

2 粒子・3 粒子運動量相関から探る ハドロン間相互作用

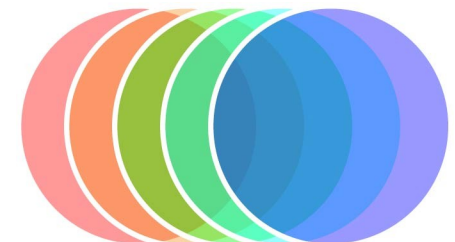
京都大学・基礎物理学研究所 大西 明

第6回クラスター階層領域研究会

新学術領域「量子クラスターで読み解く物質の階層構造」

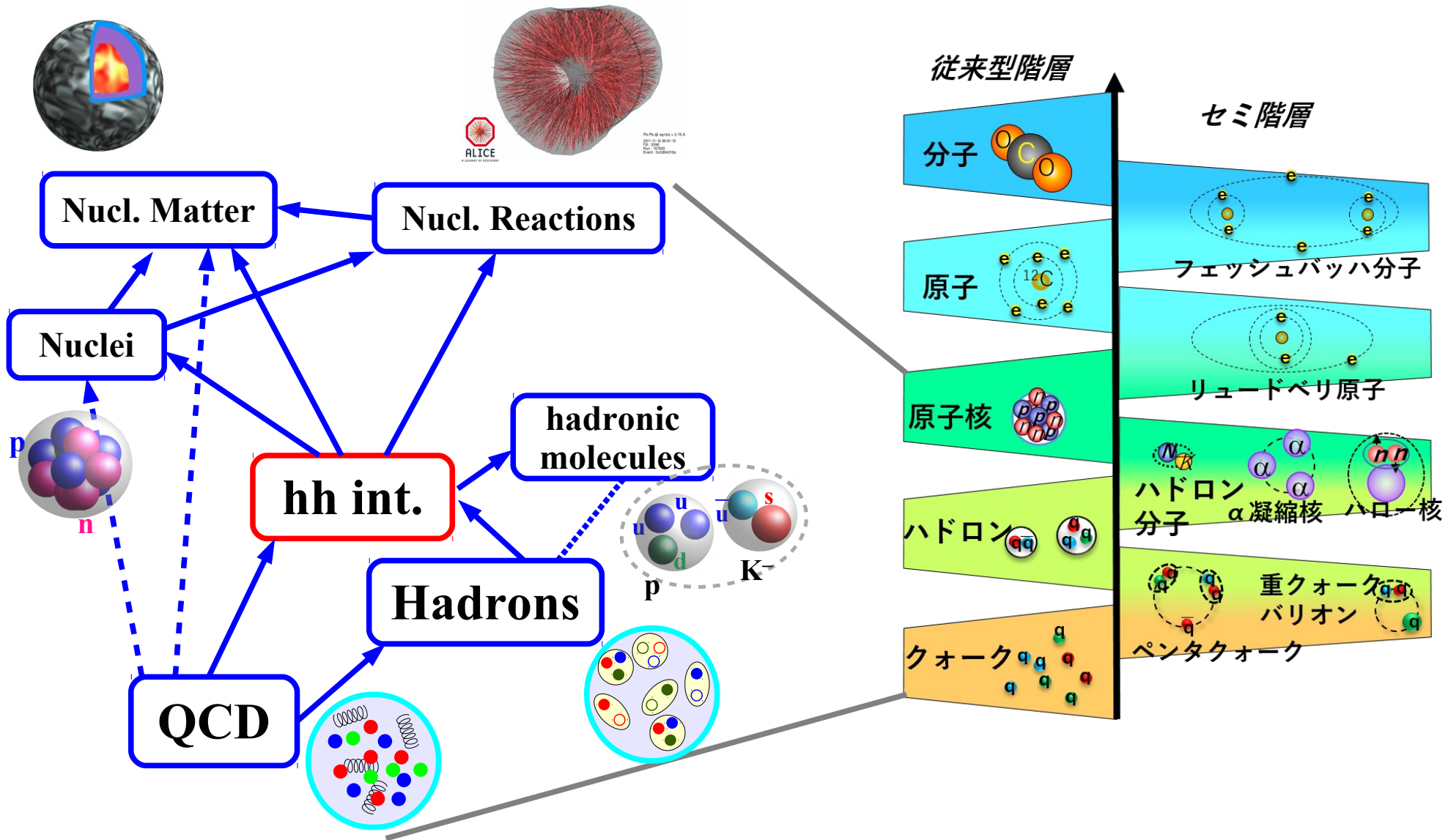
June 14 & 19, 2021, Online

- Introduction: 2 粒子運動量相関からハドロン間相互作用へ
- 「2 粒子運動量相関から探るハドロン間相互作用としきい値近辺の散乱振幅」の成果報告 (19H05151, 2019-20 年度, 40+40 万円)
- 新たな課題 (21H00121, 2021-23 年度, 30+30 万円)
 - 重陽子 - ハドロン相関、チャームハドロン、3 体相関
- Summary



Clusters & Hierarchies

Cluster & Hierarchies



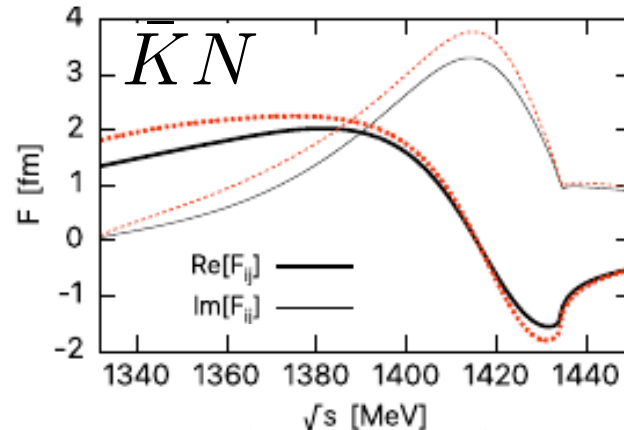
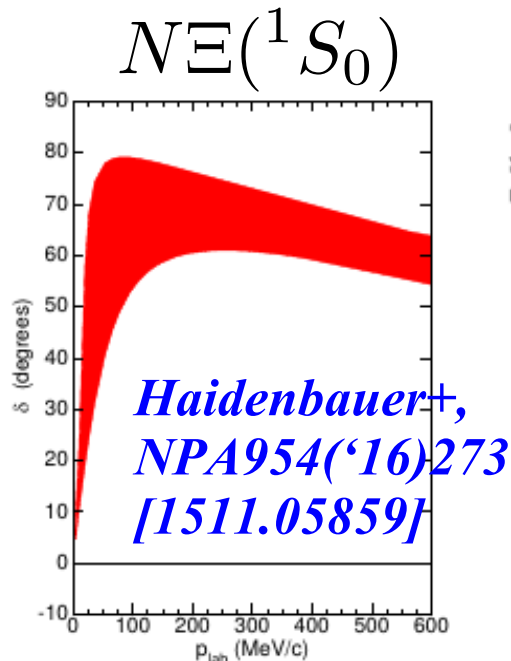
ハドロン間相互作用は原子核を含むハドロン多体問題の基礎入力

How can we access flavored hh interactions ?

Theoretical approaches

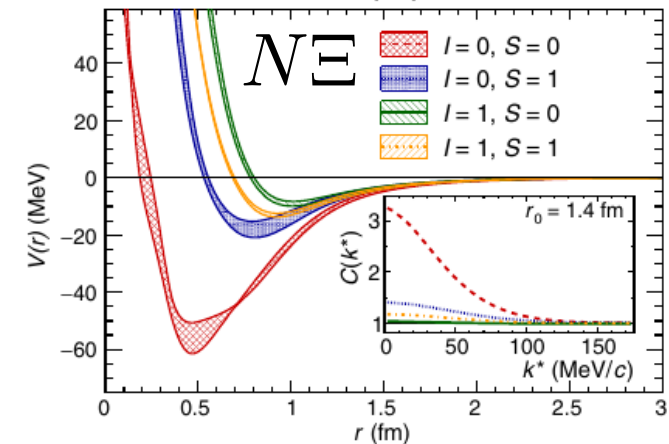
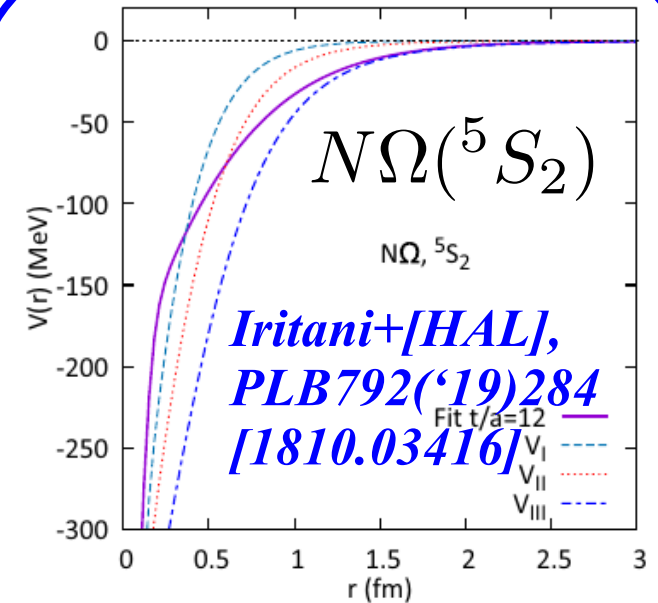
- Nuclear force models: meson exch., quark model, ... (need **data**)
- *Ab initio*: chiral EFT (χ EFT), lattice QCD (need **data** or **CPU resources**)

Chiral



*Miyahara, Hyodo,
Weise, PRC98('18),
025201 [1804.08269]
(Ikeda-Hyodo-Weise
amplitude)*

Lattice



*Sasaki+ [HAL], NPA998
(‘20)121737 [1912.08630]
(taken from ALICE(‘19))*

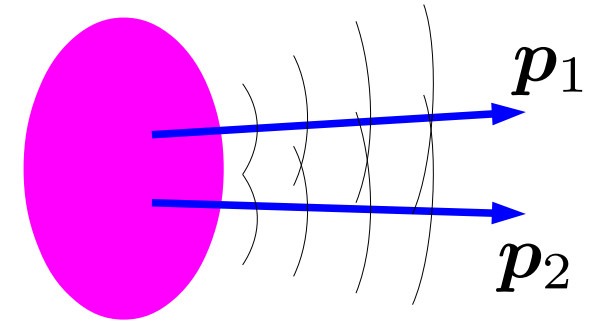
How can we access flavored hh interactions ?

■ Experimental approaches

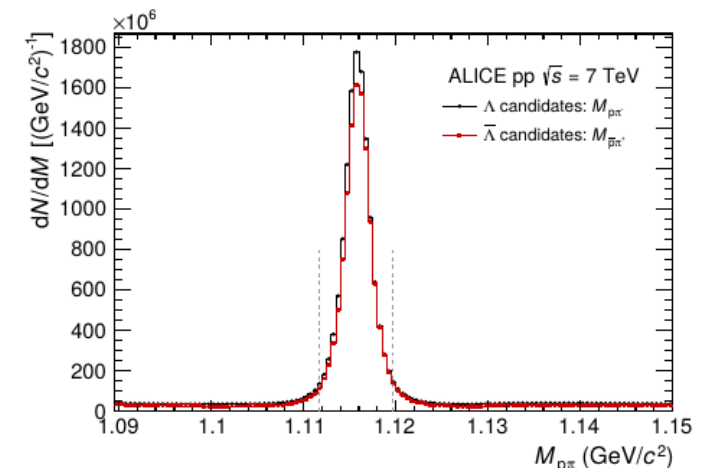
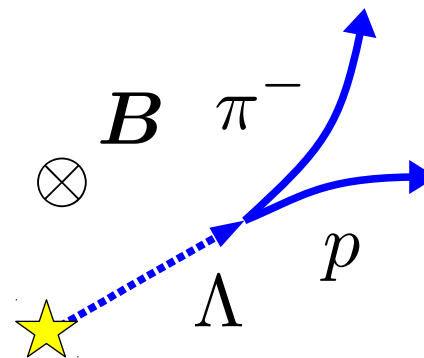
- hh scattering (NN, YN, π N, KN)
- Hadronic nuclei (normal nuclei, hypernuclei, kaonic nuclei) and atom (π^- , K^- , Σ^- , Ξ^- , ...)
- **Femtoscopy**

■ Femtoscopic study of hh interactions

- Applicable to various hh pairs (NN, YN, KN, DN, YY, Yd, YNN, ...)
- Valid when the source is chaotic
- Weakly decaying particles → Good pair purity
- Future measurements: Charmed hadron, hNN, ...



$$C(q) = \frac{N_{12}(p_1, p_2)}{N_1(p_1)N_2(p_2)} = \frac{N_{12}^{\text{same}}(p_1, p_2)}{N_{12}^{\text{mixed}}(p_1, p_2)}$$



