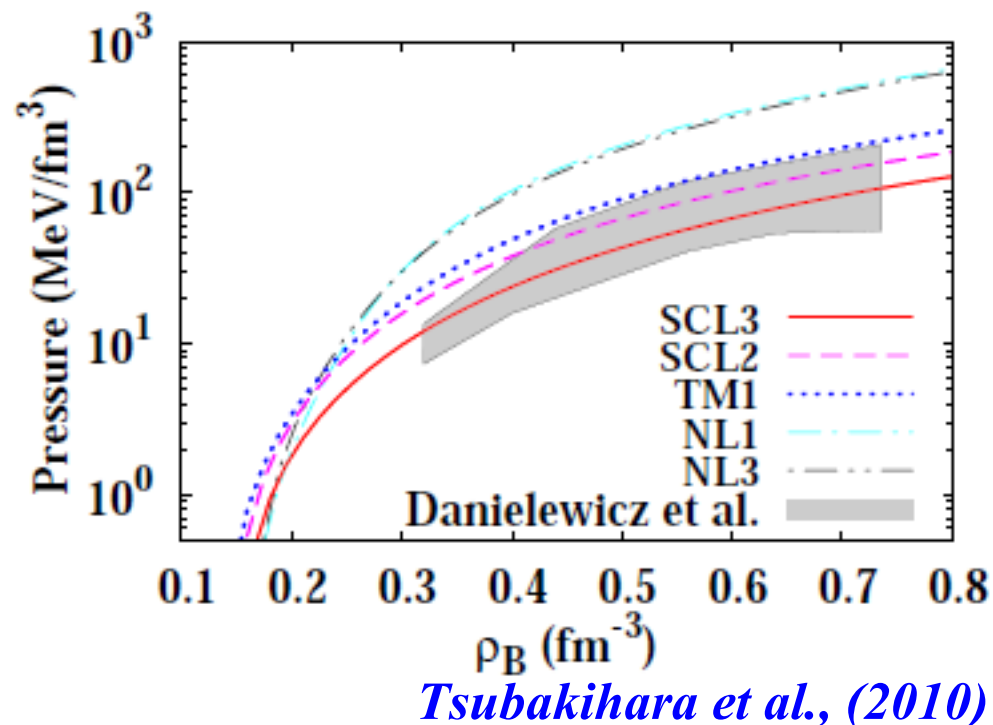
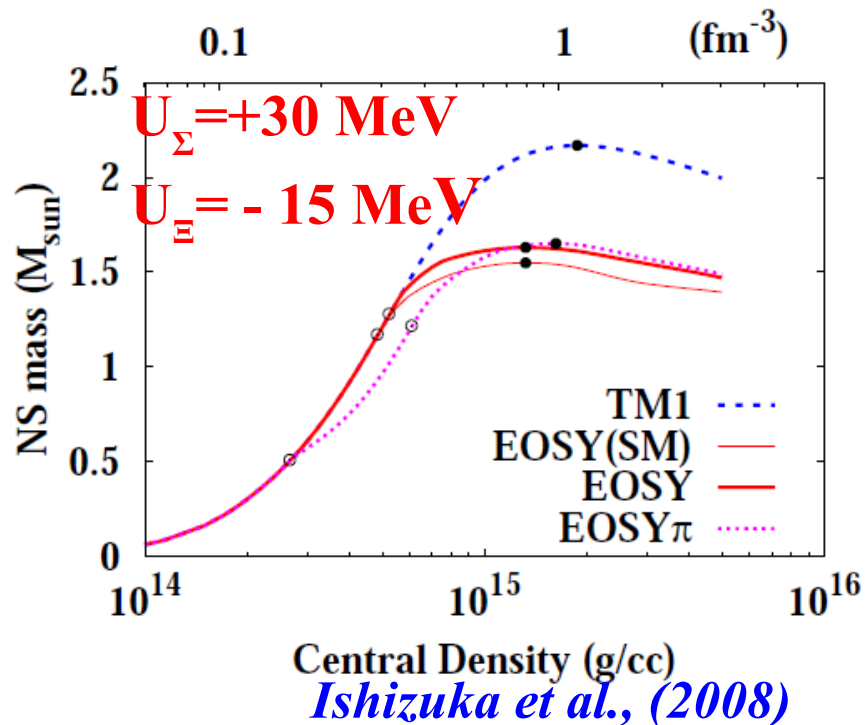
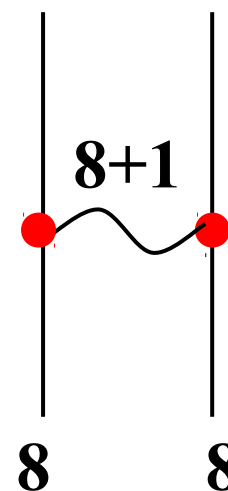
The Judgement Day, Oct. 28, 2010.

*Can hyperon survive in $1.97 M_{\odot}$
neutron star ?*

Which type of EOSs are rejected ?

Rejected Hyperonic Matter EOS

- Relativistic Mean Field model
 - GM3: Glendenning & Moszkowski (1991)(npY)
 - GS1: Glendenning & Schaffner-Bielich (1999)(npK)
- Coupling \sim Quark Counting ($g_{\omega Y}/g_{\omega N} \sim 2/3$)
- Even with rel. effects, we cannot support $1.97M_{\odot}$ as long as we respect hypernuclear & HIC data.

