

# *Collapse of directed flow as a signal of the softest point of QCD matter*

**Akira Ohnishi (YITP, Kyoto U.)**

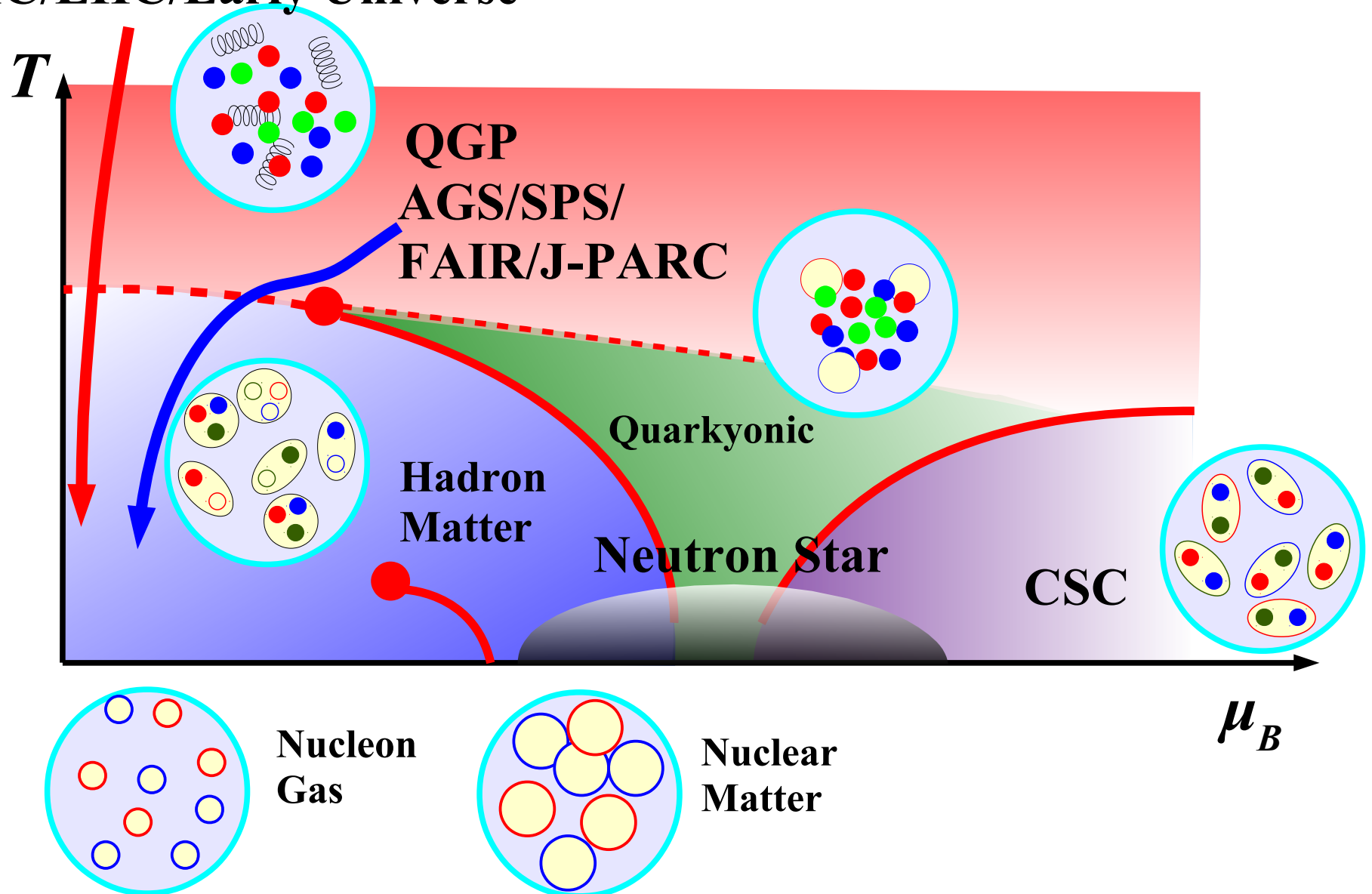
*YITP and IOPP Joint workshop on Heavy Ion Physics  
@IOPP, CCNU, Wuhan, Feb.20, 2016.*



**Y. Nara, A. Ohnishi, arXiv:1512.06299 [nucl-th] (QM2015 proc.)**  
**Y. Nara, A. Ohnishi, H. Stoecker, arXiv:1601.07692 [hep-ph]**

# QCD Phase Diagram

RHIC/LHC/Early Universe



# Signals of QGP formation & QCD phase transition

## ■ Signals of QGP formation at top RHIC & LHC energies

- Jet quenching in AA collisions (not in dA)
- Large elliptic flow (success of hydrodynamics)
- Quark number scaling (coalescence of quarks)

## ■ Next challenges

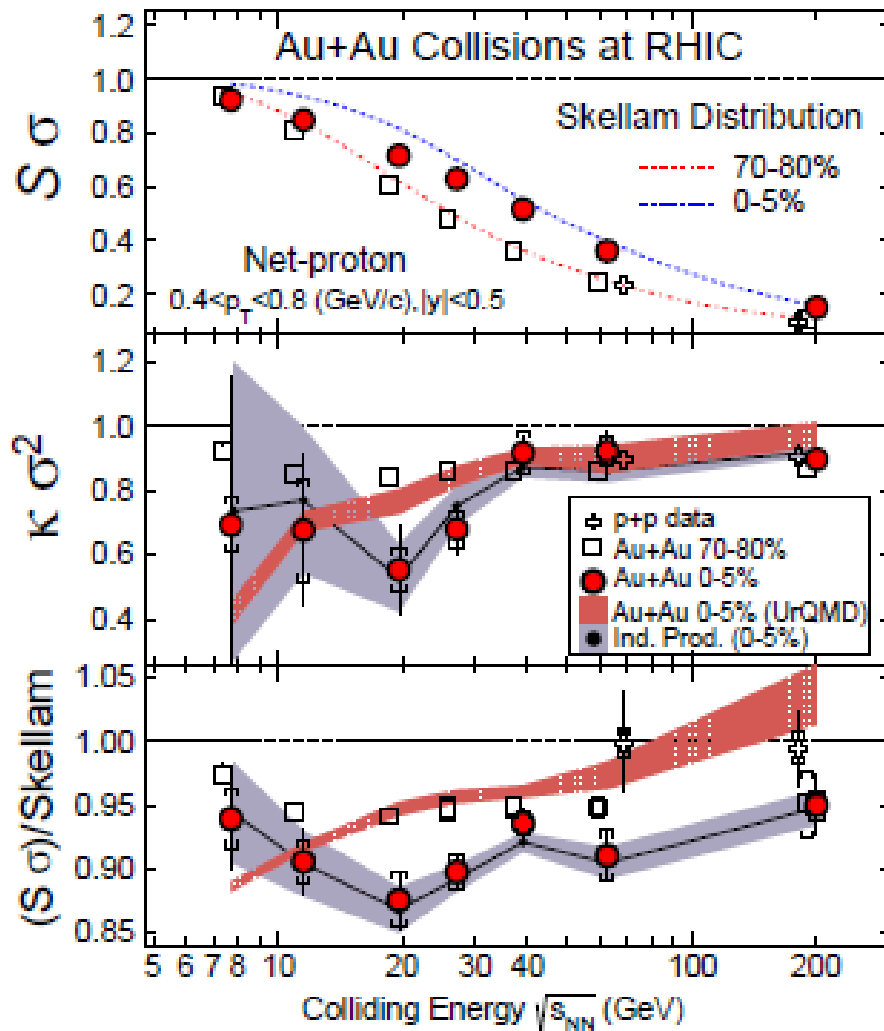
*Tsukiji et al.*

- Puzzles: Early thermalization, Photon  $v_2$ , Small QGP, ...  
→ Complete understanding from initial to final states
- Discovery of QCD phase transition

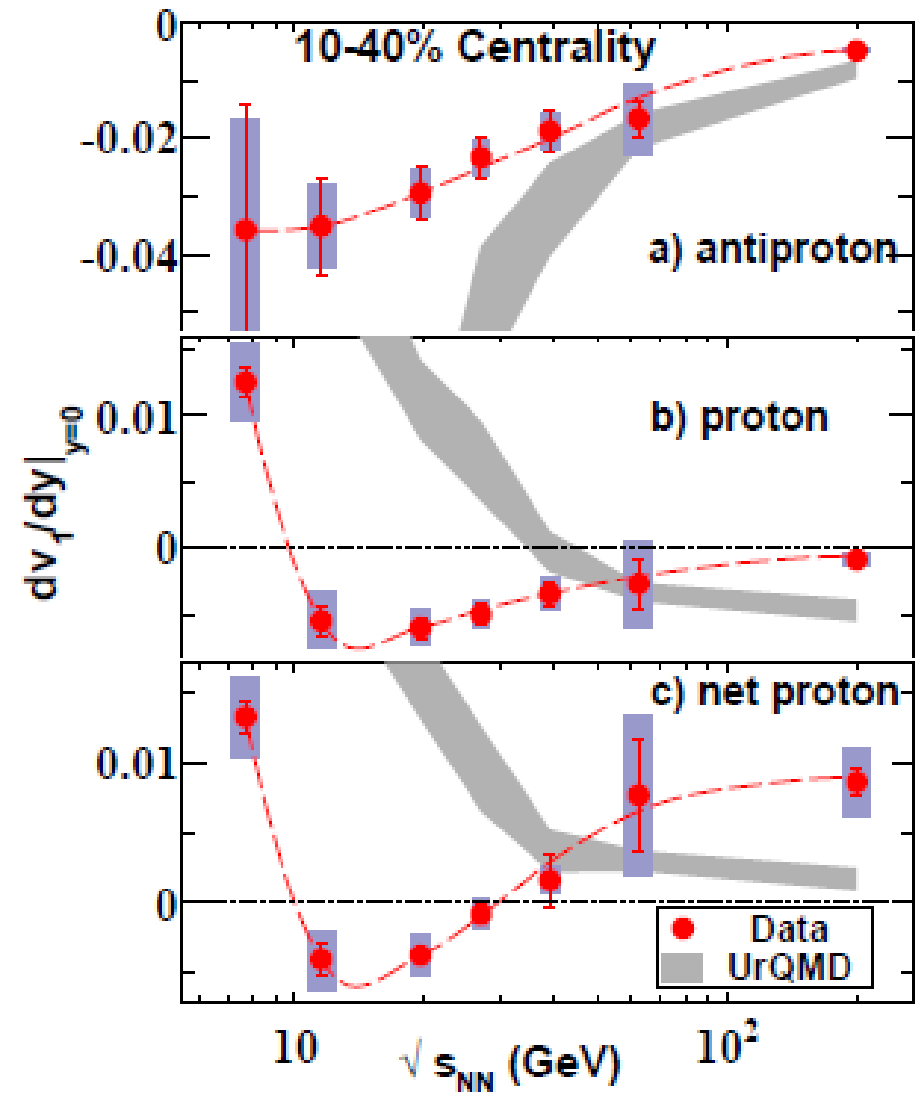
## ■ Signals of QCD phase transition at BES energies ?

- Critical Point → Large fluctuation of conserved charges
  - First-order phase transition → Softening of EOS
- Non-monotonic behavior of  
proton number moment ( $\kappa\sigma^2$ ) and collective flow ( $dv_1/dy$ )

# Net-Proton Number Cumulants & Directed Flow



STAR Collab. PRL 112('14)032302



STAR Collab., PRL 112('14)162301.

# Signals of QGP formation & QCD phase transition

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*Tsukiji et al.*

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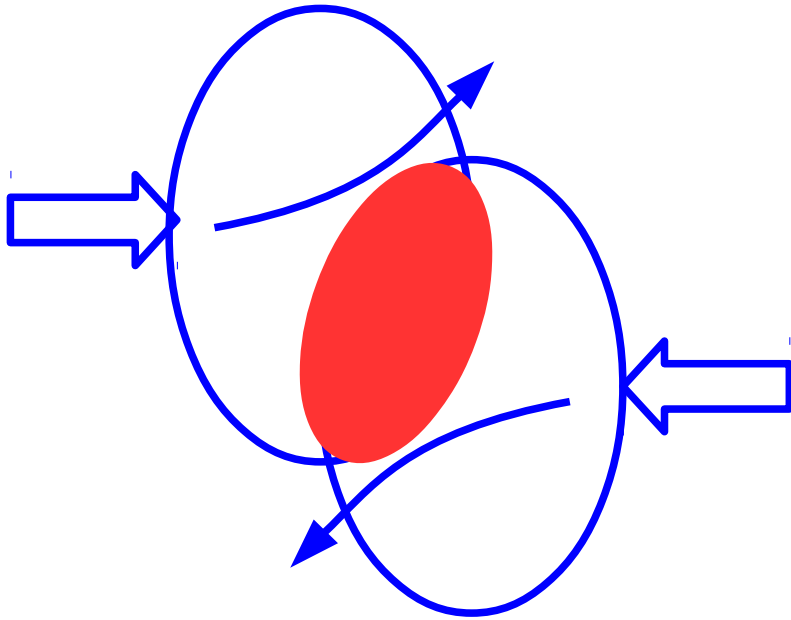
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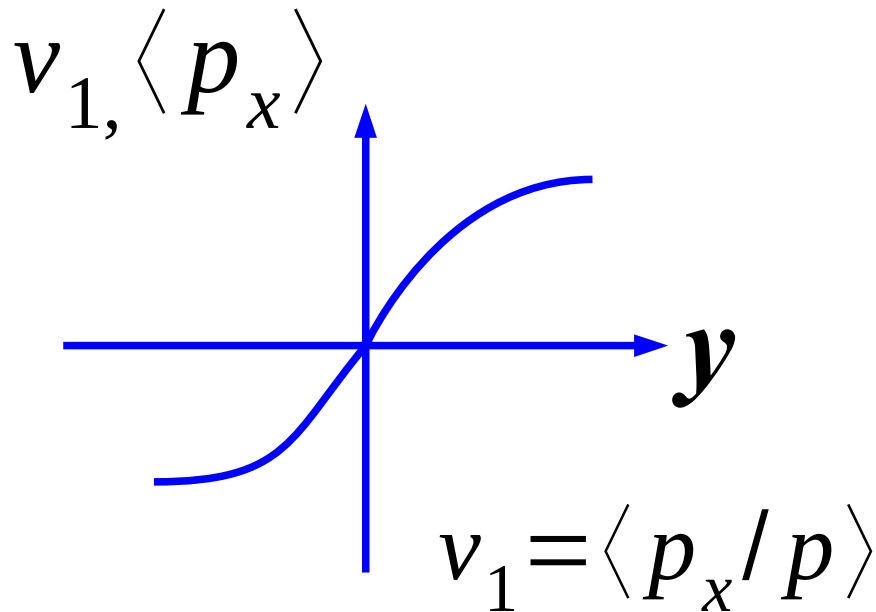
*Ichihara,  
Morita, AO  
Doi, Tsutsui*

→ Non-monotonic behavior of  
proton number moment ( $\kappa\sigma^2$ ) and collective flow ( $dv_1/dy$ )

# What is directed flow ?



- $v_1$  or  $\langle p_x \rangle$  as a function of  $y$  is called directed flow.
- Sensitive to the EOS in the early stage.
- Becomes smaller at higher energies.

