

QCD critical point in the strong coupling lattice QCD and during black hole formation



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*HIC for FAIR workshop & 28th Max Born Symposium
Three days on Quarkyonic Island, Wroclaw*

- **Questions & Conclusion**
- **QCD phase diagram in strong coupling lattice QCD**
K. Miura, T. Z. Nakano, AO, PTP 122('09)1045.
K. Miura, T. Z. Nakano, AO, N. Kawamoto, PRD 80 (2009), 074034;
PoS LAT2010 (2010), 202; in prep.
T. Z. Nakano, K. Miura, AO, PTP 123('10)825; PRD 83('11)016014.
- **Critical Point sweep during black hole formation**
AO, H. Ueda, T.Z.Nakano, M. Ruggieri, K. Sumiyoshi, arXiv:1102.3753.
K. Sumiyoshi, C. Ishizuka, AO, S. Yamada, H. Suzuki, ApJL690('09),L43.
- **Summary**

Questions and Conclusion

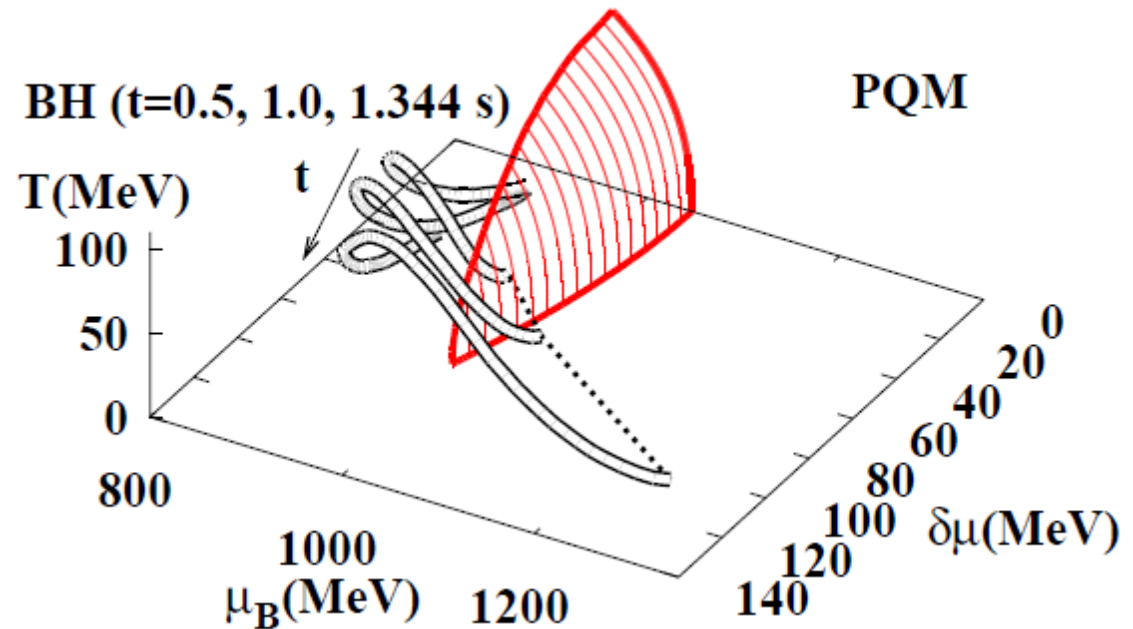
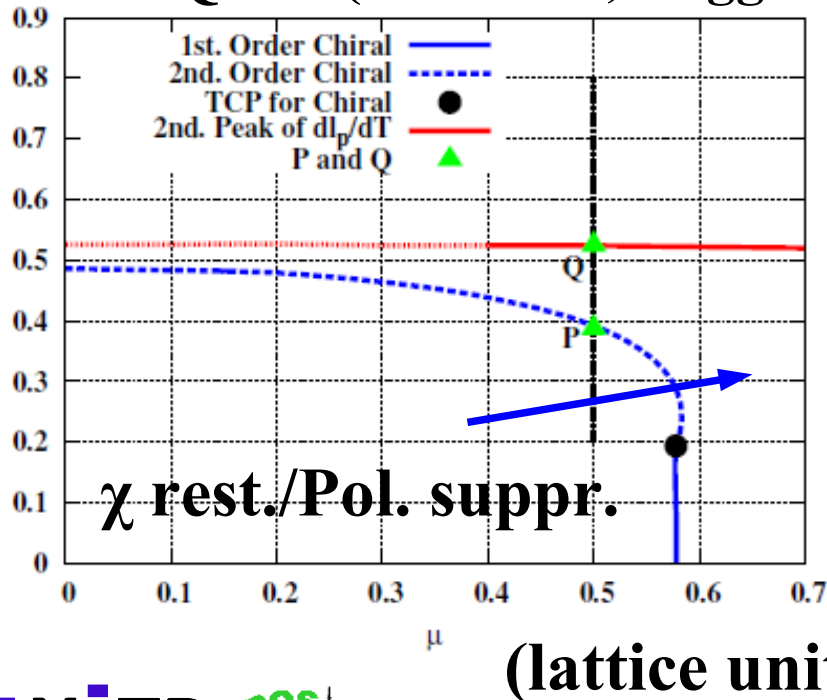
■ Does Quarkyonic matter exist in QCD with $N_c=3$?

→ There is χ restored & Polyakov loop suppressed region at low T and large μ in Strong Coupling Lattice QCD

■ Is there any site where Quarkyonic matter is formed ?

→ During the dynamical black hole formation, CP may be swept and quarkyonic matter may be formed.

P-SC-LQCD (NLO+LO, staggered)



*Phase diagram in
strong coupling lattice QCD
with Polyakov loop effects
(P-SC-LQCD)*

Quarkyonic matter

■ Do χ and Z_{N_c} transitions deviate at large μ ?

● Large N_c : Yes

L. McLerran, R. D. Pisarski, NPA796 ('07)83

● Effective Models: Yes and No

◆ Yes, in PNJL with some parameter set

L. McLerran, K. Redlich, C. Sasaki, NPA824('09)86; H. Abuki et al. ('08); Y. Sakai et al. ('10); D. Blaschke et al. ('11)

◆ No, with FRG or phen. inputs

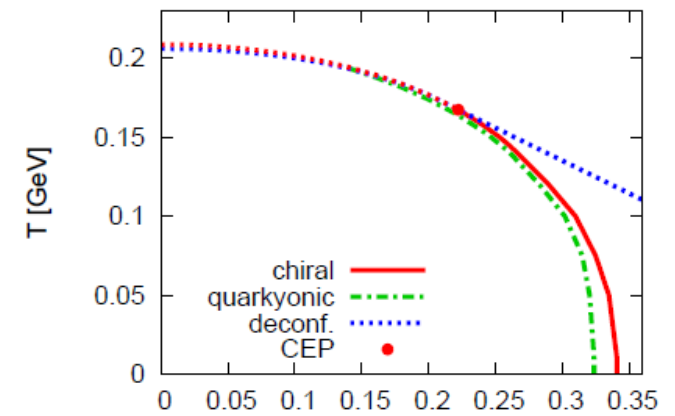
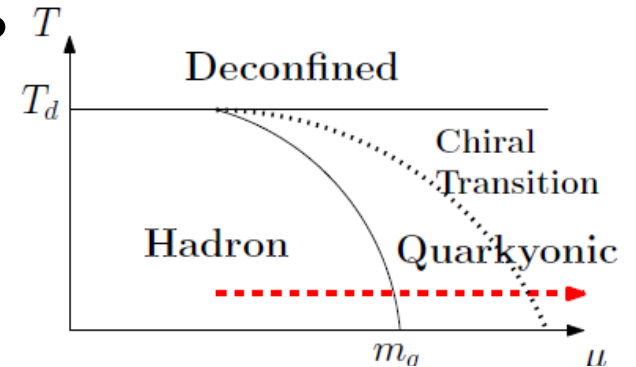
T. K. Herbst, J. M. Pawłowski, B. J. Schaefer, PLB 696 ('11)58 (PQM-FRG), K. Fukushima, PLB 695('11)387 (PNJL+Stat.)

■ QCD with $N_c=3$: Difficult

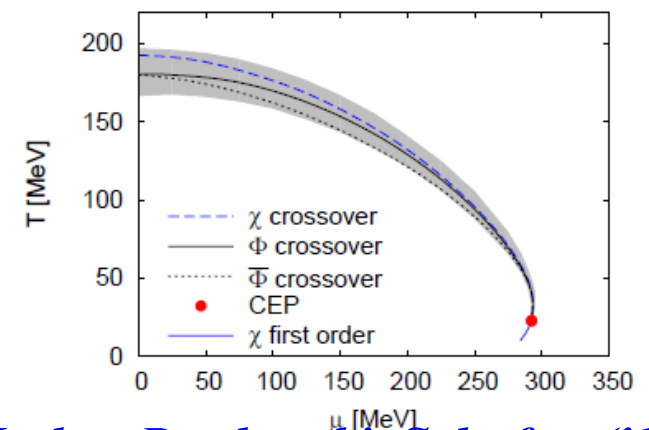
● AC, Taylor expansion, ... $\rightarrow \mu/T < 1$

● QCD-FRG: Not yet

● *SC-LQCD: This work*



McLerran, Redlich, Sasaki ('09)



Herbst, Pawłowski, Schaefer, ('11)

Strong Coupling Lattice QCD

- SC-LQCD has been a successful tool from the beginning of the lattice QCD formulation !
 - Pure Yang-Mills theory → **Confinement**
Area Law (Wilson ('74)), S.C. Expansion (Munster ('81)),
Finite T Pol. loop eff. action (Langelage, Münster, Philipsen ('08)), ..
 - With fermion → **SSB and restoration of Chiral Symmetry**
SSB [Kawamoto, Smit ('81)]
meson mass [Kluberg-Stern, Morel, Petersson ('83)],
Chiral restoration [Damgaard, Kawamoto, Shigemoto('84)],
phase diagram [Bilic, Karsch, Redlich ('92), Fukushima ('04),
Kawamoto, Miura, AO, Ohnuma ('07), de Forcrand, Fromm ('10)],
Finite coupling [Miura, Nakano, AO, Kawamoto ('09-'11)]
 - Combination → **Chiral and Polyakov loop dynamics**
Chiral Polyakov Dynamics [Ilgenfritz, Kripfganz ('85),
Gocksch, Ogilvie ('85), Fukushima('03), Nakano, Miura, AO('11),
Miura, Nakano, AO, Kawamoto('11)]

Does SC-LQCD show quarkyonic matter ?

