

$\bar{K}N$ interaction and Kaonic nuclei



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$\bar{K}N$ interaction

- **Systematic analysis in chiral SU(3) dynamics**

[Y. Ikeda, T. Hyodo, W. Weise, PLB 706, 63 \(2011\); NPA 881 98 \(2012\)](#)

- **Realistic $\bar{K}N$ potential**

[T. Hyodo, W. Weise, PRC77, 035204 \(2008\)](#)

[K. Miyahara, T. Hyodo, PRC93, 015201 \(2016\)](#)



(Selected topics of) Kaonic nuclei

- **Few-body systems up to $A=6$**

[S. Ohnishi, W. Horiuchi, T. Hoshino, K. Miyahara, T. Hyodo, arXiv:1701.07589 \[nucl-th\], PRC in press.](#)

\bar{K} meson and $\bar{K}N$ interaction

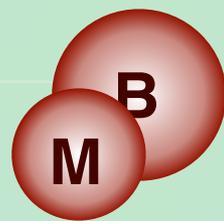
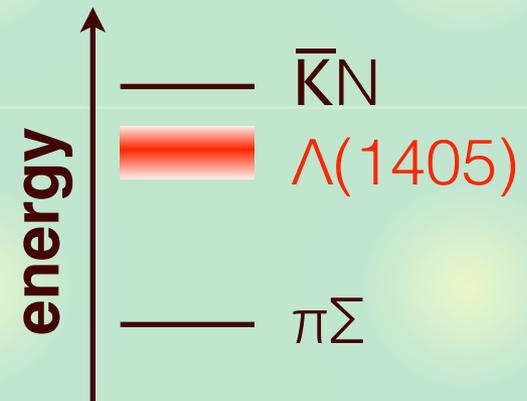
Two aspects of $K(\bar{K})$ meson

- **NG boson** of chiral $SU(3)_R \otimes SU(3)_L \rightarrow SU(3)_V$
- **Massive** by strange quark: $m_K \sim 496$ MeV
- > **Spontaneous/explicit** symmetry breaking

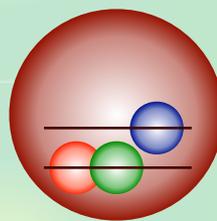
$\bar{K}N$ interaction ...

T. Hyodo, D. Jido, Prog. Part. Nucl. Phys. 67, 55 (2012)

- is coupled with $\pi\Sigma$ channel
- generates $\Lambda(1405)$ below threshold