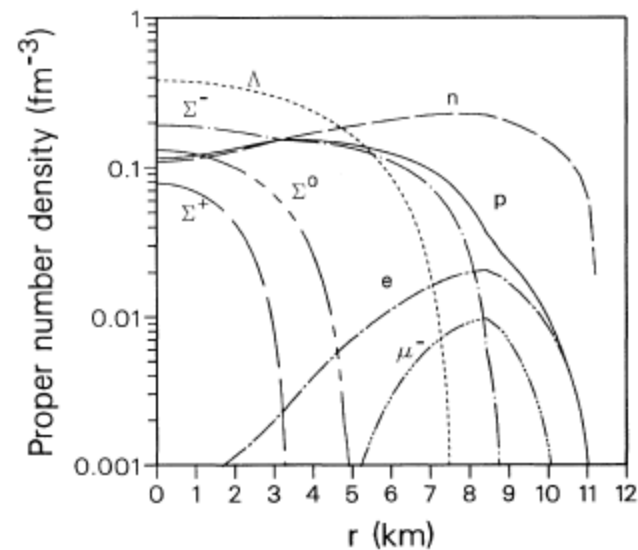
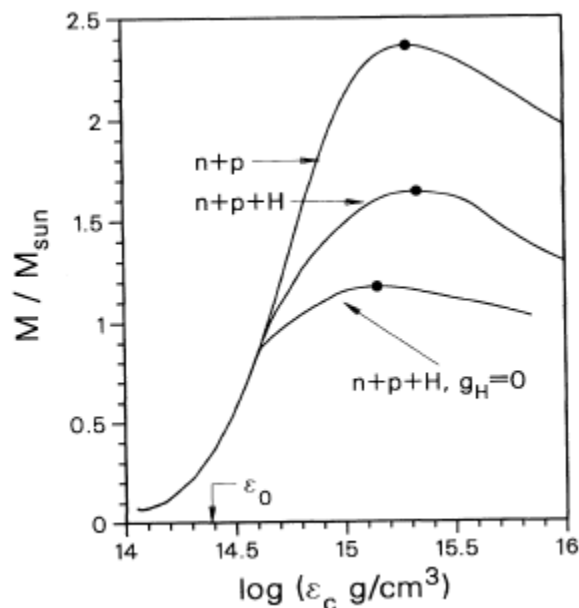
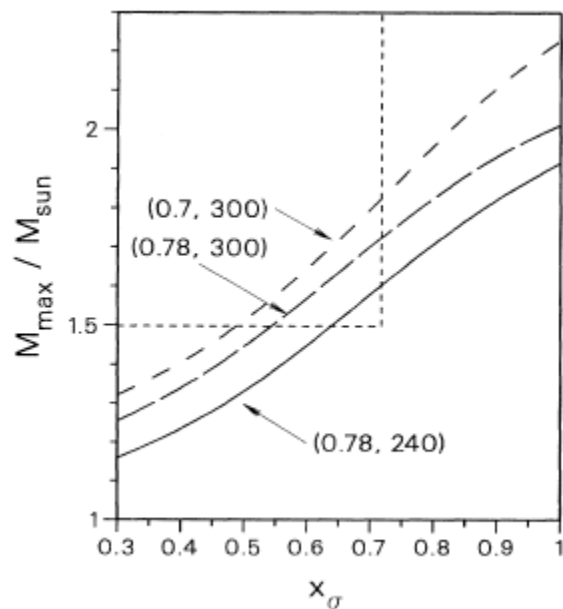


■ RMF with hyperons

- $n, p, Y, \sigma, \omega, \rho / \sigma^3, \sigma^4$
- Give $x_\sigma = g_{\sigma Y} / g_{\sigma N}$ and fix $x_\omega = g_{\omega Y} / g_{\omega N}$ to fit Λ separation energy.
- $x_\sigma = 0.6 \rightarrow m^*/m=0.7, x_\omega=0.653$
(similar to quark number counting result, $x=2/3$)
 $\rightarrow M_{\max} \sim 1.6 M_\odot$

TABLE I. Values of the hyperon-to-nucleon scalar and vector coupling that are compatible with the binding of -28 MeV for Λ hyperons in nuclear matter for two values of the nucleon (Dirac) effective mass at saturation density.