SC-LQCD with Fermions & Polyakov loop (1)

Effective Action & Effective Potential (free energy density)

$$Z = \int D[\chi, \bar{\chi}, U_0, U_j] \exp \left[\begin{array}{c} \chi \\ \uparrow U \\ \bullet \\ \bar{\chi} \end{array} \quad \begin{array}{c} \bullet \\ \downarrow U^+ \\ \circ \end{array} \quad \bullet \circ \frac{1}{g^2} \quad \begin{array}{c} \square \\ \square \\ \square \\ \square \end{array} \right] = S_{\text{LQCD}}$$

NLO
NNLO

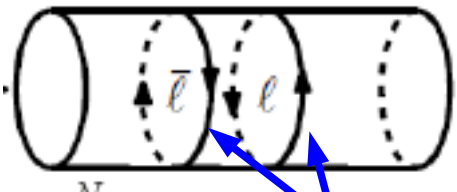
Spatial link integral

$$= \int D[\chi, \bar{\chi}, U_0] \exp \left[\begin{array}{c} \text{SCL} \\ \begin{array}{c} \circ \\ \vdots \\ \bullet \\ V^+ \end{array} \quad \begin{array}{c} \bullet \\ \vdots \\ \circ \\ V^- \end{array} \quad \begin{array}{c} \bullet \\ \text{---} \\ \circ \\ MM \end{array} \end{array} \right]$$

Bosonization

$$\approx \int D[\chi, \bar{\chi}, U_0] \exp(-S_{\text{eff}}[\chi, \bar{\chi}, U_0, \Phi_{\text{stat.}}])$$

$$\approx \exp(-V F_{\text{eff}}(\Phi; T, \mu)/T) \quad (\text{fermion} + U_0 \text{ integral})$$



Polyakov loop

SC-LQCD with Fermions & Polyakov loop (2)

- Effective potential [free energy density, NLO + LO(Pol. loop)]

$$\mathcal{F}_{\text{eff}}(\Phi; T, \mu) \equiv -(T \log \mathcal{Z}_{\text{LQCD}})/N_s^d = \mathcal{F}_{\text{eff}}^{\chi} + \mathcal{F}_{\text{eff}}^{\text{Pol}}$$

aux. fields

$$\mathcal{F}_{\text{eff}}^{\chi} \simeq \left(\frac{d}{4N_c} + \beta_s \varphi_s \right) \sigma^2 + \frac{\beta_s \varphi_s^2}{2} + \frac{\beta_{\tau}}{2} (\varphi_{\tau}^2 - \omega_{\tau}^2) - N_c \log Z_{\chi}$$

w.f. ren.
zero point E.
thermal

$$- N_c E_q - T (\log \mathcal{R}_q(T, \mu) + \log \mathcal{R}_{\bar{q}}(T, \mu))$$

$$\mathcal{R}_q(T, \mu) \equiv 1 + e^{-N_c(E_q - \tilde{\mu})/T} + N_c \left(L_{p,x} e^{-(E_q - \tilde{\mu})/T} + \bar{L}_{p,x} e^{-2(E_q - \tilde{\mu})/T} \right)$$

$$\mathcal{F}_{\text{eff}}^{\text{Pol}} \simeq -2T d N_c^2 \left(\frac{1}{g^2 N_c} \right)^{1/T} \bar{\ell}_p \ell_p - T \log \mathcal{M}_{\text{Haar}}(\ell_p, \bar{\ell}_p)$$

quad. coef.
Haar measure

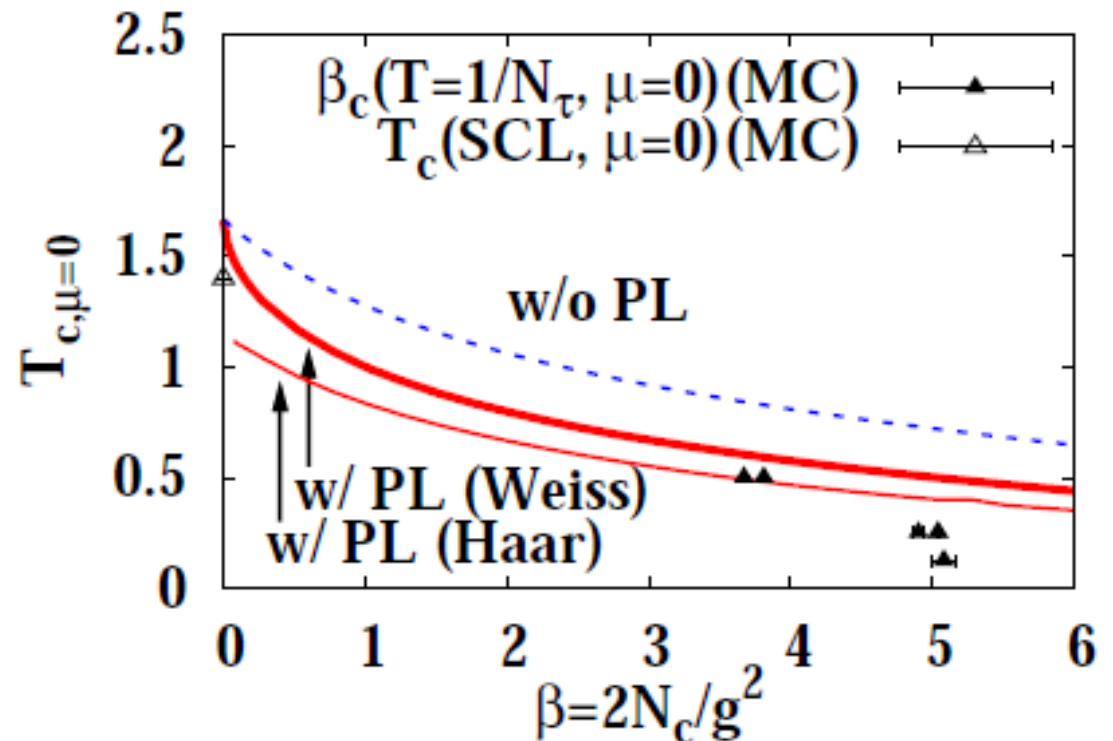
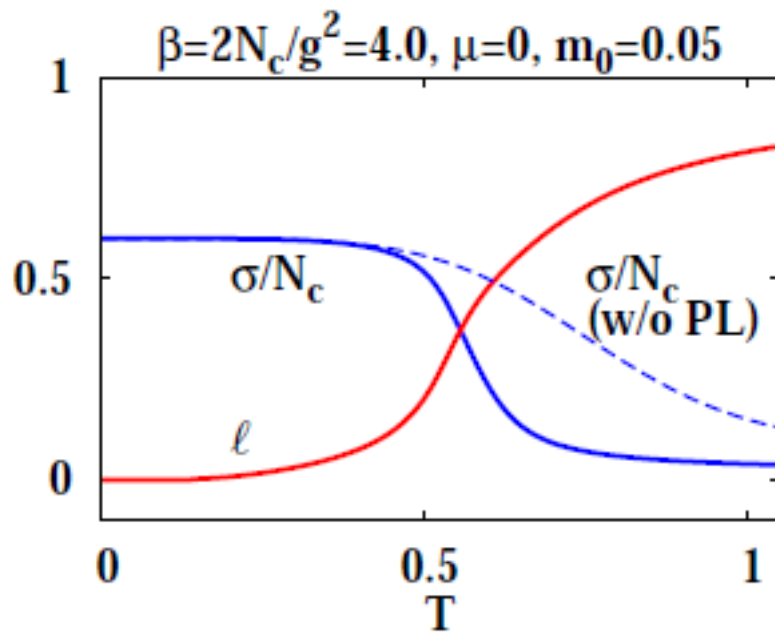
- Strong coupling lattice QCD with Polyakov loop (P-SC-LQCD) = Polyakov loop extended Nambu-Jona-Lasino (PNJL) model (Haar measure method, quadratic term fixed)
 - + higher order terms in aux. fields
 - quark momentum integral

P-SC-LQCD at $\mu=0$

T. Z. Nakano, K. Miura, AO, PRD 83 (2011), 016014 [arXiv:1009.1518 [hep-lat]]

- **P-SC-LQCD reproduces $T_c(\mu=0)$ in the strong coupling region**
 ($\beta = 2N_c/g^2 \leq 4$)

MC data: SCL (Karsch et al. (MDP), de Forcrand, Fromm (MDP)), $N_\tau=2$ (de Forcrand, private), $N_\tau=4$ (Gottlieb et al.('87), Fodor-Katz ('02)), $N_\tau=8$ (Gavai et al.('90))