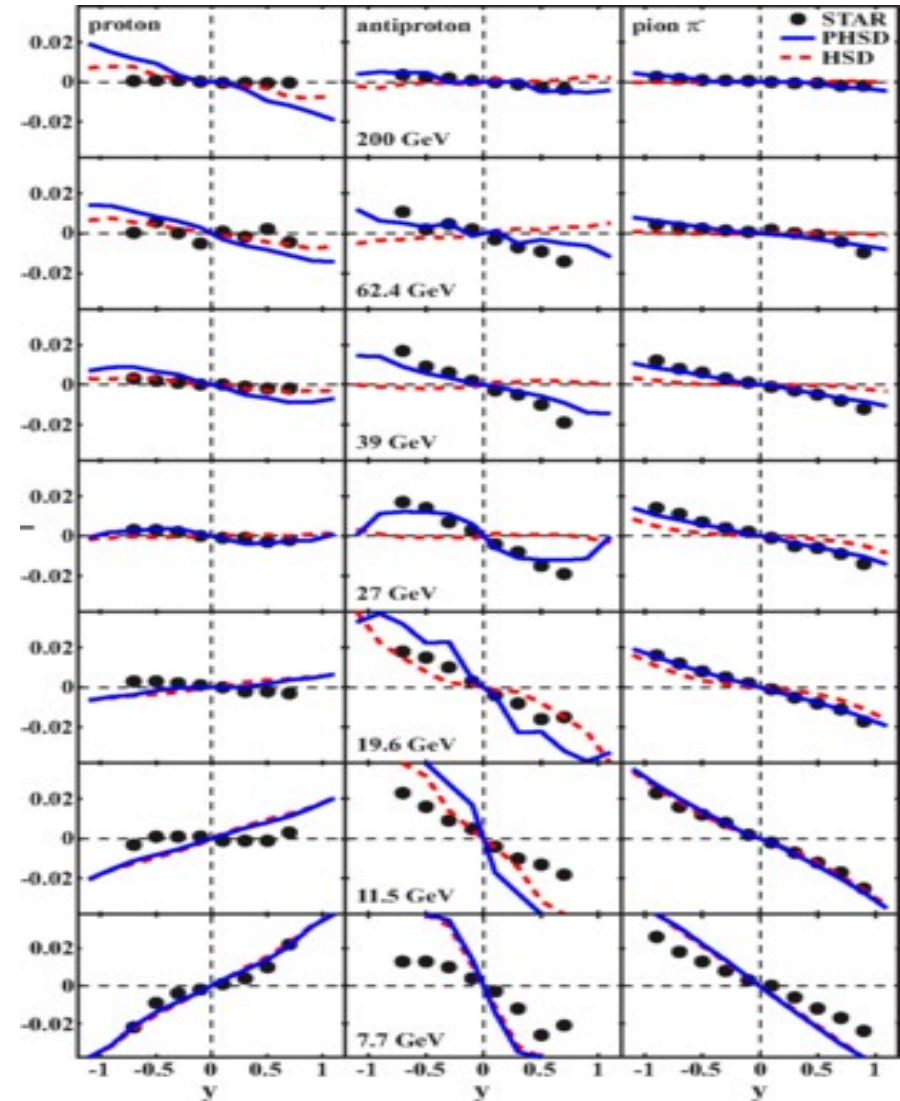
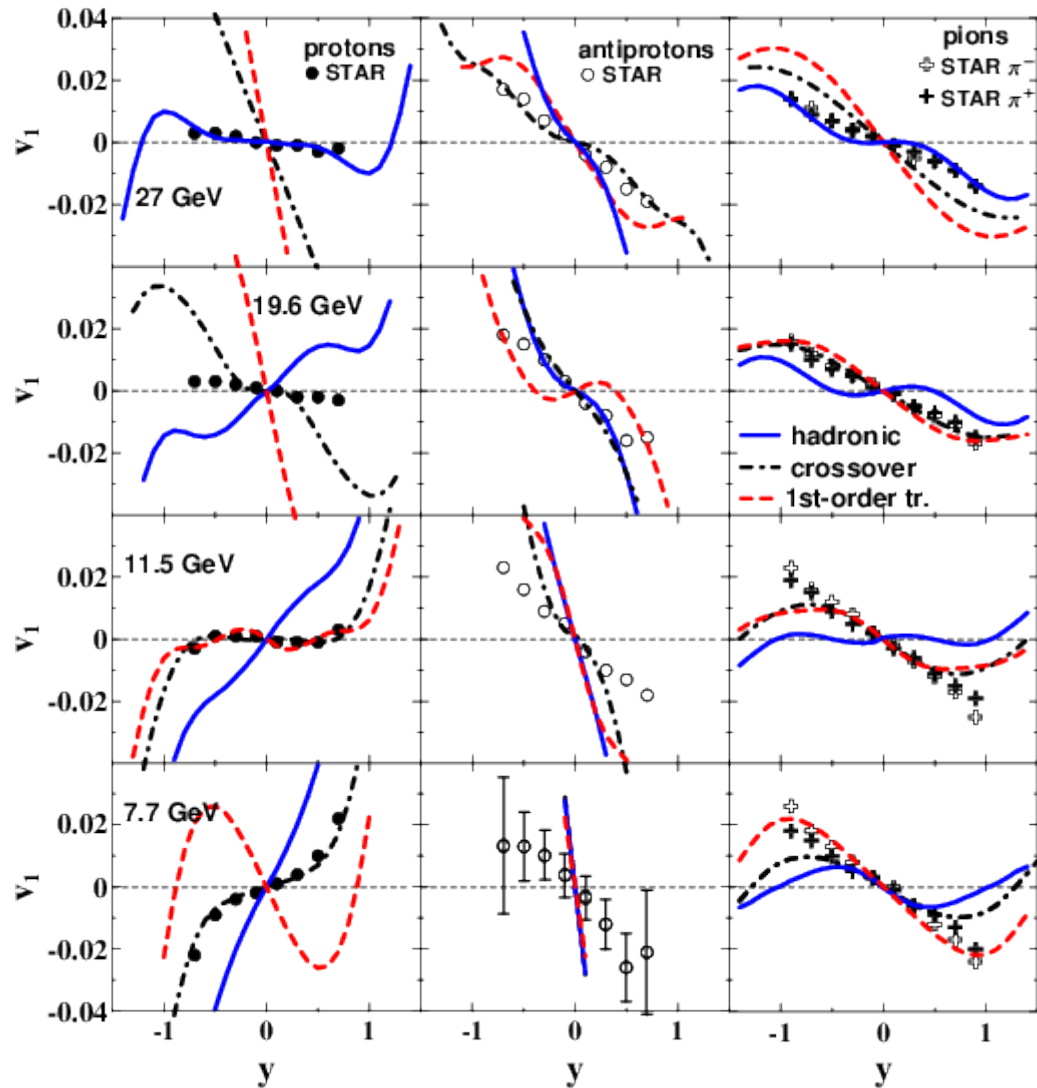


# V1 from hydrodynamics

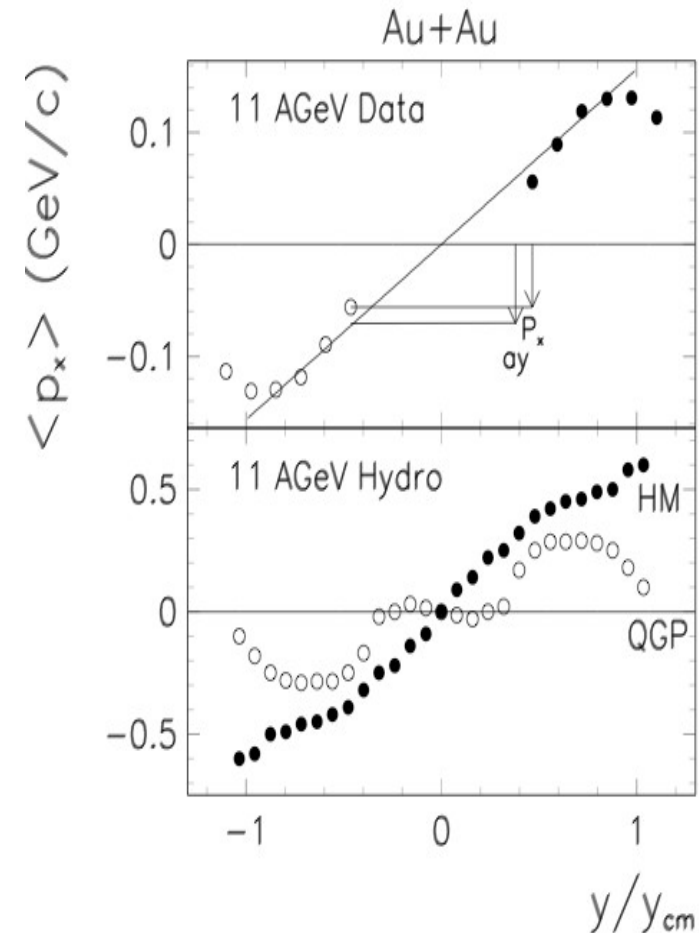
# PHSD/HSD predictions

Y. B. Ivanov and A. A. Soldatov, Phys. Rev. C91, no. 2, 024915 (2015)

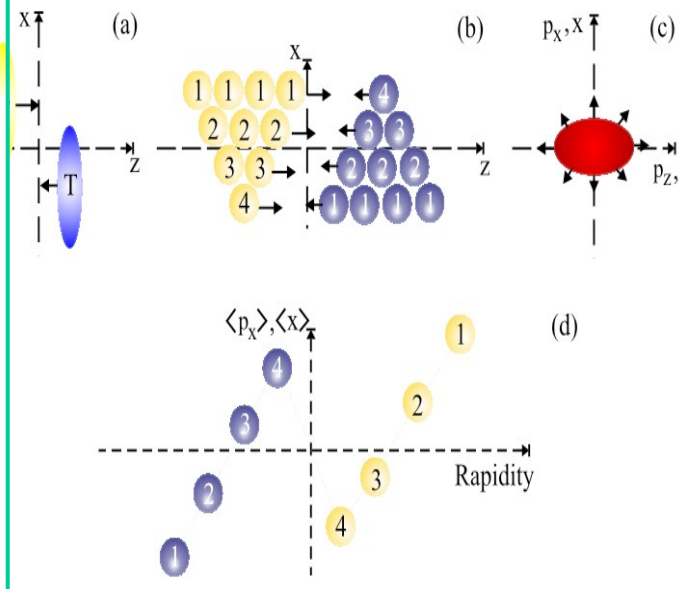
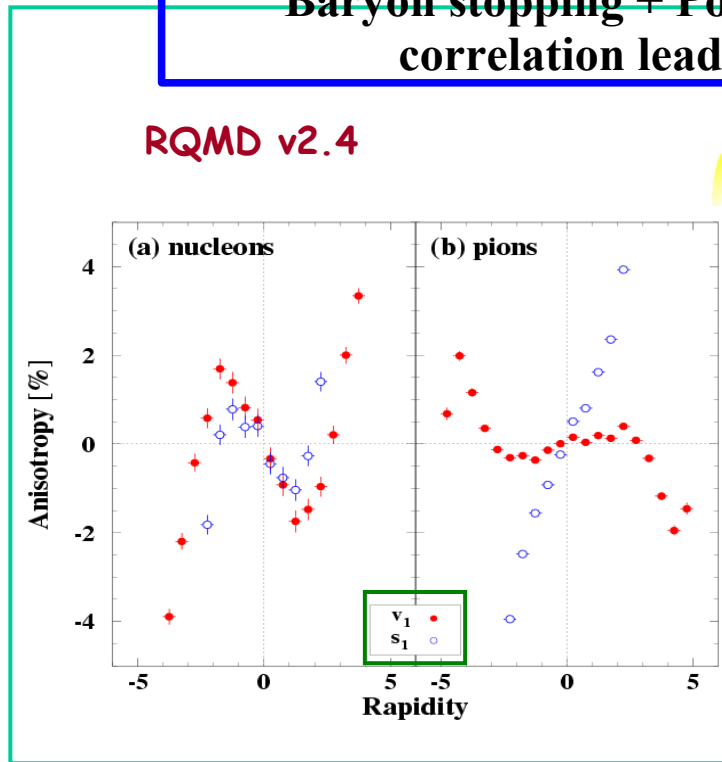
V. P. Konchakovski, W. Cassing, Y. B. Ivanov and V. D. Toneev, Phys. Rev. C90, no. 1, 014903 (2014)