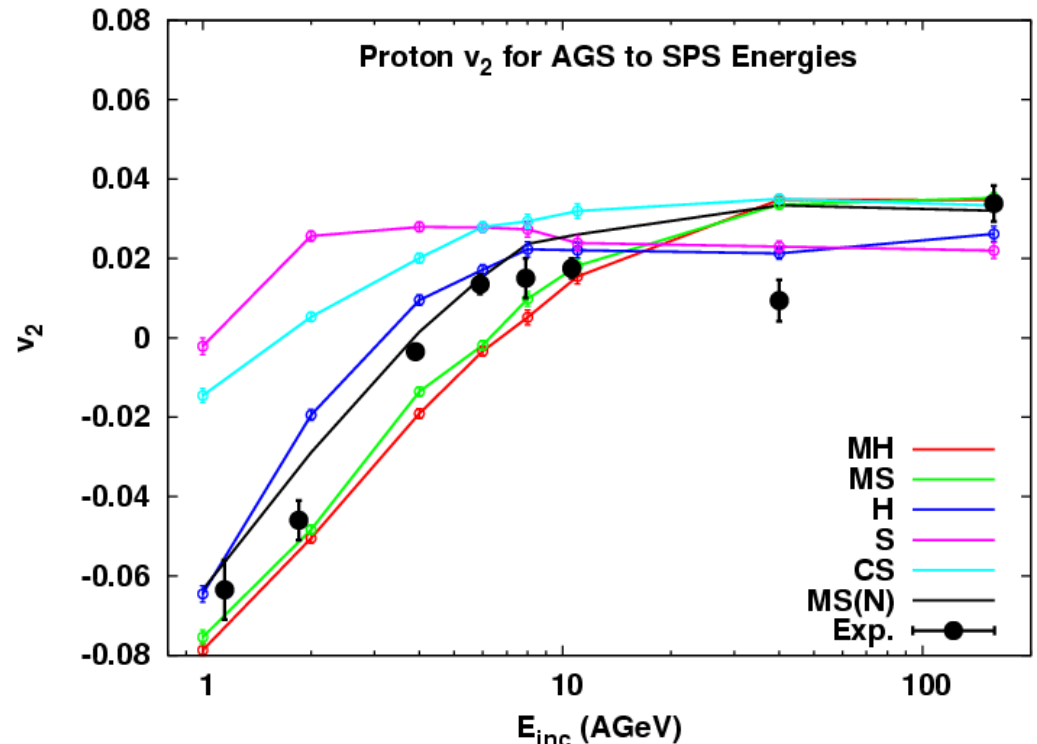
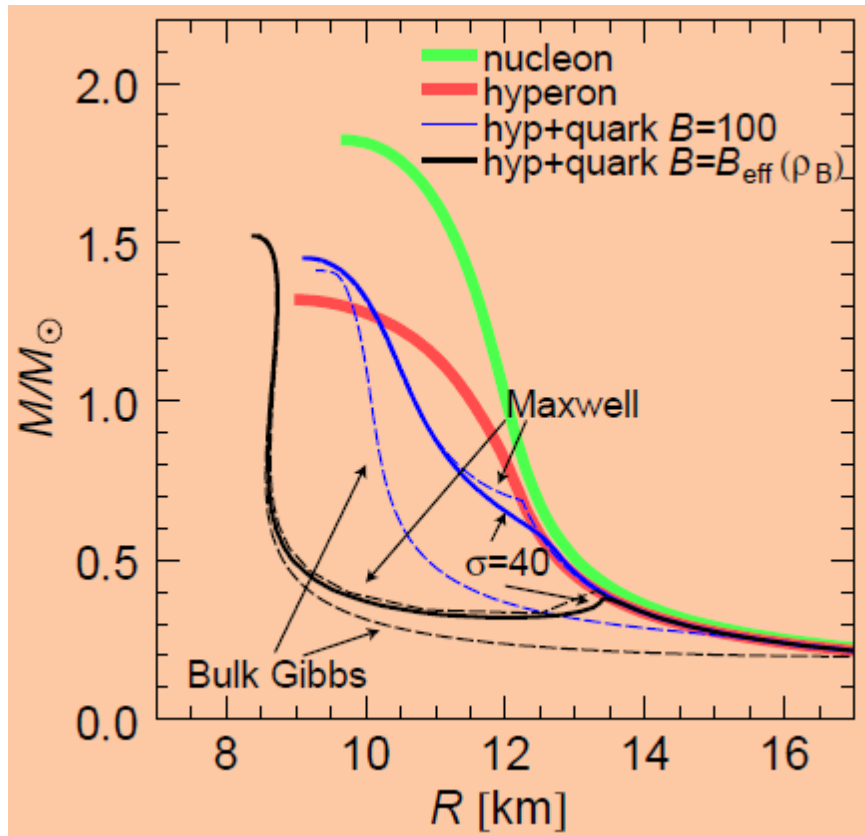
x_σ	x_ω	$m^*/m=0.7$	$m^*/m=0.78$
0.2		0.131	0.091
0.3		0.261	0.233
0.4		0.392	0.375
0.5		0.522	0.517
0.6		0.653	0.568
0.7		0.783	0.800
0.8		0.913	0.942
0.9		1.04	1.08
1		1.17	1.23



N.K.Glendenning, S.A.Moszkowski, PRL67('91)2414

How can we solve it ?

- No Hyperons, No Kaons
→ How can it be consistent with YN interaction ?
- Stiff nuclear matter EOS + transition to quark matter at small ρ_B
→ How can it be consistent with HIC data at AGS-SPS energies ?
- Three-body force for baryons, quarks, ...