Lattice Unit

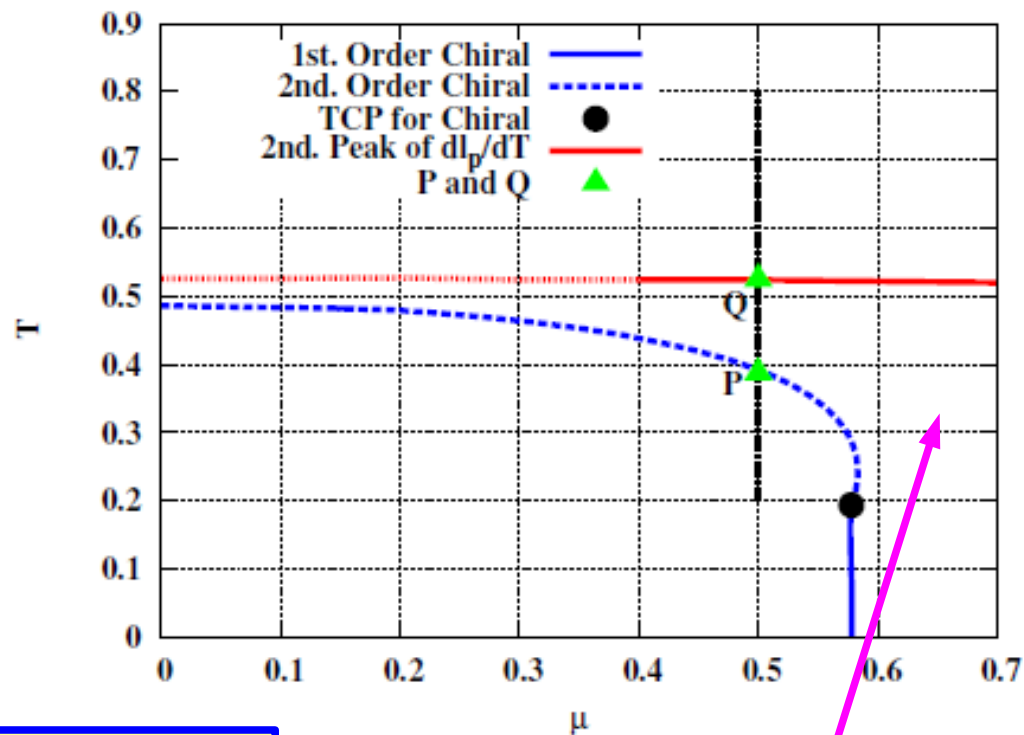
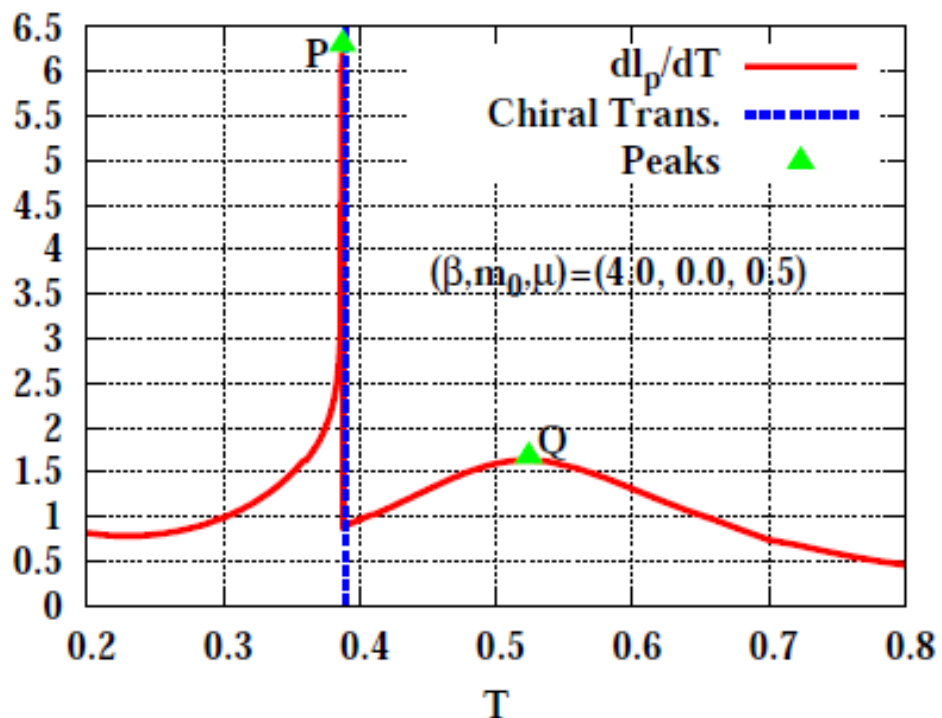
Phase diagram in P - SC - $LQCD$

K. Miura, T.Z. Nakano, AO, N. Kawamoto,

PoS LATTICE2010 (2010), 202 [arXiv:1012.1509 [hep-lat]] ; in prep.

and predicts the existence of the “Quarkyonic-like” matter

dl_p/dT has two peaks: Chiral-induced & Z_{N_c} -induced.



“Q” depends only weakly on μ and m_0 .
 $\rightarrow Z_{N_c}$ -induced peak

Quarkyonic-like
 (χ restored,
 Pol. loop suppressed.)

■ Disclaimer

- Unrooted staggered fermion ($N_f=4$ @ cont.)
- NLO/NNLO & LO in quark & Polyakov loop effective actions (strong coupling ($1/g^2$) expansion)
- LO in $1/d$ expansion, mean field (min. # of quarks for a given plaq. config.)

■ Followings may modify the present conclusion.

- μ dependent coef. in Polyakov loop effective action, or χ -Pol. entanglement

$$\mathcal{U}(\Phi) = (aT^4 + b\mu^2T^2 + c\mu^4)\Phi^2 + a_2T_0^4 \ln(1 - 6\Phi^2 + 8\Phi^3 - 3\Phi^4)$$

Dexheimer, Schramm, NPB(PS)199('10)319; Blaschke et al., PTPS186('10)81; Sakai, Sasaki, Kouno, Yahiro, PRD82('10)076003.

- Different fermion, e.g. (Staggered-)Wilson Fermion
- With higher order corrections,

*Critical Point sweep
during black hole formation*

Compact Astrophysical Phenomena

Neutron Star

- Cold ($T \sim 0$), Dense ($\rho_B \sim 5 \rho_0$)
Highly Asymmetric ($Y_p \sim (10-20) \%$)

Supernovae

- Warm ($T \sim 20$ MeV), Dense ($\rho_B \sim 1.8 \rho_0$)
mildly asymmetric ($Y_p \sim (30-40) \%$)

- QCD phase transition ?

T. Hatsuda, MPLA2('87)805; I. Sagert et al., PRL102 ('09) 081101.

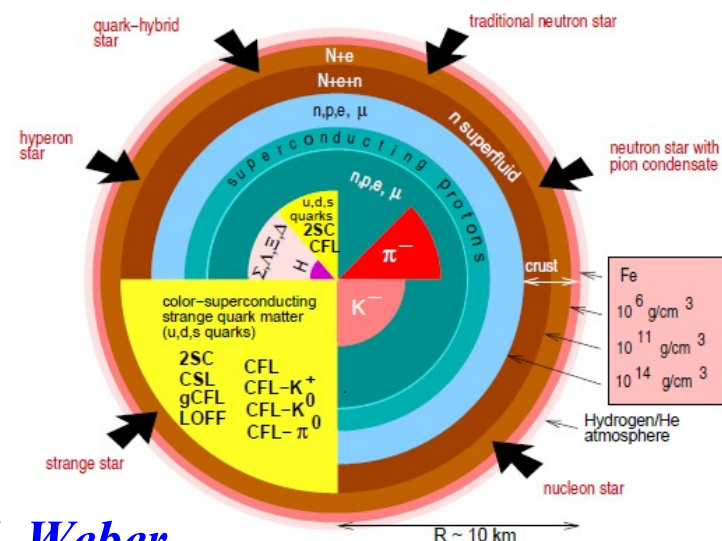
Dynamical black hole formation

- Hot ($T \sim 70$ MeV), Dense ($\rho_B \sim 5 \rho_0$)
Asymmetric ($Y_p \sim (10-30) \%$)

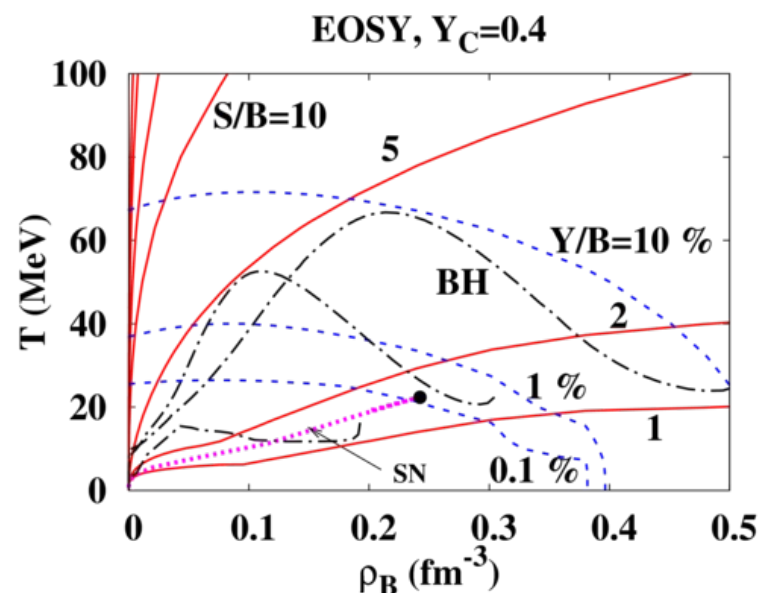
K. Sumiyoshi, et al., PRL97('06) 091101.

K. Sumiyoshi, C. Ishizuka, AO, S. Yamada,

H. Suzuki, ApJL690('09), L43



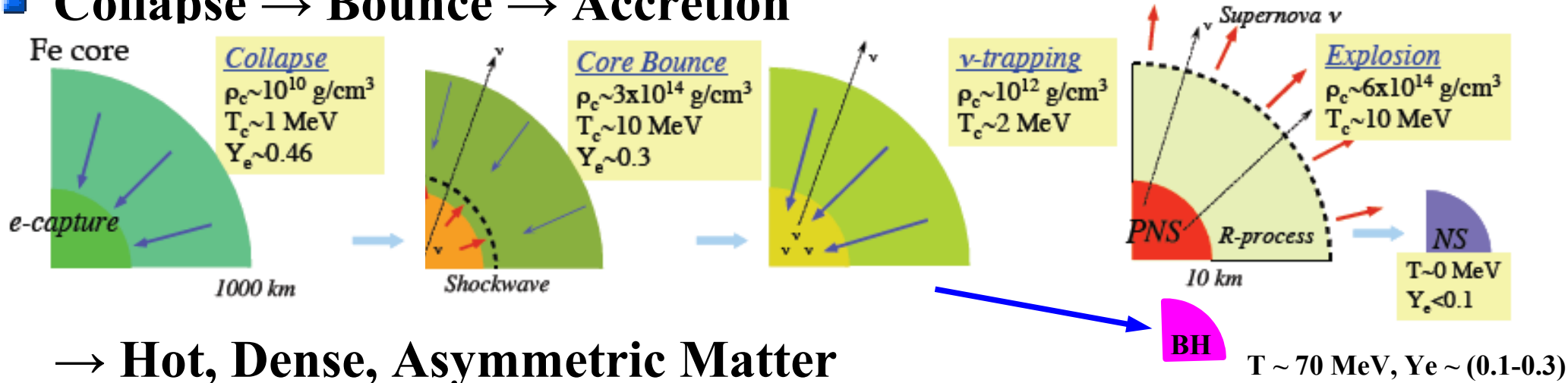
F. Weber, Prog.Part.Nucl.Phys.54('05) 193



