



©2022 YHAL, YITP, Kyoto University  
京都大学基礎物理学研究所 湯川記念館史料室  
c033-855~892 狭込

c033-854

N98

尺士

NOTE BOOK

Manufactured with best ruled foolscap  
Brings easier & cleaner writing

April, 1970 ~  
~ July, 1971

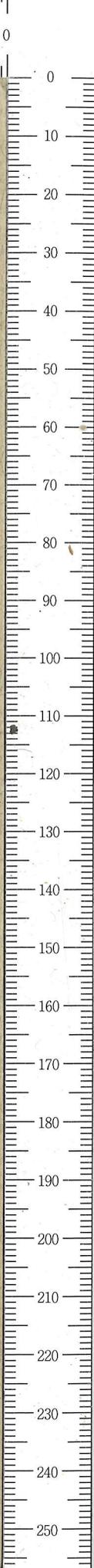
VOL. 尺士

100  
E  
A

H. Yukawa

98 Nissho Note

BOX 35





G. Börner  
Some Aspects of C.F.T.  
in Curved Space-Time

April 9, 1970

湯川記念館

embedded in 5-dim. Mink. space

$$\eta_{a,b} = \text{diag}(\tau, \dots)$$

$$\sum_a \eta_{ab} \zeta^b = -R^2$$

$$SO(1,4)$$

$$a, b = 0, 1, \dots, 4$$

$$T^{\mu\nu} = 0,$$

$$\lambda \neq 0$$

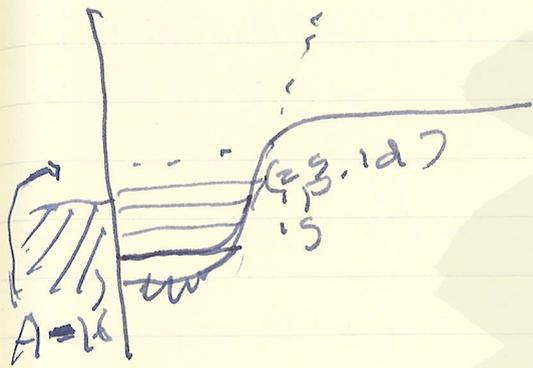
$$B_\mu = \frac{1}{R} J_{4\mu}$$

$$\mu = 0, \dots, 3$$

Malcolm Harvey  
 (Chalk River Natl. Lab.)

April 10, 1970

SU(3) Model and Harree-Fock Model



$$A = 16 \sim 40$$

$$H = H_0 + V$$

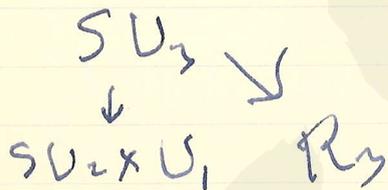
$$Q = (v_i^2 \gamma^2 + p_i^2 \gamma^2)$$

$$V = \sum (\beta_0 \tau \beta_2 \frac{r_{ij}^2}{a^2} + \beta_4 \frac{r_{ij}^4}{a^4} + \dots)$$

Elliot

$$A_{ij} = \frac{1}{2} (a_i^\dagger a_j + a_j^\dagger a_i)$$

$$a_i^\dagger = \frac{1}{\sqrt{2}} (\alpha + i \gamma x) \dots$$



Harree-Fock

V<sub>L</sub>: mag potential → SU<sub>3</sub>  
 Comparison with experiment

<sup>28</sup>Si

<sup>20</sup>Ne

1 Q Q + Pairing    SU(4)  
 1 Q Q + (S P)

Arima

高次考法

高次考法 = April 21, 1970

4次元の ~~物理~~ 理論の example

と 高次考法 (高次考法の)

Poincaré 群の generator & operator

の 高次考法

$$P_\mu = P_{\mu 0}$$

$$M_{\mu\nu} = M_{\mu\nu 0}$$

$$P_\mu = P_{\mu 0} + \sum_n P_{\mu n}^{(n)}$$

$$M_{\mu\nu} = M_{\mu\nu 0} + \sum_n M_{\mu\nu n}^{(n)}$$

} → generator equations  
 $i = -\lambda \mu \tau$   
 $\mu \nu \tau$

" $\tau$ " を 高次考法, 高次考法 or simple  $\tau$ ...

$$N = \int \frac{d^3 p}{(2\pi)^3} A^\dagger(\mathbf{p}) A(\mathbf{p}) \quad p_0 = \sqrt{\mathbf{p}^2 + m^2}$$

$$[P_\mu, N] = [M_{\mu\nu}, N] = 0$$

高次考法の  $\tau$  子

$$P_\mu, \quad W_\alpha = \epsilon_{\alpha\beta\gamma\delta} M_{\beta\gamma} P_\delta$$

2次元

bound state  
 scattering state  
 wave packet の 高次考法

$$\langle p p' | S | q q' \rangle = \frac{1}{\sqrt{p_0 p_0' q_0 q_0'}} \langle p p' | q q' \rangle^{(+)}_{(-)}$$

unitary

格内

R. Gatto, *Revista del Nuovo Cim.*, 1,  
 514 ('69)

Leading Divergences in Weak  
 Interactions, the Algebra of  
 Compound Fields and Broken  
 Scale Invariance.

塔領 2022 in u April 28, '70

$$L_w = g \{ j_\mu^e W^\mu + j_\mu^{ct} W^{\mu\dagger} \}$$

$$S_{\alpha\beta} = \delta_{\alpha\beta} - \delta^+ (P_\alpha - P_\beta) M_{\alpha\beta}$$

chiral  $SU(3) \otimes SU(3)$

$$L = L_0 - I^+$$

$$I^+ = \sum_{l=0}^{\infty} \epsilon_l u_l(x)$$

ps density  
 $(3, 3^*), (3^*, 3)$

$$u_l \rightarrow v_l$$

$$[F_i, u_l] = i f_{ikl} u_k$$

$$[F_i^s, u_l] = -i d_{ikl} v_k$$

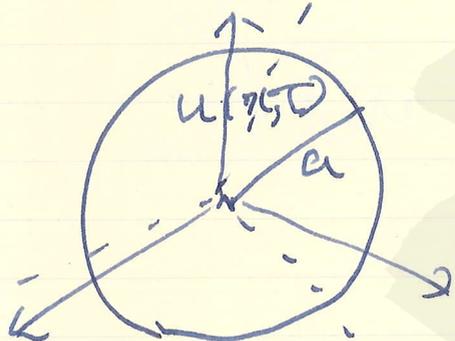
$$[F_i^s, v_l] = i d_{ikl} u_k$$

原稿 of  
 Deformable Sphere Model  
 湯川 of hadrons  
 May 18, 1970

non-relat.

non-homog. deform.

$$\frac{u}{a} \ll 1$$



$$x_i = x_i + u_i$$

$$(q, 0, \gamma)$$

$$T = \frac{1}{2} \int \dot{x}_i^2 dm$$



Truncated system

$$S = T + \text{level } \tau_2 \text{ 'T}$$

$\tau_2 \text{ 'T}$

$$S - T = u_0$$

$$\frac{\hbar^2}{I \pi a^3} \ll 1$$

$$S - \bar{J} = 0 \sim 1/2$$

$$S = \bar{J} + \Theta \quad S = \frac{\hbar}{2} \quad (\omega \neq 0)$$

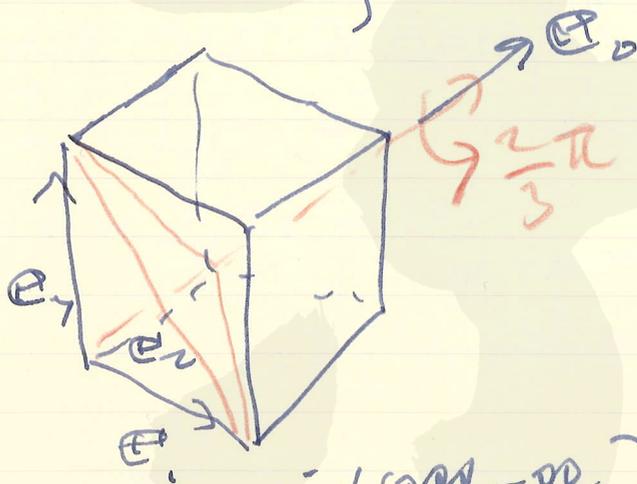
$$\downarrow S = \bar{J}$$

$$L = \frac{1}{2} \int d^3x \left[ p \dot{\alpha}_\alpha^* \alpha_\alpha + \alpha_\alpha^* F \alpha_\alpha \right] dV$$

quark or boson

triality

$$I_{rs} \rightarrow I_p$$



$$U_t = e^{i\alpha(m-n)}$$

$$m - n = 3N$$

$$\alpha = \frac{2\pi}{3}$$

$$U_t \cdot \psi = \psi$$

$$H = \nu \sum (l + a_n + b) (\nu \nu_{l m n \alpha}^{\mu} + \nu \nu_{l m n \alpha}^{\mu}) \\
 + \Delta \nu \sum (m_{l m n \alpha}^3 + n_{l m n \alpha}^3) \\
 + \frac{1}{2\tau} \sigma^2$$

$m^2 =$

$\beta$  (3, 0) (4, 1) (5, 2) - -  
 $M$  (1, 1) (2, 2) - -  
 normal                  exotic

$$\nu = 1.10 \times (\text{BeV})^2 \\
 c = 0.24 (0.2, 0.23) (\text{BeV})^2 \\
 m_0^2 = -0.98 (\text{BeV})^2 \\
 b = 0.49 ( )^2$$

湯川正 (Smithsonian Institution)  
Neutron star

発行: 5月20日, 1970

1950年  
二つ  
Oppenheimer, Volkoff  
Zwicky

石井  
Wheeler, Nakano

1954: X-ray

1968: Pulsar

$\rho > 10^{12} \text{ gm/cm}^3$

$5 \times 10^{13} \sim 10^{14}$

$\rho > 10^{14}$

neutron  
matter

n, p, e<sup>-</sup>

$\mu$ , hyperon

general relativity

重力

超伝導  
超伝導

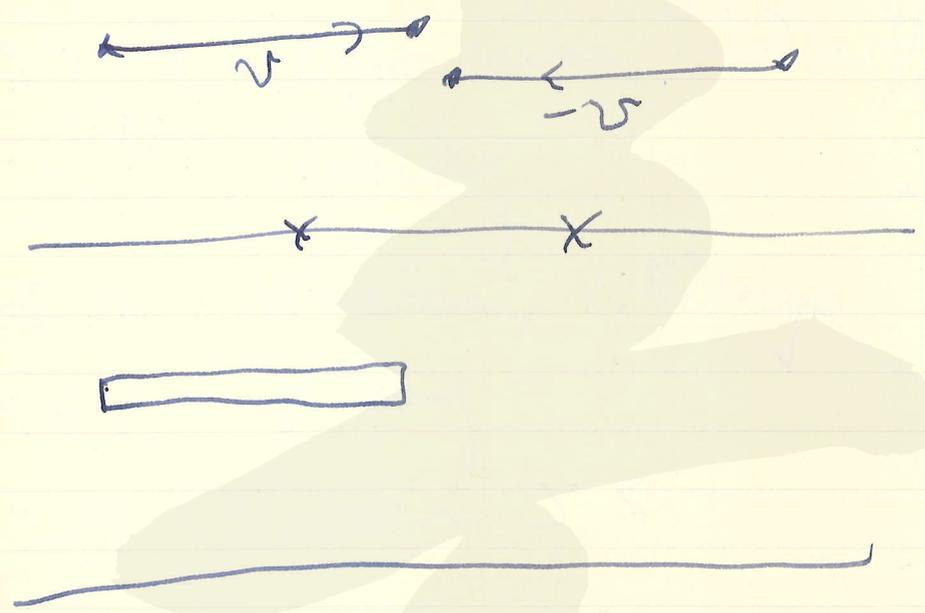
neutron star  $\rightarrow$  crystal  
a few nuclei  
 $10^{14} > \rho > 10^{11}$

Pulsar



“ Lorentz 変換の性質 ”  
 林 忠 = 貞

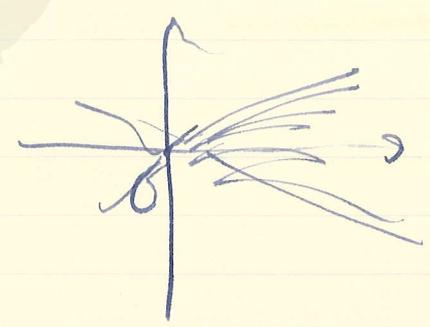
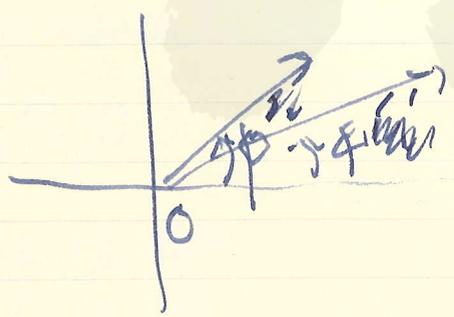
基研 May 25, 1970



1959 Terrel, Phys. Rev.

aberration

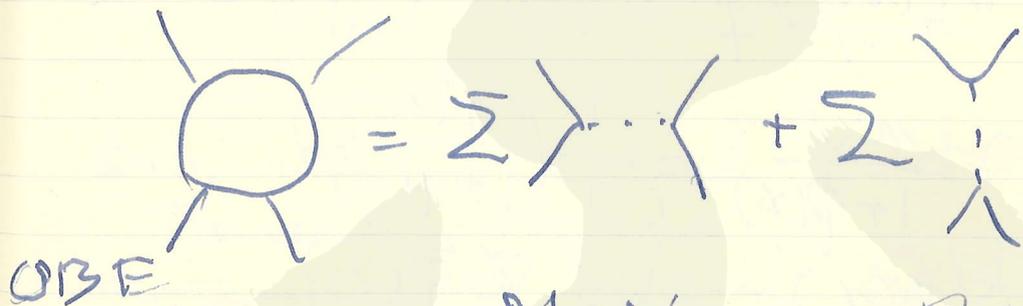
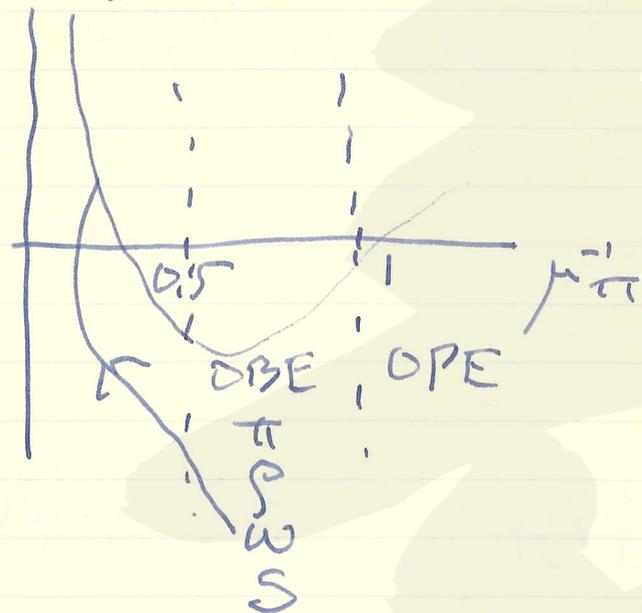
$$\tan \phi' = \frac{\sqrt{1 - v^2/c^2} \sin \phi}{\cos \phi + v/c}$$



核子-核子相互作用と extended particle model

基研 June 9, 1970

$V(r)$  (湯川型  $\sim \frac{1}{r}$ )

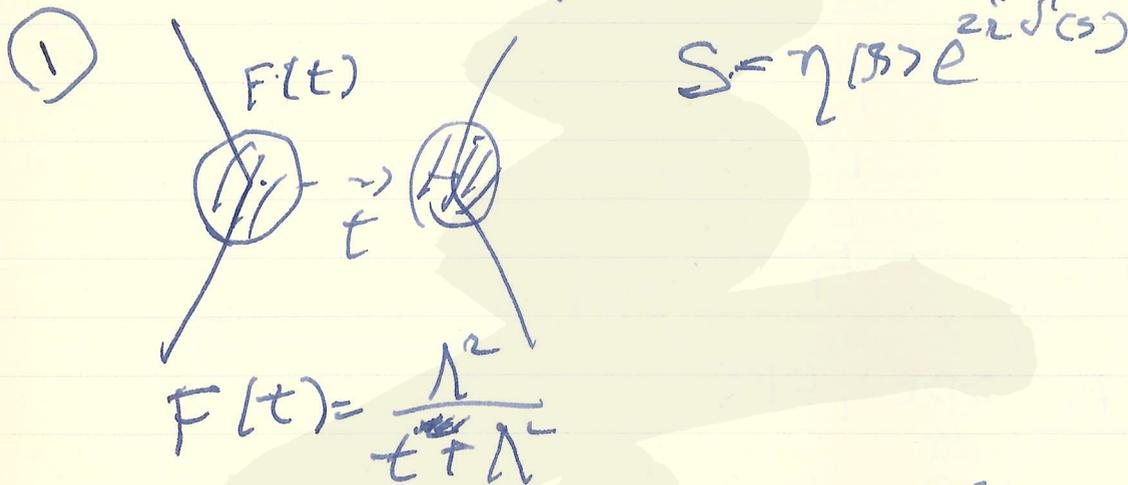


$E_{lab} < 350 \text{ MeV}$

'S<sub>0</sub> 状態の核子-核子相互作用 ...

