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京都大学基礎物理学研究所 湯川記念館史料室

c033-832~853換込

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N97

XXVI

NOTE BOOK

*Manufactured with best ruled foolscap  
Brings easier & cleaner writing*

Sept. 1969  
~ March, 1970

VOL. XXVI

M. Yukawa

50

97 *Rissho Note*

BOX35

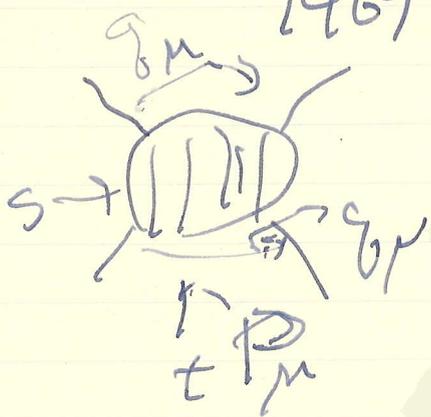




Veneziano's  $\pi$ -Nucleon  $\pi$

1967年

9月19日 (土) 湯川



$O(3, 1)$

$\pi, \ell, m$

$\left\{ \begin{array}{l} n \text{ integer} \\ p \text{ (Gaussian } q \cdot v \cdot z, \text{ etc.)} \\ \Delta: \text{ pointlike} \end{array} \right.$

$$f(s, t, u) = A(s, t) + \sum_{\text{cyclic}}$$

$$A(t, s) = g^2 \frac{\Gamma(1 - \alpha(t)) \Gamma(1 - \alpha(s))}{\Gamma(1 - \alpha(s) - \alpha(t))}$$

$$t = P_\mu^2$$

$$s = (q - q')_\mu^2$$

$$u = (q + q')_\mu^2$$

$$P_\mu^2, q_\mu, q'_\mu, q_\mu q'_\mu$$

$$P q \cdot x, P q' \cdot x$$

$P_\ell(\cos \theta) \rightarrow (\pi(q_\mu, q'_\mu))$   
 gegenüber

$$\sqrt{\frac{A(q,t)}{g^2}} = (-a(t)) \sum_{m=0}^{\infty} \frac{\Gamma(a(t)+m+1)}{\Gamma(m+1) \Gamma(a(t)+1)} \frac{1}{z_t^{a+m}} \frac{\delta t^m}{\delta}$$

$$z_t = \tilde{q}_\mu \tilde{q}_\mu$$

$$\gamma = 2a(q_\mu^2) (q_\mu^2)$$

$$\delta = 1 - b - a(q_\mu^2 + q_\mu'^2)$$

$$a(t) = at + b$$

$$A(t, \sigma) = \int_0^\infty dx A^s(x, t) C_{x-1}^1(z_t) / \Gamma(x) x$$

$$z^{-a} = \frac{1}{\Gamma(a)} \int_0^\infty e^{-zp} p^{a-1} dp$$

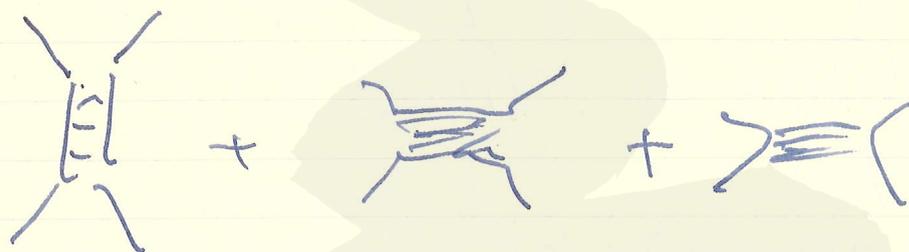
$$A^s(x, t) = g^2 \int$$

~~bilocal~~ bilocal  
 p-magnets

$$W(g, \kappa) = \sqrt{2\pi} g \left( \sum_{\kappa=1}^{\infty} \sum_{l=0}^{\kappa-1} \sum_{m=0}^{\kappa-l} \right) \left( \sum_{n=0}^{\infty} \int_0^\infty dp \right)$$

$$\times \int d^d p e^{i p_\mu x_\mu}$$

$$= \sqrt{2\pi g} \int d^4x_1 d^4x_2 \delta^4(x - \frac{x_1 + x_2}{2}) \\ \Pi(x_1) \Pi(x_2) \rho(x, x_1 - x_2)$$

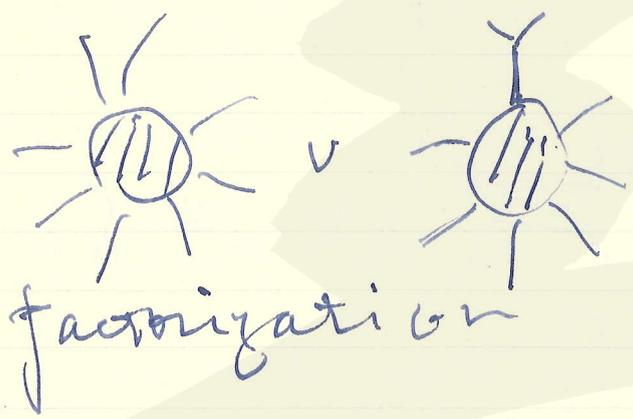


$$\frac{1}{2} A(\tau, \eta) \\ + \frac{1}{2} A(\tau, \eta)$$

# Quark Model and Factorization of Veneziano Amplitude

Y. Nambu

河原 裕之 氏 発行 Sept. 30, 1969



$V_4 = \sum_n \frac{C_n(t)}{s - m_n^2}$

$\sum_n$  } 1) mass spectrum  
 } 2) coupling constant

infinite component equation  $\rightarrow$

tree diagram

$$V_N = \int_0^1 x^{(12)} y^{(123)} z^{(1234)} \dots w^{(n-1, n)}$$

$$\times \left[ \frac{1-x}{1-xy} \right]^{(23)} \left[ \frac{(1-y)(1-xyz)}{(1-xy)(1-yz)} \right]^{(34)}$$

analogy  $\int_0^1 x^2 y^3 = \int_0^1 x^2 y^3 dx dy \dots dw$

$$\int \frac{dx dy \dots dw}{(1-xy)(1-yz) \dots}$$

$$\{a_\alpha^{(r)}, a_\beta^{(s)\dagger}\} = -\delta_{rs} g_{\alpha\beta}$$

$$\alpha, \beta = \dots + -$$

$$r, s = 1, 2, \dots, \infty$$

$$e^A e^B = e^B e^A e^{[A, B]}$$

$[A, B]$ : c-number

$$H = -\sum_r r a_\alpha^{(r)\dagger} a_\alpha^{(r)}$$

$$\langle N | \Sigma | 0 \rangle = \langle N | e^{i \sum_r \sqrt{\frac{r}{2}} a_\alpha^{(r)\dagger} \pi} | 0 \rangle$$

$$N = -\sum_{r, \alpha} r a_\alpha^{(r)\dagger} a_\alpha^{(r)}$$

$$\langle N' | \Sigma | N \rangle = \dots$$

$$V_W = \langle 0 | \Sigma(p_n) \frac{1}{H - \alpha_{n-1}} \Sigma(p_{n-1}) \frac{1}{H - \alpha_{n-2}}$$

$$\dots \Sigma(p_2) \frac{1}{H - \alpha_1} \Sigma(p_1) | 0 \rangle$$

$$\phi_\alpha(z) = \sum_{r=1}^{\infty} \sqrt{\frac{r}{2r}} \{ a_\alpha^{(r')} + a_\alpha^{(r)\dagger} \} \cos rz$$

$$\pi_\alpha(z) = \sum \dots$$

$0 \leq z \leq 2\pi$

$$H = -\frac{1}{\pi} \int_0^{2\pi} i \psi \partial_z \phi \partial_{\bar{z}} \psi + \pi [\psi] \psi \bar{\psi} dz$$

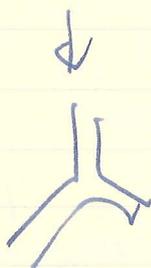
$$(\square - H) \Psi(X, \phi(z)) = 0$$

$$\Psi^\dagger \Sigma \Psi \phi$$

$$\Sigma = i \exp[2i\kappa\phi(0)]$$

$$\int \mu \cdot \phi(x)$$

$$\phi(x, y)$$



quark =  $q \gamma_0 \tilde{z}$  ( $q, \tilde{q}, \tilde{p}$ )

$$H = a^{\dagger 0} a^0 + \sum_{\mu=1,4}^n n a_{\mu}^{\dagger} a_{\mu}$$

$a^{\dagger 0}$ : radial excitation  
 $n=1$ :  $a_{\mu}^{\dagger}$  l-excitation  
 $n \geq 2$ :  $(q\tilde{q})$  excitation  
 $3S, 3P_0$

$i q \gamma_5$   
 $a_0 \gamma_5$   
 $a_m \gamma_5$   
 $a_m \gamma_5$   
 $n \geq 2$

$(\bar{q} q)$  excitation  $(\bar{q} \gamma_5 q)$   
 $(\bar{q} \gamma_5 q)$   
 $(\bar{q} \gamma_5 q)(\bar{q} q)^n$

湯川 研  
 Self-Energy の計算

~~Oct. 21~~ 湯川 研  
 淡路. He  
 13044 10

Oct. 21, 1969  
~~1969~~

Yukawa coupling

$$H = \int d^3x \left[ (\pi^* \pi + \nabla \phi^* \nabla \phi + M^2 \phi^* \phi) \right.$$

$$\left. + \frac{1}{2} (E^2 + (\nabla A)^2 + m^2 A^2) + g A \phi^* \phi \right]$$

$$= \sum_{\mathbf{k}} \Omega_{\mathbf{k}} (a_{\mathbf{k}}^* c_{\mathbf{k}} + b_{\mathbf{k}}^* b_{\mathbf{k}}) + \sum_{\mathbf{k}} \omega_{\mathbf{k}} a_{\mathbf{k}}^* a_{\mathbf{k}}$$

+ H<sub>I</sub>

$$H_I = \frac{g}{\sqrt{V}} \sum_{\mathbf{p}, \mathbf{q}} \frac{1}{\sqrt{2^3 \Omega_{\mathbf{p}} \Omega_{\mathbf{q}} \Omega_{\mathbf{p}+\mathbf{q}}}} \phi_{\mathbf{p}}^* \phi_{\mathbf{q}} A_{\mathbf{p}+\mathbf{q}}$$

$$\phi_{\mathbf{k}} = c_{\mathbf{k}} + b_{-\mathbf{k}}^*$$

$$\Omega_{\mathbf{k}} = \sqrt{k^2 + M^2}$$

$$A_{\mathbf{k}} = \alpha_{\mathbf{k}} + \alpha_{-\mathbf{k}}^*$$

$$\omega_{\mathbf{k}} = \sqrt{k^2 + m^2}$$

$$H|0\rangle = E_0|0\rangle$$

$$H_0|0\rangle = E_0|0\rangle$$

$$H|\mathbf{k}\rangle = (E_0 + \omega_{\mathbf{k}})|\mathbf{k}\rangle$$

$$H_0|\mathbf{k}\rangle = (E_0 + \Omega_{\mathbf{k}})|\mathbf{k}\rangle$$

$$\Delta E_R = \epsilon_R - E_R^F$$

$$E_R^F = \langle 0 | \psi_R \psi_R^\dagger | 0 \rangle$$

$$(H - \epsilon_0 - E_R^F) \psi_R = \Delta E_R \psi_R$$

$$\psi_R = \psi_R^\dagger | 0 \rangle + \sum_l c_{l,R} A_l^\dagger \psi_{l-R}^\dagger | 0 \rangle$$