C. Ishizuka, AO, K. Tsubakihara, K. Sumiyoshi, S. Yamada, JPG 35('08)085201

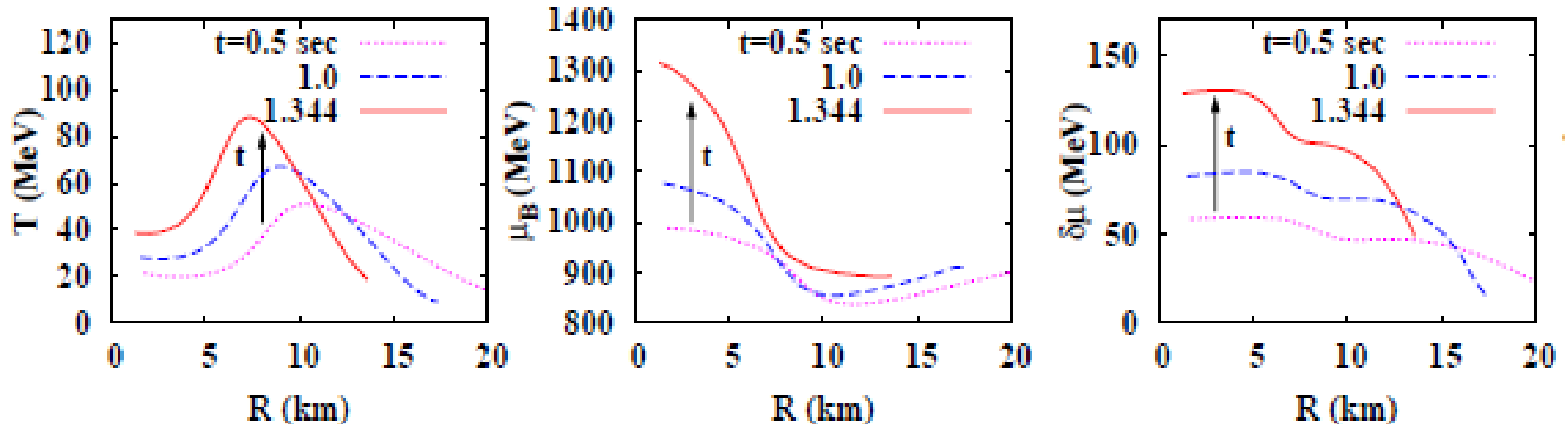
Dynamical Black Hole Formation

■ Collapse → Bounce → Accretion



→ Hot, Dense, Asymmetric Matter

$$T \sim 70 \text{ MeV}, \mu_B \sim 1300 \text{ MeV}, \delta\mu = \mu_e/2 \sim 130 \text{ MeV}$$



→ Black Hole

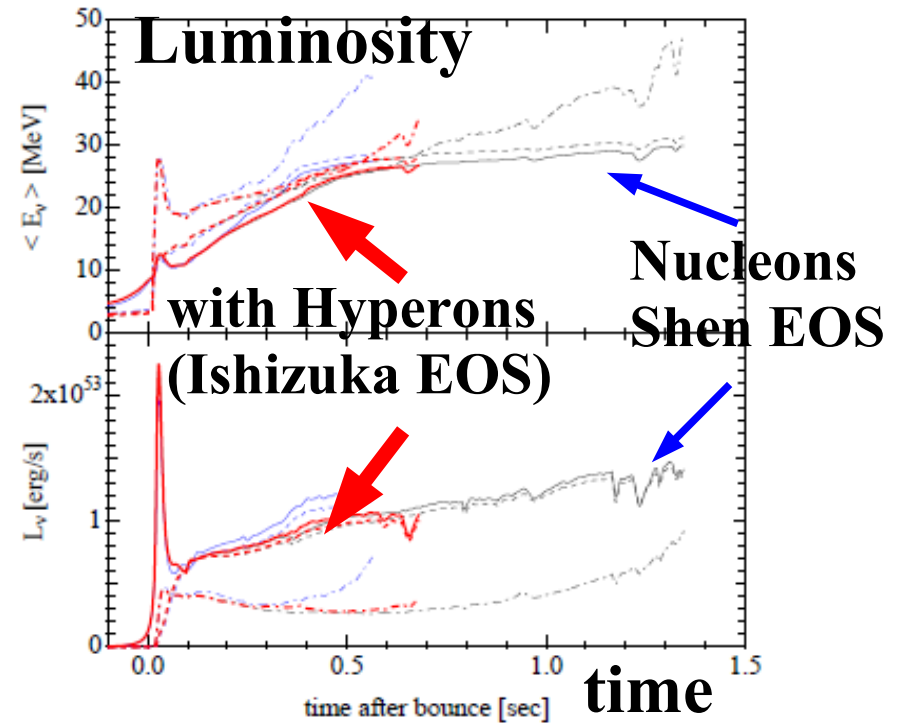
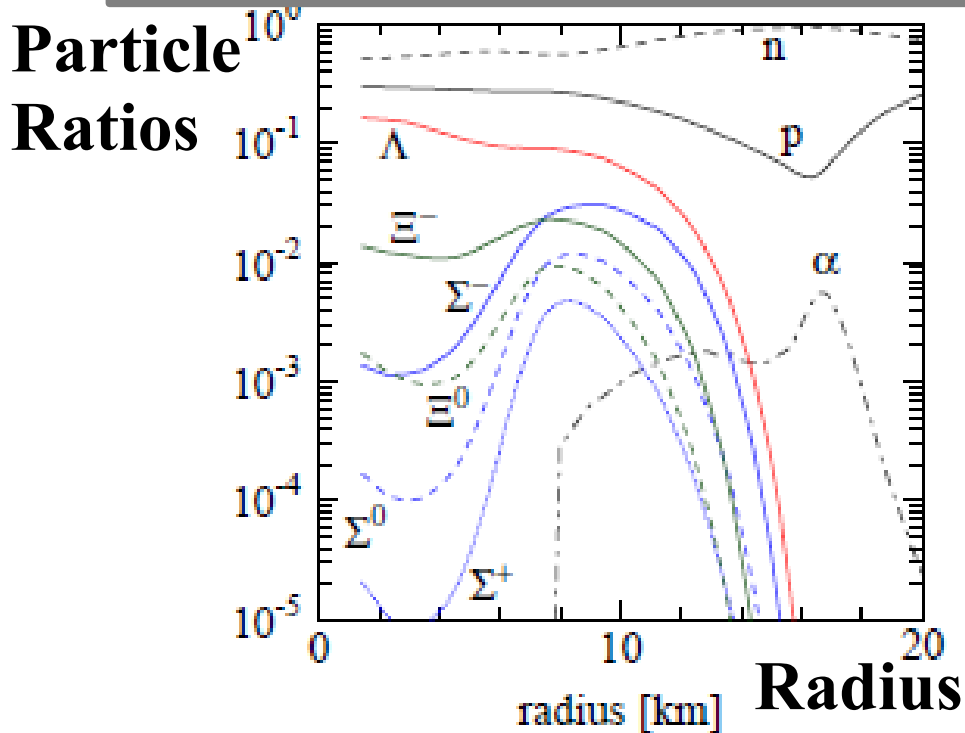
K. Sumiyoshi, et al., ('06); K. Sumiyoshi, C. Ishizuka, A.O., S. Yamada, H. Suzuki ('09)

Black Hole Formation (Failed Supernova)

High T during BH formation

→ Abundant hyperons → Soft EOS → Earlier Collapse to BH

Short ν emission may be the signal of Hyperon Admixture at high density and/or temperature