molecule



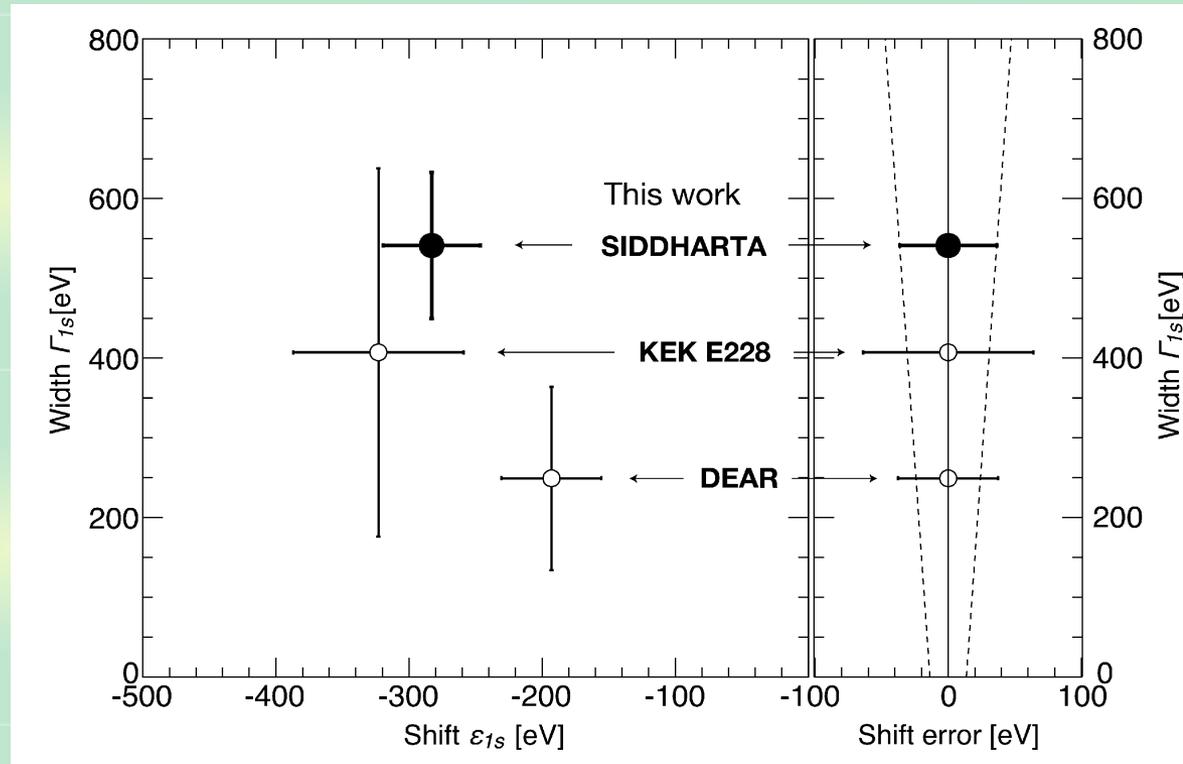
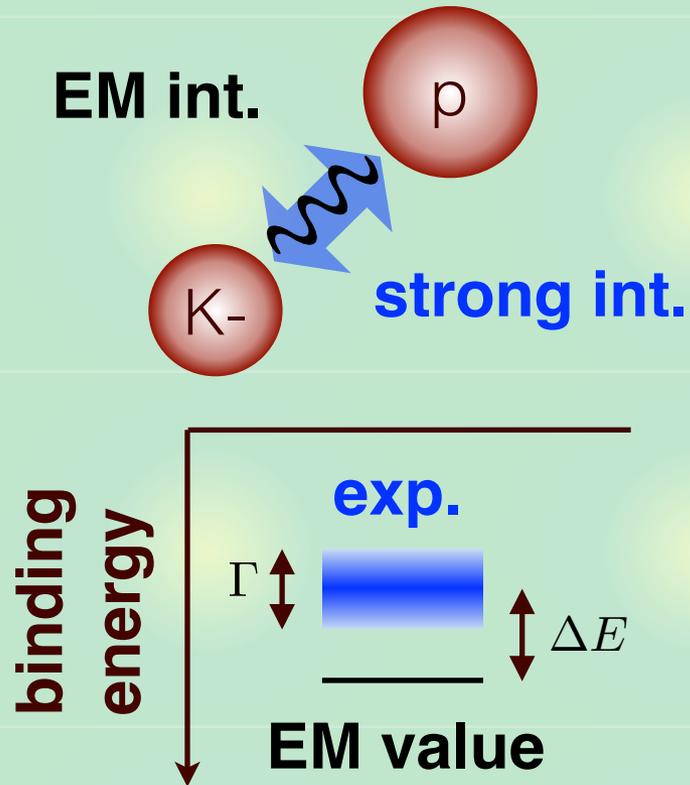
three-quark

- is fundamental building block for \bar{K} -nuclei, \bar{K} in medium, ...₃

SIDDHARTA measurement

Precise measurement of the kaonic hydrogen X-rays

M. Bazzi, *et al.*, Phys. Lett. B704, 113 (2011); Nucl. Phys. A881, 88 (2012)



- Shift and width of atomic state \leftrightarrow K-p scattering length

U.-G. Meissner, U. Raha, A. Rusetsky, Eur. Phys. J. C35, 349 (2004)