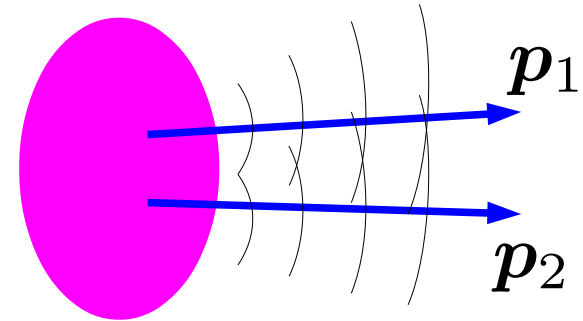
ALICE [1805.12455]

2 粒子運動量相関関数

- 粒子の放出点分布関数

$$N_i(\mathbf{p}) = \int d^4x S_i(x, \mathbf{p})$$

- 2 粒子運動量相関関数



- 2 粒子が独立に作られ、終状態の波動関数で相関が作られるとする。

Koonin('77), Pratt+('86), Lednicky+('82)

2 粒子 w.f.

$$C(\mathbf{q}) = \frac{N_{12}(\mathbf{p}_1, \mathbf{p}_2)}{N_1(\mathbf{p}_1)N_2(\mathbf{p}_2)} \simeq \frac{\int d^4x d^4y S_1(x, \mathbf{p}_1) S_2(y, \mathbf{p}_2) |\Psi_{\mathbf{p}_1, \mathbf{p}_2}(x, y)|^2}{\int d^4x d^4y S_1(x, \mathbf{p}_1) S_2(x, \mathbf{p}_2)}$$

$$= \int dr S(r) |\varphi(r; \mathbf{q})|^2 = 1 + \int dr S(r) [|\varphi_0(r; \mathbf{q})|^2 - |j_0(qr)|^2]$$

重心座標積分 ソース関数

相対波動関数

s 波

球対称ソース・異種粒子
・s 波のみ・クーロン無し

- 運動量相関の利用方法

- 相関関数 + 波動関数 → ソースサイズ

Hanbury Brown & Twiss ('56); Goldhaber, Goldhaber, Lee, Pais ('60)

- 相関関数 + ソース関数 → ハドロン間相互作用

R. Lednicky, V. L. Lyuboshits ('82); K. Morita, T. Furumoto, AO ('15)

Bird's-eye view of $C(q)$

- 相関関数の大まかな振る舞い→漸近形を用いた解析模型 (LL 模型)

R. Lednicky, V. L. Lyuboshits ('82)

$$C(q) = 1 + \frac{|f(q)|^2}{2R^2} F_3\left(\frac{r_{\text{eff}}}{R}\right) + \frac{2\text{Re} f(q)}{\sqrt{\pi}R} F_1(2qR) - \frac{2\text{Im} f(q)}{R} F_2(2qR)$$

$$f(q) = [q \cot \delta - iq]^{-1}, \quad F_1(x) = \int_0^x dt e^{t^2 - x^2} / x, \quad F_2(x) = (1 - e^{-x^2}) / x, \quad F_3(x) = 1 - x / 2\sqrt{\pi}$$

(漸近形・ガウス型ソース・s波・クーロン無し・1チャンネル・異種粒子・スピン因子無視)

- 引力 ($a_0 < 0$) による wf 増大

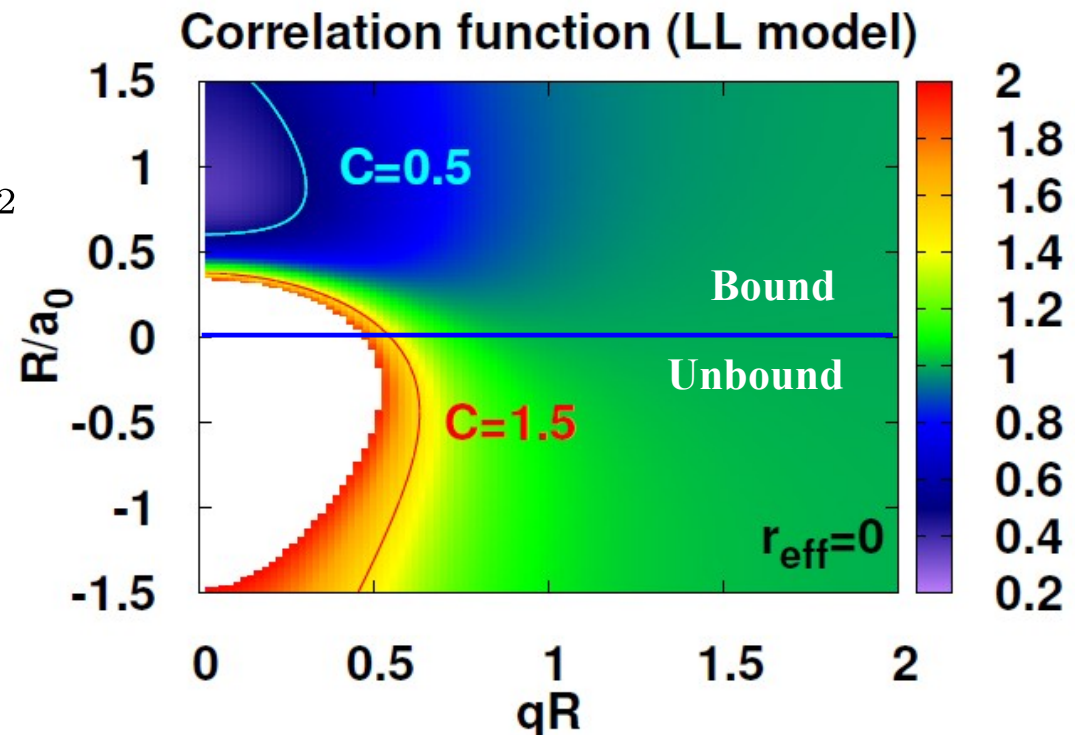
→ $C(q)$ の増大

$$C_{\text{LL}}(0) = 1 - \frac{2}{\sqrt{\pi}} \left(\frac{a_0}{R}\right) + \frac{1}{2} \left(\frac{a_0}{R}\right)^2$$

- 斥力 or 束縛状態あり ($a_0 > 0$)

→ $r \sim a_0$ で wf に節

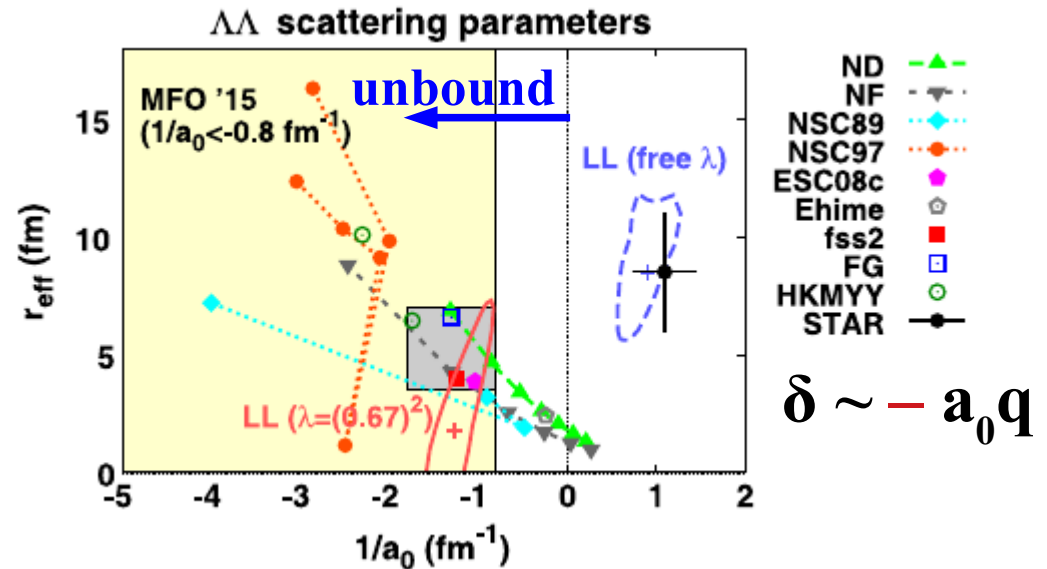
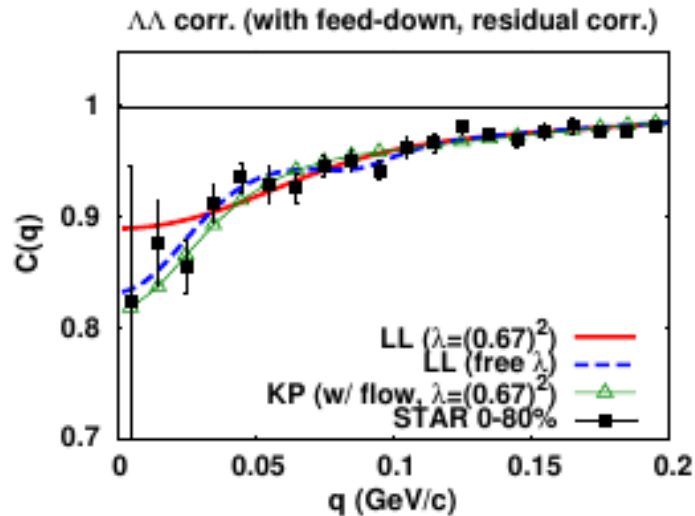
→ $R \sim a_0$ で $C(q)$ の抑制



Example: Λ correlation fn. and Λ interaction

$$C(\mathbf{q}) = 1 - \frac{\lambda}{2} e^{-4q^2 R^2} + \frac{\lambda}{2} \int dr S(r) \{ |\varphi_0(r)|^2 - |j_0(qr)|^2 \}$$

$\lambda =$ pair purity prob.



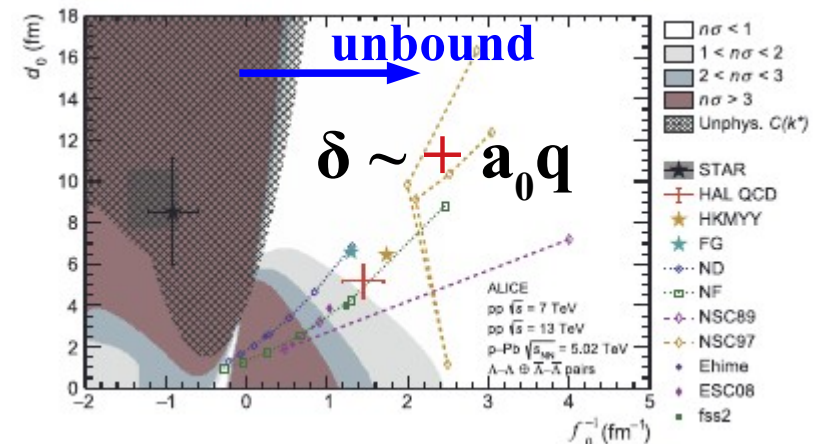
- ND ▲
- NF ●
- NSC89 ◆
- NSC97 ●
- ESC08c ◆
- Ehime ☆
- fss2 ■
- FG □
- HKMY ○
- STAR ●

$$\delta \sim -a_0 q$$

*L. Adamczyk+[STAR],
PRL114('15)022301;
K.Morita, T.Furumoto, AO,
PRC 91('15)024916;
AO, K. Morita, K. Miyahara,
T. Hyodo, NPA954('16)294.*

$$-1.25 \text{ fm} < a_0 < 0.$$

*S. Acharya+[ALICE],
PLB797('19)134822*



2 粒子運動量相関から探るハドロン間相互作用としきい値近辺の散乱振幅 (19H05151 成果報告)

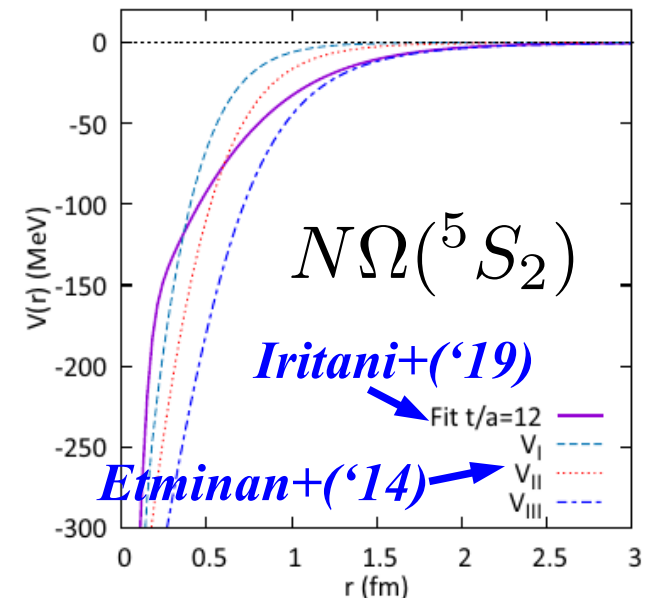
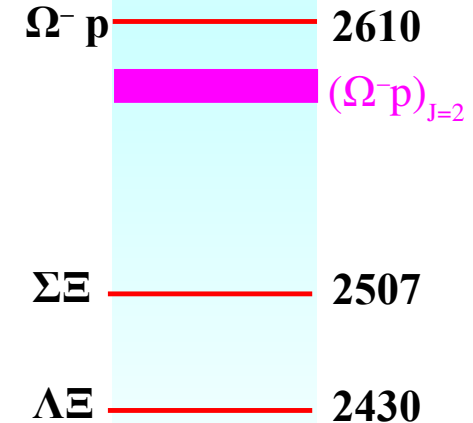
- Probing $\Omega\Omega$ and $p\Omega$ dibaryons with femoscopic correlations in relativistic heavy-ion collisions, K. Morita, S. Gongyo, T. Hatsuda, T. Hyodo, Y. Kamiya, AO, PRC101('20), 015201 (Editors' Suggestion).
- K^-p correlation function from high-energy nuclear collisions and chiral SU(3) dynamics, Y. Kamiya, T. Hyodo, K. Morita, AO, W. Weise, PRL124 ('20), 132501.
- Deuteron breakup effect on deuteron- Ξ correlation function, K. Ogata, T. Fukui, Y. Kamiya, and AO, PRC, to appear (arXiv:2103.00100).
- Femoscopic study of coupled-channel $N\Xi$ and $\Lambda\Lambda$ interactions, Y. Kamiya, K. Sasaki, T. Fukui, T. Hatsuda, T. Hyodo, K. Morita, K. Ogata, AO, in prep.

