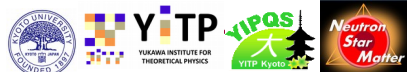
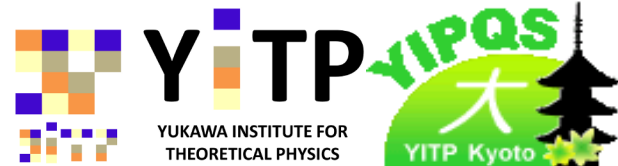
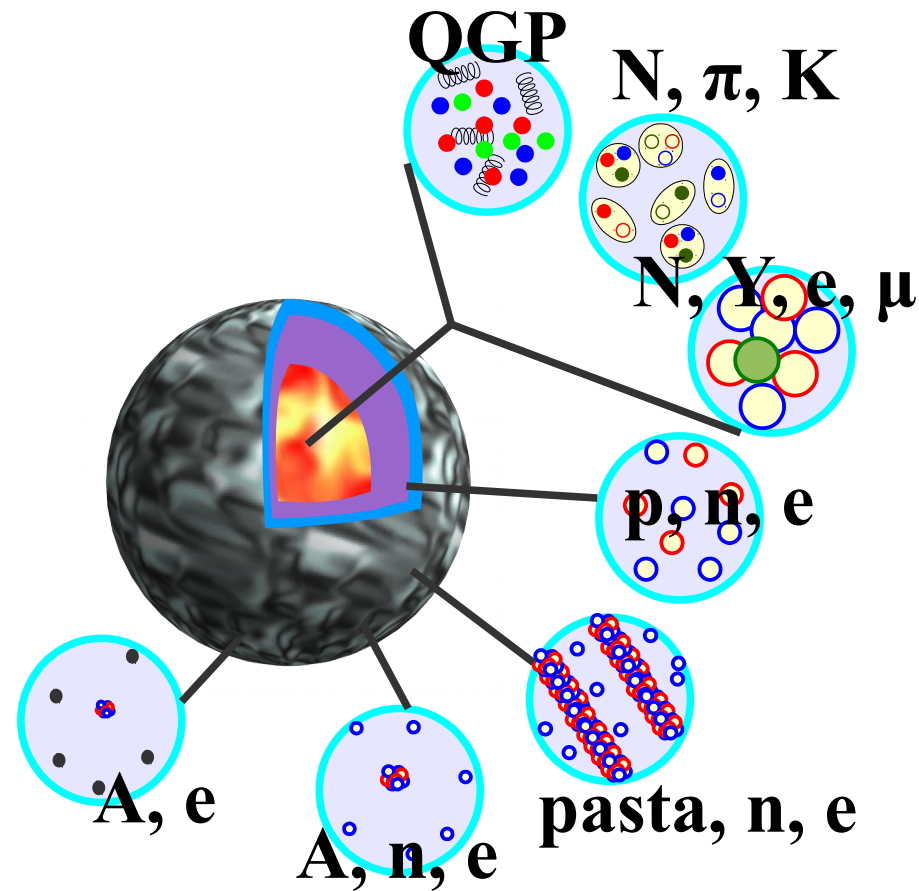
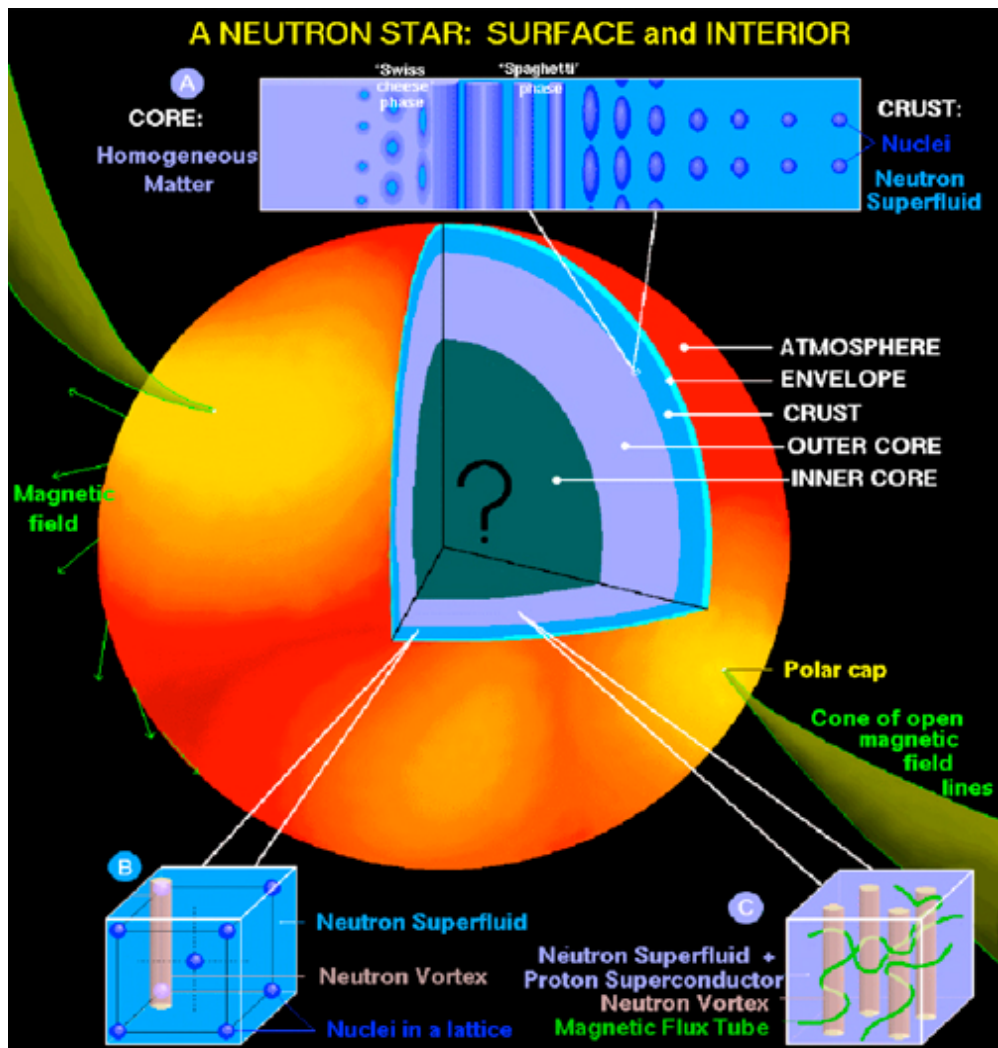

Theoretical developments in physics of neutron star matter (Report from Group D01)

Akira Ohnishi (YITP, Kyoto U.)

**International Symposium on
Neutron Star Matter 2016 (NSMAT2016)
Nov.21-23, 2016, Sendai, Japan**



Inside Neutron Stars



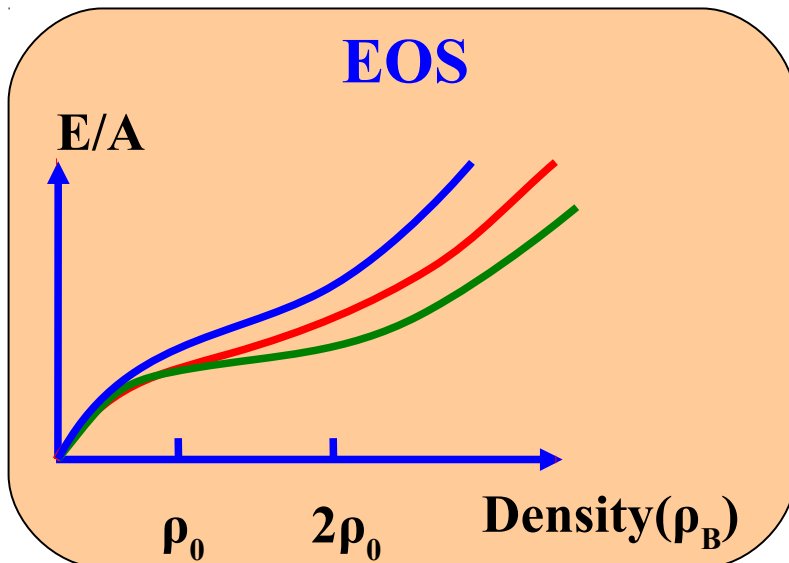
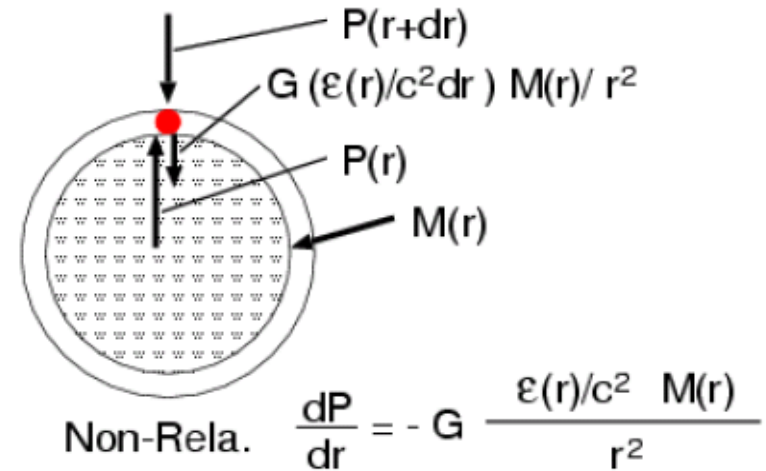
Dany Page

M-R curve and EOS

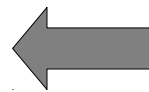
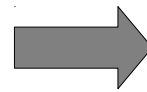
- M-R curve and NS matter EOS has 1 to 1 correspondence
 - TOV(Tolman-Oppenheimer-Volkoff) equation =GR Hydrostatic Eq.

$$\frac{dP}{dr} = -G \frac{(\epsilon/c^2 + P/c^2)(M + 4\pi r^3 P/c^2)}{r^2(1 - 2GM/rc^2)}$$

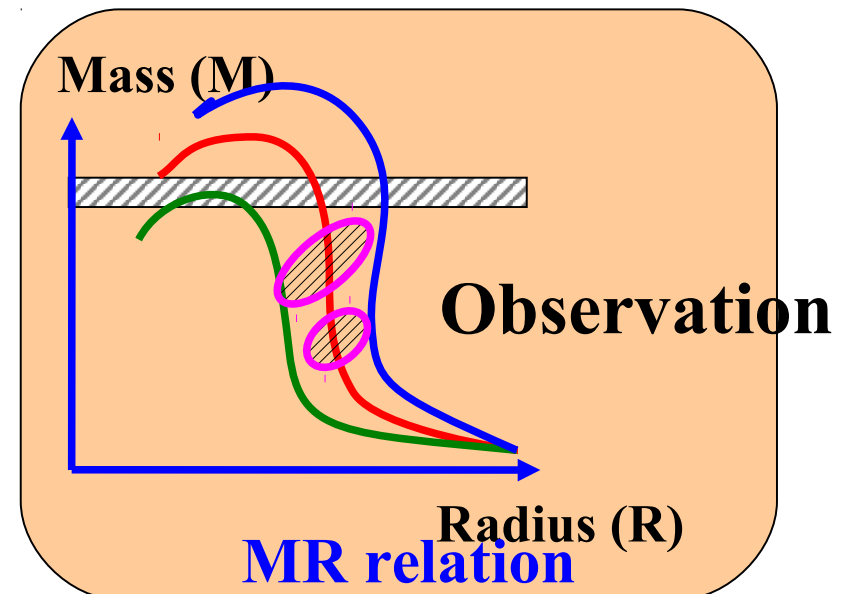
$$\frac{dM}{dr} = 4\pi r^2 \epsilon/c^2, \quad P = P(\epsilon) \quad (\text{EOS})$$



prediction



Judge



NS matter Grant-in-Aid Study (2012-2017)

High ρ (Group A)
PI: Tamura, Takahashi

Hypernuclei, Kaonic nuclei
YN & YY int.,
Eff. Interaction
(Heavy-ion collisions)

Hyperons, mesons, quarks

Asym. nuclear matter
+elec.+ μ

Nuclei+neutron gas+elec.

Nuclei + elec.

J-PARC



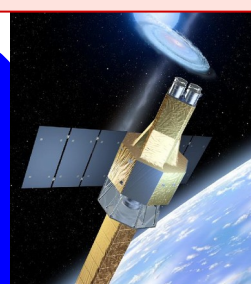
Area PI: H. Tamura

Low ρ (Group B)
PI: Murakami,
Nakamura, Horikoshi

NS Obs. (Group C)
PI: Takahashi

ASTRO-H

Radius, Mass,
Temp. (Cooling),
Star quake, Pasta



Sym. E, Pairing gap,
BEC-BEC cross over,
Cold atom, Unitary gas

RIBF



Theory (Group D)
PI: Ohnishi

Loaded ^6Li atoms

D01 members

- **Project members:**

A. Ohnishi, T. Harada, H. Nakada, K. Iida, M. Matsuo, M. Kimura, T. Tatsumi, A. Ono, A. Dote, K. Nakazato

- **Project PDs:**

H. Sotani, K. Morita, J. Yamagata-Sekihara, K. Tsubakihara, S. Ohnishi, T. Inakura, N. Ikeno, C. Ishizuka, T.-G. Lee

- **Research Collaborators:**

T. Kunihiro, S. Nishizaki, K. Oyamatsu, T. Maruyama, H. Abuki, Y. Ohashi, N. Shibasaki, Y. Yamamoto, T. Takatsuka, M. Kohno, T. Miyagawa, T. Muto, K. Sumiyoshi, H. Sagawa

- **Proposed Project PIs:**

K. Hagino, H. Nemura, K. Kiuchi, N. Yasutake, Y. Ohashi, M. Nitta, H. Sotani, T. Furumoto

Challenges in Neutron Star Physics

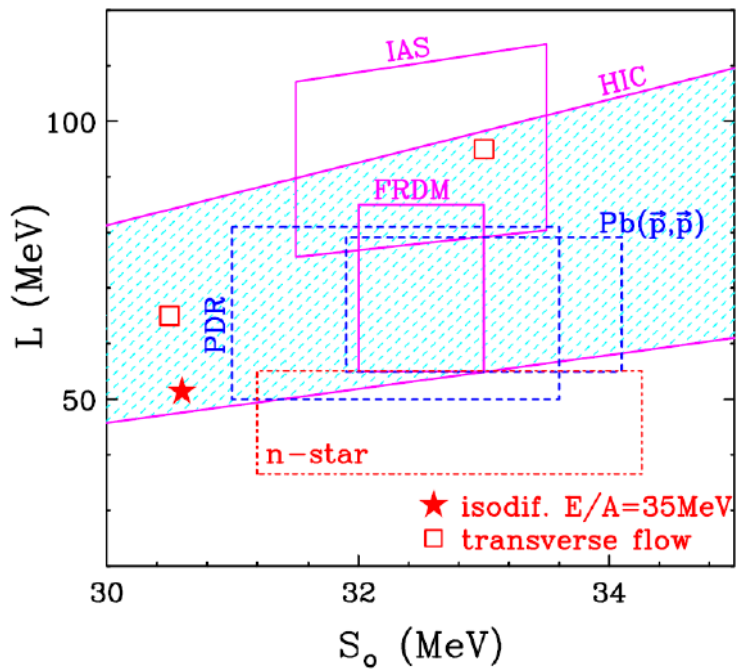
- **Symmetry Energy**
 - Symmetry Energy Parameters (S0, L)
 - Symmetry Energy at Supernuclear densities
 - Effects of Symmetry Energy on NS matter EOS
- **Relation of Neutron Star Matter and Cold Atom**
 - Low density Neutron Matter EOS and Cold Atom EOS
- **Strangeness in Nuclear Matter**
 - Hyperons and anti-Kaons in Nuclear Matter
- **NS Matter EOS**
 - Mass and Radius of Neutron Stars
 - Hyperon Puzzle
 - Do we have quark matter in NS ?
- **NS astrophysics: QPO, Cooling, Glitches, Magnetic field, ...**