Quantitative constraint on the $\bar{K}N$ interaction at fixed energy

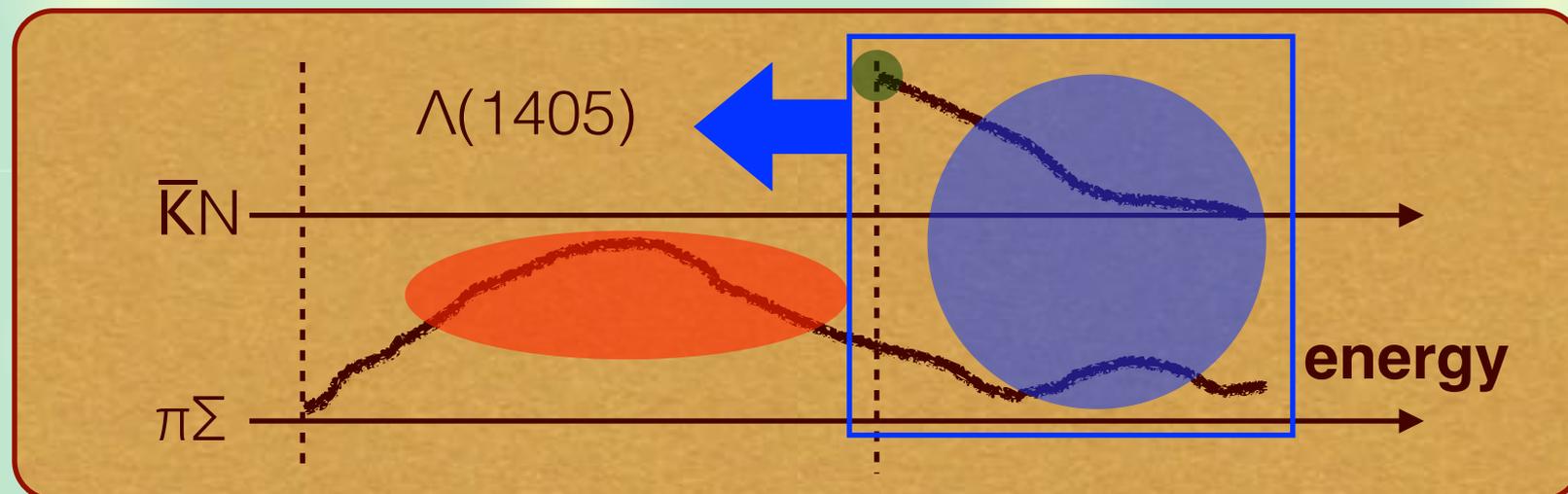
Strategy for $\bar{K}N$ interaction

Above the $\bar{K}N$ threshold: direct constraints

- K - p **total cross sections** (old data)
- $\bar{K}N$ **threshold branching ratios** (old data)
- K - p **scattering length** (new data: SIDDHARTA)

Below the $\bar{K}N$ threshold: indirect constraints

- $\pi\Sigma$ **mass spectra** (new data: LEPS, CLAS, HADES,...)