Ω_p correlation function

$N\Omega$ interaction and $N\Omega$ bound state

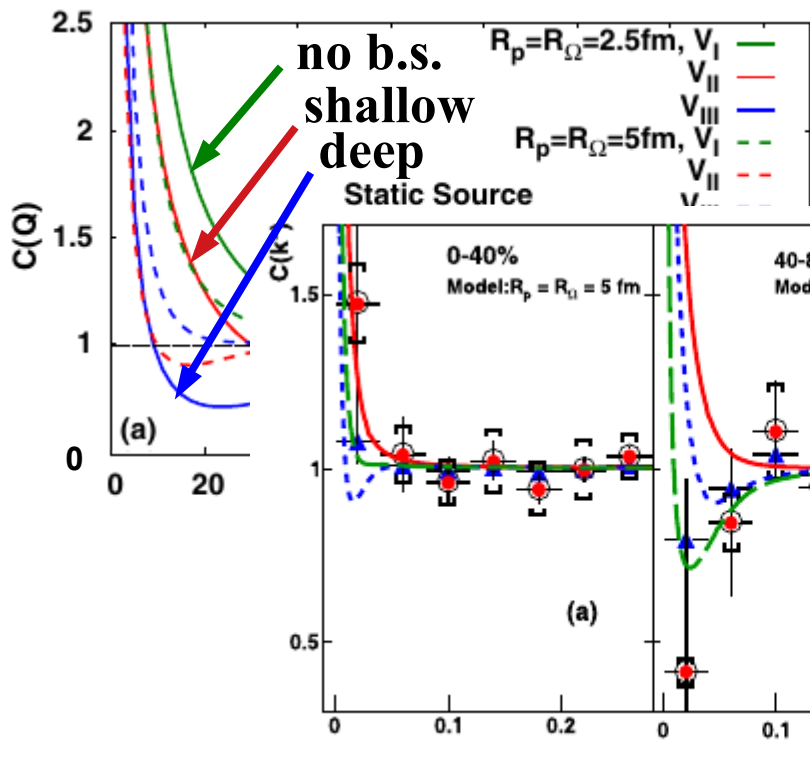
K. Morita, S. Gongyo, T. Hatsuda, T. Hyodo, Y. Kamiya, AO, PRC 101('20)015201.

- Ω^- (sss): $J^\pi=3/2^+$, $M=1672$ MeV
- Ω^- p bound state as a $S=-3$ dibaryon ?
 - No quark Pauli blocking in ΩN , $H=uuddss$, and $d^*=\Delta\Delta$ channels. *Oka ('88), Gal ('16)*
 - $J=2$ state (5S_2) couples to Octet-Octet baryon pair only with $L \geq 2$ → Small width is expected. *T. Goldman+, PRL59('87),627; F. Etminan+[HAL], NPA928('14)89; Iritani+[HAL], PLB792('19)284; Sekihara,Kamiya,Hyodo, PRC98('18)015205.*
 - Correlation has been measured at RHIC & LHC ! *STAR ('19); ALICE ('20)*



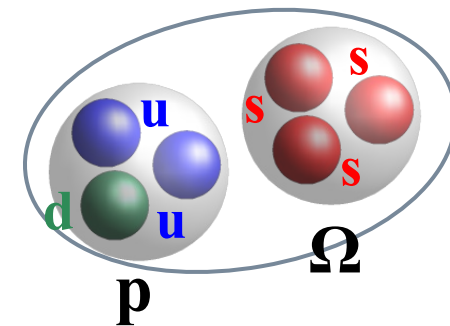
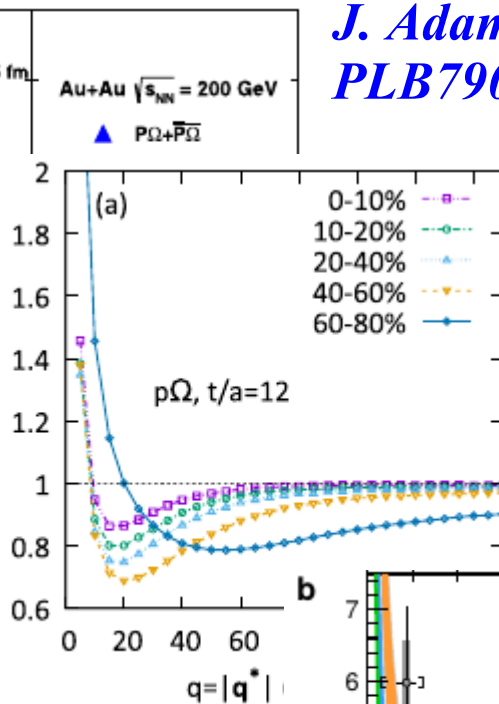
Let us try to discover the first $S<0$ dibaryon !

$p\Omega$ correlation function



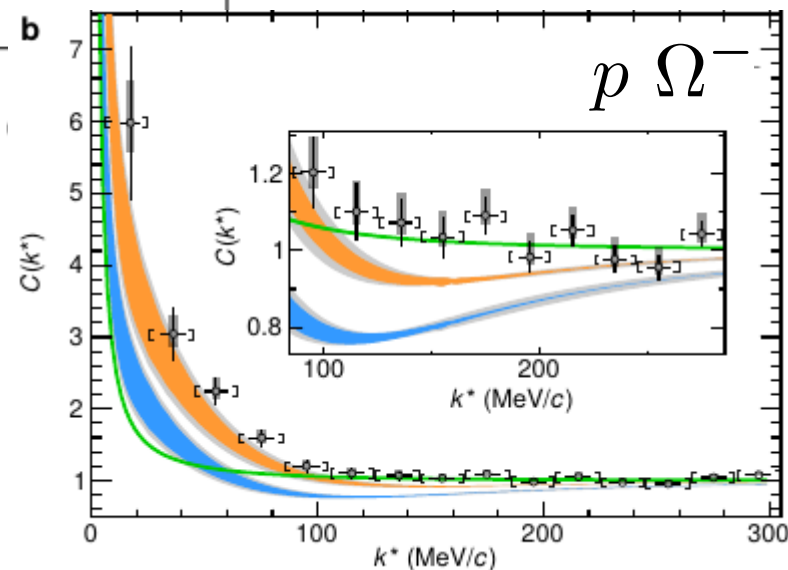
*K. Morita, AO, F. Etminan,
T. Hatsuda, PRC94('16)031901(R)
(w/ Lattice potential with heavier quark mass)*

*J. Adam+[STAR],
PLB790('19)490.*



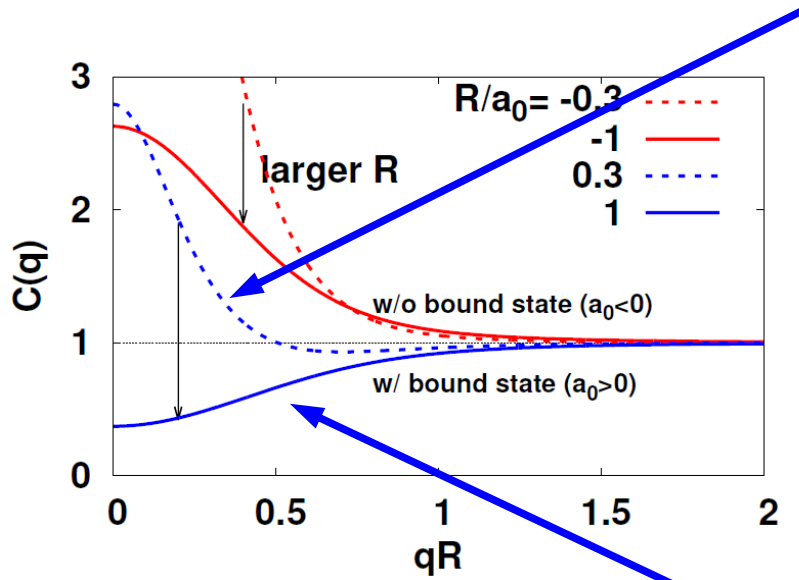
*K. Morita, S. Gongyo, T. Hatsuda,
T. Hyodo, Y. Kamiya, AO,
PRC 101('20)015201. (w/ Lattice
potential at physical quark mass,
 $a_0 \sim 3.4\text{ fm}$, expanding source)*

*S. Acharya+[ALICE],
Nature 588 ('20), 232
[2005.11495] (pp 13 TeV)*



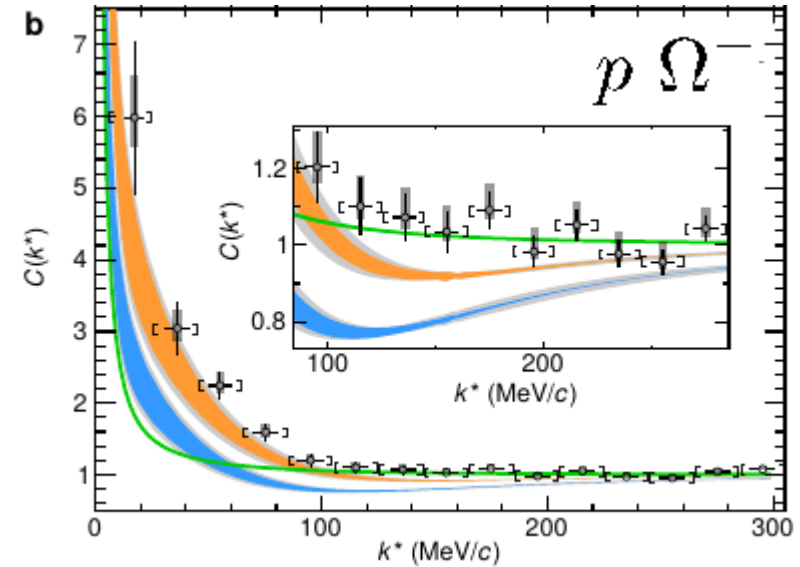
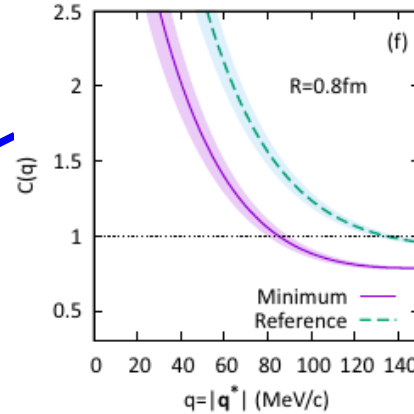
STAR+ALICE suggests a $N\Omega$ dibaryon state

Morita+, PRC101('20)015201
[1908.0414] (Gaussian source)

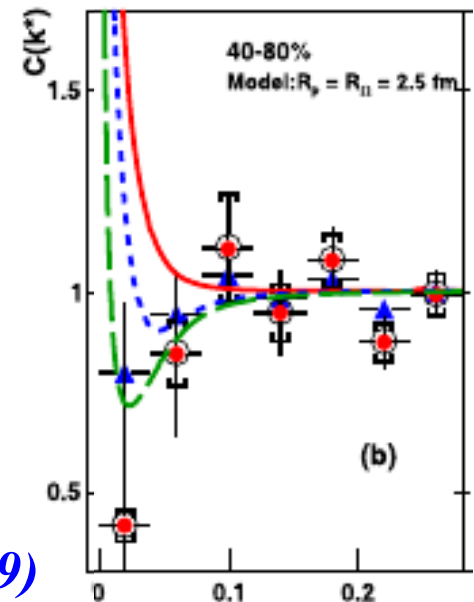
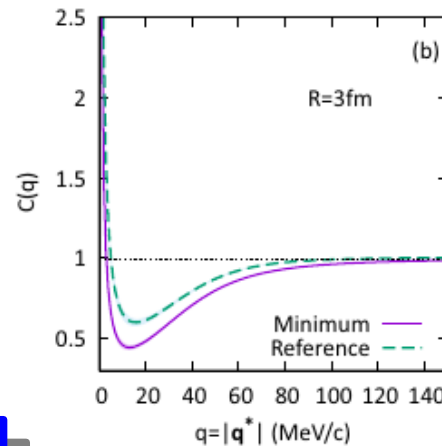


Reference: $V_{J=1} = V_{J=2}$
Minimum: $\phi_{J=1} = 0$

Dip from a bound state survives Coulomb.