$P \text{ 状態 } \dots$   
 $g_{\omega}^2 = 6 \sim 10$   
 $g_{\omega}^2 = 25 \sim 35$

- ① 'S<sub>0</sub> form factor  $\tilde{\rho}(k)$
- ② 高エネルギー ( $> 5 \text{ GeV}$ ) にある状態
- ③ non-locality



$$V(r, \nabla) = \bar{V}(r) + V_\Delta(r) \nabla^2 + V_\Delta(r) (\nabla^2)$$

$$\psi'' - \frac{m \ell(\ell+1)}{r} \psi + (p^2 - V_{\text{eff}}(r)) \psi = 0$$

$$V_{\text{eff}}(r) = \frac{m \bar{V}}{1 + \phi(r)} - \frac{1}{4} \left( \frac{\phi'(r)}{1 + \phi(r)} \right)^2$$

$$+ p^2 \frac{\phi(r)}{1 + \phi(r)} + \frac{1}{2} \frac{\nabla^2 \phi(r)}{1 + \phi(r)}$$

$$\phi(r) = \frac{1}{m} \sum_{i=s, v} g_i \frac{e^{-\mu_i r}}{\Lambda_i^2 r}$$

$$\phi^E(r) = \frac{1}{m} \sum_{i=s, v} g_i \left( \frac{\Lambda_i^2}{\Lambda_i^2 - \mu_i^2} \right) \left[ \frac{e^{-\mu_i r}}{r} - \frac{e^{-\Lambda_i r}}{\left( 1 + \frac{\Lambda_i^2 - \mu_i^2}{2\Lambda_i} r \right)} \right]$$

(2)  $\frac{E^{2d}}{T - T_0}$

pp 542V,  $\ln T - T_0 \sim g_{\omega}^2$  for  $T \rightarrow T_0$   
 $\frac{d\sigma}{d\Omega} \sim P, \text{Re}/g_{\mu} : \text{OK}$

Duality  $\sum_s \gamma_s = t\text{-ch Regge}$

H.E. pp =  $\left| \gamma \right| + \text{diffraction}$   
 structure

(3) Non-locality  
 original bilocal field  
 Tanaka-Bando  
 more general bilocal field

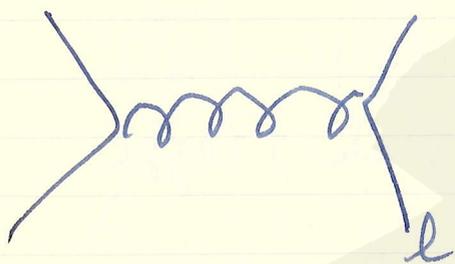
$$\begin{cases} \mathcal{F}(x_{\mu}, x_{\nu} \frac{\partial}{\partial x_{\mu}} (\frac{\partial}{\partial x_{\nu}})^2) U(x, \gamma) = 0 \\ (\square_x + M^2) U = 0 \\ x_{\mu} \frac{\partial}{\partial x_{\mu}} U = 0 \end{cases}$$

Fierz Relation:

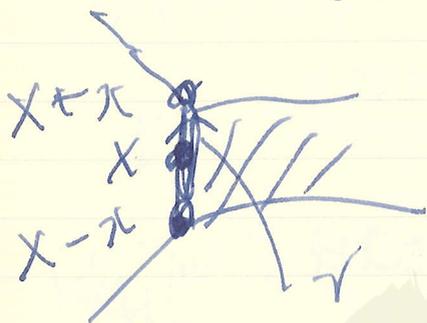
$$U(P, x) = \delta(Px) \sum_{l=0}^{\infty} b_l (x_{\mu_1} - x_{\mu_2})$$

$$x_{\mu_1} - x_{\mu_2} = \mu_l(P, x^2)$$

$$b_l = (-1)^l \frac{(2l+1)!}{4\pi i l}$$



$$H(X) = g \int d^4x \psi^*(X+\pi) \psi(X-\pi) \times U(X, x)$$



$$\begin{aligned} & \langle 0 | U(P, Q) U^*(P', Q') | 0 \rangle \\ &= \delta(P-P') \Delta(P^2, M^2) N(P^2, Z) \\ N(P^2, Z) &= \frac{4\pi}{iP^2} \sum_{l=0}^{\infty} (2l+1) \frac{(h_l(Q))^2}{P^2 (1-Z)} \\ Z &= -1 - \frac{4E^2}{Q^2} = -\frac{Q Q'}{Q^2} \end{aligned}$$

$\downarrow$   
 $h_l(Q) h_l(Q')$

$$h_l(a^2) = \int_0^\infty dr r^{2+l} j_l(\sqrt{a^2} r) j_l(r^2)$$

$a^2 > 0$

$$= \int_0^\infty dr r^{2+l} i_l(-\sqrt{a^2} r) j_l(r^2)$$

$a^2 < 0$

$$i_l(z) = \sqrt{\frac{\pi}{2z}} I_{l+\frac{1}{2}}(z)$$

Practical formula

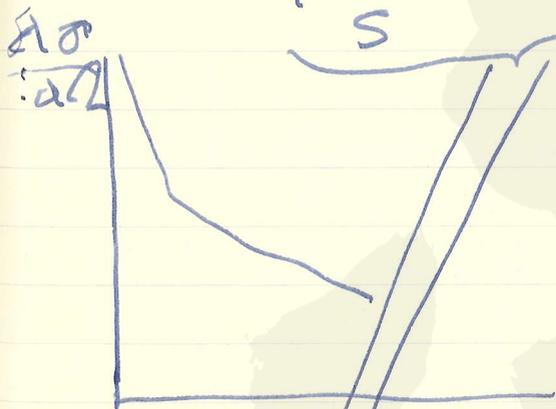
Over

$$5 \text{ GeV} \sim 30 \text{ GeV}$$

$$\frac{d\sigma}{d\Omega} = B p^2 \exp(-\alpha P_T^2)$$

$$+ \frac{A}{s} \exp\left(-\frac{P_T}{p_0}\right)$$

non-pert. part



Re. part  
 bilocal  
 exchange

$$A_{\text{emp}}(p^2, z) = \sum_{n=1}^3 A_n \exp\left(-\frac{\sqrt{-q^2}}{2p_0} x(a_n z + b_n)\right)$$

$$F(p^2) = \left( \frac{\Lambda^2}{p^2 + \Lambda^2} \right) \quad (102)$$

~~Dr. Hori~~

N.C. LXVI A No. 1. (1970) p. 36  
 Unified Treatment of  
 heptons

A. O. Barut, P. Cordaro and  
 G. C. Ghirardi

~~Dr. Hori~~ <sup>Dr. Hori</sup> 6/16/70, 1970

$$O(4, 2)$$

$$O(6)$$

$$\circ \circ \dots \sim SU(4)$$

$$\sum_{a=1}^6 \lambda_a x^a = iuv, \quad \equiv g_{ab} x^a x^b$$

$(a, b = 1, 2, 3, 4; 5, 6)$   
space                      time  
 - - - - + +

15-Generators

$$[L_{ab}, L_{cd}] = -i(g_{ac}L_{bd} + \dots)$$

$$L_{ab} \equiv \frac{i}{2} \gamma_a \gamma_b \quad (a \neq b)$$

$$\gamma_a \equiv (\gamma_1, \gamma_2, \gamma_3, -\gamma_5, \gamma_0, -iI)$$

$$\gamma_5 \equiv \gamma_0 \gamma_1 \gamma_2 \gamma_3$$

$$\gamma_i \equiv \begin{pmatrix} 0 & \sigma_i \\ -\sigma_i & 0 \end{pmatrix}$$

4-dim. repr.  
 $L^{05} \quad J^2 \quad L^{12} \equiv J^3$   
 $n \quad j(j+1) \quad m$

4dim  $\rightarrow n = \pm \frac{1}{2}, j = \frac{1}{2}, m = \pm \frac{1}{2}$

$$j_\mu = \bar{\psi}(x) (\alpha_1 \delta_\mu - i \alpha_2 \overset{\leftrightarrow}{\partial}_\mu) \psi$$

↓

$$O_\mu = \alpha_1 \delta_\mu - \alpha_2 P_\mu + \alpha_6 (\partial P) P_\mu + \alpha_8 (\partial \cdot q) P_\mu$$

$$\left( i \partial_\nu (\delta_\mu \partial_\nu) + \alpha_2 \partial_\mu \partial_\nu - i (\beta \delta_\mu \partial_\nu) \partial^2 - \kappa \right) \psi(x) = 0$$

$$\beta = \alpha_6 + \alpha_8$$

$$\kappa = \beta m_\nu m_\mu$$

$$\beta m^2 - \alpha_2 m^2 + \alpha_1 m - \kappa = 0$$

$m_\nu = 0$   
 $\kappa = 0$  ↓

$$\begin{cases} \beta m^2 - \alpha_2 m + \alpha_1 = 0 \\ m_\nu + m_\mu = \alpha_2 / \alpha_6 \\ m_\nu m_\mu = \alpha_1 / \alpha_6 \end{cases}$$

$$\begin{aligned} & \rightarrow (i \gamma_{\mu} \partial_{\mu} - m_e) (i \gamma_{\mu} \partial_{\mu} - m_e + \frac{\alpha_2}{a_1}) = 0 \\ & \gamma_{\mu} = \gamma_{\mu} - \frac{\alpha_6}{a_2} \beta_{\mu} - \frac{\alpha_6}{a_2} \gamma_{\mu\nu} g^{\nu} \end{aligned}$$

同相相関性  
 因果律の破れと Pomeron 理論  
 の定式化 6月2, 10, 1970

Pomeron 理論  $\rightarrow$  local field theory

non-local field theory

1)  $\sigma_{AB}^{tot}(s) = \sigma_{\bar{A}\bar{B}}^{tot}(s)$   
 ( if  $\lim_{E \rightarrow \infty} \sigma_{AB}^{tot}(E) = \sigma_{AB}^{tot}(s)$   
 $\lim_{E \rightarrow \infty} \sigma_{\bar{A}\bar{B}}^{tot}(E) = \sigma_{\bar{A}\bar{B}}^{tot}(s)$  )

2) Serpukhov 実験結果  
 { P. h. 30 B (69) 500 }

20 GeV  $\sim$  65 GeV

1)  $\pi^- - p, \pi^- - n (= \pi^+ - p)$

$\bar{K}^- - p, \bar{K}^- - n$

$\sigma^{tot}$  は 30 GeV 付近  $\pi^- - p$

$\bar{p} - p, \bar{p} - n$  等 (9:10) (23)

$\sigma(\pi^- - p) = 25 \text{ mb}$

$\sigma(\pi^- - n = \pi^+ - p) = 24 \text{ mb}$

$\sigma(\bar{K}^- - p) = 21 \text{ mb}$

$\sigma(\bar{K}^- - n) = 20 \text{ mb}$

(ii)  $\sigma(\pi^-p) - \sigma(\pi^-n) = \sigma(\pi^+p) = 1.3 \pm 0.7$  <sup>mb</sup>

$\sigma(\bar{K}^-p) - \sigma(\bar{K}^-n) = (3 \sim 4)$  mb

↑  
 20 GeV 以上 extrapolate  
 ↓  
 17 mb

$\sigma(\bar{K}^-p) - \sigma(\bar{K}^-n) \approx 1.0 \pm 0.6$  <sup>mb</sup>

3) Power Theor. of  $1/s$

Soviet Physics JETP 11(158)

499  
 高エネルギーの強相互作用  
 河原林 久

dispersion relation  $F(E, 0)$  analytic or  
 microcausality

(charge-independence  
 unitarity)

$\lim_{E \rightarrow \infty} \frac{F(E, 0)}{E} = \text{const.}$

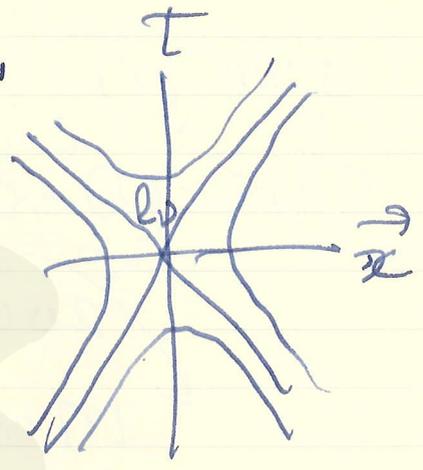
4) micro-causality

$[A(x_1), B(x_2)] = 0$

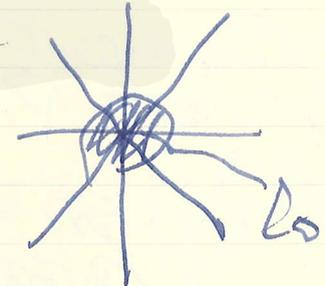
相対論的因果性

$x_1, x_2$   
 i-space-like

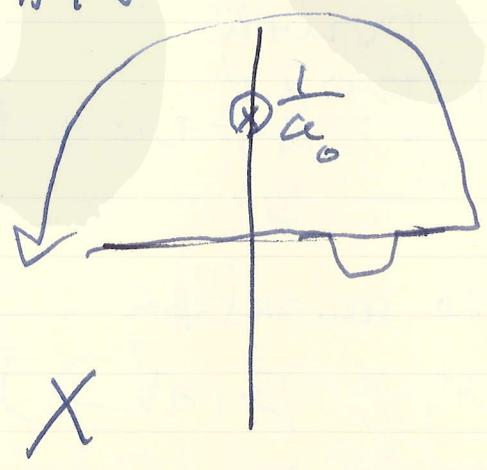
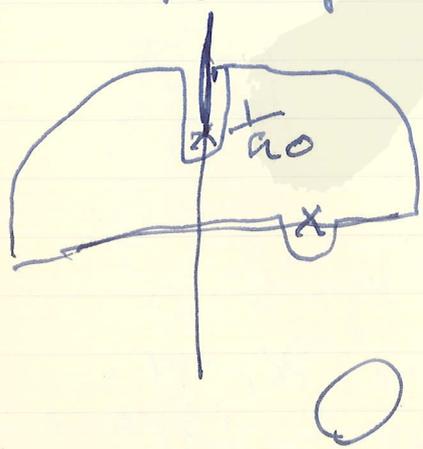
i)  $|x^2| < c^2 t^2$  光速度



ii) Blochintan, 固地  
 time-like vector  
 $|x^2 - 2(n^2)^2| < c^2 t^2$   
 $n(1, 0, 0, 0)$



1) 相互作用の素粒子  
 論述している内容  
 完全な相互作用の方向  
 2) 真空に存在している内容  
 n の方向に存在する方向



DI.

Blochintsev and G. T. Kolesov

~~DI.~~ D. C. 34 (1964), 163

spectral condition

$$p_\mu p^\mu = p_0^2 - \vec{p}^2 = m^2 > 0$$

$$p_0 \geq 0$$

$$p = \frac{\omega}{\sqrt{\omega^2 + \Omega^2}}$$

$$\Omega = \frac{1}{a_0}$$

$\pi^+ - \pi^- :$

$$a_+(\omega) - a_-(\omega) = 8\pi \left[ \right]$$

$$a_0 \sim 10^{-15} \text{ cm}$$

混雑中

July 16, 1970

Field:

lepton: Barut

QED: Lee-Wick  
indefinite metric

$\Gamma_\mu(p, q)$   
weak lepton current  $\left\{ \begin{array}{l} p = p_1 + p_2 \\ q = p_1 - p_2 \end{array} \right.$

$\int \Gamma_\mu = 0 \Rightarrow$  3種  $\nu$  と  $e, \mu$

$$f(m) = 0$$

lepton  $m_i \quad i \geq 3$

$$f(\sigma p) \psi(p) = 0$$

$$f(m_i) = 0$$

$$f(x) = e^{g(x^2)} \prod_{i=1}^{\infty} (x - m_i)$$

$$f(\sigma p) = (\sigma p - \nu_1)(\sigma p - \nu_2)(\sigma p - m_e) \\ \times (\sigma p - m_\mu) f(\sigma p)$$

$\nu_1, m_e$ : positive metric

$\nu_2, m_\mu$ : negative metric

Unitary

$$\langle x | (-i)^{\bar{a}a} \dots | x \rangle \quad \text{positive}$$

"  $\eta$

$N_{\mu} + N_{\nu} = \text{invariant}$

- ① muon number of (28/28)  
 (e-number of (28/28))

electromag. current

$$f(\sigma p) \psi(p) = 0$$

$$\sigma p \rightarrow \sigma(p - eA)$$

②  $v_1 = v_2$

$$(\sigma p - v)^2$$

- ③ neutral current  $\rightarrow$  no effect

weak current

$$F_{\lambda}^W = g \left( \frac{p_1^2 + p_2^2}{2}, p_3 \right) \gamma_{\lambda} \frac{1 + \gamma_5}{2}$$

$$g(m_1^2 + m_2^2, m_1^2 - m_2^2)$$

$$g(\mathbf{p}, \mathbf{q}) = \sqrt{\frac{G}{(pq)}} \prod \left( \frac{p^2 + q^2}{2} - m_{2i}^2 - m_{2j}^2 - 1 \right)$$

③ universality  
 $\langle ev \rangle, \langle \mu v \rangle$   
 $\sqrt{m_{\nu}^2 - m_{\nu'}^2}$  order