M. Isse, A.O., N. Otuka, P. K. Sahu, Y. Nara, PRC72 ('05)064908

H.-J. Schulze, NFQCD10

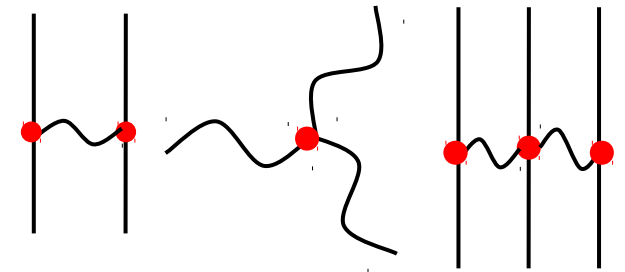
■ Three-baryon coupling term

$$L = L_B^{\text{free}} + L_M^{\text{free}} + L_{BM} + L_M^{\text{Int}} + \delta L$$

$$\delta L = -U_\sigma(\sigma) - \frac{1}{2} c_{\sigma\omega} \sigma \omega_\mu \omega^\mu - \frac{1}{4} c_{\omega\omega} (\omega_\mu \omega^\mu)^2$$

$$- \sum_B \bar{\Psi}_B \left[g_{\sigma\sigma B} \sigma^2 + g_{\sigma\omega B} \sigma \omega_\mu \gamma^\mu + g_{\omega\omega B} \omega_\mu \omega^\mu \right] \Psi_B$$

v = 3 terms



- **BBMM terms are ignored in standard RMF.**

(They can be absorbed in other terms by field re-definitions.)

R.D.Furnstahl, B.D.Serot, H.-B. Tang, NPA615 ('97)441

- **But field re-definition modifies the order of NDA.**

Naïve dimensional analysis (NDA)

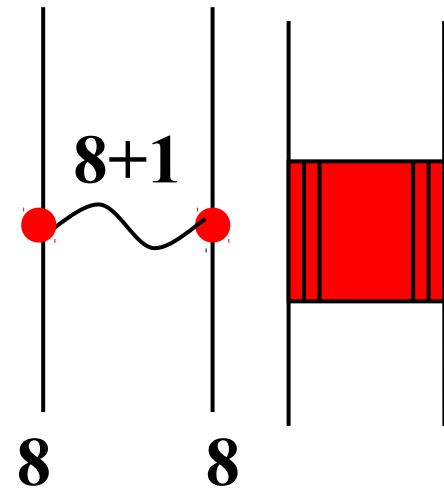
$$v = B/2 + M + d$$

(B, M, d=# of baryon and non-NG boson field, derivatives to NG fields)

- **Higher v terms are found to be suppressed at $\rho \sim \rho_0$, but they will contribute more at high densities.**

$SU(3)_f$ “violating” coupling

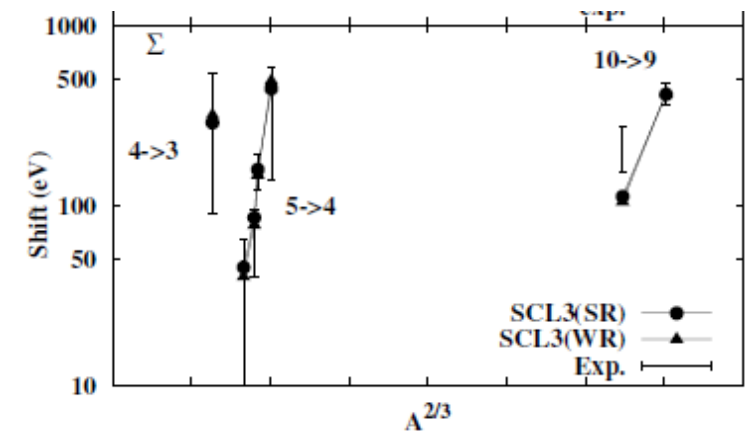
- Naïve RMF assumption = BM coupling follows $SU(3)_f$.
- Short range BB interaction comes from quark Pauli blocking + one-gluon exch.
Oka, Yazaki; Faessler et al.; Fujiwara et al.; HAL QCD collab.
- Short-range BB repulsion is sensitive to (S,T) in the s-channel. When we include those interactions in the bosonized form, BM coupling violates $SU(3)_f$.



$$V = \sum_{\alpha, \beta} (\bar{\psi} \bar{\psi})_{\alpha} \Gamma_{\alpha\beta} (\psi \psi)_{\beta} \rightarrow -\frac{1}{2} \sum_{\alpha} m_{\alpha}^2 \omega_{\alpha}^2 + \sum_{\alpha} g_{\alpha} \omega_{\alpha} (\psi \Gamma \psi)_{\alpha}$$