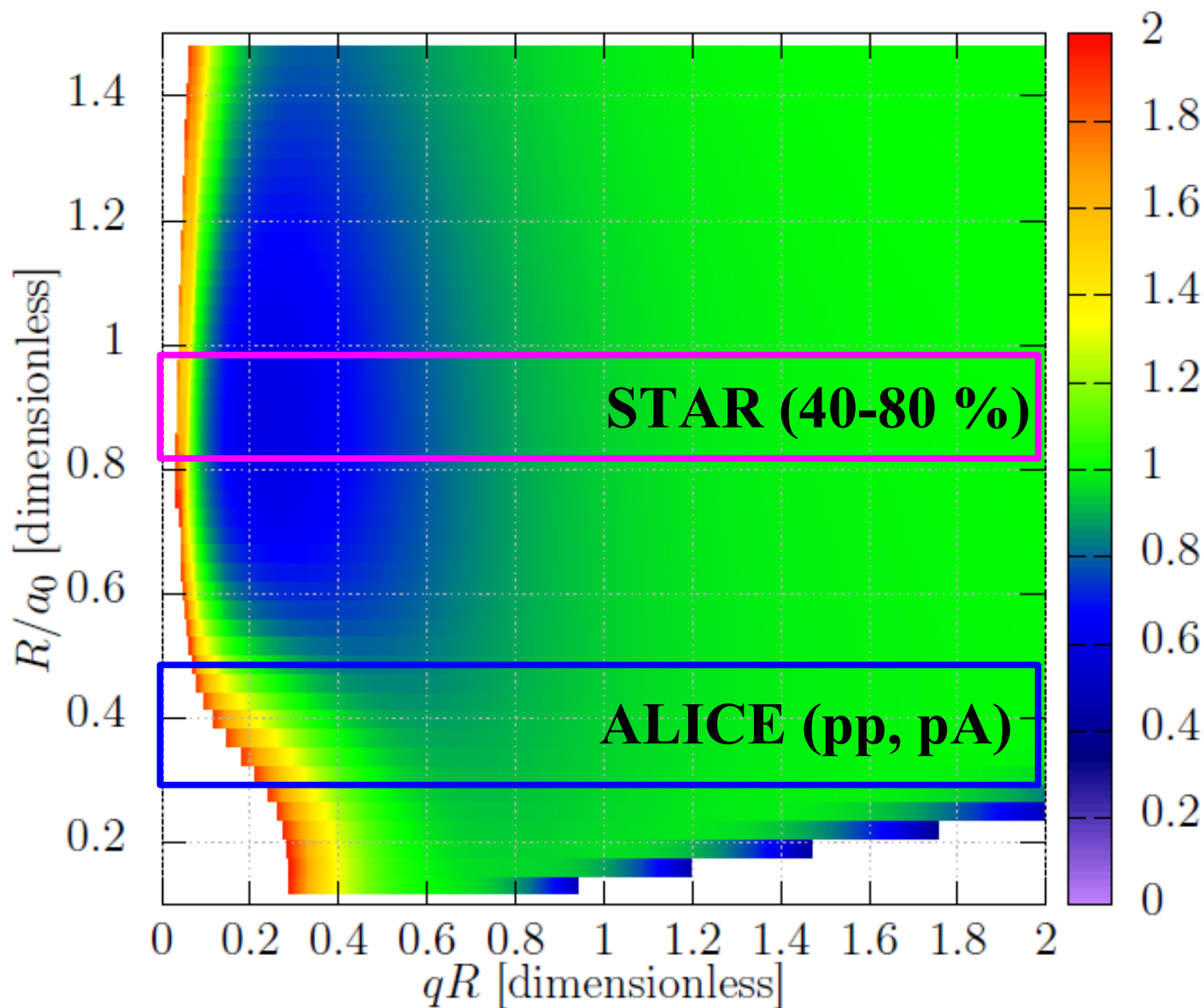


ALICE, Nature588('20)232 [2005.11495]



STAR, PLB790 ('19)
490 [1808.02511].

Ωp Correlation Function with Gaussian source



$N\Omega$ potential (J=2, HAL QCD, $a_0=3.4$ fm) + Coulomb

$K^- p$ correlation function

$\bar{K} N$ interaction and pK^- correlation function

■ $\Lambda(1405) = \bar{K} N$ quasi-bound state

Dalitz, Tuan ('60); Koch ('94); Kaiser, Siegel, Weise ('95); AO, Nara, Koch ('97)

● Positive scattering length in K^- atoms

M. Iwasaki et al. PRL 78 ('97) 3067;

M. Bazzi et al. [SIDDHARTA Collab.], PLB 704 ('11) 113.

■ Kaonic nuclei ?

Nogami ('63); Akaishi, Yamazaki ('02); Shevchenko, Gal, Mares ('07); Ikeda, Sato ('07); Dote, Hyodo, Weise ('09); S. Ajimura+ [J-PARC E15], PLB 789 (2019) 620.

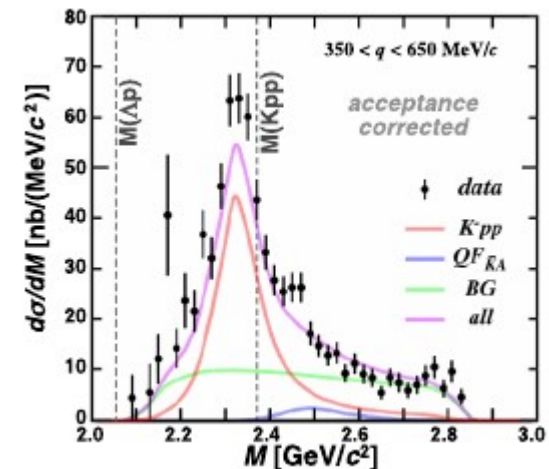
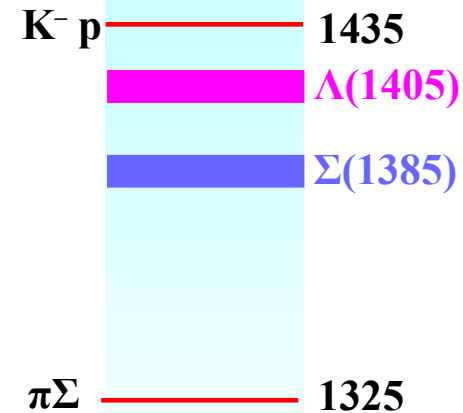
→ Needs precise info. on $\bar{K} N$ int.

■ Scattering amplitude and Potential fitting scattering and SIDDARTA data in chiral approach

Ikeda, Hyodo, Weise ('11, '12);

A. Cieplý, J. Smejkal ('12, NLO30);

Miyahara, Hyodo, Weise ('18, CC $N\bar{K}-\pi\Sigma-\pi\Lambda$ potential)



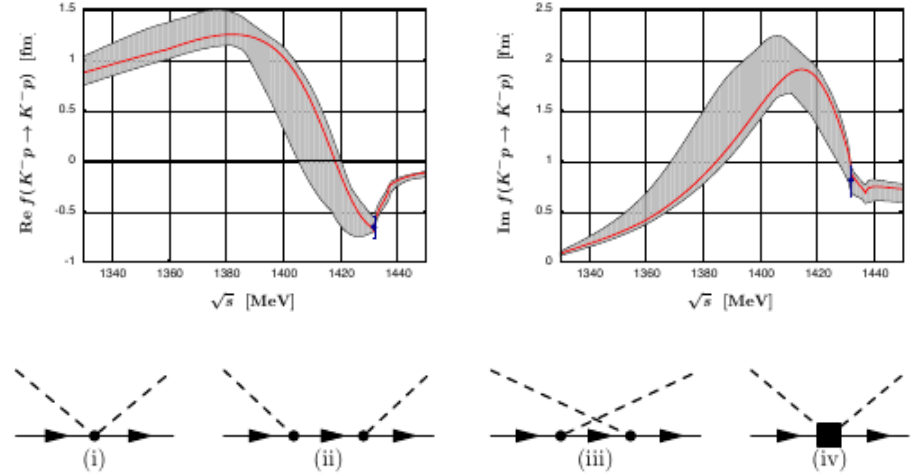
J-PARC E15 ('19)

Chiral $SU(3)$ $\bar{K}N$ interaction

■ Chiral $SU(3)$ $\bar{K}N$ scattering amplitude

Y. Ikeda, T. Hyodo, W. Weise, NPA881('12)98.

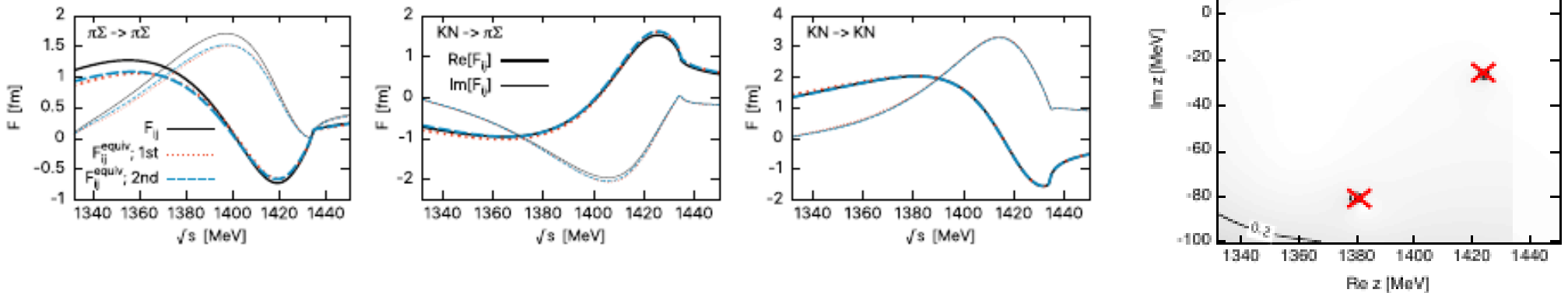
- Tomozawa-Weinberg + Born (w/ Exchange) + NLO
- Fit to SIDDHARTA data of $\bar{K}N$ diagonal scattering amplitude at threshold.
- $\bar{K}N$ - $\pi\Sigma$ - $\pi\Lambda$ - $\eta\Lambda$ - $\eta\Sigma$ - $K\Xi$



■ Coupled-channel $\bar{K}N$ - $\pi\Sigma$ - $\pi\Lambda$ potential based on IHW amplitude

K. Miyahara, T. Hyodo, W. Weise, PRC98('18)025201.

- Fit to IHW amplitude and pole positions of



Correlation Function with Coupled-Channel Effects

- To evaluate pK^- correlation function, we need to take account of coupled-channel effects of $NK-\pi\Sigma$!
- Correlation function formula with CC (KPLLL formula)

- Coupled-channel contributions with $\psi^{(-)}$ boundary cond.

R.Lednicky, V.V.Lyuboshits, V.L.Lyuboshits, Phys.Atom.Nucl.61('98)2950;

J. Haudenbauer, NPA981('19)1 [1808.05049].

$$C(\mathbf{q}) = \int d\mathbf{r} \sum_j \omega_j S_j(\mathbf{r}) |\Psi_j^{(-)}(\mathbf{r})|^2$$

$$= 1 - \int d\mathbf{r} S_1(r) |j_0(qr)|^2 + \int d\mathbf{r} \sum_j \omega_j S_j(r) |\psi_j^{(-)}(q; r)|^2$$

$$\psi_{j=1}(r) \rightarrow [e^{iqr} + A_1(q)e^{-iqr}]/2iqr \quad (\omega_1 = 1)$$

$$\psi_{j\neq 1}(r) \rightarrow A_j(q)e^{-iqr}/2iqr \quad [\Psi^{(-)} \text{ boundary condition}]$$

$$\omega_j S_j(\mathbf{r}) |\psi_j^{(-)}(q; r)|^2$$

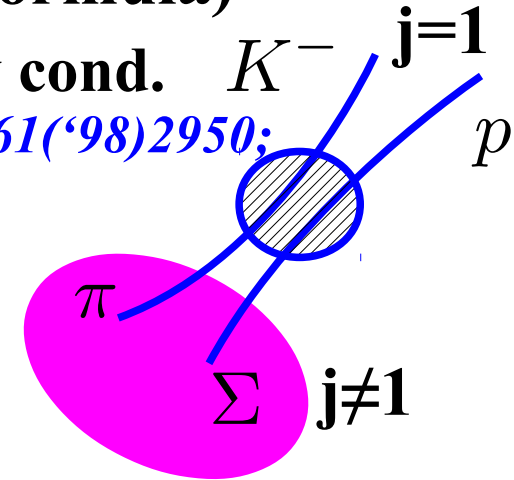
Source weight **Normalized Source fn.**

(No Coulomb case)

- Effects of coupled-channel, strong & Coulomb pot., and threshold difference are taken into account in the charge base.