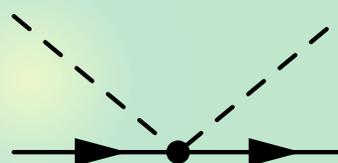
Construction of the realistic amplitude

Chiral coupled-channel approach with systematic χ^2 fitting

Y. Ikeda, T. Hyodo, W. Weise, Phys. Lett. B706, 63 (2011); Nucl. Phys. A881 98 (2012)



1) TW term

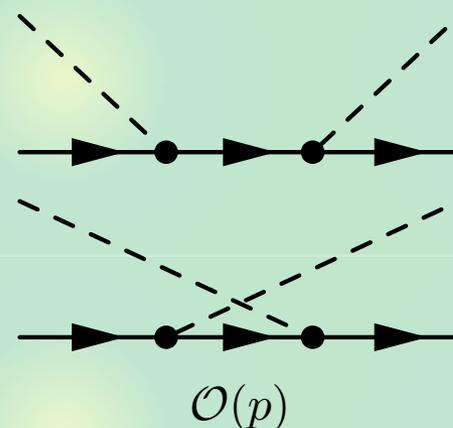


$\mathcal{O}(p)$

6 cutoffs

TW model

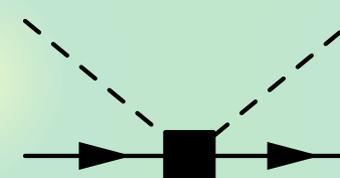
2) Born terms



$\mathcal{O}(p)$

TWB model

3) NLO terms



$\mathcal{O}(p^2)$

7 LECs

NLO model

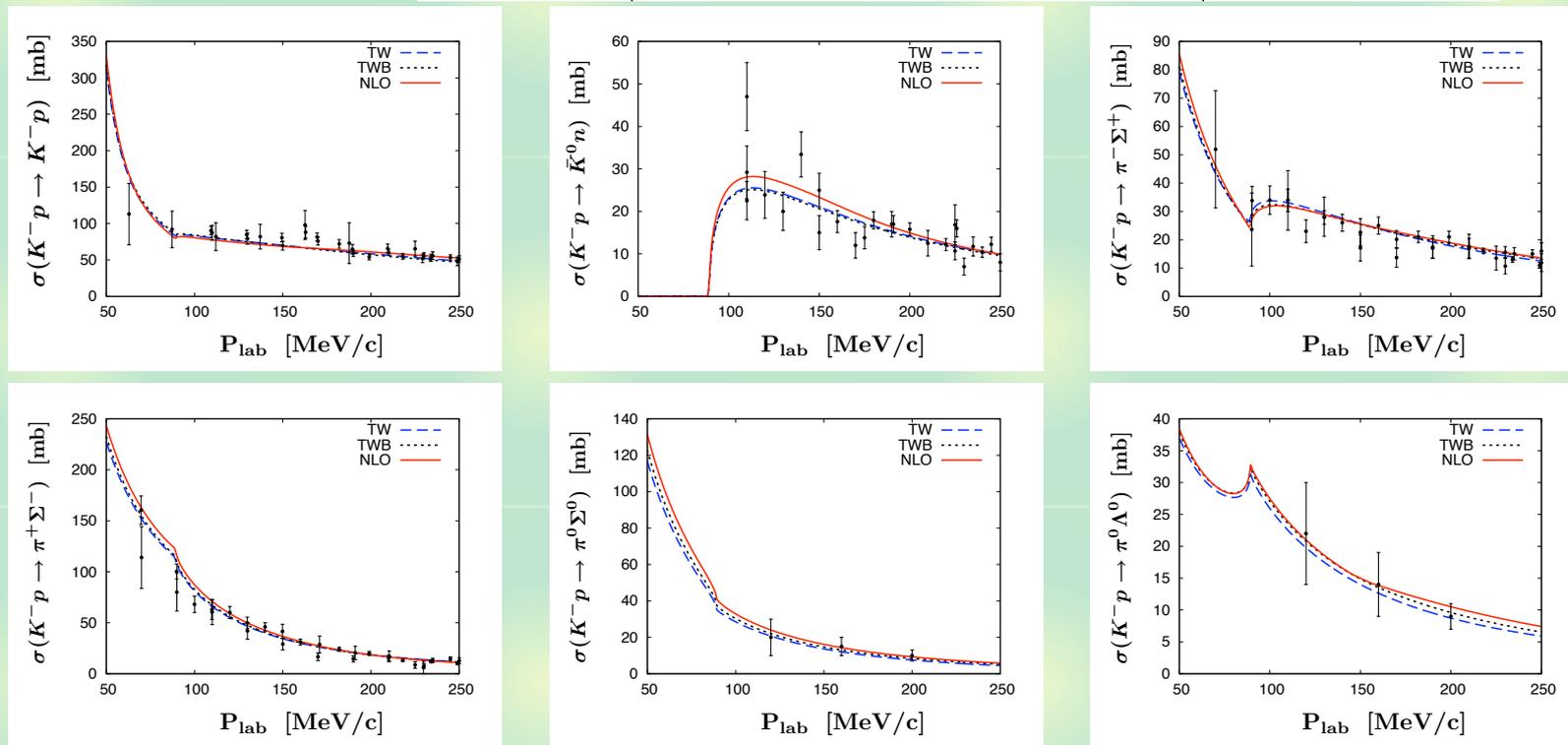
Best-fit results

SIDDHARTA

Branching ratios

	TW	TWB	NLO	Experiment
ΔE [eV]	373	377	306	$283 \pm 36 \pm 6$ [10]
Γ [eV]	495	514	591	$541 \pm 89 \pm 22$ [10]
γ	2.36	2.36	2.37	2.36 ± 0.04 [11]
R_n	0.20	0.19	0.19	0.189 ± 0.015 [11]
R_c	0.66	0.66	0.66	0.664 ± 0.011 [11]
$\chi^2/\text{d.o.f}$	1.12	1.15	0.96	