Dirac,  $e, \mu$  QED



$$\sigma_{\mu} \rightarrow z, \frac{\partial}{\partial z}, p, \frac{\partial}{\partial p}$$

$$[P_{\mu} \frac{\partial}{\partial x} + \kappa] \psi = 0$$

$$[L_{\mu}, P_{\nu}] = S_{\mu\nu}$$

$$(S_{\mu\nu}, P_{\nu}) \rightarrow O(4,1)$$

(spin  
 mag. mom  $\rightarrow$  Zitterbewegung

$$\langle \psi | = \mathcal{H} R \psi$$



坂沢幸男 (Univ. Michigan)  
 W-Boson

基礎講演会 Aug. 11, 1970

Vector type charged  $W_\mu$ ,  $m_W \sim 3 \sim 5 \text{ GeV}$

1958 V-A theory  
 G. F. S. M.

$$H_W = G_F / \sqrt{2} J_\mu^\dagger J_\mu$$

$$J_\mu = J_\mu^{\Delta S=0} + J_\mu^{\Delta S=1} + l_\mu$$

lepton current

leptonic  
 semi-leptonic

$$J_\mu = V_\mu + A_\mu$$

$$l_\mu = \left( \bar{\nu}_\mu \right) \gamma_\mu (1 + \gamma_5) \nu$$

$$H = g J_\mu W_\mu$$

$$\frac{g^2}{M_W^2} = \frac{G_F}{\sqrt{2}}$$

$$G_F = 10^{-5} \text{ M}_N^{-2}$$

non-leptonic

$$H_{NL} = \frac{G_F}{\sqrt{2}} J_\mu^{\Delta S=0} J_\mu^{\Delta S=1}$$

G. h. C.  $\sqrt{\frac{1}{4}}$   
 angle  $\frac{1}{4}$

④ 群:  $U(1) \times SU(2) \times SU(3)$  の破れ

1)  $U(1) \times SU(2)$  real  $\rightarrow$

2)  $SU(3)$

$$8 \times 8 = 1 + 8 + \dots + 27$$

$$\Delta I = 3/2 \quad \text{etc.}$$

3) CP violation (etc. あり)

$K_L \rightarrow 2\pi$

$SU(3)$  から出現する破れ  $\rightarrow$  CP 破れ

W-boson の質量

$$M_W = \frac{1}{2} g v$$

$$(J_\mu)_P = \bar{q}^a \gamma_\mu (1 + \gamma_5) q^b$$

$$M_W = 10 \text{ GeV} \sim 60 \text{ GeV}$$

W: octet of  $SU(3)$

Pines, Neutron Star  
Sept. 1970

Lichtenberg, quark-like  
model  
Sept. 1970

河津原 邦子 同  
sept. 16, 1970

gd: Quark-like - -

1970年代: duality

W. Alessandrini et. al.

C. Lovelace



Reggeon

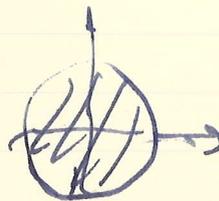
$$V_{ij}(p_i, a_i^n, p_j) \sim$$

$$p_{ij}(a_i^n)$$

$$p = a_i^n$$

↓  
 $a_i$

Dirichlet product



宇子重子化

田中

handwritten '90  
 spin statistics  
 superselection rule  
 Sept. 24, 1970

Doplicher  
 Haag-Roberts  
 '69  
 Drühl-Haag  
 Roberts '73

comm.  
 or  
 anticomm.

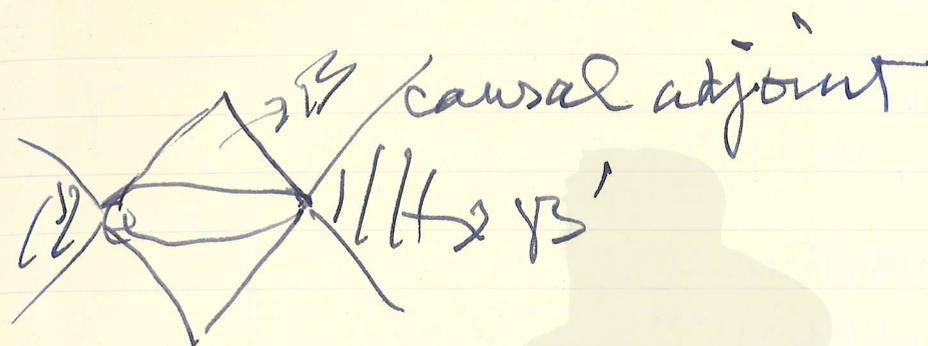
- Wightman field
1. 真空 field of covariant field of finite comp
  2. 2-body infinite field component free
  3. para statistics (Green field)

Local Algebra



$\mathcal{B}_1 \supset \mathcal{B}_2$   
 space-like  $\mathcal{P}_0 = 0$   
 $\mathcal{B}_1, \mathcal{B}_2$  :  $\mathcal{O}(\mathcal{B}_1) \times \mathcal{O}(\mathcal{B}_2)$   
 $\rightarrow$  commute

Observable algebra  
 Field algebra  $\mathcal{F}(\mathcal{B})$



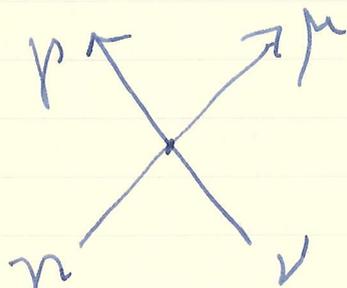
duality

谷川先生の: Weak Interaction

第4回, 混沌化  
 Oct. 15, 1970

Simple Structure

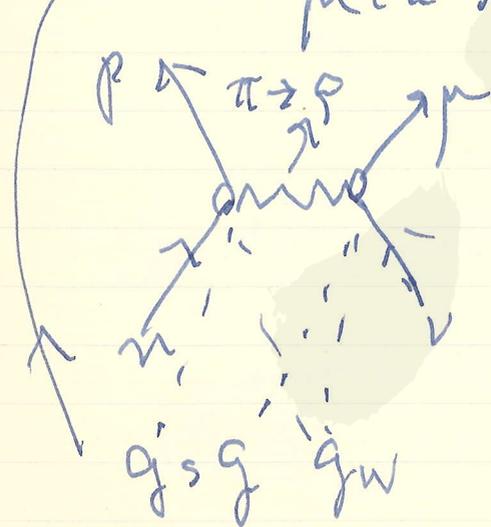
1) Fermi Interaction V-A



$G \bar{p} \gamma_{\mu} (1 + \gamma_5) n \bar{\pi} \gamma_{\mu} \nu$   
 V helicity -  
 two component

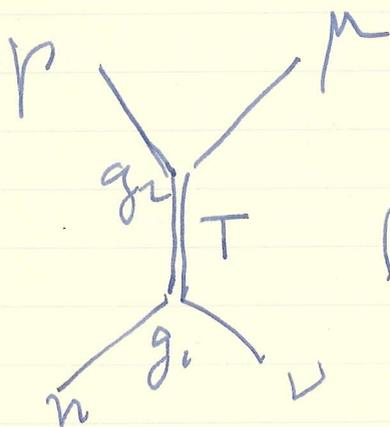
2) Yukawa-Ogawa-V-G.  
 Vector boson theory

$$g_w^2 \bar{p}(x) \gamma_{\mu} (1 + \gamma_5) n(x) \frac{D_{\mu\nu}(x-x')}{m^2} \bar{\pi}(x') \gamma_{\mu} \nu(x')$$



revival  
 V-A ~~T~~ weak boson

3) Tanikawa-Watanabe



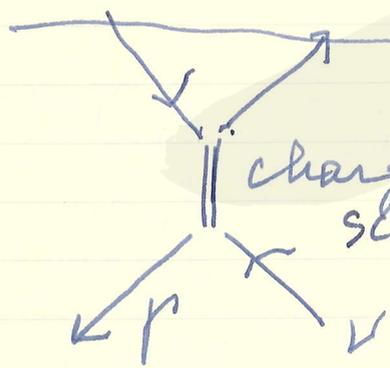
neutral scalar

$$g_1 g_2 \bar{p}(x) (1 - \gamma_5) \psi(x) \times D(x-x') \bar{\nu}(x') n(x')$$

V-A

(Fierz - Pauli 交換)

$\nu + n \rightarrow p + \mu$  resonance



$$f_1 f_2 \bar{p}(x) \psi(x) D(x-x') \bar{\nu}(x') (1 - \gamma_5) n(x')$$

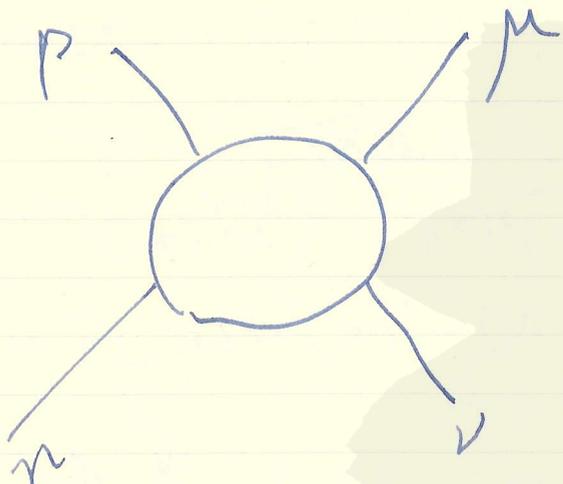
V+A

$\nu + \bar{p} \rightarrow \bar{n} + \mu$  resonance

neutral spin 1  $\nabla + A$

charged spin 1  
 vector  $V - A$

general structure

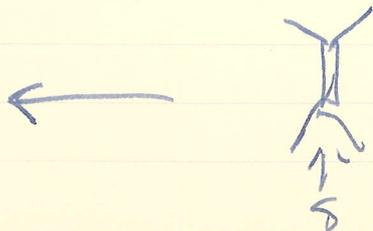


$$\begin{aligned}
 & \sqrt{m_\nu p_\nu} \langle \mu p | T | \nu n \rangle \sqrt{v_\nu n_\nu} \\
 &= \bar{p} \left( F_V \gamma_\mu - \frac{F_V'}{M} \sigma_{\mu\nu} \gamma_\nu - i \frac{F_S}{m_\mu} \gamma_\mu \right) n \\
 & \quad \text{muon spinor} \quad \times \quad \bar{\mu} \sigma_{\mu\nu} \\
 &+ \bar{p} \left( F_A \gamma_\mu \gamma_5 - \frac{i F_P}{m_\mu} \gamma_5 \gamma_\mu \right) n - \bar{\mu} \gamma_\mu \nu \\
 &+ (\bar{p} F_T \sigma_{\mu\nu} n) \bar{\mu} \sigma_{\mu\nu} \nu + \dots
 \end{aligned}$$

CP invariance

$$F_V(t), F_A(t) = \left( \frac{1}{1 + \frac{t}{M^2}} \right)^2 \quad \rightarrow t \quad \text{[scribble]}$$

resonance  
 kinoshita あり



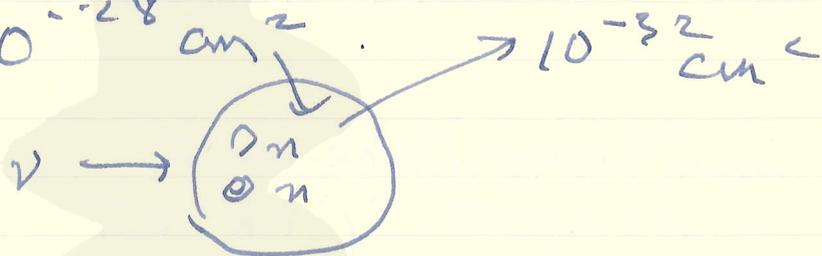
CEBNの實驗

$\nu_0 \sim 2 \text{ GeV}$   
 Kuroshita

$\sigma_{\text{res}} \approx 10^{-28} \text{ cm}^2$

$10^{-38} \text{ cm}^2$

$\pi^-$  resonance



$|g_1|^2 \ll |g_2|^2$  ;  $\frac{g_1 g_2}{M^2} = \frac{G}{\sqrt{2}}$   
 $\frac{g_2^2}{\pi G} < 10^{-13}$

$\rightarrow \frac{g_1^2}{\pi G} > 10^{-9} \rightarrow 10^{-35} \text{ cm}^2$

duality

$\sum_n \left( \begin{matrix} s \\ w_n \\ A_1 \end{matrix} \right) = \sum_n \left( \begin{matrix} t \\ T \\ \text{spin } 1 \\ \text{spin } 0 \end{matrix} \right)$

$\sum_n \frac{\rho_n(s)}{t-t_n} = \sum_n \frac{C_n(t)}{s-s_n}$

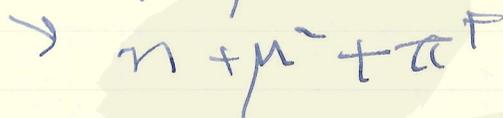
Saito model

$F_\nu(\tau, s) = \sum_n \frac{h_n^\nu(s)}{t-t_n}$

$F_\nu(0, M^2) = \sum_n \frac{h_n^\nu(M^2)}{0-t_n} = G$  (Fermi constant)

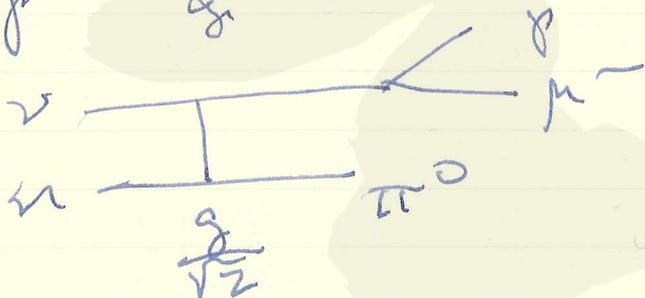
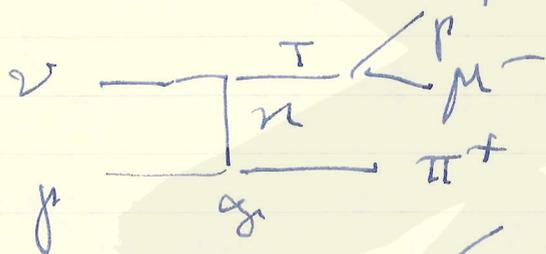
$$= \sum_n \frac{C_n^V(\omega)}{M^2 - S_n}$$

Tani-Kenwa-Nakamura



(1)

(2)



参考文献: Saito Model

$$F_V(s, t) = \frac{G}{\sqrt{2}} \left[ V_1 \frac{\Gamma(1 - \alpha_T(s)) \Gamma(1 - \alpha_P(t))}{\Gamma(2 - \alpha_T(s) - \alpha_P(t))} - V_2 \frac{\Gamma(1 - \alpha_T(s)) \Gamma(1 - \alpha_{P'}(t))}{\Gamma(2 - \alpha_T(s) - \alpha_{P'}(t))} \right]$$

$$\alpha_T(s) = \frac{1}{3} \alpha (s - M_T^2) + 1$$

$$\alpha_p(t) = t + \sqrt{2}$$

$$\alpha_{p'}(t) = t + 0.4$$

山崎 啓一

量子論による重力の量子化  
 と重力場の量子化

基礎 ①

Nov. 10, 1970

Dicke-Goldenberg  
 重力場の量子化

①  $5 \times 10^{-5}$   
 8% くらい

harmonic coordinate → 重力場

1 次元の flat

$$H = \frac{p^2}{2m} - \frac{p^4}{8c^2 m^3} - \frac{GMm}{r} - \frac{3GM}{2m} \frac{p^2}{r} + \frac{G^2}{2c^2} \frac{mM^2}{r^2}$$