# Wiggle: QGP signal in the directed flow?



**Baryon stopping + Positive space-momentum correlation leads wiggle (no QGP)**



R. Snellings, H. Sorge, S. Voloshin, F. Wang, N. Xu, PRL (84) 2803(2000)

L. P. Csernai, D. Röhrich, PLB 45 (1999), 454.

**QGP EoS predicts wiggle in hydro**



# *Collapse of directed flow*

- Negative  $dv_1/dy$  at high-energy ( $\sqrt{s_{NN}} > 20$  GeV)
  - Geometric origin (bowling pin mechanism), not related to FOPT  
*R.Snellings, H.Sorge, S.Voloshin, F.Wang, N. Xu, PRL84,2803(2000)*
- Negative  $dv_1/dy$  at  $\sqrt{s_{NN}} \sim 10$  GeV
  - Yes, in three-fluid simulations.
  - No, in transport models incl. hybrid.  
Exception: *B.A.Li, C.M.Ko ('98) with FOPT EOS*

*We investigate the directed flow at BES energies  
in hadronic transport model  
with / without mean field effects  
with / without softening effects via attractive orbit.*

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*Hadronic Transport Approach  
Cascade / Cascade + Mean Field*

# Microscopic transport models (event generator for nuclear collisions)

- **UrQMD 3.4** Frankfurt **public**  
resonance model N\*,D\*, string pQCD, PYTHIA6.4
- **PHSD** Giessen (Cassing) **upon request**  
D(1232),N(1440),N(1530), string, pQCD, FRITIOF7.02
- **GiBUU 1.6** Giessen (Mosel) **public**  
resonance model N\*,D\*, string, pQCD,PYTHIA6.4
- **AMPT** **public**  
HIJING+ZPC+ART
- **JAM** Japan (Y. Nara) **public**  
resonance model N\*,D\*, string, pQCD, PYTHIA6.1

# Transport Model

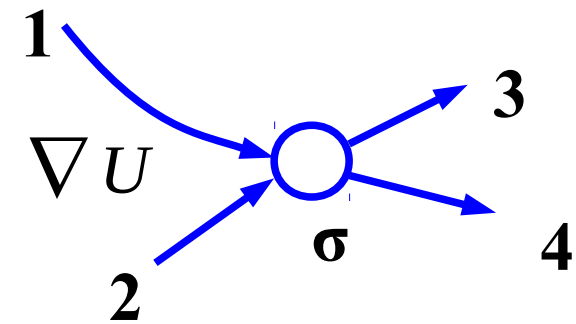
## ■ Boltzmann equation with potential effects

*E.g. Bertsch, Das Gupta, Phys. Rept. 160( 88), 190*

$$\frac{\partial f}{\partial t} + \mathbf{v} \cdot \nabla f - \nabla U \cdot \nabla_p f = I_{\text{coll}}$$

$$I_{\text{coll}}(\mathbf{r}, \mathbf{p}) = -\frac{1}{2} \int \frac{d\mathbf{p}_2}{(2\pi)^3} d\Omega v_{12} \frac{d\sigma}{d\Omega} [f f_2 (1 - f_3)(1 - f_4)] - (12 \leftrightarrow 34)]$$

(NN elastic scattering case)



## ■ Hadron-string transport model JAM

- Collision term → Hadronic cascade with resonance and string excitation

*Nara, Otuka, AO, Niita, Chiba, Phys. Rev. C61 (2000), 024901.*

- Potential term → Mean field effects in the framework of RQMD/S

*Sorge, Stocker, Greiner, Ann. of Phys. 192 (1989), 266.*

*Tomoyuki Maruyama et al., Prog. Theor. Phys. 96(1996), 263.*

*Isse, AO, Otuka, Sahu, Nara, Phys.Rev. C 72 (2005), 064908.*

# Relativistic QMD/Simplified (RQMD/S)

- RQMD is developed based on constraint Hamiltonian dynamics  
*H. Sorge, H. Stoecker, W. Greiner, Ann. Phys. 192 (1989), 266.*

- 8N dof  $\rightarrow$  2N constraints  $\rightarrow$  6N (phase space)
- Constraints = on-mass-shell constraints + time fixation

- RQMD/S uses simplified time-fixation

*Tomoyuki Maruyama, et al. Prog. Theor. Phys. 96(1996),263.*

- Single particle energy (on-mass-shell constraint)

$$p_i^0 = \sqrt{\mathbf{p}_i^2 + m_i^2 + 2m_i V_i}$$

- EOM after solving constraints

$$\dot{\mathbf{r}}_i = \frac{\mathbf{p}_i}{p_i^0} + \sum_j \frac{m_j}{p_j^0} \frac{\partial V_j}{\partial \mathbf{p}_i} \quad \dot{\mathbf{p}}_i = - \sum_j \frac{m_j}{p_j^0} \frac{\partial V_j}{\partial \mathbf{r}_i}$$

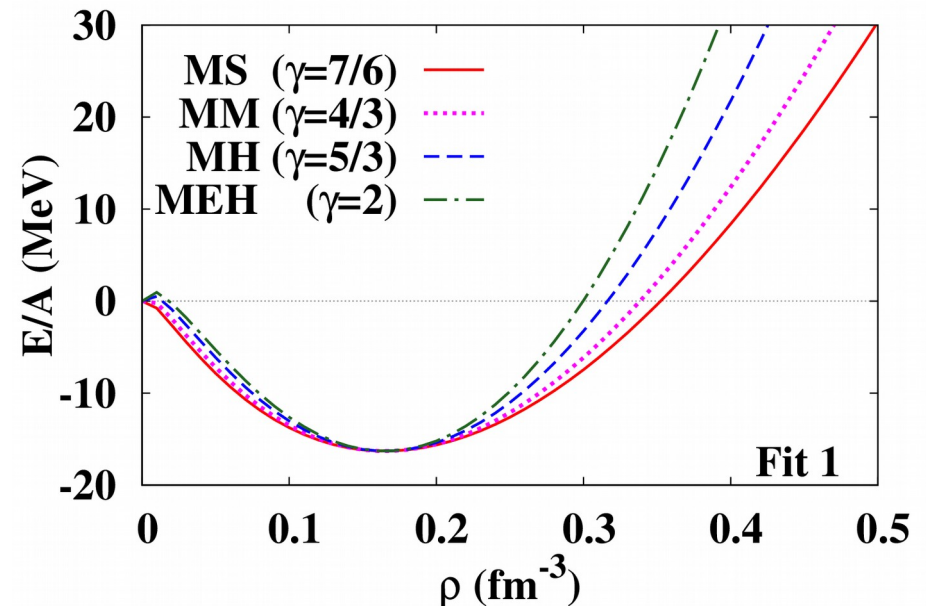
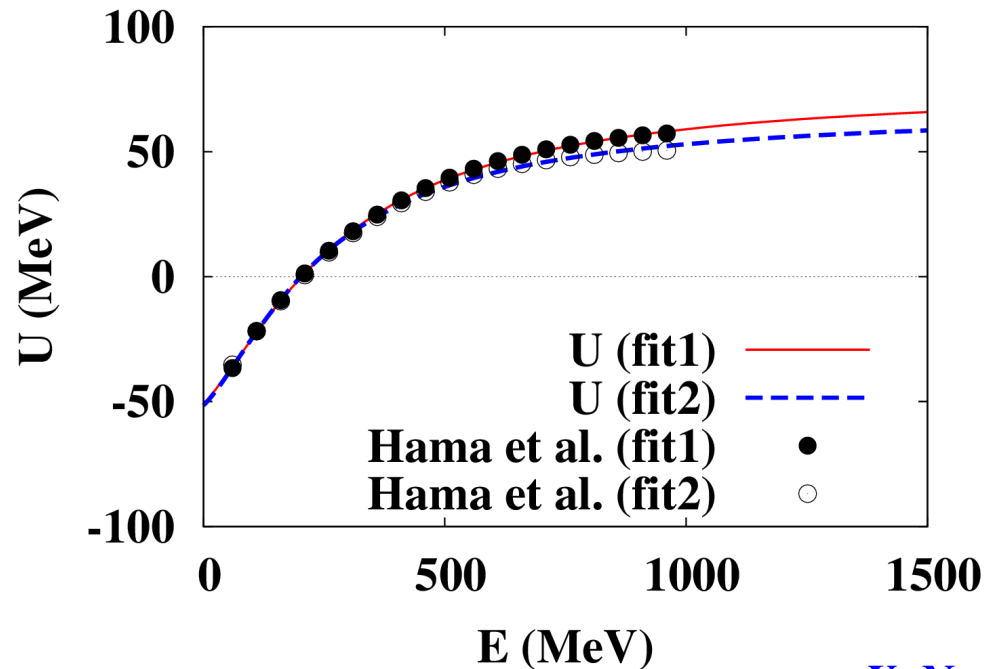
- Relative distances  $(\mathbf{r}_i - \mathbf{r}_j)^2$  are replaced with those in the two-body c.m.  
 $\rightarrow$  Potential becomes Lorentz scalar

# Mean field potential

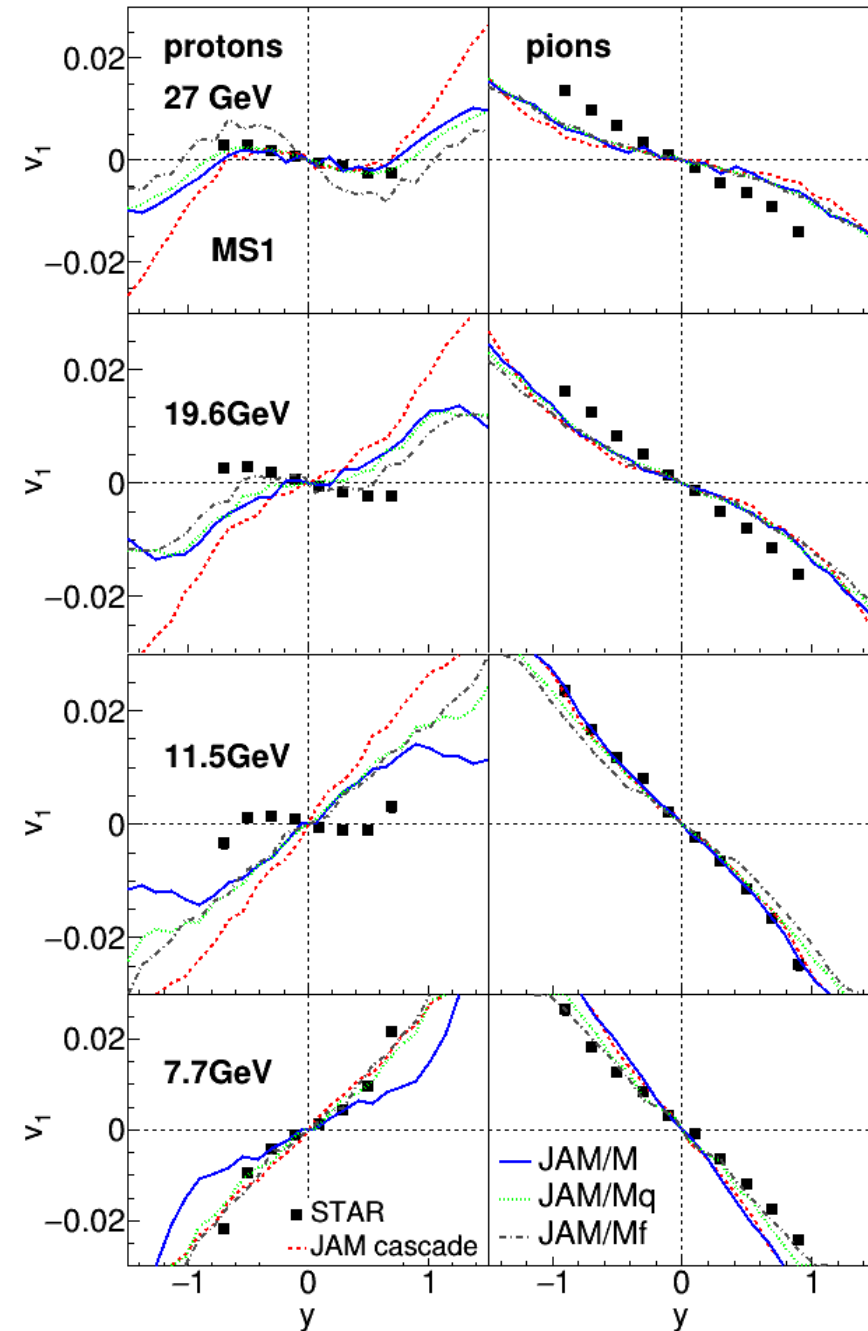
Skyrme type density dependent + Lorentzian momentum dependent potential

$$V = \sum_i V_i = \int d^3r \left[ \frac{\alpha}{2} \left( \frac{\rho}{\rho_0} \right)^2 + \frac{\beta}{\gamma+1} \left( \frac{\rho}{\rho_0} \right)^{\gamma+1} \right] + \sum_k \int d^3r d^3p d^3p' \frac{C_{ex}^{(k)}}{2\rho_0} \frac{f(\mathbf{r}, \mathbf{p}) f(\mathbf{r}, \mathbf{p}')}{1 + (\mathbf{p} - \mathbf{p}')^2 / \mu_k^2}$$

Type	$\alpha$ (MeV)	$\beta$ (MeV)	$\gamma$	$C_{ex}^{(1)}$ (MeV)	$C_{ex}^{(2)}$ (MeV)	$\mu_1$ (fm <sup>-1</sup> )	$\mu_2$ (fm <sup>-1</sup> )	$K$ (MeV)
MH1	-12.25	87.40	5/3	-383.14	337.41	2.02	1.0	371.92
MS1	-208.89	284.04	7/6	-383.14	337.41	2.02	1.0	272.6



# Comparison of $v_1$



Effects of potential on the  $v_1$  is significant

Hadronic approach does not reproduce the correct beam energy dependence of the directed flow.