Heitler's damping theory  
 lowest non-vanishing  $\alpha$  matrix  
 element  $\sim \eta \psi_R^\dagger$

$$\mathcal{J}_S A_R \mathcal{J}_S^\dagger = b_R$$

$$\mathcal{J}_S \psi_R \mathcal{J}_S^\dagger = \psi_R$$

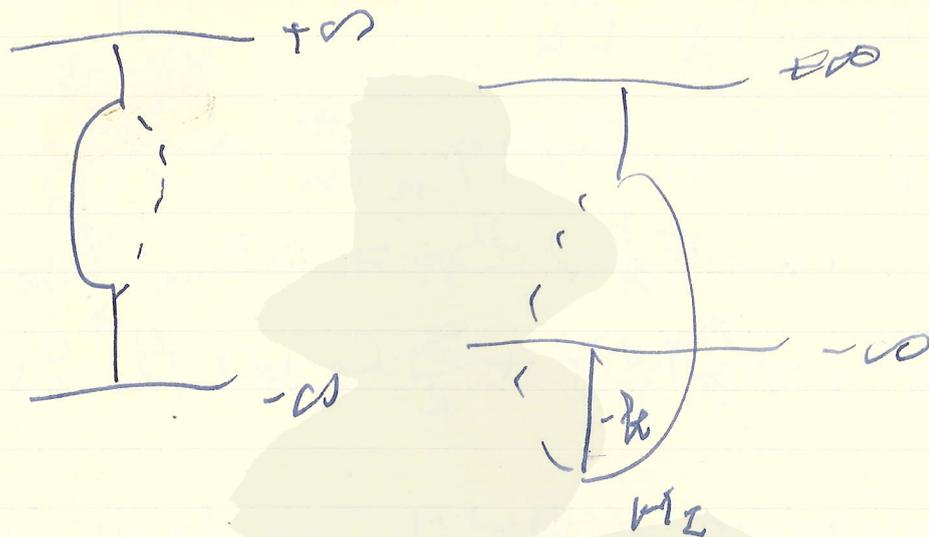
$$\Delta E_R = - \sum_l \frac{|\langle 0 | \psi_{l-R} A_l (H - \epsilon_0 - \Omega_R) \psi_R^\dagger | 0 \rangle|^2}{\Omega_{l-R} + \omega_l - \Omega_R}$$

true vacuum is  $\psi_R^\dagger$ ?

$$| 0 \rangle = | 0 \rangle + \frac{1}{E_0 - H_0} H_I | 0 \rangle + \dots$$

$$\Delta E_R = \frac{g}{\sqrt{2} \omega_l \Omega_{l-R} \Omega_R} \left( \frac{2 \Omega_R}{\Omega_{l-R} + \omega_l + \Omega_R} \right)$$

↓ damping factor



# 標型と構造研究記

梶研 Oct. 23, 1969  
 ~25

宇野

- 大場氏:
- SU(6) → static fields
- i) Lorentz pole  
 pole  $\neq 0$  of  $\frac{\partial}{\partial x^\mu} \left( \frac{\partial}{\partial x^\nu} \right) \phi$   
 $\mu \neq \nu \Rightarrow \gamma^\mu \gamma^\nu \phi$   
 $\mu = \nu \Rightarrow \gamma^\mu \gamma^\mu \phi$
  - ii) chiral invariance  
 Goldstone boson

B.S. amplitude

$$\chi_{\alpha\beta}(P, q) = \gamma_\alpha (A + (q \cdot P) \gamma_5) \gamma_\beta + C \not{q} + D(\not{q} \not{P} + \not{P} \not{q})$$

$$P^2 = -m_\pi^2$$

$$A, B, C, D = f_\pi((q^2)^2, q^2)$$

$$\chi = \begin{pmatrix} \chi_{++} & \chi_{+-} \\ \chi_{-+} & \chi_{--} \end{pmatrix}$$

$\beta \equiv \gamma_4$  diagonal es  
表示.

(i)  $|q| \ll M$

(ii)  $|\chi_{++}| \gg |\chi_{+-}|, |\chi_{-+}|, |\chi_{--}|$  } weak binding

rest system

$$\chi_{\pm\pm} = A \pm \mu_\pi (B q_0^2 + C)$$

$$\chi_{\pm\mp} = (D q_0) (\pm \mu_\pi D \pm B q_0 \mu_\pi)$$

$m_\pi = 0: \chi_{\pm\mp} \rightarrow 0 \quad \chi_{++} = \chi_{--}$   
 $\chi_{\alpha\beta} \rightarrow \delta_{\alpha\beta} A$

$$\chi_{++}^{\pi} - \chi_{--}^{\pi} = O(\mu_{\pi}) \quad (= C \mu_{\pi})$$

$$\chi_{++}^{\kappa} - \chi_{--}^{\kappa} = O(\mu_{\kappa}) \quad (= C \mu_{\kappa})$$

$$\langle 0 | A_{\mu}(0) | \pi \rangle = f_{\pi} \cos \theta \frac{P_{\mu}^{\pi}}{2}$$

$$\langle 0 | A_{\mu}(0) | \kappa \rangle = f_{\kappa} \sin \theta \frac{P_{\mu}^{\kappa}}{2}$$

chiral PS  $f_{\pi} \approx f_{\kappa}$   $SU(6)$   
 PS,  $V$

$$V = \begin{pmatrix} 0 & 1/\sqrt{2} \\ 1/\sqrt{2} & 0 \end{pmatrix}$$

weak binding  $\rightarrow$  弱結合  $\rightarrow$   $Z$  (SU)

strong binding

Dirac の  $\mathbb{Z}_2$  の  $\pi$  の

line is symmetrize  $\mathbb{Z}_2$

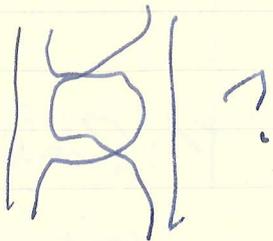
$\uparrow\uparrow$   
 $\chi_{\pi\alpha}$

$\uparrow\uparrow\uparrow$   
 $\chi_{\alpha, \alpha, \alpha}$

line is unitary  
 spin  $\alpha \in \mathbb{Z}_2$  の  
 Dirac  $\alpha$  sufficient  $\mathbb{Z}_2$

on shell ( $\chi$  etc) of  $\omega$   $\tau = \eta$   
 $(\sigma_m^{\dagger} \sigma_n + m) \chi \dots = 0$   
up-down  $\tau = \eta$   $\tau = \eta$

Iizuka rule of  $\chi$  etc?  $\tau = \eta$   
disconnected graph  
is  $\chi$  etc...



Hori  
three triplet model

exotic resonance  $\chi$  etc?

Smith  $\omega$   $\Sigma$   $\Sigma$  1

宇野 = 河原正樹  
 北河. 系統 T.R.E.

Veneziano model  
 i) Finite Energy Sum Rule (FESR)  
 Freund Mandelstam

$$T(s, t, \dots) = T_{\text{diff.}} + T_{\text{non-diff.}}$$

$$\int_0^N ds \text{ Im } T_{\text{non-diff.}}(s, t) ds$$

$$\approx \sum_{i \neq P} N^{\alpha_i(t)} \beta_i(t) \quad P: \text{Pomeron}$$

$$\int_0^N ds \text{ Im } T_{\text{diff.}}(s, t) ds \approx N^{\alpha_P(t)} \beta_P(t)$$

ii) Narrow Resonance Saturation  
 for non-diff. part of T

iii) Non-exotic resonance

Veneziano test (i) (ii) (iii) (iv)

A) Application

i) meson systems

a generalized exchange degeneracy

$$\left. \begin{aligned} \alpha_p &= \alpha_f ; \beta_p = \beta_f \\ &= \alpha_w = \alpha_{A_2} ; \beta_w = \beta_{A_2} \end{aligned} \right\} \leftrightarrow \begin{matrix} m_{\pi^+}^2, m_{\pi^0}^2 \\ m_f^2, m_{A_2}^2 \end{matrix}$$

1, 2<sup>T</sup> Nonet scheme  
 Okubo, Suzuki

$\rho$  chiral dynamics & consistent  
 $\rho$   $\rho$ -universality  $\leftrightarrow$  trajectory  
 a derivative of universality

$$SU(6) \otimes O(3)$$

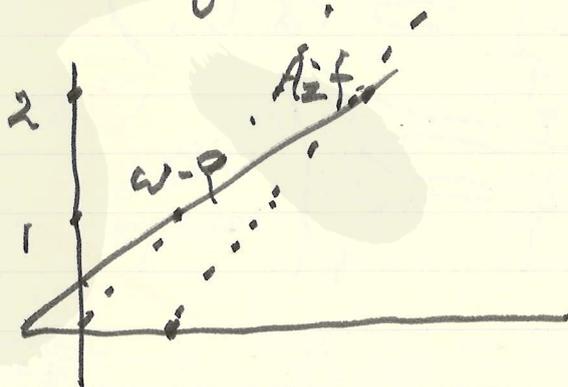
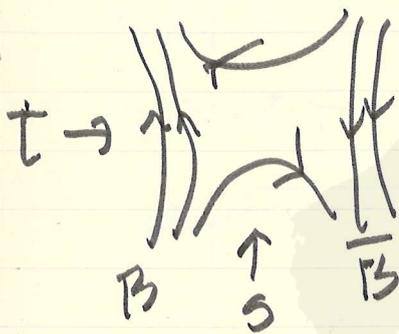
ii) meson + baryon

Zweig  
 baryon spectrum  $SU(6) \otimes O(3)$

$\Sigma - \Lambda$  f-type  
 duality breaking (ii) & (i) の結合

iii) baryon-antibaryon  
 no solution

K. K. Y. (exotic resonance  $\pi \lambda \Lambda \Sigma$  の  
 結合 ... の duality の破れ)



B) Formulations

- i) IV 條の Veneziano formula
- ii) unitarity (higher order correction)

→ level structure of degeneracy

$$N_E \sim e^E$$

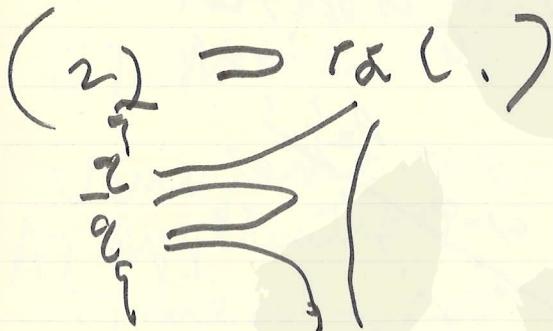
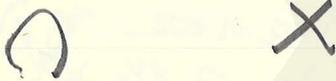
ghost state e.s. c.c.

(chiral invariance)

c) Selection rule based on duality

Franks, Ramer, Wally

1)  $\gamma$  vertex of a pair  $\psi \bar{\psi} c$   
 $\psi \bar{\psi} \rightarrow$  quark line  $\psi \bar{\psi} \psi \bar{\psi}$



composite particle  
 a  $\psi \bar{\psi} c$

Oct. 24

以前 後藤氏の  $U(6)$  model  
 three quark model  
 quark model  $\rightarrow$

$\Psi_{\alpha} = \begin{pmatrix} \psi_{\alpha}^{(1)} \\ \psi_{\alpha}^{(2)} \end{pmatrix} \rightarrow a, a^{\dagger}$   
 6 種の oscillator  
 の系 (図)

今、この系  
 について

$(0, 4, \phi) \rightarrow 2\text{-comp. spinor}$

$(a, a^{\dagger}) \rightarrow 4$  種の oscillator

物理的理論の unique  $T$  である。  
 (意味: Lorentz 群の unitary 表現と nonunitary 表現の区別)  
 abstraction

(基底):

(Isart?)  $SO(4, 2) \rightarrow (a_i, a_i^{\dagger})$   
 physical is  $SO(3, 1)$  spinor  $(b_{\frac{1}{2}}, b_{\frac{1}{2}}^{\dagger})$   
 4 x 4 方

湯川氏  
 unit. def.  $\rightarrow$  discrete の基底 (??)  
 (???)  $\rightarrow$  (???)  
 unit def. configuration space  $\tau$  の基底

$$[C^{(a)}, C^{(j)}] = \epsilon_{\alpha\beta} g^{ij}$$

$i, j = 1, 2, 3$

$$\epsilon_{\alpha\beta} = \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$$

9.1.13

$$SL(2, \mathbb{C})$$

$$SO(3, \mathbb{C}) \rightarrow SO(3, 1) \otimes SO(3, 1)$$

10.2.11

$$L = \frac{1}{2} \omega^2$$

$$\vec{\omega} \rightarrow \frac{d\vec{x}}{dt} \rightarrow dc$$

$$[(P_\mu)^2 - \frac{1}{2} T^2] u = 0$$

i)  $dc^2 = dx_\mu dx_\mu$

ii)  $dc = \frac{p_\mu dx^\mu}{p_\mu^2}$

body frame  
 in rotation

$$[P^\mu P_\mu - \kappa] u = 0$$

majorana

$$m = \frac{\kappa_0}{J + \frac{1}{2}}$$

$$[P_\mu^2 - \kappa P_\mu P^\mu] u = 0$$

$$m = \kappa_0 (J + \frac{1}{2})$$

negative energy state w/

11: daughter trajectory  
 mass spectrum  
 infinite comp. & unitarity

see the difference  
 eq?

