

Space-Time Description of Elementary Particles

Sept. 27, 1965

1. Comparison of various approaches to
a unified theory

a) composite model

extension of successful efforts in the past
of ~~to the future~~

of dividing matter into more and
more fundamental constituents

atoms \rightarrow electron, nucleus

\rightarrow elementary particles

\rightarrow baryons, quarks, etc.

b) group theoretical approach

higher symmetries in order to

introduction of
cover more particle in the scheme
of classification

What is lacking or what is not explicitly
considered is the relation of matter

in a) ~~to~~ space-time. What is discovered of
in a), b) trichotomy in contrast to dichotomy.

c) field theoretical approach

Weisenberg's one spinor field
(U-matter) \rightarrow indefinite metric

Three field theory (Marshall)
(chirality) ~~etc.~~

d) abandonment of field concept

S-matrix approach Chew
bootstrap

self-consistency
e) generalization of field concept
nonlocal field
particles with space-time extension

(A)

(E) is the most primitive approach
It was originated by Greek natural philosophers
like ~~to~~ Leucippus and Democritus and
followed by Newton, Dalton, Boltzmann.
In classical mechanics, it was not difficult
to give size and shape to a body.
We may imagine elastic sphere as dealt
with in detail, Boltzmann.
That such a naive approach could not
account for matter in everything was
clear even in early days.

Light was something different from
the things consisting of atoms in
the above sense.

electromagnetism
electrodynamics

ether aether pervading in space
should have been introduced.

At the present stage

- i) size and shape must be understood
in terms of internal wave function
- ii) special relativistic invariance is
to be taken into account

Since wave function is probability amplitude,
the distinction between an extended
body in q.m. sense and the
quantized field is not clear cut
but rather controversial.

A ~~theory~~ nonlinear field theory,
(Winsten) can be interpreted as a
new kind ether theory.

This is a rather controversial point.
But, they are very much different
from each other at start points
in

(3)
This situation may be compared with (only in some respect) shell model versus collective model for the nucleus.
If we go further and further, they may well come closer and closer to each other.

Also the distinction between a) composite model and, b) with our approach is not so clear as it appears, because as a result of abstraction the difference between many particle system and a rigid body, say, becomes a subtle matter.

Having all such things in mind, let us start talking about my own approach. I have been only very slowly and I know I am still very far from the goal, perhaps far behind other approaches.

2. Brief Summary of our works until about 1956.

3. Interpretation of Isospin

4. Tetrahedron model

5. ~~Remarks on~~ ^{Problem in} Interaction of interactive forces and constructive forces

6. ~~Remarks on various points not covered in my talk~~

$$\sigma_1 = \sigma_3 \sigma_2 = i \sigma_2$$

$$\sigma_2 = \sigma_3 \sigma_1 = -i \sigma_1$$

$$\sigma_3 = \sigma_3$$

$$[\sigma_1', \sigma_2'] = [\sigma_2, \sigma_1] = -i \sigma_3'$$

$$[\sigma_3', \sigma_1'] = i[\sigma_3, \sigma_2] = \sigma_1 = i \sigma_2'$$

$$[\sigma_2', \sigma_3'] = -i[\sigma_1, \sigma_3] = -\sigma_2 = i \sigma_1'$$

$$\psi^* U \sigma_3 \cdot \sigma_3 U \psi = \frac{1}{2} (\cos \theta - i \sin \theta) (\cos \theta + i \sin \theta) \psi^* \sigma_3 \psi$$