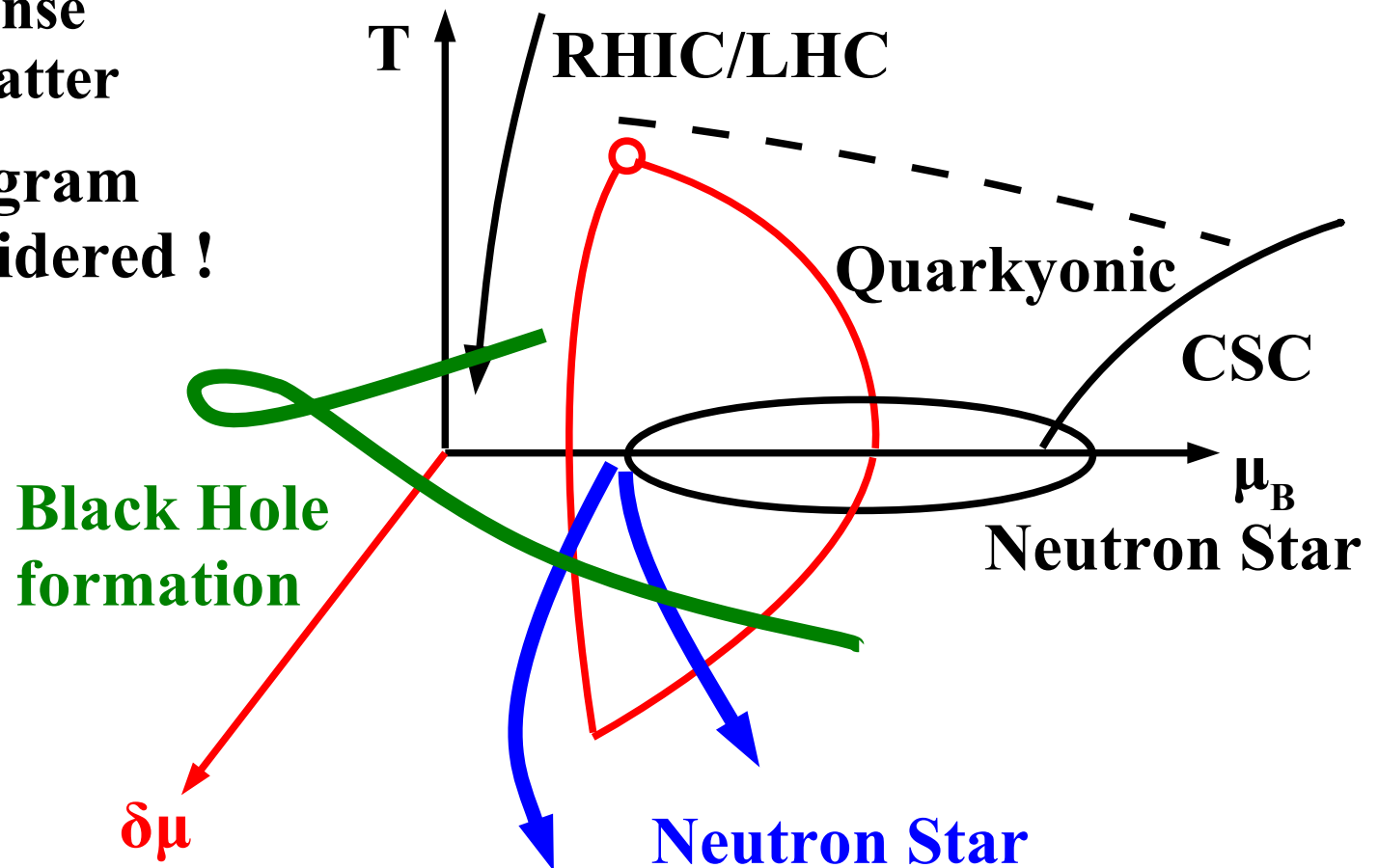


K. Sumiyoshi, C. Ishizuka, AO, S. Yamada, H. Suzuki, ApJL 690('09)L43

C. Ishizuka, AO, K. Tsubakihara, K. Sumiyoshi, S. Yamada, JPG 35 ('08)085201

QCD phase diagram in Compact Astrophys. Phen.

- Phase diagram probed in High-Energy Heavy-Ion Collisions
 - Hot & Dense *Symmetric* matter
 - Phase diagram probed in Compact Astrophysical Phenomena
 - Hot and/or Dense *Asymmetric* matter
- 3D phase diagram must be considered !



Chiral Effective Models (1)

■ Chiral Effective models

- Spontaneous breaking of chiral sym. → const. quark mass
- Polyakov loop extension → chiral & deconf. transitions

■ NJL model *Nambu, Jona-Lasinio ('61)*

■ PNJL *Fukushima('03), Ratti, Thaler, Weise ('06), Sakai et al. ('08)*

■ PQM model

B.J.Schafer, Pawłowski, Wambach ('07), Skokov, Friman, E.Nakano, Redlich ('10)

$$\mathcal{L}_{PQM} = \bar{q} (i \not{D} - g(\sigma + i\gamma_5 \vec{\tau} \vec{\pi})) q + \frac{1}{2}(\partial_\mu \sigma)^2 + \frac{1}{2}(\partial_\mu \vec{\pi})^2 - U(\sigma, \vec{\pi}) - \mathcal{U}(\Phi, \bar{\Phi})$$

$$\Omega_{PQM}(\Phi, \bar{\Phi}, \sigma) = \Omega_{\bar{q}q}(\Phi, \bar{\Phi}, \sigma) + U_{vac}(\sigma) + U(\sigma) + \mathcal{U}(\Phi, \bar{\Phi})$$

$$\Omega_{\bar{q}q}^{u,d} = -2T \int \frac{d^3k}{(2\pi)^3} \left[\ln \left(1 + 3\Phi e^{-(E_k - \mu_{u,d})/T} + 3\bar{\Phi} e^{-2(E_k - \mu_{u,d})/T} + e^{-3(E_k - \mu_{u,d})/T} \right) \right]$$

$$U_{vac} = -2N_f N_c \int \frac{d^3k}{(2\pi)^3} E_k \theta(\Lambda^2 - k^2) \quad U(\sigma) = U(\sigma, \vec{\pi} = \mathbf{0}) = \frac{\lambda}{4}(\sigma^2 - v^2)^2 - c\sigma$$

$$\frac{\mathcal{U}(\Phi, \bar{\Phi})}{T^4} = -\frac{a(T)}{2} \Phi \bar{\Phi} + b(T) \log[1 - 6\Phi \bar{\Phi} - 3(\Phi \bar{\Phi})^2 + 4(\Phi^3 + \bar{\Phi}^3)]$$

Chiral Effective Models (2)

■ Polyakov loop effective potential

- log (Haar measure) type
Lattice data → coef. (a(T), b(T))

■ Vector-Vector coupling

$$-G_\rho [(\bar{q}\gamma^\mu \tau q)^2 + (\bar{q}i\gamma_5\gamma^\mu \tau q)^2] - G_\omega (\bar{q}\gamma^\mu q)^2$$

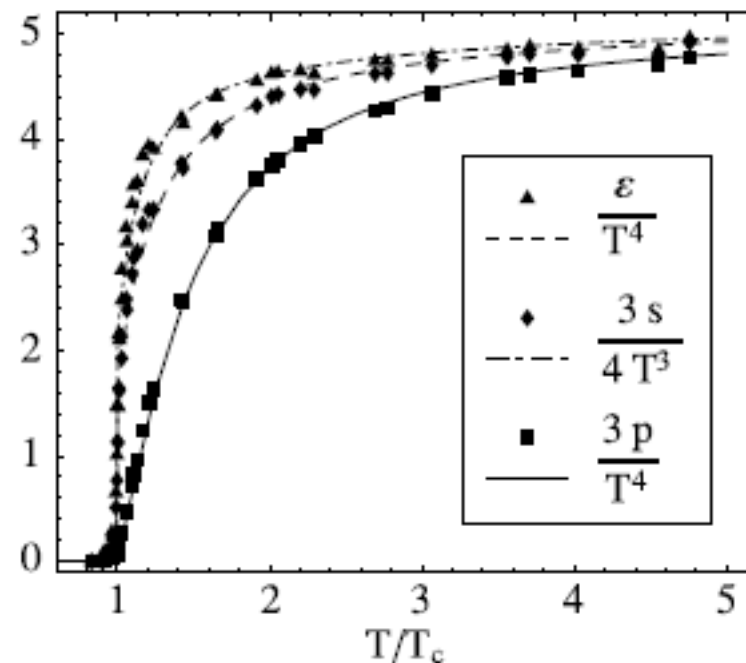
- Modifies chem. pot. effectively.
- Compare the results with
 $G_v/G_s = 0, 0.2$

■ 8 Fermi interaction

T. Sasaki, Y. Sakai, H. Kouno, M. Yahiro ('10)

$$G_{\sigma 8} \left[(\bar{q}q)^2 + (\bar{q}i\gamma_5\tau q)^2 \right]^2$$

- modifies quark masses
in vacuum



Roessner et al.('07)

*We compare the phase diagram
in NJL, PNJL, PNJL8, PQM
with ν -radiation Hydro. results.*

Isospin chemical potential

■ Isospin chemical potential

$$\delta\mu = (\mu_d - \mu_u)/2 = (\mu_n - \mu_p)/2 \rightarrow \mu_d = \mu_q + \delta\mu, \mu_u = \mu_q - \delta\mu$$

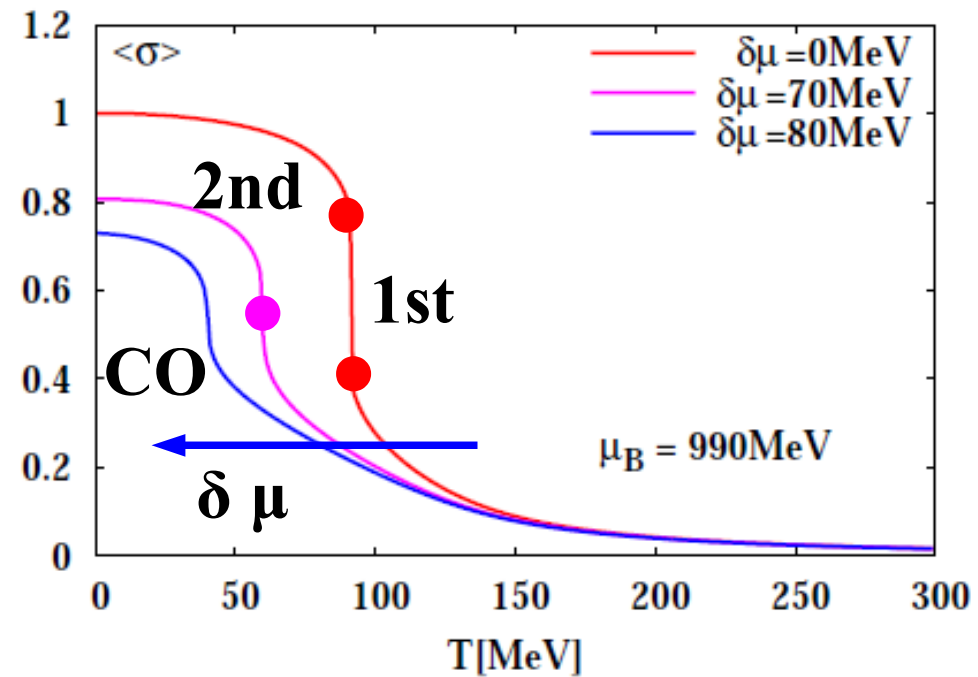
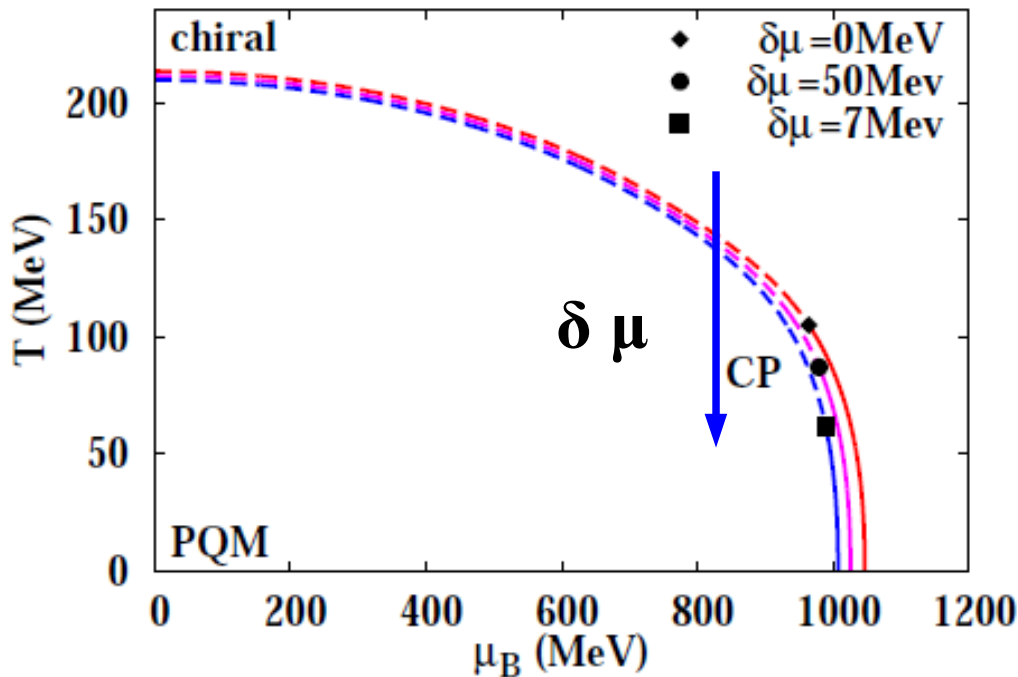
■ (Iso)Asymmetric matter $N_u \neq N_d$