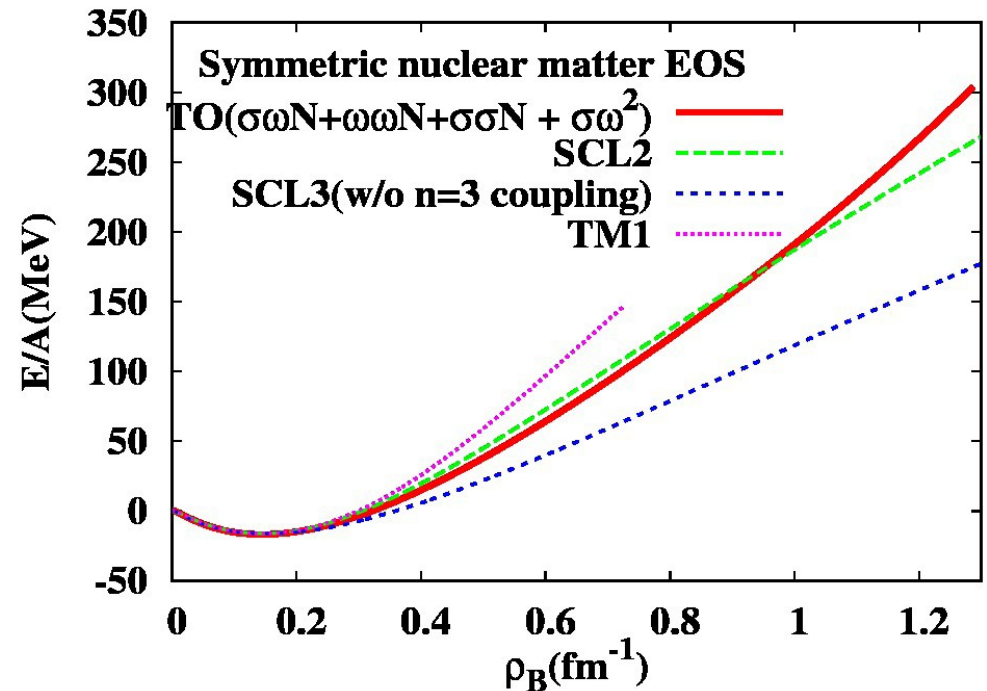
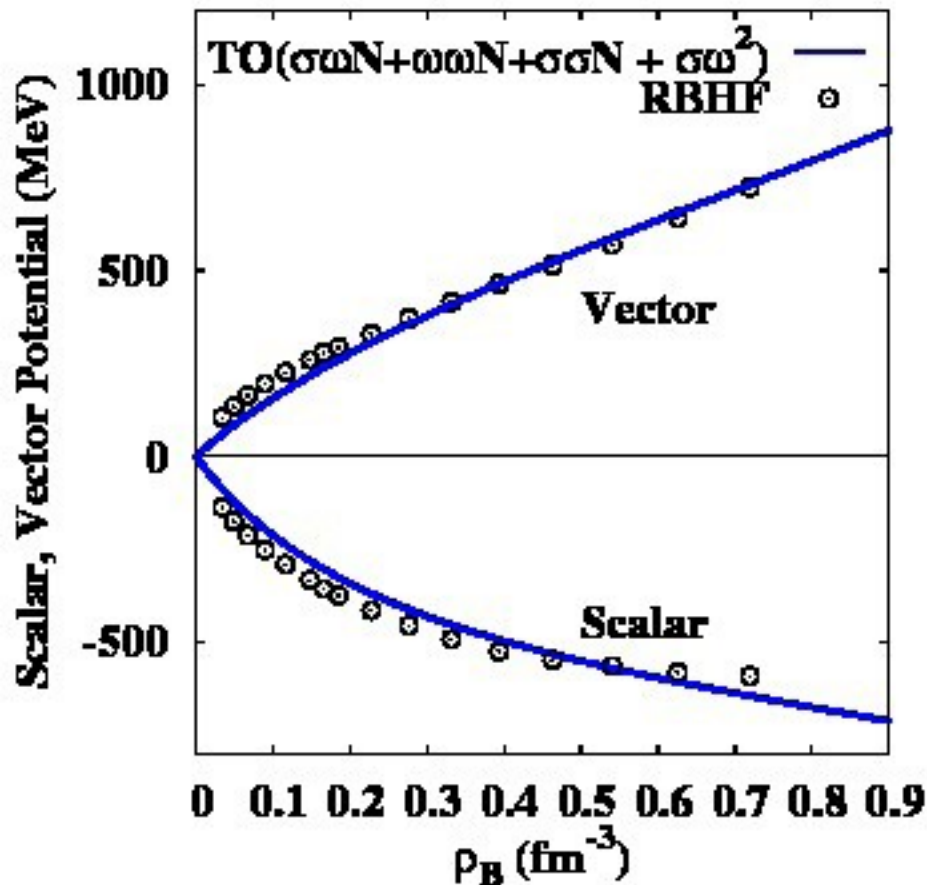
E.g., Σ atomic shift

$\rightarrow g_{\sigma\Sigma} \sim g_{\sigma\Sigma} (SU(3)) \times (0.2-0.3)$



Tsubakihara et al., (2010)

- Nucleon vector potential $U_v(\rho)$ in DBHF: Non-linear behavior in ρ_B .
 → EOS becomes gradually stiffer at high density !