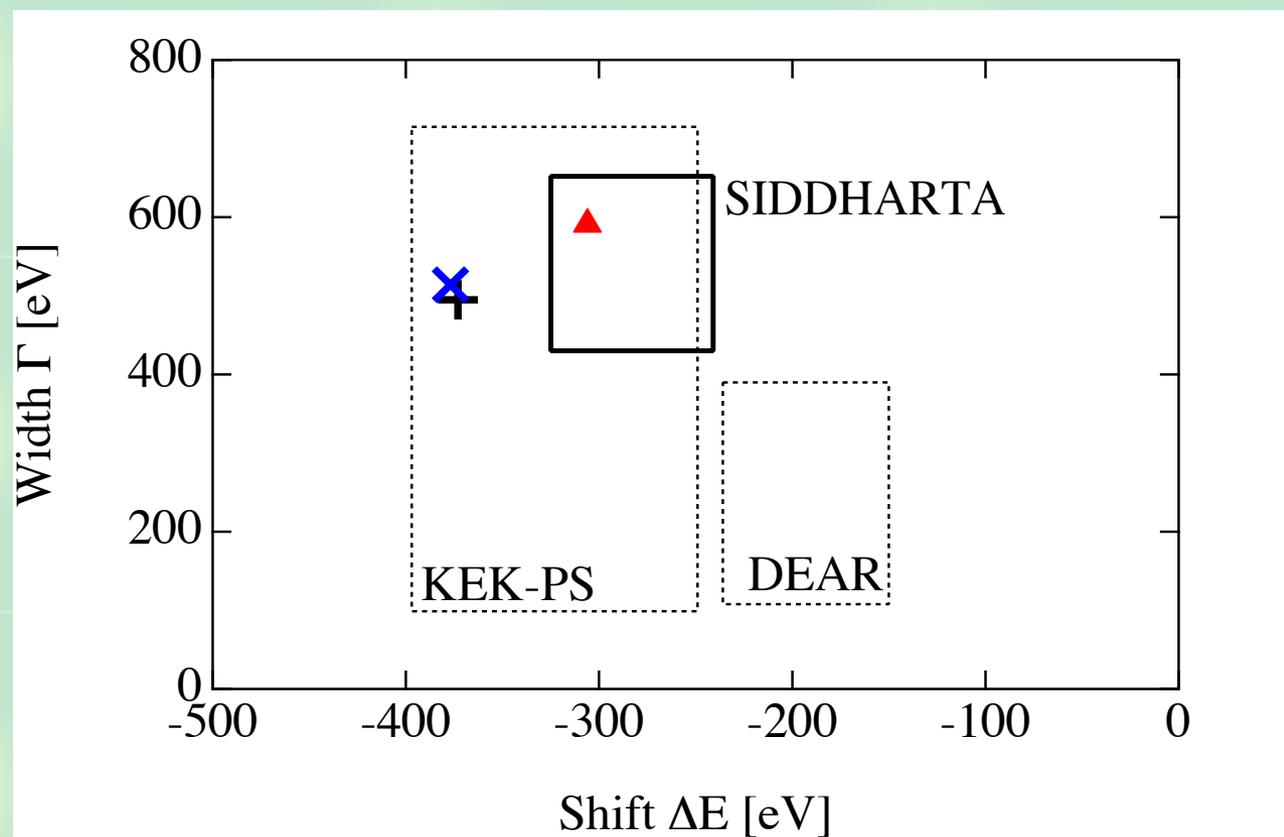
cross sections



K-hydrogen and cross sections are consistent (c.f. DEAR).

Comparison with SIDDHARTA

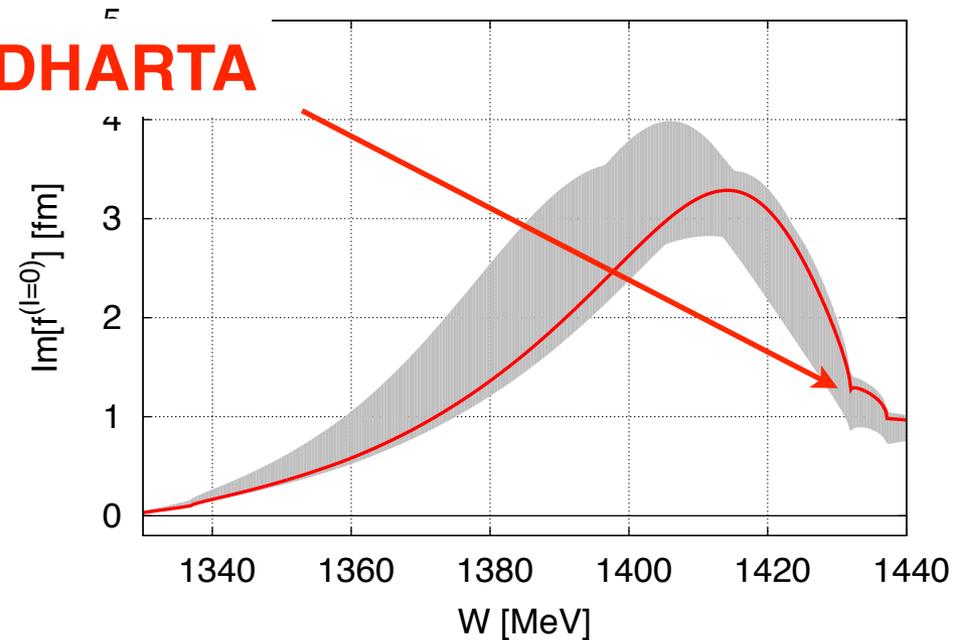
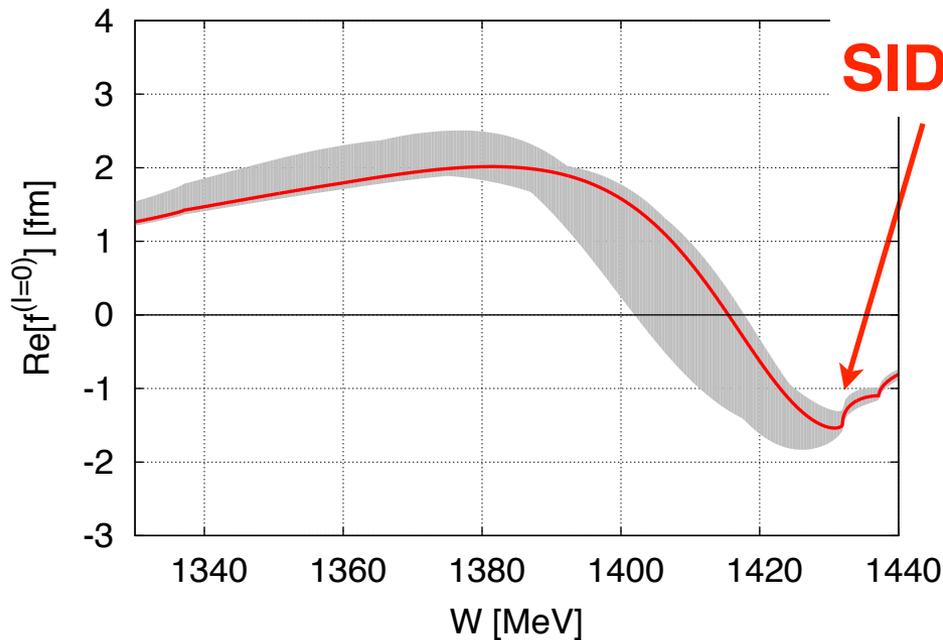
	TW	TWB	NLO
$\chi^2/\text{d.o.f.}$	1.12	1.15	0.957



TW and **TWB** are reasonable, while best-fit requires **NLO**.