Something happens around 10-20GeV?

**JAM/M:** only formed baryons feel potential forces  
**JAM/Mq:** pre-formed hadron feel potential with factor 2/3 for diquark, and 1/3 for quark  
**JAM/Mf:** both formed and pre-formed hadrons feel potential forces.

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# *Hadronic Transport Approach with Softening Effects*



# Softening Effects via Attractive Orbit Scattering

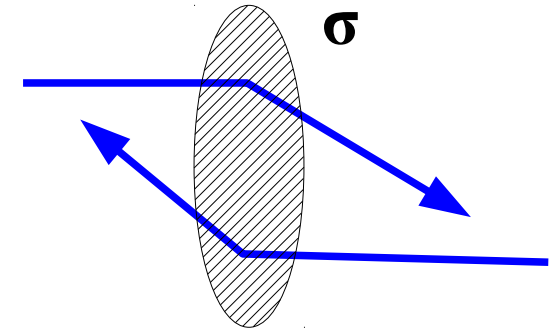
- Attractive orbit scattering simulates softening of EOS

*P. Danielewicz, S. Pratt, PRC 53, 249 (1996)*

*H. Sorge, PRL 82, 2048 (1999).*

$$P = P_f + \frac{1}{3TV} \sum_{(i,j)} (\mathbf{q}_i \cdot \mathbf{r}_i + \mathbf{q}_j \cdot \mathbf{r}_j)$$

(Virial theorem)



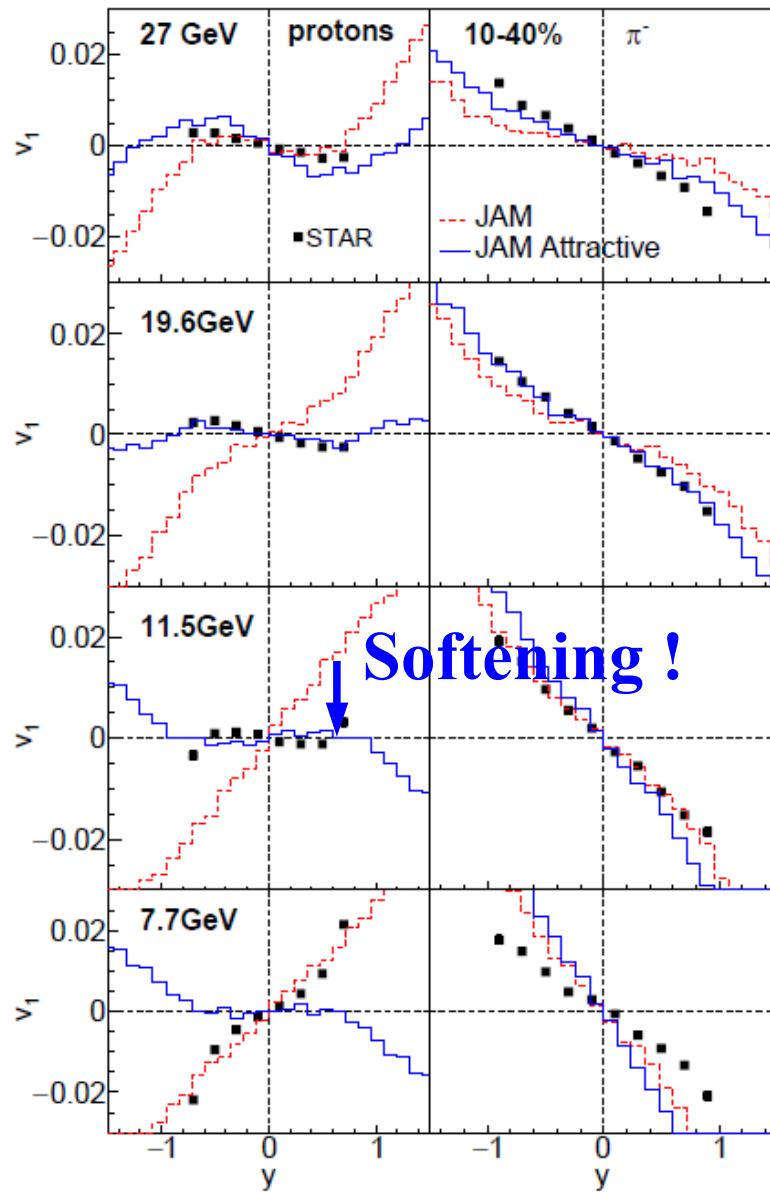
- Attractive orbit → particle trajectory are bended in denser region

*Let us examine the EOS softening effects,  
which cannot be explained in hadronic mean field potential,  
by using attractive orbit scatterings !*

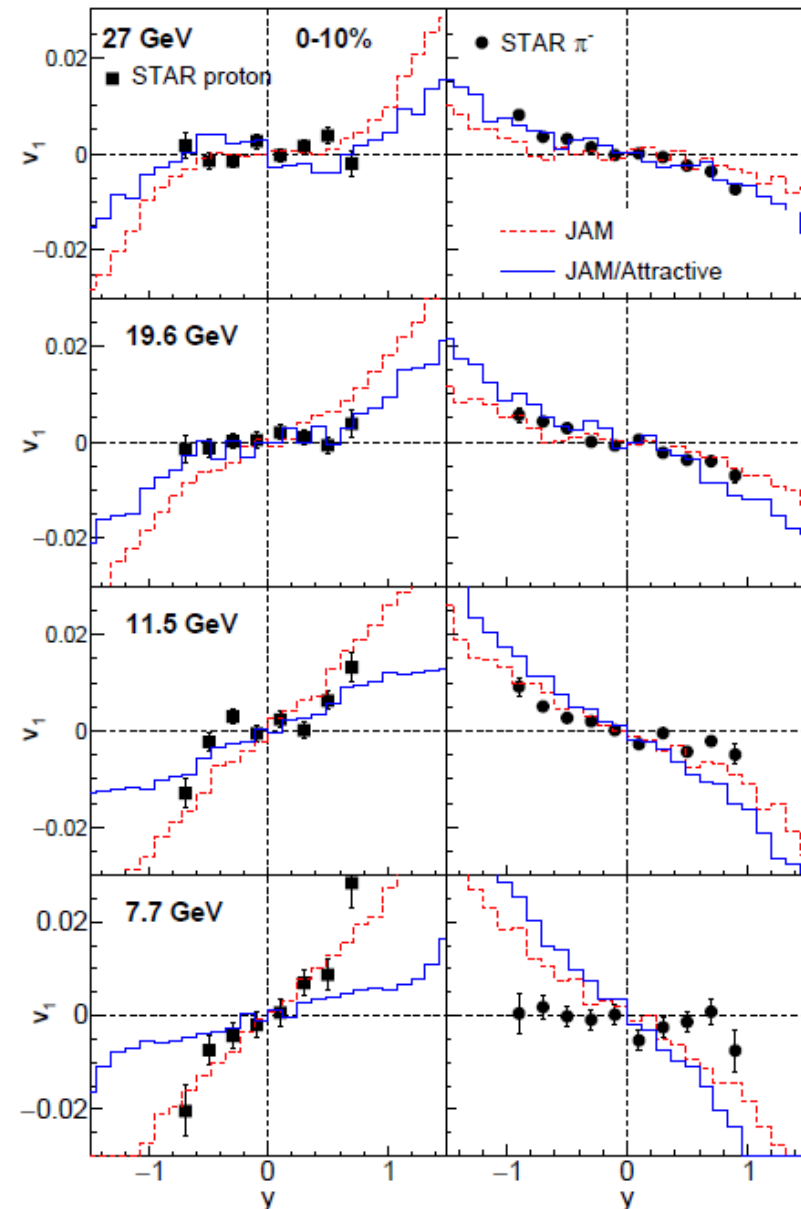
*Y. Nara, AO, H. Stöcker, arXiv:1601.07692 [hep-ph]*

# Directed Flow with Attractive Orbits

Nara, AO, Stöcker ('16)



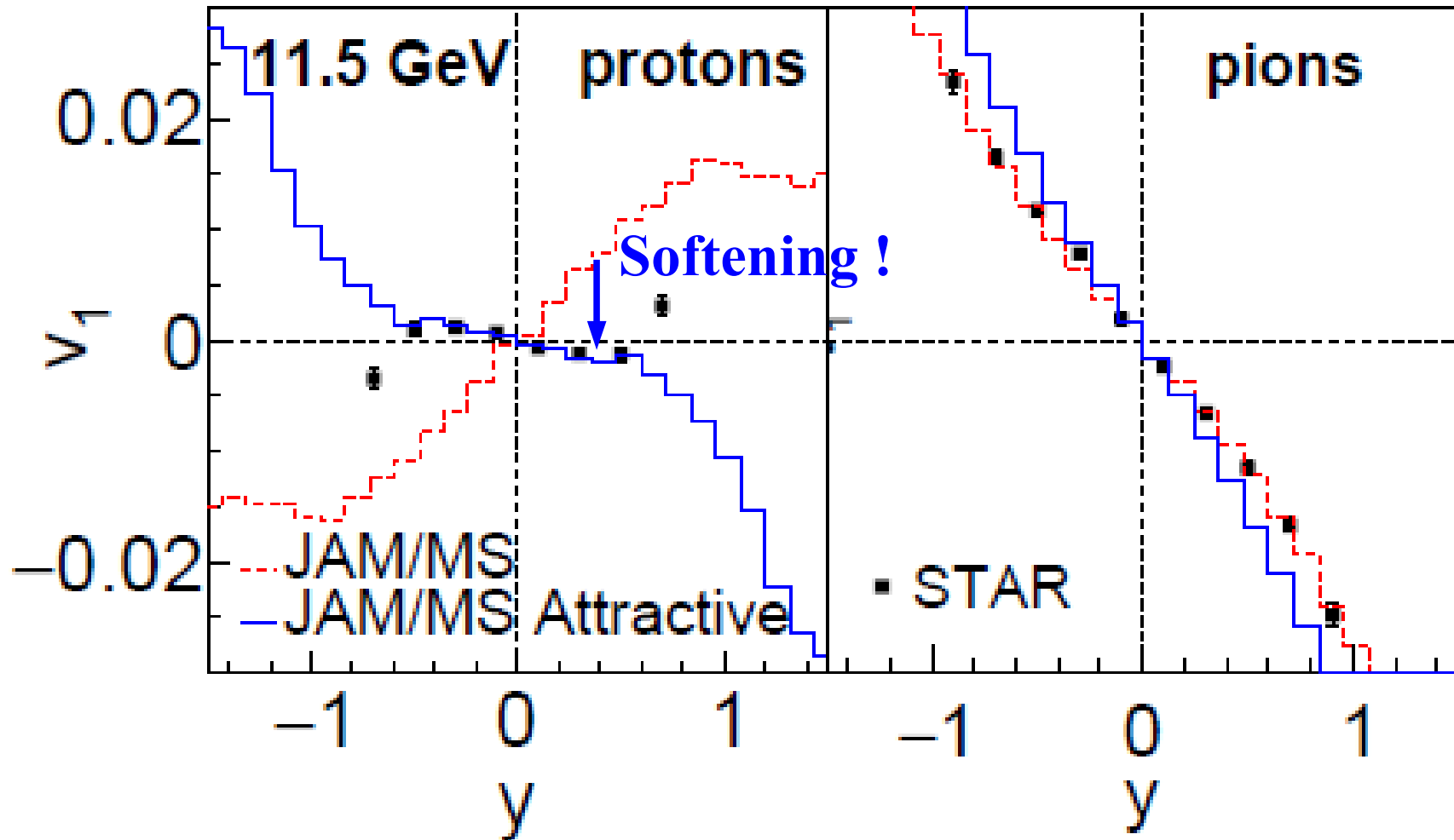
mid-central (10-40 %)



central (0-10 %)