2 次元の場合 (Einstein-Hilbert  
 reffermann  
 2 Stück)

$$H = \frac{1}{2} \left( \frac{p_1^2}{m_1} + \frac{p_2^2}{m_2} \right) - \frac{1}{8c} \left( \frac{p_1^4}{m_1^3} + \frac{p_2^4}{m_2^3} \right)$$

$$\left[ \frac{Gm_1 m_2}{2c^2 r} \right] + \frac{G^2 m_1 m_2 (m_1 + m_2)}{2c^4 r^2}$$

~~~~~

$\int \sqrt{-g}$

massless spin 2

Gauge invariance

→ conserved-energy-momentum

& couple to

→ self-interaction  $\leftrightarrow$   $T_{\mu\nu}$

scalar source  $\leftrightarrow$   $T_{\mu\nu}$

$\int \sqrt{-g}$

$\int T_{\mu\nu}$

~~$\int T_{\mu\nu}$~~

$\int \sqrt{-g}$   
 $\otimes$   
 $\int T_{\mu\nu}$

Einstein's equation  $R_{\mu\nu} - \frac{1}{2}Rg_{\mu\nu} = 8\pi T_{\mu\nu}$

spinor particle source  $\leftrightarrow$   $T_{\mu\nu}$

$g^{\mu\nu} T_{\mu\nu}$  is conserved

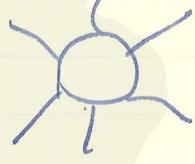
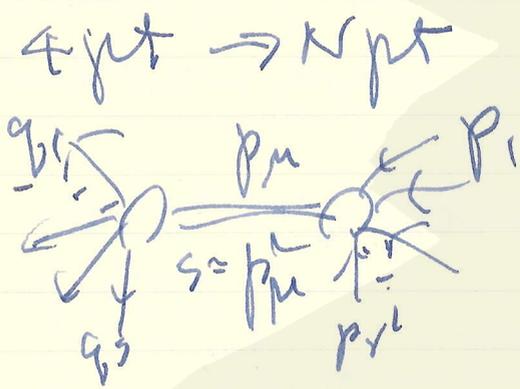
Bergmann-Wigner with  
 Tasso

$$\frac{N}{6} \times \text{Einstein}$$

# General behavior structure of dual Resonance Model with J. Soifer (CERN)

位相空間

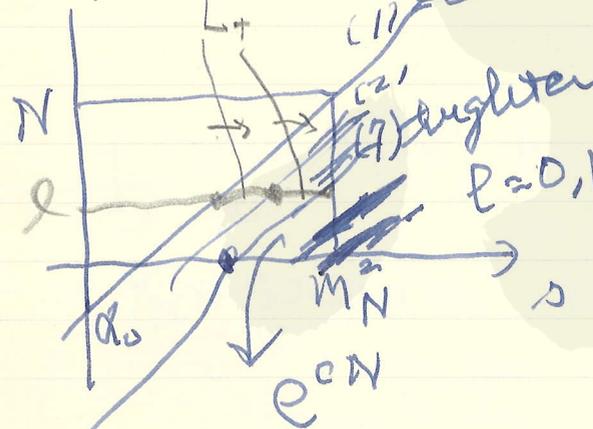
Nov. 10, 1970



factorization  
 prop.

$$\sum_i g(q_i) f(p_i)$$

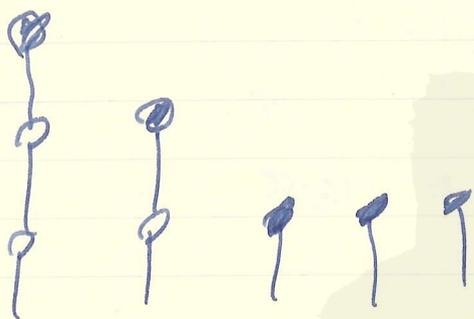
→ enormous degeneracy



$$\alpha(s) = \alpha' s + \alpha_0$$

gauge conditions → removal  
 of spurious states

ghost (gauge cond.  $\epsilon^{\mu\nu\rho\sigma} \dots$ )



$$[a_\mu^{(m)}, a_\nu^{(n)}] = g_{\mu\nu} \delta_{mn}$$

$$g_{00} = -g_{ii} = 1$$

$$a_\mu^{(m)} |0\rangle = 0$$

occupation number space

$$\langle \Phi | \eta | \Psi \rangle \quad \prod_{n=1}^{\infty} \eta = (-1)^{\sum_{n=1}^{\infty} a^{(n)} + a^{(n)}}$$

$$h_0(p) = \sum_n a^{(n-1)} a^{(n)} - \alpha' p^2$$

$$h_+(p) = \sum \sqrt{n(n+1)} a^{(n+1)} a^{(n)} + p a^{(1)}$$

$$h_-(p) = \sum \sqrt{n} a^{(n)} a^{(n+1)} - p a^{(1)}$$

$$\left\{ \begin{array}{l} [h_0, h_\pm] = \pm h_\pm \\ [h_+, h_-] = -2h_0 \end{array} \right\} \begin{array}{l} SO(2, 1) \\ \text{or} \\ SU(1, 1) \end{array}$$

twisting operator  $\Omega(p)$

$$\left. \begin{array}{l} \Omega(p) = e^{h_+} (-1)^{\sum_{n=1}^{\infty} a^{(n)}} = (-1)^N e^{-h_+} \\ \Omega^+(p) = (-1)^{\sum_{n=1}^{\infty} a^{(n)}} e^{h_-} \\ \Omega^2 = \Omega^{+2} = 1 \end{array} \right\}$$

$$A(p) \equiv h_0(p) - h_-(p)$$

resonance states at rest

$$p_\mu = (m_N, \vec{0})$$

# 湯川秀樹

NOV. 26, 1970

物 = 理論 : 学歴史

1952 卒業 (文理学部)

1932 ~ 1952

Meis, Yukawa, Fermi

- 2400g  
Field Theory

~ 1950



(1) 異質性 - strangeness

→ 相互作用 → quantum

(2) parity violation - V-A

(3) "Regge" 物理

(1) SU4-physics

(2) IBY-physics

# 湯川記念館

1970年 12月 17日 ~ 19日

基研. 小浜義克

17日 午前 姓名 湯川

片山氏: 歴史的概観.

1. 双対変数  $\alpha$  と  $\beta$  の関係に  $\delta(\alpha - \beta)$  のような  
reciprocity

$\gamma_\mu$ : space-like vector として導入.

2. 内部自由度 (新自由度) は 湯川-記述の

$\gamma$  の  $\alpha$  と  $\beta$  の可換性.

$\pi \in \mathbb{R}^4$  の内部自由度.

双対性.

bilocality

$$\frac{1}{4} \epsilon_{\mu\nu\rho\sigma} S^{\mu\nu} S^{\rho\sigma} = 0 \rightarrow \text{integer spin}$$

3.  $\pi \in \mathbb{R}^4$  の記述形式

中群は:

群の対称性.

parameter group

湯川氏:

bose 対称性 → fermi ...

湯川氏:

Zitterbewegung

Vierbein

charge of fusion

→ spinor  $\psi$  の  $z$  成分

$$b_{\mu}^{\dagger} \propto P_{\mu} \quad (\text{原})$$

$b_{\mu}$

真空  $\Omega$

proper time  $\tau$  の

真空

$\langle \psi | \psi \rangle = 1$

Dirac 方程式

Dirac 方程式

17日午後、先生、田・P-5

弦理論: 無限次元?

duality

string

詩歌的方程式

弦理論と相互作用

indefinite metric

$$-1 \leq \alpha \leq 1$$

$$\{x_{\mu}(\alpha), \pi_{\nu}(\alpha')\}$$

$$= i g_{\mu\nu} \delta(\alpha - \alpha')$$

$$\{x_{\mu}(\alpha), x_{\nu}(\alpha')\} = \{\pi_{\mu}(\alpha), \pi_{\nu}(\alpha')\} = 0$$

$$\mathcal{F}[x_\mu(u)]$$

$$P_\mu = \int_{-1}^1 \pi_\mu(u) du$$

$$[x_\mu(u), P_\nu] = i g_{\mu\nu}$$

$$M_{\mu\nu} = \int_{-1}^1 x_\mu(u) \pi_\nu(u) du$$

$x_0(u)$  : 弦の位置関数の  $u$  成分

$$X_\mu = \int_{-1}^1 f(u) x_\mu(u) du$$

$$\int_{-1}^1 f(u) du = 1$$

弦の運動方程式 (弦の位置関数の方程式)  
 $H(u) \Psi = 0$

$$H(u) = \pi(u)^2 + \left(\frac{dx}{du}\right)^2 + \mathcal{F}(u)$$

global 上の運動方程式  
 global 上の可積分性

$$[H(u_1), H(u_2)] = \int_{-1}^1 K(u_1, u_2, u') H(u') du'$$

$$H(u) = \frac{\pi(1-u^2)}{2} \left[ \frac{\pi(u)^2}{\kappa} + \kappa \left(\frac{dx(u)}{du}\right)^2 \right]$$

$$- \frac{i}{2} \int_{-1}^1 (1-u'^2) \left\{ \frac{dx(u')}{du'} \pi(u') \right\} \frac{du'}{u-u'} + w_0$$

principal value

$$[H(u_1), H(u_2)] = \frac{z(1-u_1 u_2)}{(u_1 - u_2)^2} (H(u_1) - H(u_2))$$

$$- \frac{1}{u_1 - u_2} \left[ (1-u_1^2) \frac{dH(u_1)}{du_1} + (1-u_2^2) \frac{dH(u_2)}{du_2} \right]$$

$$\pi(u) \Leftrightarrow \kappa \frac{d\chi(u)}{du} \quad \text{symmetry}$$

$$\frac{dw(u)}{x(w)} \quad \pi(w) = \left| \frac{du}{dw} \right| \pi(u)$$

$$u = \cos \sigma \quad i \in \mathbb{Z} \quad 0 \leq \sigma \leq \pi$$

$$Z_\mu(\sigma) = \sum_{r=0}^{\infty} z^r \cos r\sigma$$

$$P_\mu(\sigma) = \frac{1}{\pi \lambda_0} \left( \frac{1}{2} \pi^0 + \sum_{r=1}^{\infty} a^r \cos r\sigma \right)$$

$$[Z_\mu^r, \pi_\nu^s] = i \delta_{rs} g^{\mu\nu}$$

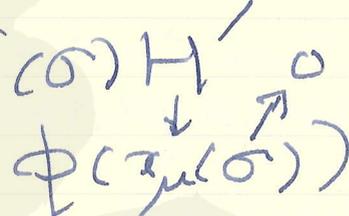
Veneziano: mass spectrum  
 oscillator model

plus  $\infty$  number of subsidiary  
 conditions

external scalar field

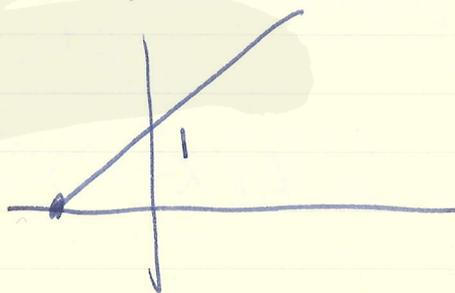
$$\phi(x)$$


$$\hat{H}(\sigma)\Psi = 0$$

$$\hat{H}(\sigma) = H(\sigma) + g\delta(\sigma)H' \quad \phi(x_{\mu}(\sigma))$$


imaginary mass

$$\log N \sim \frac{1}{2} \log \frac{1}{\epsilon}$$



FRK:

1. Rigid Body

$$H = \frac{1}{2I} S^2$$

half-integer spin

$J = \frac{1}{2} \Rightarrow$  2-component spinor

spinor 2-component spinor

Weyl spinor:  $SL(2, \mathbb{C})$  spinor 2-component

Euler angle & complex

$SL(2, \mathbb{C}) \rightarrow$  inversion

Dirac spinor

$K = \pm \frac{1}{2}$ : particle-antiparticle

2. deformable body  
 non-uniform deformation  
 spin integer  
 spin half-integer  
 SU<sub>3</sub>

3. Interaction

i) Propagator  $H = \sum_n n a^{\dagger n} a^n$

ii) vertex

$$e^{ikx} \left[ \sqrt{\frac{2}{n}} (a^n + a^{\dagger n}) + x \right]$$

$$\int A(x+u) \delta q \rightarrow \mathcal{Q} A(x+u)$$

$\chi(\mu, \sigma)$  Lagrange  $\delta q$

$\sigma$  or  $\tilde{\sigma}$   $\tilde{\sigma} = \gamma \sigma \gamma$  covariance,  
 Klein of  $S = \mathcal{K} \tilde{\sigma}$  or

$$\sigma \rightarrow \sigma' = \sigma + \epsilon \sum_{p=-\infty}^{\infty} \tilde{\sigma}^p e^{ipx}$$

3- $\tilde{\sigma}$  Lorentz  $\tilde{\sigma}$  (10)

後  $\tilde{\sigma}$  : 関数

第2回. 1810  
 午前. 11時 大講  
 講師: heptonの内部構造  
 1. 構造  
 2. 相互作用  
 3. 実験

I. Q.E.D. の test

QED

photon propagator

lepton

vertex

$$\frac{1}{q^2 + \Lambda_1^2} - \frac{1}{q^2 + \Lambda_2^2}$$

$$\frac{1}{q^2 + \Lambda_3^2}$$

$$\frac{1}{q^2 + \Lambda_2^2}$$

$$\frac{1}{q^2 + \Lambda_3^2}$$

$\mu$  の a.m.m. :

$$a = \frac{q-2}{2}$$

$$\Delta a = a_{exp} - a_{th} = (29.534) \times 10^{-8}$$

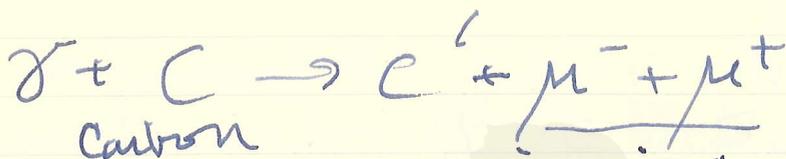
$$\Lambda_1 \geq 3.6 \text{ GeV}$$

$$\Lambda_2 \geq 10 \text{ GeV}$$

$$\Lambda_3 \geq 5 \text{ GeV}$$

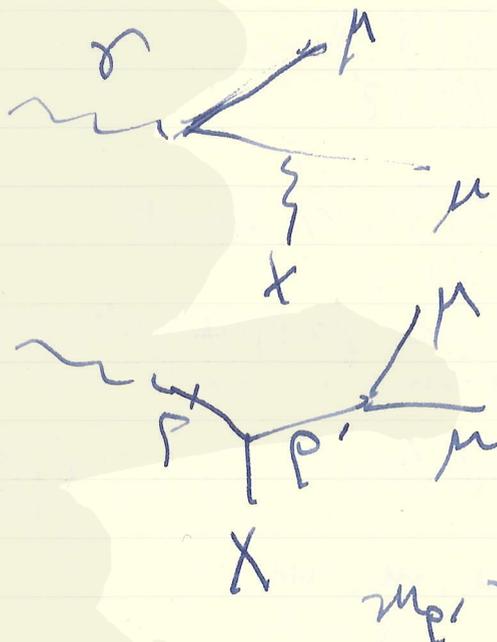
e-e } scattering  $\rightarrow$   $\left\{ \begin{array}{l} D_F^{(0)} \\ D_F^{(1)} \\ D_F^{(2)} \end{array} \right.$   
 e- $\mu$   
 $\mu$ - $\mu$

$$\left( \frac{\Lambda_1^2}{q^2(q^2 + \Lambda_1^2)} \right)^2 \left( \frac{\Lambda_2^2}{q^2 + \Lambda_2^2} \right)^4$$



invariant mass  $2\text{ GeV} \sim 2\text{ GeV}$  (高エネルギー)

A.E.D. の半径  
 $D \leq 9 \times 10^{-15} \text{ cm}$

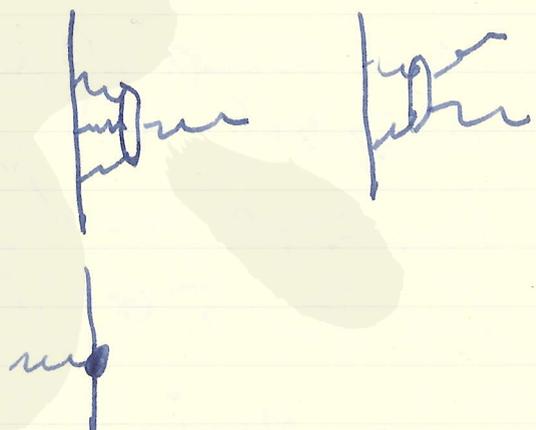


lepton on a  $\mu$   $\mu$   $\mu$  :  
 photon  $\rightarrow$   $\mu$   $\mu$   $\mu$

electric polarizability

$$H \sim \frac{1}{2} \alpha E^2$$

magnetic " "  
 $\frac{1}{2} \beta H^2$   
 $\frac{1}{2} \gamma E H$



II, Weak Interaction  