● Finite $\delta\mu \rightarrow$ “Effective” number of flavors $1 \leq N_f \leq 2$

● large k_F (for a given ρ_B) \rightarrow smaller E gain in NG phase

\rightarrow small transition T, small T_{CP}

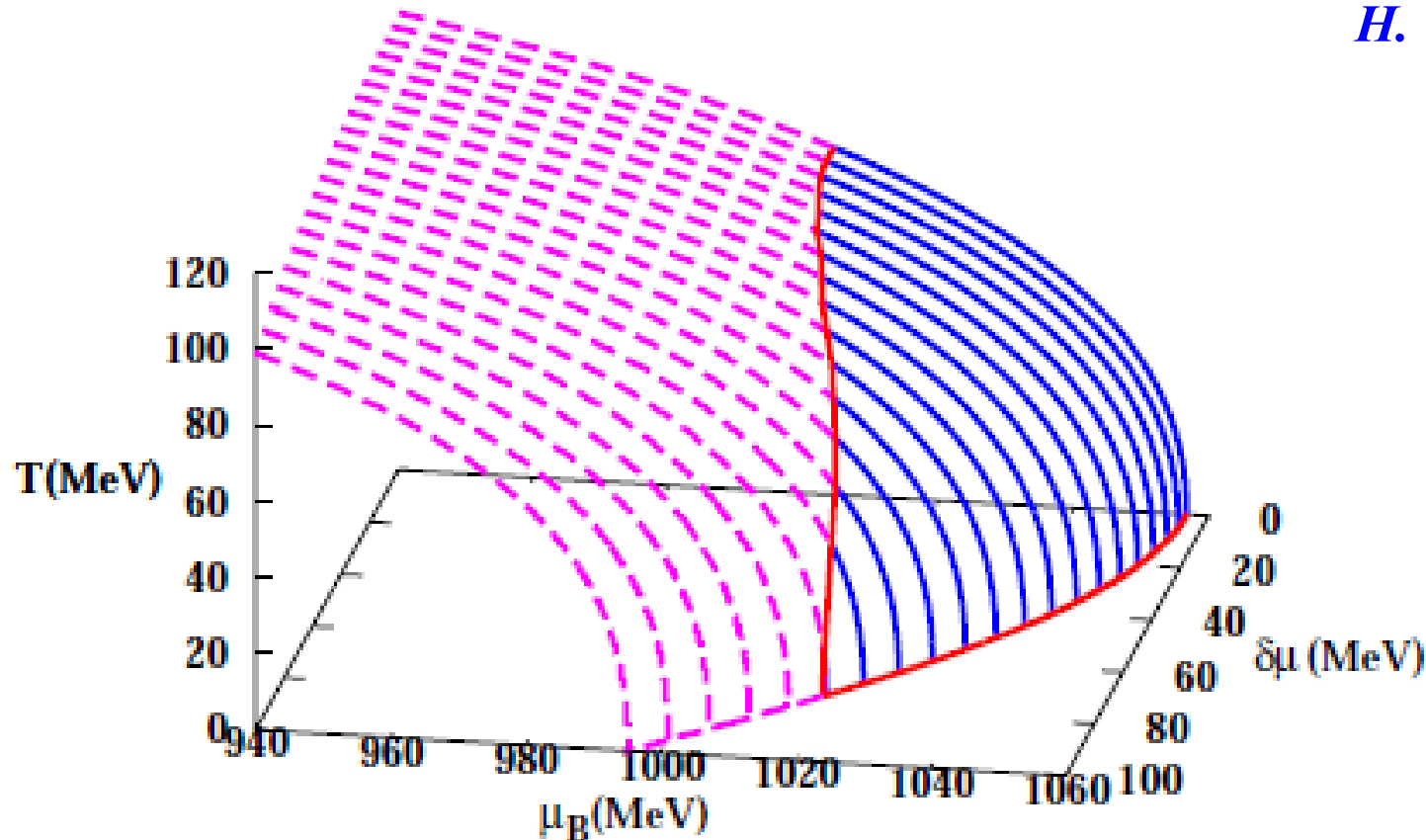
H. Ueda, M. thesis



3D phase diagram in PQM

- Phase diagram in $(T, \mu, \delta\mu)$ space $\delta\mu = (\mu_d - \mu_u)/2$

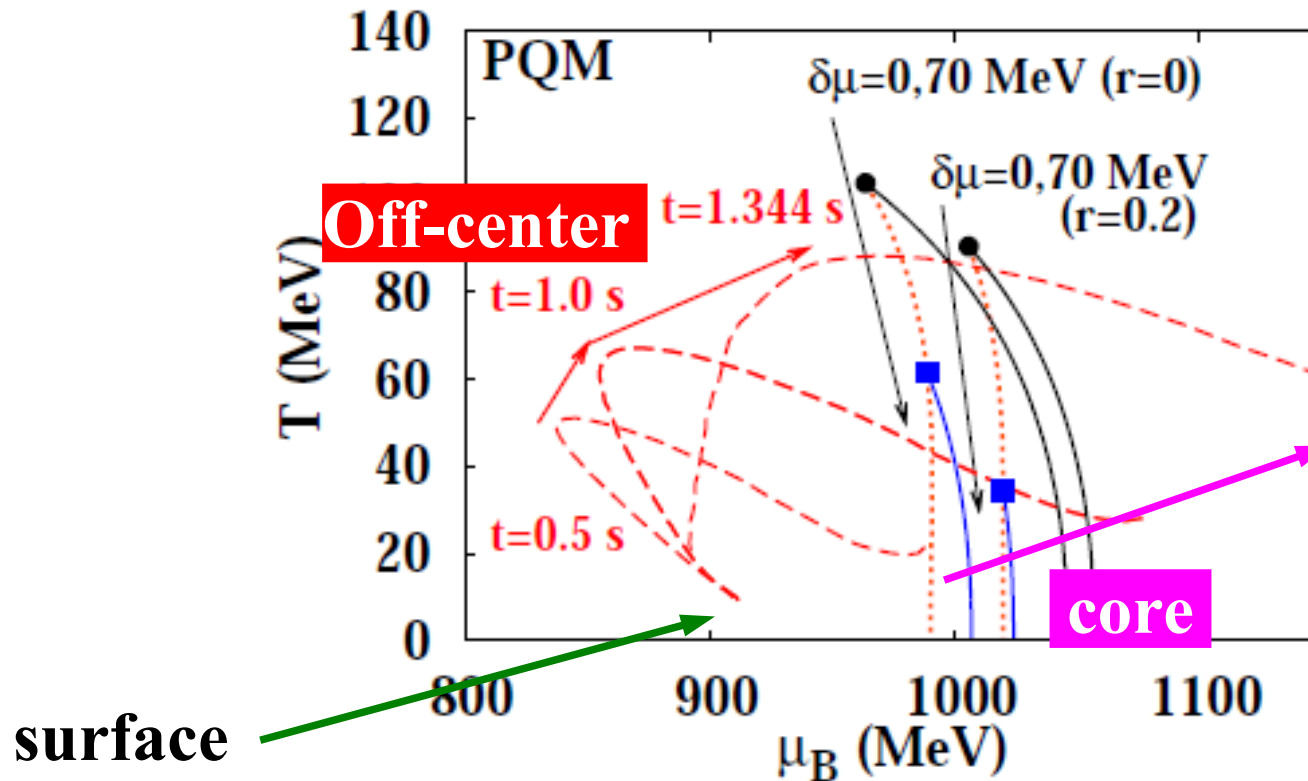
H. Ueda, M. thesis



CP temperature goes down at finite $\delta\mu$ in the range reachable during BH formation.