# Mean Field + Attractive Orbit

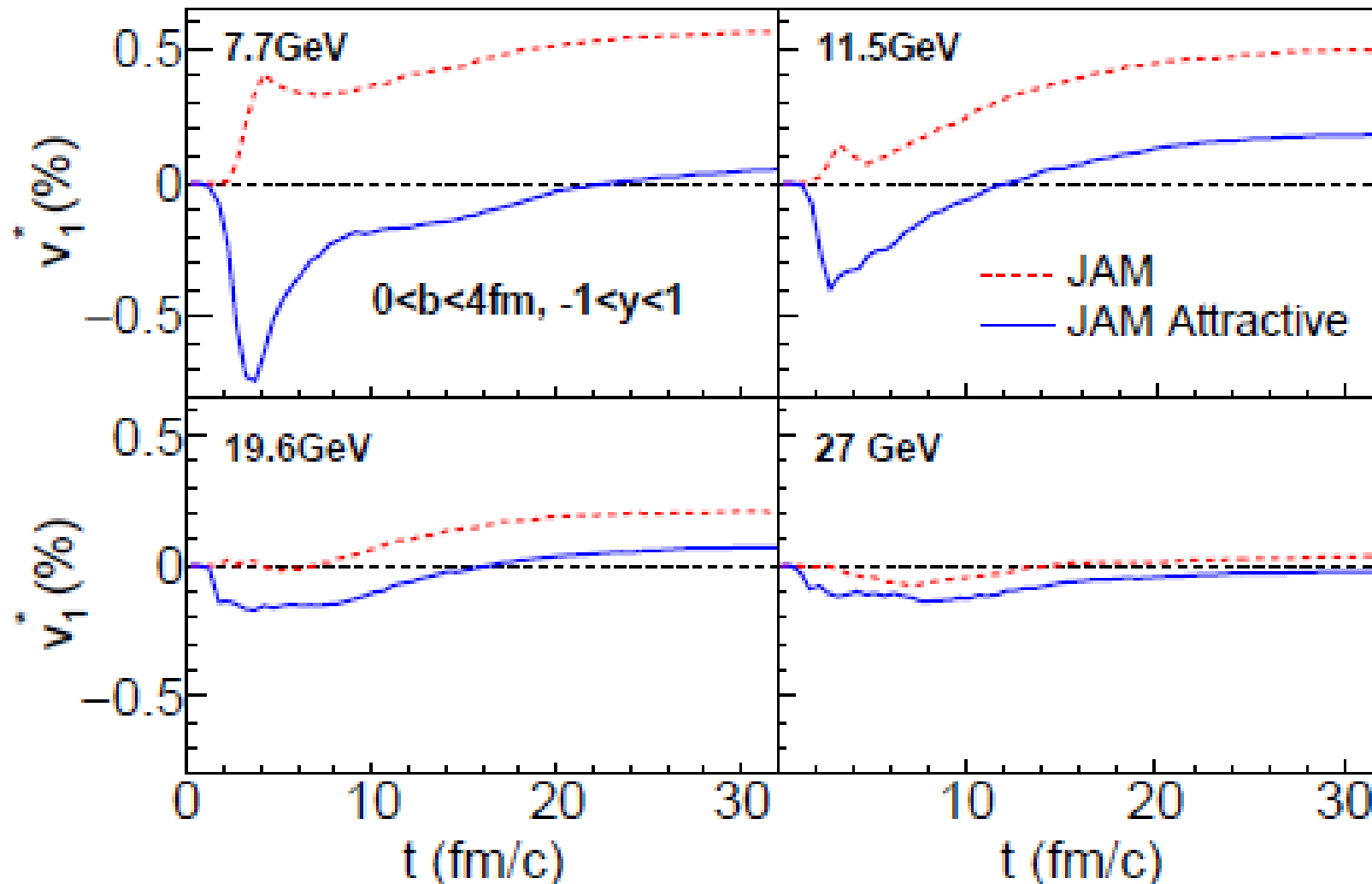
Nara, AO, Stöcker ('16)



*MF+Attractive Orbit make  $dv_1/dy$  negative at  $\sqrt{s_{NN}} \sim 10$  GeV*

# When is negative $v_1$ slope generated ?

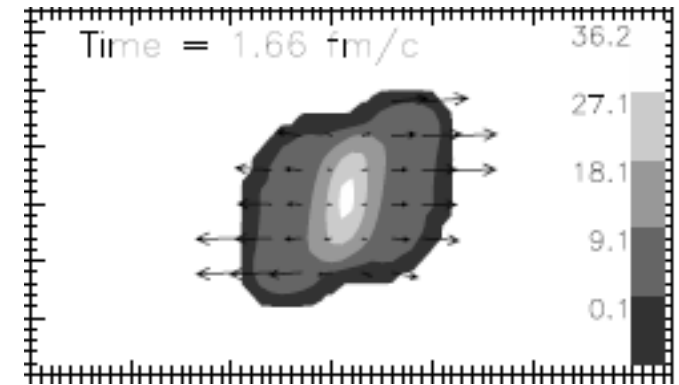
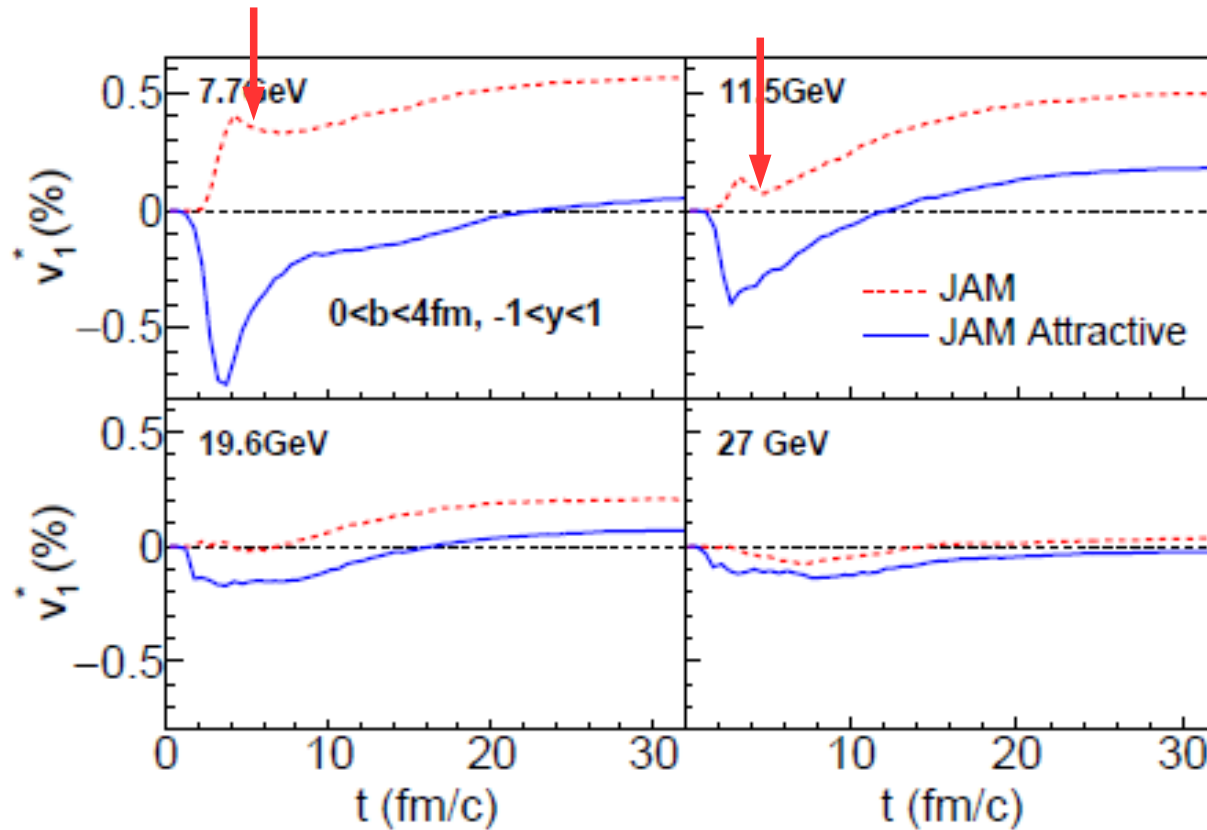
Nara, AO, Stöcker ('16)



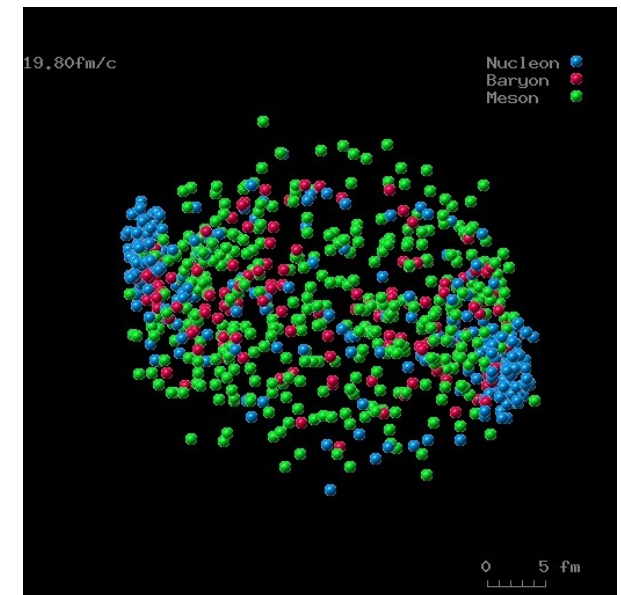
*We need to make  $v_1$  slope negative in the compressing stage.*

# Tilted Ellipsoid ?

Nara, AO, Stöcker ('16)



**18 GeV, 3-fluid**  
**Toneev et al. ('03)**



Transport model results also show tilted-ellipsoid-like behavior, but it is not enough.

# Summary

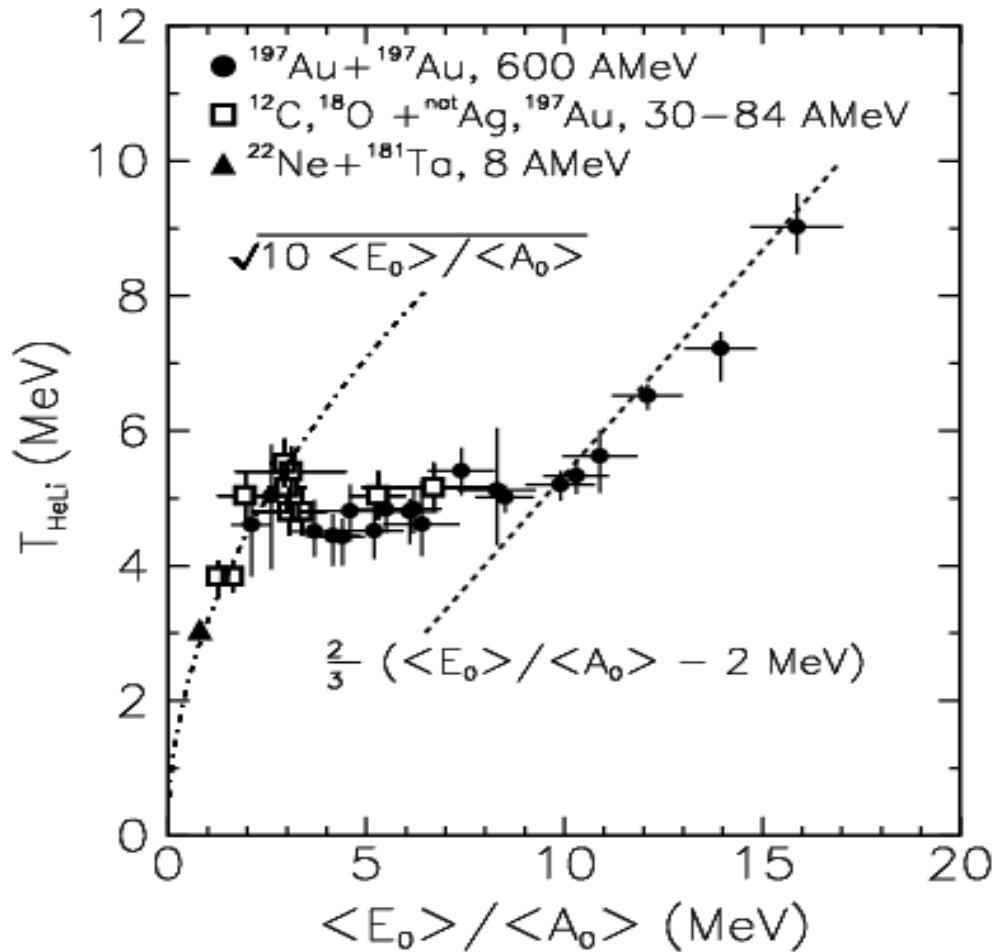
- We may see **QCD phase transition (1<sup>st</sup> or 2<sup>nd</sup>) signals at BES (or J-PARC) energies** in baryon number cumulants and  $v_1$  slope.
- **Hadronic transport models cannot explain negative  $v_1$  slope below  $\sqrt{s_{NN}} = 20$  GeV.**
  - Geometric (bowling pin) mechanism becomes manifest at higher energies (JAM, JAM-MF, HSD, PHSD, UrQMD, ....).
- **Hadronic transport with EOS softening can describe negative  $v_1$  slope below  $\sqrt{s_{NN}} = 20$  GeV.**
  - **Attractive orbit scattering** simulates EOS softening (virial theorem).
  - We need more studies to confirm its nature.  
First-order phase transition ? Crossover ? Forward-backward rapidities ? MF leading to softer EOS ?
- ***We need “re-hardening” at higher energies, e.g.  $\sqrt{s_{NN}} = 27$  GeV.***

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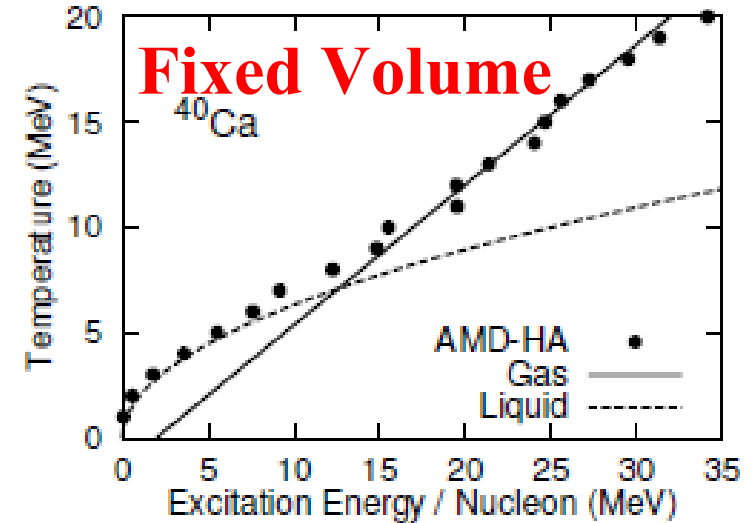
*Thank you !*