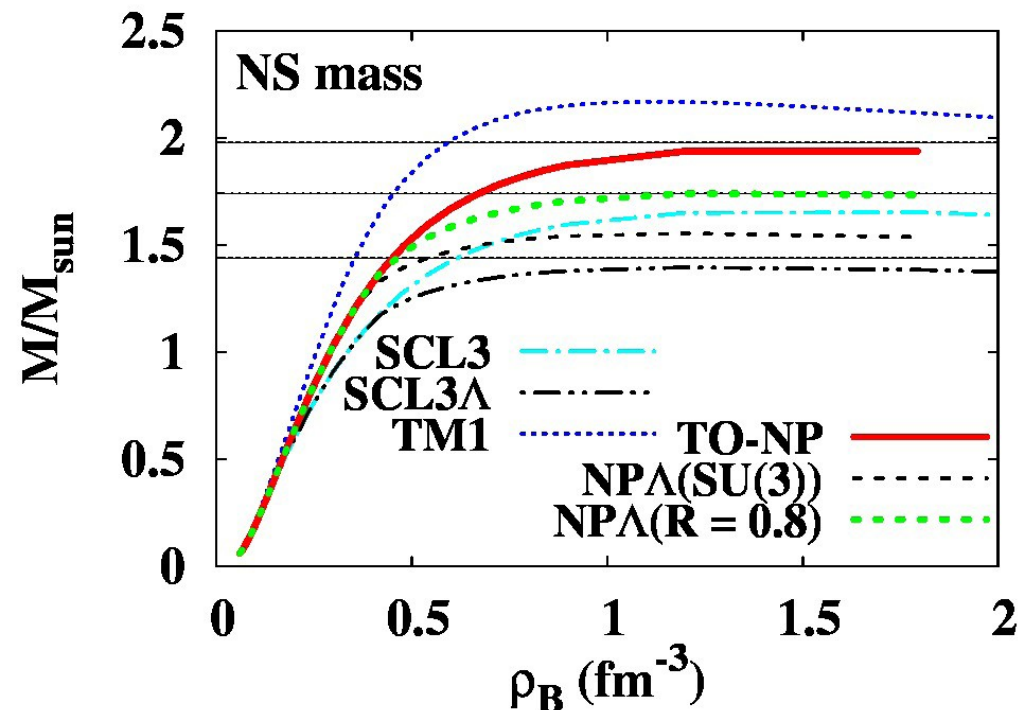
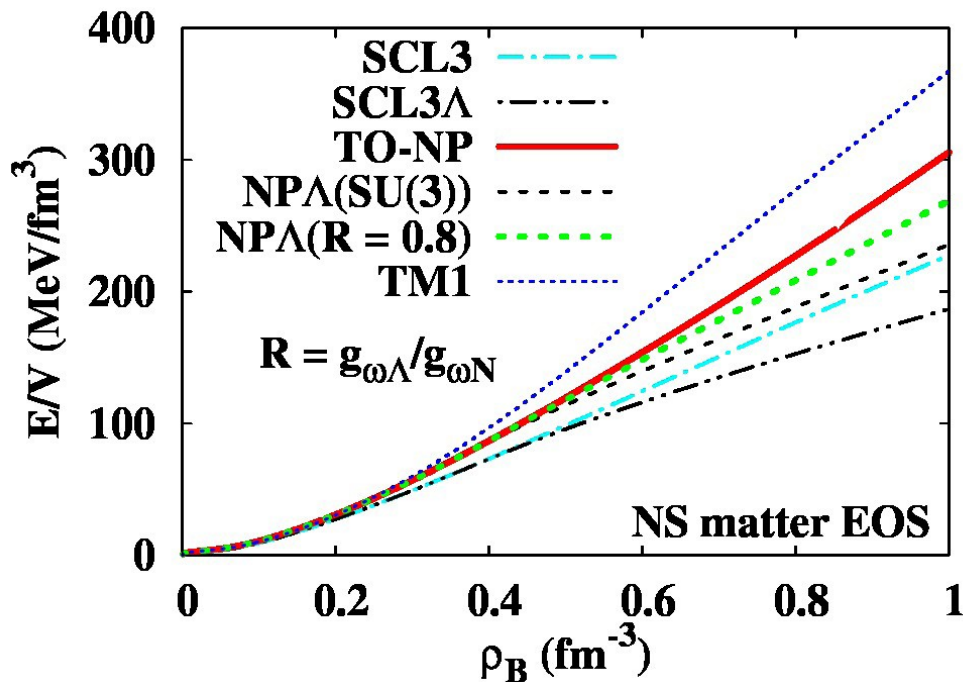
RMF with 3BF + $SU(3)_f$ “violation”

Tsubakihara, AO, in prep.

■ Two types of modification

- 3-baryon repulsion \rightarrow EOS becomes stiff gradually at high density. (Fitting meson mass (E325) and U_V in RBHF)
- $R = g_{\omega\Lambda} / g_{\omega N} \sim 0.8$ ($\sim 2/3$ ($SU(3)$))

$\rightarrow M_{\max} \sim 1.7 M_{\odot}$ with hyperons ($\sim 1.4 M_{\odot}$ w/o 3BF, violation)



Summary

- Hyperons in dense matter is still an important problem.
- Standard RMF with hyperons cannot support $1.97 M_{\odot}$ neutron star.
 - Various data / DBHF results can be fitted in RMF.
 - Vector Coupling $\sim SU(3)_f$, linear BM coupling ($\bar{B}MB$)
- RMF with $3BF + SU(3)_f$ “violation” may help to support the heavy NS.
 - Atomic shift data of Σ atom suggests the “violation” of $SU(3)_f$.
Similar trend is seen in previous RMF with hyperons.
R.Brockmann, W.Weise, PLB69('77)167; J.Boguta, S.Bohrmann, PLB102('81)93.
 - Ab initio calculations with induced/bare 3B force are helpful for phen. approaches to fix parameters.
 - Discussions during DCEN 2011 were encouraging.
(Importance of 3BF, large effects of 3BF at ρ_0)
- Can we support $1.97 M_{\odot}$ neutron star with hyperons ?
→ Open problem.