Symmetry Energy

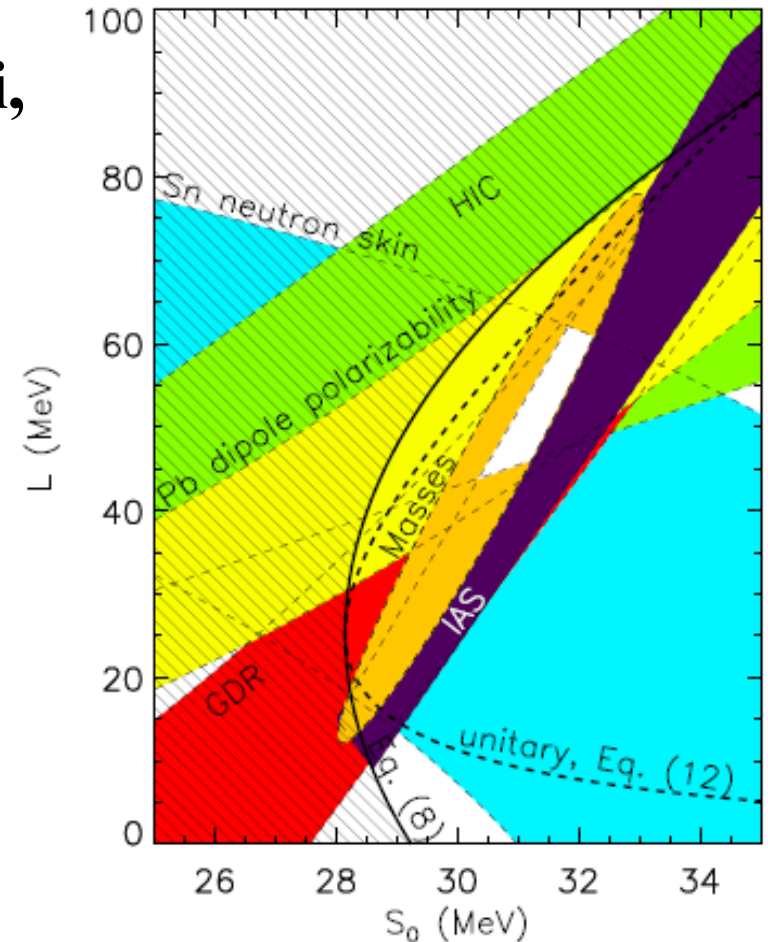
■ Symmetry Energy Parameters

$$S(u) = S_0 + \frac{L}{3} (u-1) + \frac{K_{\text{sym}}}{18} (u-1)^2 + \mathcal{O}[(u-1)^3] \quad (\mathbf{u=n/n_0})$$

(Nakamura, Li, Trautmann, Murakami, Ono, Zenihiro, Colo, Aumann, Tamii, Inakura)



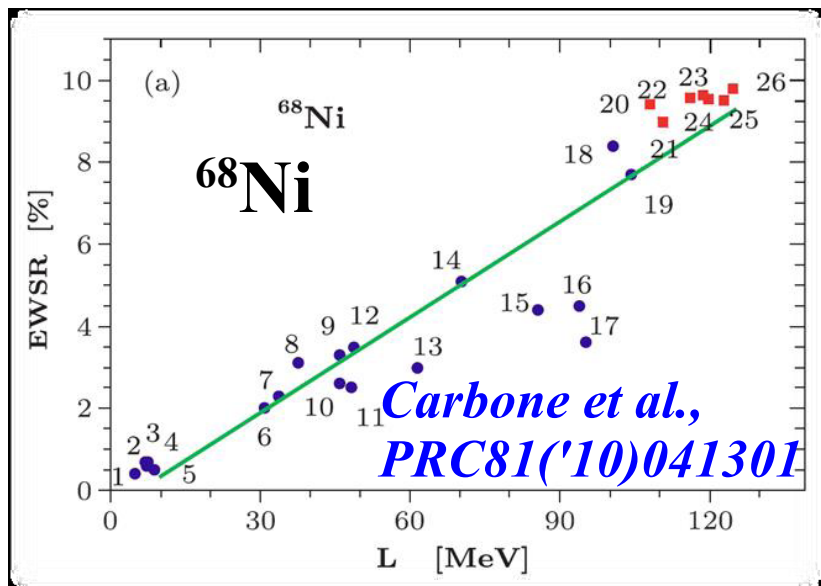
Tsang et al. ('12): NuSYM 2011



*Lattimer, Lim ('13), Lattimer, Steiner ('14)
Kolomeitsev, Lattimer, AO, Tews ('16)*

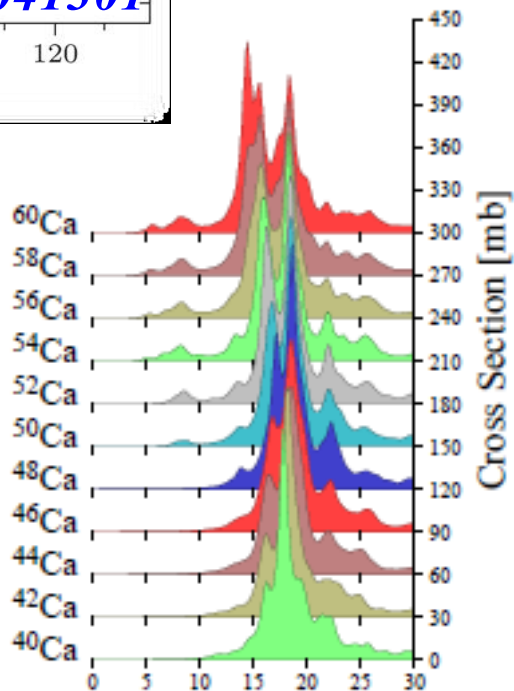
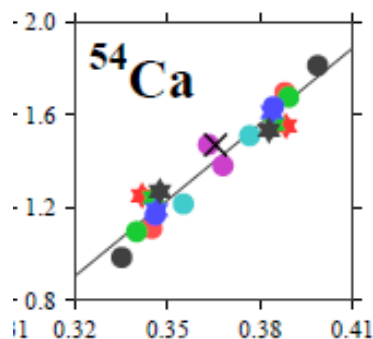
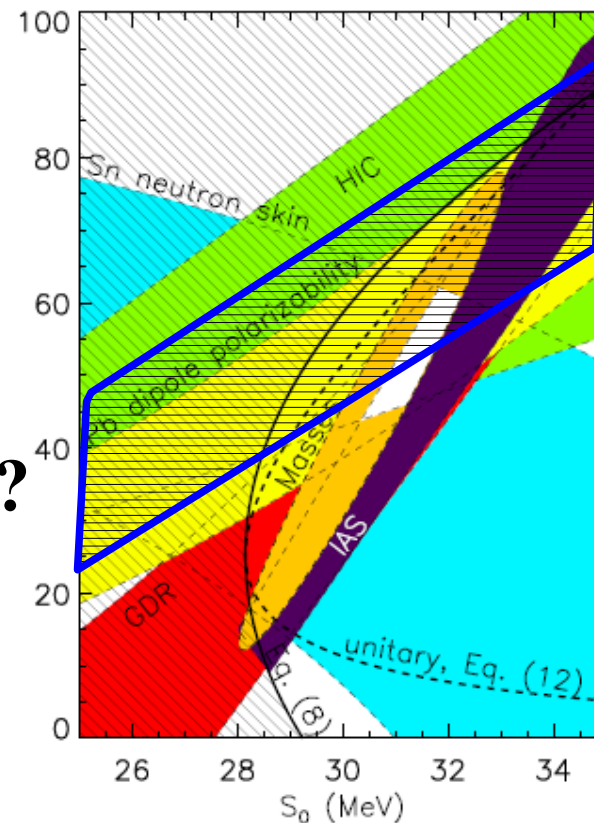
Low Energy Dipole Strength

Low Energy Dipole Strength and L (Nakamura, Inakura, Colo, Aumann)



Nakamura
(B02)

→ L (MeV)
???

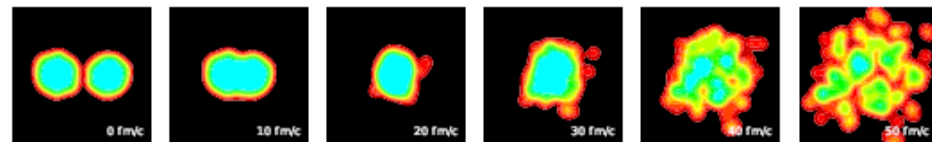


Let's wait for B02
experiments !

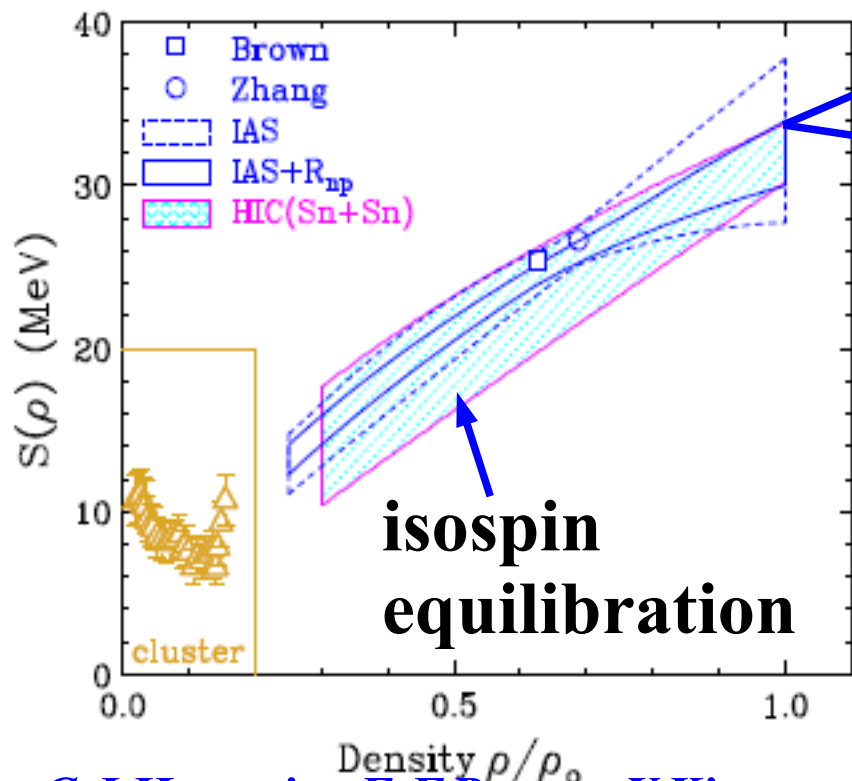
High Density Symmetry Energy

- Symmetry energy at $\rho=(2-4) \rho_0$ dominantly determines NS radius.

→ Central Heavy-Ion collisions at a few 100 MeV !

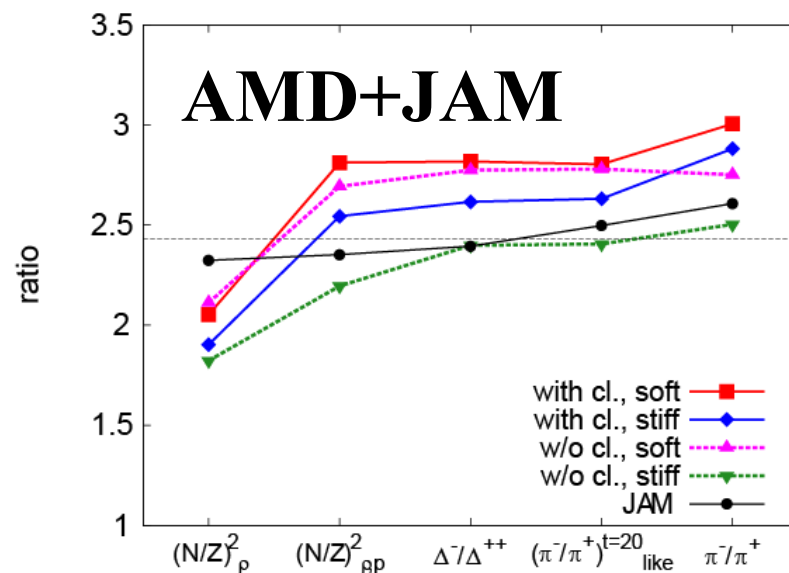


(Li, Trautmann, Murakami, Ono)



Let's wait for SπRIT B01 results (Murakami) ! More theor. work needed.

π^-/π^+
B.A.Li

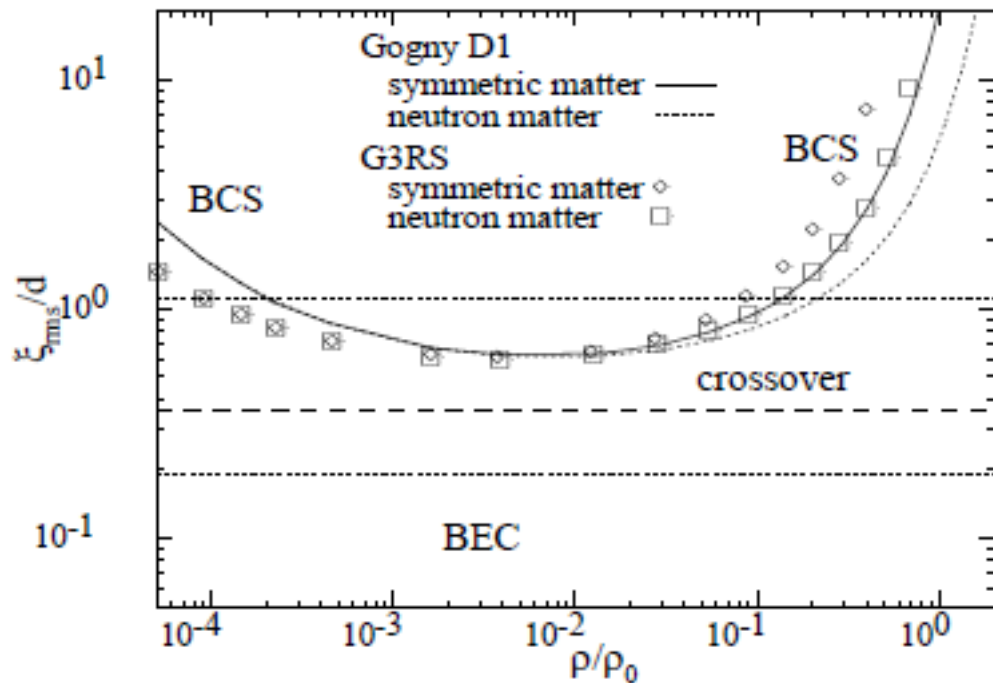


C.J.Horowitz, E.F.Brown, Y.Kim, W.G.Lynch, R.Michaels, A. Ono, J. Piekarewicz, M. B. Tsang, H.H.Wolter (NuSYM13), JPG41('14) 093001

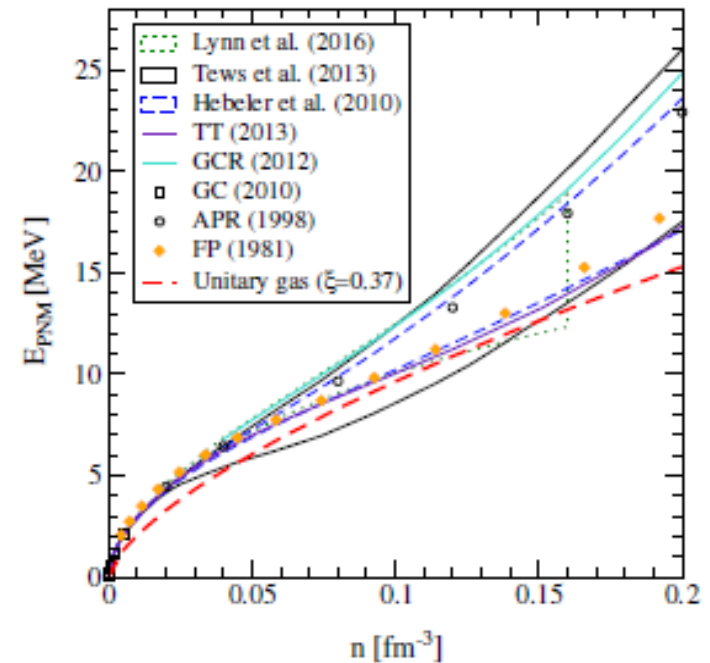
Ikeno, Ono, Nara, AO ('16)

Cold Atom around crossover and Neutron Matter

- Neutron matter at low $\rho \sim$ Unitary gas ($1/a_0 k_F \rightarrow 0, r_{\text{eff}} k_F \rightarrow 0$) (Tan, Horikoshi, Ohashi)
 - Large nn scattering length ($a_0=18.9 \text{ fm} \rightarrow 1/a_0 k_F = 0.03$ at ρ_0)
 - Cooper pair rms radius \sim nn average distance
- Unitary gas E. \sim Lower bound of neutron matter E. (Conjecture)



M.Matsuo, PRC73('06)044309



Kolomeitsev, Lattimer, AO, Tews ('16)
arXiv:1611.07133 (today !)