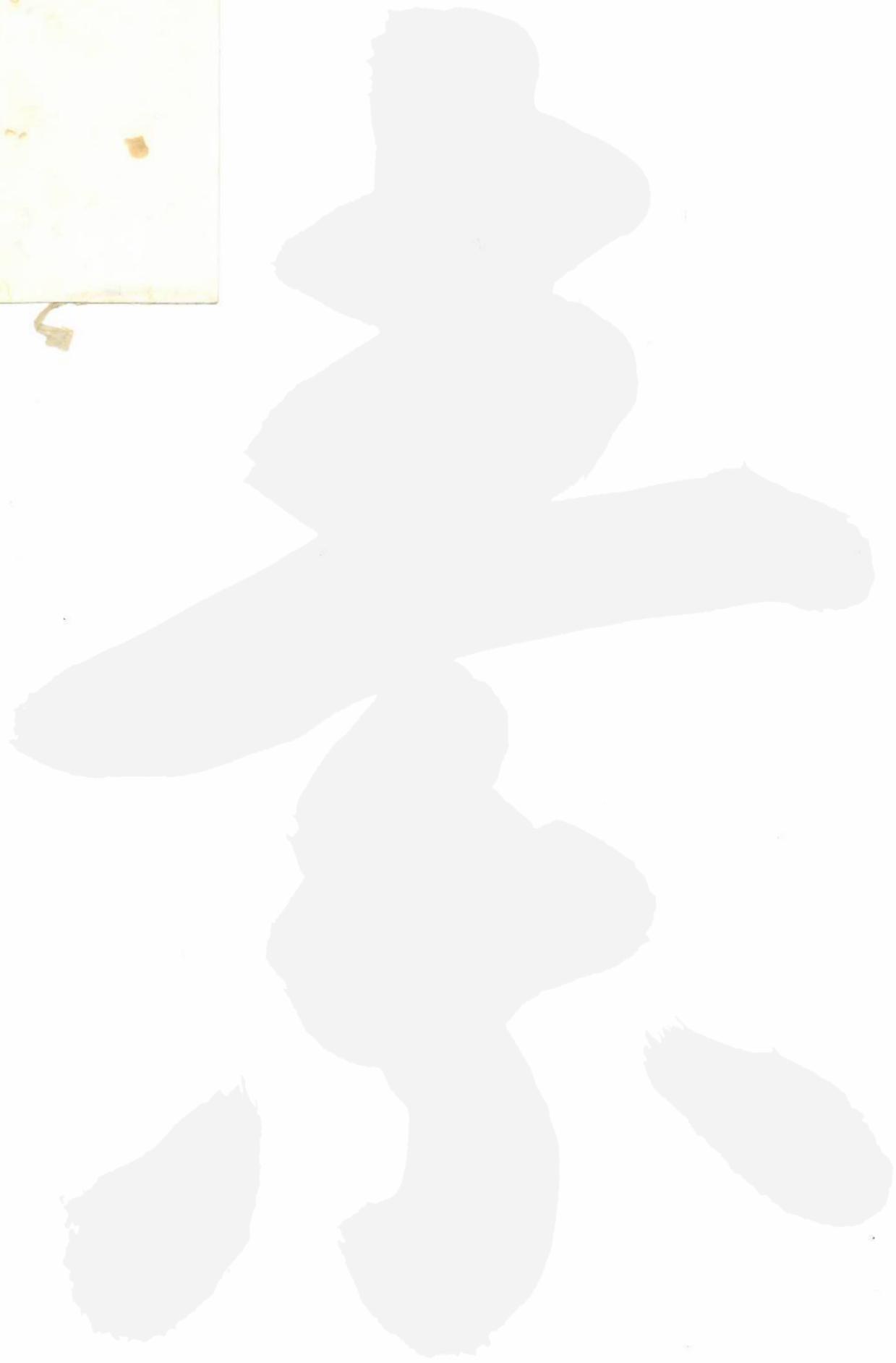
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$$U^*U = \begin{pmatrix} \cosh \frac{\theta}{2} & -\sigma_2 \\ \sigma_2 & -\sinh \frac{\theta}{2} \end{pmatrix}$$

$$= \left(\cosh^2 \frac{\theta}{2} + \sinh^2 \frac{\theta}{2} \right) - 2\sigma_2 \cosh \frac{\theta}{2} \sinh \frac{\theta}{2}$$

$$= \cosh \theta - \sigma_2 \sinh \theta$$

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$$U = \exp[i\sigma_1 \theta]$$

$$= \exp[-\sigma_2 \theta]$$

$$= \cosh \theta/2$$

$$- \sigma_2 \sinh \theta/2$$

$$U^* = \cosh \theta/2$$

$$- \sigma_2 \sinh \theta/2$$

$$U^* \sigma_3 U = \sigma_3 \left(\cosh \frac{\theta}{2} + \sigma_2 \sinh \frac{\theta}{2} \right) \times \left(\cosh \frac{\theta}{2} - \sigma_2 \sinh \frac{\theta}{2} \right)$$

$$\stackrel{= \sigma_3}{\Psi^* U^* \sigma_3 U \Psi} = \Psi^* \sigma_3 \Psi$$

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