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京都大学基礎物理学研究所 湯川記念館史料室

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N91⁹¹

NOTE BOOK

Manufactured with best ruled foolscap

Brings easier & cleaner writing

石川行光 June, 1965 ~

~ Dec. 1965

VOL. XX

Nissho Note

c033-756~770 挟込

c033-755

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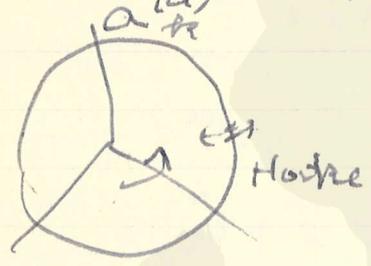
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11月 湯川 博士

6月 11日 12月
 湯川 博士 1965

11月	湯川 博士 微小粒子物理 model	湯川 博士 微小粒子物理	湯川 博士 2.30 23.00 micro -space-time
12月	湯川 博士 Embedding の理論 10.30 → 12.00	湯川 博士 De-sitter Model 湯川 博士 理論の inhomog. と CP-violation	

11月 湯川 博士
 湯川 博士: 微小粒子物理 model



strain tensor S_{ab}

$$V = \frac{\lambda}{2} (T_n S)^2 + \frac{\mu}{2} T_n (S^2)$$

$$T = \frac{\kappa_0}{2} \left(\frac{dX_n}{dt} \right)^2$$

X_n : lab. coord.
 x^a : body frame coord.
 $X_n = X_n(x^a)$
 $\kappa_n = a_n^{(a)} x^{(a)}$ du
 ↓
 平直空間

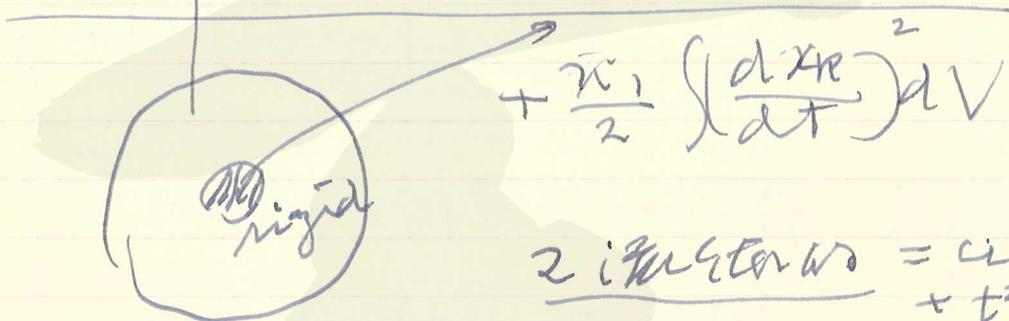
$$x^a \rightarrow x^a + u^a(x)$$

$$S_{ab} = \frac{1}{2} \left(\frac{\partial u^b}{\partial x^a} + \frac{\partial u^a}{\partial x^b} \right)$$

$$X_k = a_k^{(a)} (x^{(a)} + u^{(a)}(x^{(b)}, t))$$

$$L = \frac{\pi_0}{2} \left(\frac{dX_{kr}}{dt} \right)^2 - \frac{\lambda}{2} \int \text{Tr} S^2 dV$$

$$- \frac{\mu}{2} \int \text{Tr} S^2 dV$$



2 interactions = core + shell

力 $\vec{a}_k^{(a)}(t) \quad u^{(a)}(x, t)$

$$\frac{dX_{kr}}{dt} = \vec{a}_k \left(\partial_t \vec{u} - (\vec{x} + \vec{u}) \times \vec{\omega} \right)$$

$$\frac{dX_{kr}}{dt} = \vec{a}_k \cdot \vec{x} \times \vec{\omega}$$

$$\vec{\omega} \rightarrow \ddot{a}_k^{(a)} a_k^{(b)}$$

can. conj.

$$\vec{L} \rightarrow \vec{L} = I_1 \vec{\omega} + \square \omega + \square \partial_t u$$

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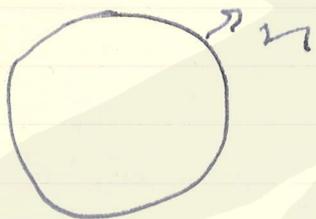
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$$\vec{u} \rightarrow \vec{\pi} = \rho_0 \partial_t \vec{u} - (\vec{x} + \vec{u}) \times \vec{\omega}$$

$$W_{KE} = \frac{1}{2I} \left[\vec{L} - \int dV (\vec{x} + \vec{u}) \times \vec{\pi} \right]^2 + \frac{1}{2\kappa_0} \int \vec{\pi}^2$$

$$V = \frac{\Delta}{2} (\text{Tr } S)^2 + \frac{\mu}{2} (\text{Tr } S^2)$$



$$\nabla \cdot \vec{\pi} = 0$$

$$\Gamma^{ap} = \frac{\partial V}{\partial g_{ap}}$$

$$\vec{u} \rightarrow 1, 2 \rightarrow \begin{matrix} \uparrow \\ \downarrow \end{matrix} \text{ or } 3 \text{ directions}$$

$$Y_{ij|e} = \vec{L} Y_e^m / \sqrt{e(r+1)}$$

$$3 \text{ directions } \left[\begin{matrix} \omega_1 = \omega_2 \\ \omega_3 \end{matrix} \right]$$



$$\vec{u} \cdot \vec{u} = 0$$

積は

$$d\vec{\omega} \cdot \vec{u} = 0$$

$$\vec{L} Y_e^m$$

$$\omega_3$$

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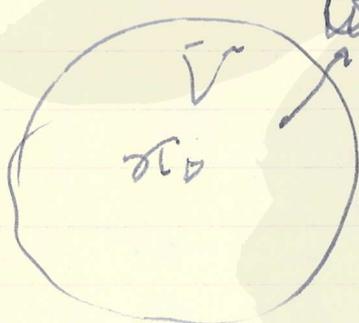
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2) 回転 + 振動
 ω_1, ω_2

$$H = \frac{1}{2} \sum_{i=1}^2 (\vec{p}_i^2 + \omega_i^2 q_i^2) + \frac{1}{2I} \left[\vec{L} - \sum \vec{q}_i \times \vec{p}_i - b \vec{p}_3 \right]^2$$

AN FN model $\pi_0 V$ *coupling*



$W^\mu(x) - \pi_0$

$$ds^2 = -\pi_0 \left(dz_0^2 + dz_1^2 + dz_2^2 \right) \sqrt{g_{00}}$$

$$ds^2 = \sqrt{g_{\mu\nu}} dx^\mu dx^\nu$$

had. frame L \vec{z}
 matter frame E x^μ

$$g_{\mu\nu} = \frac{\partial x^\mu}{\partial z^\alpha} \frac{\partial x^\nu}{\partial z^\beta}$$

$$U_\mu dx^\mu = 0$$

$$dx^\mu dx_\mu = 0$$

rigidity of $\vec{z}(\tau)$
 (Bohr)

$$x^\mu = f^\mu(z_0^0) + a_\mu(z_0^0) \vec{z}^0$$

$$L = -\pi_0 \left(dz_0^0 \right) d\vec{z}^0 \sqrt{(1 - \vec{w} \cdot \vec{z}^0)^2 - (\vec{w} \times \vec{z}^0)^2}$$

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$$\frac{\partial f^{\mu}}{\partial z^{\nu}} = \Lambda a_0^{\mu}$$

$$\dot{a}_0^{\mu} = -\omega_a a_a^{\mu}$$

$$\ddot{a}_a^{\mu} = \omega_a a_0^{\mu} - \omega_{ab} a_b^{\mu}$$

$$L = \frac{I}{2} \omega^2 - M_0 \rightarrow \frac{I}{2} (\dot{a}_a^{\mu} \dot{a}_a^{\mu} + \dot{\omega}^{\mu} \dot{\omega}^{\mu})$$

(for $|\vec{\omega}_0| \cdot r_0 \ll 1$
 $|\vec{\omega}| r_0 \ll 1$)

$$L = \frac{1}{2} \sum_a I_a \omega_a^2 + I_a' \omega_0 a^2$$

$$z^a \rightarrow \xi^a + u^a$$

$z \rightarrow$ harmonic oscillator

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Newton $3+1$
 $p = \frac{1}{3}u$

Foliat
 (divergence, irrotational, $SU(3)$)

i) Non-local Field

$\psi(x_\mu, r_\mu) \rightarrow \text{spin}$
 $SU(2)$

$\psi(x_\mu, r_\mu^{(a)}) \rightarrow SU(3)$
 $a=1,2,3$

ii) non-linear
 非線形, 非局所性

iii) Tati
 N_μ

iv) Extended Model
 拡張モデル

deformable $\rightarrow J, J_3, J^3$
 $SU(3)$ symmetry
 violation

$4+2=7 \rightarrow 7$ 次元

$g_{\mu 5}, g_{\mu 6}, g_{\mu 7} \rightarrow$ 拡張

湯川: あの時とこの時

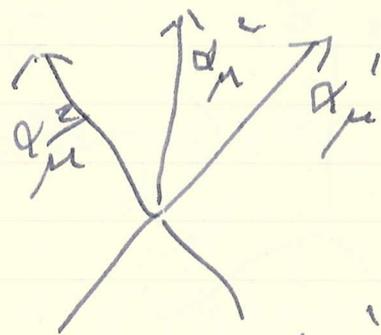
湯川: Triad model

light cone \perp 3本の軸
 $\alpha_\mu^1, \alpha_\mu^2, \alpha_\mu^3$: real null vectors

$$U(\eta) \alpha_\mu^i \alpha_\mu^i = 0$$

ξ_a : 12-component $\xi =$ two comp

$$[\xi_\alpha^{\mu\nu}, \pi_\beta^{\sigma\tau}] = i \delta_{\mu\sigma} \delta_{\nu\tau}$$