$$(\Gamma_\mu \alpha_\mu - \kappa \alpha_\mu \Sigma^\mu) u = 0$$

$$(4\text{p. 1st} : m^2 = \kappa_0 [5 + \frac{1}{2}])$$

three spinors  
 $\vec{u}^{(i)}(\vec{x})$



2nd 2nd of 1st of 3rd of 3rd of 3rd

infinite component  
 rest frame

$$\vec{S} = \frac{1}{2} a^* \vec{\sigma} a$$

$$R_3 = \frac{1}{2} (a_1 a_2 - a_1^* a_2^*) \quad (\text{helicity})$$

$$e^{\frac{i\omega}{2} (a_1 a_2 - a_1^* a_2^*)} |n_1, n_2, 0\rangle_{\text{rest}}$$

$$= |0; \omega\rangle$$

$$|0; \omega\rangle = \frac{1}{\text{ch} \frac{\omega}{2}} e^{a_1^* a_2^* \tanh \frac{\omega}{2}} |0; 0\rangle$$

$\omega$   
 $0$

$$|s_1, s_2; \omega\rangle = \frac{1}{(\text{ch} \frac{\omega}{2})^{2s+1}} \frac{1}{\sqrt{(s_1+s_2)! (s_1-s_2)!}} e^{a_1^* a_2^* \tanh \frac{\omega}{2}} (a_1^*)^{s_1+s_2} (a_2^*)^{s_1-s_2} |0; 0\rangle$$

$$(P_\mu^2 - \kappa P_\mu P^\mu) u = 0$$

$$P_2 \neq 0$$

$$m \equiv m(\kappa) \rightarrow J = J(m)$$

$m$ : time-like

$\rightarrow$  space-like

space-like solution

Ex. 6: Veneziano & extended model  
 Narukou

1976

factorization



is  $\mathbb{R}^4$  の harmonic oscillator

$$H = \sum_{n=1}^{\infty} n a^{(n)\dagger} a^{(n)}$$

$\rightarrow$  Narukou

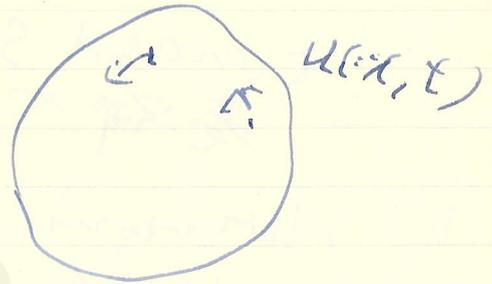
level density  $\rho(E)$

$$H = \sum_{(n_1) \dots (n_d)} \sum_{n=1}^{\infty} n a^{(n_1, \dots, n_d)\dagger} a^{(n_1, \dots, n_d)}$$

$\rightarrow$  deformable body

予備的

$H \sim \int d^3x \mathcal{L}(u, \partial_\mu u)$   
 $\mathcal{L}(u, \partial_\mu u)$



vertex

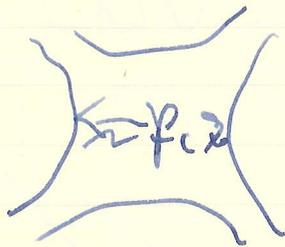
$V \approx \phi(0)$   
 boundary condition  
 湯川: 統計

田中: 構造力学

$SU(3) SU(6) \times O(3)$   
 Regge

duality

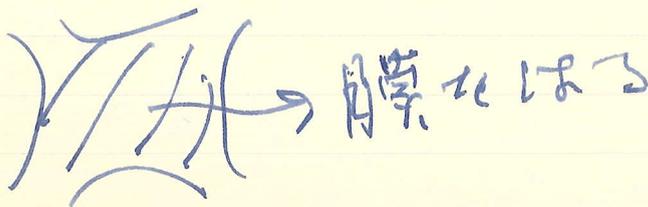
reciprocity of  $\alpha \leftrightarrow \alpha'$



$$e^{apq^2} \rightarrow e^{-\frac{\gamma \mu^3}{ap}}$$

$p \rightarrow 0$ : pole contrib.

oscillator model  $\times$   $\sigma$   $|z|$   $\sigma$   
 Narain  $\psi(x, r(u))$   $u: (0, U)$   
 Dasgupta



北内新研

Leonard Susskind の 8h 5  
 基礎 Nov, 4, 1969

1) Harmonic Oscill. Analogy  
 for  $V, M,$

$$\begin{array}{l} \uparrow \downarrow \\ (\Box_1 + M^2) (\Box_2 + M^2) \psi(x_1, x_2) \\ + U(x_1, x_2) \psi(x_1, x_2) = 0 \\ M^2 \rightarrow \infty \quad \chi = \frac{1}{2}(x_1 + x_2) \end{array}$$

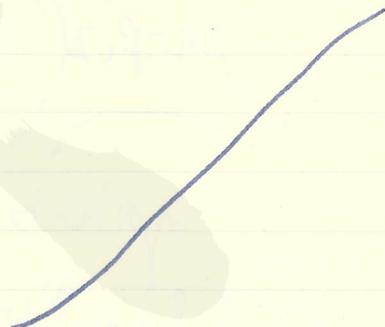
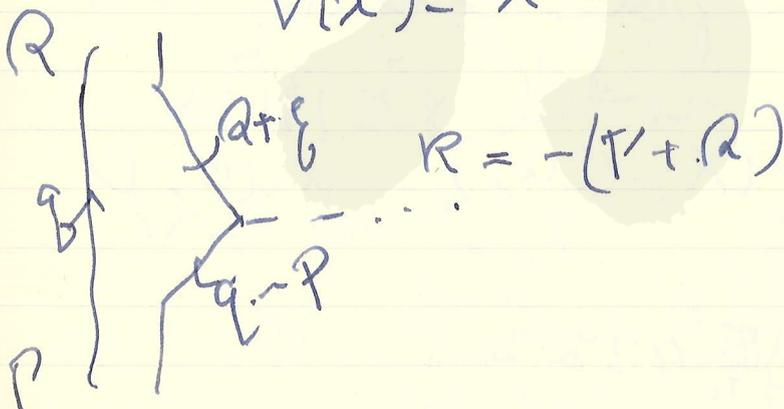
$$x = x_1 - x_2$$

$$\left[ \frac{\Box_x}{2} + 2\Box_x + V(x) \right] \psi(x, \chi) = 0$$

$$\lim_{M^2 \rightarrow \infty} \frac{M^4 + U}{M^2} = V(x)$$

$$(-\nabla + \frac{V}{2}) \psi = \frac{P^2}{4} \psi$$

$$V(x) = x^2$$



$$\frac{0 \quad n \quad 0}{\vdots \quad \vdots \quad \vdots}$$

$$\Gamma = \int x^{-p^2} (e^{-x})^{-\frac{t_{12}}{2}} dx$$

$$\frac{1}{p^2 - n} = \int x^{-p^2 + n - 1} dx$$

$$e^{-x} \rightarrow 1 - x = e^{\ln(1-x)}$$

$$= e^{-\sum_j \frac{x^j}{j}}$$

2) structure of hadrons implied by duality

$m \rightarrow n$

$$\langle n | e^{a^\dagger k} e^{-a k} | m \rangle =$$

Nambu

$$T(k_1, k_2) = \langle 0 | T(k_1) | n \rangle$$

$$\times \frac{1}{s - \sum n - c} \langle n | T(k_2) | 0 \rangle$$

$$x \rightarrow \sum g_i x^i$$

$$a_\mu^\dagger, a_\mu \rightarrow a_{\mu}^{i\dagger}, a_{\mu}^i$$

$$\langle n_\mu^i | e^{A_\mu^\dagger k_\mu} e^{-A_\mu k_\mu} | m_\mu^i \rangle$$

$$A_\mu = \sum g_i a_{\mu}^i$$

$$\Rightarrow \int x^{-s+c-1} [e^{-\sum g_i x^i}]^{-t_{12} + 2M^2}$$

$$\sum g_i^2 x^i = \sum \frac{x^i}{i} = \ln(1-x)$$

3) Phys. Interpretation of Duality

$$\int_{u=0}^{u=\pi} \frac{x(u)}{i}$$

M. Kommu and M. Nakagawa  
Universal V-A Interaction  
with CP Violation  
普遍・対称性

Nov. 11, 1969

current-current  
 $V - e^{i\phi} A$

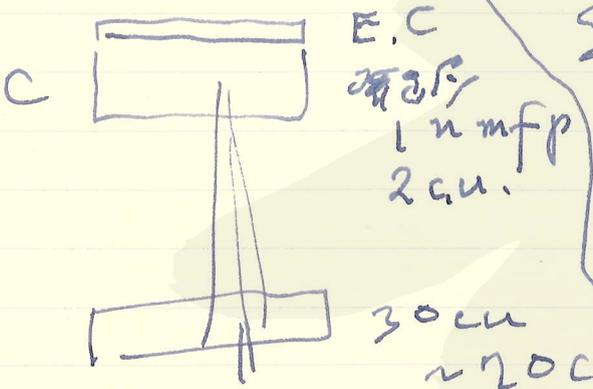
( charged current  
neutral current

火の玉 研究会 1969  
12月1日 ~ 4日

第3日 12月3日

お昼の後の一 ;  $\Sigma E_{\gamma} = 12 \times 9$  の話  
4ヶ所に分布

ch. 12 (1965) 2ヶ所  
ch. 13  
ch. 14 48m<sup>2</sup> Clean Air Jet  
ch. 15 (1969) 4ヶ所  
機流室  
機流室  
= 2ヶ所 4ヶ所



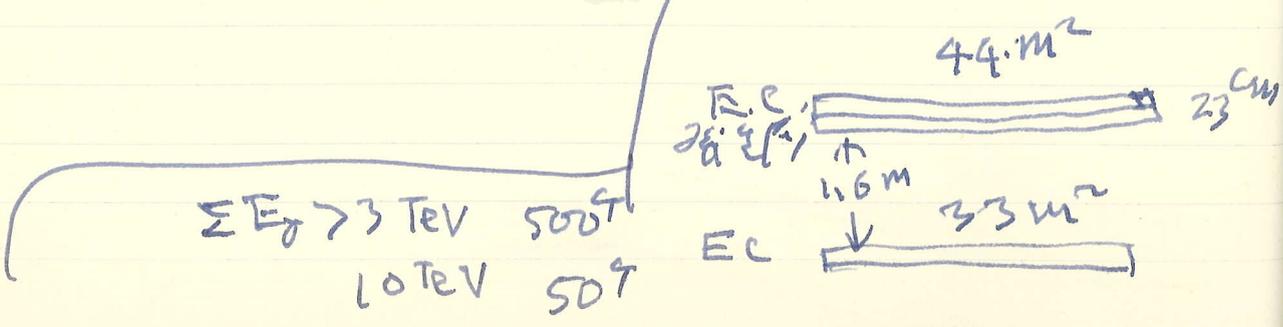
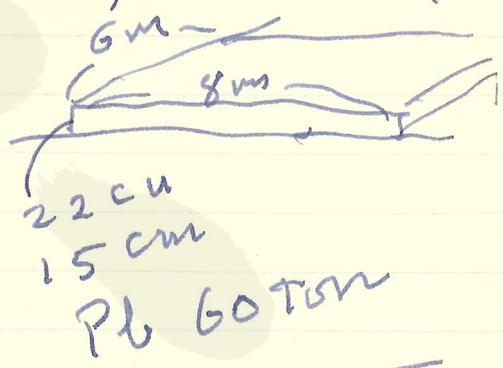
$\Sigma E_{\gamma} \approx 3 \times 10^{12} \text{ eV}$

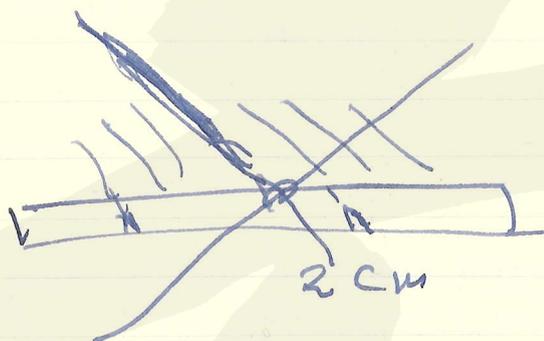
90%

粒子の H. 2.6 GeV

粒子の  $\gamma$  : (5 ~ 7) MeV  
SH.