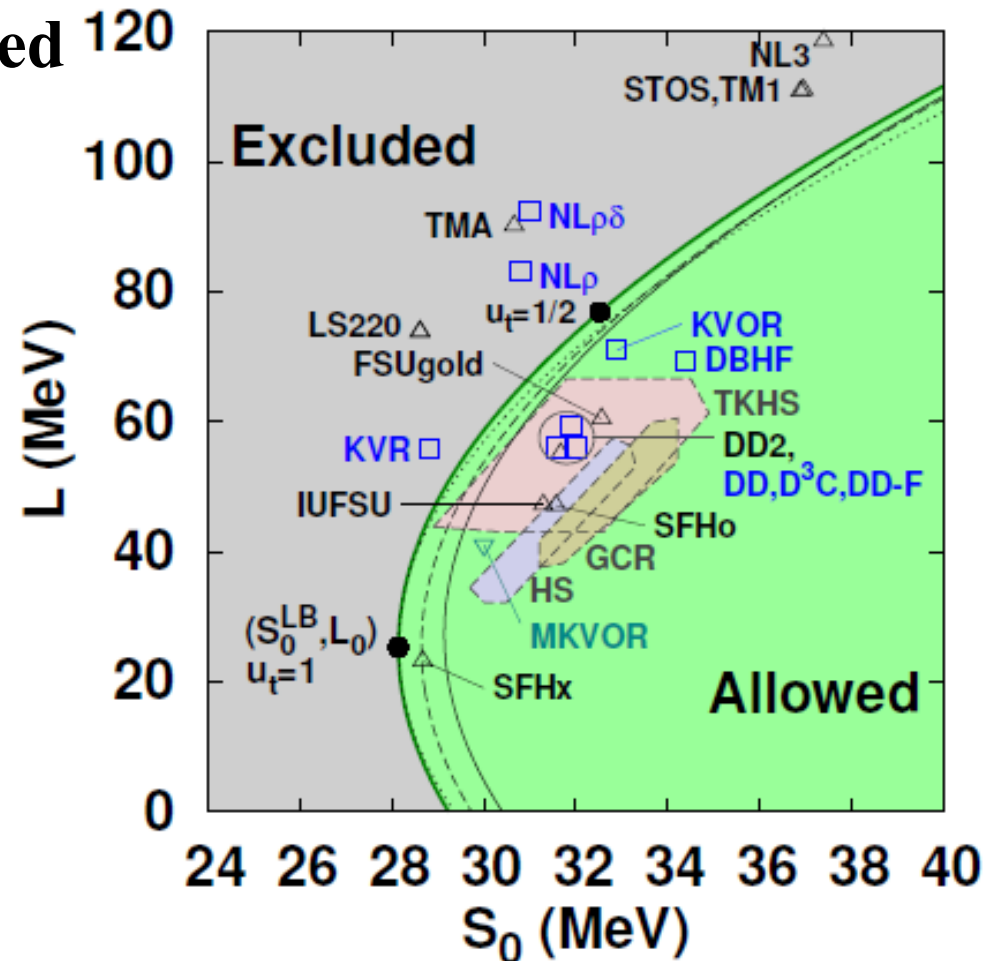
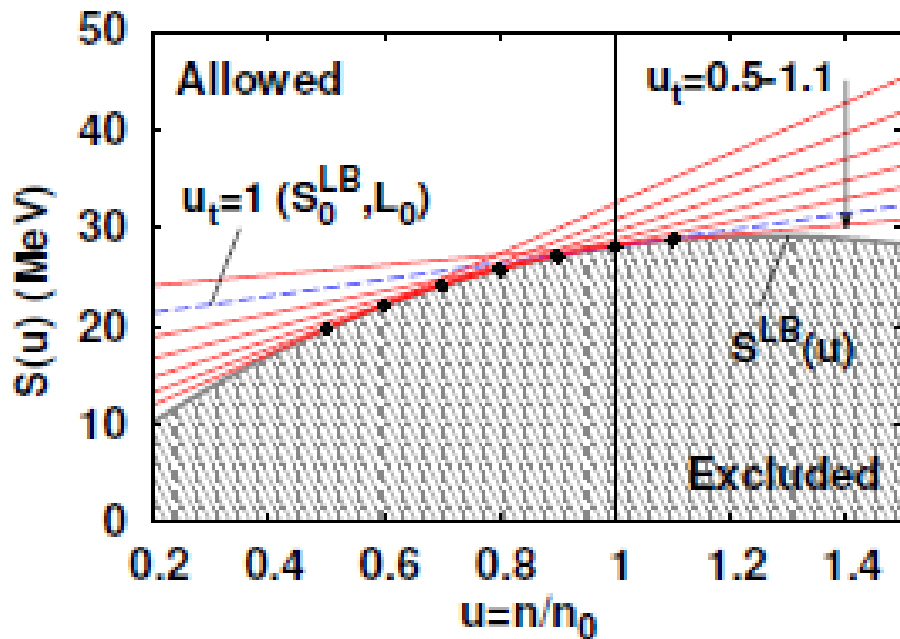
Unitary gas constraint on symmetry energy parameters

- Conjecture: $E(\text{neutron matter}) > E(\text{unitary gas})$

$$S(u) \geq E_{\text{UG}}^0 u^{2/3} - \left[E_0 + \frac{K}{18} (u - 1)^2 \right] \equiv S^{\text{LB}}(u)$$

→ Sym. E. parameters are constrained !

- Many tabulated EOSs are excluded
Fisher et al.('14), Klahn et al.('06)

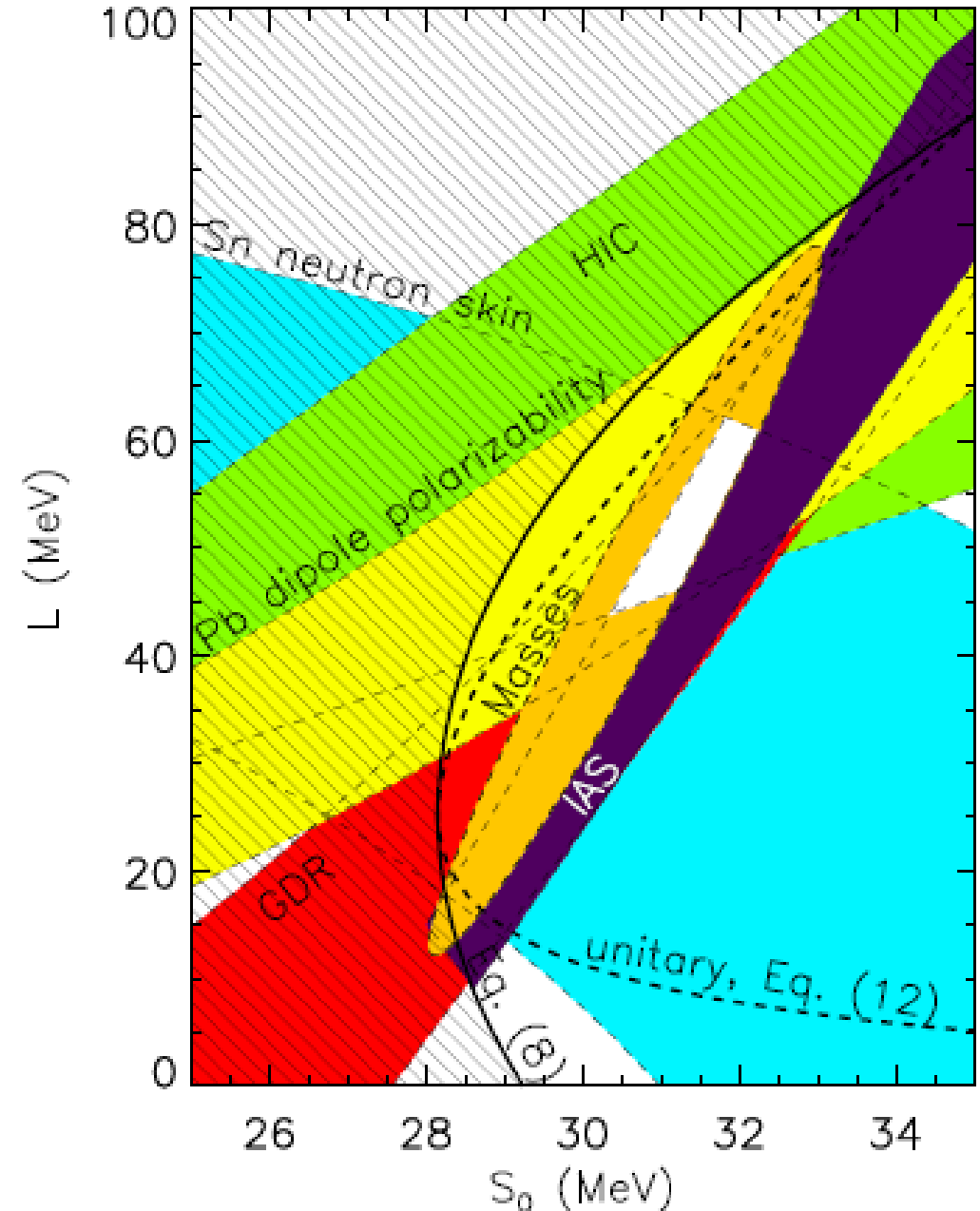


Kolomeitsev, Lattimer, AO, Tews ('16)

Unitary gas constraint on symmetry energy parameters

- Unitary gas constraint is consistent with experimental constraints.

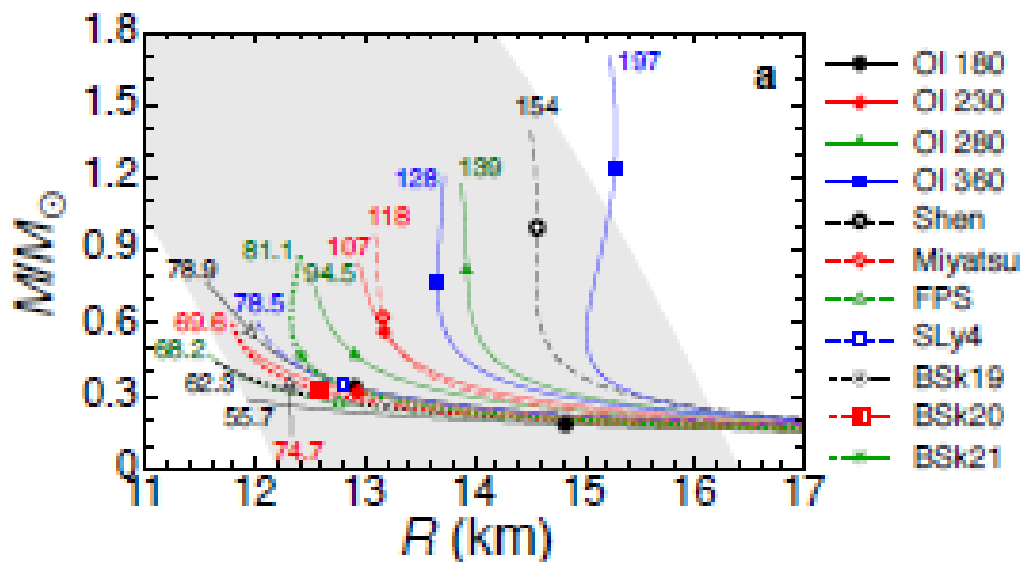
Does Cold atom EOS with finite $1/a_0 k_F$ constrain (S_0, L) more severely ?
Horikoshi, Ohashi
We need more works !



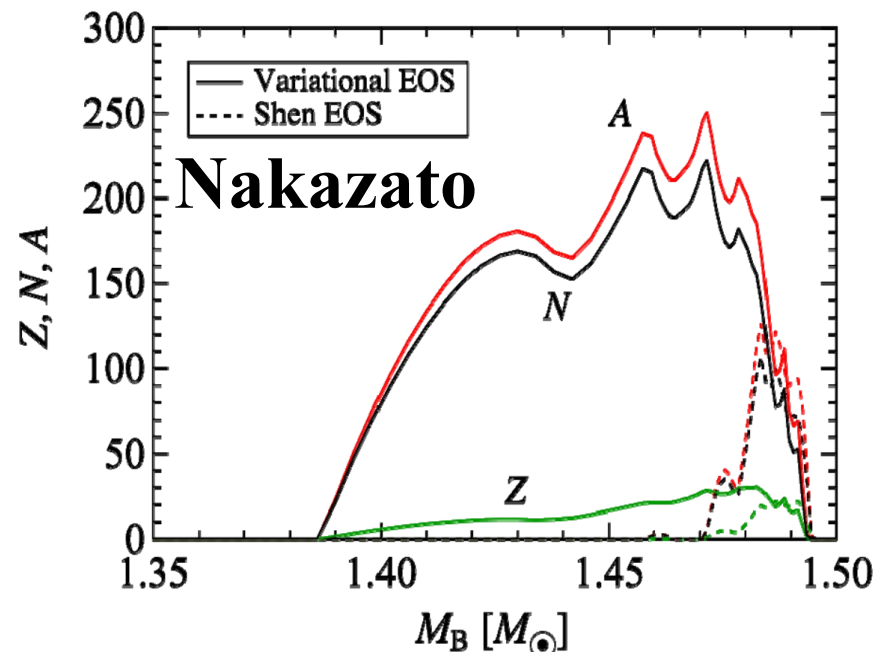
Kolomeitsev, Lattimer, AO, Tews ('16)

Symmetry Energy \rightarrow Neutron Star

- Sym. E dominantly determines NS radius. *Lattimer, Prakash('01)*
- What is the role of K (incompressibility) ?
 \rightarrow With EOS fitted to finite nuclear masses and radii,
 $\eta = (KL^2)^{1/3}$ determines low mass NS radii !
- Small L enlarges the density range of pasta phase
 Shen EOS (L=111 MeV) \rightarrow Variational EOS (L=35 MeV)
- NS torsional oscillation remains as a problem.