$$\xi = \begin{pmatrix} \xi \\ i\pi^* \end{pmatrix}$$

4-comp. spinor

$$\xi_\alpha^{\mu\nu} + i\pi_\alpha^{\mu\nu*} = a_\alpha^{\mu\nu}$$

$$\xi^* + i\pi = b_\alpha^{\mu\nu}$$

$\xi \xi$: invariant

$$U(12) \rightarrow U(6) \times U(3) \rightarrow U(2)$$

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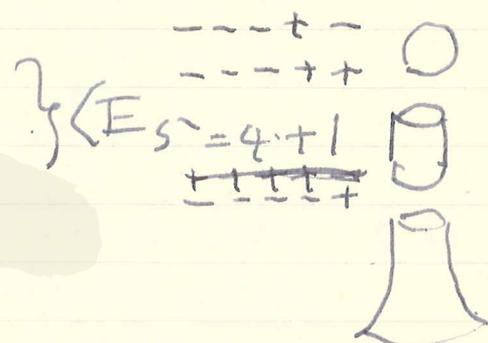
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$$\begin{aligned} z^1 &= \cos \alpha^1 \\ z^2 &= \sin \alpha^1 \\ z^3 &= \cos \alpha^2 \\ z^4 &= \sin \alpha^2 \end{aligned}$$

$$\sum_{\alpha} (dz^{\alpha})^2 = (d\alpha^1)^2 + (d\alpha^2)^2$$

locally $\cong \mathbb{R}^4$ \rightarrow $(ds^2 = -dt^2 + dx^2 + dy^2 + dz^2)$
 globally $\cong \mathbb{S}^3$ (topology of \mathbb{S}^3)

de Sitter
 Einstein
 Relativistic cosmology
 V_4 $---$ ∇



{ geodesic motion }
 局所的に直線的な運動 ($g_{\mu\nu}$ を正規化して δ_{ij})
 局所的に直線的な運動

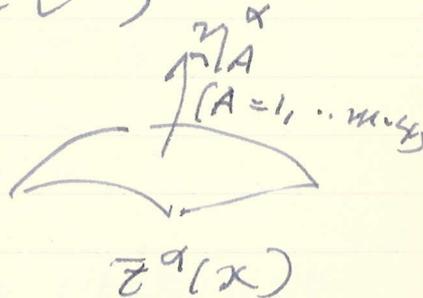
Schwarzschild $\subset E_6$ (Kasner (21))
 Frusdal (199)
 singularity $r = 2m$

(Kruskal (160): 4次元の時空の構造)
 r 座標 $r = 2m$ ($r < 2m$, $r > 2m$)
 $r \rightarrow r = 2m$ $r = 0$

Local embedding

局所的な方程式
 m 次元の可微分多様体

E_m
 z^{α} \downarrow $z^{\alpha} (a=1, \dots, m)$
 unique r 座標



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i) 球面座標

$$ds^2 = (dz^1)^2 + (dz^2)^2 + \dots$$

$$\left. \begin{aligned} z^1 &= kr \gamma^{1/2} \sin(t/kr) \\ z^2 &= \dots \cos(\dots) \\ z^3 &= f(r) \\ z^4 &= r \sin \theta \sin \phi \\ z^5 &= r \dots \cos \phi \\ z^6 &= r \cos \theta \end{aligned} \right\} \gamma = 1 - \frac{2m}{r}$$

$$\left(\frac{dt}{dr} \right)^2 = \frac{2m\gamma^3 + m^2/k^2}{r^2(\gamma - 2m)}$$

(Fischer $k=1$)

ii) $ds^2 = (dz^1)^2 + \dots$

$$\left. \begin{aligned} z^1 &= kr \gamma^{1/2} \sin(kr/2) \\ z^2 &= \dots \cos(\dots) \\ z^3 &= g(r) \end{aligned} \right\} \left(\frac{dt}{dr} \right)^2 = \frac{2m\gamma^3 - m^2 k^2}{r^2(\gamma - 2m)}$$

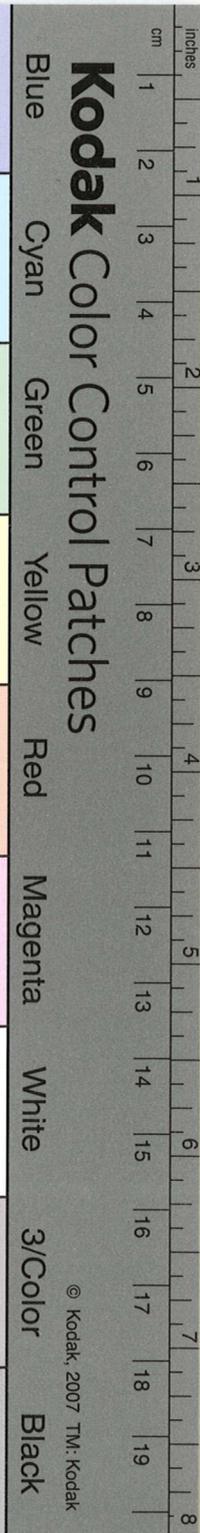
(Fronsdal $k=4m$)

iii) 球面座標

$$ds^2 = \dots$$

$$\left. \begin{aligned} z^1 &= (t^2 - 1) r^{1/2} / 2 + h(r) \\ z^3 &= (t^2 + 1) r^{1/2} / 2 + h(r) \\ z^2 &= t r^{1/2} \end{aligned} \right\} \frac{dh}{dr} = r \gamma^{-1/2}$$

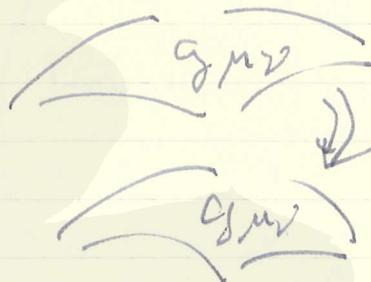
rigidity of embedding



Symmetry & the group $m=4$
 $V_4 \subset E_{10}$ Lorentz

G.

Rigidity



$$z^\alpha \rightarrow d_p^\alpha z^\beta$$

第20年以内

答(1) G: 素粒子 & Cosmology

1. Minkowski space

translation \rightarrow energy, momentum

rotation \rightarrow angular momentum

(Lorentz transf. \rightarrow spin)

$t+t - P_0 < 0 \rightarrow$ anti-particle

$P_4 > 0, P_4 < 0$

Reciprocity

$$x^\alpha \geq 0$$

2. Constant curvature
 translation \rightarrow local

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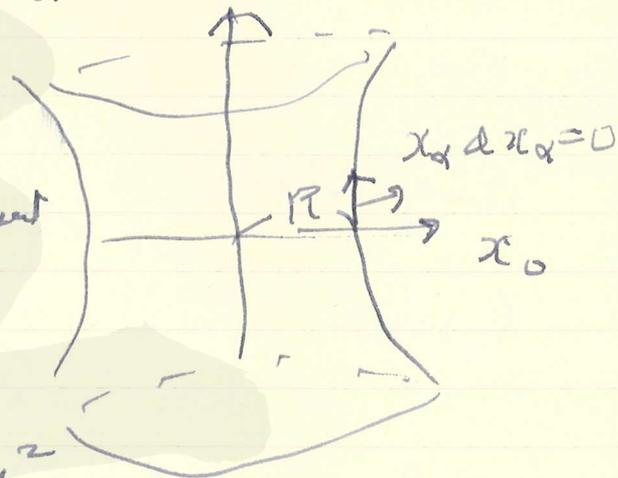
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rotation → global in phase space.

de Sitter space
 $\begin{matrix} 0 & 1 & 2 & 3 & 4 \\ + & + & + & + & - \end{matrix}$
 linear momentum
 $p_\alpha + x_\alpha \Phi(x_\alpha^2)$
 $\begin{matrix} z_0 & z_1 & z_2 & z_3 \end{matrix}$

$$x_\alpha^2 = R^2$$

$\int p_\alpha dx_\alpha$: invariant



$$p_\alpha x_\alpha = 0$$

$$(p_\alpha + x_\alpha \Phi)$$

$$= p_\alpha^2 + x_\alpha^2 \Phi^2 = -m^2$$

$x_0 = R$ の 2次元切片 $x_1^2 + x_2^2 + x_3^2 = R^2$

momentum space
 $R = m = 1$

$$\int (p_\alpha \frac{dx_\alpha}{d\tau} + \lambda p_\alpha p_\alpha + \mu x_\alpha x_\alpha + \nu p_\alpha x_\alpha) d\tau$$

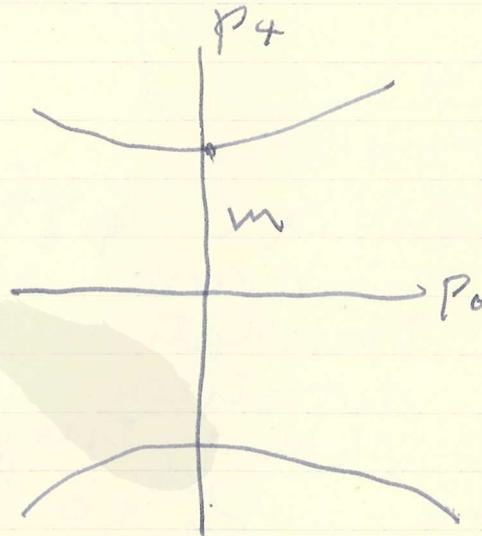
$$\lambda = -\mu, \quad \nu = 0$$

$$\frac{dx_\alpha}{d\tau} = -p_\alpha, \quad \frac{d p_\alpha}{d\tau} = -x_\alpha$$

$$= m^2 / x_\alpha, \quad = m^2 / p_\alpha$$

$$L = p_\alpha p_\alpha + x_\alpha x_\alpha$$

$$H = -p_\alpha p_\alpha + x_\alpha x_\alpha$$



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$$\tilde{O}(110) \quad \tilde{U}(5) \quad S\tilde{U}(5)$$

$$45 - 20 = 25 \quad 25 - 1 = 24$$

$$\pi_0 = \epsilon R \quad \pi_0 = -R$$

Zitterbewegung
 $\gamma_\alpha \rho_\alpha + \gamma'_\alpha \pi_\alpha$

isospin

$$10 = 4 \otimes 0 \text{ spin } \frac{1}{2} \otimes \frac{1}{2}$$

$$25 = 3 \otimes 2 = 8 \oplus 8 \oplus 8 \oplus 8$$

$$(\gamma_\alpha \rho_\alpha + \gamma'_\alpha \pi_\alpha) \Psi(\pi_0, \dots, \pi_4) = 0$$

$$= \frac{\partial \Psi}{\partial \pi}$$

④ ④ ④: $K_2^0 \rightarrow \pi^+ + \pi^-$
 $\sim 1.3 \text{ GeV} \sim 10 \text{ GeV}$
 $K_2^0 \rightarrow 2\pi \sim 10^{-6}$
 $K_1^0 \rightarrow 2\pi$