$\Sigma E_{\gamma}$  20 ~ 100 TeV  
SH 2ヶ所  
EAS 粒子の  $\gamma$   $\approx 10^{16}$   
粒子の  $\gamma$   $\approx 10^{15}$   
粒子の  $\gamma$   $\approx 10^{15}$





Andromeda 一見貴粒子

Magalhães  $10^{15} \text{ eV}$

$E_{\gamma} > 1 \text{ TeV}$  2359  
 $\Sigma E_{\gamma} = 555 \text{ TeV}$

$E_{\gamma} \geq 0.5 \text{ TeV}$  +) 1019

$\Sigma E_{\gamma}$  +) 71 TeV

$E_{\text{ph}} > 1 \text{ TeV}$  209

$\Sigma E_{\gamma}$  +) 60 TeV



真空中の電子の遷移

1. 真空中の電子のエネルギー  
 $E_0 \approx 3 \times 10^5 \text{ eV}$
2. 遷移の transition の max.  $\gamma$  c.u. ( $10^{10} \text{ eV}$ )
3. 粒子の  $\beta$  の値
4.  $e^{-\gamma}$   $\beta = 0.5 \text{ cm}$

Mag.

$\beta = 0.2 \sim 0.3 \text{ cm}$   
 high energy  $\gamma$  balance background

真空中:  $10^{12} \text{ eV}$

$3 \times 10^4 \text{ g}$

U 300 y

1.2 cm

E $\gamma$

真空中  $10^{15} \text{ g}$  ) X  
 $10 \text{ cm}$

$3 \times 10^{15}$   $10^{16} \text{ g}$  ) X  
 $8 \text{ cm}$

$3 \times 10^{14}$   $10^{17} \text{ g}$  ) O  
 $6 \text{ cm}$

UH 1000 eV

$\gamma$  T

300 MeV

乗数  $\mu$ :

Multiplicity versus energy  
 $10^{10} \sim 10^{11}$  eV  $N=10$  one fire  
 $10^{11} \sim 10^{14}$  eV  $N=10$  one fire  
 (10 =  $\sqrt{N} \times 2$ )  
 two fire  
 three fire  
 four fire

1/2  $\alpha E \rightarrow H$  quantum

1°  $\beta$  isotropic

2° main  $\beta E = 1.35 \rightarrow \beta E = 2.65 \text{ GeV}$   
 $\beta E \quad 2 \sim 3 \text{ GeV mN}$

3°  $\beta E \sim m\pi$   $p \cdot e^{-p/\beta} \sim e^{-E/\beta}$

$10^{14} \sim$

S.H. quantum

$$\beta E = 5 \sim 10 \beta E_H$$

$$\beta E \approx 3 m\pi$$

$$N \sim 3 N_H$$

S.H.  $\rightarrow H \rightarrow \pi$

U.H. ( $\beta E \sim 100 mN$ )

1) Resonance  $\times$   $\beta E$  の関数

1°  $\beta E$  の関数

2° cut-off  $e^{-p/\beta}$  (Wataghi)

宇宙線のエネルギー (hatter)

3° NN

2) 1/2 の Z の dynamics

$$\begin{cases} \Delta \sim \text{MN} (1/2) \text{MN} \\ \text{MN} \sim 3 \text{MN} \end{cases}$$

縦 } 横 }  
 空 } 逆 }

duality ?

$$E_0 \rightarrow E_1 + E_2$$

$$P_0 \rightarrow P_1 + P_2$$

3) 逆未結

H 粒子の存在層

multiperipheral = 逆未結  
 (P1, P2)



その過程 multiplicity 6 (2' 4')

4) 増幅

$$H \rightarrow SH \rightarrow UH \dots EAS$$

H 粒子の 2 fire

第4回 QED 基礎  
 Parton Model 1 Dec. 9, 1969

Feynman

e-p inelastic scattering



lab. 5 GeV ~ 20 GeV  
 Mark II 40 GeV

Kinematics

$$s = (p + p')^2 \quad t = (l - l')^2$$

$$w = \sqrt{p'^2}$$

$$s \approx m(m + l_0)$$

$$t \approx -4l_0 l'_0 \sin^2 \frac{\theta}{2}$$

$$w = m^2 + 2m(l_0 - l'_0) + t$$

$$\frac{d\sigma}{d\Omega dl'_0} = \frac{e^2}{4k^4} \frac{w'}{|p|} \phi^{\mu\nu} A_{\beta\gamma} T_{\mu\nu}$$

$$k = l - l'$$

$$K = l + l'$$

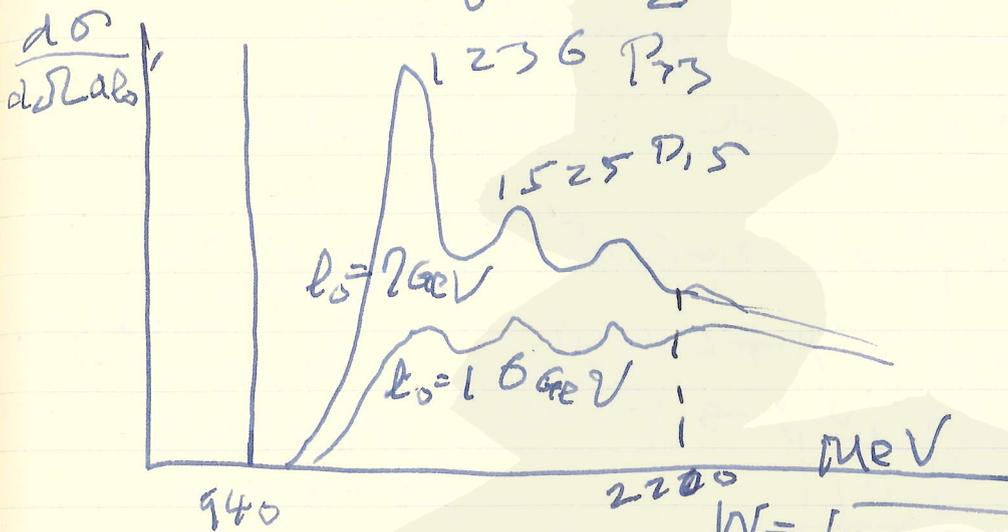
$$\phi^{\mu\nu} = \frac{1}{4} (\not{K} \not{K} - k^\mu k^\nu + \pi^2 g^{\mu\nu})$$

$$g^{\mu\nu} = (1, -1, -1, -1)$$

$$\text{dir } T_{\mu\nu} = (2\pi)^3 \pi \sum \delta(p_\mu - p - k)$$

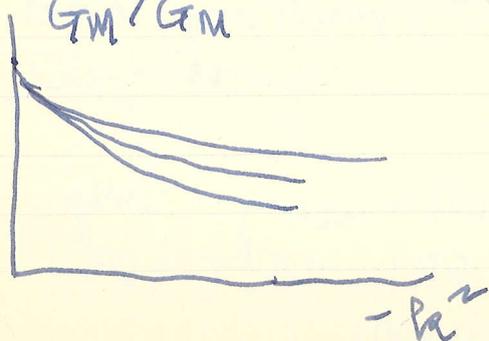
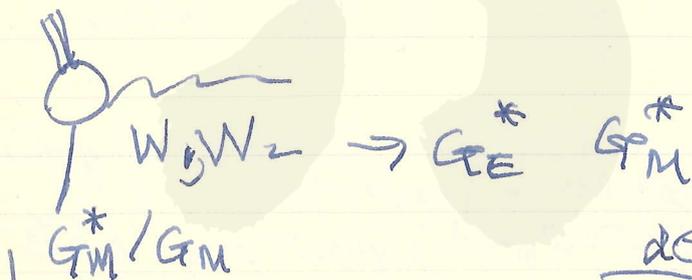
$$\times \sum_s \langle N_{ps} | j_\mu | n \rangle \langle n | j_\nu | N_{ps} \rangle$$

$$\frac{d\sigma}{d\Omega d\alpha d\beta} = \frac{\alpha^2 \cos^2 \theta}{4l_0 \sin^2 \frac{\theta}{2}} (2W_1 \tan^2 \frac{\theta}{2} + W_2)$$



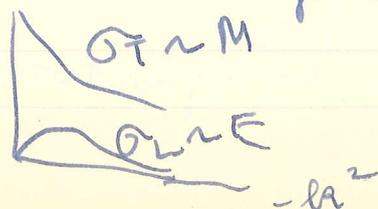
$$W = \sqrt{m(m + 2l_0)}$$

$$- 2(m + 2l_0 \sin^2 \theta) l_0$$



$$\frac{d\sigma}{d\Omega d\alpha d\beta} = \{ (\sigma_T + \sigma_L) \}$$

virtual photon



deep inelastic region

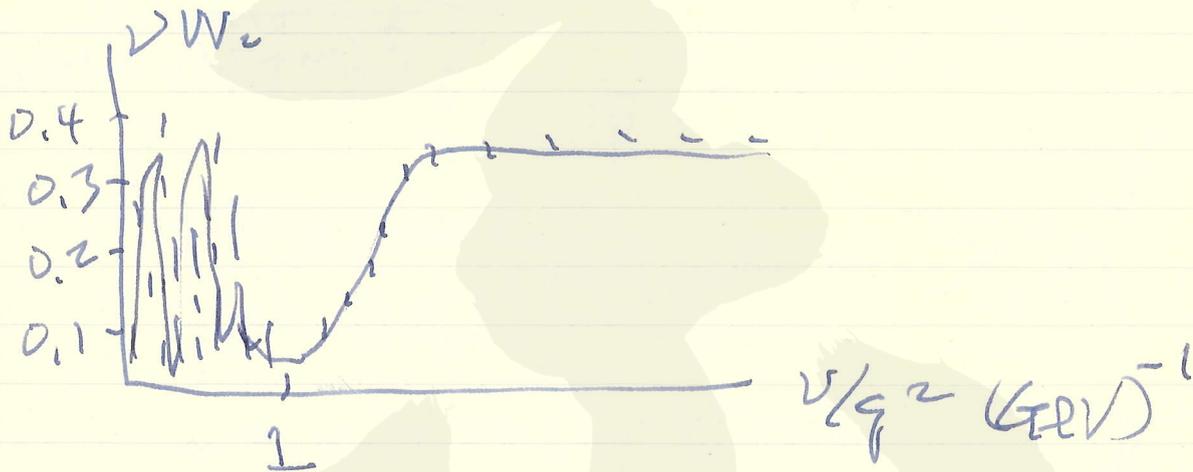
$$\nu \equiv k_0 = k_0 - k_0' \rightarrow \infty$$

$$q^2 \equiv -k^2 = 4k_0 k_0' \sin^2 \frac{\theta}{2} \rightarrow \infty$$

$$\nu/q^2 = \text{fixed}$$

1)  $\nu W_2(q^2, \nu) \rightarrow \text{const } \nu$  as  $\nu \rightarrow \infty$   
 $\frac{\nu}{q^2} W_1(\dots) \rightarrow \text{const.}$   $q^2$ : fixed

2)  $\nu W_2(q^2, \nu) \rightarrow F(\omega)$   $\omega = \nu/q^2$   
 as  $\nu \rightarrow \infty$   $\omega \rightarrow \infty$   
 $F(\omega) \rightarrow \text{const.} \neq 0$



Parton model

Drell

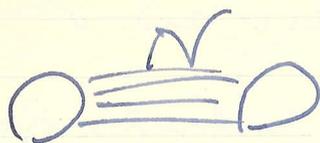
(S. J. Brodsky - Partons  
(Stanford)

point-like  
quasifree



parton

Drell-Henry-Yang  
 PR 221 (1969)  
 [hep]