Sotani, Iida, Oyamatsu, AO ('14)



Strangeness Nuclear Physics

■ Before Oct.2010,

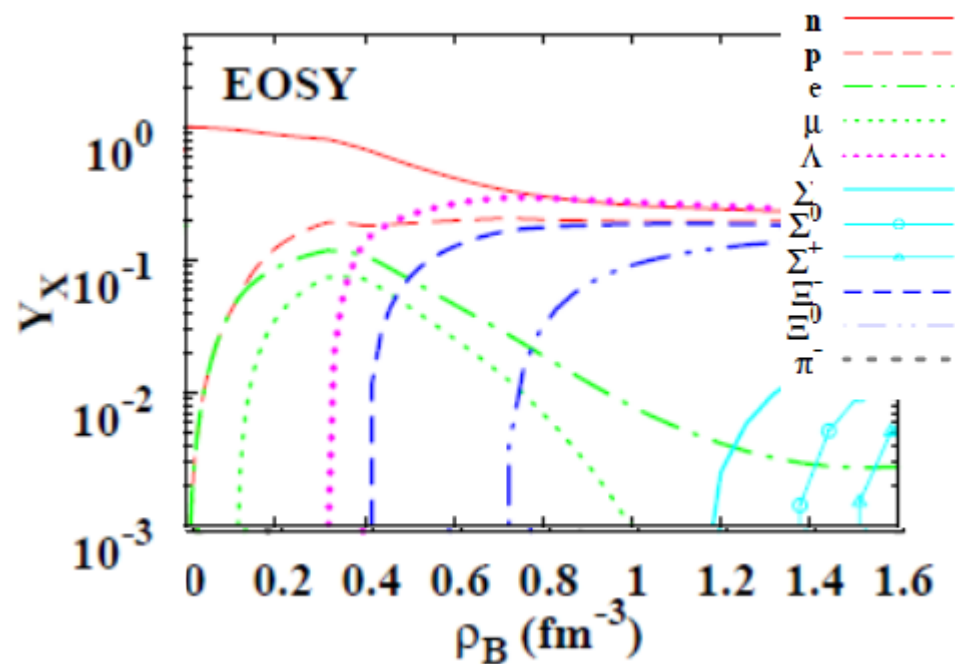
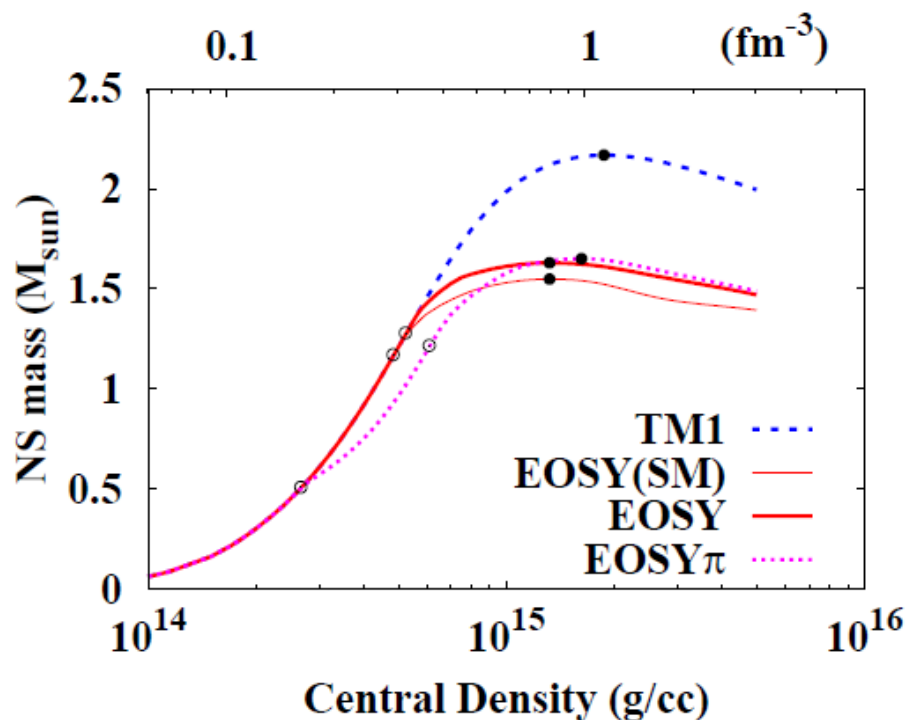
$$U_{\Lambda}(\rho_0) \sim -30 \text{ MeV}, U_{\Sigma}(\rho_0) > +20 \text{ MeV}, U_{\Xi}(\rho_0) \sim -14 \text{ MeV}$$

Harada, Hirabayashi ('05), Noumi et al. ('02),

Fukuda et al. PRC58('98),1306; Khaustov et al. PRC61('00), 054603;

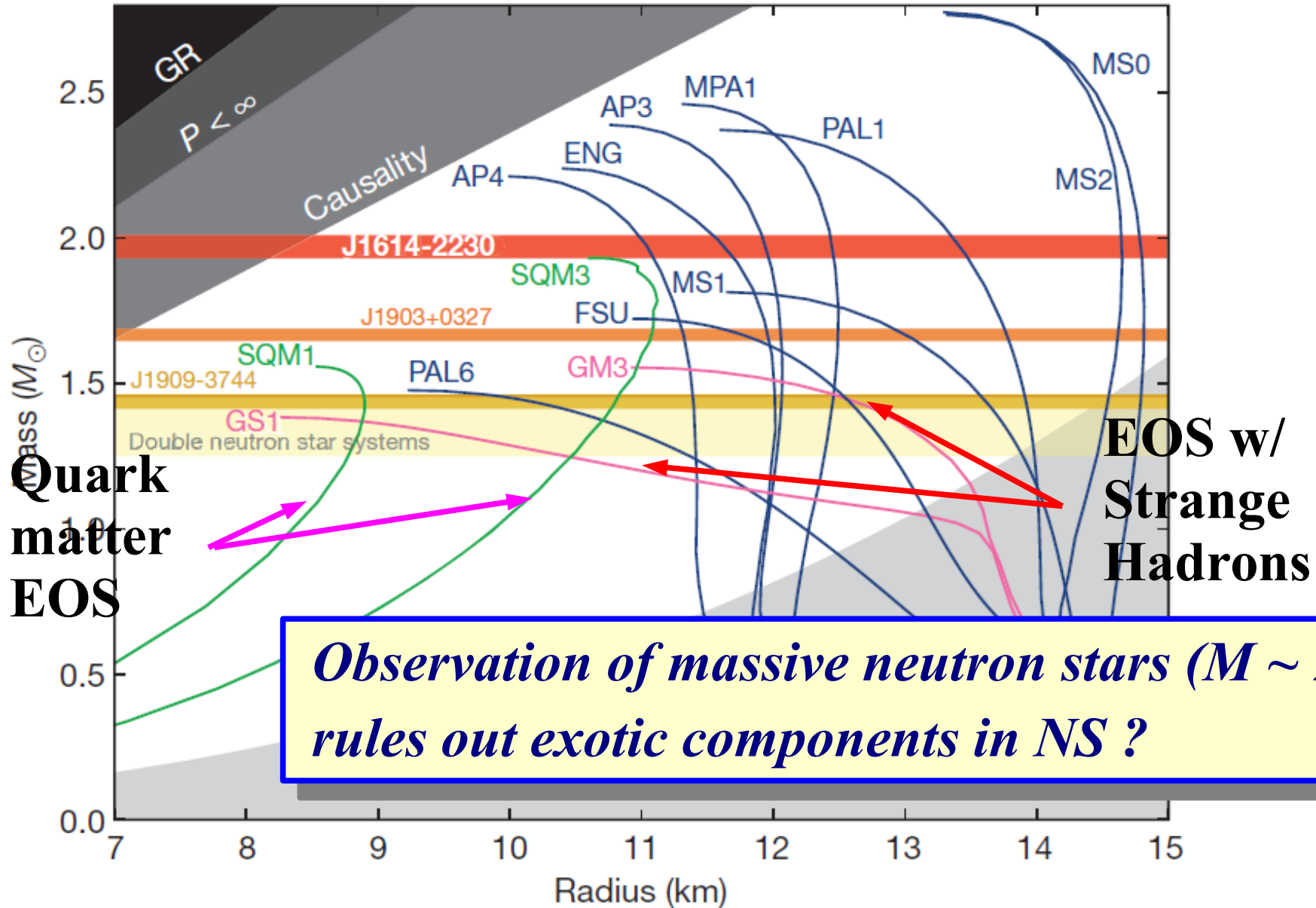
Aoki et al. PLB355('95),45.

→ **Maximum mass of NS $\sim 1.6 M_{\odot}$**



Ishizuka, AO, Tsubakihara, Sumiyoshi, Yamada ('08)

Hyperon Puzzle



PSR J1614-2230: $1.97 \pm 0.04 M_{\odot}$ *Demorest et al., Nature 467('10)1081 (Oct.28, 2010).*

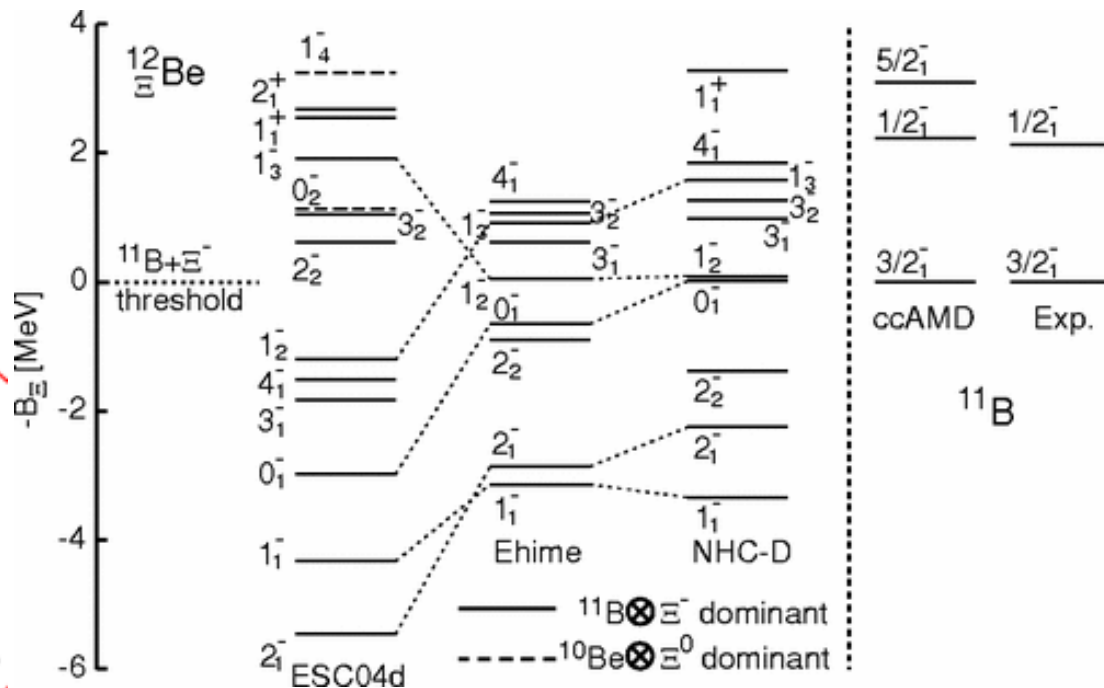
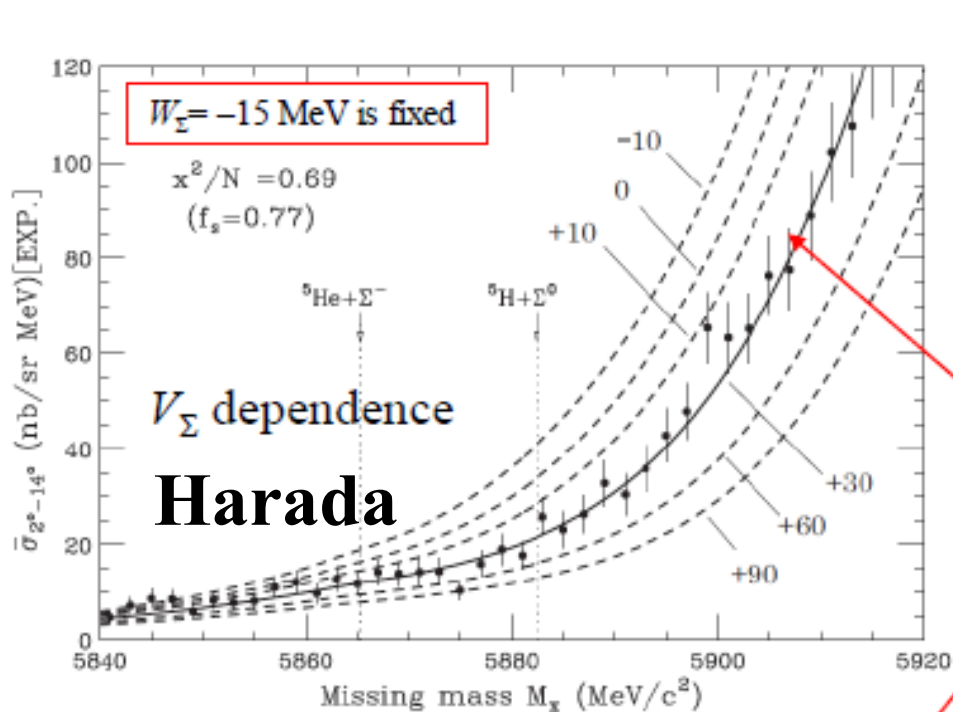
PSR J0348+0432: $2.01 \pm 0.04 M_{\odot}$ *Antoniadis et al., Science 340('13)1233232.*

What did we miss ?

- **Hyperon potential in nuclear matter ?**
 - $U_{\Lambda}(\rho_0) \sim -30 \text{ MeV}, U_{\Sigma}(\rho_0) > +20 \text{ MeV}, U_{\Xi}(\rho_0) \sim -14 \text{ MeV}$
- **Hyperon-Hyperon potential ?**
 - If vacuum $\Lambda\Lambda$ potential is much more attractive than Nagara event implies, $\Lambda\Lambda N$ potential must be very repulsive.
- **Kaon potential in nuclear matter ?**
- **Three-baryon (3B) interaction ?**
- **Quark matter core ?**
- **Modified gravity ?**

Σ or Ξ potential in nuclei ?

- New analysis of Σ production reaction: ${}^6\text{Li} (\pi^-, \text{K}^+) \Sigma^- {}^5\text{He}$ (Honda, Harada)
 - $U_\Sigma \sim +30 \text{ MeV}$ (consistent)
- New Ξ hypernuclei → B.E. = 9 MeV & 1 MeV (Takahashi (A01), Nakazawa, Kanatsuki, Yamamoto)
 - Deeper than previous estimate !



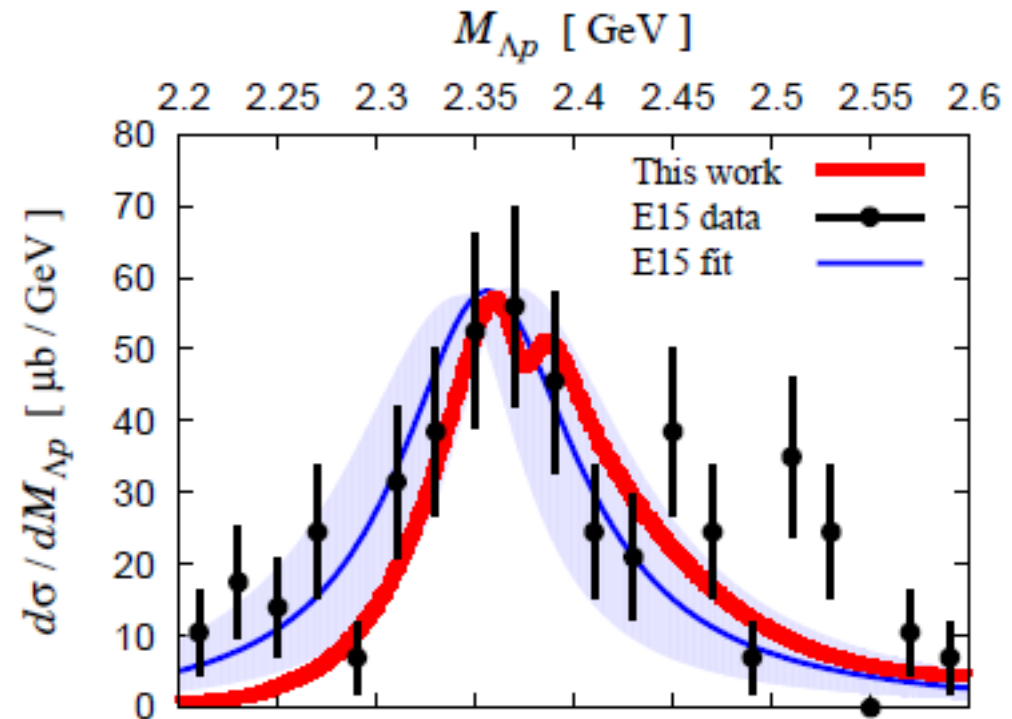
Matsumiya, Tsubakihara, Kimura, Dote, AO ('11)

Anti-Kaon potential in Nuclear Matter ?