Subthreshold extrapolation

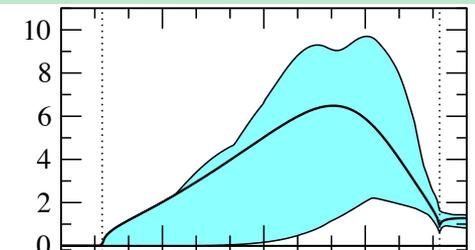
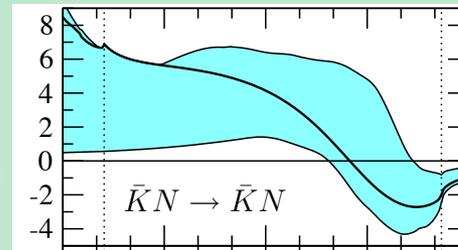
Uncertainty of $\bar{K}N \rightarrow \bar{K}N$ ($l=0$) amplitude below threshold



Y. Kamiya, K. Miyahara, S. Ohnishi, Y. Ikeda, T. Hyodo, E. Oset, W. Weise, Nucl. Phys. A954, 41 (2016)

- c.f. without SIDDHARTA

R. Nissler, Doctoral Thesis (2007)



SIDDHARTA is essential for **subthreshold** extrapolation.

Construction of $\bar{K}N$ potential

Local $\bar{K}N$ potential is useful for

- extraction of the wave function of $\Lambda(1405)$
- application to few-body Kaonic nuclei

Single-channel energy-dependent $\bar{K}N$ potential

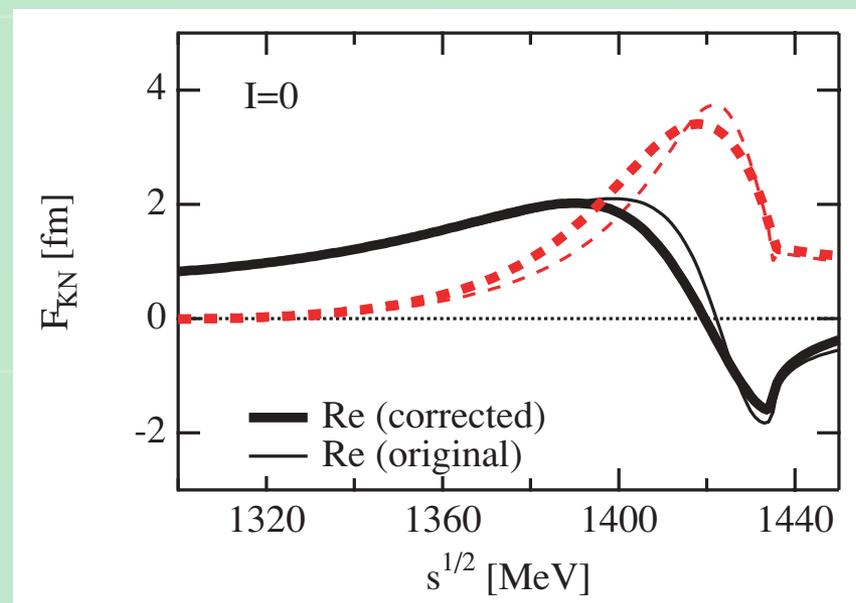
T. Hyodo, W. Weise, Phys. Rev. C 77, 035204 (2008)

- Chiral dynamics (thin)

$$T(W) = V(W) + V(W)G(W)T(W)$$

- Potential (thick)