Y. Kamiya+, PRL('20)

- **Source size R and weight ω_j ($j\neq 1$) are taken as the parameter.**

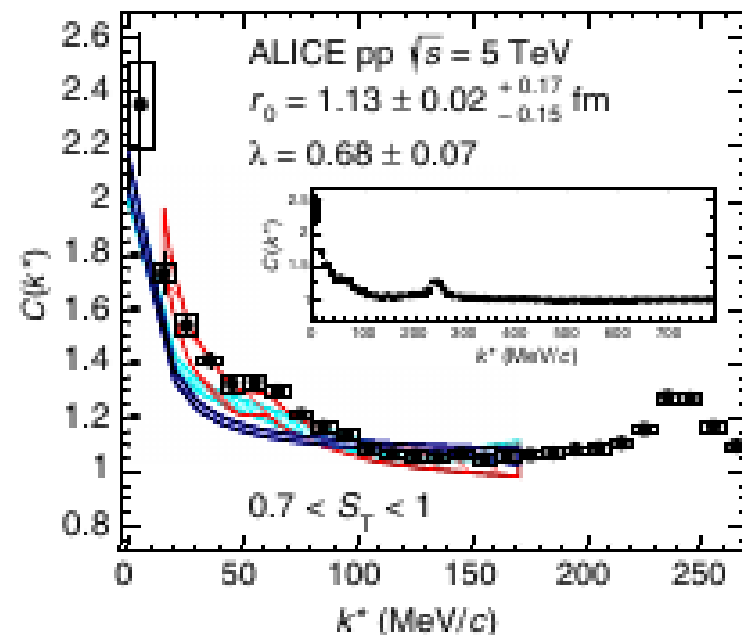


Comparison with ALICE data

■ 物理パラメータ = R and $\omega_{\pi\Sigma}$

- ALICE value (single channel) $R=1.13$ fm (K^+p 相関関数 (Jülich+Gamow) で決定)
- R はチャンネルに依存しないと仮定し、 $(R, \omega_{\pi\Sigma})$ 平面で実験をよく説明する領域を決定

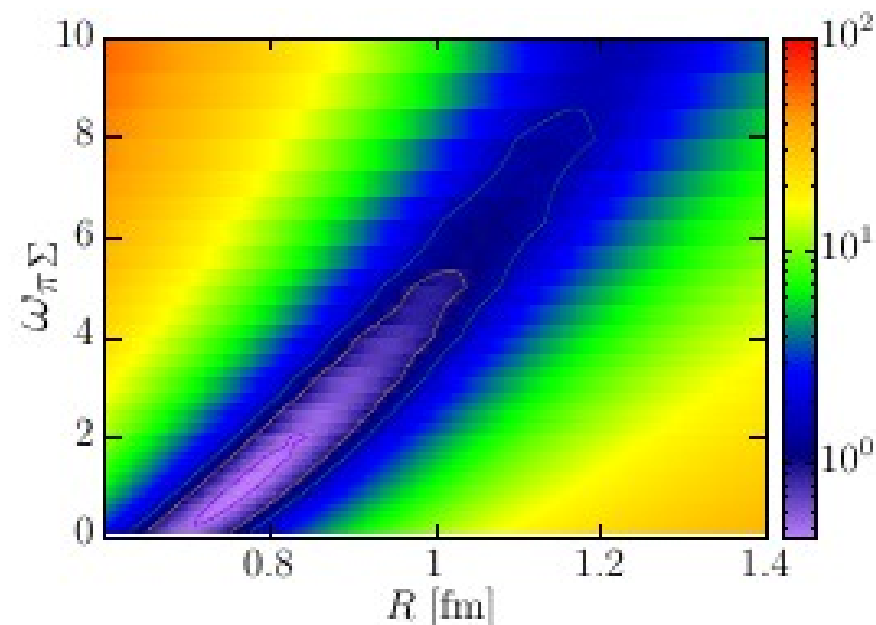
S. Acharya+[ALICE], PRL124('20)092301.



■ 観測パラメータ = N and λ

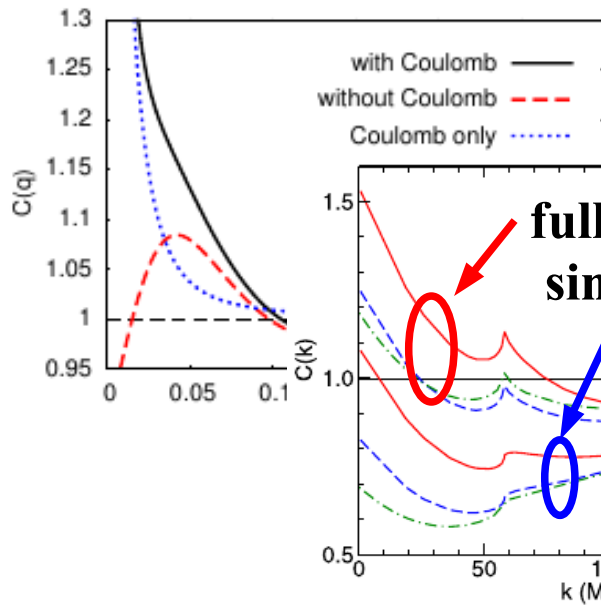
$$C_{\text{fit}}(q) = \mathcal{N} [1 + \lambda(C(q) - 1)]$$

- 規格化パラメータ (N) と pair purity (λ , 直接生成された pK^- の割合) は観測による
→ $(R, \omega_{\pi\Sigma})$ ごとに fit して決定



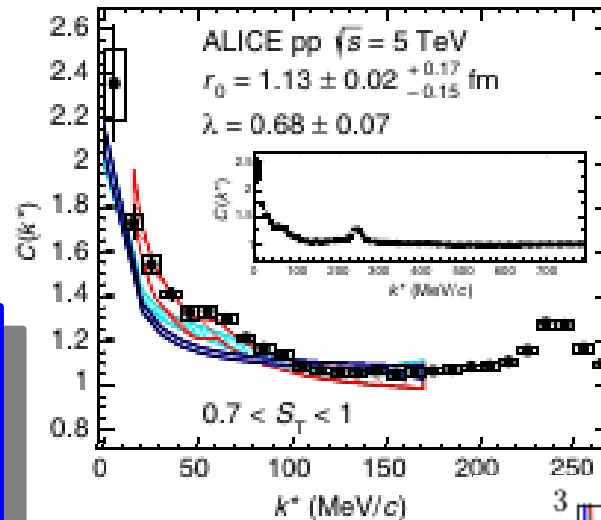
Y. Kamiya, T. Hyodo, K. Morita, AO, W. Weise, PRL124('20)132501.

pK - correlation



*S. Cho+ [ExHIC], PPNP95('17)279.
(Insufficient coupled-channel effects)*

*J. Haidenbauer, NPA981('19)1.
(Julich, NLO30, w/ CC effects,
w/o Coulomb)*

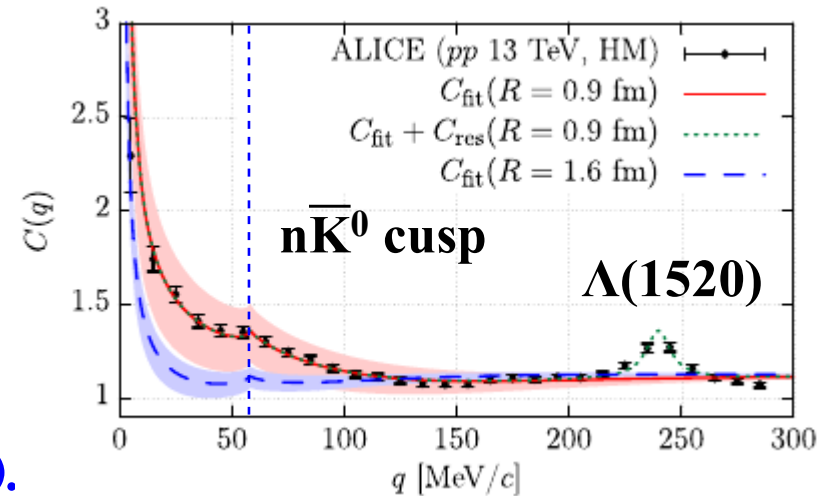


*S. Acharya+[ALICE],
PRL124('20)092301*

- ◆ $Kp \oplus K^*p$
- Coulomb
- Coulomb+Strong (Kyoto Model)
- Coulomb+Strong (Julich Model)

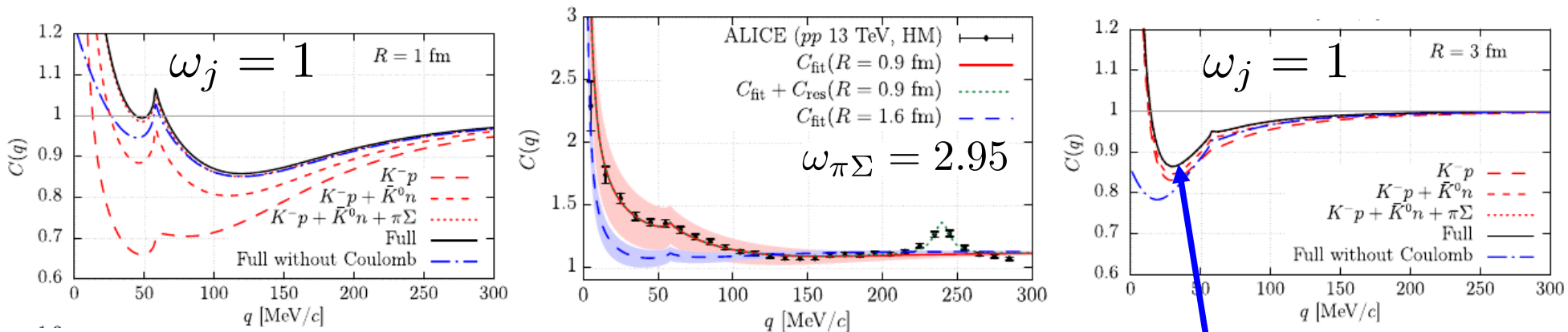
*CF with small
source is explained!
Source size dep. may
clarify bound state
nature of $\Lambda(1405)$.*

*Y. Kamiya, T. Hyodo, K. Morita, AO,
W. Weise, PRL124('20)132501
[1911.01041] (Chiral SU(3) dynamics).*

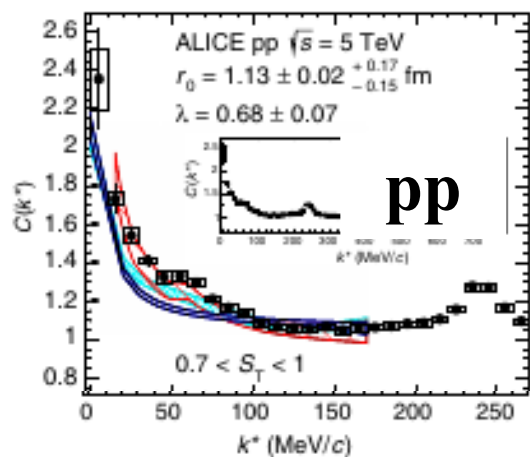


Source Size Dependence of $C(pK^-)$

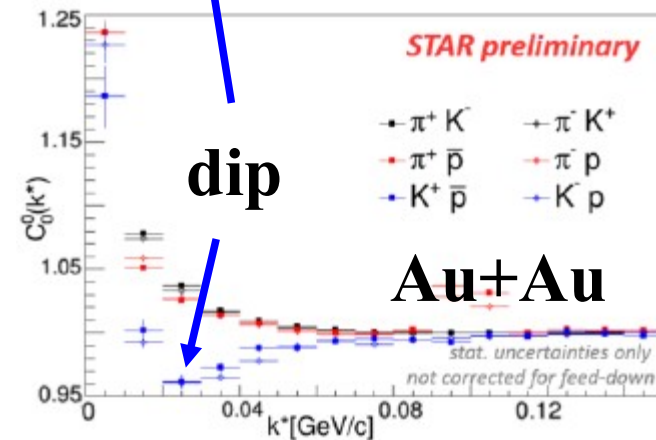
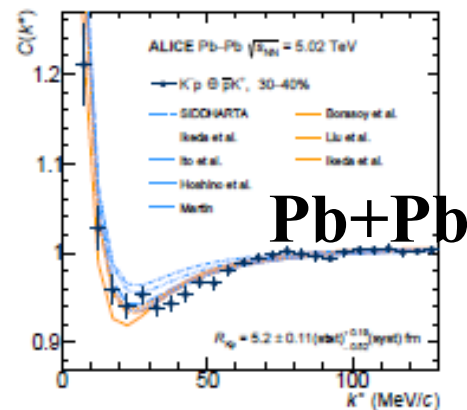
- Coupled-channel effects are suppressed when R is large, and “pure” pK^- wave function may be observed in HIC.