CP-non-invariance

$$P_M = P_M^{(0)} + N_M \int H(\pi, N) d\sigma$$

$$[\phi(\pi, N), \phi(\pi', N)] =$$

CP=+1



$$\phi_{K_1^0} \phi^* \phi$$

$$\phi_{K_2^0} [\phi^* \phi F(N; i\partial)] \phi - \phi F(N; i\partial) \phi^*$$

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News 平井

TRG:

1. D. Ivanenko, On Mesons and Cosmology
 intermediate boson

$$\Delta S = 0: W_1, m_1$$

$$\Delta S = 1: W_2, m_2$$

$$m_1 \neq m_2$$

CP-invariance

$$e^{i\theta} = (1 \pm F)^{\pm 1} dS^2$$

conformal

$$K_2 = (K_2)_0 + F \cdot (K_1)_0$$

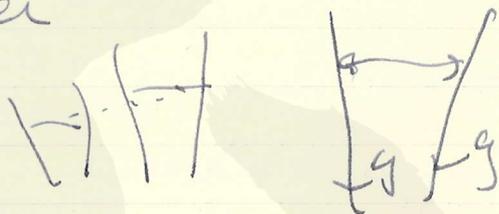
2. J. A. Wheeler, The Non-locality of Force

力

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by J. A. Wheeler
 同上



3. 平井

Wentzel: On Baryon ground states
 in Yukawa Theories

Strong coupling

SU(3) singlet ground state τ

D-coupling

F-coupling (Dallemond)

singlet τ ground state τ

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Lindan
#1510

June
July

1965

July 1, Dirac: Foundation of Q.M.,
Yukawa: Space-Time Description
and Matter
Heisenberg: Fine structure
Constant

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模範工研究会 基研

July 19 ~ July 21, 1965
 19日: 午前
 午後

社名: 日田

社名: ~~日田~~

社名: Urbaryon

Urbaryon 内部の力や相互作用か?
 magnet

$N \leftrightarrow S$

3, 3*

χ_i monopole or spin 2 の baryon member の triplet $\rightarrow N = 0, 1, 2, \dots$
 χ_i \rightarrow $N = 0, 1, 2, \dots$
 χ_i \rightarrow $N = 0, 1, 2, \dots$

R -symmetry
 $R: +1, -1$

N_8, N'_8
 $+1(-1) \rightarrow -1(+1)$
 $1480 N_i^*$

$N_8, N_8 \pi_8 \rightarrow D$ -type
 $N_8, N_8 \pi_8 \rightarrow F$ -type
 $\pi_8 \rightarrow \pi_8 + V_8$

baryon: $\chi: \bar{A}_i \pm \chi_j A_i$

M.C.	+1	-1
χ_i	χ_i	χ_j
A_i	A_i	\bar{A}_j

π meson: $u\bar{d}$ meson, $\bar{u}d$ meson
 i) $t\bar{t}$
 ii) $t\bar{t}$
 π meson $\bar{t}t$

$SU(6)$
 $\mu_t/\mu_u = -3/2$

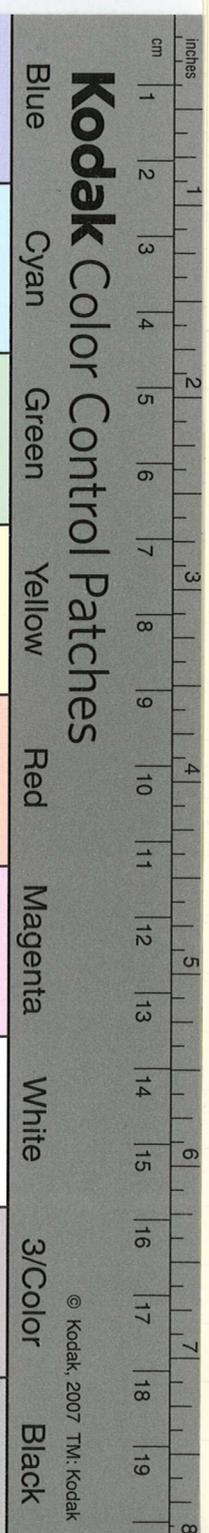
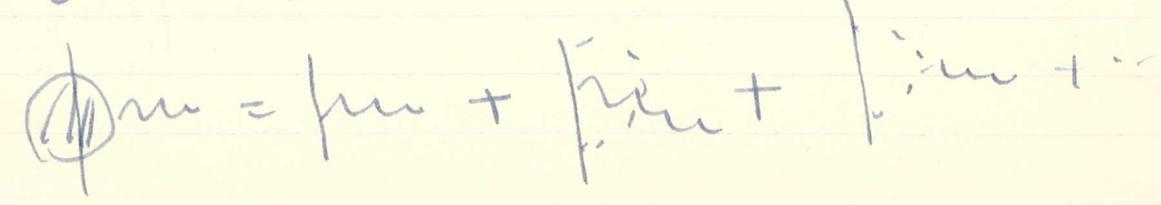
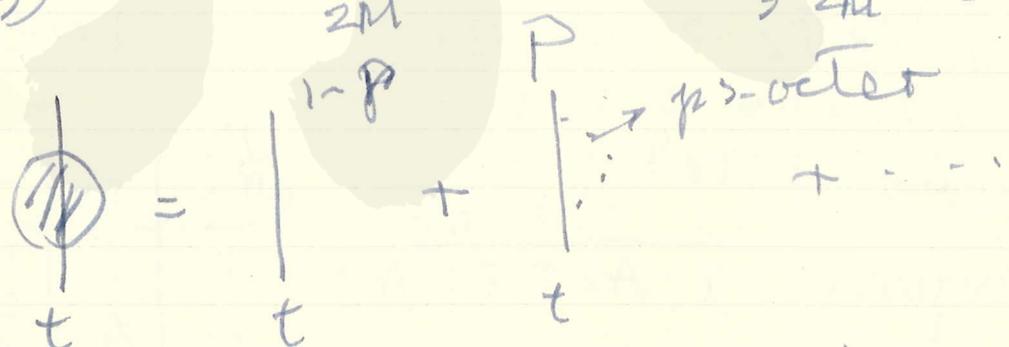
this: quarks q $\mu_t \propto q_t$

$M_t = \frac{t\bar{t}a_t}{2m_c} \pi S$

$M_B = \frac{1}{M} \sum_i q_i J_i$ ($\kappa = 1$ for without S.I., $\kappa > 1$ with S.I.)

$t\bar{t}t$: $J = 1/2$
 (A) fermion $8 \rightarrow SU(6) 20 = \bar{3}\pi$
 (B) para-fermion $8 \rightarrow SU(6) 56 = \bar{3}\pi$

(A) $-\frac{1}{3} \frac{e}{2M} \pi$ $\frac{2}{3} \frac{e}{2M} \pi$
 (B) $\frac{e}{2M} \pi$ $-\frac{2}{3} \frac{e}{2M} \pi$



$$\begin{array}{c} u \\ | \\ d \quad -\frac{1}{3} \quad \vdots \quad \pi^+ \\ | \\ u \quad \frac{2}{3} \end{array}$$

$$\begin{array}{c} u \\ | \\ s \quad \vdots \quad K^+ \\ | \\ u \end{array}$$

$$\frac{\kappa}{2M} = (1-P) \frac{1}{2M} + P \frac{1}{2M} \left(\frac{1}{24} + \frac{M}{\omega} \frac{3}{4} \right)$$

ω : meson cloud の 平均のエネルギー

form factor

$$P^{(q)}(r) = Q^{(q)} \{R(r)\}^2$$

$$P^{(u)}(r) = \mu^{(p)} \{R(r)\}^2$$

$$\langle \sigma_{EN} \rangle = 0 \quad \text{の 説明が できる。}$$

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2001: 4/19

7/19: 相対

5/19: 相対. 田代. 技術: CP-violation
 $K_2 \rightarrow \pi^+ \pi^-$

N_μ

$n_\mu = \lambda N_\mu$

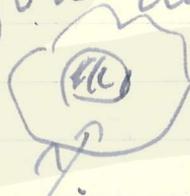
$\pi^+ F(n_\mu \delta_\mu) \pi^-$

$\lambda \approx 10^{-17} \text{ cm}$

田代, 田代: baryon current

level I

baryon



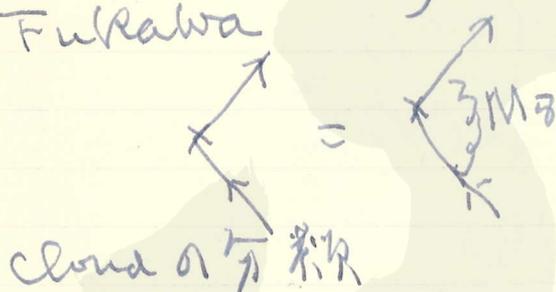
level II

mbaryon

core n (7/19)

cloud of particles

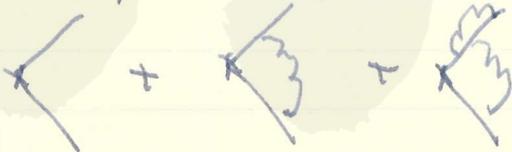
Fukawa



$$\frac{F}{D} = \frac{f}{d} = \frac{1}{3}$$

weak strong

cloud of particles



"single cloud"



"double cloud"

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定理 1. octet cloud is relevant
 self-energy diagram in D/F
 ratio is not zero.

定理 2. single cloud of χ is not relevant, $d/f = \pm 1/3$

$$\begin{aligned} & \left(\begin{array}{l} J(8) \approx J^V + J^A \\ F \end{array} \right. \quad D:F = 3:1 \\ & \left. \begin{array}{l} SU(6) \rightarrow F, \quad D:F \approx 3:2 \end{array} \right) \end{aligned}$$

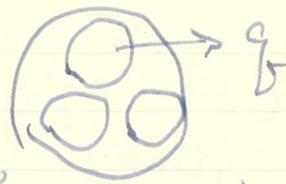
定理 3. single cloud correlation
 is $d/f = \pm 3$ or $\pm 5/3$

$D/F = \pm 3$ or $\pm 5/3 \rightarrow$ not relevant
 or $\pm D/F$ ratio is not zero.