 weak boson mass  $\geq 5 \text{ GeV}$

CERN

$$\nu + n \rightarrow \mu^- + p$$

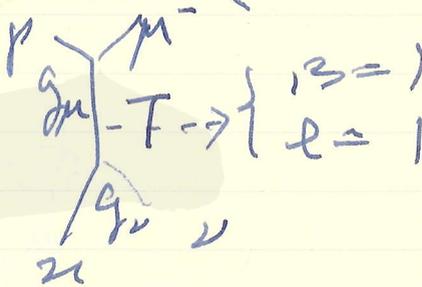
$$M_T \sim 200 \text{ GeV} \text{ (Tanikawa boson)}$$

Resolution 100 MeV

$$\sigma_{obs} \sim \frac{2}{3} \times 10^{-38} \text{ cm}^2$$

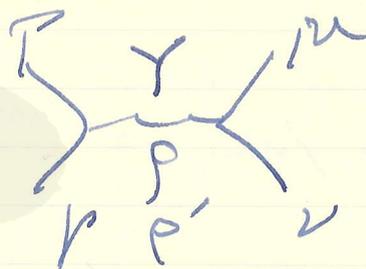
Hakawaki - Saito - Tanikawa

$$\frac{G'}{\sqrt{2}} \equiv \frac{g_\mu g_\nu}{M_T^2} < 10^{-8} M_N^{-2} \sim G' 10^{-3}$$



$\nu + A$ : superweak  
 $\Gamma \sim 10^{-3} \text{ eV}$

duality  
 T-Y duality



V-A theory

$$\bar{\psi}_A \psi_B \quad \bar{\psi}_C \psi_D$$



neutral current ( $e \nu (e \nu)$ ) ?

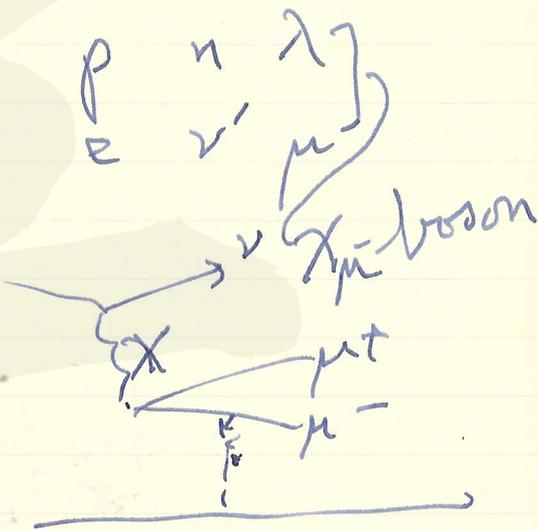
(III)  $\mu$ -e difference

mass

$(\nu_{\mu} \mu)$   $(\nu_e e)$   
 $m_{\nu_{\mu}} \leq 5 \text{ MeV}$

$m_{\nu_e} \leq 60 \text{ eV}$

$$\frac{f_X}{m_X^2}$$



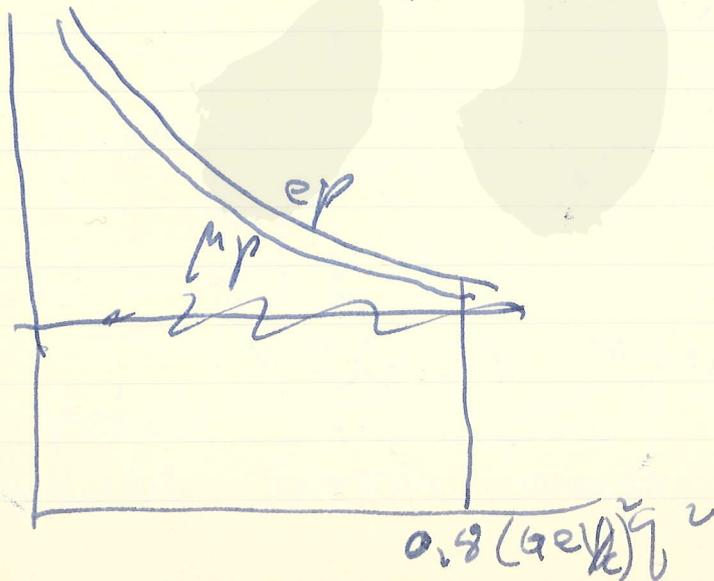
---


$$m_{\nu_{\mu}}/m_{\nu_e} = m_{\mu}/m_e \quad \text{if } \nu_{\mu} \text{ and } \nu_e \text{ are } \nu_{\mu} \text{ and } \nu_e$$


---

for  $\nu_{\mu}$  and  $\nu_e$

$\nu_e, \nu_{\mu}$  scatt



Lepton symmetry  
 $e^*$   
 $\mu^*$  ?

$$\begin{aligned} \textcircled{1} \quad \nu_1 &= \cos\theta \nu_e + \sin\theta \nu_\mu \\ \times \quad \nu_2 &= -\sin\theta \nu_e + \cos\theta \nu_\mu \end{aligned}$$

$e^+$   $\nu_1$   $\nu_2$   $\mu^+$   
 $p$   $n$   $\lambda$   $\chi'$

$SU(3) \times U(1)$   
 $SU(2) \times SU(2)$

Maki

注 14.6 :

hadron 現象 a theory

chiral symmetry  $\rightarrow$  current conservation  
 strong  $\rightarrow$  weak  
 weak  $\rightarrow$  electromagnetic

chirality  $\rightarrow \partial A = C \pi$

C. A. + PCAC Treatment  $\rightarrow$  low energy theorem (1965-67)

Weinberg effective Lagrangian  
 $SU(2) \times SU(2)$  ( $m_q \rightarrow 0$ )

i) chiral symmetry +  $\pi$  (N.G. Boson)

$$\langle 0 | A_\mu | \pi \rangle = i F_\pi f_\pi$$

$$\left. \begin{aligned} m_\pi^2 &= 0 \\ f_\pi &\neq 0 \end{aligned} \right\}$$

ii) C.S.  $a^2 \delta^2 \alpha$

$$\partial A = g \partial \alpha$$

$$m_\pi^2 = EM(E)$$

$$M(0) \neq 0$$

$$E \ll M$$

$$m_\pi \ll E$$

Skuba

$E \sim$  ultraviolet bare mass

$u, d : 9 \text{ MeV}$

$s : 150 \text{ MeV}$

ii) ~~skuba~~ phase transition

$$\langle 0 | A_\mu(0) | \pi \rangle \neq 0$$

iii)  $A, V \rightarrow$



current & locality

光の 散乱 収  
 1/2 1/2 1/2  
 ... 1/2 1/2 1/2

核子との相互作用 → 散乱 1/2 1/2  
 Nucleon Compton Scat

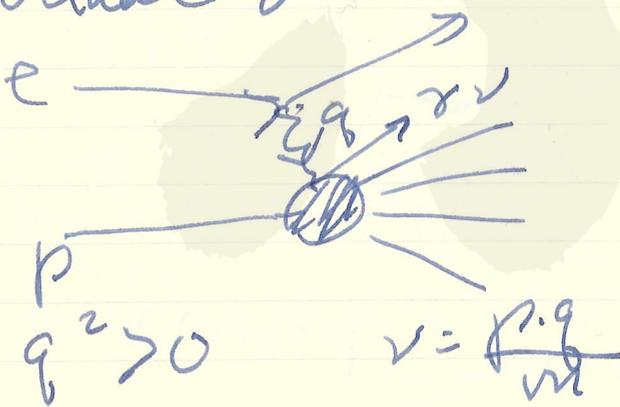
$$\sigma_T(\sigma p) = 24 + \frac{24.6}{\sqrt{v}} \mu b \quad \leftarrow \frac{1}{2}$$

$$\sigma_T(\sigma n) = 25 + \frac{24.6}{\sqrt{v}} \mu b \quad \leftarrow \frac{2}{3}$$

$$\sigma_T(\sigma p) - \sigma_T(\sigma n) = \frac{24.6}{\sqrt{v}} \mu b \quad \leftarrow \frac{1}{3}$$



virtual  $\sigma$



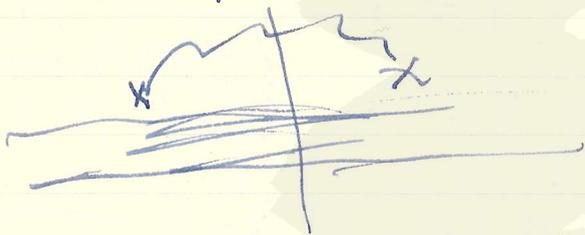
Stanford  
 $F_2(x, q^2)$



scaling law ←  $\frac{2m v}{q^2} = x$

scaling law of origin  
 light cone ± of singularity  
 境界の問題.

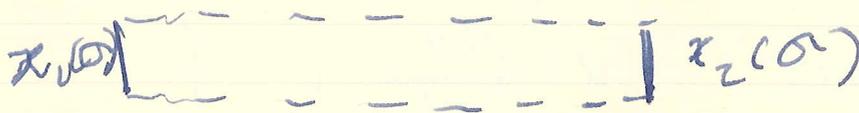
$\delta m_p \rightarrow$  quadratic order



$$q^2 \sim 15 (\text{GeV}/c)^2$$

関係は: duality & world sheet

$$\sum_A \frac{f(t)}{s-s_R} = \sum \frac{f(s)}{t-t_R}$$



由中子 $\psi$ :

河内氏: 対応原理

{ '実証・検証に基づいて'  
 場の論の発展を '架橋' とする }  
 粒子論の発展の方向

quark 場の自由な

Chiral dynamics

レプトン  
 の世界

1925 ~ 1928

$$(\gamma_\mu \partial_\mu + \kappa) \psi = 0$$

$$O(\psi) = O(L) \times O(R)$$

$$\frac{\vec{\sigma} \cdot \vec{L} + i\vec{\sigma} \cdot \vec{R}}{2} = \begin{matrix} L \\ R \end{matrix}$$

$$\eta = (\psi_L, \psi_R)$$



$\xi(\eta_L)$

$\xi(\eta_R)$

$$\psi(x, \eta) = \begin{matrix} L \\ R \end{matrix} \psi + \begin{matrix} L \\ R \end{matrix} \psi$$

$$= \varphi_L(x) \xi_L(\eta_L) + \lambda_R^*(x) \xi_R(\eta_R)$$

$$\psi = \begin{pmatrix} \varphi \\ \chi \end{pmatrix}$$

$$\kappa \psi =$$

$$[i \gamma_\mu \partial_\mu + D] \psi(x, \eta) = 0$$

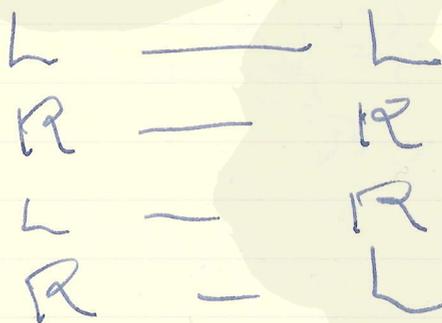
collision operator

proper  $[E_{\mu}, \Xi] = \partial_{\mu} \alpha \Xi = p$   
 $\Xi \equiv \begin{pmatrix} \xi_i (\gamma_L) \\ \eta_i (\gamma_R) \end{pmatrix}$

1)  $\vec{v}_i \parallel \vec{p} \propto \vec{\sigma} \cdot \vec{v} \rightarrow \tau_L \omega \tau_R \omega$   
 縦向きだと  $\tau_L \omega \tau_R \omega$

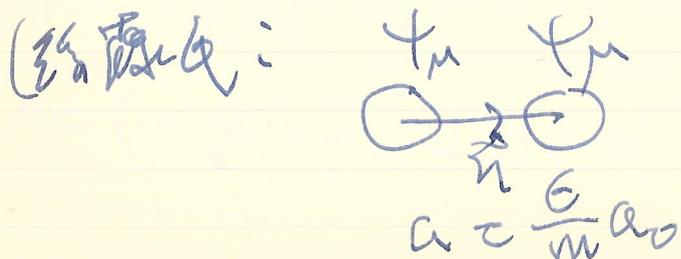
(1)

(2)



interaction

(1) L — L  
 R — R  
 L — R }  
 R — L } interaction  
 (2)  $\tau_L \omega \tau_R \omega$   
 $\tau_R \omega$   
 $\rightarrow V-A$  (Fierz invariant)



$\psi^* \vec{n} (\vec{v}_1 - \vec{v}_2) \psi = 0$   
 $\rightarrow V-A$



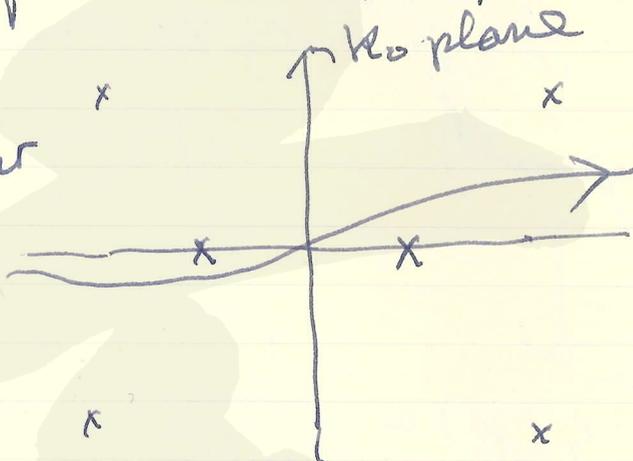
$$(e^{\partial, \bar{\partial}} + 1) u = 0$$

第3回 12月19日

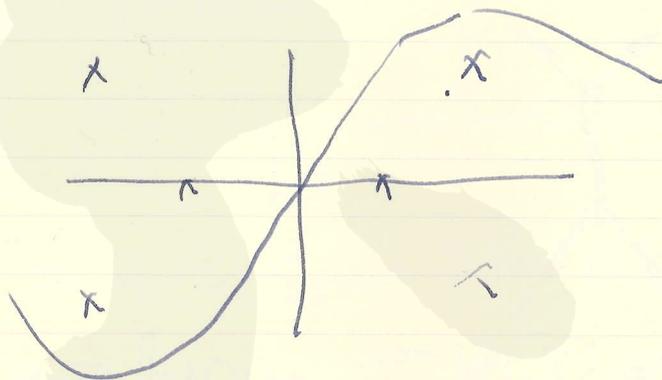
気前 先生 先生

山本氏: Complex manifold  $t=1$  の空円

Samurai  
 Hint =  $i$  hint



Lee-Wick  
 $t \rightarrow \pm i \infty$   
 諸君,



徳田氏: 田=次元電子化  
 Hyperquantization

漸進

光の

存在:  $\psi^2$

横軸: Non polynomial  
 Lagrangian theory

Fradkin, Efimov, Volkov

$$W_{eff} \equiv \int \frac{d^4x}{i} \mathcal{L}$$

1954

1963 ~ '68

$$\mathcal{L}_{int} = g U(\phi)$$

$$= g \sum_n \frac{v_n}{n!} (\phi)^n$$

$$\frac{G}{1+f\phi} \rightarrow v_n = f^2 n!$$

Delbrück - Salam - Strathdee  
 x-space method

Salam - Strath,  
 p-space method

chiral  $SU(2) \times SU(2)$

$$h = \frac{(\partial_\mu \phi)^2}{1+f\phi}$$

Weak interaction, mass

$$\mathcal{L}_{int} = p \bar{\psi} \gamma_5 (1 + \gamma_5) \psi A_\mu + m \bar{\psi} (e^{i\gamma_5 \theta} - 1) \psi$$

# Quantization

二粒子の相互作用

1) 先決条件

$$\langle \psi | \psi \rangle = 1$$

2) 縮約の次数

3) high energy behavior  
 (central momenta)  
 $U(\phi) \rightarrow \phi^D$

$$D > 4$$

$$D \leq 4$$

$$D \leq 3$$

$$D \leq 2$$

4) unitarity, causality 因果性



Borel sum

$$n! = \int_0^{\infty} e^{-z} z^n dz$$

9 弦の理論,

Weylmann 展覧?

考稿: 式

Removal of Level Degeneracy  
 in P.R.M. (Dual Resonance  
 Model)

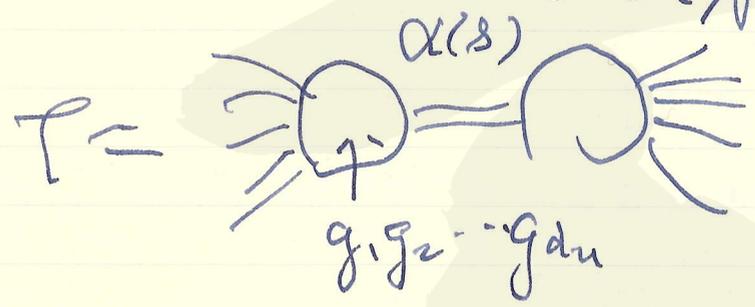
Feb. 12, 1971. 草

N-point Veneziano amp.

$$n = \alpha(s_n) \quad s_n = M_n^2$$

Multiplicity near a resonant state  
 $a_n \sim e^{a\sqrt{n}}$

$$a = 2\pi/\sqrt{b}$$



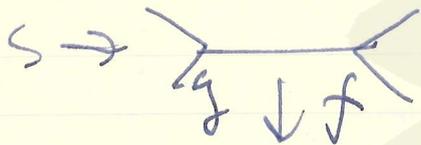
unitarity  $\Rightarrow$   $\frac{1}{s} \frac{1}{t} \dots$   
 remove  $\frac{1}{s}$

higher order  $\Rightarrow$  unitarity  
 $\frac{1}{s} \frac{1}{t} \dots$

$$T_{\psi\psi} = \langle \psi | \mathcal{P} T \mathcal{P} | \psi \rangle = \langle 0 | \mathcal{P} T \mathcal{P} | 0 \rangle$$

$$T_S = \frac{1}{\sqrt{2D} \sqrt{2D}} \langle = \langle 0 | \Gamma^\dagger D I D \Gamma | 0 \rangle$$

2 → 2 unitarity → factorization



$$\frac{g f}{s - M^2}$$

$$\frac{\delta(p) \delta(p)}{s - a(p)}$$

$$\frac{d\alpha \sum_{n=1}^{\infty} g_n f_n}{s - M_n^2} \quad X$$

中野浩夫: 重力理論

浮沈会

1971年 2月 17日

1963年: 超弦の発見

dinac particle

phase transformation  
charge conservation

$$\psi \rightarrow e^{i\lambda} \psi$$

$$\psi(x) \rightarrow e^{i\lambda(x)} \psi(x)$$

$$i) \quad D_\mu \psi = (\partial_\mu - i a_\mu(x)) \psi(x)$$

$$\delta a_\mu(x) = \partial_\mu \Lambda(x)$$

$$\bar{\psi} \sigma_{\mu\nu} \psi f_{\mu\nu}(x)$$

$$(ii) \quad a_\mu \equiv \frac{\bar{\psi} \partial_\mu \psi - \partial_\mu \bar{\psi} \psi}{2\psi\bar{\psi}}$$

任意関数

$$j^\mu = f j^\mu + 4\alpha (\partial_\nu f) f_{\mu\nu}$$

$$\partial_\nu j^\mu = 0$$

$$\alpha = \frac{1}{4e^2}$$

$$Q^\pm = \int j_0^\pm dV$$

f: arbitrary fm

$$f_{\mu\nu} = \partial_\mu a_\nu - \partial_\nu a_\mu$$

$$a_\mu = e A_\mu$$

Infinite Lie group  
 無限群

$$\delta x^\mu = \epsilon^\mu(x)$$

$$\delta \psi = 0, \quad \delta \bar{\psi} = 0$$

無限群

$$D_R \psi = \left\{ \partial_R + \phi_R^\mu(x) \partial_\mu \right\} \psi$$

$$= h_R^\mu(x) \partial_\mu \psi$$

$$h_R^\mu = \delta_R^\mu + \phi_R^\mu$$