Y. Kamiya, T. Hyodo, K. Morita, AO, W. Weise, PRL124('20)132501.



pA



S. Acharya+[ALICE], PRL124('20)092301

S. Acharya+[ALICE], 2105.05683

Siejka+[STAR, preliminary], NPA982 ('19)359.

STAR(prel.) & new ALICE data show dip at small q .

Ξ^{-d} correlation function

Hadron-Deuteron correlation function

- Hadron-deuteron correlation (Λd , K^-d , Ξ^-d , Ω^-d , ...)

*S.Mrówczyński, Patrycja Słoń, Acta Phys.Polon.B51('20),1739 [1904.08320](K-d,pd);
J.Haidenbauer, PRC102('20)034001[2005.05012](Λd); F.Etminan+[2006.12771](Ωd).*

- Scattering length data of these are important to evaluate

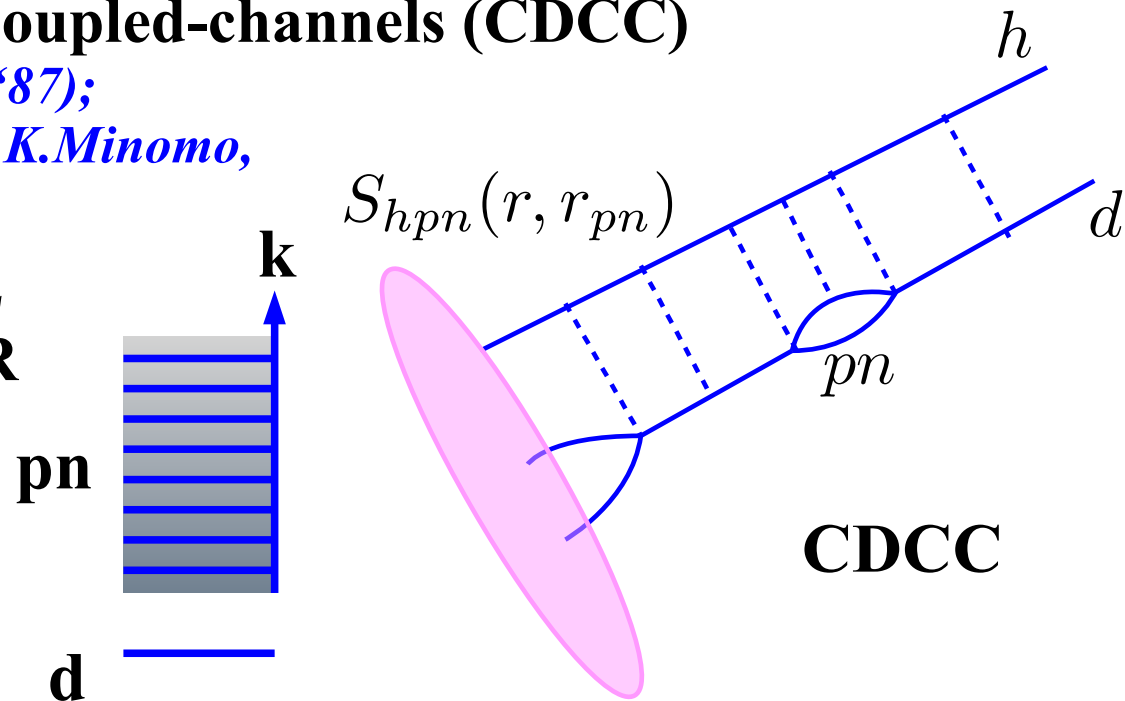
- ◆ binding energy and lifetime of hyper triton (Λd)
- ◆ $I=1$ $\bar{K}N$ interaction (K^-d , Ξ^-d)
- ◆ and the existence of a bound state.

- Problem: **Breakup and Dynamical Formation of d** ($d \leftrightarrow pn$)

→ Continuum-discretized coupled-channels (CDCC)

*M.Kamimura+('86); N. Austern+('87);
M.Yahiro, K.Ogata, T.Matsumoto, K.Minomo,
PTEP 2012 (2012) 01A206.*

- Measurable at LHC-ALICE and (probably) RHIC-STAR



$\Xi^- d$ $C(q)$ using CDCC

■ Three-body wave functions (s-wave)

$$\psi^{(-)}(r, \rho; q) = \sum_n \sum_k A_{kn} \varphi_k(\rho) \chi_{nk}(r; q_{nk})$$

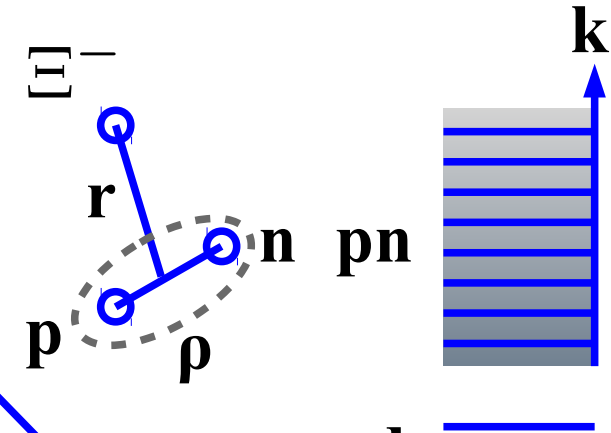
J, spin, isospin, ...

intrinsic
momentum
bin

kinematic
factor

normalized
pn w.f.
in k-th bin

Ξ^- -pn w.f.



■ $\Xi^- d$ Correlation function

$$C(q) = \underbrace{C_{\ell>0}^C(q)}_{\text{pure Coulomb}} + \frac{1}{2 \cdot 3} \int dr S(r) \sum_{nk} |\chi_{nk}(r; q_{nk})|^2$$

$\frac{1}{(2J_1+1)(2J_2+1)}$ “ $\Xi^- d$ ” source fn.

■ Potential = HAL QCD potential at almost physical quark masses

K. Sasaki et al. [HAL QCD Collab.], NPA 998 ('20) 121737 (1912.08630)

(coupling with $\Lambda\Lambda$ is ignored).

$\Xi^- d$ correlation function: Result

■ CDCC results of $\Xi^- d$ correlation function

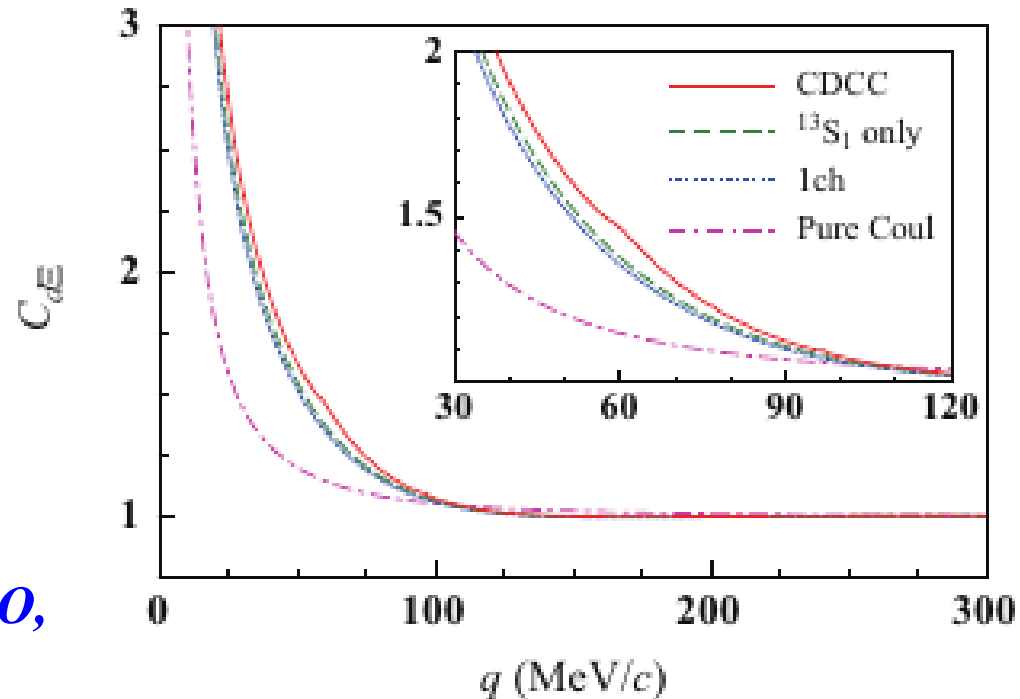
- Enhancement from pure Coulomb $C(q)$ by ΞN interaction from HAL QCD potential.
- Breakup & Reformation effects $\sim 10\%$ (Barely measurable)
- Dynamical formation of deuteron is (maximally) included.

Implicit assumption: $\int d\rho S(\rho) |\varphi_k(\rho)|^2 \simeq \text{const.}$

- Threshold cusp at $d \rightarrow pn$ threshold is seen, but not prominent.

Single channel description may not be bad.

→ Bound or Unbound in Ξd from Experimental data (if measured).

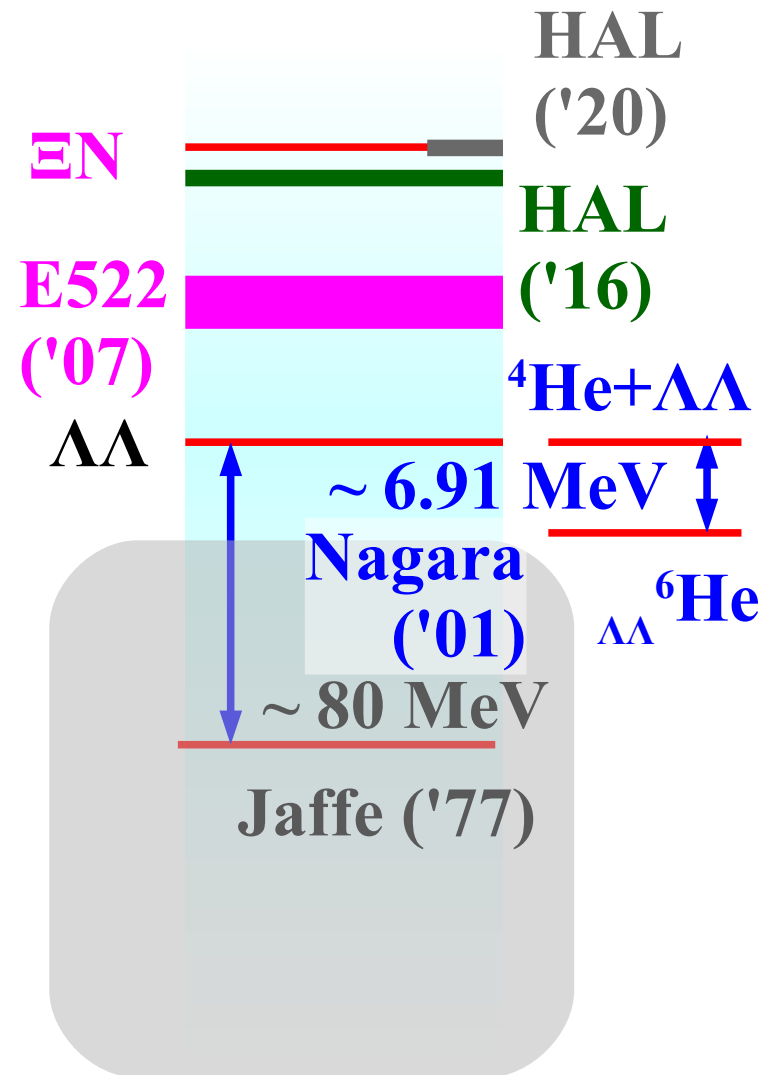


*K. Ogata, T. Fukui, Y. Kamiya, and AO,
PRC, to appear (arXiv:2103.00100).*

Ξ^- p and Λ correlation function

H dibaryon state, to be bound or not to be bound ?