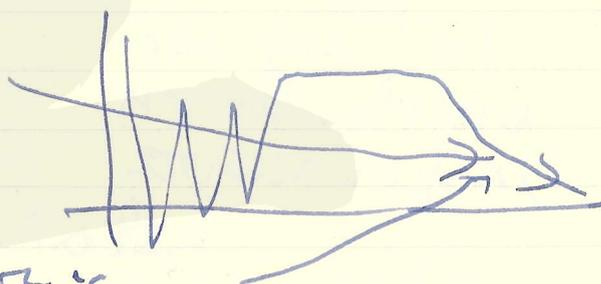


$$P(N) \rightarrow \frac{1}{\sqrt{2}}$$

parton mass : 0

$$\sqrt{\langle a^2 \rangle} = 0.4$$

① quark model  
 qq̄q



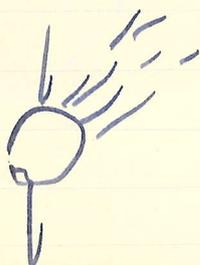
N: TH  $P_e \rightarrow P_p, l, \tau, \nu, c$   
 $P(N) = 0$

② qq̄q + n(qq̄)

$$a(N) = \left(\frac{2}{3}\right)^1 + \left(\frac{2}{3}\right)^2 + \left(\frac{1}{3}\right)^2 + \frac{1}{3} \left( \left(\frac{2}{3}\right)^2 + 1 \right) \times (N-3)$$

$$= \frac{1}{3} + \frac{2N}{9}$$

Barbanel - Goldberger - Treiman  
 PRL 22 (1969)



G. Börner  
 "Quasars": Speculations on  
 Sources of gravit. radiat. and  
 discussions of Weber's experiments



← 1 m →

$10^{-30}$  erg sec<sup>-1</sup>  
 earth-moon  
 super nova

$10^5$  erg sec<sup>-1</sup>  
 $10^{50}$  erg sec<sup>-1</sup>

Weber GAL (1969)  
 1660 Hz ± 0.01 Hz  
 $10^2$  erg cm<sup>-2</sup>

transverse wave  
 far > galactic center  
 $10^4$  erg cm<sup>-2</sup>

	1 KPC	10 KPC	10 MPC	1 GPC
	Pulsar	Gal. Cent.	Quasars	Quasars
E	$10^{53}$	$10^{55}$	$10^{61}$	$10^{65}$
$m_0$	$Y_{20}$	5	$5 \cdot 10^6$	$5 \cdot 10^{10}$
	$10^{-6.3}$ sec	$10^{-4.5}$ sec	1 min	1 week
$\tau^{-1}$				

Kerr 1962  
galaxy expanding  $7 \text{ km/sec}$   
 $70 \text{ m}_\odot/\text{year}$  mass-loss  
for  $10^8$  years

Schwarzschild radius  $R_s$   
$$1+z = \frac{1}{\sqrt{1-R_s/R}}$$

cluster of black holes  
"quasar"  
quasar  $\rightarrow$  quasar

重力場と一般相対性

高橋 謙一

書下 1.21.9.10, 1969

Dicke

higher spin + lower spin  
 mass spin

$\gamma$  0  $\bar{l}^-$   
 $\pi$  135 MeV  $0^-$   
 $\rho$   $\leq 3 \times 10^{-29}$  eV/c  $0^+ 2^+ 4^+ 6^+ \dots$

$\nu$   $m_{\nu} \leq 300$  eV  
 $m_{\mu} \leq 3$  MeV  
 $m_{\gamma} \leq 10^{-13}$  eV

$$\left. \begin{array}{l} \square \varphi_{\mu\nu} = 0 \\ \varphi_{\mu\nu} = \varphi_{\nu\mu} \\ \varphi_{\mu\mu} = 0 \\ \partial_{\mu} \varphi_{\mu\nu} = 0 \end{array} \right\} \frac{1}{i} \left. \begin{array}{l} \square \varphi_{\mu\nu} = T_{\mu\nu} \\ T_{\mu\nu} = T_{\nu\mu} \\ T_{\mu\mu} \neq 0 \\ \partial_{\mu} T_{\mu\nu} = 0 \end{array} \right\}$$

$$L = L_m + L_f + L_i$$

$$L_m = -\frac{m}{2} \int ds \dot{z}^i \dot{z}^m \eta_{im}$$

$$L_i = \int m \int ds \dot{z}^i \dot{z}^m \phi_{im}(s)$$

$$L_m + L_i = -\frac{m}{2} \int ds \dot{z}^i \dot{z}^m g_{im}(s)$$

$$g_{im} = \eta_{im} - 2f \phi_{im}(u)$$

Fierz

Gupta

Weyl

Thirring

湯川素子氏の講演録

12月22日(月) 午前中 (12月22日)  
湯川素子 - Introduction

経路積分  
 自由場の経路積分

$$[P_\lambda^2 + M_0^2 + \sum_{i=1}^n M^2(p_i, z_i)] \psi_n(P, z_1, \dots, z_n) = 0$$

$$M^2(z, p) = \frac{1}{z} (p^2 + \omega_0^2 z^2) \quad n=0, 1, 2, \dots$$

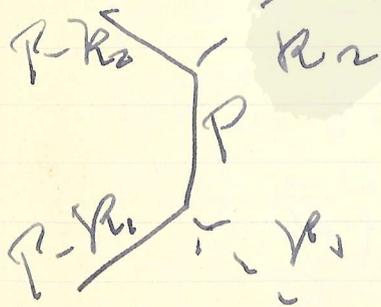
$$\left. \begin{aligned} P_\lambda z_\lambda &= 0 \\ P_\lambda p_\lambda &= 0 \end{aligned} \right\}$$

$\langle 0 | 0 \rangle$

$$\left( P^2 + M_0^2 + \sum_N \omega_N a_N^* a_N \right) \psi(P, a^*)$$

経路積分

$$\left[ P_\lambda^2 + M_0^2 + \sum_{s,\lambda} \omega_s a_{s\lambda}^* a_{s\lambda} + P_\lambda \sum_s p_s \left( \frac{a_{s\lambda}^2 - a_{s\lambda}^{*2}}{i} \right) + g M_0 A(x_N) \right] \times \psi(P, a^*, A^*) |0\rangle = 0$$



$\Lambda = S$   
 $\Lambda = S \pm \frac{\sqrt{3}}{2}$   
 非一様変形  
 deformable sphere Model  
 Non-uniform deformation

$\psi(x)$  real field  
 $\psi_\alpha(x)$  complex field  
 $\alpha = 1, 2$  spinor field

$$\psi_\alpha = \sum_r \sum_{\mu\nu\alpha} U_{r\mu\nu\alpha} \psi_{r\mu\nu}$$

$\downarrow$   
 $\psi_\alpha(x)$   
 $\downarrow$   
 quark

$$H = \sum_r \psi_{r\mu\nu} (m_{r\mu\nu} + n_{r\mu\nu}) + \Delta \psi \sum_r (m_{r\mu\nu} + n_{r\mu\nu}) + \frac{1}{2} \psi^2$$

$+ b$   
 $\downarrow$   
 $m^2$

triality  
 i) lepton  
 $(m, n) = (3, 0)$

$$6 \times 6 \times 6 = 56 + 20 + 20 + 20$$

$\square$        $\square$        $\square$   
 0            X            X

$l = 0, 0, 0$

$$m^2 = \nu(l + \alpha n + \beta) - \frac{l}{2I} \sigma^2 + b$$

$$(m, n) = (4, 1)$$

ii) meson  
 (1, 1)

在  $\alpha$ : 内部標  $\alpha$   
 外部標  $\alpha$

multilocal  
 固結 model

$n \rightarrow \infty$

$$X_\mu = \frac{1}{N} \sum_{\alpha=1}^N y_\mu^\alpha$$

$$x_\mu^\alpha = y_\mu^\alpha - X_\mu$$

$$\sum x^\alpha = 0$$

$$q^\alpha = \frac{1}{i} \frac{\partial}{\partial y^\alpha}$$

$$P_\mu = \sum q^\alpha$$

$$p^\alpha = q^\alpha - \frac{1}{N} P$$

$$[x_\mu^\alpha, p_\nu^\beta] = i \delta^{\alpha\beta} g_{\mu\nu} - i \frac{1}{N} g_{\mu\nu}$$

$$H \psi = 0$$

$$H = \frac{1}{2\mu} \sum_{\alpha=1}^N q^\alpha q^\alpha + \frac{\kappa}{2} U + C$$

$$U = \sum_{\alpha=1}^N (y^\alpha - y^{\alpha+1})^2 - \sum_{\alpha=1}^N \left( \frac{y^\alpha - y^{\alpha+2}}{2} \right)^2$$

$$T \sum_{\alpha=1}^N \left( \frac{y^\alpha - y^{\alpha+3}}{3} \right)^2 \dots$$

$$\text{or } U = \sum_{\alpha=1}^N \sum_{\nu=1, \dots, \frac{N}{2}} \frac{(-1)^\nu}{\nu^2} (x^\alpha - x^{\alpha+\nu})^2$$

same as 2.14  $(y^\alpha - y^{\alpha+1})^2$  etc

~~N~~ normal coordinates

$$x^\alpha = \frac{1}{\sqrt{N}} \sum_{l=-\frac{N}{2}}^{\frac{N}{2}} a_l e^{i2\pi l \alpha / N}$$

$$a^{-l} = a_l^* \rightarrow a^0 = 0$$

$$H = \sum p^\alpha p^\alpha$$

$$U = \sum_l a_l^\dagger a_l \sum_{\nu=1}^{N/2} 2(1 - \cos \frac{2\pi l \nu}{N}) \frac{(-1)^{\nu-1}}{\nu^2}$$

$$\frac{1}{N} \sum_{l=0}^N 2 \left( \frac{\pi l}{N} \right)^2 \quad -\frac{N}{2} \leq l \leq \frac{N}{2}$$

$$M^2 = \sum \omega_l' (a_l^\dagger a_l + b_{l+2}^\dagger b_{l+2})$$

$$\omega_l' = 2\nu \omega_l \rightarrow 2\sqrt{2\pi k} \cdot \pi \cdot l = 2m_0^2$$

$$\langle 0 | \pi_\mu^{\alpha 2} | 0 \rangle = (\sigma + \log \frac{N}{2}) \frac{1}{m_0^2}$$

第2回. 12月23日.

予習: 1. 2. 3. 4.

田中先生: duality と  $\infty$  V R の関係

duality の  $\leftrightarrow$  関係

time-like      space-like (momentum)

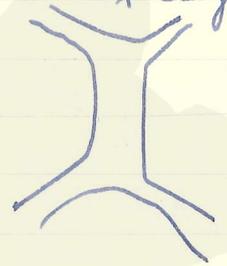
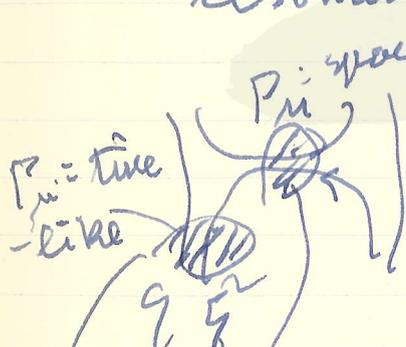
composite

elementary

resonance

exchange

Regge



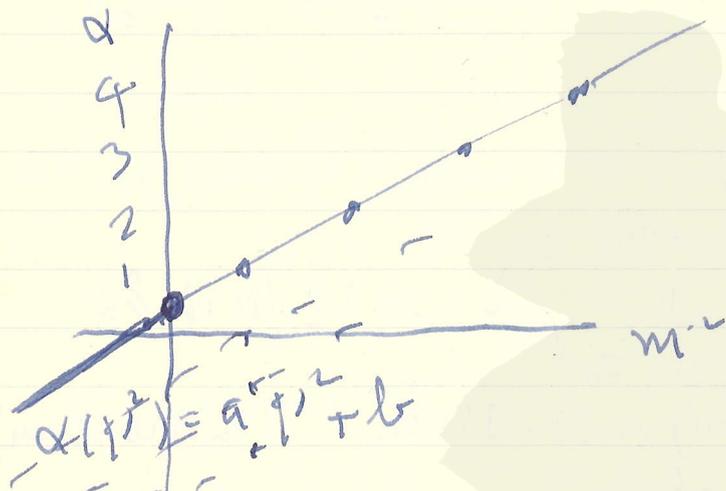
composite, space-like (momentum)