$$\delta h_R^\mu = \partial_\nu \epsilon^\mu \cdot h_R^\nu$$

$$h_R^\mu \cdot h_{R\nu} = \delta_R^\mu, \quad h_R^\mu h_{R\mu} = \delta_{R\mu}$$

$$L = \frac{1}{2} h_R^\mu (\bar{\psi} \partial_R \psi - \partial_\mu \bar{\psi} \psi)$$

$$+ m \bar{\psi} \psi$$

無限群の生成子

$$C_{R\mu\nu} = h_{R\nu} (h_R^\mu h_{R\mu,\nu} - h_{R\mu}^\nu h_{R,\mu}^\mu)$$

$$h_{R\mu,\nu} \equiv \partial_\nu h_{R\mu}$$

$C_{R\mu\nu}$  の無限群



for  $\pi$ :  
 $\pi^+ - \pi^0$ ;

Q.E.D. : some  $\infty$  ?

Q.G.D. : unrenormalizable.

Salam

non-polynomial Lagrangian

E. Fermi  
 T. D. Lee  
 V. L. Kor

1963:  $L = \frac{g\phi^n}{1 + f\phi^m}$

O. Kubo 1954  
 exponential

$L = g \exp(f\phi)$

$= g \sum \frac{f^n}{n!} (\phi)^n$

Tafte micro-causality  $\neq$   
~~micro-causality~~  $\neq$   $\neq$

$$\frac{\delta m}{m_e} = \frac{3}{4\pi} \sum_n \alpha \log(\kappa^2 m^2)^n$$



→ boson h.c.

iii) weak  $\Delta I = 1/2$  or exciton  
 のような性質がある。

7.10 2.11

$$H_W \approx (\bar{t}^\alpha O_i t_R) (\bar{l}^\beta O_i l_L)$$

$$O_i = \sigma_\mu (1 + \sigma_5)$$

t<sup>d</sup>: base is  $\Delta I = 1/2$

iv) exciton → background

v) binding of the  $\pi$  meson. (potential)

exciton の形:

$$a_{a\lambda} \quad a_{a\lambda}^\dagger$$

deformable body of the spinor  $\alpha$ . (spinor)

粒子の相互作用の形は  $\lambda$ .

$$\text{相互作用} \rightarrow SU_3$$

電荷は  $U(1)$  の、 $U(1) \times U(1)$  の相互作用の  
 間。  $U(1) \times U(1) \times U(1)$  の相互作用  
 の形は  $U(1) \times U(1) \times U(1)$  の形である。

原理論

$SU_3$  の violation の 横断と  
 縮退の 50V, ,

Triality 0 の 状態  
 A. Kohn

真空状態の取り方に  
 対して arbitrary

mass operation

$$m^2 = f(m, n)$$

fermion  $\leftrightarrow$  antiquark

fermion, boson に共通の式,  
 縮退の式に一致.

原理論  $\rightarrow$  粒子 I-511

$\rightarrow$  真空状態  
 縮退 - 対称性

対称性

(i) ghost

(ii) Lagrangian の 対称性.

縮退状態

$$\pi^\mu(\sigma)$$

$$p_\mu(\sigma)$$

$$\sigma = (0, 2\pi]$$

$$D = \frac{\partial}{\partial \sigma^\mu}$$

$$\left[ \int_0^{2\pi} \left( \frac{1}{2} \dot{x}^\mu{}^2 + (\partial \alpha^\mu)^2 \right) d\sigma \right] \psi = 0$$

$$[P^2 + (\quad)] \psi = 0$$

$$H = \frac{1}{2} \int C^\mu(\sigma)^\dagger C^\mu(\sigma) d\sigma$$

$$C^\mu(\sigma) = -i D A^\mu$$

$$A^\mu(\sigma) = \frac{1}{\sqrt{2}} (x^\mu - D^{-1} p^\mu)$$

$$\sigma = f(\sigma')$$

$$\sigma = \sigma' + \epsilon f(\sigma')$$

$$\sigma' = [0, 2\pi)$$

$$f(\sigma') = \sum_{n=0}^{\infty} \zeta_n e^{in\sigma}$$

一般の場合の値は:

$$f(\sigma) = \zeta_0 + \zeta_1 e^{i\sigma} + \zeta_{-1} e^{-i\sigma}$$

Virasoro の代数は  $L_n$  の形。  
 ghost の挿入は  $\xi, \eta$  の形?

$L_n$  - 代数の表現  
 $x^\mu(\sigma, \tau)$

$$g_{00} = \frac{\partial x^\mu \partial x^\mu}{\partial \sigma \partial \sigma}$$

$$g_{01} = \frac{\partial x^\mu \partial x^\mu}{\partial \sigma \partial \tau}$$

$$g^{11} = \frac{\partial x^\mu \partial x^\mu}{\partial \tau \partial \tau}$$

$$\det g = g_{00} g^{11} - g_{01}^2$$

$$L = \mu \int d\sigma d\tau \sqrt{-\det g}$$

$$p_\mu p^\mu + \mu (Dx^\mu)^2 = 0$$

$$p_\mu \frac{\partial x^\mu}{\partial \sigma} = 0$$

Takabayasi 17 2025 2017 2018 2019

$$L = \mu \int \sqrt{-g_{00}} d\tau \sqrt{(d_\perp x^\mu)^2}$$

$$v_\mu = \frac{1}{\sqrt{g_{00}}} \frac{\partial x^\mu}{\partial \tau}$$

$$v_\mu d_\perp x^\mu = 0$$

弦の内部

和をとり

vertex の 1/25 5/25 10/25 15/25 20/25 → local limit

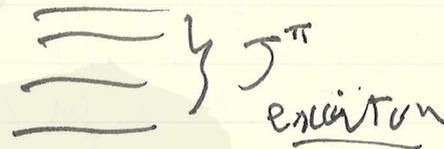
1/25 2/25 3/25 4/25 5/25 の 1/25 2/25 3/25 4/25 5/25  
 duality

1932:  $\pi$  meson :  $\pi$  meson &  $\pi$  meson  
 1932  $n, p$   
 $\pi$

one-particle motion x liquid drops mode

1960 microscopic theory (1949: Mayer, Jensen shell model) nuclear matter

excitation mode  
 excitation in nucleus  
 $\pi$  meson...



### 31. Nuclear Shell-Model

$$H = \sum T c^\dagger c + \sum V c^\dagger c^\dagger c c$$



$$H' = \sum_n \hbar \omega x_n^\dagger x_n + \sum V_{eff}$$

$x, x^\dagger$ : boson  
 or fermion

$$\{\psi^\dagger(x), \psi(x')\} = \delta(x, x')$$

$$\psi^\dagger(x) = \sum_\alpha c_\alpha^\dagger \varphi_\alpha^\dagger(x)$$

$\varphi_\alpha$ : shell model wave function

$$\alpha \equiv (n, l, j, m, \tau)$$

$$\downarrow a \equiv (n, l, j)$$

$$H \rightarrow H_0 = \sum_a E_a^{(0)} c_a^\dagger c_a$$

$$E_a \equiv E_a^{(0)} - \lambda > 0 \text{ open}$$

$$E_a \equiv E_a^{(0)} - \lambda < 0 \text{ comp.}$$

"free vacuum"  
 $|0\rangle$

$$c_a^\dagger = \begin{cases} e_{\alpha}^\dagger & E_a > 0 \\ (-)^{j_a - m_a} (-)^{\frac{1}{2} - \tau_a} b_{-a} & E_a < 0 \end{cases}$$

$$-a \equiv (m, l, j, -m, -\tau)$$

$$a|0\rangle = b_a|0\rangle = 0$$

$$H = H_0 + H_{int}$$

$$H_{int} = \sum_{\alpha\beta\gamma\delta} \langle \alpha\beta | V_{eff} | \gamma\delta \rangle : c_\alpha^\dagger c_\beta^\dagger c_\gamma c_\delta :$$

$(\hat{n}_{\text{pair}} \hat{n}_{\text{dot}}) = -1$  : :  $\equiv$  normal product

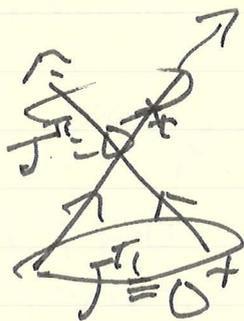


$H_{int} = H_{pp} + \dots$   
 constructive force

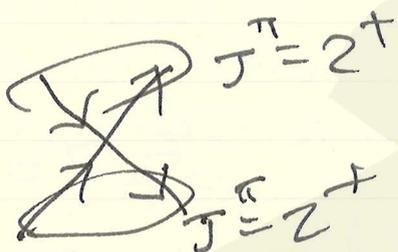


interactive part

Tamura-Dancoff App.

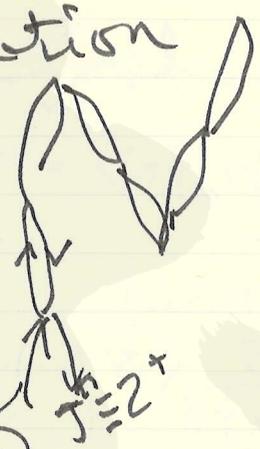


pairing interaction



§ 2. Collective Motion

R.P.A  
 (random phase approximation)  
 chain approximation



boson  $(X_n, X_n^\dagger)$

free vacuum  $\rightarrow$  true vacuum  
 $|0\rangle \quad X|\Phi_0\rangle = 0$

$|\Phi_0\rangle = c_0 |0\rangle + c_1 a^\dagger a^\dagger b^\dagger b^\dagger |0\rangle + \dots$   
 quadrupole interaction

free vacuum instability  $\equiv \frac{2^+}{0^+}$   
 Haag  $\hat{=}$   $\hat{E} \hat{P}$

phonon spectrum vibrational  $\rightarrow$  rotational spectrum

one-particle mode  $a |0\rangle = 0$

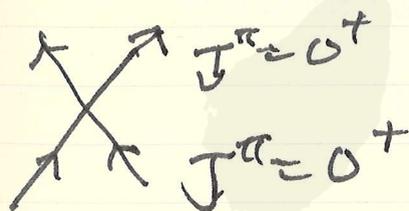
or broken symmetry

$$a' |0'\rangle = 0$$

$$b' |0'\rangle = 0$$

angular momentum conservation  $\hat{L} \hat{E} \hat{P}$   
 deformation

### § 3. Pairing Vibration B.C.S. transformation



$H_{free}$   
 free vacuum  $\rightarrow$   
 $|BCS\rangle$



one particle mode  $\pi$   $\rightarrow$   $L_{z, \pi}$   
 number conservation  $\pi$   $\rightarrow$   $L_{z, \pi}$

$$a^\dagger |BCS\rangle = 0$$

$$a^\dagger a = U_n c^\dagger - (-)^{j\alpha - m_\alpha} C \cdot a$$

for  $a^\dagger$

quasi-particle of nucleon  $L_{z, \pi}$

$$\overbrace{a^\dagger a^\dagger |BCS\rangle}^{s=2} \quad \overbrace{a^\dagger a^\dagger a^\dagger |BCS\rangle}^{s=3}$$

$$\overbrace{|BCS\rangle}^{s=0 \text{ even}} \quad \overbrace{a^\dagger |BCS\rangle}^{s=1 \text{ odd}}$$

seniority  
 charge  $\pi$   $\rightarrow$   $2\pi$  ...

3/4 of composite : fermion  
 anomalous coupling

$\pi$   $\rightarrow$   $2\pi$  ...

non-local  
 correct algebra is  $\{a, a^\dagger\} = 1$   
 non-local  $c^\dagger c_p$   $c c_p$   $c^\dagger c_p$

vacuum state  $\rightarrow$   $\langle \dots \rangle$  の状態...

逆小気:

場の理論  $\rightarrow$  quark 理論



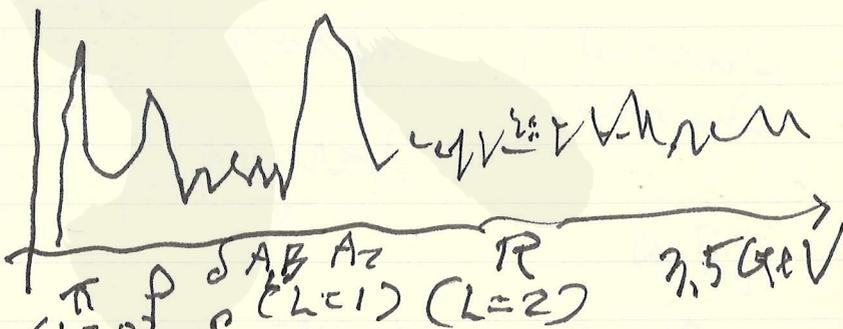
charge  
strengths  $\rightarrow$  相互作用 ) SU(6)  
 spin 56.

PKS力 + LS力 相互作用

missing mass spectrum



X の spectrum は 3 GeV  
 以下に  $\rho$ ,  $\omega$ ,  $\pi$



① 場の理論

( $L=0$ )  $\pi$ ,  $\rho$ ,  $\omega$ ,  $\phi$ ,  $A_1$ ,  $A_2$ ,  $P$  ...  
 相互作用

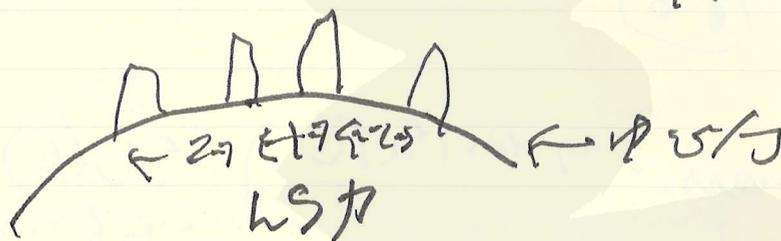
form factor  
 $\gamma \rightarrow \pi$

② 12/5 quality  
 optical model

$n \rightarrow \rho \rightarrow \pi$

interaction

one-particle mode  
 (核子核子) → giant resonance  
 (compound nucleus → liquid drop  
 one-particle mode → optical model  
 (FDD potential))



$25 \text{ MeV} \rightarrow 70 \text{ MeV}$

quark  
 準粒子

$\sigma(E) \propto E^{-n}$

(crossed channel)

|        |            |                  |
|--------|------------|------------------|
|        |            | Morison rule (n) |
| vacuum | $S=0$      | parity + 0       |
| meson  | $S=0$      | -2               |