- **H-dibaryon: 6-quark state (uuddss)**
 - Prediction: *R.L.Jaffe, PRL38(1977)195*
 - Ruled-out by double Λ hypernucleus
Takahashi et al., PRL87('01) 212502
 - Resonance or Bound “H” ?
Yoon et al.(KEK-E522)+AO ('07)
- **Lattice QCD results**
 - Bound (below $\Lambda\Lambda$ threshold):
HALQCD('11), NPLQCD('11,'13), Mainz('19)
(heavier quark mass or SU(3) limit)
 - Resonance (Bound state of $N\Xi$):
HAL QCD ('16,18) (HAL preliminary)
 - Virtual Pole (around $N\Xi$ threshold)
HAL QCD ('20) (almost physical m_q)



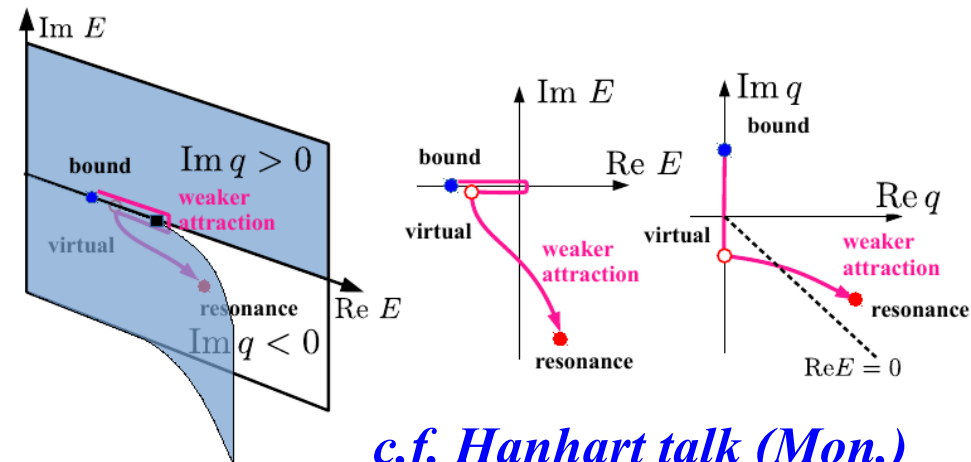
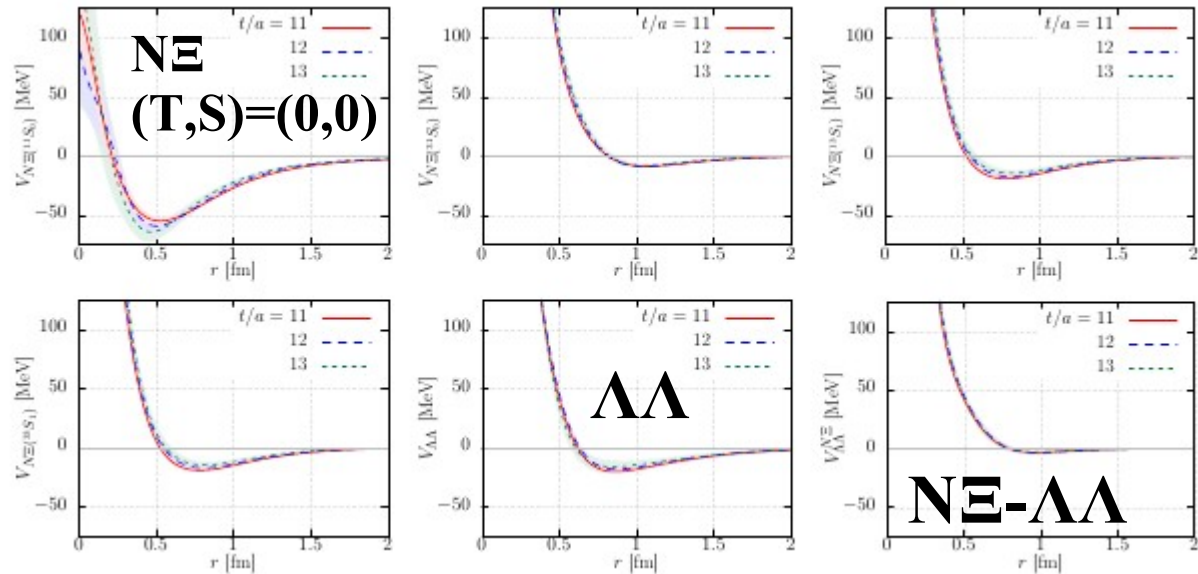
We examine LQCD $N\Xi$ - $\Lambda\Lambda$ potential and discuss H using CF !

$N\Xi-\Lambda$ potential from Lattice QCD

- $N\Xi-\Lambda\Lambda$ potential at almost physical quark mass ($m_\pi=146$ MeV) by HAL QCD Collaboration

K. Sasaki et al. [HAL QCD Collab.], NPA 998 ('20) 121737 (1912.08630)

- Strong attraction in $(T,S)=(0,0)$ of $N\Xi$
- Weak attraction in $\Lambda\Lambda$ (Coupling with $N\Xi$ causes $\Lambda\Lambda$ attraction)
- **There is no bound state in $N\Xi-\Lambda\Lambda$ system (except for Ξ^- atom), but there is a virtual pole around the $N\Xi$ threshold (3.93 MeV below $n\Xi^0$ threshold) on the irrelevant Riemann sheet, $(+, -, +)$ [relevant= $(-, +, +)$]**
 sign of $\text{Im}(\text{eigen momentum})$



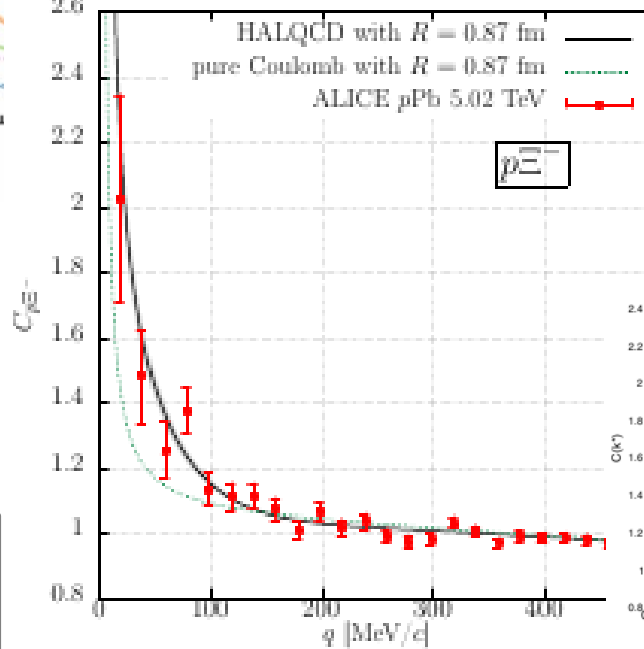
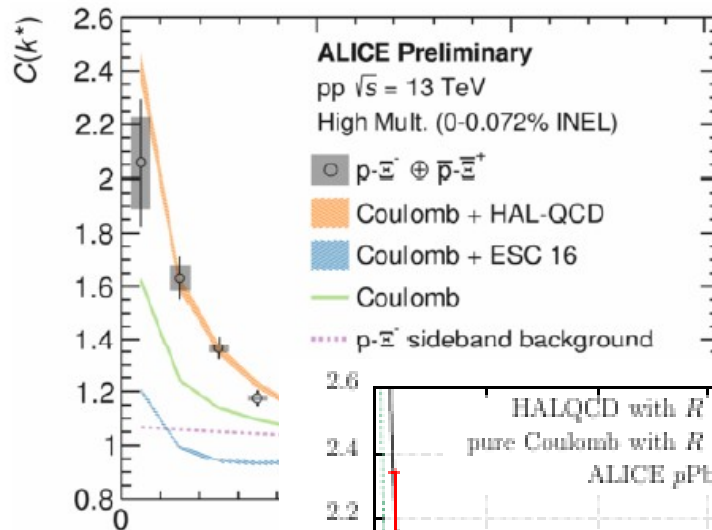
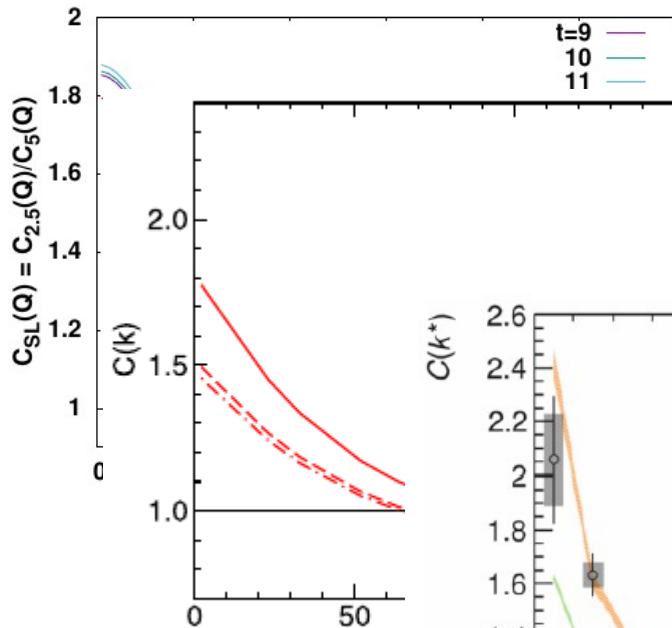
c.f. Hanhart talk (Mon.)

$p\Xi^-$ correlation function

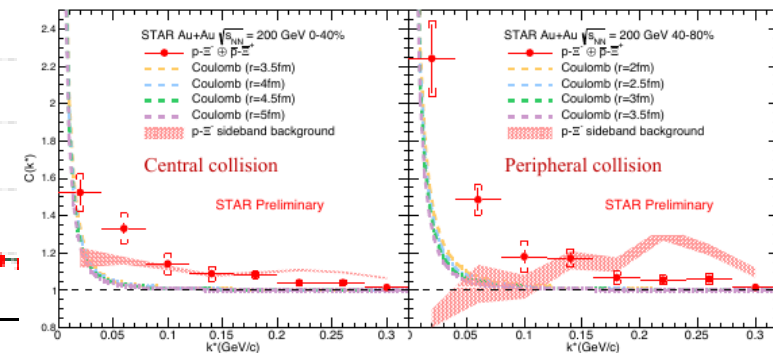
T. Hatsuda, K. Morita, AO, K. Sasaki, NPA967('17)856.
(heavier quark mass, $I=0$ only, w/o CC effects)

J. Haidenbauer, NPA981('19)1.
(NLO(600), w/ CC effects, w/o Coulomb)
(w/ Coulomb, it will be comparable with data.)

D. L. Mihairov+[ALICE], NPA 1005 ('21)121760 (QM2019). (Nijmegen pot. does not explain the data. w/o CC)
Acharya+(ALICE), Nature ('20)



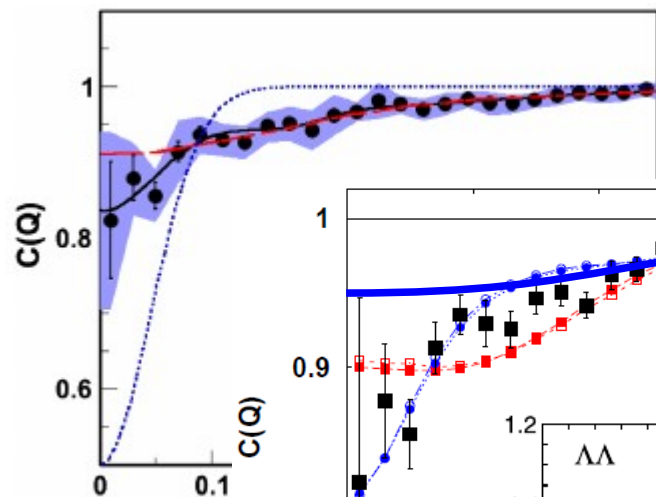
K. Mi+(STAR, preliminary), Au+Au 200 AGeV, APS2021.
(No Dip at larger R)



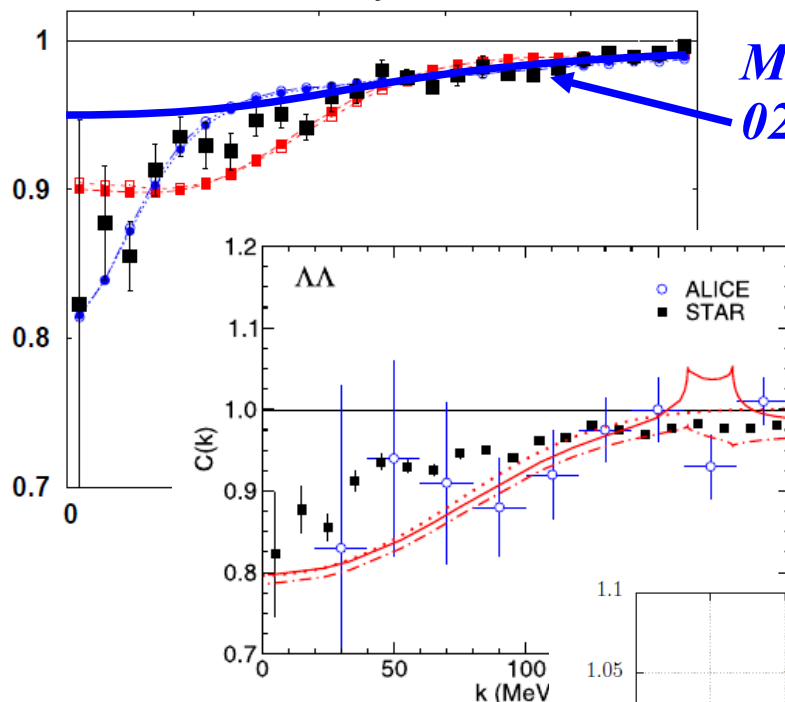
Kamiya, Sasaki, Fukui,⁵⁴⁷⁴
Hatsuda, Hyodo, Morita,
Ogata, AO (in prep.),
w/ Lattice BB pot. at phys. m_q
CC effects with $\Lambda\Lambda$.

There is no signal
of bound state.