2 spin, spin 0 の  $\leftrightarrow$  関係  $\rightarrow$  (伝達の 経路)  
 spin の 関係?  $O(2,1) \rightarrow$   
 $\rightarrow$  spin  $(0, \frac{1}{2}, 1, \dots)$   $\leftrightarrow$   $O(3,1)$

$\rightarrow$  Regge pole  $\alpha(p^2)$

finite energy sum rule (FESR)  
 $\rightarrow$  resonance (low energy) と high energy の Regge の  $\leftrightarrow$  関係

Chew-Frautschi



spin  $P_{\mu}$   $M_{\mu\nu}$   
 $P^2 = 0$   $\tau$  singular  $\epsilon$  関数  
 $\alpha = \sum_{n=0}^{\infty} \alpha_n \tau^n$  の  $\alpha_n$  の  $\tau$  関数

(Friedmann-Wang)  
 (Sabita)

0(3,1) の  $\alpha$  の  $\tau$  関数  
 Veneziano  
 Regge trajectories の  $\alpha$

この  $\alpha$  は  $\tau$  の  $\alpha$

propagator  $\alpha$  の  $\tau$  関数

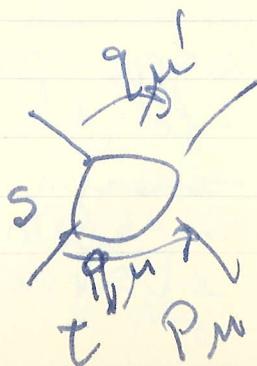
$$P_{\mu} = \omega \sum_{r,\mu} r \pi_{\mu}$$

この  $\alpha$  は  $\tau$  の  $\alpha$

2-2  $\alpha$  の  $\tau$  関数

$$s = (q - q')^2 \quad u = (q + q')^2$$

$$t = P_{\mu}$$



$$A(t, s) = \frac{P(1-a(s))P(1-a(t))}{P(1-a(s)-a(t))}$$

$O(3, 1)$      $\kappa, j, m$

$$P_m^2 = \frac{1}{a}(\kappa - l + 2n + l + m) - b$$

$$A(t, s) =$$

$\uparrow$  ?  
 $p(0, \infty)$

$$H(x) = \int d^4x_1 d^4x_2 \delta^4(x - \frac{x_1 + x_2}{2})$$

$$\times \pi(x_1) \pi(x_2) P(x, x_1, -x_2)$$

$$P(x, y) = \sum_{\kappa=1}^{\infty} \sum_{j=0}^{\kappa-1} \sum_{m=j}^{\infty} \int d^4p \sum_n P_{\kappa, j, p}^{m, n}(x)$$

$$\times F_{\kappa, j, p}^{m, n}(y) d^4p$$

$\mathbb{R}^4 \ni \mathbb{S}^1 \times \mathbb{R}^3$  is a  $\mathcal{G}$ -field or bilocal

Jacob's polynomial

in definite metric

$$\kappa - l + 2n + l + \sigma = L$$

$2\kappa - 2l + 2n + \sigma = L$



2'2' : 2'2' , 2'2' G

2'2' model: Veneziano model

2'2' model

1)  $SU(3)$  10, 10, 10

M, P

13, 13 a 10, 10, 10, 10, 10

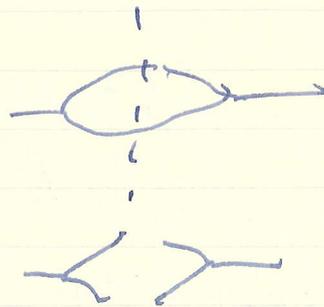
( $q\bar{q}$ ) & excitation  
 ( $q\bar{q}$ ) excitation

2)  $H = \sum n a_{\mu}^{\dagger} a_{\mu}$

N.G.F. unitarity, Born 1941

自己共役性  
 正規性

$$m T = T T^*$$



Operator formalism

$$a(t) = at + b \quad b < 0$$

$$a(m^2) = 0 : am^2 + b = 0$$

$$a_{\mu\nu} |z\rangle = z_{\mu\nu} |z\rangle$$

$$a^\dagger a |n\rangle = n |n\rangle$$

$$- \partial a_i = \langle z | z \rangle \neq 0$$

$$z = l + im \quad \text{complex}$$

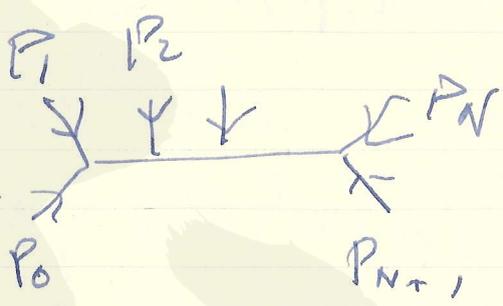
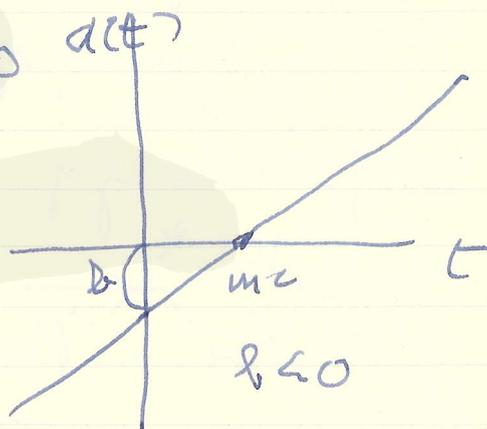
lattice point

$l = \text{Re } z, m = \text{Im } z$

(von Neumann)  $|z\rangle = e^{-|z|^2}$

$$|z\rangle = e^{-|z|^2}$$

$$\sum_{n=0}^{\infty} \frac{z^n}{\sqrt{n!}} |n\rangle$$



$$\langle z | H | z \rangle = \omega z^* z = \frac{1}{2} (\rho^2 + \omega^2 \eta^2)$$

$$|z\rangle = U(z) |0\rangle$$

driving operator

$$U(z) = \exp \tilde{v} (z a^\dagger - a^\dagger z^* a)$$

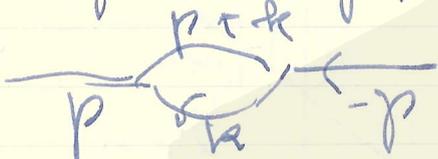
$$:U(z): = e^{i\hat{z}at} e^{-i\hat{z}^*a}$$

$$U(z) = e^{-i\hat{z}^2/2} e^{i\hat{z}at} e^{-i\hat{z}^*a}$$

$$\prod e^{\frac{p^2}{2m}} U_n(p) |0\rangle$$

✓ Klauder &  
 Sudarshan

Fund. of Quantum Optics  
 S. T. Ma: entire function  
 Self-energy



$$\Sigma(p) = \int d^4k M(k, p) A$$

$$M(k, p) = \text{Tr} [P(\alpha(-k)) V(p) P(\alpha(p+k)) \times V(-p)]$$

$$\Sigma(p) = \int d^4k \int_0^1 dx_1 \int_0^1 dx_2 \kappa_1^{-\alpha(-k^2)-1} \times \kappa_2^{-\alpha(-(p+k)^2)-1} [(1-x_1)(1-x_2)]^{-c}$$

$$\times \prod_n \text{Tr} (\kappa_1^{h_n} V_n(p) \kappa_2^{h_n} V_n(-p))$$

$$H = \sum_n a_n^{(n)} q_n^{(n)} = \sum h_n$$

state  $\leftrightarrow$   $\gamma$ - $q$  : Veneziano  $\mu_{00}$   
 Amplitude

resonance  $\times$  background  
 hard core

$I=2 \pi^+ \pi^+$	resonance $\times$	hard core $0$	$a > 0$
$I=0$	$0$	$\times$	$a < 0$

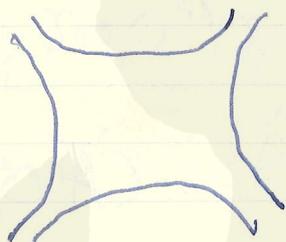
low energy  $\pi^+ \pi^+ \rightarrow \pi^+ \pi^+$   
 [resonances  $\pi^+ \pi^+ \rightarrow \pi^+ \pi^+$ ]  
 hard core ?

Imaginary part ?  
 $\delta$ - $\delta$  as.

$2^+ 2^+$  :  $\rho^+ \rho^+$  :  $\pi^+ \pi^+$

~~Amplitude~~

$\rho^+ \rho^+$  :  $\pi^+ \pi^+ \rightarrow \pi^+ \pi^+$   
 "line"



$\langle 0 | q(x) \bar{q}(y) | 0 \rangle \sim \varphi(x, y) \rightarrow$  parameter  
 current algebra  
 $\bar{q}=0$   
 $SU_6 \otimes O(3)$   
 chiral symmetry  $SU_3 \otimes SU_3$   
 $\rightarrow SU_2 \times SU_2 \rightarrow SU_2 \leftarrow SU_3$

parameter  
 力  
 対

$\gamma_5$   
 $SU_6$

$$H = \sum_n m a_n^{t(n)} a_n^{(n)}$$

quark pair

$$\psi(x, z) \rightarrow \psi(x, \phi(z))$$

12 12 12 12 12 : Bose Quarks and Non-Abelian  
 12 12 12 12 12 : Weak interaction

- i)  $\frac{1}{2} \rightarrow 3$  56  $\frac{1}{2}$
- ii) binding problem

exciton  $\rightarrow$  base shift  
 $\rightarrow$  binding of  $\psi$  and  $\bar{\psi}$   $\psi < \bar{\psi}$

$$H = (\bar{\psi} O_i \psi) (t^a O_i \psi)$$

$$O_i = (1 + \gamma_5) \gamma_\mu$$

$$(\bar{A} O_i B) (\bar{C} O_i D) = -(\bar{A} O_i D) (\bar{C} O_i B)$$

$$a = 1 + \gamma$$

A. i)  $|\Delta S| = 2$  vs  $\tau$

ii)  $|\Delta S| = 1$ :  $|\Delta I| = 1/2$

iii)  $|\Delta S| = 0$ :  $|\Delta I| = 0, 1$

B. neutral current  $\tau < \tau$   $\tau$   $\tau$   $\tau$

C.  $\tau_3 = \Lambda_0$   $\rightarrow$   $\tau$   $\tau$   $\tau$   $\tau$  process

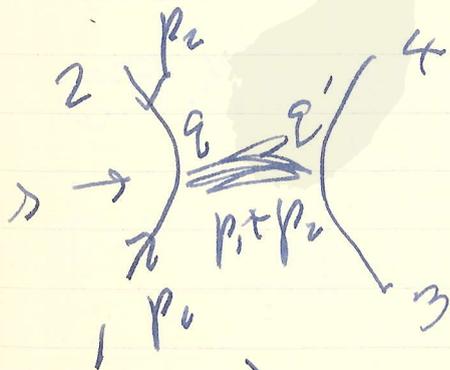
相互作用の long range force  
 $|\Delta I| = 0$   
 (weaker の  $\lambda \rightarrow \tau = \text{相互作用}$ )

第3回 12月24日  
 午前中: 記号, 相互作用  
 片山教授: 相互作用の量子化

$$\delta^4(p_1 + p_2 + k) \int d^4q \psi(p_1) \Sigma(p_1, p_2, q) \times \psi(p_2) \phi(k, q)$$