- K^-pp binding energy (Takahashi (A02), Outa, Dote)
 - E15: One state at B.E.~ (15-30) MeV, Strength at B.E. ~ 100 MeV
E27: B.E.~100 MeV ?
 - Dote: Higher pole B.E.~ 27 MeV, Lower pole B.E.~ 79 MeV (?)
Akaishi: B.E. ~ 100 MeV (DISTO, FINUDA)
S. Ohnishi: Saturating B.E. in heavier kaonic nuclei

*We need more work
to confirm the fate of
Kaon condensation*

Muto



Sekihara, Oset, Ramos ('16)

A. Ohnishi @ NSMAT 2016, Nov.23, 2016 18

$\Lambda\Lambda$ potential ?

- Nagara fit $\rightarrow a_0(\Lambda\Lambda) = -0.575$ fm or -0.77 fm

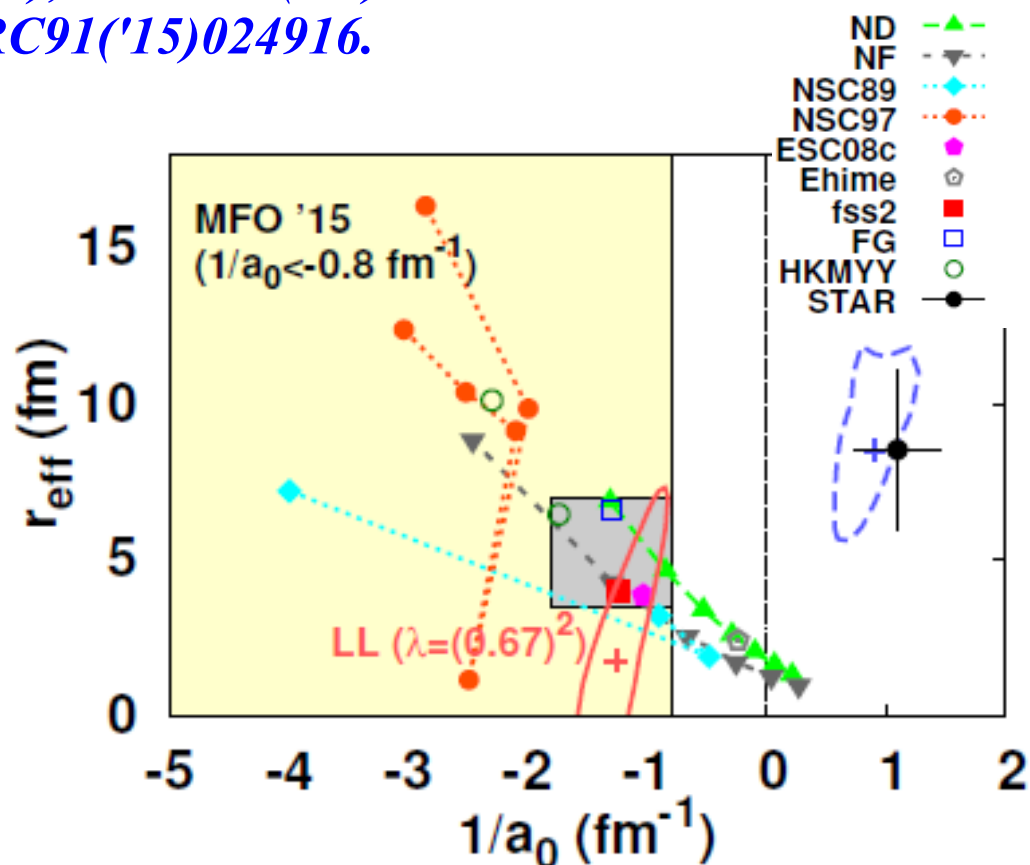
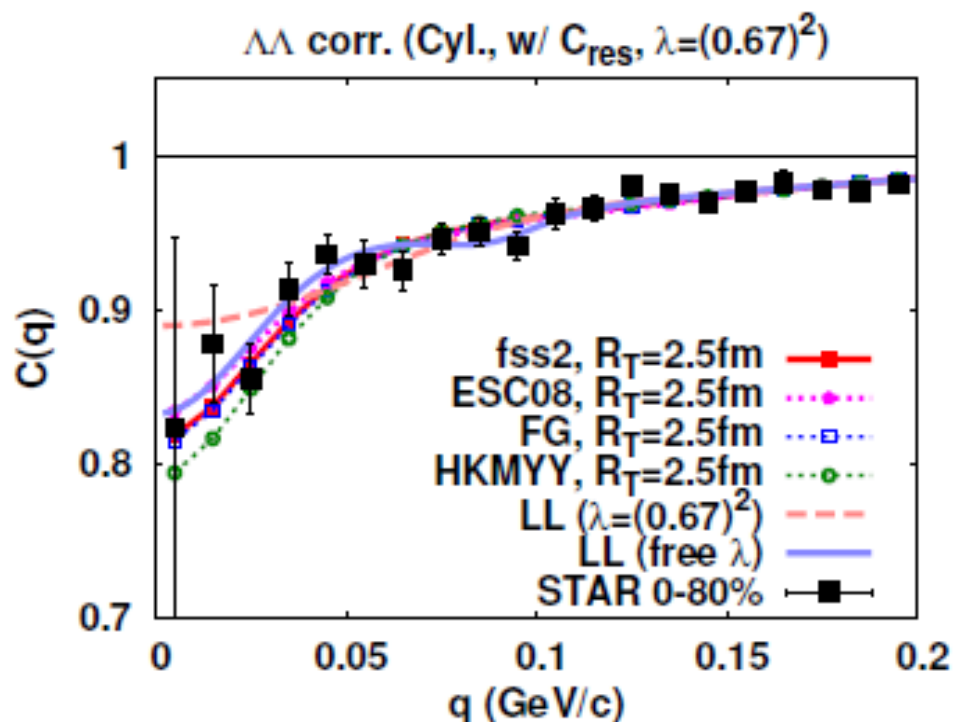
Hiyama, Kamimura, Motoba, Yamada, Yamamoto ('02), Filikhin, Gal ('02)

- New approach: $\Lambda\Lambda$ correlation from HIC (Morita)

$\rightarrow -1.25$ fm $< a_0(\Lambda\Lambda) < 0$ (Consistent with Nagara)

Exp: Adamczyk et al. (STAR Collaboration), PRL 114 ('15) 022301.

Theor.: Morita et al., T. Furumoto, AO, PRC91('15)024916.



Remaining possibilities

■ Three-baryon (3B) interaction ?

● “Universal” 3B repulsion

Nishizaki, Takatsuka, Yamamoto ('02), Tamagaki ('08), Yamamoto, Furumoto, Yasutake, Rijken ('13)

● Repulsive Λ NN potential (or density dep. Λ N pot.)

Lonardonì, Lovato, Gandolfi, Pederiva ('15), Togashi, Hiyama, Yamamoto, Takano ('16), Tsubakihara, Harada, AO ('16)

● Medium modification of baryons (Quark Meson Coupling model)

J.Rikovska-Stone, P.A.M.Guichon, H.H.Matevosyan, A.W.Thomas ('07), Miyatsu, Yamamuro, Nakazato ('13)

■ Quark matter NS core ?

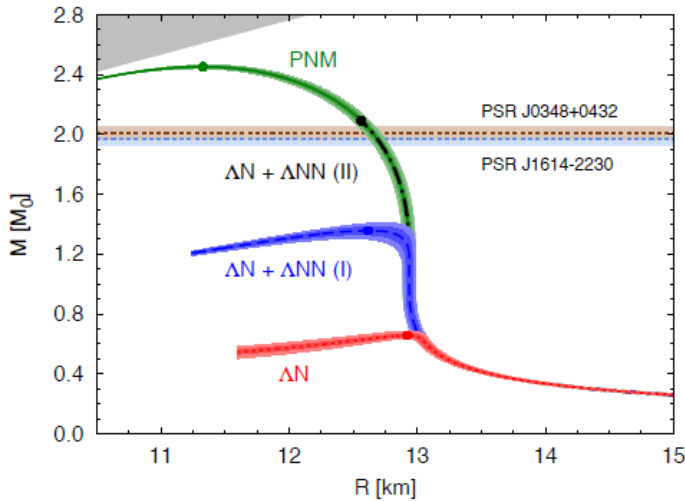
● First order phase transition

L. Bonanno, A. Sedrakian, Astron. Astrophys. 539 (2012) A16; M. Bejger, D. Blaschke, P. Haensel, J. L. Zdunik, M. Fortin, arXiv:1608.07049.

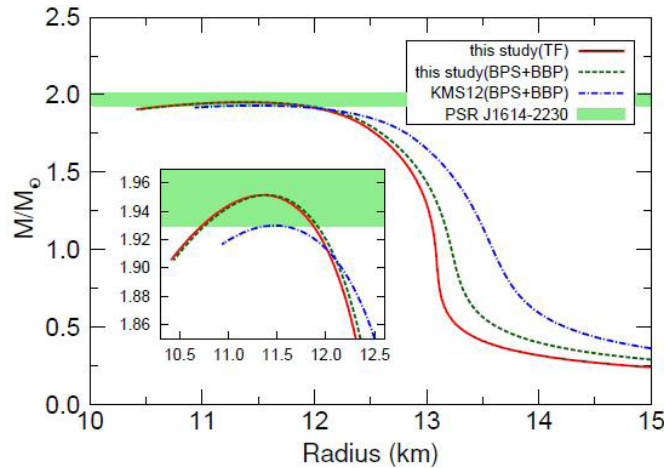
● Crossover transition to quark matter *Masuda, Hatsuda, Takatsuka ('12)*

■ Modified Gravity *Astashenok et al. ('14), M.-K. Cheoun's talk*

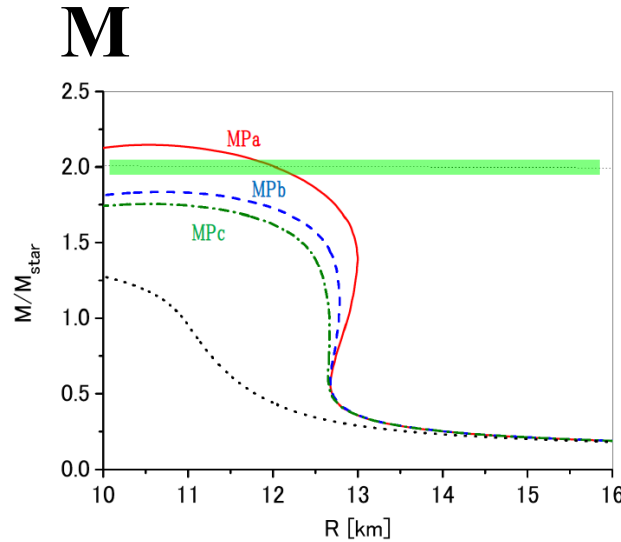
Hyperon Puzzle



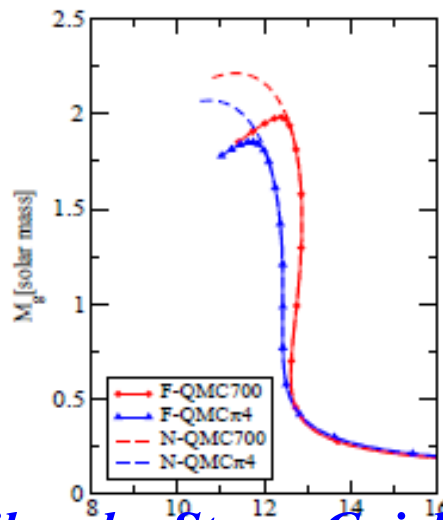
*Lonardonì, Lovato,
Gandolfi, Pederiva ('15),*



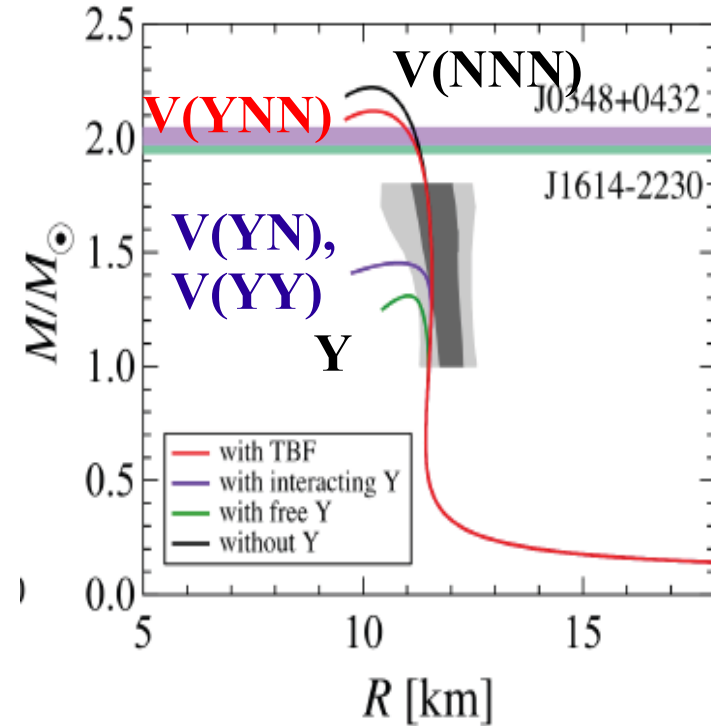
*QMC, Miyatsu, Yamamuro,
Nakazato ('13)*



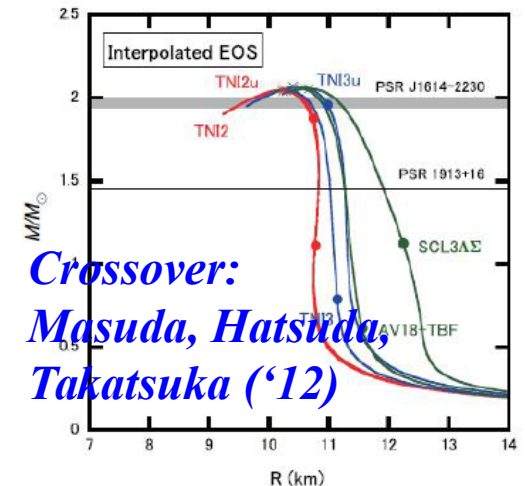
*Yamamoto, Furumoto,
Yasutake, Rijken ('13)*