$$U(W, r) + \text{Schrödinger eq.}$$



- Reasonable on-shell scattering amplitude on real axis

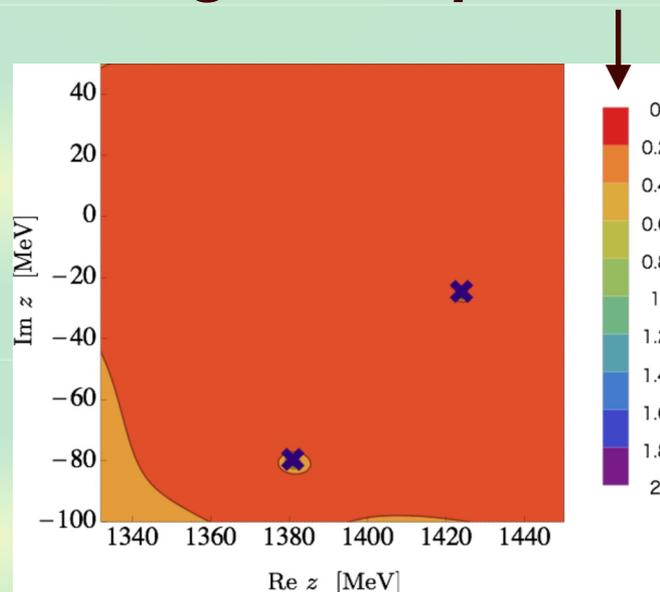
Realistic $\bar{K}N$ potential

Issues to be improved:

- Amplitude was not constrained by **SIDDHARTA**
- **Pole structure** of the amplitude was **not** reproduced.

Model	original	Pole position (MeV)	
		$F_{\bar{K}N}^{\text{Ch}}$	$F_{\bar{K}N}$ potential
ORB [68]		1427 - 17i, 1389 - 64i	1419 - 42i
HNJH [66,67]		1428 - 17i, 1400 - 76i	1421 - 35i
BNW [57,59]		1434 - 18i, 1388 - 49i	1404 - 46i
BMN [58]		1421 - 20i, 1440 - 76i	1416 - 27i

deviation from original amplitude



Construction of realistic potential

K. Miyahara, T. Hyodo, Phys. Rev. C93, 015201 (2016)

- Chiral SU(3) at NLO with SIDDHARTA
- Equivalent amplitude in the complex energy plane

Kyoto $\bar{K}N$ potential reproduces data $\chi^2/\text{dof} \sim 1$: realistic

Kaonic nuclei

Few-body \bar{K} nuclear systems

S. Ohnishi, W. Horiuchi, T. Hoshino, K. Miyahara, T. Hyodo,
arXiv:1701.07589 [nucl-th], PRC in press.

- Stochastic variational method with correlated gaussians
- $\bar{K}N$: Kyoto $\bar{K}N$ potential, NN: AV4' (hard core)

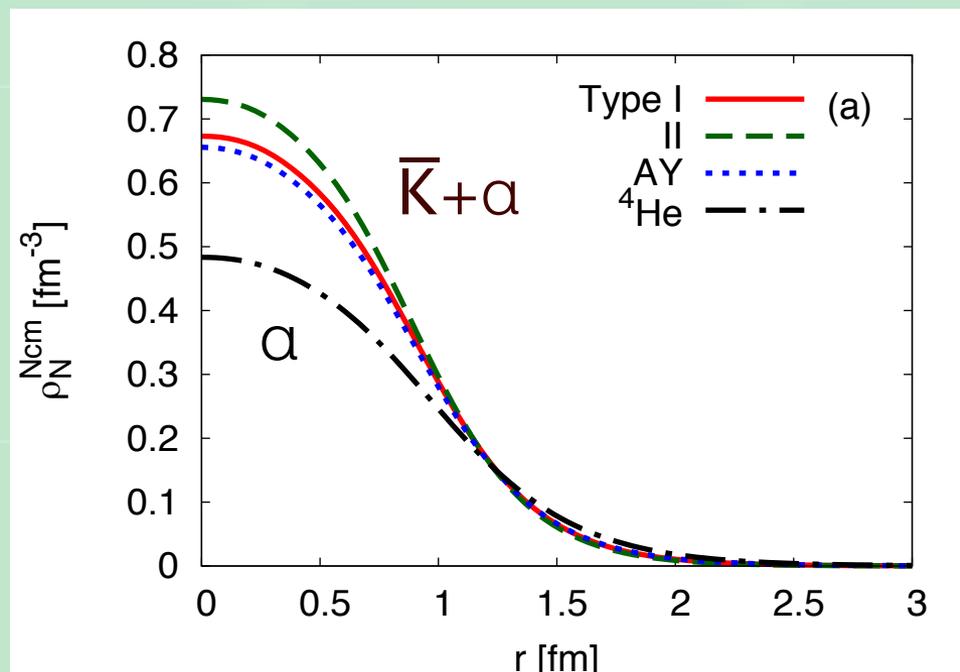
Few-body \bar{K} nuclear systems

	$\bar{K}NN$	$\bar{K}NNN$	$\bar{K}NNNN$	$\bar{K}NNNNN$
B [MeV]	25-28	45-50	68-76	70-81
Γ [MeV]	31-59	26-70	28-74	24-76

- **bound** below the lowest threshold
- **decay** width (without multi-N absorption) \sim binding energy

High density?