Thank you for your attention !

Chiral Symmetry

- Fundamental symmetry of massless QCD, and its spontaneous breaking generates hadron masses.

Nambu, Jona-Lasinio ('61)

- Many of the linear σ models are unstable against finite density (chiral collapse).

→ Log type chiral potential

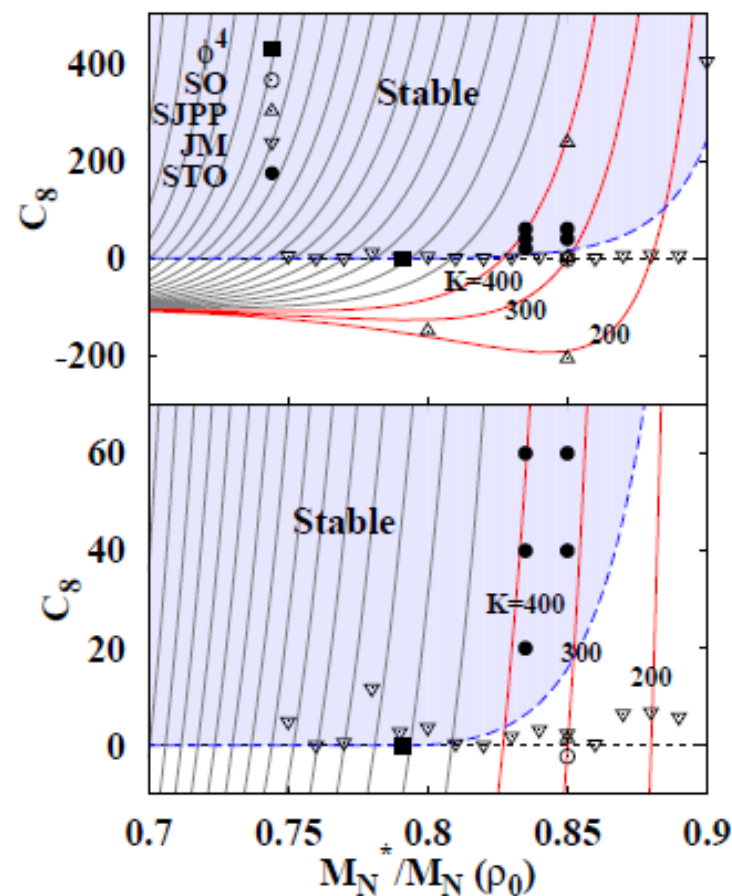
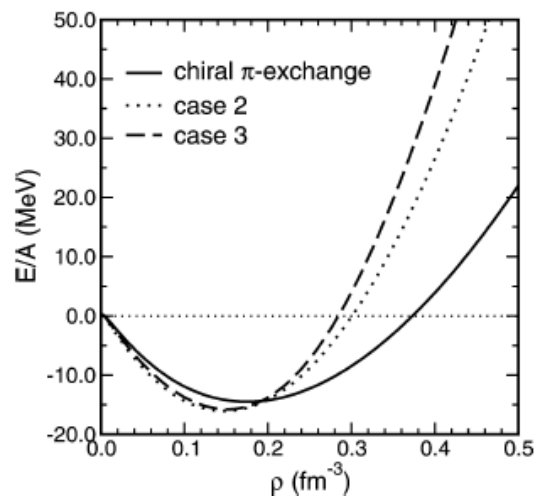
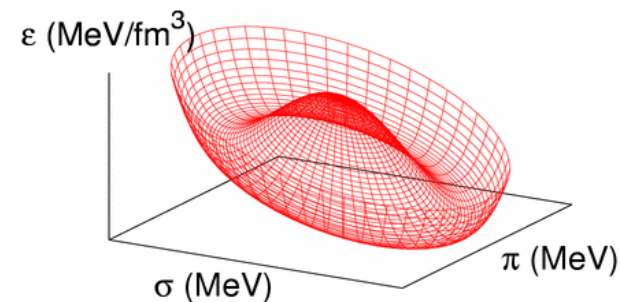
Sahu, Tsubakihara, AO('10), Tsubakihara, AO('07)

- Non-linear representation (chiral pert.) leads to density dependent coupling from pion loops.