χ の 40% の寄与は？

core の 4 quadrants の
 寄与は？

$$\begin{aligned} \Sigma^+ & \leftrightarrow \Lambda & d_A &= \frac{3}{2} \\ \Sigma^+ & \leftrightarrow \Sigma^0 & f_A &= \langle \chi | \chi \rangle \end{aligned}$$



$$\Sigma^+ \quad u^\uparrow u^\downarrow s^\uparrow$$

$$\begin{aligned} f_A &= 0 \\ d_A &= -1 \end{aligned} \quad (SU_6 \quad 20 = \frac{3}{2} \times 8 - 8)$$

$$\begin{aligned} |\Sigma^+\rangle &= a |u^\uparrow u^\downarrow s^\uparrow\rangle + b |u^\uparrow u^\downarrow s^\uparrow\rangle \\ f_A &= |a|^2 & d_A &= 2|a|^2 - |b|^2 \end{aligned}$$

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$$f_V = 1, \quad d_V = 0$$

* 例: Vector meson (bosons with double structure)

$$O^+ \sim 700 \text{ MeV} \quad \rho, \omega, \phi, \pi, \eta, \eta'$$

$$T \begin{pmatrix} \mu\nu \\ (\lambda\rho) \end{pmatrix}$$

$$T \begin{pmatrix} \mu\alpha \\ (\nu\beta) \end{pmatrix}$$

$$10 \rightarrow \mathbf{8} \rightarrow \mathbf{1} \oplus \mathbf{8}^*$$

$$8 \rightarrow \mathbf{8}$$

$$M_8^{(\pm)} = \frac{1}{\sqrt{2}} (M_8 \pm \tilde{M}_8)$$

π	725
K^*	890
ρ	780
ϕ	1020

	ρ_1	ρ_2	ϕ_1	ϕ_2
G	+1	-1	-1	+1
CP	+1	+1	+1	-1

$$\rho \quad \omega \quad \phi \quad \pi \quad \eta \quad \eta'$$

($\omega \pm \eta, \eta'$ structure)
 ($\pi, \eta, \eta', \rho, \phi$ structure)
 (π, η, η' structure)

* 例: π, η, η'

例: π, η, η' 相 (自) 荷 = 0. 例: PS bases

{1} level I,

$$[\pi \pi \pi] \quad 2_3 \rightarrow 0$$

{2} PS meson

I, π, η, η'

$$\sim (\pi \pi \pi)^+ \dots (N \bar{N})^+ \dots$$

$$\sim (\rho \pi)^+ \dots (N \bar{N})^+ \dots$$

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S-
 $\rho(\pi\pi)$
 和支カ $\pi\pi$ と η と
 ρ π
 ω η

" ρ 介在型"
 " ω 介在型"

$$\mu^2 > 2M^2$$

近距離($\ll 1/\mu$)の
 強い引力

(2) ρ - $(\rho\pi)$
 ρ π
 ω

" ρ 介在型"
 " ω 介在型"

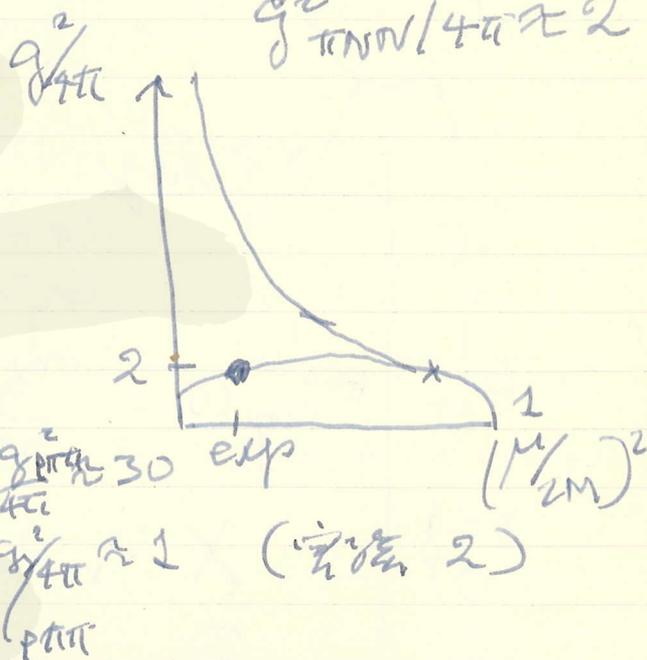
μ 大せ、

$$\frac{g_{\rho\pi\pi}^2}{4\pi} \approx 30 \text{ exp}$$

$$\frac{g_{\omega\pi\pi}^2}{4\pi} \approx 1 \text{ (実験)}$$

$$\frac{g_{\rho NN}^2}{4\pi} \approx 2$$

$$\frac{g_{\omega NN}^2}{4\pi} \approx 2$$



π, K -meson: $K = (\pi\pi\pi) + \dots (\eta, N) + \dots$
 $\sim (K^*\pi) + (K\rho) + \dots$

i) ρ $S(\pi\pi)$ x
 ii) ρ $(K^*\pi)$ ω 介在型

$$\frac{g_{K^*\pi\pi}^2}{4\pi} \approx 0.5$$

[3] ρ : " ω 介在型" ($g_{\rho NN}^2/4\pi \approx 20$)

[V] ρ :
 ρ ω :

[4]

→ 和支カ $\pi\pi$
 ω 介在型か?

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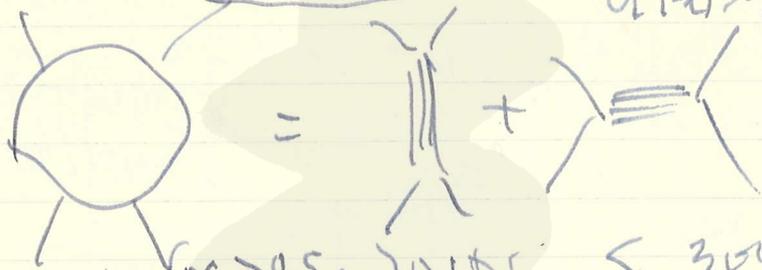
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700 MeV group: 核力 (IR. 力)
 OBEC: ~~Yang-Mills~~ g_0 の存在,
 level I. \rightarrow II \rightarrow ρ の resonance
 の同型性.



$(\tau \geq 0.5 \sim 0.6 \text{ g}) NN \lesssim 300 \text{ MeV}$

π	\odot	$G_\pi^2 \sim 14$
η	Δ	$G_\eta^2 \sim 5$
$I=0$ 0^+	\odot 600 MeV $\sim m_\rho$	$m_\rho = 700$ $g_\rho^2 \sim 15 \sim 20$ $\rightarrow \rho_0$ (ABC) (240 ~ 200 MeV) $\sim m_\rho$
$I=1$ 0^+	\times	$g_\rho^2 \rightarrow 1$ ($m_\rho \sim 200$ MeV)
ω	\odot	tensor coupling main vector coupling main
$I=1$ 0^+	\odot	1260 MeV ?
$I=0$ 0^+	\odot	1020 ?
2^+ 0^+	\odot	ρ_0 の存在の存在

1.14: TPEP の存在の存在

2.14: TPEP の存在の存在
 Hamiltonian の存在の存在

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原注: Gemisch

ϕ_1, ϕ_2, \dots states
 w_1, w_2, \dots statist. weights

$$\phi = \phi_1(x_1) \phi_2(x_2) \dots$$

$$\bar{R} = \sum w_n \bar{R}_n$$

$$\bar{R} = \frac{1}{N} \sum_i R_i$$

$$R_i = \frac{1}{N} R_i$$

i) $\frac{1}{3}$

ii) $\tau + \tau$

相互作用

iii) $\tau + \tau$ quarks or $\tau \rightarrow \tau + \nu + \bar{\nu}$?

i) $N=3$

$$H = \frac{1}{3} \sum H_i$$

$$\{\tau_i, \tau_j\} = \delta$$

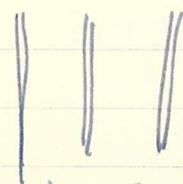
$$[\tau_i, \tau_j] = 0 \quad (i \neq j)$$

$$a_3^\dagger a_2^\dagger a_1^\dagger |0\rangle$$

(1, 2, 3)

SU_3 symmetric

symmetric



相互作用

in 10: generic

in 10: SU_6 invariance of interaction
 = 2つの場合

dynamical symmetry of hydrogen atom is $O(4)$ symmetry
 of spin (Pauli)

$$[L_i, L_j] = i \hbar \epsilon_{ijk} L_k$$

$$[A_i, L_j] = i \hbar \epsilon_{ijk} A_k$$

$$[A_i, A_j] = -2i \hbar \epsilon_{ijk} L_k$$

$$\vec{A} = \frac{1}{2} [\vec{L} \times \vec{p} - \vec{p} \times \vec{L}] + \frac{\hbar}{r} \vec{p}$$

energy (H) is conserved
 for both.

strong coupling symmetry

$$[A_\alpha, A_\beta] = 0$$

$$[I_i, I_j] = i \epsilon_{ijk} I_k$$

$$[A_\alpha, I_j] = i D_{\alpha\beta}(j) A_\beta$$

hydrogen atom $E=0$ の場合
 の場合
 meson

$$SU_2 \times SU_3 \rightarrow A_{10} \rightarrow SU_6$$

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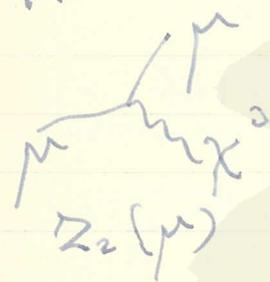
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④中：新発見の粒子の起源



SU(3)の破れ



μ - e difference

(t_1, t_2, t_3)
 B

破れ (lepton)

$n_B = 0$

$n_B = -1$



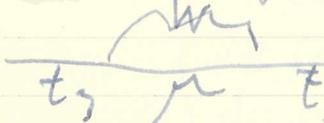
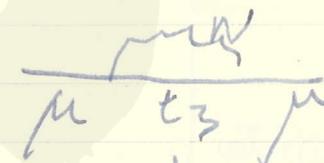
$(t t t)$
 $(t \bar{t})$

破れ charge & neutral state

t_1^+, t_2^-, t_3^-

$B^{++} \left\{ \begin{array}{l} l = +3 \\ a = +2 \end{array} \right.$

t の μ と e
semi-weak

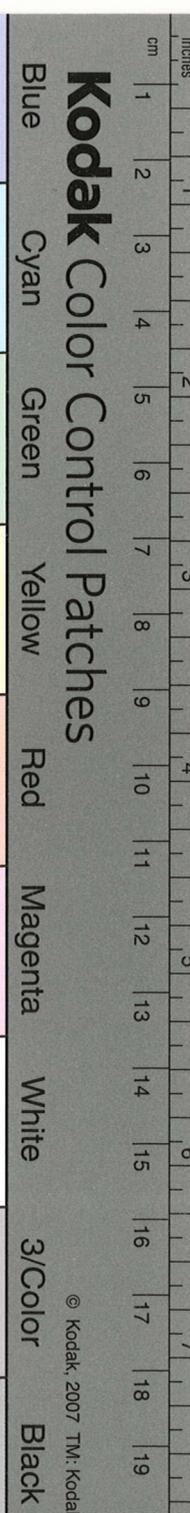


$\bar{t}_3 \gamma_\mu \mu W_1$
 $+ \frac{(1+\gamma_5)}{2} \mu W_2$
 $+ \frac{(1-\gamma_5)}{2} \mu W_3$

weak

$\{ \bar{\mu} \nu_\mu + \bar{e} \nu_e + (\bar{t}_2 + \bar{t}_3) t_1 \} W_3$
 $+ W_1^* W_2$

Okun et al.



