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Letter to the Editor
On the Nuclear Transformation
with the Absorption of the Orbital Electron

According to the present theory of β -disintegration, the nucleus of atomic number Z transforms into its isobar $Z-1$ ~~of atomic number~~ with the emission of a positron and a neutrino, if the difference ΔW of proper energies of these ~~isobars~~ isobar is larger than $m_0c^2 + \mu_0c^2$, where m_0 and μ_0 are the masses of the electron and the neutrino respectively. On the contrary, the isobar $Z-1$ transforms into Z with the emission of an electron and an anti-neutrino, if ΔW is smaller than $-m_0c^2 - \mu_0c^2$. Further, if ΔW is larger than $\mu_0c^2 - E$, where E is the total energy of an orbital electron of the isobar Z , the latter this isobar can ~~transform into~~ $Z-1$ with the absorption of the electron, ~~as most charge units at the same time~~ ~~thus~~, two isobars with consecutive atomic numbers are both stable, only if ΔW lies between $-\mu_0c^2 - \mu_0c^2$ and $\mu_0c^2 + \mu_0c^2$. This condition can be fulfilled only very rarely, if the neutrino mass is small compared with the electron mass. Since the existence of several pairs of such stable isobars was confirmed by the experiment ~~it is~~ recently, it will be permitted to give a brief account of the results of our calculation if the mean life time of the isobar Z due to the our previous ~~papers~~ ^{calculations} on this subject.²⁾ Moreover, in case when ΔW is larger than $m_0c^2 + \mu_0c^2$, the isobar Z can transform into $Z-1$ with the ~~an~~ electron absorption as well as the positron emission, so that the determination of the relative importance of these processes in various cases will be of some importance.

$$8) \frac{1.7}{57} \frac{1370}{57}$$

where α is the fine structure constant.

First, the mean life time T of the nucleus Z due to the absorption of K -electrons with $E = mc^2 \sqrt{1-\alpha^2 Z^2}$ without the change of the nuclear spin, ~~the~~ ^{the} values and columns of Table 1 show their ~~numerical~~ ^{numerical} for several values of Z , corresponding to the interaction of Fermi and Konopinski-Uhlenbeck types respectively. The relations were being assumed to be $\tau \propto Z^{-2}$.

Z	αZ	Table 1 T (Fermi)	T (K.U.)
1	$1/137$	$2740 \left(\frac{\Delta W}{mc^2} + 1\right)^{-2}$ years	
2	$2/137$	$170 \left(\frac{\Delta W}{mc^2} + 1\right)^{-2}$ years	
14	0.1	$200 \left(\frac{\Delta W}{mc^2} + 1\right)^{-2}$ days	
27	0.2	$25 \left(\frac{\Delta W}{mc^2} + 1\right)^{-2}$ days	
69	0.5	$14 \left(\frac{\Delta W}{mc^2} + 0.87\right)^{-2}$ hours	

If we assume the mean life time ^{is assumed} relative mass to be zero, the mean life time is approximately proportional to

$$\tau \propto \frac{(\alpha Z)^{2\delta+1}}{(\Delta W + \delta)^2} \quad \text{or} \quad \frac{(\alpha Z)^{2\delta+1}}{(\Delta W + \delta)^4}$$

according as the ~~int~~ ^{scheme} coupling of Fermi or Konopinski-Uhlenbeck ~~type~~ is adopted, where

$$\Delta W = \frac{\Delta W}{mc^2} \quad \delta = \sqrt{1-\alpha^2 Z^2}$$

The apparent discrepancy between these results and the existence of stable pairs of heavy nuclei can be removed only if ^{we assume} the following ~~assumptions~~ ^{assumptions} are made:
 i) the ~~large~~ ^{small} difference of nuclear spins for each pair of stable isobars, ^{to be large}

The disintegration positron emission and the K-electron absorption was calculated for several values of Z and ΔW in the case of allowed transition, the results being summarized in the following Table 2.

For ordinary radio-elements of the positron emitters, which emits ΔW is small and ΔW is larger than $2mc^2$, the ratio σ is large that the disintegration by the absorption of the orbital electrons does not affect seriously the mean life time. On the contrary, for large values of Z , such a process become much more frequent than the positron emission, as long as ΔW is not too large compared with mc^2 .

The extreme $Z=1$ corresponding to the transformation of the hydrogen atom into the neutron ^{corresponding to the extreme case} is practically little ^{except for the case of the difference of the masses of the neutron and the proton that the neutron mass is larger than the sum of the masses of the electron and the proton according to the recent experimental results.} On the contrary, the case $Z=2$ has some practical importance indicating the spontaneous transformation of He^2 into H^3 by absorbing one of the K-electrons. ^{the mean life time becomes shorter as the atomic number increases and the existence of the He^2 can be reconciled with this result only if}