*Rikovska-Stone, Guichon,
Matevosyan, Thomas ('07),*



*Togashi, Hiyama, Takano,
Yamamoto ('16).*



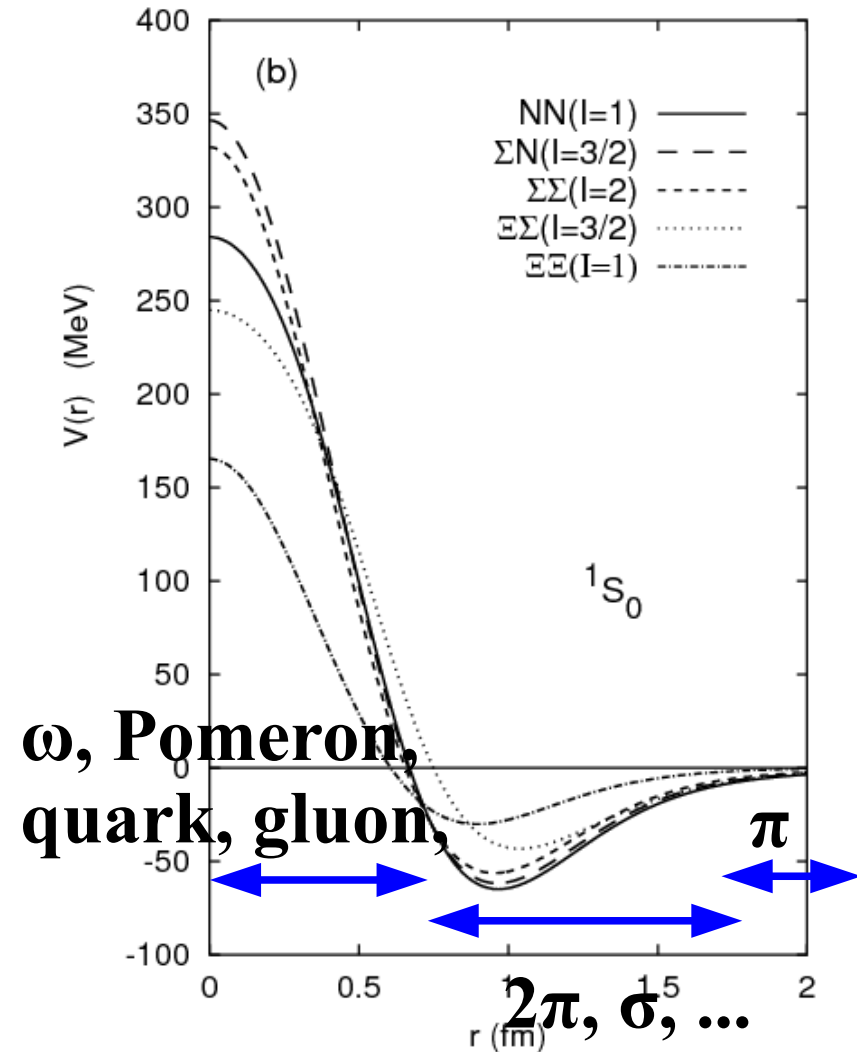
*Crossover:
Masuda, Hatsuda,
Takatsuka ('12)*

What is the origin of repulsive 3B force

- Short range ($r < 0.6$ fm) core of 2B force
vector boson exch., Pomeron exch.,
quark exclusion + one gluon exch., ...

*We may need quark-gluon DOF
to understand 3B repulsion.*

*→ Quark Meson Coupling
(Thomas),
Lattice QCD 3B force
(HAL QCD),
Quark Cluster model
(Nakamoto)*



*Fujiwara, Suzuki,
Nakamoto ('07)*

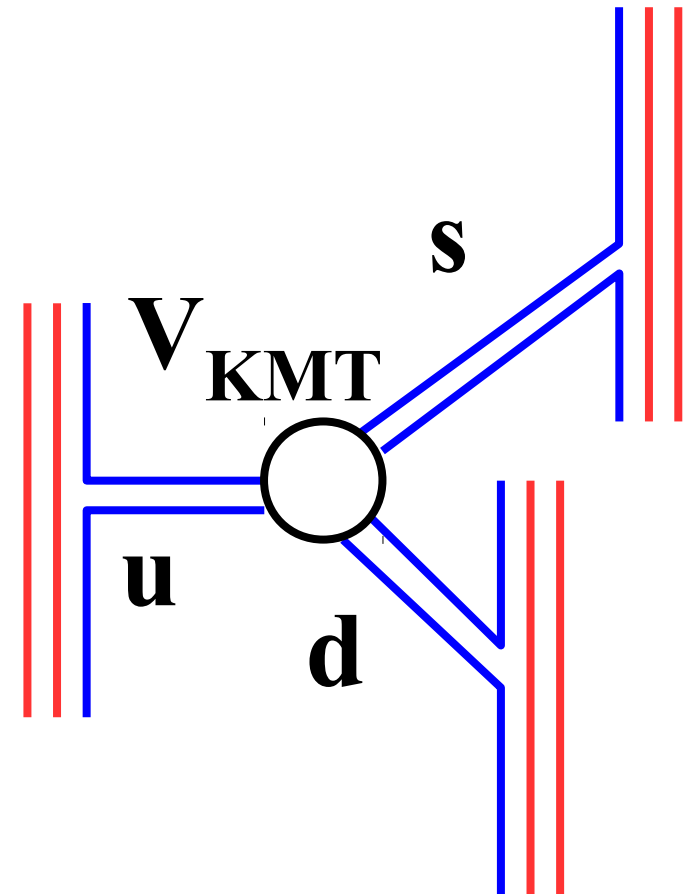
From 3-quark int. to 3B force

■ KMT interaction

Kobayashi, Maskawa ('70), 't Hooft ('76)

$$\mathcal{L} = g_D (\det \Phi + \text{h.c.}) , \quad \Phi_{ij} = \bar{q}_j (1 - \gamma_5) q_i$$

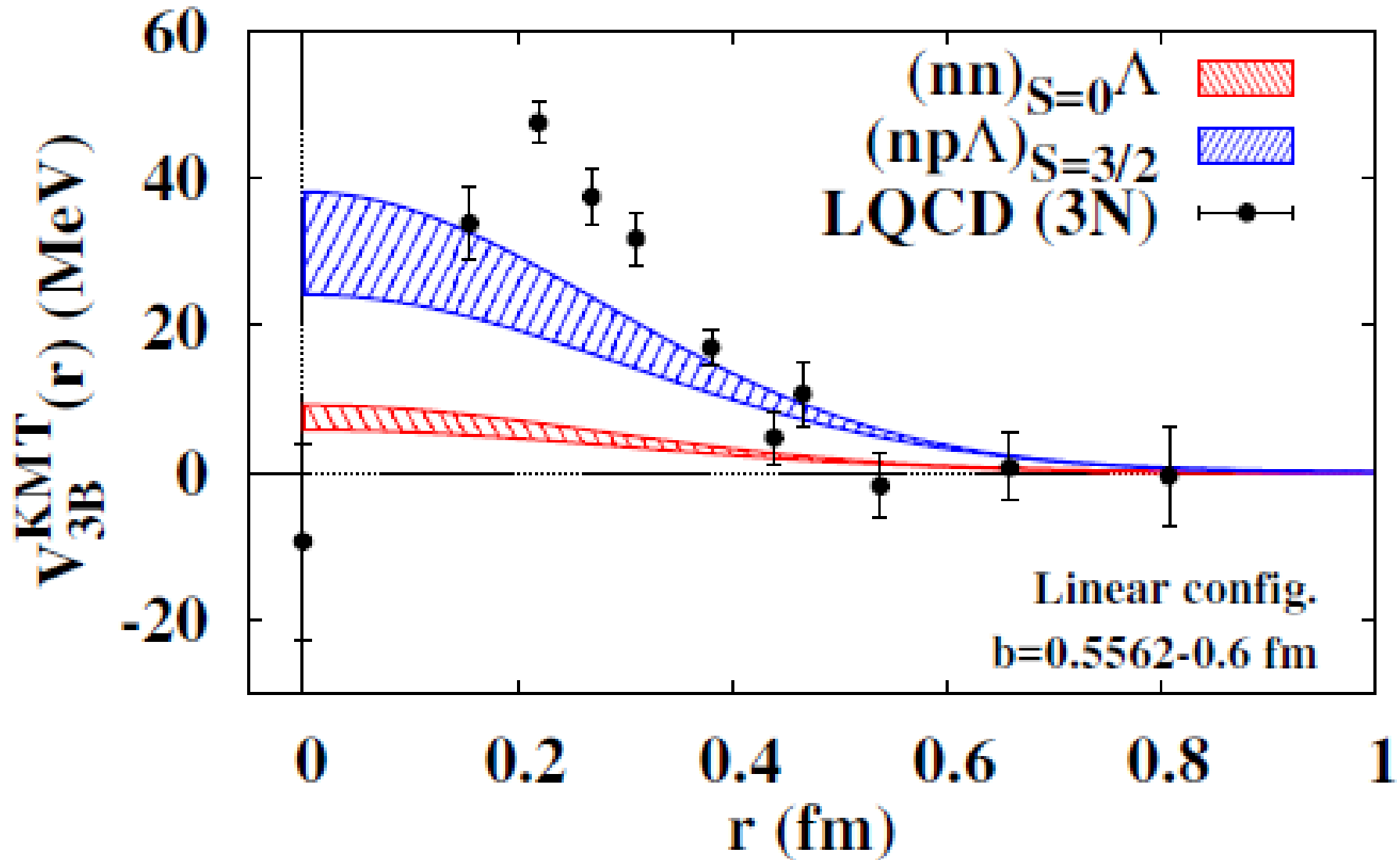
- Responsible for $U(1)_A$ anomaly
- 3-body int. among u,d,s quarks
- g_D is fixed by η - η' mass diff.
 - $g_D = -9.29$ *Hatsuda, Kunihiro ('94)*
 - 12.36 *Rehberg, Klevanski, Hufner ('96)*
- Repulsive in $\Lambda\Lambda$ system
 - Pushes up H particle energy.
 - Takeuchi, Oka ('91)*



Does the anomaly support NS ?

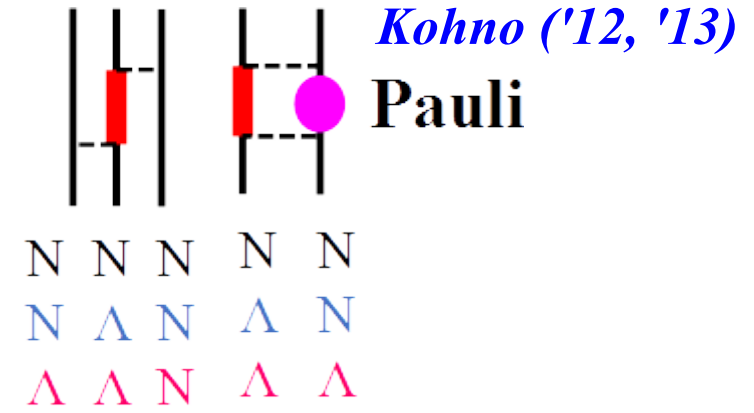
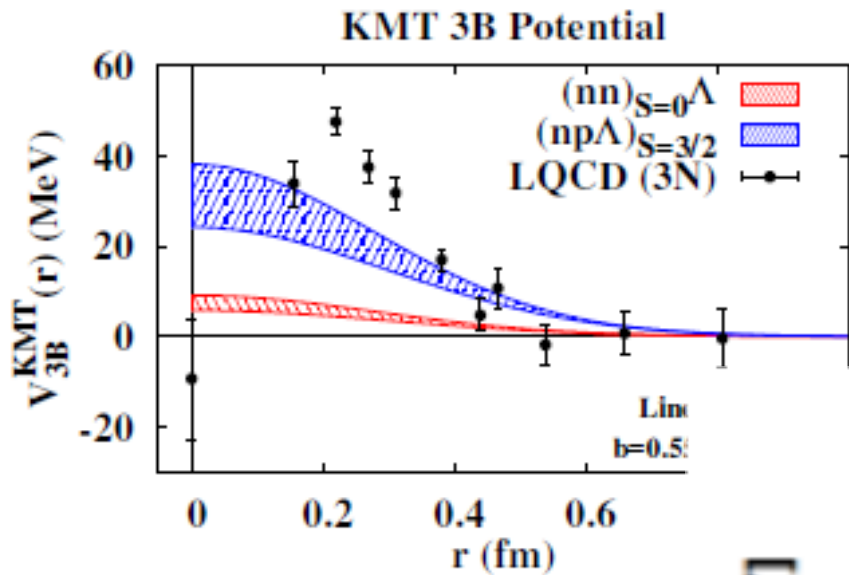
3B potential from KMT interaction

KMT 3B Potential

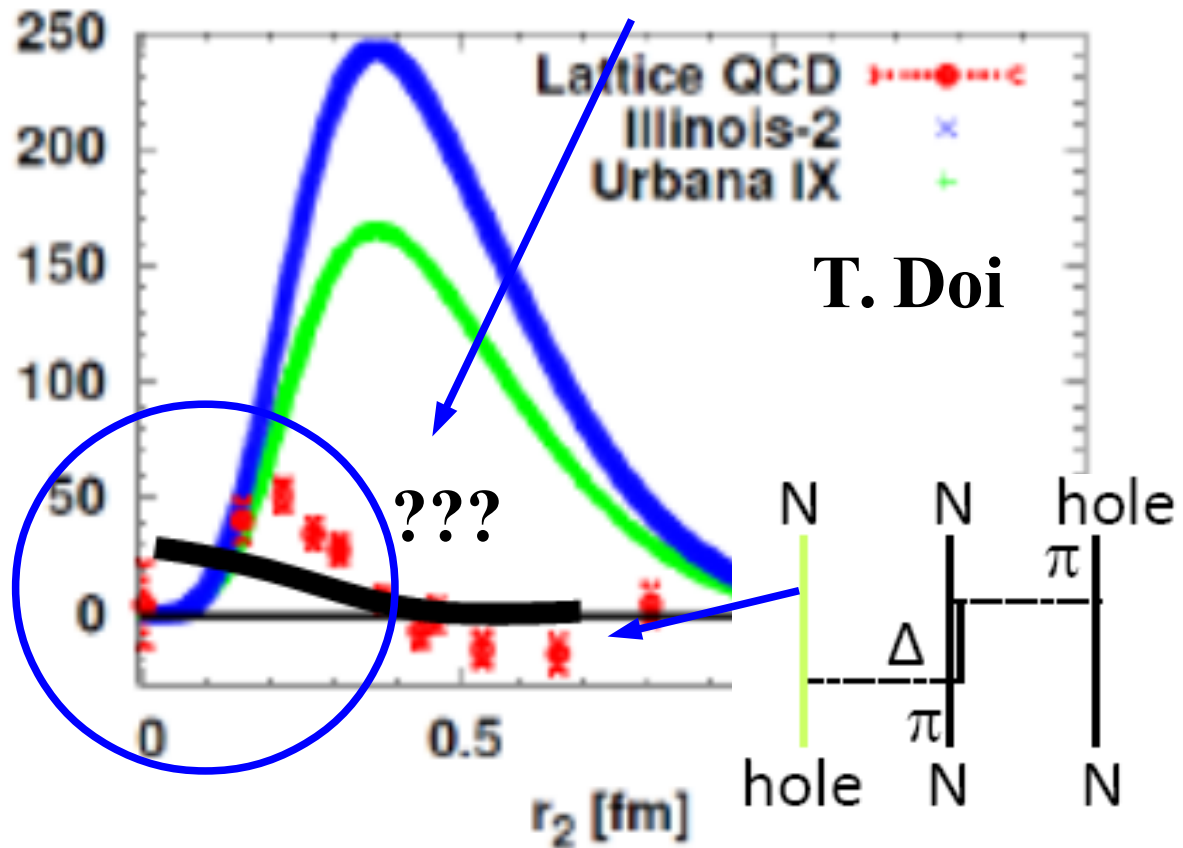


AO, Kashiwa, Morita, arXiv:1610.06306
Lattice data: Doi et al. (HAL QCD) ('07)

3B potential from KMT: Repulsive enough ?