|        | $S \neq 0$ | -3               |
| baryon |            | -4               |

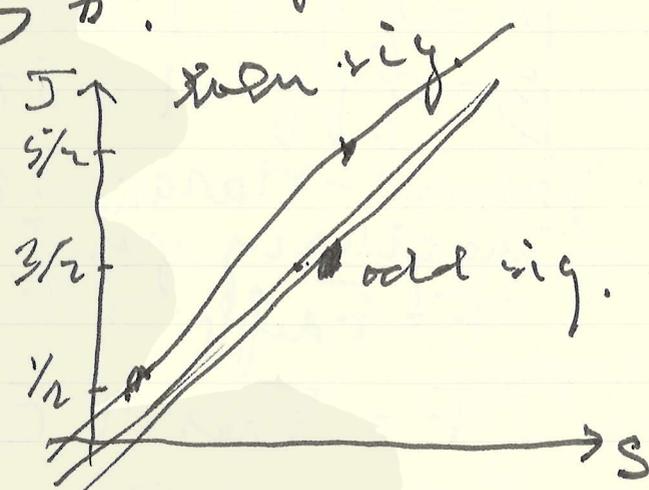
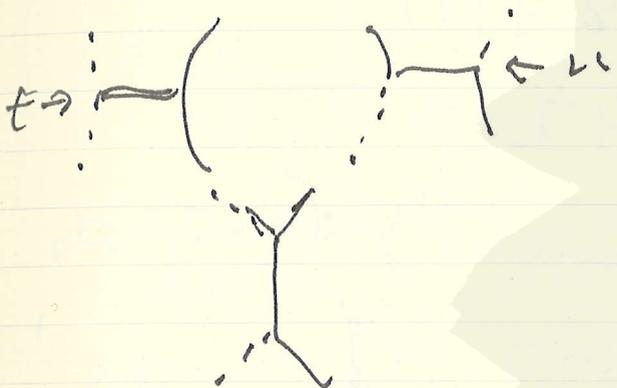
IR 1/4

multiple production

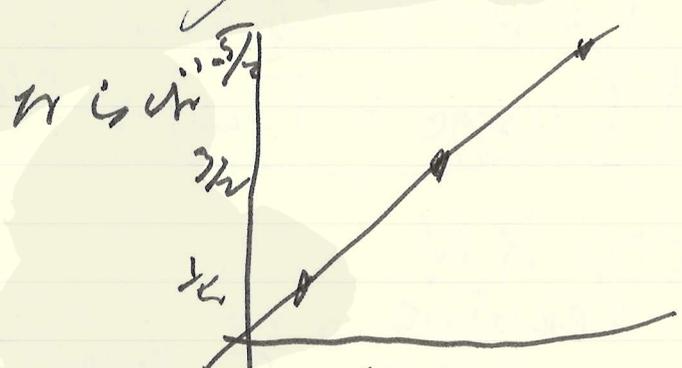
「 $\pi^+\pi^-$ 」  
 $H^+\pi^-$

3.0 W:  $\frac{E_{cm}}{m_p c^2}$

700 MeV: Veneziano's Anom. 14% の  
 5.11 MeV とあうか!



t-channel only



$$S = \sum_j \dots \left( \leftarrow t = \sum_j \dots \right)$$

Im A<sup>(1-)</sup>    ineq. part     $\pi N$

Experimentally  
 1.2, 1.7  
 4 GeV  $\sim$  2.2  
 4.4 GeV  $\sim$  2.2  
 5.11 MeV  $\sim$  L.

no exotic state one-particle  
 state

$$M = \underbrace{g \bar{g}} = 1 + 8$$

$$B = \underbrace{g \bar{g}}_B \underbrace{g \bar{g}}_B = 1 + 8 + 8 + 10$$

Frenkel-Warner の仮定  
 imaginary part

$$F_i = F_{diff} + F_{Regge}$$

$$F = F_{res} + F_{s.g.}$$

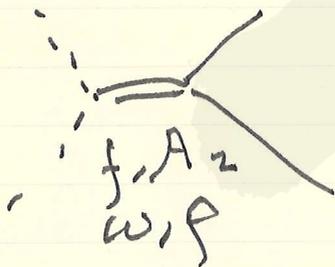


$$F_{diff} = F_{s.g.}$$

$$F_{Regge} = F_{res} \rightarrow \text{ Veneziano }$$

$KN, \bar{K}N$   
 $KN \rightarrow \text{exotic}$

$$\text{Im} [F(KN) - F_p(KN)] = \text{Im} F_{res}(KN) = 0$$



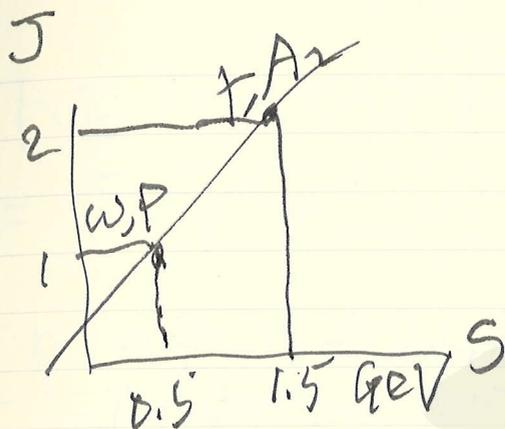
$$F_R = \int_R \frac{e^{-i\pi a_R \pm 1} v_R^{a_R(t)}}{\sin \pi \alpha_R(t)} v_R^{a_R(t)}$$

$$\alpha_f = \alpha_w$$

$$\alpha_{A2} = \alpha_p$$

exchange degeneracy

$$\begin{pmatrix} \beta_f \\ \beta_{A2} \end{pmatrix} = \begin{pmatrix} \beta_w \\ \beta_p \end{pmatrix}$$



degenerate meson

$$\psi^{(-)} \leftrightarrow \eta^{(+)}$$

baryon I,

$$\psi^{(+)} \leftrightarrow \rho^{(+)} + \psi^{(-)}$$

$$\text{II, } \rho^{(-)} + \psi^{(-)} \leftrightarrow \delta^{(+)}$$

$$V, T$$

~~$$\frac{1}{2} + - \frac{1}{2} +$$~~

$$\frac{3}{2} + - \frac{5}{2} +$$

⑧  $\frac{3}{2}$

$\eta$  meson

$$I=0 \quad (\eta)$$

$$I=1 \quad (\pi)$$

$\pi$  v degenerate?

$$m_{\eta}^2 - m_{\pi}^2 = 0.3$$

7月10日

I. Un-aron 模型

i) Quark 有色的

ii) non-rel. rel momentum  $\neq 0$   
 strong binding

iii) 統計  $\pi E^2: \frac{1}{2}$  Bose  
 56 次元 symm.

nonleptonic interaction  $\Delta J = \frac{1}{2}$

ii) 1)

iii) 混合状態  $\rightarrow$  Quark 模型

II. 一色模型

$$\psi_a(z, p)$$

$$4 \times 3 = 12$$

$$-i p_\mu \gamma^\mu \psi^\pm(z, p) = \pm \sqrt{p^2} \psi^\pm(z, p)$$

$$[\psi_a^{(\pm)}(p, z), \bar{\psi}^{(\pm)}(p', z')] = \Lambda_a^{(\pm)\beta}(p) \delta_{\beta\alpha} \delta(p-p') \delta(z-z')$$

$$\psi(p, z) = \psi^{(+)}(p, z) + \psi^{(-)}(p, z)$$

$$[\psi_a(p, z), \bar{\psi}^\beta(p', z')] = \delta_a^\beta \delta_{pp'} \delta(z-z')$$

$$\psi^{(+)}|0\rangle = \psi^{(-)}|0\rangle = 0$$

$$|\Psi\rangle = \langle p, \Psi(p, \xi) \rangle$$

$$= \sum \bar{\Psi}^{(+)} \bar{\Psi}^{(+)} \dots \Psi^{(-)} \Psi^{(-)} \mathcal{E}(\dots) |0\rangle$$

$$(p^2 - s_0 + S) |\Psi\rangle = 0$$

$$S = S^{(+)} + S^{(-)}$$

$$S^{(\pm)} = \pm \int \bar{\Psi}^{\pm}(\xi) m^2(\xi) \Psi^{\pm}(\xi) d\xi$$

Postulate:  $\mathcal{E} \in \mathbb{R}^2$  is a set  
 (hadron world)  
 spin of  $\mathcal{E}$  is  $\frac{1}{2}$  or  $0$   
 hermiticity  
 base

mass level

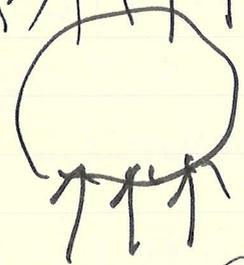
$$B: M^2 = \omega \left( \sum_{i=1}^3 \alpha_i^+ \alpha_i + 3 \right) + s_0$$

$$M: M^2 = \omega \left( \sum_{i=1}^3 \alpha_i^+ \alpha_i + 2 \right) + s_0$$

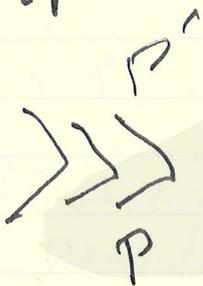


III. 非可換性 (A)

$$\phi_n^m(p) \uparrow \uparrow \uparrow p'$$



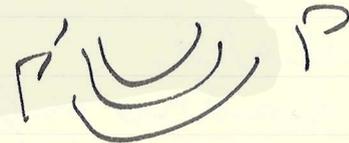
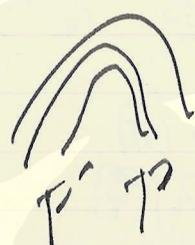
$$\phi_n^m(p) \uparrow p$$



i) connection

$$\Sigma^{(A)}(p', p) = \text{exp}[\bar{\psi}(p') \psi(p)]$$

$$\Sigma(p, p') = \sum_{p_1, p_2} \text{exp} \bar{\psi}(p) \psi(p_2)$$



ii) bilinear

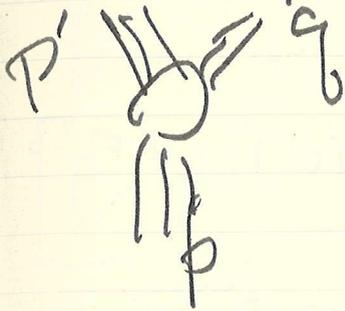
$$\text{loop} = *|| + |*| + ||*$$

$$\tilde{O} \equiv g \sum_{p, k} \int d^3z \psi(p, z) O(z) \psi(p-z)$$

$$: \tilde{O} :$$

iii) multi.

non-leptonic decay

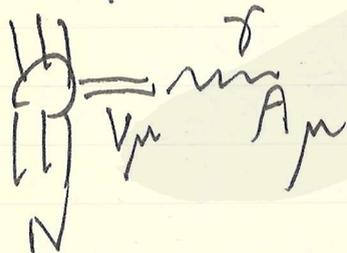


$$\Sigma W$$

$$\tilde{W} = \sum \bar{\psi} \gamma_{\mu} \psi \psi \gamma^{\mu} \psi$$

$$O_{\mu} = \gamma_{\mu} (1 + \gamma_5)$$

electromagnetic form factor

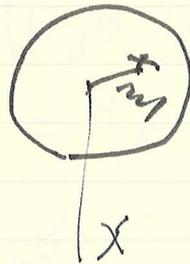


$$\langle \psi | \Sigma O_{\mu} | \psi \rangle \cdot V_{\mu}$$

baryon

$$\left( 1 + \frac{g^2}{2m^2} \right)^3$$

miton  
 $\frac{1}{2} \bar{q} q$



$$\sim \frac{1}{4\pi} \frac{g^2}{1 + \frac{g^2}{2m^2}} \left\{ \frac{(1 + \frac{g^2}{4m^2})^2}{(1 + \frac{g^2}{m^2})} \right\}$$

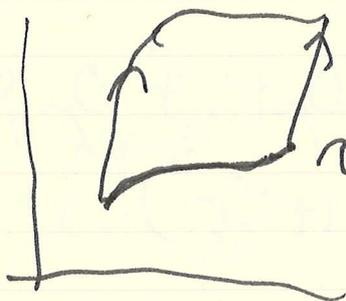
$\pi$ -meson

vector meson

$$4\pi = 5 \text{ GeV}.$$

後藤氏:  
 (青)A9

Copen,



$\sigma, \tau$

$$x_\mu = x_\mu(\sigma)$$

$\tau \sim \tau_0$

$$x_\mu = x_\mu(\sigma, \tau)$$

$$\frac{1}{\sqrt{g_{00}}} \frac{\delta x_\mu}{\delta \tau} = \gamma_\mu$$

$$g_{00} = \frac{\partial x_\mu}{\partial \sigma} \frac{\partial x^\mu}{\partial \tau}$$

$$\gamma_\mu \delta_\perp x^\mu = 0$$

$$\delta_\perp x^\mu = \delta \sigma$$

$$-d\ell^2 = (\delta_\perp x^\mu)^2$$

$$\frac{g_{01} - g_{00} \gamma_{11}}{g_{00}}$$

$\kappa d\ell$

$$L = \kappa \int d\ell ds(\ell) = \kappa \int d\sigma d\tau \sqrt{-\det g}$$

$$\sqrt{\frac{-\det g}{g_{00}}} d\sigma \sqrt{g_{00}} d\tau$$

$$p_\mu(\sigma) = \frac{\partial L}{\partial \left( \frac{\partial x^\mu}{\partial \tau} \right)} = \frac{\kappa}{\sqrt{-\det g}} \left[ -g_{\mu\nu} \frac{\partial x^\nu}{\partial \tau} + g_{01} \frac{\partial x^\mu}{\partial \sigma} \right]$$

$$p_\mu \frac{\partial x^\mu}{\partial \sigma} = 0 \quad (1)$$

$$p_\mu \frac{\partial x^\mu}{\partial \tau} = \kappa \sqrt{-\det g} = L$$

$\nabla H = 0$

$$p_\mu(\sigma); p^\mu(\sigma) \Rightarrow \pi^2 g_{\mu\nu} = 0$$

$$p_\mu p^\mu + \pi^2 \left( \frac{\partial X^\mu}{\partial \sigma} \right)^2 = 0 \quad (2)$$

変換

$$\frac{L}{\sqrt{g_{\mu\nu}}} \frac{\partial X^\mu}{\partial \xi^a}$$

$$\xi^a = (\xi^0, \xi^a)$$

$$p_\mu \frac{\partial X^\mu}{\partial \xi^a} = 0$$

$$p_\mu p^\mu + \pi^2 \det \bar{g} = 0$$

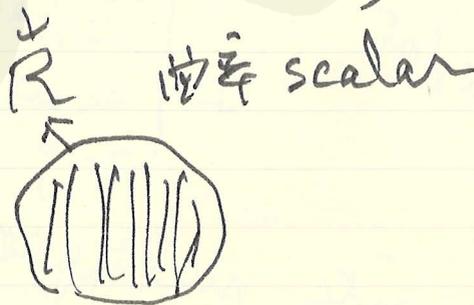
$$\left[ \frac{g_{\mu\nu}}{\sqrt{|g|}} \right]$$

$$L = \pi \int d^4 \xi \sqrt{-\det g}$$

$$\downarrow$$

$$L = \int d^4 \xi \sqrt{-\det g} \cdot \mathcal{L}(\psi; \psi^A(\xi))$$

$$p_\mu \frac{\partial X^\mu}{\partial \xi^a} + \pi \frac{\partial \psi^A}{\partial \xi^a} = 0$$



3/A31B

波函数  $(\rho, \kappa)$

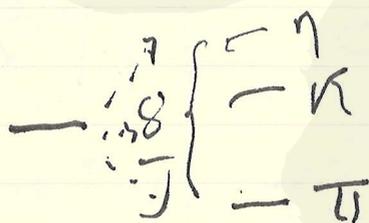
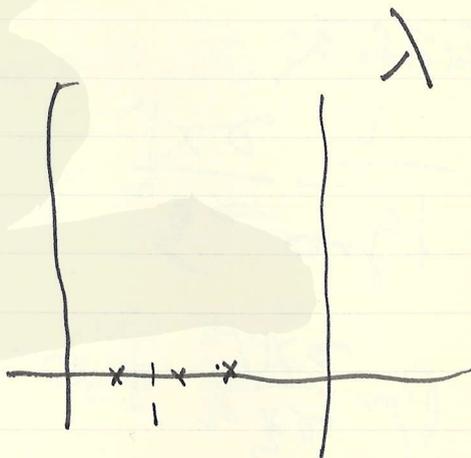
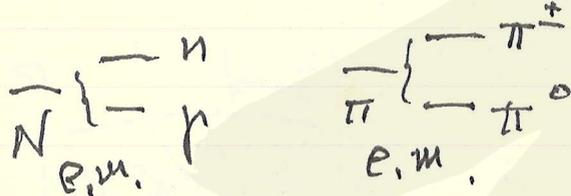
A:  $\varphi(x) \rightarrow \varphi(x') = x^{\lambda-1} \varphi(x)$

$x' = \rho x$

$\square^{1+\lambda} \varphi(x) = 0$

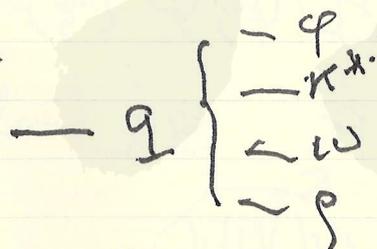
$\dim \varphi(x) = \lambda - 1$

B. 2 点 対 称 子



semi-infinity

SU(6)  
 35  
 super multiplet



"infinite multiplet"

Hadrons: composite internally structured  
(extended)

excitation

fully relativistic  
treatment

low width  
approximation

non-compact groups

i) relativistic covariance

ii)  $\vec{E} \times \vec{B} \leftrightarrow$  generator

iii) observables (Poincaré group)

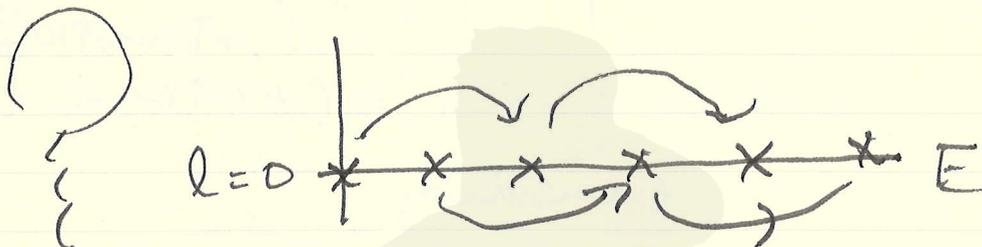
Yukawa ('56)

Sakata ('55)

infinite  
multiplet  
exciton

$\rightarrow t$

$a, a^\dagger$

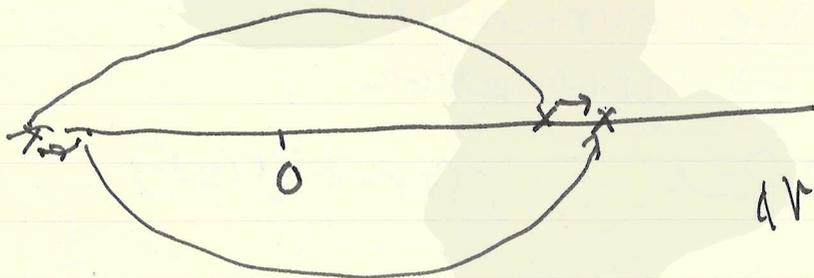


$$h_0 = \frac{1}{2}(a^\dagger a + \frac{1}{2})$$

$$h_1 = \frac{1}{4}(a^\dagger a^\dagger + a a)$$

$$h_2 = \frac{i}{4}(a^\dagger a^\dagger - a a)$$

"SO(2, 1)" dynamical group



4V 5V 7V 9V 11V

Source:

I. Nonlocal F. T.

II. Majorana-Gel'fand-Yaglom

-Nambu Theory

(1922) (1948)

Trudkin

(1966: 湯川理論: 湯川博士 X)

Takabayashi (1965)

expansion

### III. Relativistic generalization of $SU(6)$ symmetry

invariant theory

$$G_{int} \otimes P_{orb}$$

mass degenerate

$$U(6, 6)$$

$$SU(6, C)$$

unitarity  
 →  $\frac{1}{2} \text{ spin } \times \frac{1}{2} \text{ spin}$  (red mass - mathew)