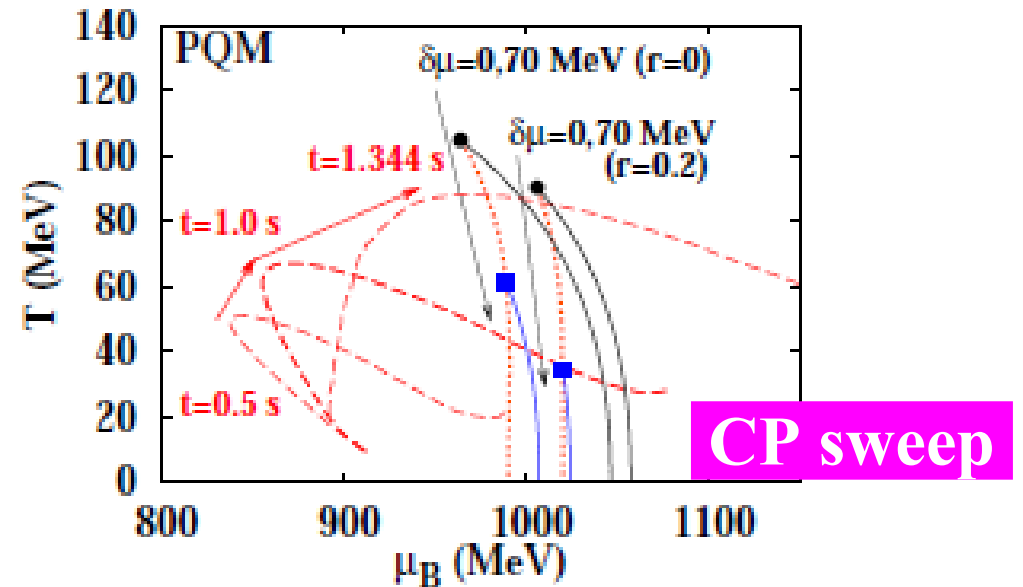
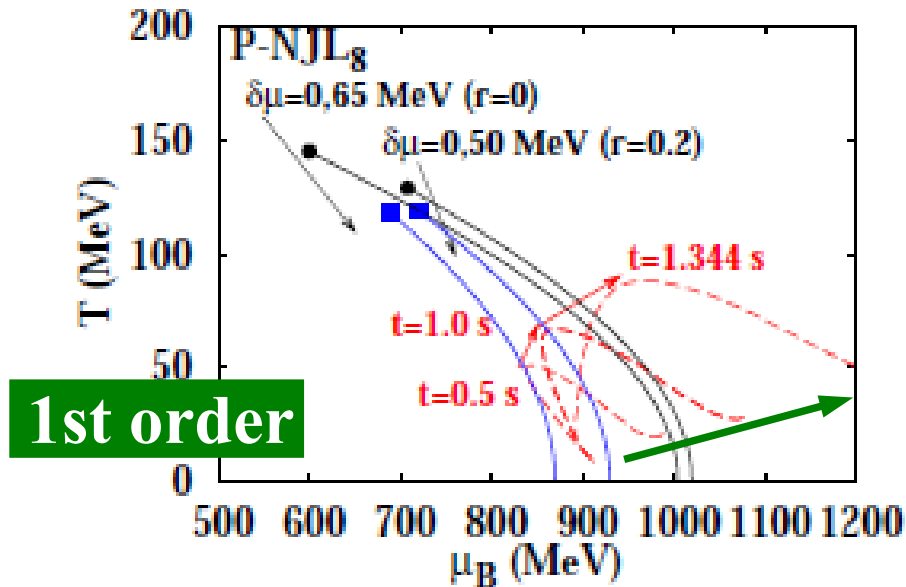
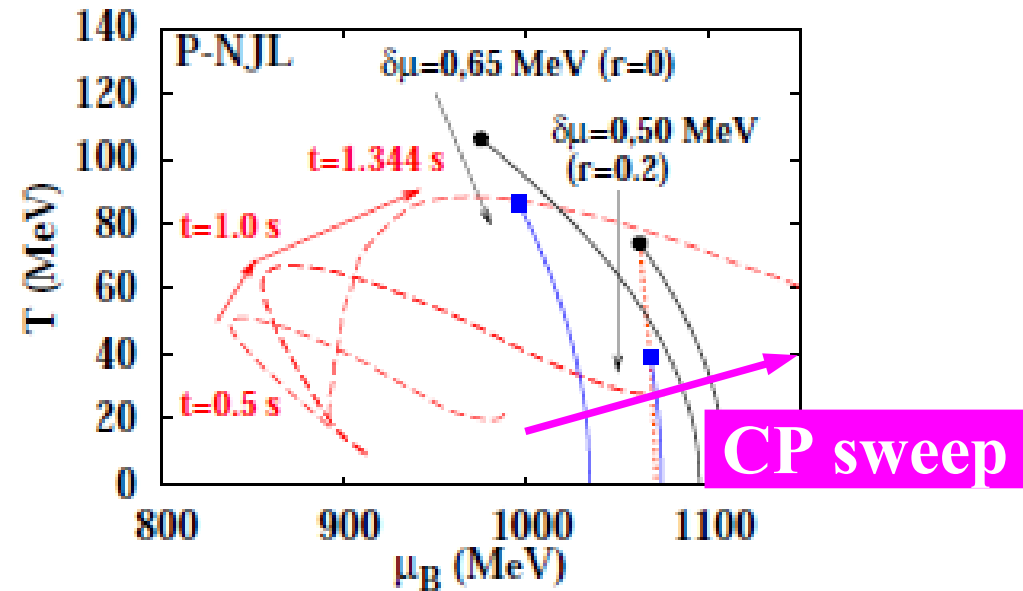
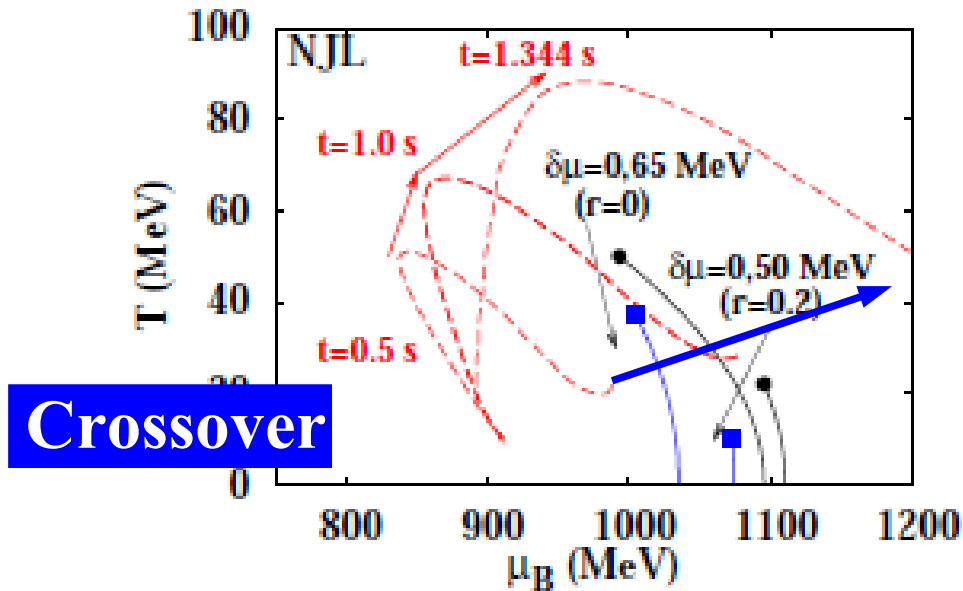
How is quark matter formed during BH formation ?

- Highest μ_B just before horizon formation ~ 1300 MeV
> QCD transition μ (1000-1100 MeV)
→ Quark matter is formed before BH formation
- Core evolves below CP, Off-center goes above CP
→ CP sweep



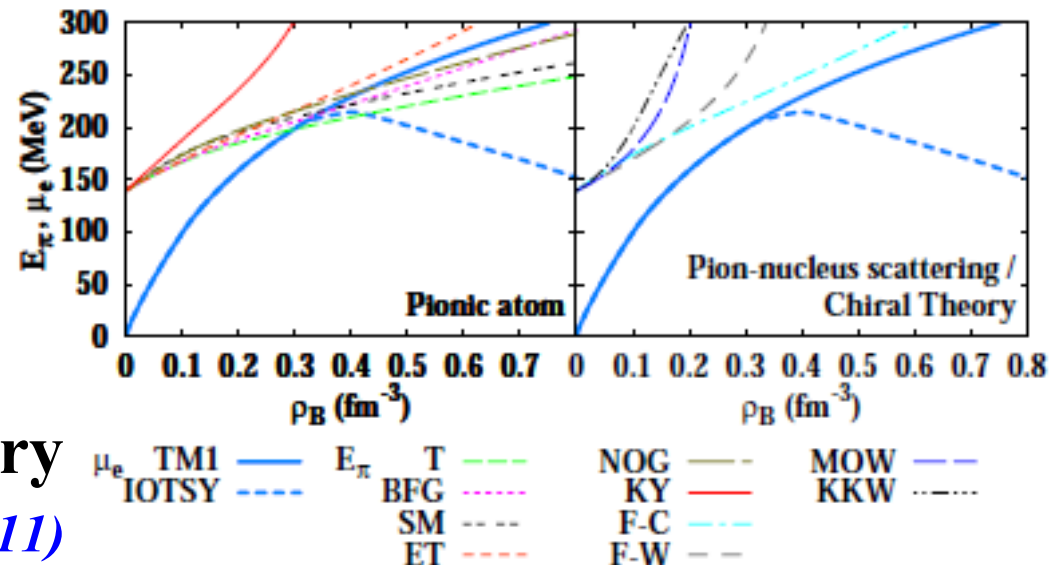
How is quark matter formed during BH formation ?