# Nuclear Liquid-Gas Phase Transition

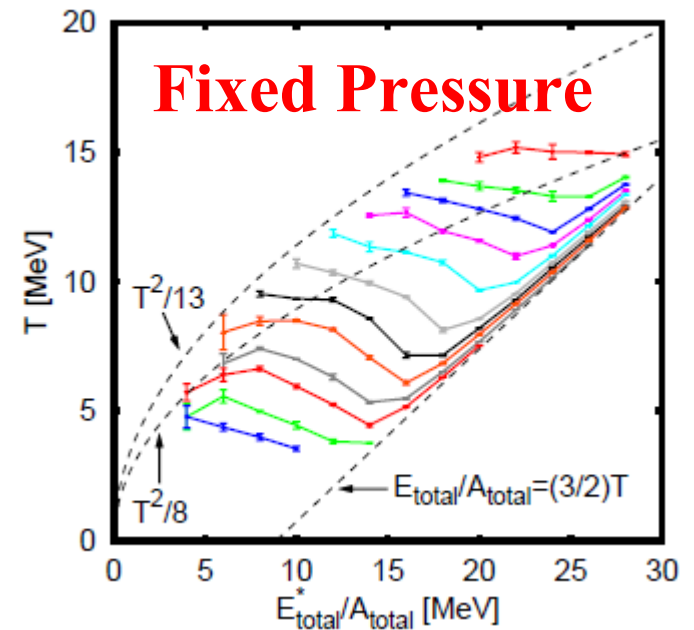
- Caloric curve  $\rightarrow$  LG phase transition (Smoking gun)



*J. Pochadzalla et al. (GSI-ALLADIN collab.), PRL 75 (1995) 1040.*



*A.O. Randrup ('98)*

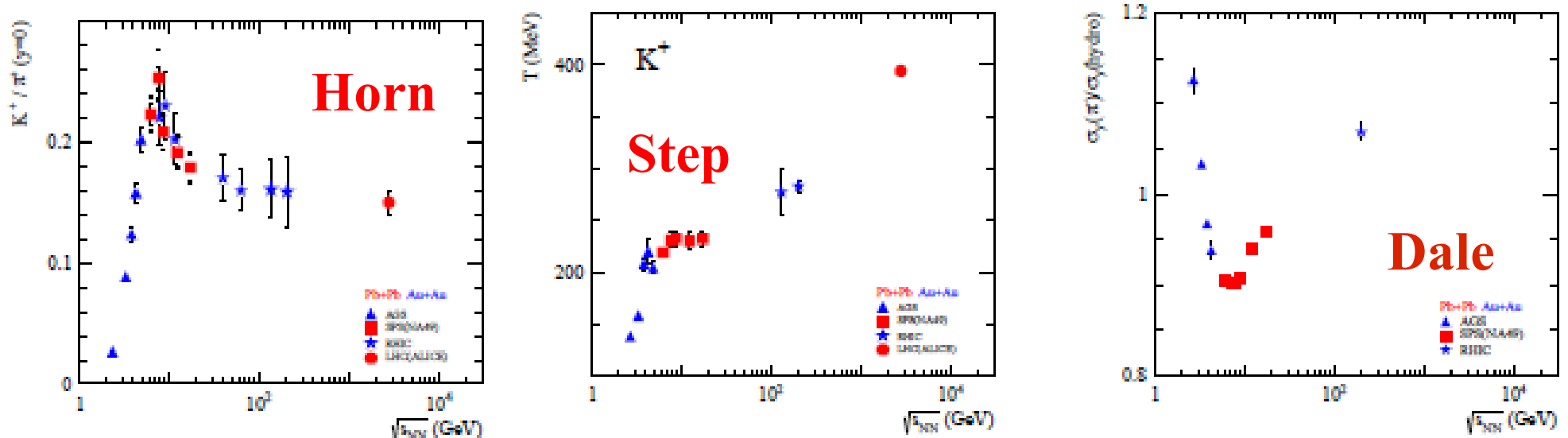


*T. Furuta, A. Ono ('09)*

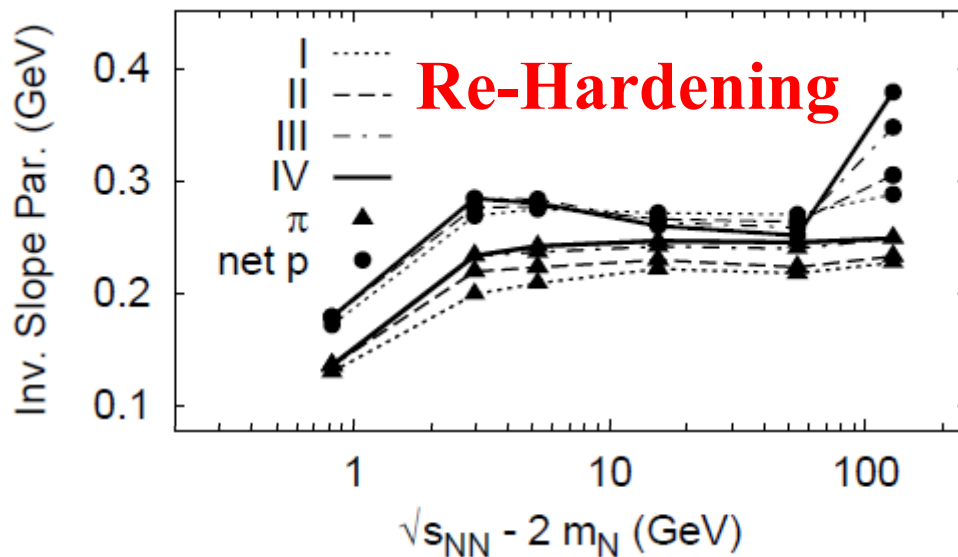


# Horn, Step and Dale

- Non-monotonic behavior in  $K^+/\pi^+$  ratio (Horn),  
 m slope par. (Step or re-hardening) rapidity dist width of  $\pi$



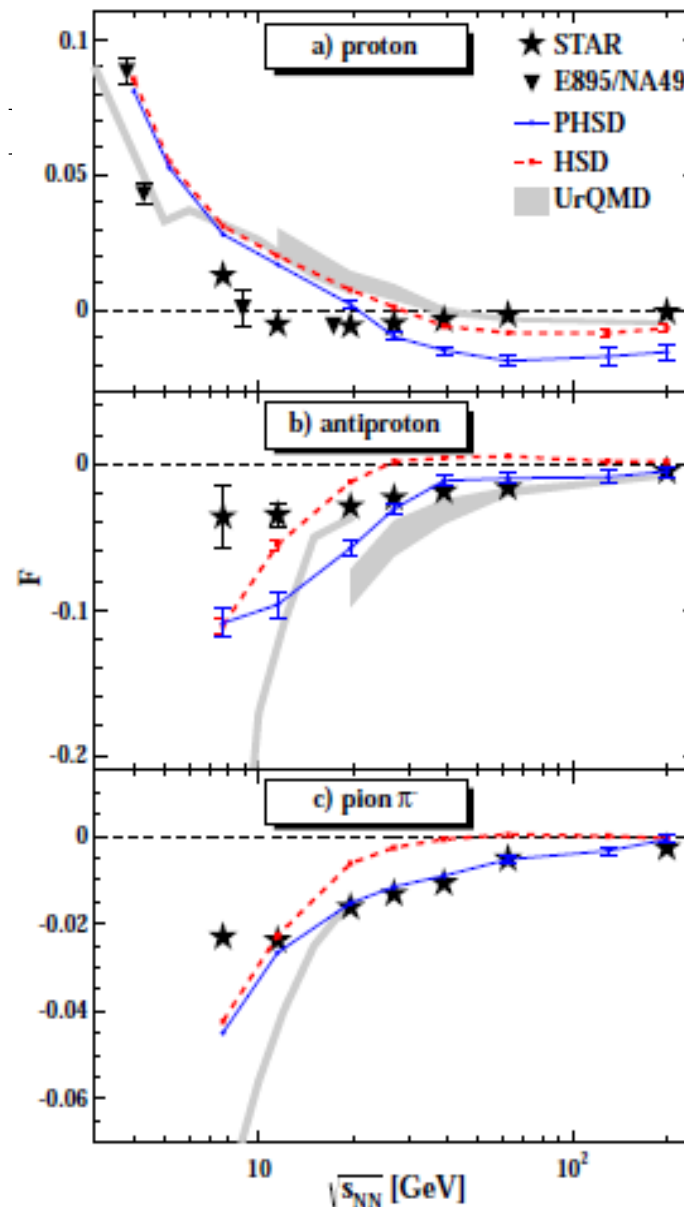
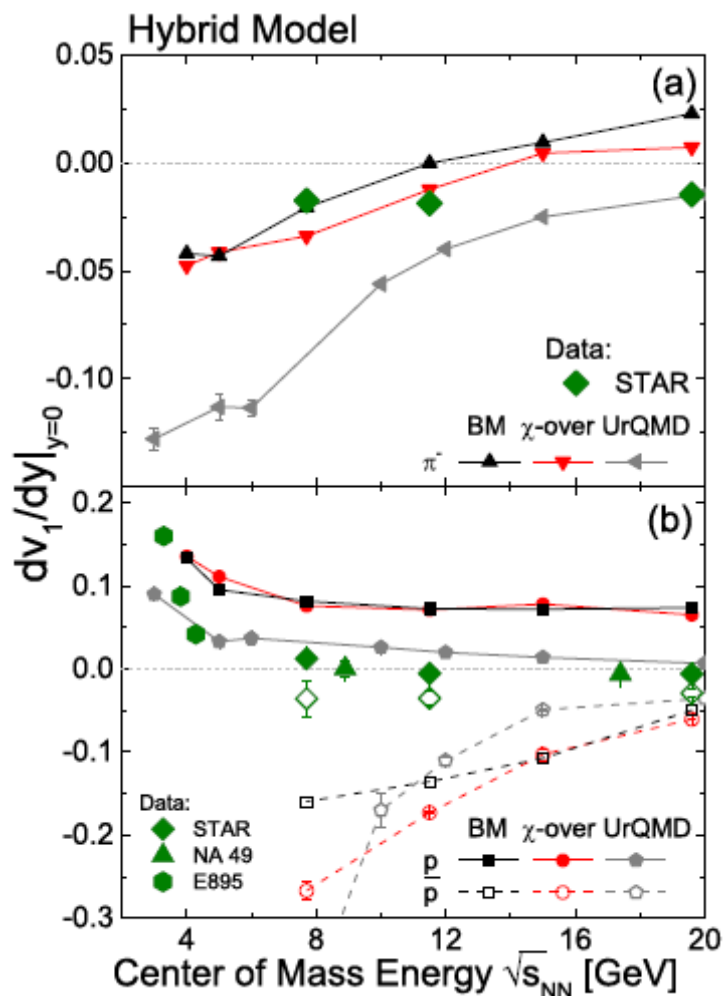
*E.g. A. Rustamov (2012)*



*N. Otuka, P.K.Sahu, M. Isse,  
 Y. Nara, AO, nucl-th/010205*

# Hybrid Approaches

- Both Hybrid model (Frankfurt) and PHSD (Giessen) show higher balance



*J. Steinheimer, J. Auvinen, H. Petersen,  
M. Bleicher, H. Stöcker, PRC89 ('14) 054913*

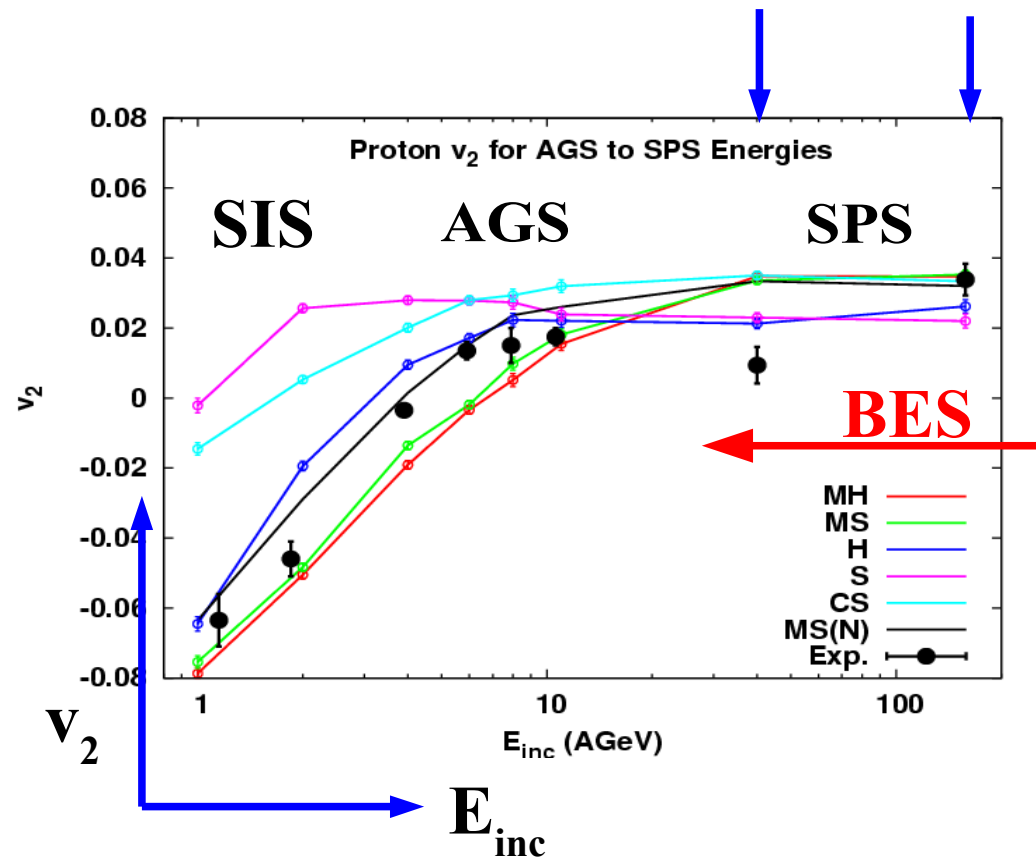
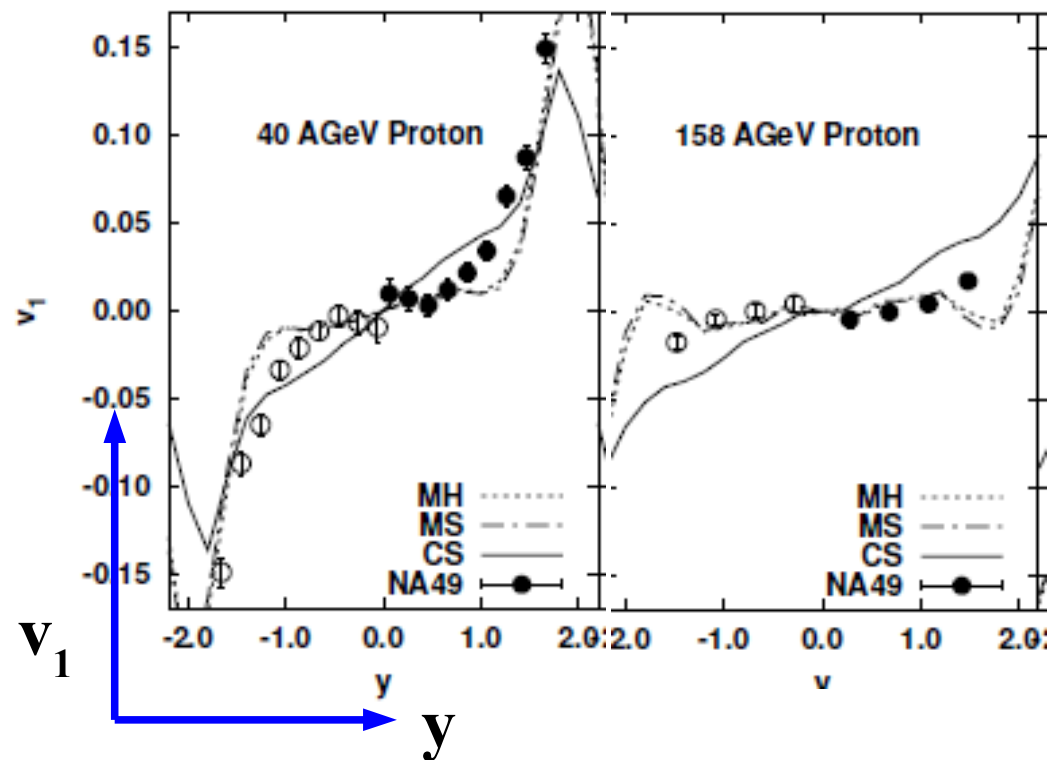
*V. P. Konchakovski, W. Cassing, Yu. B. Ivanov,  
V. D. Toneev, PRC90('14)014903*