Λ correlation function

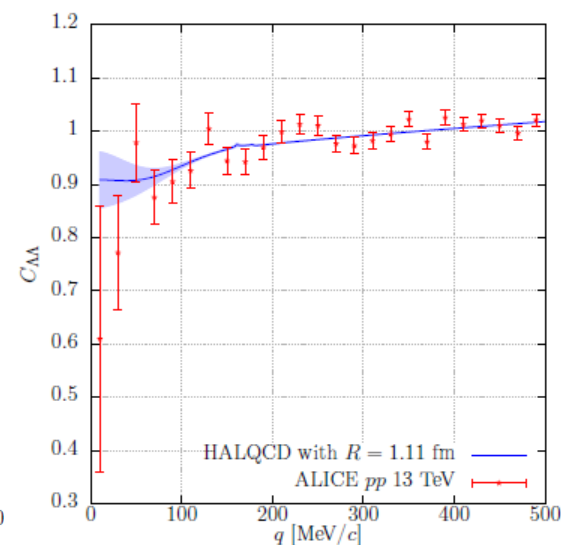
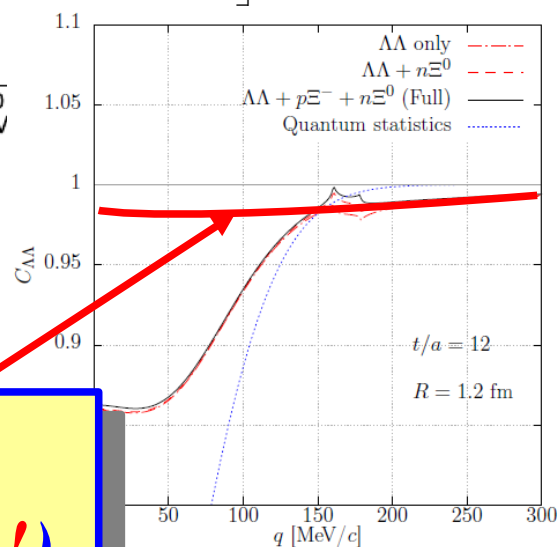


*Adamczyk+[STAR], PRL114('15)022301
(Residual source $R \sim 0.5$ fm was assumed.)*



*Morita, Furumoto, AO, PRC91('15)
024916. (Res.Source + flow)*

*J. Haidenbauer, NPA981('19)1.
(NLO600)*

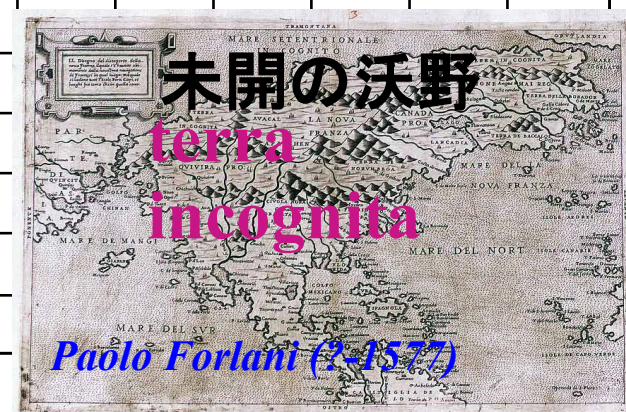


*Kamiya+(in prep.).
(CC simulates res. source !)*

Summary of 19H05151

- Correlation function is useful to access hadron-hadron interactions as well as to deduce the existence of a bound state.

	n	p	K ⁻	K ⁺	π ⁻	π ⁺	Λ	Σ	Ξ ⁻	Ω ⁻	D ⁻	D ⁺	K _s	d	pp	+α
n																
p		0	0	0	Δ	Δ	0	0	0	0	0	0		0	0	
K ⁻		0	0	0	0	0							0			
K ⁺		0	0	0	0	0							0			
π ⁻		Δ	0	0	0	0										
π ⁺		Δ	0	0	0	0										
Λ		0					0		0						0	
Σ		0						0								
Ξ ⁻		0														
Ω ⁻		0														
D ⁻		0														
D ⁺		0														
K _s			0	0												
d		0														
pp		0					0									
+α																





21H00121
チャーム・ハドロン & 3体相関

Correlation functions of Charmed Hadron and Nucleon

■ CF including charmed hadron

- Extremely important in recent hadron physics.

- $D^-(\bar{c}d)$ - $p(uud)$ correlation

- ◆ Probes $\Theta_c(\bar{c}ud-ud)$ state (replace \bar{s} in $\Theta(\bar{s}ud-ud)$ with \bar{c})

D. O. Riska, N. N. Scoccola, PLB299('93)338 (pred.);

A. Aktaset+ [H1], PLB588('04)17 (positive);

J. M. Linket+ [FOCUS], PLB622('05)229 (negative).

- ◆ Attraction from two pion exchange

S. Yasui, K. Sudoh, PRD80('09)034008.

- ◆ Easy to calculate the potential in LQCD.

Y. Ikeda et al. (private communication)

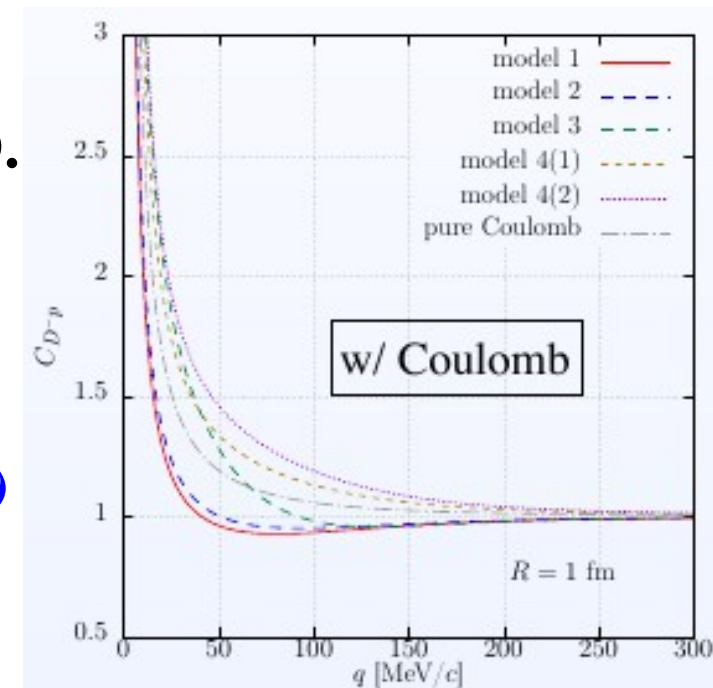
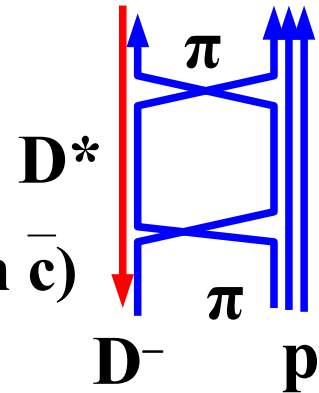
■ $D^-(\bar{c}d)$ - $p(uud)$ CFs from proposed potentials

Hofmann, Lutz ('05) (repulsive);

Haidenbauer+('07) (repulsive);

Yamaguchi+('11) (att., w/ bs); Fontoura+('13) (repulsive)

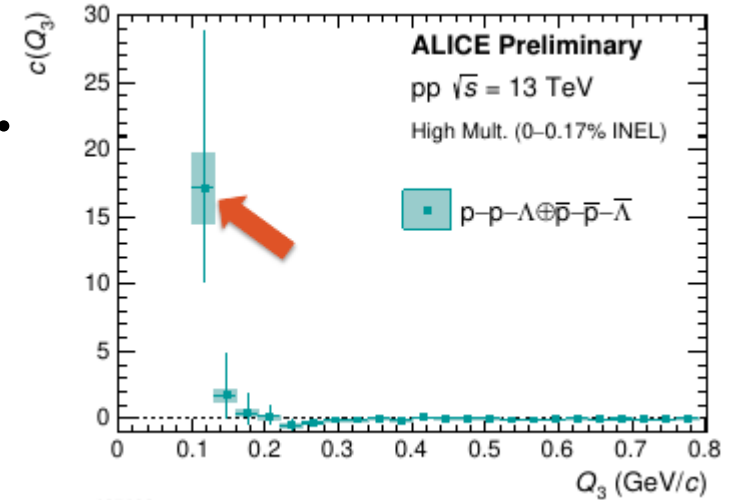
Data will discriminate these potentials !



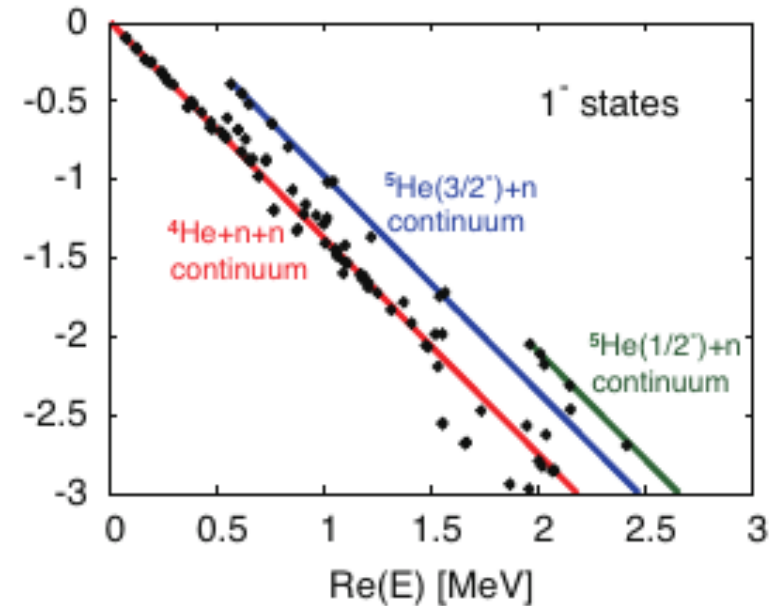
Kamiya, Hyodo, AO (in prog.)

Three-body correlation functions

- Three-body correlation functions are measured and discussed; ppp, Λ pp, pd, ...
- Continuum Three-body w.f. at various momenta with Coulomb.



V. Mantovani Sarti @SQM2021



- Riverside approximation (3π)
E.g. E. O. Alt, T. Csorgo, B. Lorstad,
J. Schmidt-Sorensen, PLB458 ('99)407.

$$\Psi_{123} = \psi(\mathbf{q}_{12})\psi(\mathbf{q}_{23})\psi(\mathbf{q}_{31})$$

→ Does not give free correct w.f.

- Complex Scaling ?
Y. Kikuchi, T. Myo, M. Takashina, K. Kato,
K. Ikeda, PTP122 ('09) 499;
T. Myo, AO, K. Kato, PTP99('98)801.

$$G^\theta(E; \xi, \xi') = \left\langle \xi \left| \frac{1}{E - \hat{H}^\theta} \right| \xi' \right\rangle = \sum_n \frac{\chi_n^\theta(\xi) \tilde{\chi}_n^\theta(\xi')}{E - E_n^\theta}$$

- Other idea ?

Summary

■ 相関関数を用いたハドロン間相互作用の研究を進めている。

● 19H05151 (2019-2020): ほぼ計画通り

- ◆ Ωp , $\Omega\Omega$ (K.Morita+('20)), $K^- p$ (Y.Kamiya+('20)), $\Xi^- d$ (K.Ogata+(to appear)), $\Xi^- p$, $\Lambda\Lambda$ (Y.Kamiya+(in prep.)).
- ◆ HAL QCD, Chiral SU(3) dynamics からの相互作用を用いた相関関数
- ◆ 結合チャネル効果を含む相関関数を求める手法を実装
- ◆ Continuum Discretized Coupled-Channels (CDCC) の利用

● 21H00121 (2021-2022):

- ◆ $p\Lambda$, $p\Sigma^0$, $\Lambda\Xi^- \rightarrow$ HAL QCD potential を用いて $C(q)$ を計算
- ◆ $D^- p$, $D^+ p \rightarrow$ 既存のポテンシャルを利用。 Pentaquark states ?
- ◆ 3 体相関関数 \rightarrow アイデア募集中。

Thank you for your attention !

Coauthors of *arXiv:1908.05414* ($p\Omega$, $\Omega\Omega$) and *arXiv:1911.01041* (pK^-),
arXiv:2103.00100 (dE^-),
and next paper on pE^- - $\Lambda\Lambda$ (Y. Kamiya, K. Sasaki, T. Fukui, T. Hatsuda,
T. Hyodo, K. Morita, K. Ogata, AO, in prep.)

K. Morita



S. Gongyo



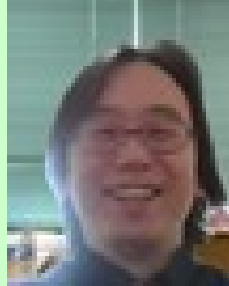
T. Hatsuda



T. Hyodo



K. Ogata



T. Fukui



(J. Haidenbauer)



K.Sasaki

Y. Kamiya

ALICE



W. Weise

