

Ex 3/11: Field group Seminar (1) Research Institute for Fundamental Physics
 Kyoto University

Zur Quantentheorie nichtlinearer Wellengleichungen
 III. W. Heisenberg, F. Kottel und H. Mitter
 (ZS. f. Naturforsch. 10a (1955), 425)

(I. W. Heisenberg, Nachr. d. Göttinger Akad. Wiss 1953 (1953); Z. f. Naturforsch. 9a (1954) 292.)

Ausgangsgl. $\partial_\mu \frac{\partial \psi}{\partial x_\mu} + \ell^2 \psi (\psi^\dagger \psi) = 0$



propagation fun (Schwingung $\delta(x^2), \delta'(x^2)$) (Schwinger)
 \rightarrow $\hbar \omega \ll \text{mass}$, δ, δ' real
 (classical n.l. eq. approximation)
 Lehmann's objection.

\rightarrow Hilbertraum III

II

I Mg

$$\langle \Phi_0 | (\psi_a(x), \bar{\psi}_b(x)) | \Phi_0 \rangle = \frac{1}{i} S_{\alpha\beta}(x-x')$$

$$\langle \Phi_0 | [\quad] | \Phi_0 \rangle = -S_{\alpha\beta}^{(1)}(x-x')$$

$$S^{(1)}(r, t) = \frac{1}{\pi} \int_{-\infty}^{\infty} \frac{dt'}{t'} S(r, t-t')$$

$$S^{(1)}(x-x') = \frac{\pi^{-2}}{4\pi} \partial_\mu \frac{\partial}{\partial x_\mu} \text{Im} \left\{ \frac{M_1^{(1)}(x\sqrt{s})}{\pi\sqrt{s}} \right.$$

$$\left. + \frac{2i}{\pi\pi^2 s} - \frac{i}{\pi} \log \frac{\gamma\pi\sqrt{s}}{2} \right\}$$

$$- \frac{\pi^2}{4\pi} \text{Im} \left\{ \frac{M_1^{(1)}(x\sqrt{s})}{\pi\sqrt{s}} + \frac{2i}{\pi\pi^2 s} \right\}$$

$$\langle 0 | T(\psi(x)\psi(x')) | \Phi \rangle = \tau(x, x')$$

$$\tau(N+2) = \varphi(N+2) + \varphi(N) + \dots$$

