

E 23 050 P 08

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Efficiency of ~~Al~~ Pb Counter

DATE
 NO.

~~10.8.18~~ ~~Ca~~ ~~23.10.18~~

i) Photoelectric Effect.

$\gamma = 1$

$\tau = 10^{15} \times 0.23 = 31.62 \times 10^{12}$

$$\begin{array}{r} 3162 \\ \times 0.23 \\ \hline 10486 \\ 6324 \\ \hline 73726 \end{array}$$

$$\begin{array}{r} 316 \\ \times 179 \\ \hline 2814 \\ 2212 \\ \hline 56534 \end{array}$$

$82) 56534 (677$

$\tau_k = 10^{15} \cdot \frac{NZ\phi_0}{Z_1} = 31.62 \times \frac{1.79}{82}$

$= 0.677$

$$\begin{array}{r} 0.846 \\ 8) 0.677 \\ \hline 0.64 \\ \hline 37 \end{array}$$

$\tau_p = \frac{5}{4} \tau_k = 0.85$

$R_p = 3.7 \times 10^{-2} \text{ cm in Pb}$

$(\frac{0.165}{2.17} \text{ cm} = 0.6 \text{ mm. in Al})$

$\tau_p R_p = 0.2\% \approx 3.14\%$

$\tau_p R_p = 0.210$ ($\tau_{\text{total}} = 0.80$)

$R_p =$

$$\begin{array}{r} 0.85 \\ \times 3.7 \\ \hline 3145 \end{array}$$

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Range of Fast Electrons in Lead

$$-\left(\frac{dE}{dx}\right)_{\text{coll}} = N Z \phi_0 \cdot \frac{3}{4} \mu \frac{1}{\beta^2} \left[\log \frac{\mu \beta^2 \cdot 2 m \rho^2}{(1-\beta^2) I^2 Z^2} + \left[\log \frac{(E-m) E^2 \rho^2}{2 \mu I^2 Z^2} + \left(\frac{m}{E}\right)^2 \right] \right]$$

$$\beta = \frac{v}{c} \quad E = \frac{m}{\sqrt{1-\beta^2}} \quad \beta = \sqrt{1 - \left(\frac{m}{E}\right)^2}$$

$$-\left(\frac{dE}{dx}\right)_{\text{coll}} = N Z \phi_0 \cdot \frac{3 M E^2}{4 (\epsilon^2 - 1)} \left[\log \frac{(\epsilon - 1) \epsilon^2 (\epsilon^2 - 1) m^2}{2 I^2 Z^2} + \frac{1}{\epsilon^2} \right]$$

$$= N Z \phi_0 \cdot \frac{3 M E^2}{4 (\epsilon^2 - 1)} \left[\log (\epsilon - 1) (\epsilon^2 - 1) + \log \frac{m^2}{2 I^2 Z^2} + \frac{1}{\epsilon^2} \right]$$

$I = 13.5$
 $\mu = 5.1 \times 10^4$
 $Z = 82$
 2
 2^{-1}

$\log 7018$
 18.42072
 2.8636
 9.1866
 -0.69315
 1.30685
 12.74795

$$\log \frac{m^2}{2 I^2 Z^2} = 12.74795$$

4.4067
 3.9318
 7.8636
 -8.8134
 9.1866

2.30259
 8
 18.42072
 1.32176
 0.69315
 2.01491
 4.02982
 5.97018



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$$-\left(\frac{dE}{dx}\right)_{coll} = 1.79 \times \frac{3M\epsilon^2}{4(\epsilon^2-1)} \left[\log(\epsilon-1)(\epsilon^2-1) + 12.748 + \frac{1}{\epsilon^2} \right]$$

$$-\left(\frac{dE}{dx}\right)_{rad} = N \frac{Z_0^2}{(137)^2} \cdot \mu\epsilon \frac{\Phi_{rad}}{\Phi} = 12.74 \cdot \mu\epsilon \frac{\Phi_{rad}}{\Phi}$$

$$range = \int_0^E \frac{dE}{-\left(\frac{dE}{dx}\right)_{coll} - \left(\frac{dE}{dx}\right)_{rad}} = \int_0^E \frac{d\epsilon}{\left(\frac{d\epsilon}{dx}\right)_{coll} - \left(\frac{d\epsilon}{dx}\right)_{rad}}$$

ϵ	0.01	0.1	1	10	100	1000	10000
$-\left(\frac{d\epsilon}{dx}\right)_{coll}$	0.00385	0.0154	0.0435	0.0244	0.00488	0.000513	0.0000513

$$\pi \int_0^{\infty} \omega \times \sin \omega dx$$

$$\approx \frac{1}{2} \sin \frac{\pi}{2}$$

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288
 12
 48
 24
 288
 15
 1440
 288
 4320

-0.