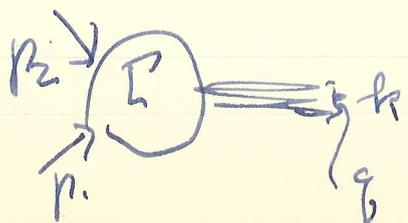
$$\langle 0 | T (\phi(k, q) \phi(k', q')) | 0 \rangle$$

$$= \delta^4(k + k') D(k; q, q')$$



$$A_s = \int d^4q d^4q' \Sigma(p_1, p_2; q) \times D(-(p_1 + p_2), q, q') \times \Gamma(p_3, p_4; q')$$

$$A_t =$$



$$A_u =$$

$$A_s = A_t = A_u$$

(I)  $q, q'$  trivial  $\sim \delta^4(q - q')$

$$D(k; q, q') = \delta^4(q - q') D(k; q)$$

(II)

$$(II-A) \quad \delta^4(k+k') D(k; q, q') = \delta^4(k+k')$$

$$\times \delta^4(q - q') A(q^2)$$

$$\Delta_F(x-x', y, y') = \delta^4(x-x') \Delta(y+y')$$

$$(II-B) \quad \Sigma(p_1, p_2; q) = V(p_1, q) V(p_2, q)$$

$$\Sigma(p_1, p_2; q) = \int d\lambda \tau(\lambda) \left[ \int d\mu f(\mu) \right]$$

$$e^{i\frac{\lambda}{2} q^2 + i\mu(p_1 + p_2)}$$

$$\times \left[ \int d\nu f(\nu) e^{i\frac{\nu}{2} q^2 + i\nu(p_2 + p_1)} \right]$$

$$(III) \quad \delta^4(p_1 + p_2 + k) \int d\lambda \tau(\lambda) \int dq \Psi(p_1, \sqrt{\lambda} q)$$

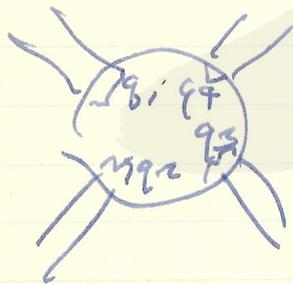
$$\times \Psi(p_2, \sqrt{\lambda} q) \Phi(k; q)$$

i)  $\mathbb{R}^4$  の空間座標  $x$  と  $\mathbb{R}^4$  の momentum  $k$  の自然性  
 と  $\mathbb{R}^4$  の自然性

ii) 場の量子論の  $\mathbb{R}^4$  の自然性 (Lorentz invariance)

$$\left( \int \psi(p_1; q) \psi(p_2; q') \phi(k; q, q') \right. \\ \left. dq dq' \right) \times \delta^4(p_1 + p_2 + k)$$

$$\langle 0 | T(\phi(k, q_1, q_2) \phi(k', q_3, q_4)) | 0 \rangle \\ = \delta^4(k + k') D(q_1, q_2, q_3, q_4)$$



$$\alpha(p^2) = \alpha(0) + \alpha'(0) p^2$$

$$\alpha'(0) / \alpha \lesssim 1$$

→ Veneziano

$$\langle 0 | T(\phi(x) \phi(x')) | 0 \rangle = \delta^4(x - x')$$

$$\langle 0 | T \phi(x, m^2) \phi(x', m'^2) | 0 \rangle \\ = \delta(m^2 - m'^2) \Delta_F(x - x', m^2)$$

$$\phi(x) = \frac{1}{\sqrt{\pi}} \int_{-\infty}^{+\infty} dm^2 f(m^2) \phi(x, m^2)$$

$$f(m^2) = 1$$

$$\langle 0 | T(\phi(x, q_1, q_2) \phi(x', q_3, q_4)) | 0 \rangle$$

$$= \delta^4(x - x') D(q_1, q_2, q_3, q_4)$$

$$\phi(x, q_1, q_2) = \sum_a \int d^4k e^{-ikx} \frac{1}{\sqrt{a}}$$

$$\times C_a(q_1, q_2, k) \phi_a(k)$$

$$\frac{i}{\pi} \sum_a \frac{C_a(q_1, q_2, p_{12}) C_a(q_3, q_4, -p_{12})}{m_a^2 - p_{12}^2}$$

$$= D(q_1, q_2, q_3, q_4)$$

対称性

5: 流と (調) との (対称) 性.

deA 流と: 微分幾何学と粒子の相互作用

Causality  
 microcausality

macrocausality

complex mass  $m \in \mathbb{C}$  と粒子の causality との関係

$$A = p^2 - \lambda^2 \quad \Gamma = 2p\lambda$$

$A \geq 0$  である。  $P_{\mu\nu}$  の性質 (  $P_{\mu\nu}^2 = P_{\mu\nu}$  )  
 伝搬関数 ( propagator )

流線図: 流線図

連続性  
 高次元流線図

2-次元流線図  $\Rightarrow$   $n=2$  の場合

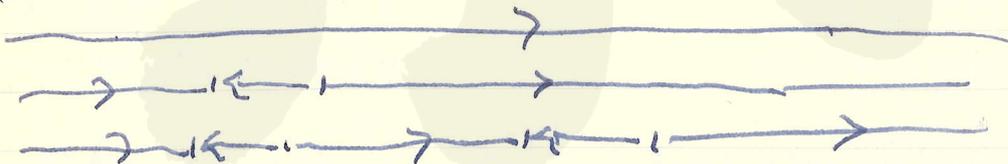
mapping  
 $\omega, \bar{\omega}$  変換



円周上の点  $z, z'$  について



一次元



$$D(g) = \begin{pmatrix} g'(0) & g''(0) \\ 0 & (g'(0))^2 \end{pmatrix}$$

1970年 湯川記念館史料室

Superfluidity due to Spin-Orbit Forces in Neutron Star (superstate)

Generalization of Bogoliubov Transformation

$$S_0 \rightarrow SP_2$$

$n \star = \text{pulse}$   
 { rotation magnetic field } ← 湯川記念館史料室

supernova 湯川記念館史料室

カ = 湯川記念館史料室  
 period (P) } 湯川記念館史料室 30 msec.  
 } 湯川記念館史料室 ~ 1 sec.

$$\frac{\Delta P}{P} \sim 10^{-9}$$



→ 湯川記念館史料室 LT<sub>2</sub> 湯川記念館史料室  
 湯川記念館史料室

$$\frac{dP}{P} \sim 10^{-5} \sim 10^{-13}$$

time in linear 湯川記念館史料室  
 湯川記念館史料室

Cold model



湯川記念館史料室 → pulse 湯川記念館史料室

$$E_{rot}(\text{rigid}) \sim 10^{49} \text{ erg} \\
 (M \approx M_0, R = 10^6 \text{ cm})$$

slow down  
 $3 \times 10^{38}$  energy loss  
 $erg/sec$   
 (radio emission  $< 10^{31}$  erg/sec)  
 cosmic ray?

$J_{\parallel} \approx \rho_{\parallel} \rightarrow$  Paradox  
 $10^{12-13}$   
 $10^5$  Gauss at surf  
 $\therefore$  at  $v = \frac{c}{\omega}$

29th:

high density  $\sim 10^{12}$

$\left( \begin{matrix} s=1 \\ p=2 \end{matrix} \right) \rightarrow$  S-wave  $\& \text{P}$

$^3P_2$

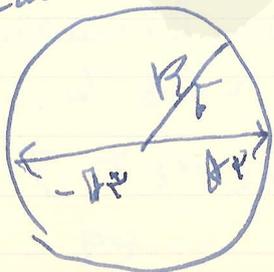
$s=1 \rightarrow j=2$   
 $l=1$

coupling

super  $\rightarrow S \rightarrow p \rightarrow H$

$\mu = \mu: T=1$

Fermi  $\mu$



$s=0: ^1S_0 \quad ^1D_2 \quad ^1G_4$

$s=1: ^3P_1 \quad ^3F_4$

$$E_F = \frac{\hbar^2 k_F^2}{2M}$$

(hab)

$$E_{NN} = 4 E_F$$

$$E_F (N.M.) = 42 \text{ MeV}$$

$\left\{ \begin{matrix} R = 7.0 \text{ fm} \\ v_0 = 1.07 \text{ fm} \\ f_{\mu} = 10 \text{ cm} \end{matrix} \right.$

$E_F \gtrsim 150 \text{ MeV}$  high density  
 ${}^3P_2$  pairing int.

$E_F = 75 \sim 150 \text{ MeV} \rightarrow n, p, e^-, \Lambda$   
 $\rho = 10^{14} \sim 10^{15} \text{ gm cm}^{-3}$   
 $\downarrow$   
 $\sim 10\%$

energy gap

spin  $N_A \times \left( \frac{\Delta(E_F)}{E_F} \right) \times M_N$   
 $\sim 10^{57} \times \frac{1}{100} \times 10^{-18} \text{ MeV}$

$\rightarrow 10^{12} \text{ Gauss (} \vec{E} \approx \vec{v} \times \vec{B} \text{)}$

片山新久

小林正樹の(電子に相互作用と)

11月13日, 1970

製作法

1930

小林正樹

小林正樹

Born

Meisenberg

Meisenberg

40

小林正樹

Markov

50

小林正樹

(1948)

60

小林正樹

70

小林正樹

S行列  
 非局所相互作用  
 電子化

1953

小林正樹

小林正樹

小林正樹の相互作用

小林正樹

小林正樹 - 現象

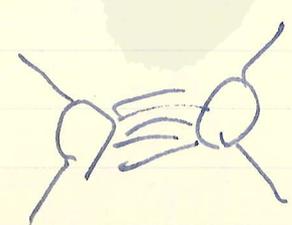
Regge

Veneziano

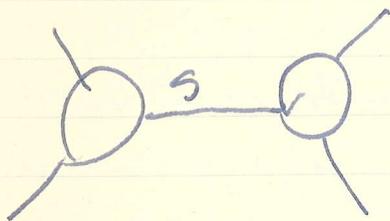
小林正樹

交叉相互作用

二重性



$$A = A_s(t, u) + A_t(u, s) + A_u(s, t)$$



$$A_s(t, u) = A_s(u, t)$$

$$\equiv A(s, t, u)$$

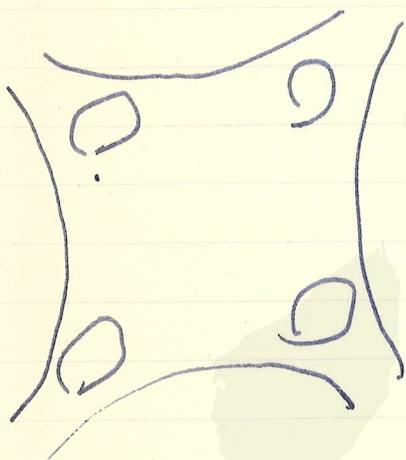
$$1) A_s(t, u) = A_t(u, s) = A_u(s, t)$$

$$2) A_s(t, u) = v_s(t) + v_s(u)$$

$$v_s(t) = v_t(s)$$

global  
local

$\phi(x, y)$   
 $\psi(y)$



$$\phi(x) = \frac{1}{\Omega} \int_{-\infty}^{+\infty} d\mathbf{m}^2 \phi(x, \mathbf{m}^2)$$

$$\phi(x)_{\Omega_0} = 0 \quad \text{等等}$$

$$(\square + m_0^2) \phi(\mathcal{R}) \Delta \mathcal{L} = 0$$

$$\int dm^2 [m_0^4 - m^4] \phi(\mathcal{R}, m^2) \Delta \mathcal{L} = 0$$

$$i) \text{ 因 } \mathcal{R} \text{ 上 } \Rightarrow x - \tau - \\ m^2 \quad (\rightarrow \infty, +\infty)$$

藤田 啓

湯川

# Hyperquantization of electromag. and spin $1/2$ fields

K. Doornik and Y. Takahashi  
relativistic ? )  
unitarity ? )  
indefinite metric  $\nu \ll \hbar$ .

# Non-local Field Theory of the Quark Model II

岩崎 良太郎

発行 2月10日, 1970

rigid separate subunits  $\sim$  quarks  
nonlocal field (bilocal)  $\sim$   
is  $\Phi_a^b(x, y)$   
 $\Phi_a^b(x, y)$

- (1) local  $\rightarrow \vec{U}(12)$
- (2) degeneracy
- (3) nonrel  $\rightarrow$  potential theory
- (4) Regge
- (5) oscillator

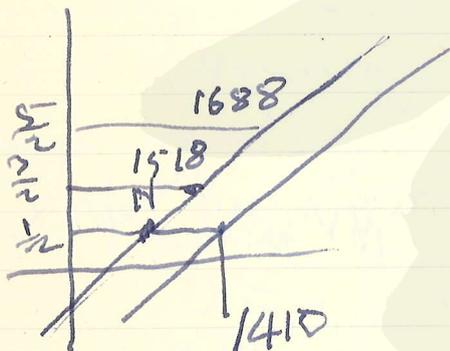
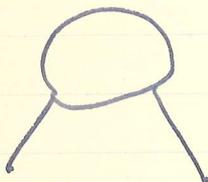
# Pomeron Surface Resonance ~~W~~ Excitation model of hadron resonances