Kaiser, Fritsch, Weise ('02),

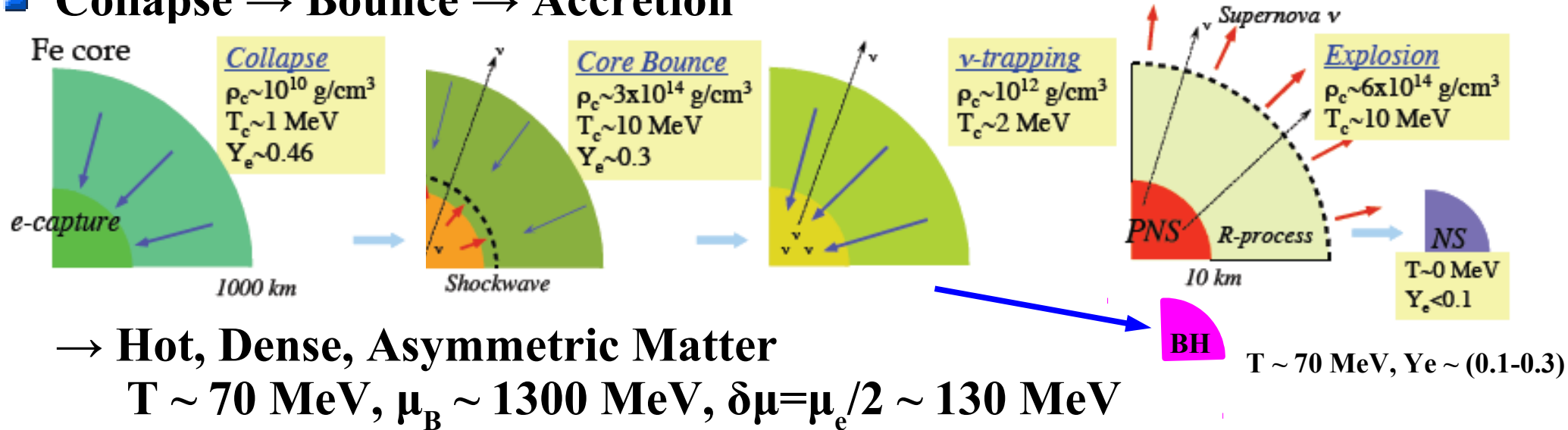
Finelli, Kaiser, Vretener

Weise ('04)



Dynamical Black Hole Formation

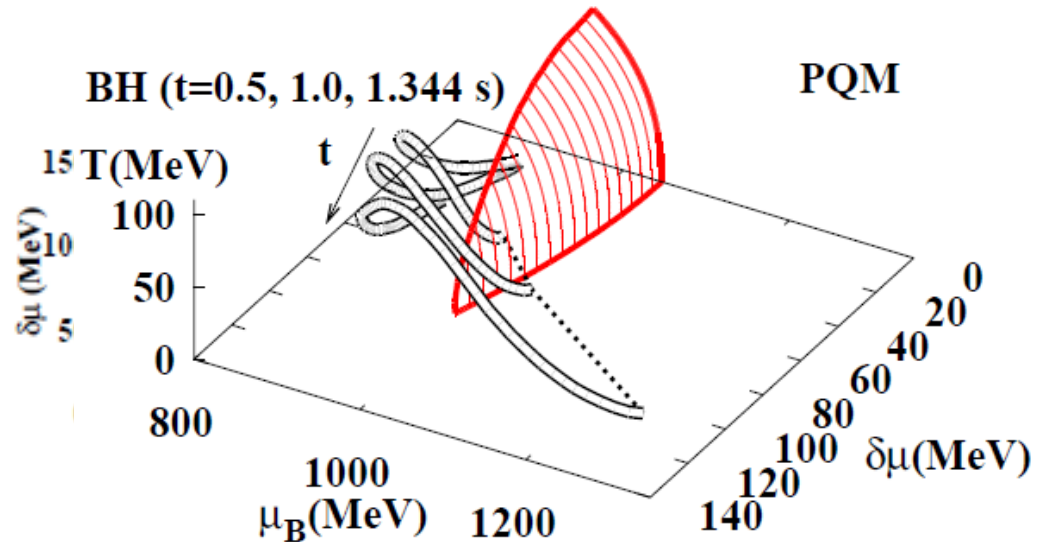
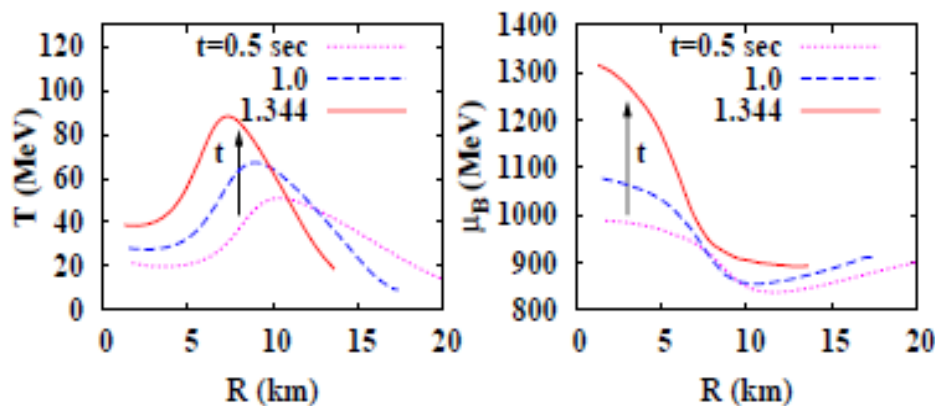
■ Collapse → Bounce → Accretion



→ Hot, Dense, Asymmetric Matter

$$T \sim 70 \text{ MeV}, \mu_B \sim 1300 \text{ MeV}, \delta\mu = \mu_e/2 \sim 130 \text{ MeV}$$

→ CP may be reachable



K. Sumiyoshi, et al., ('06); K. Sumiyoshi, C. Ishizuka, AO, S. Yamada, H. Suzuki ('09) AO, H. Ueda, T. Z. Nakano, M. Ruggieri, K. Sumiyoshi, PLB in press.