Quarks



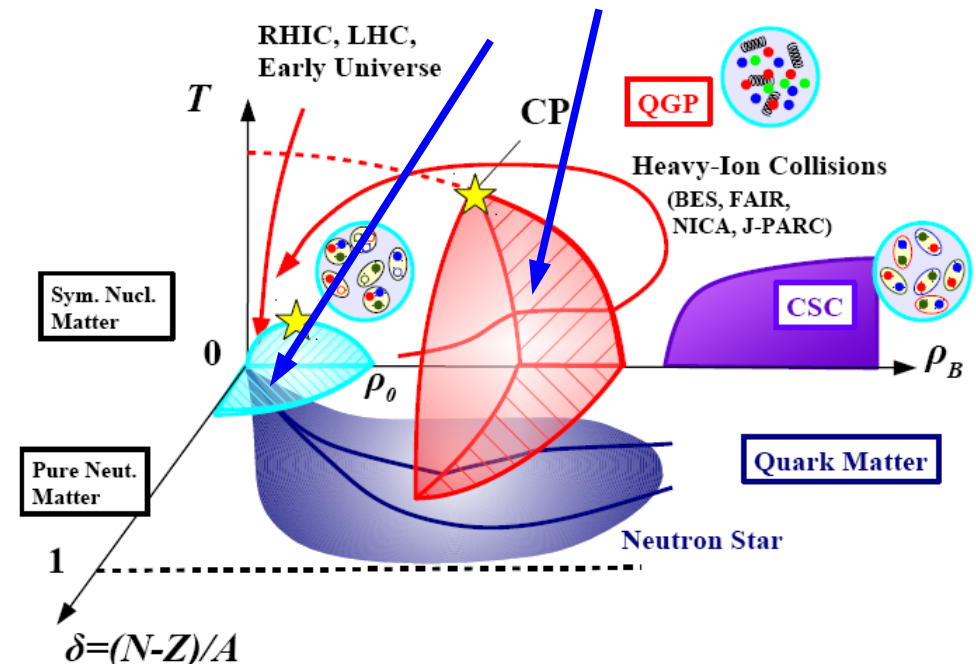
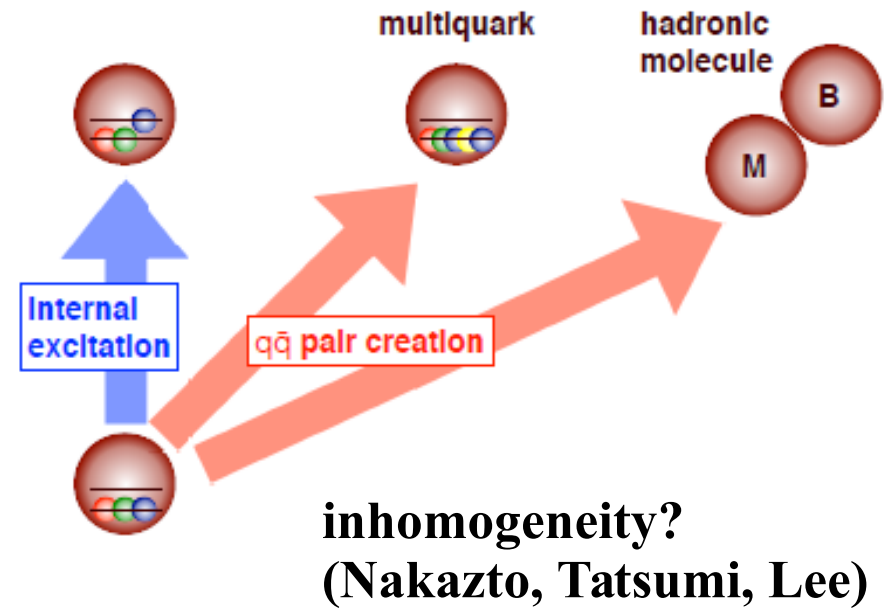
T. Doi

Summary

- Neutron Stars are treasury of various field of physics.
- NS matter grant studies have advanced understanding of NS !
 - A01, A02: Strangeness Nuclear Physics (Λ , Ξ , K, Σ , $\Lambda\Lambda$, H, ΣN , ...)
 - B01, B02: Symmetry energy (skin, pol., **pygmy**, and **$S(\rho \sim 2\rho_0)$** ...) and role of pairing
 - B03: Cold atom EOS, mixed condensate, **quantum simulation of neutron matter (r_{eff})**, ...
 - C01: **ASTRO-H, NICER \rightarrow (M,R)**
 - D01 (Theory): Support of other groups
quark matter, pasta, NS oscillation,
EOS using the achievements by A,B,C groups ...
(Sorry, members. I did not touch subjects other than EOS)
- We still need much more works to understand Neutron Stars.

Future Direction (Personal Prospect)

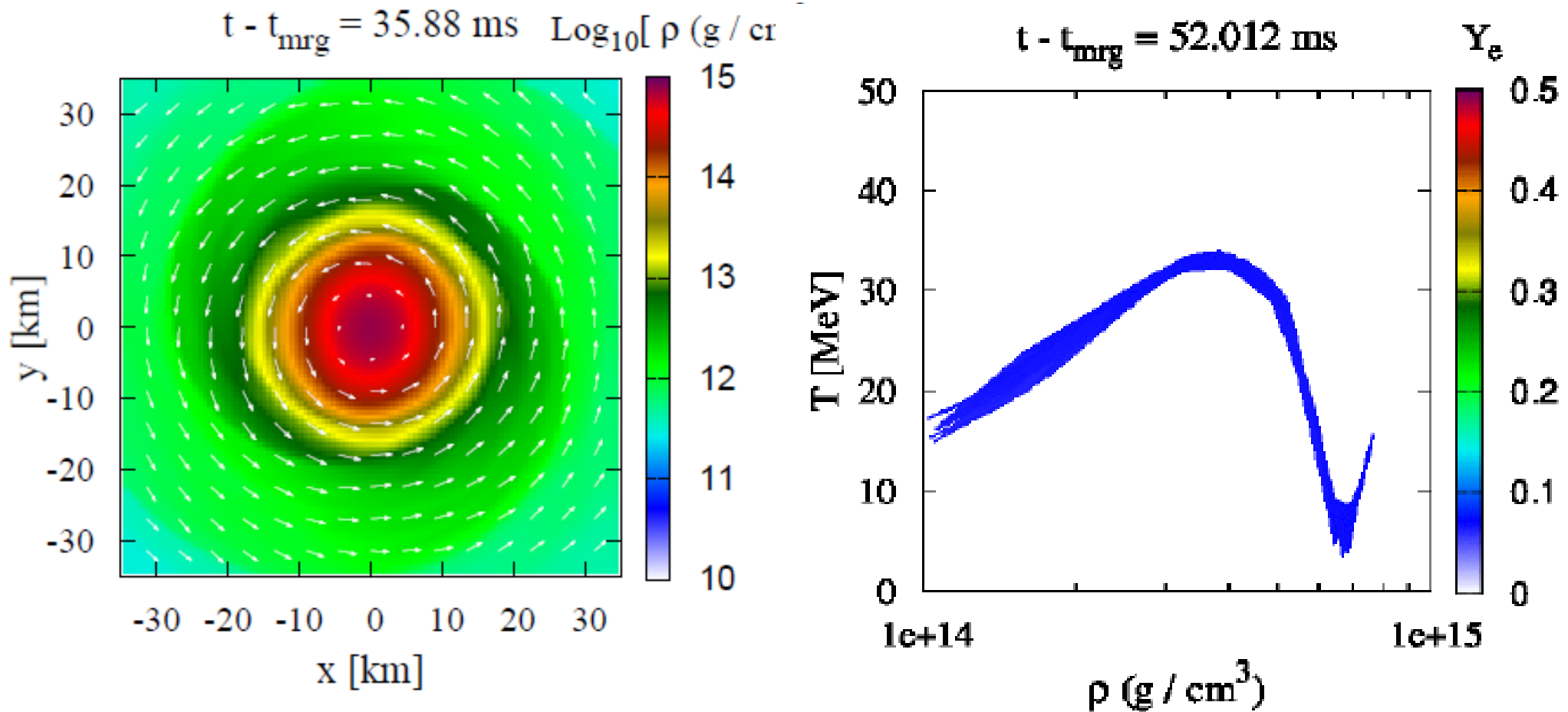
- Neutron Star Physics requires various interactions; fermion-fermion, fermion-boson, boson-boson (BB, BM, MM), which appears most strongly around the threshold
→ “Cluster” physics
- Neutron Star matter is condensed matter with possible phase transition.
→ QCD phase transition
- EOS dependence of Gravitational Wave is also important.



Thank you for your attention !

Binary Neutron Star Merger

- $T \sim 40$ MeV, $\rho_B \sim 10^{15}$ g/cm³ $\sim 4 \rho_0$ ($\rho_0 \sim 2.5 \times 10^{14}$ g/cm³),
 $Y_e \sim 0.1$



Courtesy of K. Kiuchi

Data are from Y. Sekiguchi, K. Kiuchi, K. Kyotoku, M. Shibata, PRD91('15)064059.

Neutron Star Matter EOS

Energy per nucleon in nuclear matter

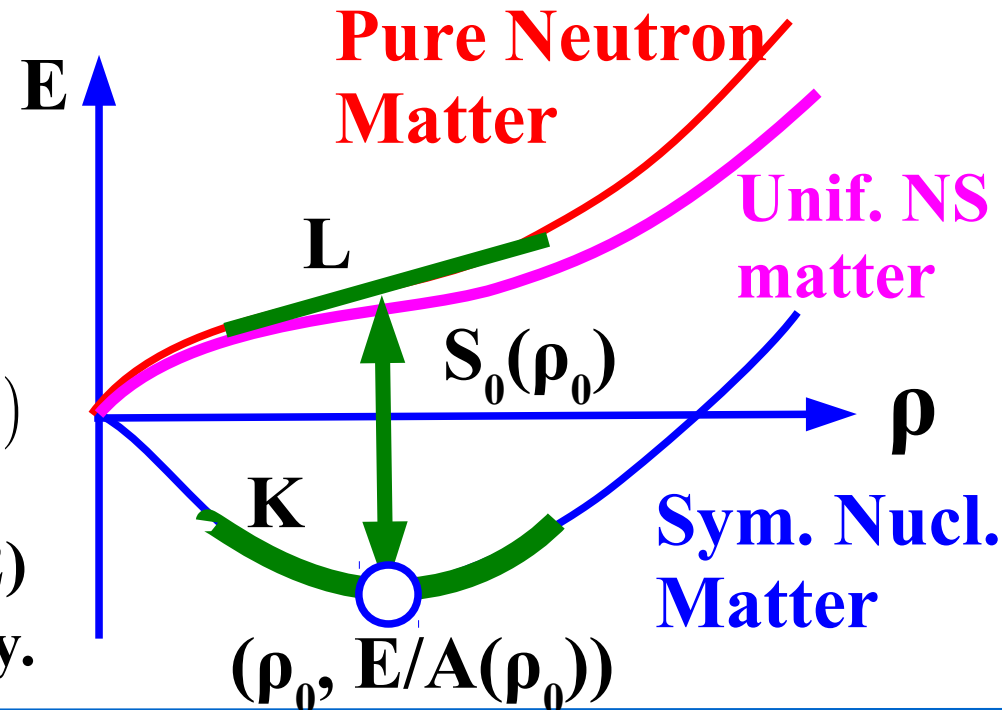
$$E_{\text{NM}}(\rho, \delta) = E_{\text{SNM}}(\rho) + S(\rho)\delta^2, \quad \delta = (N - Z)/A$$

$$E_{\text{SNM}}(\rho) \simeq E_0 + \frac{K(\rho - \rho_0)^2}{18\rho_0^2}, \quad S(\rho) = S_0 + \frac{L(\rho - \rho_0)}{3\rho_0}$$

- Saturation point $(\rho_0, E_0) \sim (0.16 \text{ fm}^{-3}, -16 \text{ MeV})$
- Symmetry energy parameters $(S_0 (=J), L) \sim (30 \text{ MeV}, 70 \text{ MeV})$
- Incompressibility $K \sim 230 \text{ MeV}$

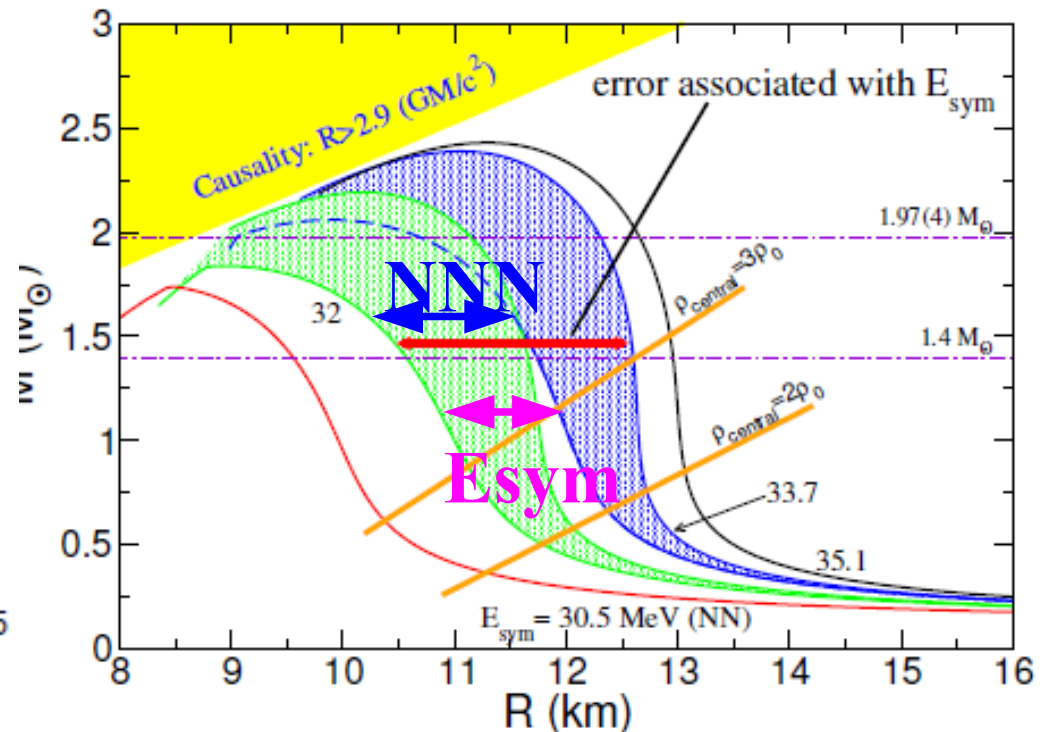
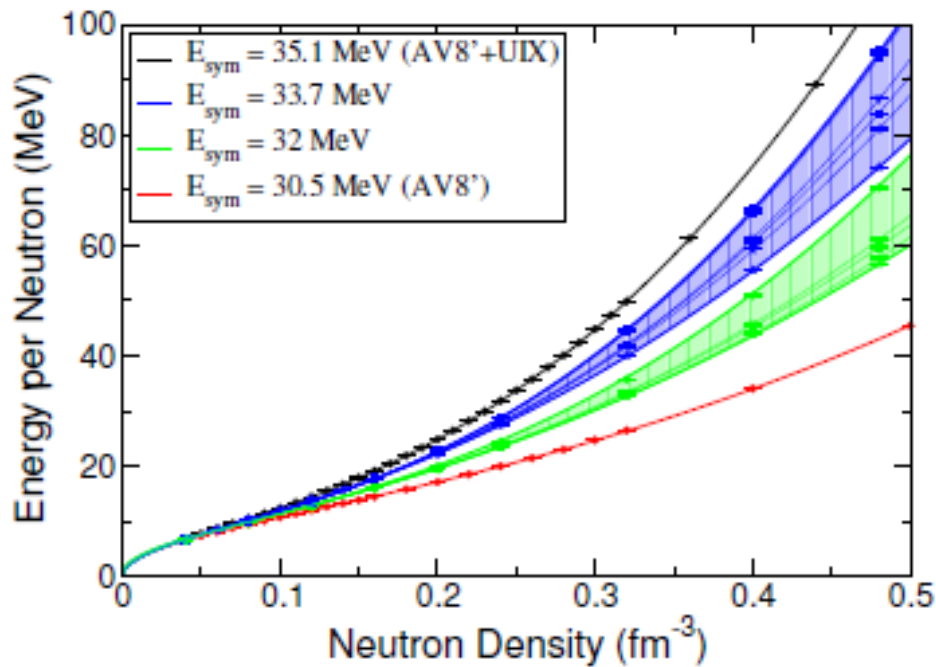
Uniform neutron star matter

- Constituents at low density = proton, neutron and electron
- Charge neutrality $\rightarrow \rho(\text{elec.}) = \rho(p) \quad (\rho_e = \rho_p = \rho(1 - \delta)/2)$
 δ is optimized to minimize energy.