研究 2.17, 1970



$N^*$	1410	$(\frac{1}{2}^+)$
	1518	$(\frac{3}{2}^-)$
	1688	$(\frac{5}{2}^+)$
	2190	$(\frac{7}{2}^-)$

$$\Delta P = (-1)^{L+J}$$

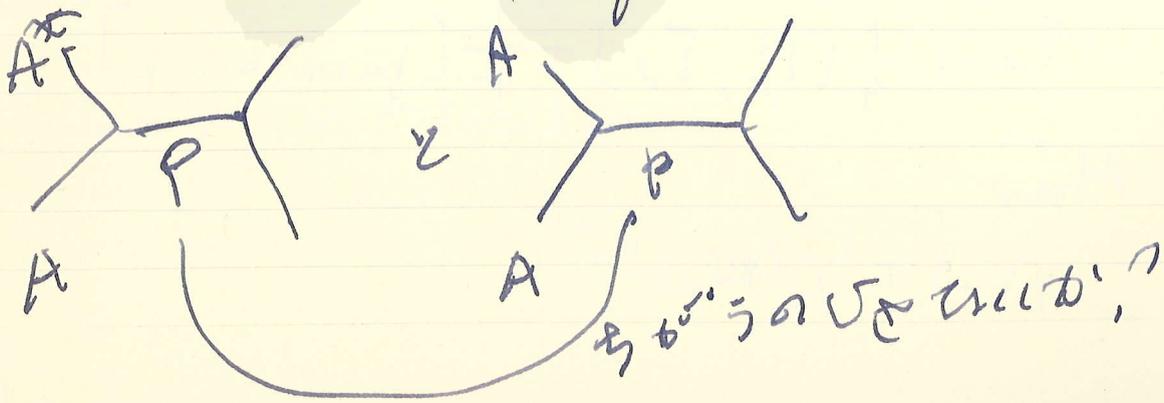


$$H = H_A + H_{res} + T_{AB} + V_{AB}$$



$$R = R_0 + \sum \sum L_{lm} Y_{lm}(\theta, \varphi)$$

## Pomeron-like resonance on background



# Success and Difficulty in Particle Picture by use of Inf. Comp. Wave Equations

March 10, 1970

## 1. Lagrangian formalism

$$\psi_\alpha(x) \quad \alpha=1, 2, \dots$$

## 2. Compositeness

Majorana, Nambu  $O(4, 2)$

$$P_\mu, M_{\mu\nu} \quad |m, J; p, J_z\rangle$$

Wigner

$$m^2 = \kappa_0^2 + \kappa_1^2 J(J+1)$$

$$W_\mu W^\mu = -P_\mu P^\mu \cdot J(J+1)$$

$$W_\mu = \hat{M}_{\mu\nu} P^\nu = \frac{1}{2} \epsilon_{\mu\nu\alpha\lambda} M^{\alpha\lambda} P^\nu$$

Takahashi

$$\{ (P_\mu P^\mu)^2 + \kappa_0^2 (P_\mu J^\mu) - \kappa_1^2 W_\mu W^\mu \} \psi(x)$$

$$\{ P_\mu P^\mu + \kappa_0 \Sigma_\mu P^\mu - \kappa_1 \Gamma_{\mu+4} W^\mu \} \psi(x) = 0$$

$$\{ \Gamma_\mu, \Gamma_\nu \} = 2g_{\mu\nu} \quad \mu, \nu = 0, \dots, 7$$

$$g_{\mu\nu} = (- + + + - + + +)$$

16 x 16

$$S_{\mu\nu} = \frac{1}{4} [\Gamma_\mu, \Gamma_\nu] + \frac{1}{4} [\Gamma_{\mu+4}, \Gamma_{\nu+4}]$$

$M_{\mu\nu}^{in}$

$$\Lambda = 1 + \frac{1}{2} \delta_{\alpha\beta\mu\nu} S^{\mu\nu}$$

phys. Lorentz group in  
 $SO(3, 1) \times S_{\mu\nu} \times M_{\mu\nu}$   
 $\times_{\text{in}} P_{\nu\gamma} + S_{\mu\nu} + M_{\mu\nu}$

Majorana:  $(a_i, a_j^\dagger) = \delta_{ij} \quad i, j = 1, 2$   
 $|j, m\rangle = \frac{1}{\sqrt{(j+m)! (j-m)!}} a_1^{j+m} a_2^{j-m} |0\rangle$

(in)  
 $M_{ij} = \frac{1}{2} a_\alpha^\dagger (\sigma_{ij})_{\alpha\beta} a_\beta$

(out)  
 $M_{ij} =$

Regge mass formula  
 $m^2 = a^2 (j + k)$

$$\left\{ (P_\mu P^\mu)^2 - \frac{a}{2} \Gamma (P_\mu P^\mu) + \delta_{\mu\nu} P^\mu W^\nu \right\} \times \Psi(x, \dots) = 0$$

$$\sigma_{\mu\nu} = \sigma_\mu \otimes \sigma_\nu$$

$$\Gamma = i \sigma_5 \otimes 1$$

$$[\Gamma_\mu, \Gamma_\nu] = 2g_{\mu\nu}$$

$\mu, \nu = 0, 1, 1, 1$

64x64

Gradsky & Streater  
 No-go theorem

河津 蘇峰

March 7, 1982  
 京都大学基礎物理学研究所 湯川記念館史料室

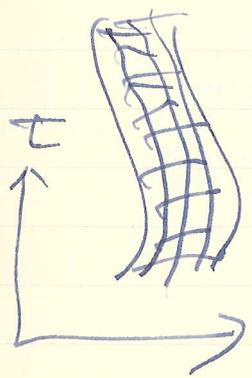
# Space-Time Approach to Duality

1. World sheet world line or "un"

$$x_\mu(\tau) \rightarrow x_\mu(u) \quad 0 \leq u \leq \pi$$

$$\downarrow$$

$$x_\mu(\tau, \theta)$$



$x_\mu$	$\tau, \theta$
$\varphi(x)$	$x_\mu(\tau, \theta)$
$\mathcal{L} = -\frac{1}{2} (\partial_\mu \varphi)^2$	$\mathcal{L} = -\frac{1}{2} \left[ \left( \frac{\partial x_\mu}{\partial \theta} \right)^2 - \left( \frac{\partial x_\mu}{\partial \tau} \right)^2 \right]$
$\square \varphi = 0$	

$$\left. \frac{\partial \varphi}{\partial x^\mu} \right|_{x=0} = 0$$

$$\left. \frac{\partial x_\mu}{\partial \theta} \right|_{\theta=0, \pi} = 0$$

$$H^{\text{tot}}(\tau) = \int d\theta \mathcal{H}(\tau, \theta)$$

$$\partial_\mu P_\mu = 0$$

2.  $\mathcal{L} \rightarrow T_{\mu\nu}$   
 3. space of meson states

$$x_\mu = c_\mu + \tau P_\mu + i \frac{1}{\sqrt{2}} \sum_{l=1}^{\infty} \left\{ \frac{a_\mu^+(l)}{\sqrt{l}} e^{il\tau} - \frac{a_\mu(l)}{\sqrt{l}} e^{-il\tau} \right\} \cos l\theta$$

$$\frac{dx^{\text{CM}}}{d\tau} = \pi P_\mu \quad x_\mu^{\text{CM}}, P_\mu$$

$$H = \pi \left[ \frac{1}{4} P^2 + \sum_{l=1}^{\infty} l a_{\mu}^{\dagger}(l) a_{\mu}(l) \right]$$

$$M^2 = \mu_0^2 + \sum_{l=1}^{\infty} l a_{\mu}^{\dagger}(l) a_{\mu}(l)$$

$$(H + \mu_0^2) | \rangle = 0$$

$$a_{\mu}^{-} | 0 \rangle = 0$$

$$P_{\mu} | 0 \rangle = 0$$

ground state  $\psi$

$$a_{\mu}^{-} | \psi \rangle = 0$$

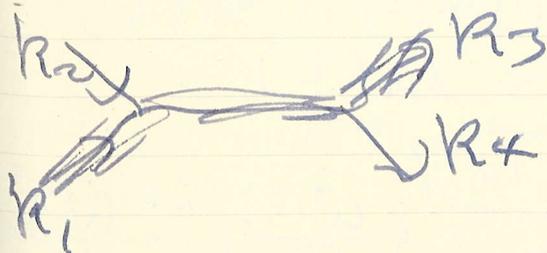
$$P_{\mu} | \psi \rangle = k_{\mu} | \psi \rangle$$

$$k_{\mu}^2 + \mu_0^2 = 0$$

$$| \psi \rangle = e^{i k_{\mu} x^{\mu}} | 0 \rangle$$

$$\left( -\square + \mu_0^2 + \sum_{l=1}^{\infty} l n(l) \right) \psi(x_{\mu}, n(l)) = 0$$

4. Meson scattering Amplitude



$$T(k_1, k_2, k_3, k_4)$$

$$= i e^{i k_2 \cdot x(0)}$$

$$\frac{1}{(k_1 + k_2)^2 + M^2}$$

$$i e^{i k_3 \cdot x(0)}$$

$$\frac{\partial^2 \chi_\mu}{\partial \sigma^2} + \frac{\partial^2 \chi_\mu}{\partial \tau^2} = 0$$

$$\lambda + i\theta = z$$

$$\left. \begin{aligned} 0 \leq \theta \leq \pi \\ -\infty < \lambda < \infty \end{aligned} \right\}$$

$\chi_\mu(z)$

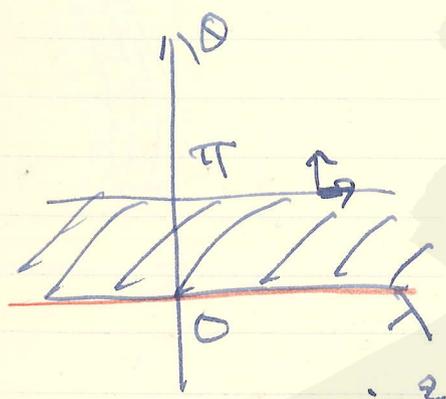
$$w = f(z)$$

Möbius 変換

$$w = \frac{az + \beta}{\gamma z + \delta}$$

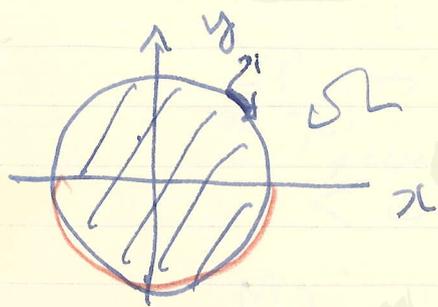
$$a\delta - \beta\gamma = 1$$

$$w = x + iy$$



$$w = \frac{-iz^2 - 1}{-iz^2 + 1}$$

duality



$$\langle 0 | \prod_{l=1}^n e^{i\alpha_l \chi(\rho_l)} | 0 \rangle$$

$$= \tilde{T}(\Omega)$$

duality invariance (conformal invariance)

5. Duality 変換

円盤 (D) に 変換

$$\chi_\mu(\tau, \sigma) \rightarrow \chi_\mu(\lambda, \theta) = \chi_\mu(z)$$

$$= F_\mu(z) + F_\mu(z^*)$$

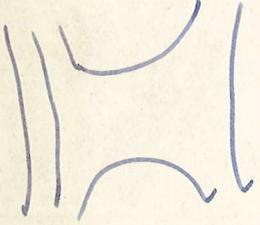
$$F_\mu(z) = \frac{p}{2}(z) + \frac{c}{2} + i\sqrt{2} \sum_{\alpha \in \mathcal{A}} \left( \frac{a^+(\alpha)}{\sqrt{e}} e^{z\alpha} + \frac{a^-(\alpha)}{\sqrt{e}} e^{-z\alpha} \right)$$

automorphic 変換

$$w = \frac{az + \beta}{\gamma z + \delta} \quad ; \quad \chi_\mu(z) = \chi_\mu(w)$$

baryon

LLL



23