→ spin  $\frac{1}{2} \times \frac{1}{2}$  of  $\frac{1}{2} \times \frac{1}{2}$   
 for  $\frac{1}{2} \times \frac{1}{2}$  (locality)

PCT

crossing symmetry

→ '68 : "Nambu theorem"

→  $\frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2}$

Miyazaki

"Tachyon"

locality

### IV. Generalized Regge th. Toller ('67)



parent trajectories  
 daughter trajectories

Friedman-Wang ('67)

Dowdson-Tinale ('67)  $SL(2, C)$

V. Current Algebra at  $|P| \rightarrow \infty$

Gell-Mann ('62)

Fubini-Furlan ('65)

cs-mom.-method

fixed  $q^2$  sum rule

Adler-Weisberg ('65)

$q_A$ -sum rule

Calicchio-Radicatti ('66) sum rule

Adler ('67) sum rule

VI. Generalized Born App.

in strong interaction

Van Hove ('67)

Halpern (unitarity)

Tanaka (convergence)

Tanaka et al ('64)

$$\Sigma \frac{e}{m^2 R^2}$$

$\frac{d}{ds}$



Trousdale, Hayashi, Ota-Rozawa  
 - Obara, Matshunoro

VII Non-compact groups from dynamics

H-atom  $SO(4, 2)$

harmonic oscillator  $SU(3, 1)$   $(O[3, 3])$

strong coupling model  $SL(4, \mathbb{R}) =$

$$(I, T) = \left(\frac{1}{2}, \frac{1}{2}\right), \left(\frac{3}{2}, \frac{3}{2}\right) \dots$$

second quantization  $\mathbb{R}^{4, 2}$   
 $\mathbb{R}^4 \times \mathbb{R}^2$

VIII S-matrix

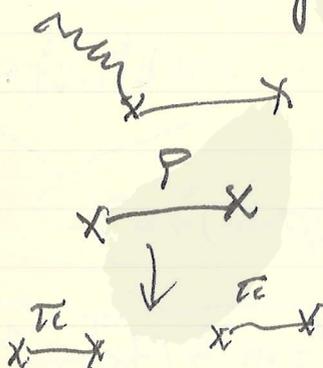
Guariniel, Nambu

Takabayashi

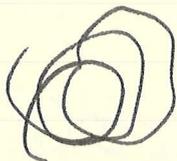
(1970)

string model

弦理論の発展



弦理論



数学

中即的: Compact group

since 7 9 2 5

compact non-unitary

indefinite metric

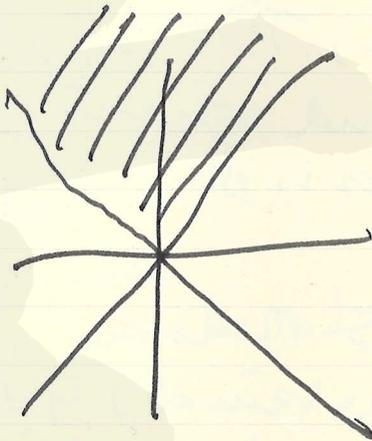
$$\psi = \psi^* \gamma_4$$

$$\bar{\psi} = \psi^* \gamma_4$$

Wick

Wightman  
 functions

$$\langle 0 | \phi \dots \phi | 0 \rangle$$



$$\bar{\psi} = \psi^*(x^+)$$

$$e^{a^2(\square \cdot m^2)}$$

$\phi$   
 $\psi$

$$\bar{\psi} f(\square) \phi \psi$$

$$(2b^2(k^2 + m^2))$$

$$S(p) = \int_{-\infty}^{+\infty} d^4 k \frac{e^{-2a^2\{(p-k)^2 + m^2\}}}{\{(p-k)^2 + m^2\} (k^2 + m^2)}$$

$$= \int_{(m+\mu)^2}^{\infty} \frac{dx^2}{p^2 + k^2} \sigma(p^2, k^2)$$

$$\sigma(p^2, \kappa^2) = \pi^2 \int_0^1 \frac{d\zeta}{a^2 \zeta^2} \theta\left(\kappa^2 - \frac{m^2}{\zeta} - \frac{\mu^2}{1-\zeta}\right) e^{-2a^2 \zeta (p^2 + \kappa^2)} + (a \leftrightarrow b, \zeta \rightarrow 1-\zeta)$$

unitarity?

$$S = \frac{1+iK}{1-iK}$$

湯川記念館  
4月1日, (1977)  
湯川記念館.

弦の波動関数

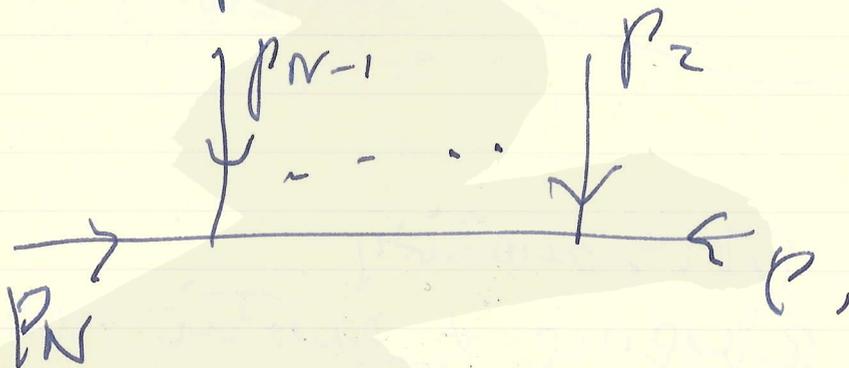
I. DRM 2 の zeroth mode (巻肉)

II. duality of  $\alpha$  and  $\beta$  (1)

誤記

April 22, 1971

I,



$$R = \sum_{n=1}^{\infty} n a^{(1)T} a^{(n)}$$

$$R^{(0)} = \frac{\epsilon}{z} a^{(0)T} a^{(0)}$$

$$V(p) = e^{\alpha p^+} p / \sqrt{\epsilon} e^{-\alpha^{(0)} p / \epsilon} e^{-\frac{p^2}{\epsilon}}$$

$$z \rightarrow 0 \frac{+}{dz}$$

Möbius 変換

$$w = \frac{az + b}{cz + d}$$

$$ad - bc = 1$$

$$SL(2, \mathbb{C}) \rightarrow \tau = \begin{pmatrix} a & b \\ c & d \end{pmatrix}$$



$$\frac{1}{\sqrt{0}} \equiv 1 \quad (\text{no velace})$$



II. DHS duality

absence of exotic resonances  
 $10, 20, 27$  mesons

→ exchange degeneracy  
 of  $V, T, \text{nonet}$

$pp(\bar{p})$ -meson & nonet  
 交換的対称性  
 定数  $K_0 = 1/2$

$V, T = \text{nonet}$   
 $P, A = \text{octet}$

$\pi, K, \eta$   
 $A, K^*, \rho$

$F_0$  is a doublet  
 trace 記  
 determinant 記

→ duality の対称性  
 dual  $U(3) \times U(3)$   
 non-dual

broken dilatation invariant  
(scale)

$$D_\mu = X_\nu \Theta_{\mu\nu} \quad DC$$

$$\partial_\mu \partial_\mu = \Theta_{\mu\mu} = (d_S + 4) \delta$$

$\delta, \delta_S$  dilatation  
massive

表の右 → 新 class  
 第2種のEWSB  
 発行, April 27, 1977

30.2. 2022 EWSB  
 VA

$$\begin{aligned}
 \text{Hint} &= J_\alpha^V \left[ \bar{\psi}_e \frac{\gamma_\alpha (1 + \gamma_5)}{\sqrt{2}} \psi_\nu \right] \\
 &+ J_\alpha^A \left[ \bar{\psi}_e i \gamma_\alpha \frac{\gamma_5 (1 + \gamma_5)}{\sqrt{2}} \psi_\nu \right] \\
 &+ h.c.
 \end{aligned}$$

$$J_\alpha^V = C_V \bar{\psi}_p \gamma_\alpha \psi_n$$

$$J_\alpha^A = C_A \bar{\psi}_p i \gamma_\alpha \gamma_5 \psi_n$$

$$T_\alpha^V = \bar{\psi}_p [f_V \gamma_\alpha - i g_V \sigma_{\alpha\beta} p_\beta + i h_V \not{p}_\alpha] \psi_n$$

$$\begin{aligned}
 T_\alpha^A = \bar{\psi}_p [ & i f_A \gamma_\alpha \gamma_5 - g_A \not{p}_\alpha \gamma_5 \\
 & - h_A \sigma_{\alpha\beta} \gamma_5 p_\beta ] \psi_n
 \end{aligned}$$

G-parity:

$$G J_\alpha^V G^{-1} = J_\alpha^V$$

$$G J_\alpha^A G^{-1} = -J_\alpha^A$$

$$h_V = h_A = 0$$

}  $\rightarrow$  1st & 2nd current

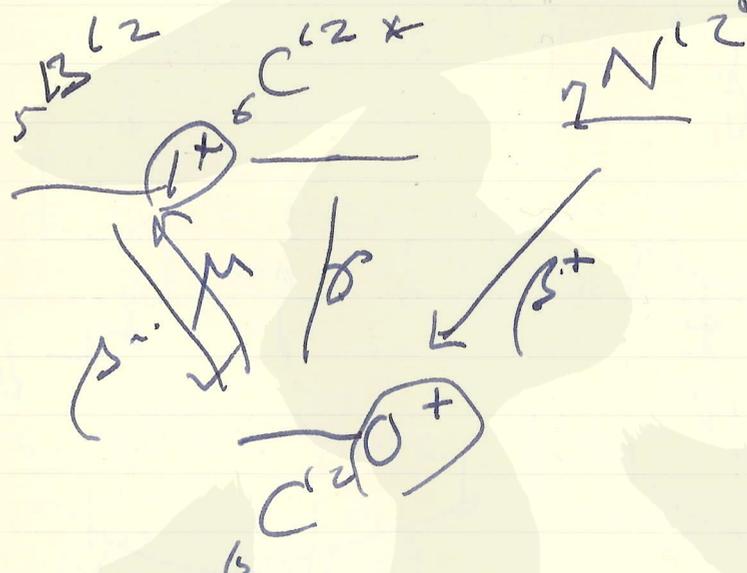
$$\partial_\alpha V_a^\nu = 0 \rightarrow h_\nu = 0$$

(CVC)

fermion  $\psi$  is  $\psi \psi^\dagger$  ?

$\beta$ -decay  
 $\mu$ -capture

mirror nuclei  $\beta^\pm$  decay



Wil Rein son

# 混雑論

巻頭. 5月27日 1971年

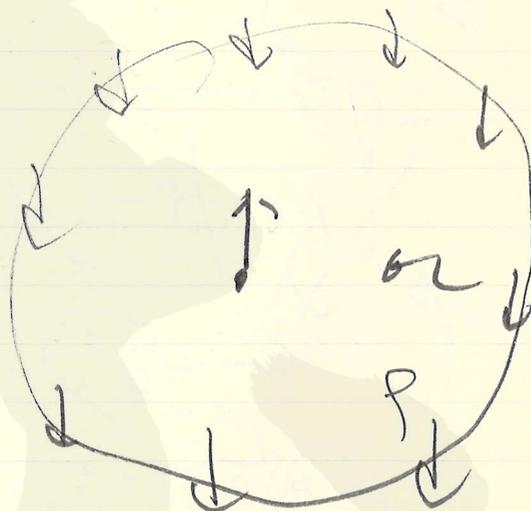
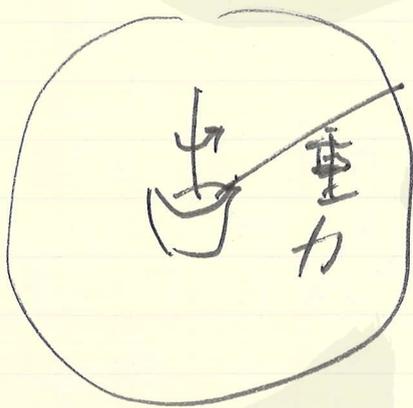
混雑論: Mach 原理

宇宙の中心がない

慣性系

重力場

Sciama, Camb. Phil. Soc.  
F. Ginzburg



加速の場の重力の  
関係

vector field

速度  $\vec{v}$   $\vec{E}$

Coriolis  $\vec{H}$

zero mass

$\frac{1}{c}$

慣性系

$$m = m_0 f(\beta)$$

$$g_{\mu\nu} = \varphi^2 \gamma_{\mu\nu} \quad (\det \gamma_{\mu\nu} = 1)$$

$$\begin{aligned} \mathcal{L} &= m_0 \dot{x}^\mu \dot{x}^\nu g_{\mu\nu} \\ &= m_0 \dot{x}^\mu \dot{x}^\nu \gamma_{\mu\nu} \varphi^2 \end{aligned}$$

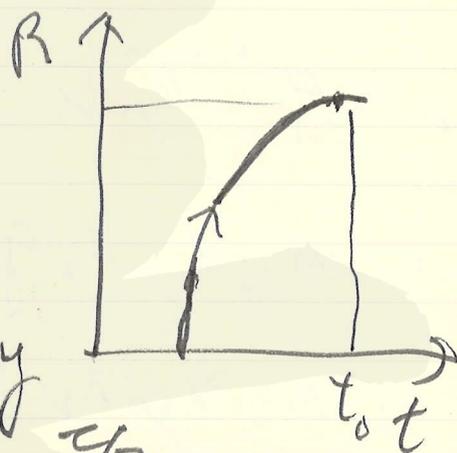
Wheeler - Feynmann  
complete absorber

Hogarth: Proc. Roy. Soc.,  
expanding universe  
Hoyle and Narlikar

依頼の：(おつ、宇宙  
 超高温の(一考)の線)  
 鏡子(燃焼)の系

膨張宇宙

$$\frac{R(t)}{R_0} \approx 1 - 10^{-3}$$



$$R(t) \propto t^{2/3}$$

$10^9 \text{ y}$

$$\frac{\dot{R}}{R} \propto \frac{1}{t}$$

$$\frac{R(t)}{R_0} = \frac{1}{3} \quad \text{QSO}$$

$$= \frac{1}{10^9}$$

He  $\downarrow$  2.7°K

3°K 超高温



天体の解法

Andromeda ( $10^{22}$  光年)

pulsar

horanty 速度を  $v$

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} = 10^{11}$$

総エネルギー

$$E = \frac{Mc^2}{\sqrt{1 - \left(\frac{v}{c}\right)^2}} = Mc^2 \gamma$$

$$\tilde{E} = \frac{E_0}{\sqrt{1 - \left(\frac{v}{c}\right)^2}} = E_0 \gamma$$

$$c(\gamma) > c_0$$

$$v \rightarrow c_0$$

$$L \rightarrow L_{max}$$

$$\frac{c_0}{c(\gamma)} = 1 - \frac{1}{\gamma^2}$$

$$10^{11} \sim L_{max} \sim 10^{11}$$

1. 高エネルギー衝突

Deep Inelastic Collision

1971年 618220 (1/2)

若狭物理学会

高エネルギー衝突

small distance

high energy phenomena

$SU(3) \times SU(3)$  - chiral sym.

SLAC-experiment

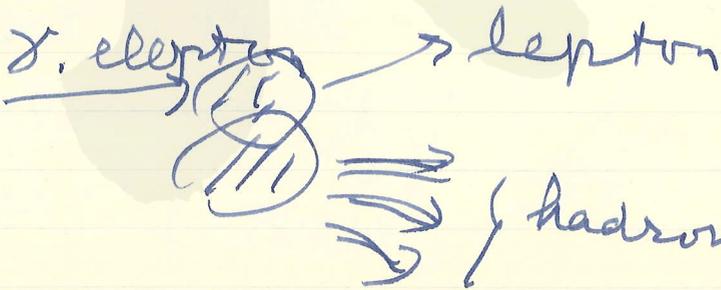
$m \approx 0 \rightarrow$  scale invariance

$q^2 \rightarrow$  large

$$v = -\frac{P \cdot q}{m}$$

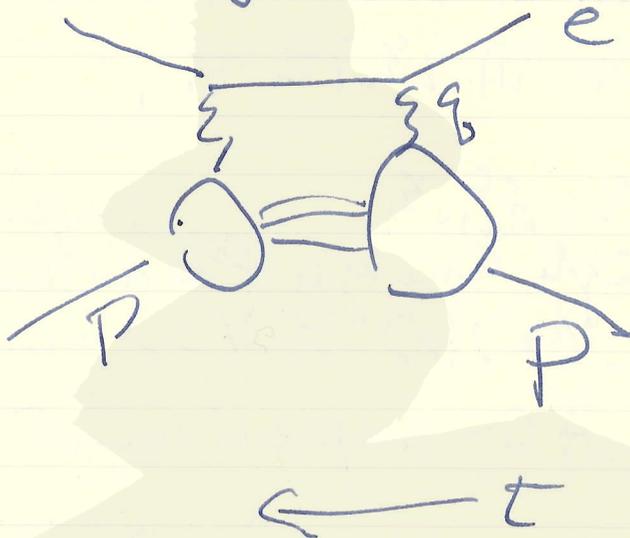
light cone singularity

Inclusive reactions



light-like charge etc  
light cone singularity

Bjorken's scaling law



localized quarks  
versus  
uniform charge distri

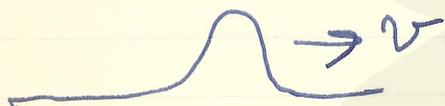


Soliton: 7.17  
 糸島信男

済世会 6月25日, 1971  
 巻併

solitary wave

nonlinear wave の 1次元空間の 1次元の波



安定 (disturbance  
 には  $L$ )

速  $v = L$

固有の速度

波 threshold を越える = 1次元の波  
~~波~~

糸島

linear wave ; 1次元

$$\omega = \omega(k) \text{ 対 } k$$

wave packet の 1次元

振幅 or amplitude に depend 波

$$\left( \frac{\partial \psi}{\partial t} + v \frac{\partial \psi}{\partial x} + \dots \right)$$

$$\square \psi + f(\psi) = 0$$

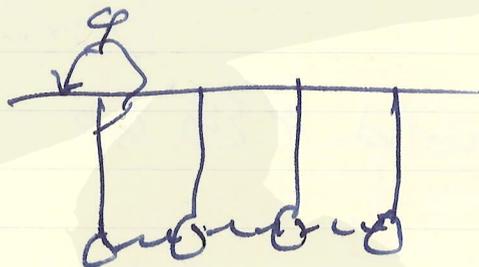
波を引く potential がある。  
 (三次元波)

$$\square \varphi + \alpha \varphi + \beta \varphi^3 = 0$$

$$\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + \int^3 \frac{\delta u}{\delta x^3} = 0$$

$$u = \lambda - \frac{1}{\psi} \frac{\delta^4}{\delta k^2}$$

$$\square \varphi + \lambda \sin \varphi = 0$$



看藤武

Operator Formalism  
of Dual Resonance Model,  
with Different Trajectories  
61729P, 1971

条件:  $\alpha_P - \alpha_{A_1} = \frac{1}{2}$

不満足  $P=0$

unitarity  $\nabla$

$\pi$ - $\rho$  phase shift  
20.0-1?