# JAM results at AGS and SPS Energies

- JAM w/ Mean-Field effects roughly explains  $v_1$  and  $v_2$  at AGS & SPS

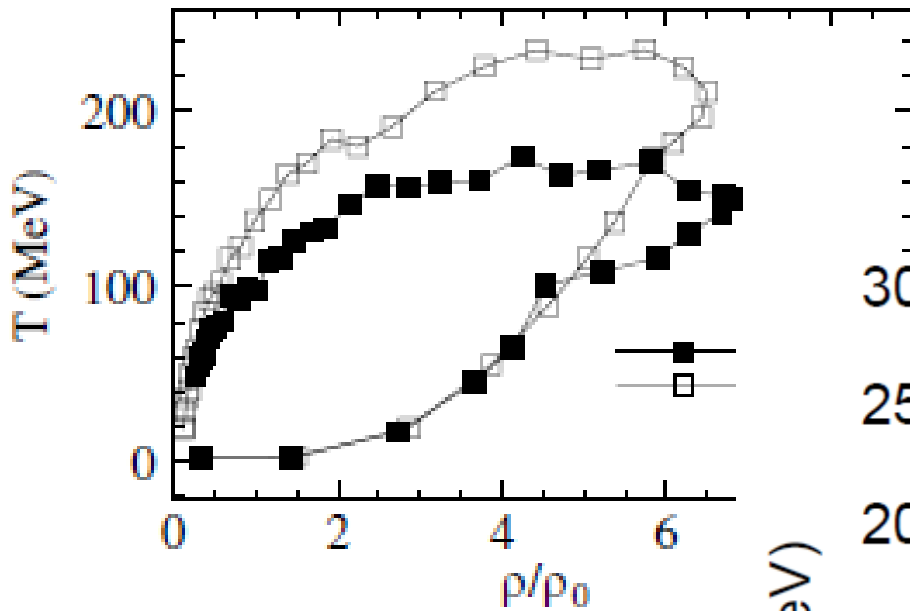
(1-158 A GeV  $\rightarrow \sqrt{s_{NN}} = 2.5-20$  GeV)

$\sqrt{s_{NN}} = 8.9$  GeV     $\sqrt{s_{NN}} = 17.3$  GeV

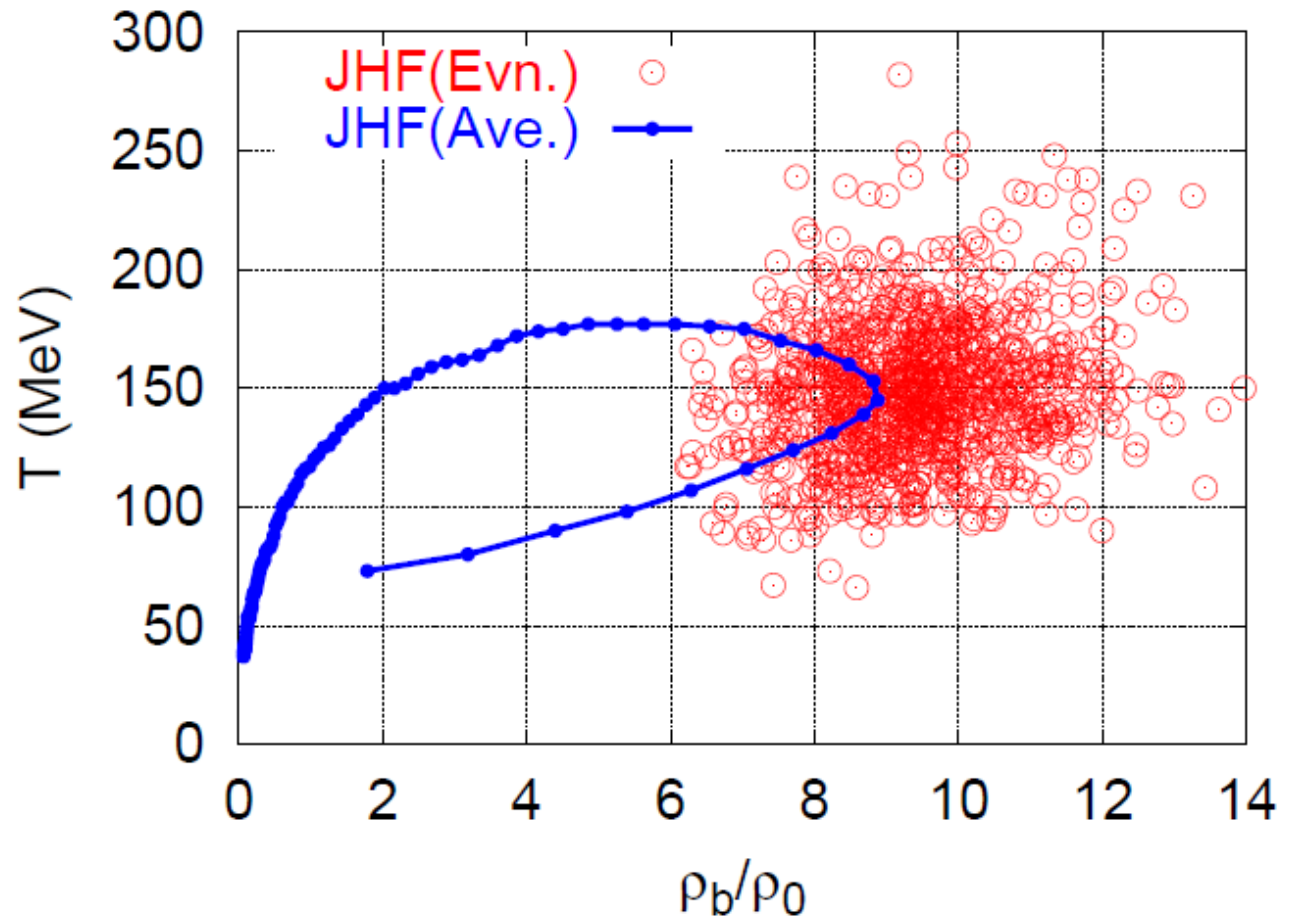


M. Isse, AO, N. Otuka, P. K. Sahu, Y. Nara, PRC72('05)064908

# Highest Density Matter at J-PARC ?



Nara, Otuka, AO,  
Maruyama ('97)



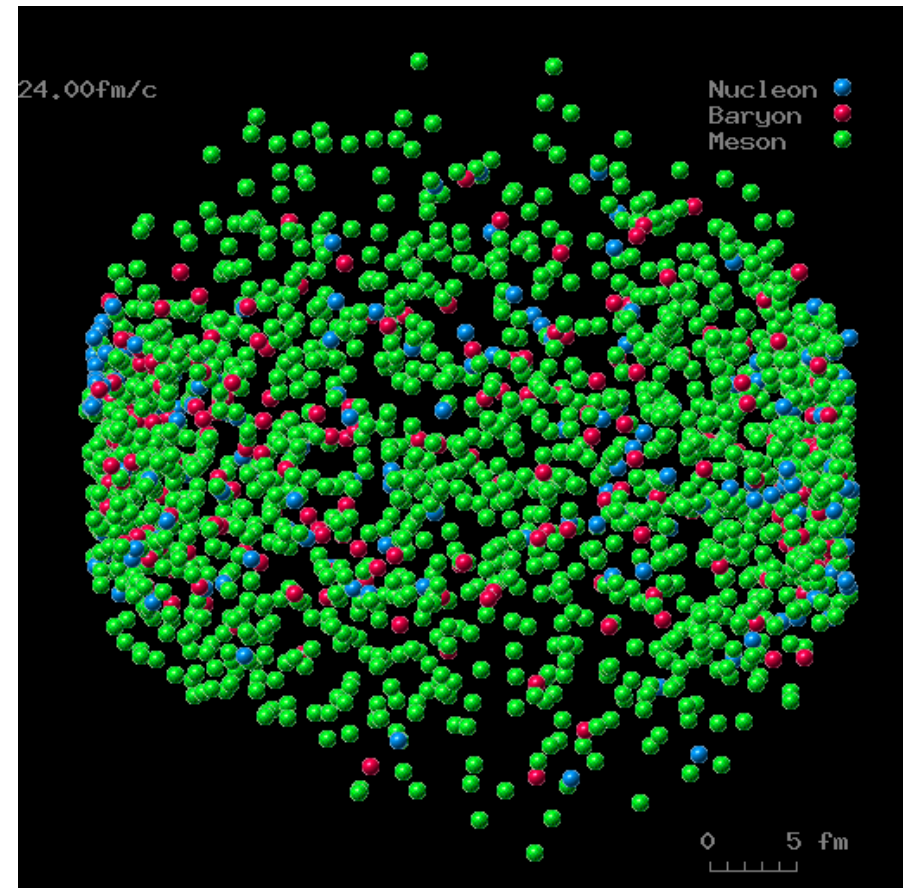
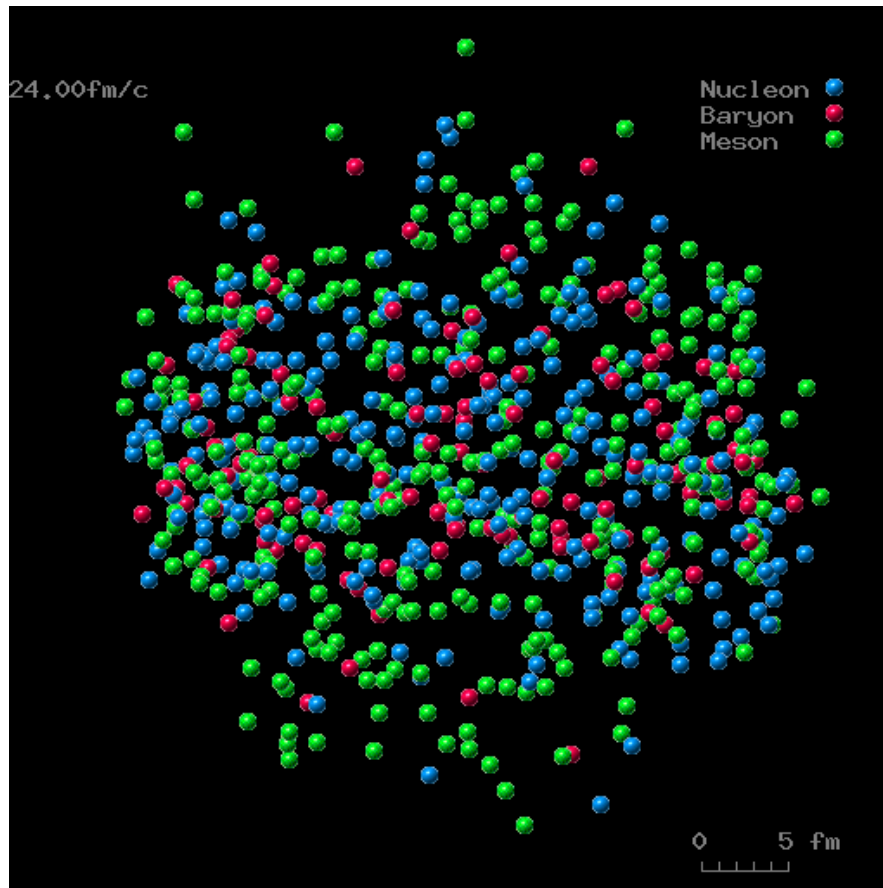
Central  $1 \text{ fm}^3$  cube.