21日 第3回: 12月 11日
 Summary, discussions
 沢田:

baryon (8) $\rightarrow B^*$
 meson (8) $\rightarrow M^*$
 Hsu: Hsu, et al の Hsu 論文
 triplet (sep 3)
 para (OK) 221
 strong.

g_{λ}

$\lambda = 1, 2, 3$
T S 2
$\frac{1}{2}$ 0 1
0 -1 1

Q, Y, N eigenstate
 combination of
 eigenstate

$$([g_{\lambda} g_{\mu}] + g_{\nu})_{\rho}$$

$$[g_{\lambda} g_{\mu}]_{\rho}$$

1, 3, 5, 5, 6

相互作用の state
 super selection rule

Green Ansatz
 $g_{\lambda} = \frac{1}{\sqrt{3}} \sum_{\alpha} t_{\lambda\alpha}$

subtriplet
 $Q_1 + Q_2 + Q_3 = -1$

electromagnetic
 interaction is
 subtriplet

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式名: 核力

O B E C

Potential

Dispersion

2. π - π O B E C π al.

l to λ π π (π π)

core

π π π π .

π π π π

S-wave

π π π π core π π π π .

(E R L O: 1S_0 π π (π π π π core π π π π).

$$\sum_i \frac{e^{-\pi_i r}}{r} \quad \pi^0 \quad O, K. \quad (\rho, \omega \text{ 系数の mass})$$

± E R L O: Concluding Remarks

4 π π π π

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初級物理研究会

7.26 ~ 7.29

予習

1. unitary symmetry
980714 (W. 8%a) 等

1965 年 夏

2. 内訳定値と Lorentz 群 の 関係
3. parastatistics

尺貫：初級物理研究会の報告

尺貫：B.S. 方程式と norm

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手紙

内容: SU_6, SU_9 & Horewty 群.

Sakita $\left\{ \begin{array}{l} \kappa^+ \kappa^0 \eta \\ p^+ n^+ \Lambda^+ \\ p^- n^- \Lambda^- \end{array} \right. \quad SU(9)$

symmetry breaking
 kinetic energy? : non-relativistic
 quantization of symmetry \approx
 破らさ!!!

1. parafermion

|||

symmetric

2. particle & anti-particle or
 adjoint repes.

$SU(9)$ & conditional symmetry
 Ψ の一部を壊す.

(Horewty 群 $SU(2, C)$ } a.s. (2, 2, 2)
 $SU(9)$ } $SL(9, C)$
 $U(18)$

$$(\Gamma_\mu \Gamma_\mu + m) \begin{pmatrix} \vdots \\ \vdots \\ \vdots \end{pmatrix} = 0$$

$\mu = 1, \dots, 18$

scalar or
spinion?

加藤:

$$O(12) \supset L \otimes SU(3)$$

例 11): de Sitter space の 4 次元の 超空間

4 次元の 超空間に 4 次元の 超空間の 部分

10 次元の 超空間の embedding

global symmetry

$\phi = \eta \pi$ の pseudo-Euclid space

$(F + F + \dots)$

$$p_\alpha^2 + x_\alpha^2 = \text{inv} \rightarrow a_\alpha^* a_\alpha = \text{inv.}$$

proper de Sitter Map $q(\alpha, i)$

$$x_0 = \tau - x_0$$

$$x_4 = \tau - x_4$$

4 次元の 超空間の 部分

$$SU(5) \times SU(4)$$

例 12): Dynamical symmetry
 strong coupling limit symmetry of J^2, T .

C. J. Geibel:

$$[A_\alpha, A_\beta] = 0$$

kinematical group \rightarrow dynamical group

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第2回 July 27, 2017

中野: $O(5)$ 対称性
 higher spin の 運動方程式

Type I, $S \geq 3/2$

Type II, $S \geq 1/2$

$$D_5(l_1, l_2) = \sum_{l_1=l_2}^{l_1} \sum_{l_2=-l_2}^{l_2} D_4(l_1, l_2)$$

$$D_4(l_1, l_2) = \sum_{l=|l_2|}^{l_1} D_3(l)$$

$$\vec{m} = (m_{23}, \dots, \dots)$$

$$\vec{n} = (m_{14}, \dots, \dots)$$

$$(\vec{m}^2 + \vec{n}^2) | \rangle = \{l_1(l_1+2) + l_2^2\} | \rangle$$

$$\vec{m} \vec{n} | \rangle = (l_1+1) l_2 | \rangle$$

$$\alpha_\mu = m_{5\mu}$$

$$(V_\mu \partial_\mu + M) \psi = 0$$

$$V_\mu = \sum_{l_1=l_2}^{l_1} \sum_{l_2=-l_2}^{l_2} \sum_{(a,b)} a_{(a,b)}(l_1, l_2)$$

$$\times P(l_1+a, l_2+b) \alpha_\mu P(l_1, l_2)$$

$$(a, b) = \{0, \pm 1\}$$

$$\{\pm 1, 0\}$$

$$S = \sum_{l_1=l_2}^{l_1} \sum_{l_2=-l_2}^{l_2} b(l_1, l_2) P(l_1, l_2)$$

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Lagrangian

$$\psi^\dagger = \psi^* \eta$$

$$\psi^\dagger (V_\mu \partial_\mu + M S) \psi$$

$$\eta = 1$$

$$\left. \begin{aligned} \eta V_R + V_R \eta &= 0 \\ \eta V_4 + V_4 \eta &= 0 \end{aligned} \right\}$$

ηV_μ : hermitian

Type I: $S=1$

$$P_1 = h_2: a \begin{pmatrix} a & b \\ a & b \end{pmatrix} (l_1, l_2) = a \begin{pmatrix} l_1 + a & -l_2 - b \end{pmatrix}$$

spin $1/2$

spin $1/2$

$$(D - M^2) \psi_a = 0$$

$$\frac{1}{2} (1 - \gamma_5) \gamma_a \psi_a = 0$$

$$\frac{1}{2} (1 - \gamma_5) (\delta_{ab} - \frac{1}{4} \gamma_a \gamma_b) \psi_b$$

$$\frac{1}{2} (1 + \gamma_5) \psi_a = \frac{1}{2} (1 + \gamma_5)$$

$$\times \left[\frac{1}{\sqrt{3}} \partial_a - \frac{1}{4\sqrt{3}} \gamma_a \gamma \partial \right] \gamma_b \psi_b$$

16 β 's \rightarrow 4 β 's
 propagator: $\frac{1}{D^2}$

$$\frac{1}{(D - M^2)^2}$$

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Unitary symmetry of
 $\mathcal{H} \supset \mathbb{R} \times \mathbb{R} \times \mathbb{R} \times \mathbb{R}$

$\mathcal{H} \supset SU(6) \times \mathbb{R} \times \mathbb{R}$

1. Non-relativistic limit X?
2. Strong coupling limit
3. Exact symmetry $\rightarrow SU(6, C) \rightarrow P_\mu (\mu=1, \dots, 6)$
4. Dynamical symmetry

3. $[\Gamma^A P_A - m] \psi = 0$ \rightarrow quarks $(G = \mathbb{R} \times \mathbb{R} \times \mathbb{R} \times \mathbb{R})$
 \rightarrow $(1, 2, 3, 4, 5, 6)$
 $A = 0, 2, \dots, 7 \pm$

$1, 2, 3, 4, 5, 6$

$P^A = \begin{pmatrix} 0 & J_A \\ J_A & 0 \end{pmatrix}$

$A = 0, \dots, 3, 5$

$P^A = \begin{pmatrix} 0 & J_A \\ -J_A & 0 \end{pmatrix}$

$J_A = \sigma_{\mu\nu} \lambda$

$\det [\Gamma^A P_A - m] = 0$

$P_0 = \text{energy}$

$P_i = \text{momentum}$

gluon v. λ or ...

$\downarrow P_i (7, 1) : \text{real}$

or $P_0 : \text{real}$

light cone:
 mass shell!