- Model dependence to form quark matter → Three ways



Discussion

- How can we observe the phase transition signal ?
 - ν spectrum ? Gravitational waves ?
Supernova: Second peak in ν & $\bar{\nu}$ emission
Hatsuda('87), Sagert et al.('09)
- Large $\delta\mu$ in hadronic EOS comes from strong vector coupling.
 - $g_\omega / g_\sigma > 1$ in RMF \rightarrow Large sym. E & large $\delta\mu$
 - $G_v/G_s < 0.3$ in PNJL or no CP (c.f. Poster by Blaschke)
- Strangeness may reduce $\delta\mu$ in hadronic / quark matter
 - No s-wave π cond. in NS
AO, D. Jido, T. Sekihara, K. Tsubakihara, PRC80('09)038202.
- Hadron-Quark EOS is necessary
E.g. Steinheimer, Schramm, Stocker('11)



Questions and Conclusion

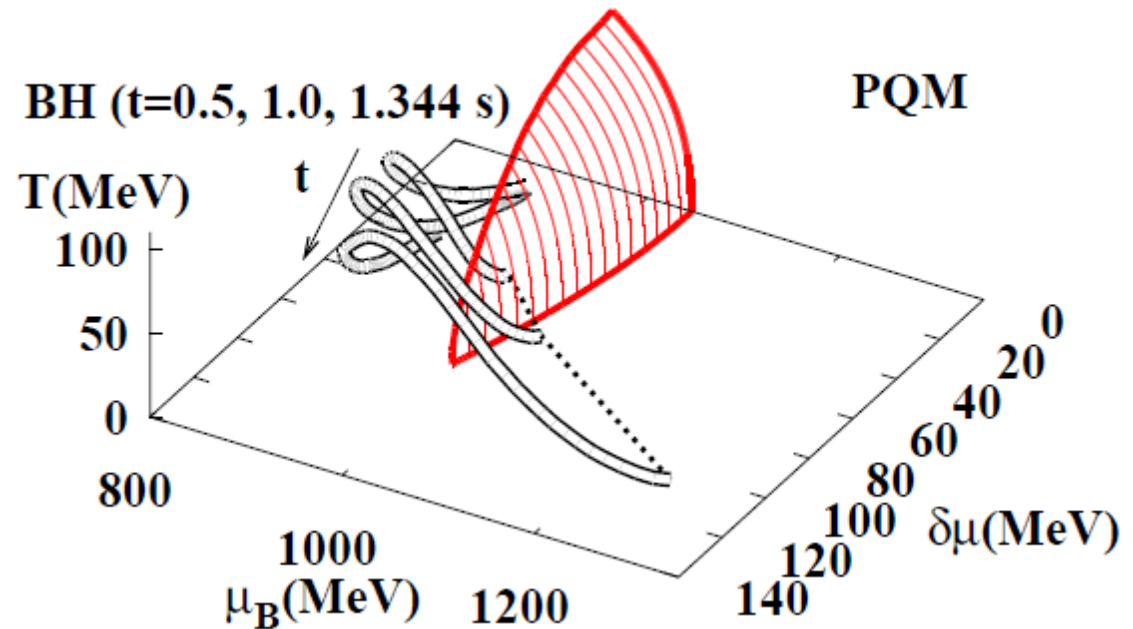
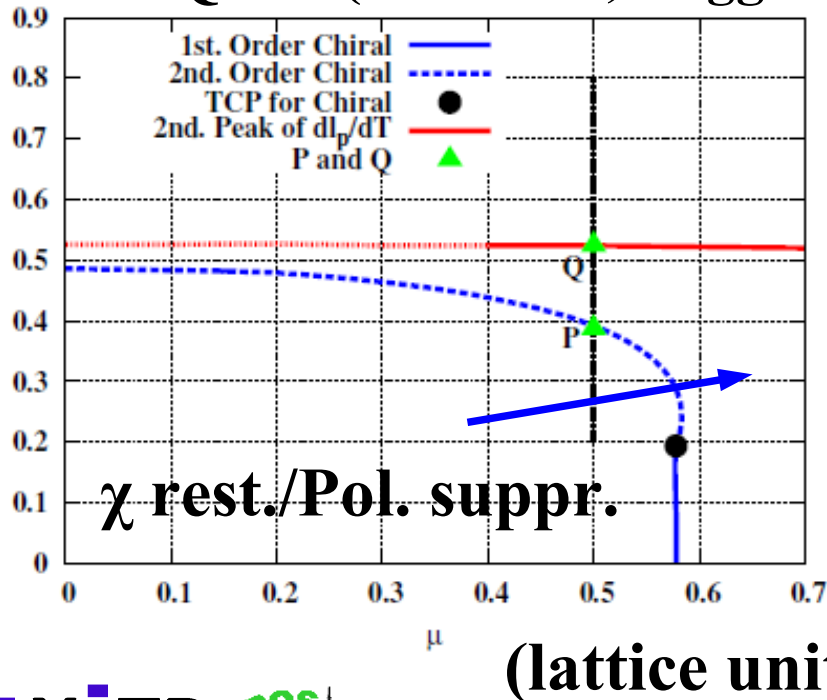
■ Does Quarkyonic matter exist in QCD with $N_c=3$?

→ There is χ restored & Polyakov loop suppressed region at low T and large μ in Strong Coupling Lattice QCD

■ Is there any site where Quarkyonic matter is formed ?

→ During the dynamical black hole formation, CP may be swept and quarkyonic matter may be formed.

P-SC-LQCD (NLO+LO, staggered)



Summary and Discussion

- P-SC-LQCD reproduces MC results of T_c at $\mu=0$, and predicts *Quarkyonic-like state in cold-dense matter*.
 - P-SC-LQCD: Strong coupling lattice QCD with Polyakov loop
 - Quarkyonic-like = χ restored & Polyakov loop suppressed matter
- Comparison of χ effective models & ν -radiation hydrodynamics suggests *the possibility of CP sweep during BH formation*.
 - TCP decreases with increasing $\delta\mu$.
 - Hadronic EOS favors large isospin chemical potential ($\delta\mu$).
(cf. neutral constraint in χ eff. models predicts smaller $\delta\mu$.)
- *Construction of Hadron-Quark matter EOS with CP and its application to BH formation are desired.*

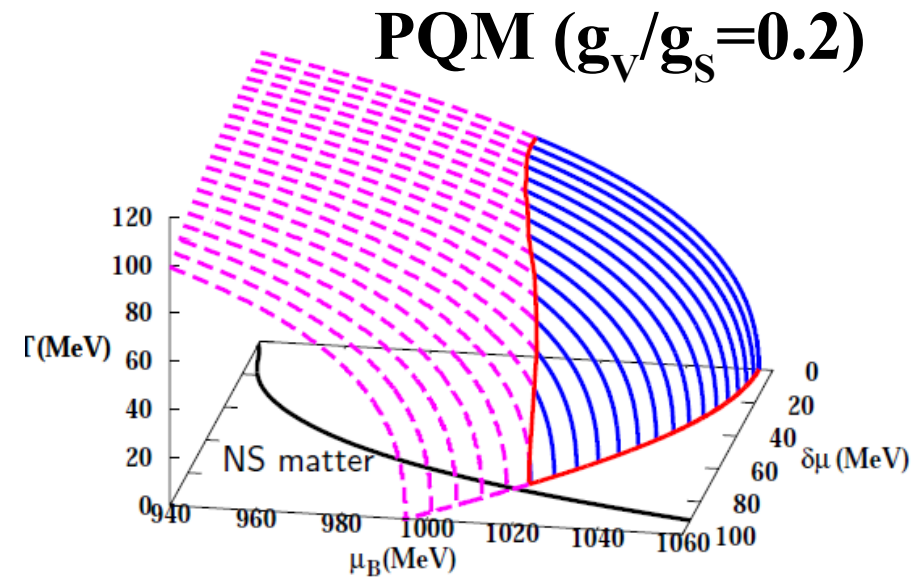
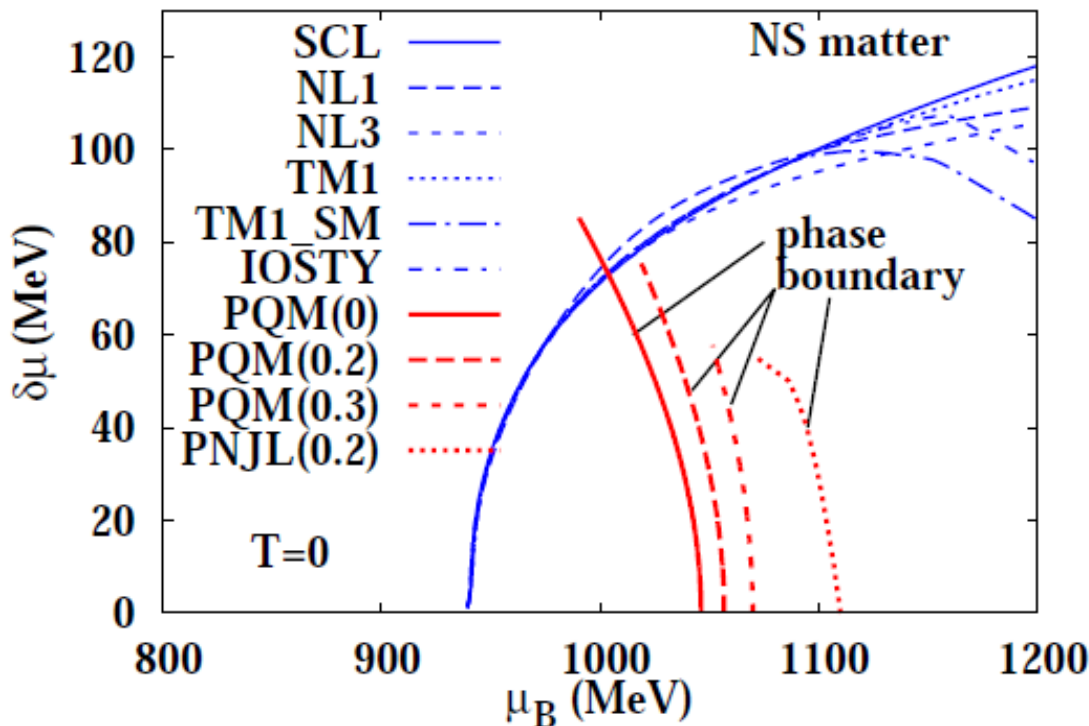
Thank you for your attention !

Collaborators

**K. Miura (Frascati), T.Z.Nakano (Kyoto U./YITP),
N. Kawamoto (Hokkaido U.)
H. Ueda (Kyoto U.), M. Ruggieri (YITP)
K. Sumiyoshi (Numazu), K. Tsubakihara (Hokkaido U.),
C. Ishizuka (Tokyo U. of Sci.),
S. Yamada (Waseda), H. Suzuki (Tokyo U. Sci.),**

Crossover in Neutron Star Matter ?

- 1st order phase transition disappears at $\delta\mu = (60-80)$ MeV
 → There may be no 1st order transition in NS.
- General trend of TCP decrease as a function of $\delta\mu$ is confirmed by using GL analysis (M. Ruggieri et al., in prep.) and in FRG analysis (K.Kamikado, in prep.)



H. Ueda, M. thesis