Quantum Monte-Carlo calc.

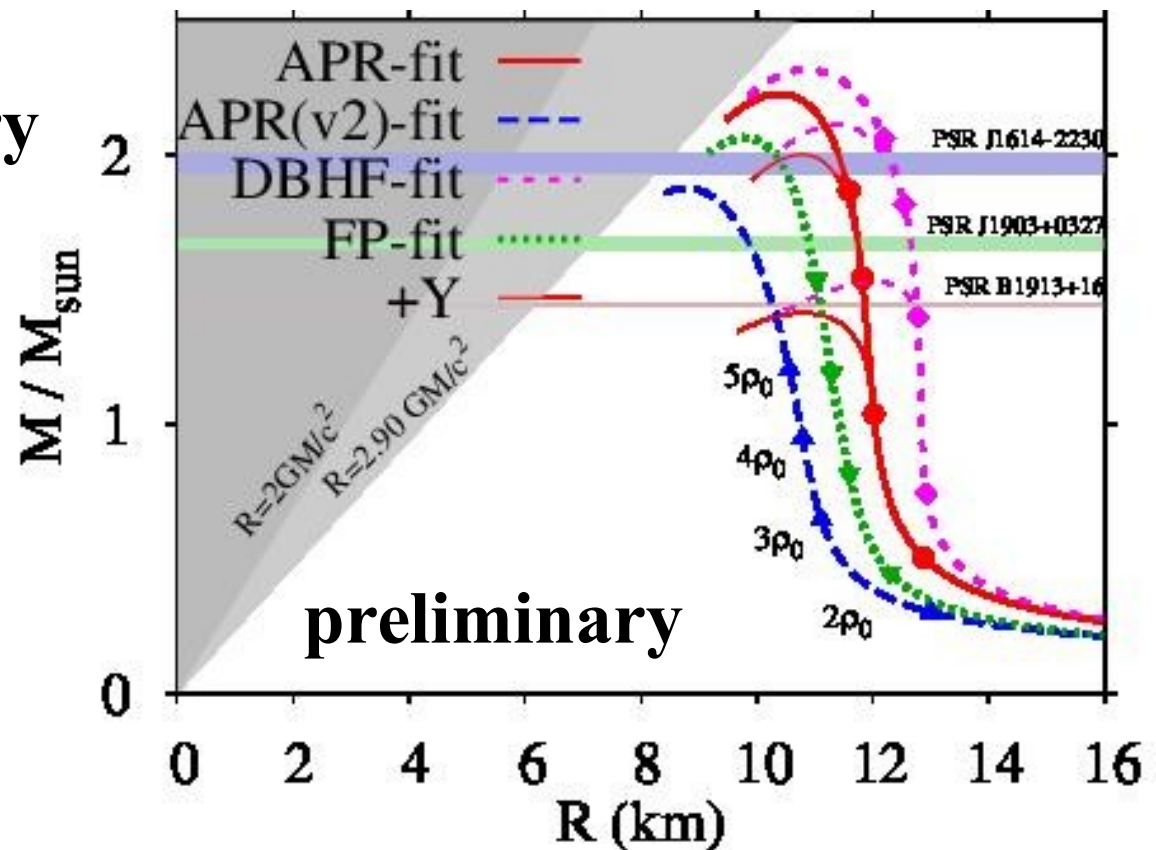
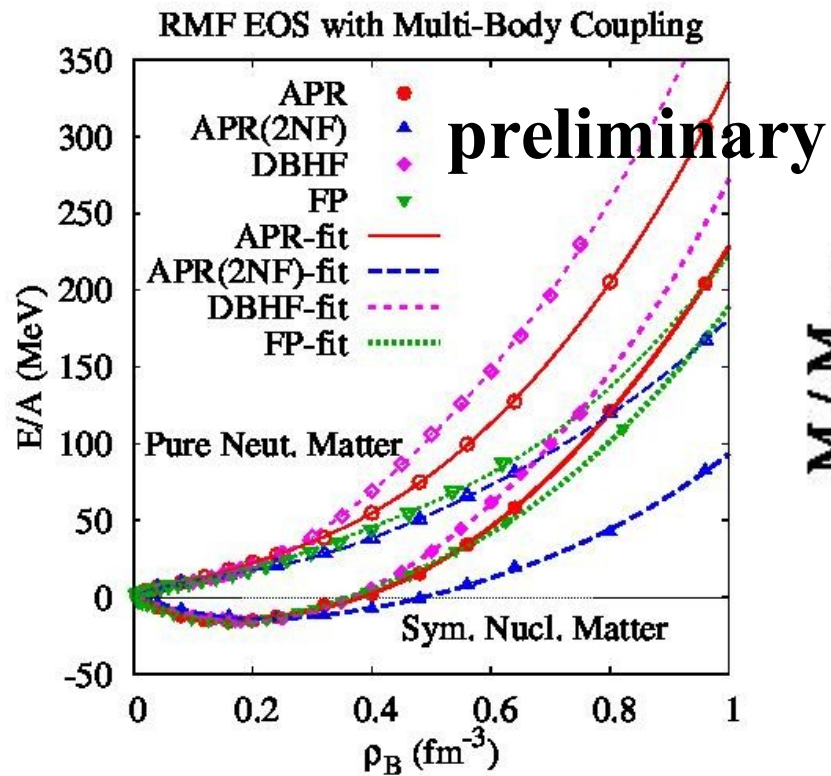
- Auxiliary Field Diffusion Monte-Carlo (AFDMC) calc.
 - Hubbard-Stratonovich transf. + MC integral over aux. fields.
 - 3n force parameters are tuned to fit finite nuclei.
 - 2 MeV Difference in E_{sym} results in 1.5 km (15 %) diff. in R_{NS} .



Gandolfi, Carlson, Reddy, PRC 032801, 85 (2012).

NS matter in “ab initio”-fit + Λ

- Fit to ab initio EOS (FP, APR, DBHF)
+ phen. Λ potential ($U(\rho_0) \sim -30$ MeV)



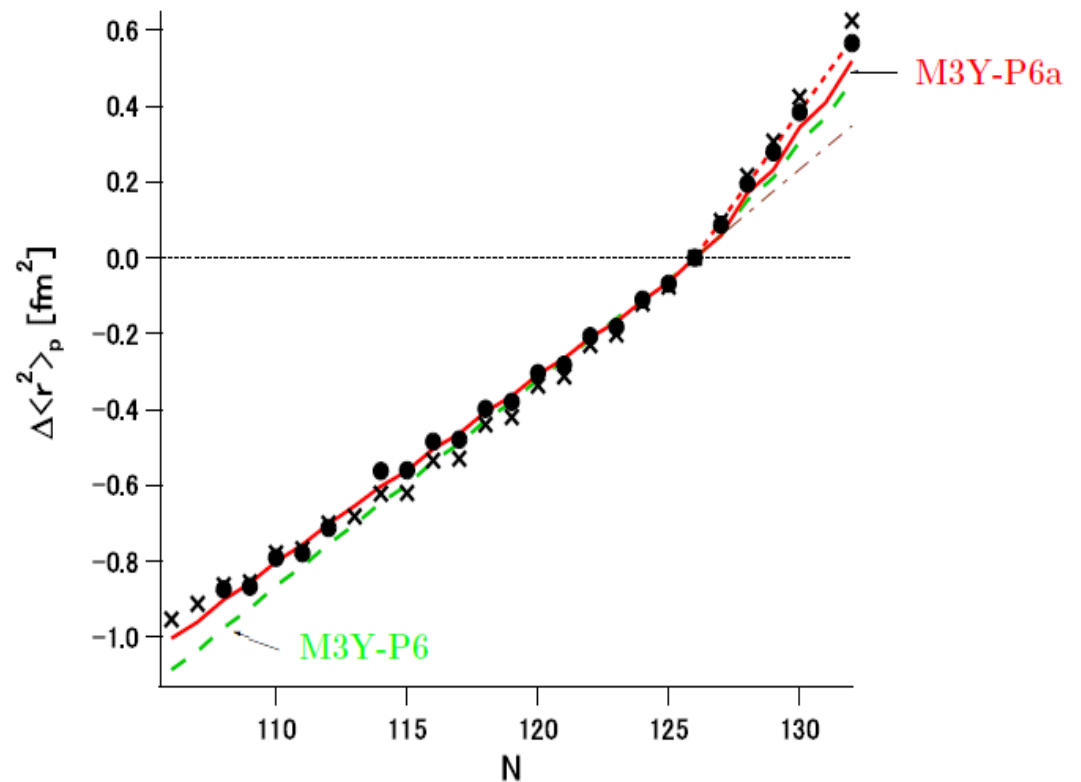
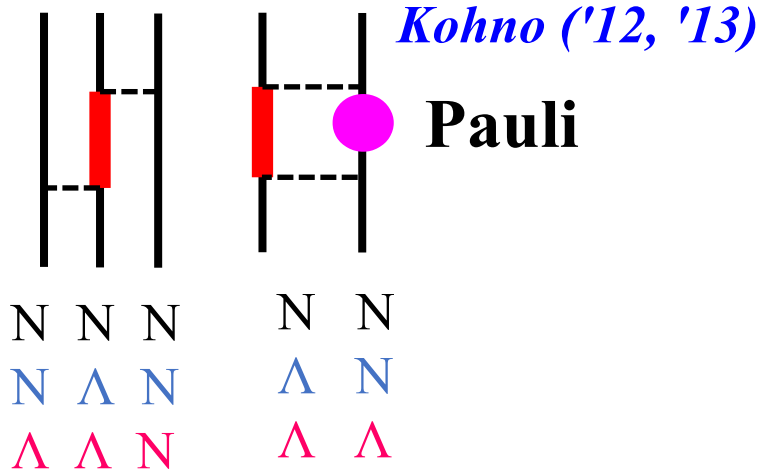
Strength of BBB force

- Three-body force leads to stiff EOS and stronger LS int.

Kohno ('12, '13)

- Density dep. LS int. explains long-standing Pb isotope puzzle.

Nakada, Inakura ('15)



Nakada, Inakura ('15)

Early crossover transition to quark matter

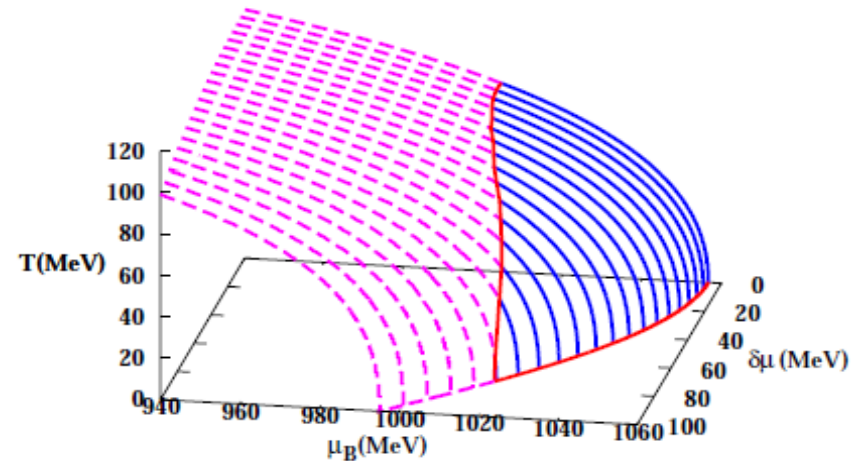
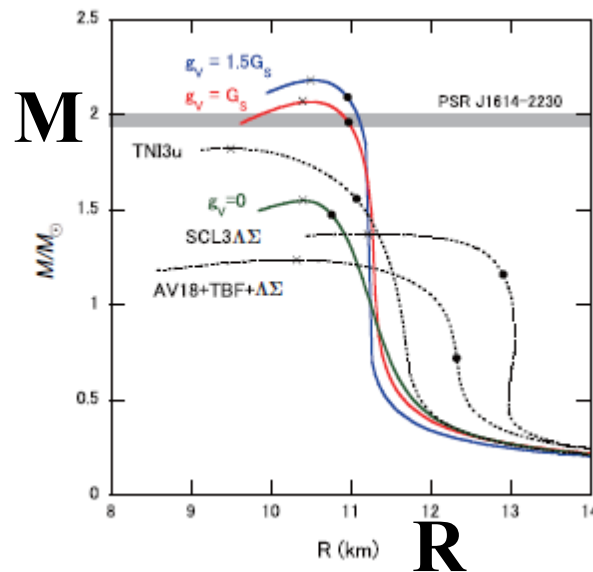
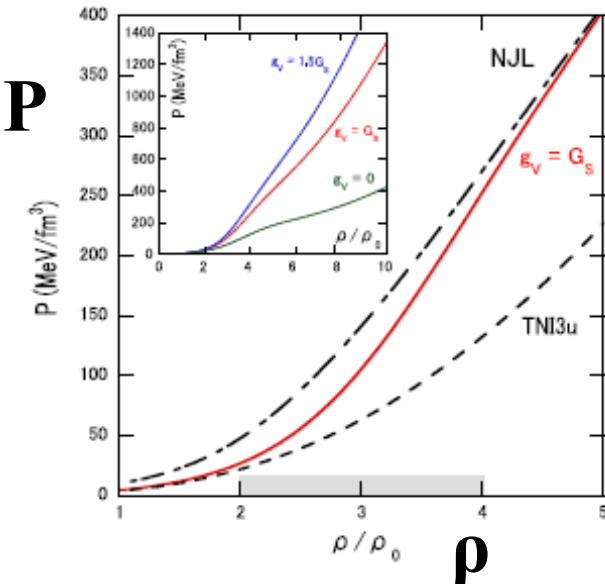
- Early **crossover** to quark matter → massive NS

K. Masuda, T. Hatsuda, T. Takatsuka, ApJ764('13)12

- QCD phase diagram in asymmetric matter

AO et al. ('11), Ueda et al. ('13)

- Disappearance of 1st order phase transition at large isospin chem. pot.



Masuda, Hatsuda, Takatsuka ('13)

*AO, Ueda, Nakano, Ruggieri, Sumiyoshi, PLB704('11),284
H. Ueda, et al. PRD88('13),074006*

NNN force

- NNN force is necessary to reproduce saturation point and to support massive neutron stars

- Variational cal. + phen. NNN force

A. Akmal, V.R.Pandharipande, D.G. Ravenhall, PRC58('98)1804;

H. Kanzawa, K. Oyamatsu, K. Sumiyoshi, M. Takano, NPA791 ('07) 232.

- Chiral EFT NN+NNN force

M. Kohno, PRC88('13)064005