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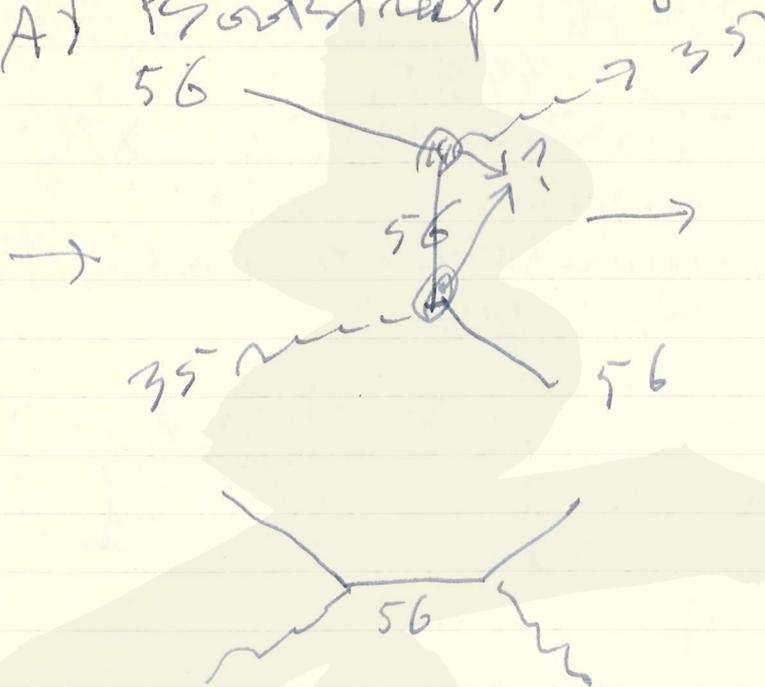
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4. Dynamical symmetry
 A) $SO(2,1)$ trap



$31(1\pi)$	
56	$1/5$
70	$-2/5$
200	$2/5$
1134	$-2/45$

B) $[H, J_i] \neq 0$

$$[J_i, J_j] = i f_{ijk} J_k$$

$$|b(\alpha)\rangle = e^{i\alpha_i J_i} |a\rangle \text{ の基底}$$

H.O. H at a

$$\left. \begin{aligned} [H, a] &= -\dot{a} \\ [H, a^\dagger] &= \dot{a}^\dagger \\ [a, a^\dagger] &= 1 \\ [a, a] &= 0 \end{aligned} \right\}$$

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\mathbb{R}^4 上の P : Internal space & Lorentz 群
 group generator
 \mathbb{R}^4 I (H, E) \mathbb{R}^4
 I.H.L. \mathcal{P} L (P, M)
 \mathcal{G}

$$[I, L] = 0 \text{ と } P \text{ の } \mathbb{R}^4 \text{ 上}$$

$$[P_0, E_\alpha] \neq 0$$

of $\mathcal{P} \times \Lambda$ の realization

of $\mathcal{G} \supset \mathcal{P}$

McGlinn (1964) \rightarrow O'Raifeartaigh (1965)

if $\mathcal{G} = \mathcal{G} \otimes \mathcal{P}$

(ii) \mathcal{G} : 無限次元の Lie 群代数, parameter \mathbb{R}^4

(iii) $P_\mu P^\mu = -m^2$ self-adjoint \mathcal{P} の spectrum

(iv) Hilbert space \mathcal{H} with positive metric

(a) Hilbert space \mathcal{H} indefinite metric \mathcal{H}

(b) P^2 : self-adjoint \mathbb{R}^4 の X

(c) \mathcal{G} : infinite dim.

(d) \mathcal{P} を modify

(b) Stueckelberg (1965)

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(3) 4085 498
絶対的 498 498

charge
baryon number
lepton number

管状見: 多次元化

小論文) 文章執筆

福留氏の other theory

Wigner,

Relativity

記号 (Helvetica)

$$\left. \begin{array}{l} \chi_{\mu} \\ \frac{\partial}{\partial \chi_{\mu}} \end{array} \right\} \rightarrow \left. \begin{array}{l} \varphi_{\mu} \\ \frac{\partial}{\partial \varphi_{\mu}} \end{array} \right\}$$

$$\Psi(\varphi(x))$$

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physical (field?)

plenum reality → strong
miukowski → weak

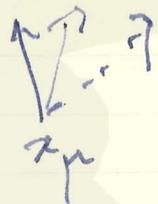
(4) plenum or energy
 (4) plenum or energy



ある点での場の値

$$\chi_a(x)$$

field value



$$\varphi(x_\mu; \chi_{ap}(x))$$

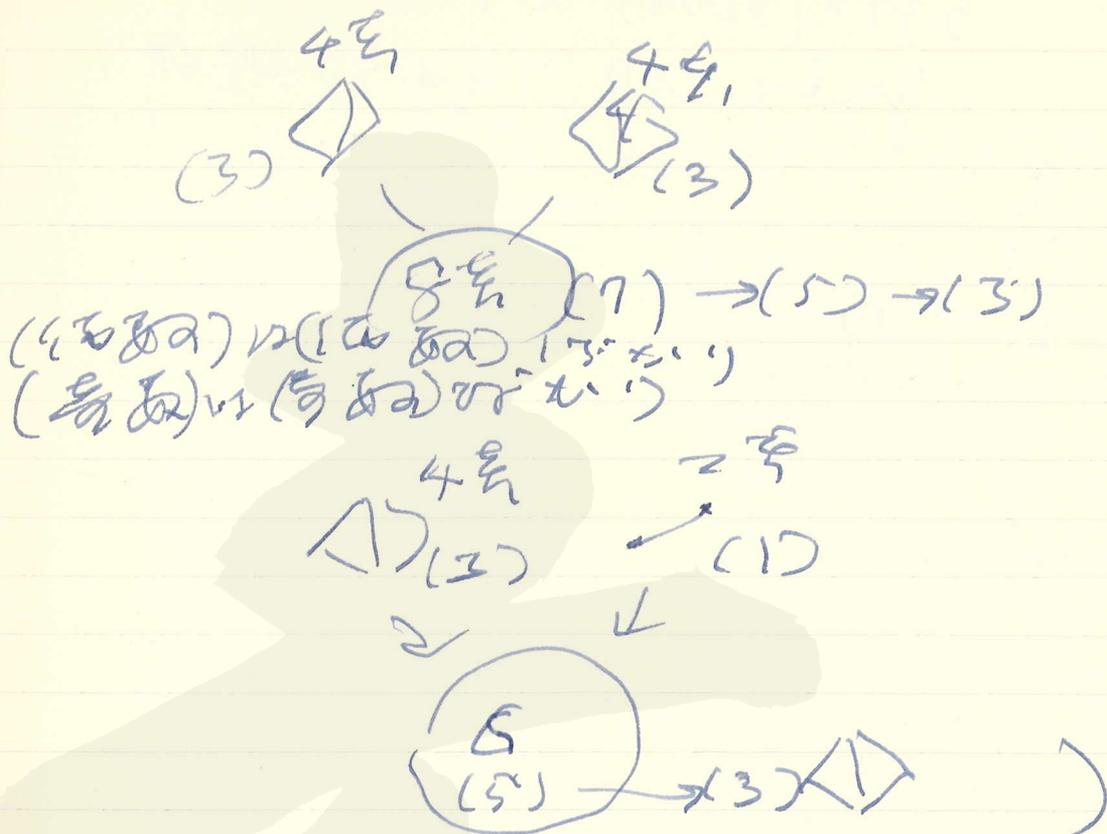
- 1) Translation x_μ の displacement
- 2) Lorentz $x_\mu, \chi_{ap}(x)$ の変換
- 3) SU3 $\chi_{ap}(x)$ の変換

(5) 構造の場の量子化 → 相互作用
 相互作用



(6) 7 構造 $x_\mu, 5, 3$

構造の成立
 相互作用



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S行の理論の終り 猪熊
July 29, 1965, 豊崎

寛波: ...

何封

流の中心

林 (学大物理)

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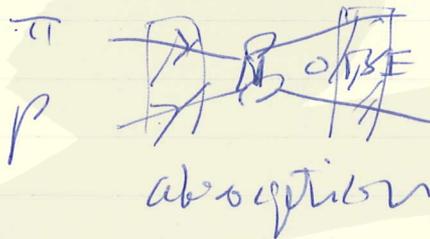
Oct. 27, 1965

chap. High Energy Scattering
elastic backward $\pi^+ p \rightarrow \pi^+ p$
charge exchange

forward $\pi^+ p \rightarrow \pi^+ p$
large angle scatt., $K p \rightarrow K^* p$
($\sim 90^\circ$)

§ 1. Byers-Yang

§ 2. peripheral absorption model



§ 3. large angle scattering

§ 4. Analyticity, $s \leftrightarrow t$ Analysis

chap. 2 Symmetry

Byers-Yang: $\pi^+ p$ charge exchange
scattering and a "coherent Droplet"
Model of H. E. P.

$$-t = 2R^2(1 - \cos\theta) = (2R \sin \frac{\theta}{2})^2$$

$$\frac{d\sigma}{dt} = \pi \lambda^2 \frac{d\sigma}{d\Omega}$$

Exp. Results

$$\frac{d\sigma}{dt} = A e^{\alpha t}$$

$$\alpha \sim \frac{1}{2} R^2$$



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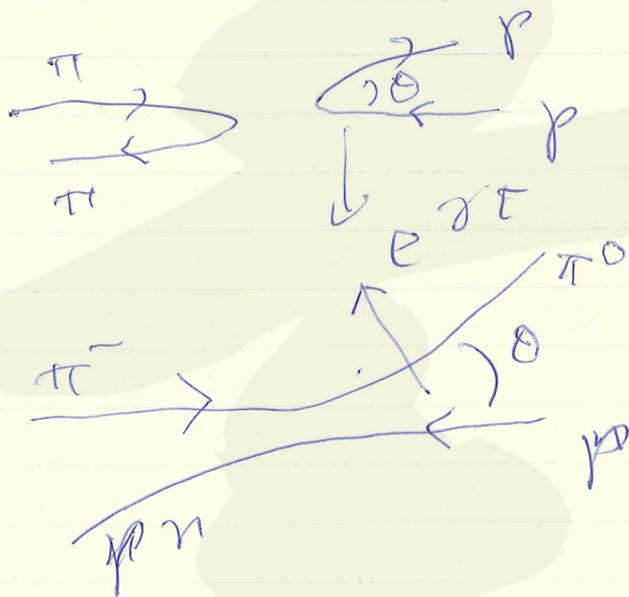
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$$\gamma \sim 10 (GeV/c)^{-2}$$

$$\rightarrow R \sim 0.3 \gamma \rightarrow 10^{-13} \text{ cm}$$

(hadron hard core meson)