大西、JHF workshop (2002)

# How do heavy-ion collisions look like ?

Au+Au, 10.6 A GeV

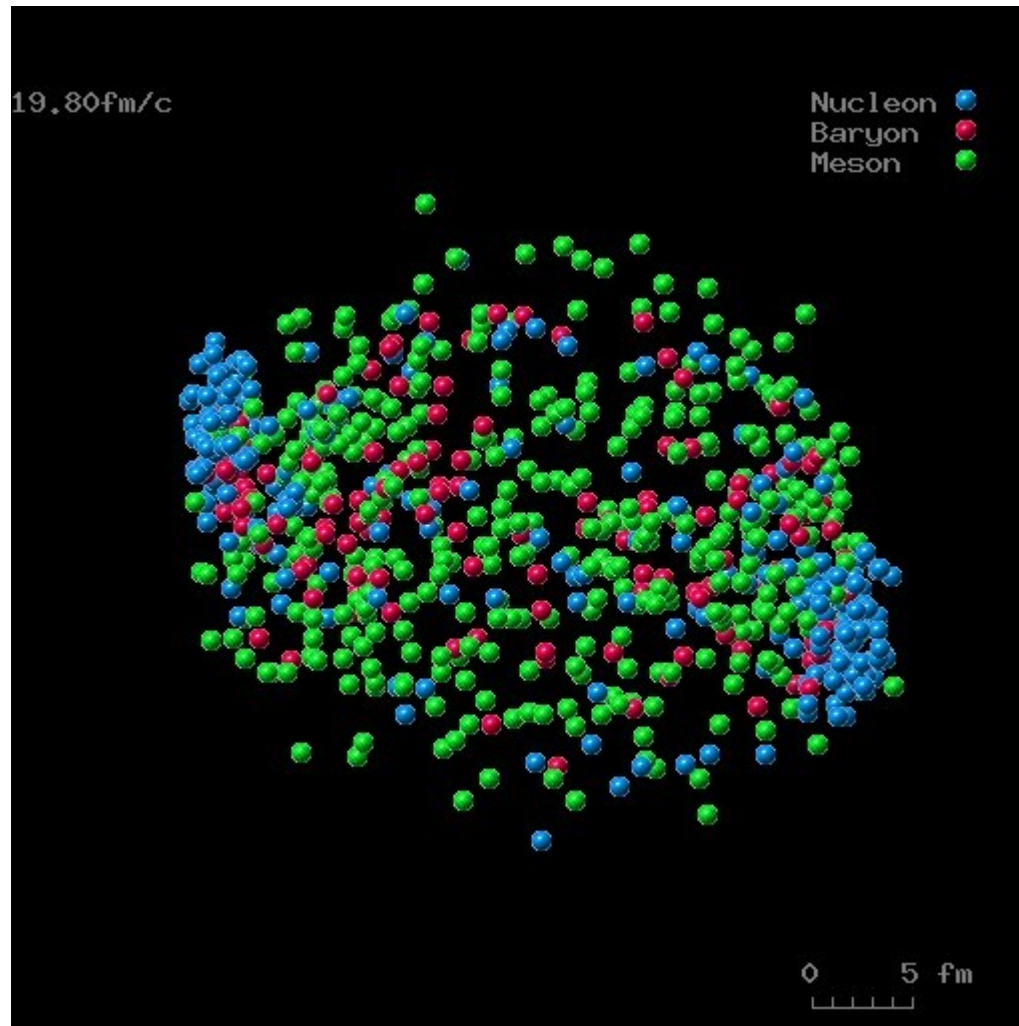
Pb+Pb, 158 A GeV



JAMming on the Web <http://www.jcprg.org/jow/>

A. Ohnishi @ YITP-IOPP, Feb.20, 2016 29

# J-PARC energy



**Au+Au, 25 AGeV, b=5 fm (JOW)**

# *QCD phase transition at BES (J-PARC) Energies ?*

- ***J-PARC Energies:***  $\sqrt{s_{NN}} = 4-40$  GeV (or  $\sqrt{s_{NN}} = 1.9-6.2$  GeV)
  - $E(p)=30$  GeV  $\rightarrow E(\text{Au}) \sim 12$  AGeV (full strip,  $\sqrt{s_{NN}} = 5.1$  GeV for Au+Au)
  - $E(p)=50$  GeV  $\rightarrow E(\text{Au}) \sim 20$  AGeV ( $\sqrt{s_{NN}} = 6.4$  GeV)
  - $E(p)=30$  GeV (50 GeV) Collider  $\rightarrow \sqrt{s_{NN}} = 26$  GeV (42 GeV)
- **Two Aspects of J-PARC energies**
  - Formation of highest baryon density matter
  - Various non-monotonic behaviors  $\rightarrow$  Onset of deconfinement

# *QCD phase transition at BES (J-PARC) Energies ?*

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  - **Various non-monotonic behaviors  $\rightarrow$  Onset of deconfinement**

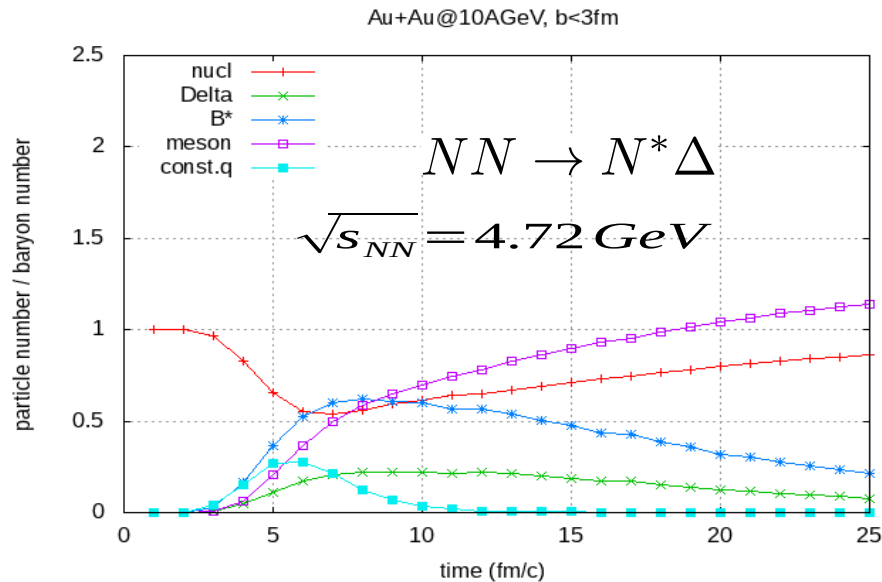
## *Question*

*Do these Non-mono. behaviors signal the onset of QCD phase transition and/or QCD critical point ?  
or Do they show some properties of hadronic matter ?  
 $\rightarrow$  Let's examine in hadronic transport models !*

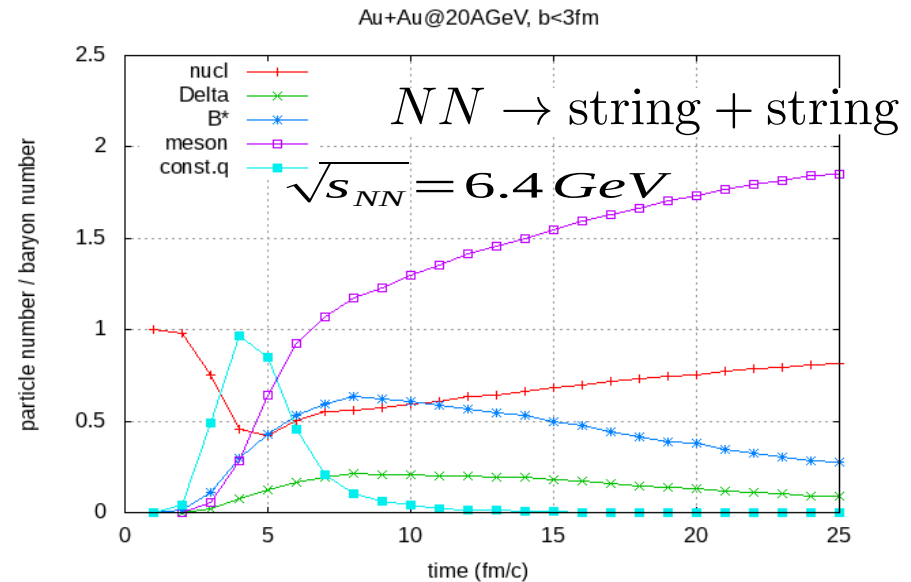


# How to treat mean-field for excited matter?

## Hadronic resonance dominant



## constituent quark dominant due to string



**Model 1 JAM/M: potential for all formed baryons**

**Model 2 JAM/Mq: potentials for quarks inside the pre-formed hadrons**

**Model 3: JAM/Mf: both formed and pre-formed baryons**

# Hadronic transport Approach

**Purpose : Effects of hadron mean field potential on the directed flow  $v_1$**

**JAM hadronic cascade model : resonance and string excitation**

**Mean field by the framework of the Relativistic Quantum Molecular Dynamics**

**Nuclear cluster formation by phase space coalescence.**

**Statistical decay of nuclear fragment**

# Relativistic QMD/Simplified (RQMD/S)

**RQMD** based on Constraint Hamiltonian Dynamics

Sorge, Stoecker, Greiner, Ann. Phys. 192 (1989), 266.

**RQMD/S**: Tomoyuki Maruyama, et al. Prog. Theor. Phys. 96(1996),263.

Single particle energy:  $p_i^0 = \sqrt{\mathbf{p}_i^2 + m_i^2 + 2m_i V_i}$

$$\dot{\mathbf{r}}_i = \frac{\mathbf{p}_i}{p_i^0} + \sum_j \frac{m_j}{p_j^0} \frac{\partial V_j}{\partial \mathbf{p}_i} \quad \dot{\mathbf{p}}_i = - \sum_j \frac{m_j}{p_j^0} \frac{\partial V_j}{\partial \mathbf{r}_i}$$

Arguments of potential  $\mathbf{r}_i - \mathbf{r}_j$  and  $\mathbf{p}_i - \mathbf{p}_j$  are replaced by the distances in the two-body c.m.

# Relativistic QMD/Simplified (RQMD/S)

## ■ RQMD = Constraint Hamiltonian Dynamics

*(Sorge, Stocker, Greiner, Ann. of Phys. 192 (1989), 266.)*

## ■ Constraints: $\varphi \approx 0$ (Satisfied on the realized trajectory, by Dirac)

- Variables in Covariant Dynamics =  $8N$  phase space:  $(q_\mu, p_\mu)$

- Variables in EOM =  $6N$  phase space

→ We need  $2N$  constraints to get EOM

## ■ On Mass-Shell Constraints

$$H_i \equiv p_i^2 - m_i^2 - 2m_i V_i \approx 0$$

## ■ Time-Fixation in RQMD/S

$$\chi_i \equiv \hat{a} \cdot (q_i - q_N) \approx 0 \quad (i=1, \sim N-1) \quad , \quad \chi_N \equiv \hat{a} \cdot q_N - \tau \approx 0$$

$\hat{a}$  = Time-like unit vector in the Calculation Frame

*(Tomoyuki Maruyama et al., Prog. Theor. Phys. 96(1996), 263.)*

# RQMD/S (cont.)

- Hamiltonian is made of constraints

$$H = \sum_i u_i \phi_i \quad (\phi_i = H_i (i=1 \sim N), \chi_{i-N} (i=N+1 \sim 2N))$$

- Time Development  $\frac{d f}{d \tau} = \frac{\partial f}{\partial \tau} + \{f, H\}$  ,  $\{q_\mu, p_\nu\} = g_{\mu\nu}$

- Lagrange multipliers are determined to keep constraints

→ *We can obtain the multipliers analytically in RQMD/S*

$$\frac{d \phi_i}{d \tau} \approx 0 \rightarrow \delta_{i,2N} + \sum_j u_j \{\phi_i, \phi_j\} \approx 0$$

- Equations of Motion

$$H = \sum_i (p_i^2 - m_i^2 - 2m_i V_i) / 2p_i^0, \quad p_i^0 = E_i = \sqrt{\vec{p}_i^2 + m_i^2 + 2m_i V_i}$$

$$\frac{d \vec{r}_i}{d \tau} \approx -\frac{\partial H}{\partial \vec{p}_i} = \frac{\vec{p}}{p_i^0} + \sum_j \frac{m_j}{p_j^0} \frac{\partial V_j}{\partial \vec{p}_i}, \quad \frac{d \vec{p}_i}{d \tau} \approx \frac{\partial H}{\partial \vec{r}_i} = -\sum_j \frac{m_j}{p_j^0} \frac{\partial V_j}{\partial \vec{r}_i}$$

*We can include MF in an almost covariant way in molecular dynamics*

## Particle “DISTANCE”

$$r_{Tij}^2 \equiv r_\mu r^\mu - \left( r_\mu P_{ij}^\mu \right)^2 / P_{ij}^2 = \vec{r}^2 \quad (\text{in } CM)$$

$$P_{ij} \equiv p_i + p_j \quad , \quad r \equiv r_i - r_j$$

## Particle “Momentum Difference”

$$p_{Tij}^2 \equiv p_\mu p^\mu - \left( p_\mu P_{ij}^\mu \right)^2 / P_{ij}^2 = \vec{p}^2 \quad (\text{in } CM)$$

$$p \equiv p_i - p_j$$

*Lorentz Invariant, and Becomes Normal Distance in CM !*