$\gamma = 10$;

$\tau_M = 0.24 \text{ cm}^{-1}$ $\tau_{mean} = 4 \uparrow 1$ $R_M = 0.18 \text{ cm}$

$\text{eff}_M = 2 \times \tau_M \times R_M = 0.864$ $\approx 14\%$

$\tau_P = 1.2 \times N \times \frac{1}{2}$ $R_P = 0.3 \text{ cm}$ 4.35%

$\tau = \frac{1.19}{0.6} = 1.98 \text{ cm}^{-1}$ $\approx 0.0576 = 5.8\%$

$\tau_C = 1.2 \times 1.19 = 1.428 \text{ cm}^{-1}$ $R_C = 0.3 \text{ cm}$ 4.35%

41) $\frac{1.19}{0.6} = 1.98$ $\text{eff}_P = 0.026 \times 0.3 = 0.0078 = 0.78\%$

$\frac{1.19}{3.58} = 0.332$ $\tau_C = 0.12 \times 1.19 = 0.1428 \text{ cm}^{-1}$

$\frac{1.19}{0.2148} = 5.54$ $R_C = 0.3 \text{ cm}$

$\tau \cdot \text{eff}_C = \beta \times 0.21 \times 0.3 = \beta \times 0.063$

$\beta = \frac{0.4}{0.063} = 6.35$ $\approx 0.0489\% = 4.89\%$

$\text{eff}_{total} = 10\% + 11\% \sim 21\%$ $\approx 0.0489\% = 4.89\%$

$\gamma = 2$;

$\tau_P = 0.20 \text{ cm}^{-1}$ $R_P = 0.046 \text{ cm}$

$\tau_P R_P = 0.012 = 1.2\%$

$\tau_{RC} = 0.31 \times 1.19 = 0.3689 \text{ cm}^{-1}$

$R_{RC} = 1.6 + 1$

$\tau_{RC} R_{RC} = 1.1 + 1 \rightarrow R_{RC} = 0.04$

$\tau_C R_C = 0.55 \times 0.04 = 0.022 = 2.2\%$

$\text{eff}_{total} = 1.2 + 2.2 = 3.4\%$

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$\gamma = 5:$ $\tau_M = 0.08 \text{ cm}^{-1}$ $\epsilon_{\text{mean}} = 1.5 + 1.$ $R_M = 0.045$
 $\text{eff}_M = \beta \times \tau_M R_M = \beta \times 0.0036$
 $\beta = 4.5 = 0.09054 = 0.554\%$

$\tau_P = 0.055 \text{ cm}^{-1}$ $\epsilon = 5 + 1.$ $R_P = 0.14 \text{ cm}$
 $\tau_P R_P = 0.00775 = 0.18\%$

$\tau_C = 0.35$ $\epsilon_{\text{max}} \leq 5 + 1.$ $R_C = 0.16$
 $\epsilon_{\text{mean}} \approx 4 + 1$ $R_C = 0.12 \text{ cm}$

$\tau_C R_C = 0.042 = 4.2\%$
 $\text{eff}_{\text{total}} = 5.4\% = \textcircled{5\%}$

$\frac{35}{12} = 2.916$
 $\frac{25}{420} = 0.0595$

$\gamma = 20:$ $\tau_M = 0.5 \text{ cm}^{-1}$ $\epsilon_{\text{mean}} \rightarrow 1 + 9$
 $R_M \approx 0.3 \text{ cm}$

$\tau_M R_M = 0.15$ $\text{eff}_M = 15\%$
 $\tau_C = 0.15 \text{ cm}^{-1}$ $\epsilon_{\text{mean}} \approx 1920$
 $R_M \approx 0.5 \text{ cm}$ $\epsilon_{\text{max}} \approx 1920$

$\tau_M R_M = 0.045$ $\text{eff}_C = 4.5\%$
 $\epsilon_{\text{max}} = 1920$

$\text{eff}_{\text{total}} \approx 20\%$

$\tau_P = 0.54$ 0.54
 $\frac{0.019}{486} = 0.0012$ $\text{eff}_{\text{total}} \approx 20\%$
 $\frac{108}{54} = 2$
 $\frac{0.01026}{0.00648} = 0.3$

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$\gamma = 200$ (10⁸ eV)
 $\tau = 1.16 \text{ cm}^{-1}$ $R_{\text{eff}} = 0.3$
eff $\approx 35\%$