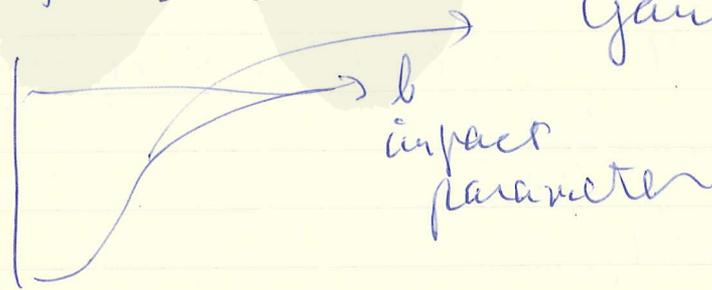
	0.2 γ
	0.5 γ
	1.4 γ



diffraction scattering

$$f = \frac{i}{2\pi} \sum (2l+1) (e^{2i\delta_l} - 1) P_l(\cos\theta)$$

gauge theory



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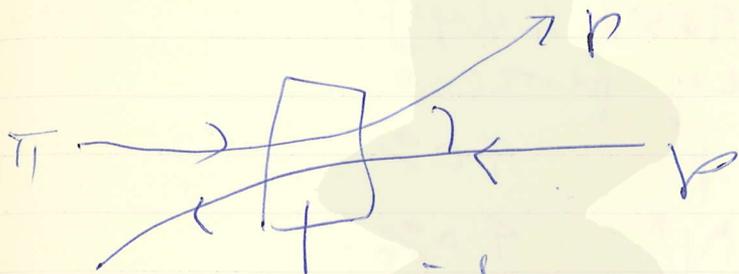
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Black

charge exchange $\pi^+ p \rightarrow \pi^0 n$, $\pi^- p \rightarrow \pi^0 n$, $\pi^- p \rightarrow \pi^- p$

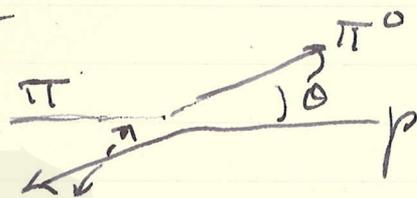


with quantum number transfer
 exchange
 0.87.

第21回 Nov. 5, 1965
 Polarization

$$f = A + B i \sigma \cdot \hat{n}$$

$$P = \frac{2 \operatorname{Im} A B^*}{|A|^2 + |B|^2}$$



polarization $\pi^+ p$
 $\pi^- p$, diffraction in $\pi^+ p$

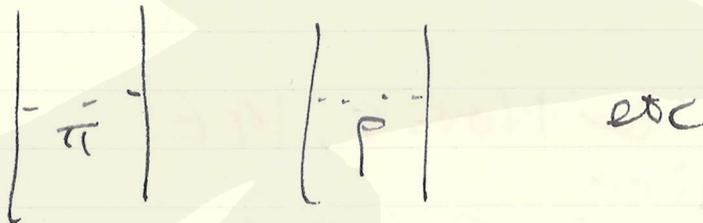
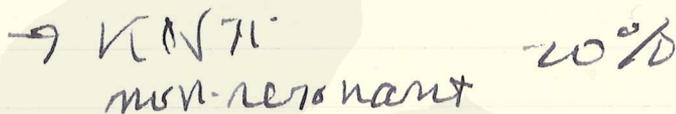
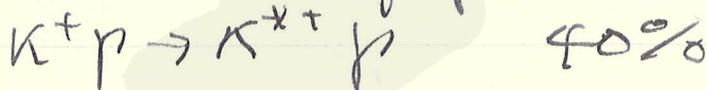
2 GeV $\pi^+ p \rightarrow \text{elas}$ 宇野
 Suwa et al, P.R.L.
 Sept. 27, 1965

Kodak Color Control Patches

Blue Cyan Green Yellow Red Magenta White 3/Color Black

J. D. Jackson, Peripheral Production
and decay correlations of Resonances
(RMP 30 (1965), 484)

quasi-two-body process



Kodak Color Control Patches

Blue

Cyan

Green

Yellow

Red

Magenta

White

3/Color

Black

Hama, p-p collision
研究 Nov. 16, 1965

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Blue

Cyan

Green

Yellow

Red

Magenta

White

3/Color

Black

π -p collision

湯川 π -p: Energy dependence
 large angle scattering

湯川 Nov. 17, 1965

(π^+ π^-)

$$-t = 2k^2(1 - \cos \theta)$$

$$\frac{d\sigma}{dt} = A e^{\alpha t}$$

experimental
Data

Yang T peripheral

Regge

elastic
forward
backward

$$\left. \frac{d\sigma}{dt} \right|_{t=0} = A e^{\alpha t} \text{ const}$$

diffracton
OK
OK

diffracton
OK (?)

pole
(P, P, P)
Pomeron
sgn
P (?)

π -p
charge
exchange
forward

$$\left. \frac{d\sigma}{dt} \right|_{t=0} = \frac{1}{P_L}$$

$$P_L = 6.2/8 (GeV/c)$$

const.
X

OK
(P)
Re $\alpha(0)$
= 1/2

Polarization

elastic
forward
backward

$e^{-i\alpha}$
T

$e^{-i\alpha}$
—

$\sigma^{\pi p}$
T
? πp

π -p C.E. forward

T

$e^{-i\alpha}$

$e^{-i\alpha}$

elastic pp $0(90^\circ)$
 $e^{-\alpha E \ln t}$

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Nov. 24, 1965

† 論文: Pommeranchuk's Theorem
 and its Extension

Pomer. Theorem (1958)

$$p + p \rightarrow p + p \quad \sigma_+$$

$$\bar{p} + p \rightarrow \bar{p} + p \quad \sigma_-$$

$$i) \sigma_+(s) \xrightarrow{s \rightarrow \infty} \sigma_+(\infty) \neq 0, \infty$$

$$ii) \sigma_-(u) \xrightarrow{u \rightarrow \infty} \sigma_-(\infty) \neq 0, \infty$$

iii) dispersion relation for $\sigma = 0$ is valid,

iv) force range R is finite (for $p-p$)

$$\sigma_+(\infty) = \sigma_-(\infty)$$

$$|f(0)|^2 < C E p^2$$

$\sigma \neq 0$ (for $1 \cdot 1 \cdot 1 \cdot 1$) $\neq f(u) \neq 0$

van Hove P.L., July 15, 1963

$$\sigma_{tot} \propto A(s, 0)/s$$

$$ii) A(s, t)/s \xrightarrow{s \rightarrow \infty} a(t)$$

$$iii) A(u, t)/u \xrightarrow{u \rightarrow \infty} \bar{a}(t)$$

$$iv) d\sigma_{el}/dt = \frac{4\pi^3}{k^2 s} \{ |A|^2 + |D|^2 \}$$

$$D/s < \infty$$

$$\bar{a} = a$$

$$T(s, t) = D(s, t) + i A(s, t)$$

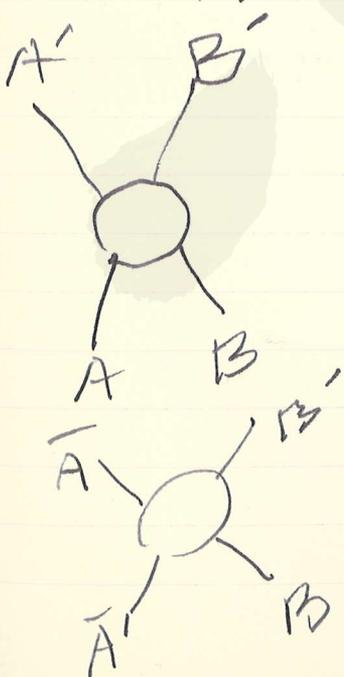
$$s = (p_A + p_B)^2$$

$$t = (p_A - p_B)^2 = (p_{A'} - p_{B'})^2$$

$$T(u, t) = \bar{D}(u, t) - i A(u, t)$$

$$u = (p_B - p_{A'})^2$$

$$\text{top } \left\{ \begin{array}{l} T \sim 1/2 \\ \bar{T} \sim 3/2 \end{array} \right.$$



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Blue Cyan Green Yellow Red Magenta White 3/Color Black

Exchange Contribution
van Hove, PL Oct. 15, 1963

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Blue

Cyan

Green

Yellow

Red

Magenta

White

3/Color

Black

© Kodak, 2007 TM: Kodak

世に於て : High Energy Collisions
of S I P (R. M. P. April 1969
L. van Hove 655)

Kodak Color Control Patches

Blue

Cyan

Green

Yellow

Red

Magenta

White

3/Color

Black

~~湯川~~ Symmetry Group

湯川
 Dec. 10
 1965

Salam: Theory of Groups and the
 Symmetry Physicist, July 1965

Jan. 1964

- | | |
|-----------------------|--------------------|
| 1) 8 particles | spin $\frac{1}{2}$ |
| 2) 9 particles | spin $\frac{3}{2}$ |
| 3) 8 ps-meson | spin 0 |
| 4) 9 meson
excited | spin 2 |

$2(\alpha = I_3) = Y$
 $I_3, Y \rightarrow \text{rank } 2. \rightarrow U_3$

Sept. 1964

N	$J = \frac{1}{2}$	$8 \times 2 = 16$	} 5 6
N*	$J = \frac{3}{2}$	$10 \times 4 = 40$	
M	$J = 0$	$8 \times 2 = 8$	} 3 5
M*	$J = 1$	$9 \times 3 = 27$	

$U(6)$

Dynamical Considerations and Non-Compact
 Group

i) $U(3)$ ii) $SL(2, C)$
 the subgroup $U(2, 1)$ group
 $SL(6, C) \supset U(6)$
 $U(12) \supset U(6) \times U(6)$
 $\tilde{U}(12) \supset SL(6, C)$

Kodak Color Control Patches

Red

Magenta

White

3/Color

Black

Dec. 18, 1965
 SU(6) model

1. mass formula
2. mag. mom. $F/D = -2/3$
3. ps-meson-baryon scattering
4. strong decay $\rho \rightarrow 2\pi$
5. ~~Weak~~ int.
 - a. leptonic decay
 - b. non-leptonic decay

Dec. 22, 1965

Hipkin, Meshkov, PRL. 19 April
 1965, Vol 14, No. 16, 670

W-spin, B-spin

SU(6)_W

$$W_i = \left\{ \frac{1}{2} \beta \sigma_1, \frac{1}{2} \beta \sigma_2, \frac{1}{2} \sigma_3 \right\}$$

$\Lambda_{34} \times$ commute

2. 8重の運動 W_3 対称性

B 8 $W = 1/2$

13^* 10 $W = 3/2$

$\left\{ \begin{array}{l} V_{\pm 1} \\ P_0 \end{array} \right. \quad W = 1 \quad W_3 = \pm 1$

$\left\{ \begin{array}{l} V_0 \\ P_0 \end{array} \right. \quad W = 1 \quad W_3 = 0$

$V_0 \quad W = 0 \quad W_3 = 0$

i) $\rho \rightarrow 2\pi$

ii) $N^* \rightarrow N + \pi$

iii)

最近の宇宙論

(天体物理学) Dec. 21, 1965
 林忠正印

1930 Expanding Universe
 ~ Hubble's law
 big bang theory

1940's Steady state universe
 ~ Bondi, Gold, Hoyle

Hubble's Law

$$\frac{\delta\lambda}{\lambda} = \frac{v}{c}$$

$$v = \frac{dl}{dt} = H_0 l$$

H_0 (in km/sec Mpc)

Mpc = 3×10^6 light year

1929

500

1936

550

1952

290

1958

75 ± 25

time-scale $\frac{1}{H_0} = 1.3 \times 10^9 \text{ y} \pm 30\%$

($\frac{\delta\lambda}{\lambda} < 0.1$ $l \ll R$)

initial matter density

1958 $\rho_0 \approx 1 \times 10^{-31} \text{ g/cm}^3$

1965: (17) Quasar (starlike) の

red shift

$$\frac{\delta\lambda}{\lambda} \approx 0.16 \sim 2.01$$

3C9

光線

Ly α

1217 \AA

$\rightarrow 3666 \text{ \AA}$

9113

CTV

$1550 \text{ \AA} \rightarrow 4668 \text{ \AA}$

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steady state = 定常状態...