Nucleon density distribution in four-nucleon system



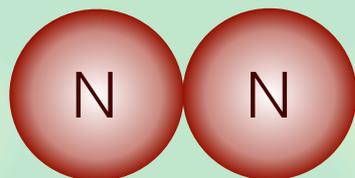
- central density increases (not substantially \leftarrow NN core)
- $B = 68\text{-}76$ MeV (Kyoto $\bar{K}N$)
- $B = 85\text{-}87$ MeV (AY)

Central density is **not always** proportional to $B \leftarrow$ tail of w.f.₁₃

Interplay between NN and $\bar{K}N$ correlations 1

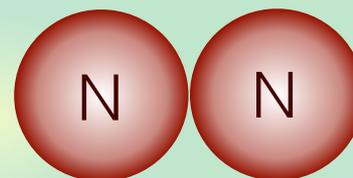
Two-nucleon system

1S_0 ($I_{NN}=1$)

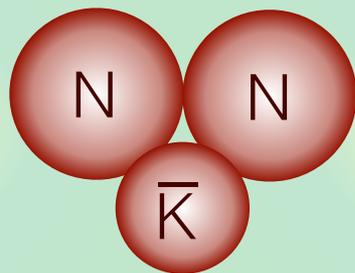


unbound

3S_1 ($I_{NN}=0$)

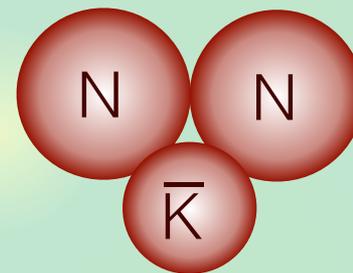


bound (d)



bound

$\bar{K}N(I=0):\bar{K}N(I=1) = 3:1$



unbound

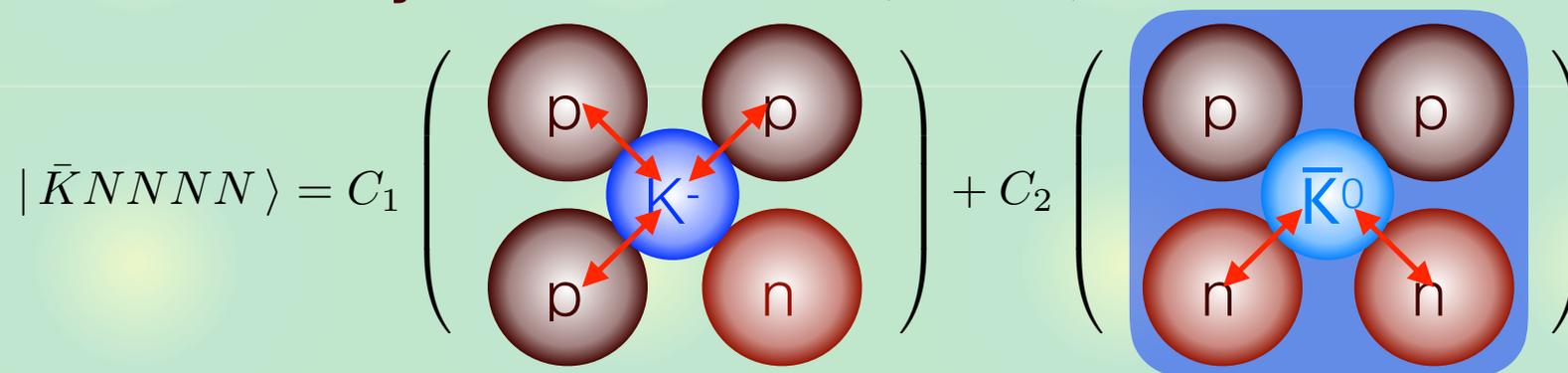
$\bar{K}N(I=0):\bar{K}N(I=1) = 1:3$

$\Lambda(1405)$

NN correlation $<$ $\bar{K}N$ correlation (also in $A=6$)

Interplay between NN and $\bar{K}N$ correlations 2

Four-nucleon system with $J^\pi=0^-, I=1/2, I_3=+1/2$



- $\bar{K}N$ correlation

$I=0$ pair in K^-p (3 pairs) or \bar{K}^0n (2 pairs) : $C_1 > C_2$

- NN correlation

$ppnn$ forms α : $C_1 < C_2$

- Numerical result

$$|C_1|^2 = 0.08, \quad |C_2|^2 = 0.92$$

NN correlation $>$ $\bar{K}N$ correlation

Summary: $\Lambda(1405)$

- $\bar{K}N$ scattering is quantitatively described ($\chi^2/\text{d.o.f.} \sim 1$) by **NLO chiral coupled-channel approach** with accurate K - p scattering length.
- Realistic $\bar{K}N$ potential** is now available.
- Few-body kaonic nuclei exist as quasi-bound states. Structure is determined by the **interplay between NN and $\bar{K}N$ correlations**.