(2) Quasar - stellar galaxy (blue stellar object)

距離 100 Mpc の 500 $\frac{1}{10}$
 $2 \times 10^5 \square$

$$\frac{\delta\lambda}{\lambda} = 0.09, 0.13, 1.24$$

(3) 電波の noise

100 cm 100 cm

$T_b = 3.5 \pm 1.0 \text{ }^\circ\text{K}$ black body radiation

(4) 銀河の 30% の He $\frac{4}{\text{He}}$

20% を 10% non-zero

質量比 $Y = 0.30$

宇宙初期 He の生成 $\sim Y \approx 0.30$

その変化 $\Delta Y = 0.02 \quad \Delta Z = 0.02$

初期 $Y = 0.30 \quad Z = 0.02$

$X = 0.68$

$X = 0.70 \quad Y = 0.30 \quad Z = 0$

(5) $\frac{1}{H_0}$
 $13 \times 10^9 \text{ y}$

平均の age

$25 \times 10^9 \text{ y}$ (Sandage 1958)

↓ stars

$U^{235} / U^{238}, U/Th$
 $(7 \sim 13) \times 10^9 \text{ y}$

- 共動座標系: co-moving coordinates

$$ds^2 = c^2 dt^2 - R^2(t) \{ dx^2 + \sigma^2(x) (d\theta^2 + \sin^2\theta d\phi^2) \}$$

$$\sigma(x) = \begin{cases} \sin x & (\text{closed, } k=+1) \\ x & (\text{flat } k=0) \\ \sinh x & (\text{open } k=-1) \end{cases}$$

$$\frac{\dot{R}^2}{R^2} + \frac{2\ddot{R}}{R} + \frac{8\pi G \rho}{c^2} = -\frac{k c^2}{R^2} + \Lambda c^2$$

$$\frac{\dot{R}^2}{R^2} - \frac{8\pi G \rho}{3} = -\frac{k c^2}{R^2} + \frac{\Lambda c^2}{3}$$

$$\frac{d}{dt}(\rho c^2 R^3) + p \frac{d}{dt} R^3 = 0$$

$$p < \rho c^2$$

$$H_0 = \dot{R}_0 / R_0$$

deceleration parameter q_0

$$q_0 = -\ddot{R}_0 / R_0 H_0^2 = -\ddot{R}_0 R_0 / \dot{R}_0^2$$

$$q_0 = \frac{4\pi G \rho_0}{3 H_0^2}$$

$$2q_0 - 1 = k c^2 / H_0^2 R_0^2$$

$$\frac{1}{2} > q_0 > 0$$

open

$$q_0 = \frac{1}{2}$$

flat

$$q_0 > \frac{1}{2}$$

closed

$$H_0 = 13 \times 10^9 \text{ yr}^{-1}$$

$$\rho_0 = 2.1 \times 10^{-29} q_0 \text{ g/cm}^3$$

$$(\rho_0 \approx 1 \times 10^{-31} \text{ g/cm}^3)$$

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Blue

Cyan

Green

Yellow

Red

Magenta

White

3/Color

Black

$$q_0 = 0 \sim 1$$

q_0	0	0.5	1.0
M_0 / L_0	1.00	0.667	0.571
$t_d(\log)$	13.0	8.7	7.4

redshift-magnitude relation

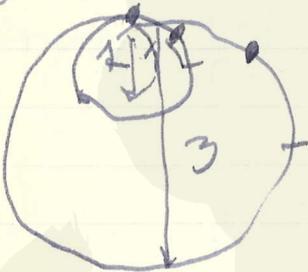
$$\begin{matrix} t_1 & \rightarrow & t_0 \\ R_1 & \rightarrow & R_0 \end{matrix}$$

$$1+z \equiv \frac{\lambda + \delta\lambda}{\lambda} = \frac{R_0}{R_1}$$

$$z \rightarrow \infty \quad \text{光の遅延}$$

$$3C9 \quad z = 2.01$$

$$q_0 = 1 \quad \sin \chi = \frac{z}{1+z}, \quad \chi = 42^\circ$$



count-magnitude relation

$$\text{@. S. G. (Sandage)} \quad q_0 = 0 \sim 1$$

観測される光の初期

$$P_0, T_0$$

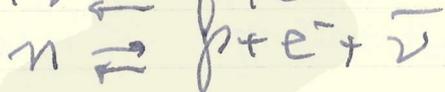
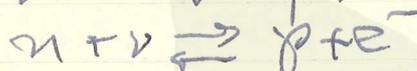
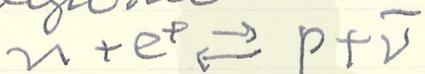
$$\frac{R}{R_0} = \sqrt{\frac{8\pi G P}{3} - \frac{H_0^2}{R_0^2}}$$

$$P_{\text{rad}} \gg P_{\text{mat.}} \quad (q > 0)$$

$$P = P_{\text{rad}} + P_{\text{el. pair}} + P_{\text{ne. pair}} + P_{\text{non-rel. pair}}$$

$$10^{12} \text{ K} > T > 10^9 \text{ K}$$

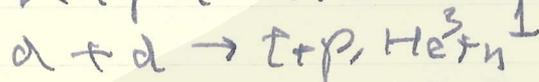
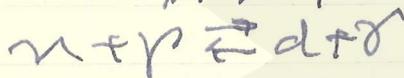
Mayardu



$$\#_n: p/n = 4 \quad n_p/n_n$$

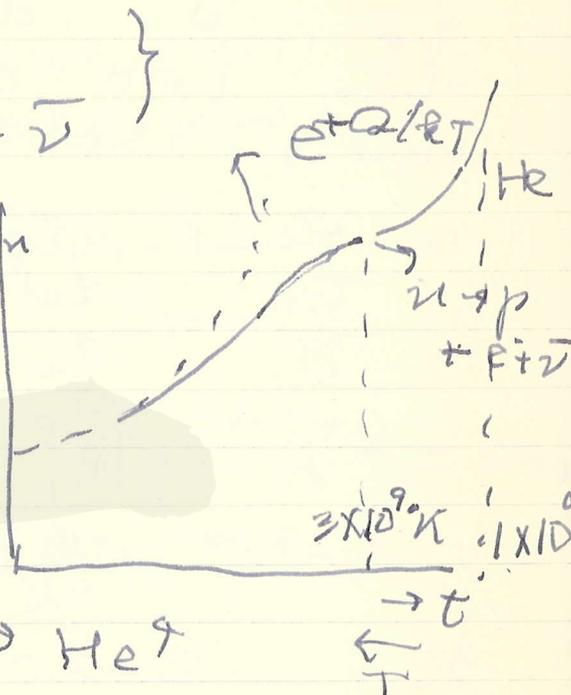
$$\#_p: p/n = 5.5 \sim 6.0$$

これより ρ_0

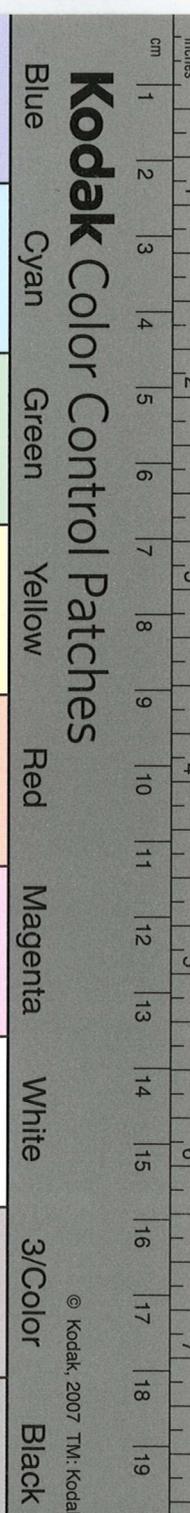


$$T_0 = 3.5 \times 10^9 \text{ K}$$

$$\rho_0 = 10^{-31} \sim 10^{-29} \text{ g/cc}$$



$$\frac{\text{He}}{\text{H}} = 0.062 \sim 0.11$$



~~4/2/65~~

Dec. 22 777

Harari, Lipkin
preprint, Trieste June 1965
(P.R.L. in press)

exp. test of Broken $O(12)$

$\gamma_0 p_0, \gamma_3 p_3$

$\lambda_j, \sigma_3 \lambda_j, \sigma_4 \sigma_1 \lambda_j, \sigma_4 \sigma_2 \lambda_j$ } $SU(6)_W$

$O(12)$ symmetry
Delburgo et al. (Trieste
Aug. 1965)

$$\begin{cases} \gamma_k^+ = -\gamma_k \\ \gamma_0^+ = \gamma_0 \end{cases}$$

$$\begin{aligned} \gamma_5^2 &= -1 \\ \gamma_5^+ &= -\gamma_5 \end{aligned}$$

$U(6) \times U(6)$

$B = (56, 1)^+$

$M = (6, 6)^- = 35 + 1$ \rightarrow 950 MeV